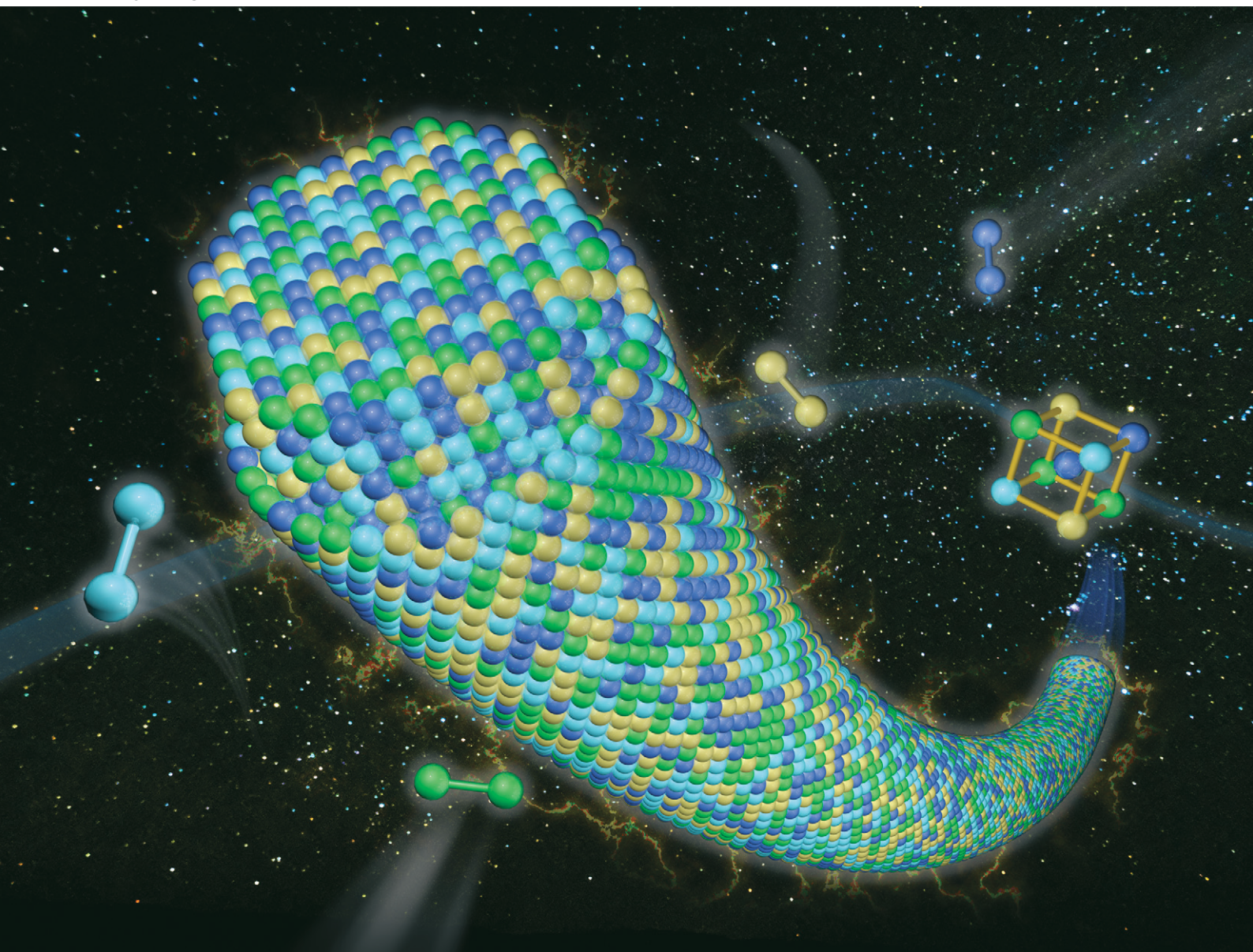


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Deformation behavior and yield strength prediction of [112] oriented NbMoTaW refractory high entropy alloy nanowires†

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Refractory high entropy alloys (RHEAs) have garnered widespread attention due to their potential applications at extremely high temperatures. However, accurately predicting the mechanical properties of these materials is challenging due to the complex slip systems in body-centered cubic (BCC) metals. In this work, the tensile behaviors of NbMoTaW RHEA single crystalline nanowires with various radii under tensile deformation were investigated using molecular dynamics simulations, focusing on their deformation behavior, mechanical response, and size-dependent effects. The results revealed a transition in yield stress from the Hall–Petch relation to the inverse Hall–Petch relation with the decrease of the nanowire radius. The primary deformation mechanism observed was the nucleation and glide of dislocation from the surface. A thermal activation-based theoretical model was developed for determining the yield stress, incorporating stacking fault energy and surface energy as pivotal parameters. This model could effectively predict the yield stress of the RHEA in the inverse Hall–Petch stage and exhibit significant potential in predicting the mechanical properties of other BCC metals.

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1. Introduction

BCC refractory high entropy alloys (RHEAs), such as NbMoTaW and NbMoTaWV,¹ have attracted considerable attention due to their exceptional properties, including high strength, thermal stability, and resistance to high temperatures and oxidation.^{2–5} These properties make them promising candidates for applications in aerospace, biomedicine, and the development of radiation-resistant materials. Extensive research has demonstrated the importance of microstructure and characteristic dimensions of nanomaterials in determining their mechanical properties, particularly strength and toughness. Consequently, there is considerable interest in the design and optimization of these mechanical properties by tailoring their microstructure and size in the fields of materials science and engineering.^{6–8}

Nanowires (NWs), as a kind of one-dimensional material with diameters typically below 100 nm, exhibit remarkable

mechanical, electromagnetic, and optical performance, making them highly versatile for applications in wearable devices,^{9,10} nanogenerators,¹¹ water purification,¹² biosensors^{13,14} and other fields. The small size of nanowires makes their mechanical properties particularly sensitive to their radius, leading to the size effects similar to those observed in polycrystalline materials. While the Hall–Petch (HP) relation^{15,16} generally shows a ‘smaller is stronger’ correlation between grain size and yield strength in most metals,¹⁵ this trend may shift to the inverse Hall–Petch (IHP) relation when the grain size is reduced to a few nanometers,^{17,18} characterized by “the smaller, the weaker”.^{19,20} This shift can be attributed to a change in the deformation mechanism from dislocation-dominated activity to grain boundary (GB)-dominated behavior, such as GB sliding or migration^{21–24} and grain rotation.^{25,26} For single-crystalline materials like nanowires, numerous studies have shown the strong size-dependence of their mechanical properties,^{27–29} like HP. However, as the sample size is further decreased, the HP relation may transition to the IHP relation; analogous to the role of GBs in polycrystalline materials, the surface effect^{30–32} may become a crucial factor affecting the mechanical properties of NWs due to the sharp increase in surface content.

Although extensive research has been conducted on FCC metals, investigations on BCC metals are still in the nascent stages, primarily due to the complexity and uncertainty of their deformation behaviors. Unlike the stable slip system in FCC metals, the deformation behavior of BCC metals is

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highly dependent on the loading direction,^{33–35} and exhibits remarkable tension-compression asymmetry.^{36–38} Slip in BCC metals can occur on multiple slip planes (such as {110}, {112}, {123}), even with a consistent slip direction along the $\langle 111 \rangle$ direction, leading to a competition between dislocation glide and twinning.^{39,40} While some studies have elucidated the deformation behavior and predominant mechanisms of BCC nanowires under loading along specific orientations,^{34,41} a unified theory that can comprehensively describe this phenomenon is still lacking. Consequently, predicting the mechanical properties of BCC metals remains a significant challenge.

Conventional models for predicting mechanical properties usually rely on empirical formulas, which may encounter challenges when applied to materials with smaller dimensions. To address these challenges, various alternative models have been proposed from diverse viewpoints, aiming to offer more effective descriptions and predictions of mechanical properties. For instance, one innovative approach differs from the traditional crystal plasticity by assigning a slip system to each Burgers vector, which facilitates the replication of the results obtained by molecular dynamics (MD) simulations and provides valuable insights into the plasticity of single crystals.⁴² Zhao *et al.* proposed a model that addresses the size-dependent fracture mechanisms of nanowires by identifying critical aspect ratios that describe the relation between the fracture strain and aspect ratio.²⁷ Additionally, machine learning techniques have been utilized to determine the influencing factors of fitting parameters (σ_0 and k) in the HP relation, enabling the development of new relations based on key parameters without relying on constant experimental data fitting.⁴³ In material-property-based models for nanopolycrystalline metals, the GBs are treated as distinct phases from the grain interior, allowing for the assessment of the maximum strength based on the activation energy required for the transition between crystalline and amorphous phases.⁴⁴ Notably, the amorphous model⁴⁴ not only effectively predicted the mechanical properties of BCC Ta at the IHP stage but also showed great potential for predicting mechanical properties of other materials.^{45,46}

In this work, the mechanical responses of the NbMoTaW nanowires with different radii under tension are studied using MD simulations, to explore the deformation mechanisms and the key factors affecting the mechanical properties of these nanowires at the IHP stage. Additionally, a theoretical model is developed for predicting the yield stress. In section 2, the establishment of nanowire samples and MD simulation details are introduced. In section 3, the mechanical responses and deformation mechanism of the NbMoTaW nanowires with different radii under tension are presented and discussed. In section 4, a theoretical model incorporating thermal activation is developed, which is used to describe the yield stress of nanowires and is extended to predict the mechanical properties of other BCC metals. Finally, conclusions are drawn in section 5.

2. Simulation details

In this work, the spectral neighbor analysis potential (SNAP) parameters identified by Li *et al.*⁴⁷ are utilized to describe the interatomic interaction in NbMoTaW RHEAs. The single-crystalline nanowires with orientations of $x//[111]$, $y//[\bar{1}10]$, and $z//[112]$ are built using the software ATOMSK.⁴⁸ These nanowires have radii R ranging from 2 nm to 15 nm and a fixed height of 8 nm, with an atomic composition of Nb:Mo:Ta:W set as 1:1:1:1 (equal atomic ratio), as shown in Fig. 1.

All MD simulations are conducted using LAMMPS.⁴⁹ Periodic boundary conditions are applied in the x , y , and z directions, with a vacuum layer in the radial direction to mimic the surface of nanowires. Prior to the mechanical test, the samples undergo a 30 ps relaxation at 10 K under NPT ensemble, maintaining zero pressure in all directions to achieve a stable system. Subsequently, the nanowires are uniaxially stretched at a strain rate of $1 \times 10^9 \text{ s}^{-1}$ in the z direction at 10 K using NVT ensemble, with the maximum strain of 0.2. The timestep is set to 1 fs. Since the calculated tensile stress corresponds to the stress of the simulation box along the z axis, it is necessary to convert it to the tensile stress of the nanowire due to the introduction of a vacuum layer in the radial direction. This is done using the relation $\sigma_{\text{NW}} = \sigma_{\text{Box}} \times S_{\text{Box}}/S_{\text{NW}}$, where σ_{NW} is the tensile stress of the nanowire, σ_{Box} is the z -axis tensile stress of the box, S_{Box} is the cross-sectional area of the simulation box in the z direction, and $S_{\text{NW}} = \pi R^2$ is the cross-section area of the nanowire, with R as the nanowire radius.

To account for latent effects of atomic distribution in the RHEAs, three sets of samples (labeled as sample groups A, B, and C) with different random seeds are built to enhance the statistical robustness and reliability of our results. All the simulations are performed under identical loading conditions. Microstructure analysis and visualization are carried out using OVITO,⁵⁰ where blue balls represent the internal atoms in the BCC lattice, white balls denote surface atoms or defects, and green and pink lines indicate the $\langle 111 \rangle$ and $\langle 110 \rangle$ type dislocations.

3. Results and discussion

Fig. 2(a)–(c) show the stress–strain (σ – ε) curves of sample groups A, B, and C, respectively. These curves exhibit similar trends, initially showing nearly linear growth until reaching the yield stress, with slight variations in slope. At a strain of approximately 0.13 ($\varepsilon \approx 0.13$), all the samples begin to yield, characterized by a rapid drop in stress from the peak (yield stress), followed by a plastic flow stage where stress fluctuates within a certain range as strain increases. Fig. 2(d) shows the variation of yield stress with the radius R , revealing a trend analogous to the HP and IHP relations, with a critical transition radius around 6 nm. In the range of $R > 6$ nm, the yield stress increases with the decrease of R , consistent with the HP stage and showing a “the smaller, the stronger” trend.

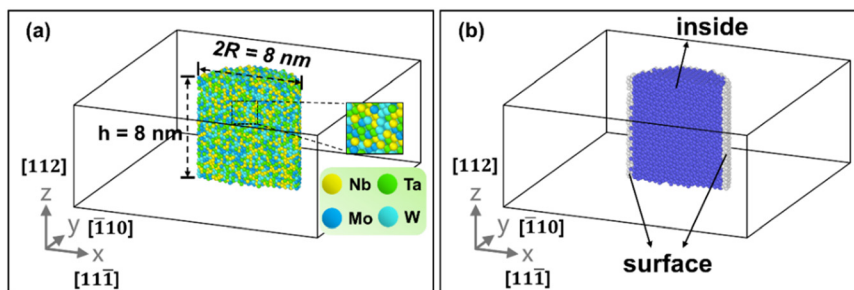


Fig. 1 Atomic configuration and cross-section of the NbMoTaW RHEA nanowire with a radius (R) of 4 nm and the loading direction of [112]. (a) Cross-section with atoms colored by the element type. (b) Cross-section with atoms colored by the local structure, with blue and white balls denoting inner and surface layer atoms, respectively.

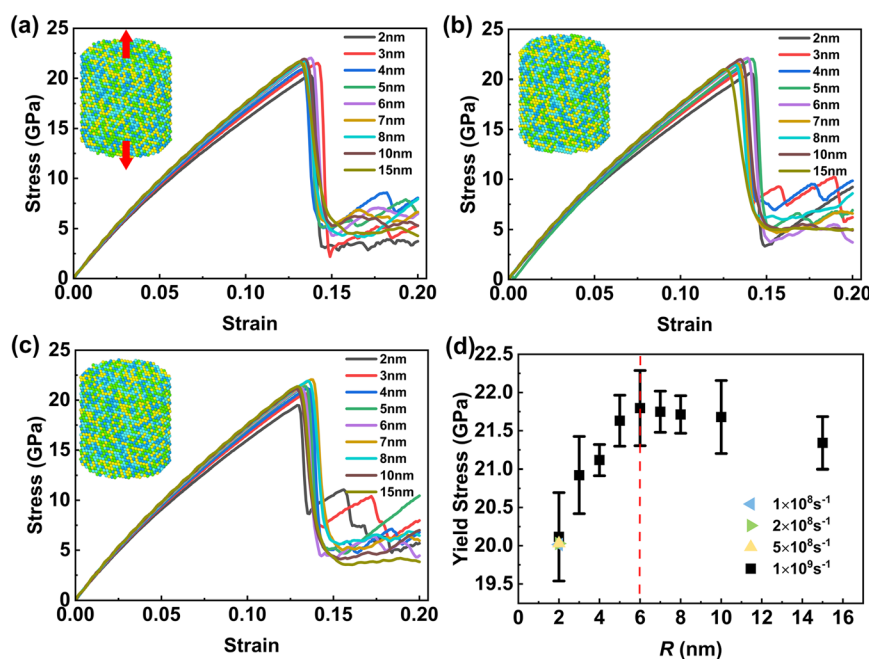


Fig. 2 (a)–(c) Stress–strain curves of sample groups A, B, and C with different R . (d) Variation of yield stress with R , revealing a transition from the HP relation to the IHP relation at $R = 6$ nm. Simulations on sample group A with $R = 2$ nm at different strain rates confirm that the deviation of the yield stress obtained with different strain rates remains within the error range.

Conversely, for $R < 6$ nm, the yield stress decreases with the decrease of R , aligning with the IHP stage and reflecting a trend of “the smaller, the weaker”. Notably, the stress change in the IHP stage is within 2 GPa, which differs from the IHP stages observed in Mo (ref. 35) and Fe (ref. 51) nanowires, where stress changes exceed 3 GPa. This discrepancy can be attributed to that the radius R we used corresponds to the minimum sample diameter of $d = 4$ nm, which is larger than the diameter of $d = 1$ nm for BCC Mo (ref. 35) and $d = 1.42$ nm for BCC Fe.⁵¹ Additionally, it can be seen that the yield stress would not saturate with the increase of radius but transitions into the HP stage. A similar transition has also been observed in $\langle 111 \rangle$ oriented Mo nanowires,³⁵ supporting our results.

In order to assess the effect of the strain rate, additional simulations on sample group A with $R = 2$ nm are conducted at

various strain rates. The results [Fig. 2(d)] show that the yield stress at a strain rate of $1 \times 10^9 \text{ s}^{-1}$ differs only slightly from those at lower strain rates ($1 \times 10^8 \text{ s}^{-1}$ to $5 \times 10^8 \text{ s}^{-1}$), with all values falling within the error range, which confirms that the strain rate of $1 \times 10^9 \text{ s}^{-1}$ is reasonable for this study. Furthermore, although the SNAP potential used in this work is highly accurate, it has relatively low computational efficiency. Therefore, we selected $1 \times 10^9 \text{ s}^{-1}$ as the strain rate to balance the requirement of accuracy and computational efficiency.

Fig. 3(a) shows the σ – ϵ curve of the nanowire with $R = 4$ nm, where yield occurs at $\epsilon \approx 0.13$. To analyze the microstructure evolution and dominant deformation mechanism, the microstructures corresponding to the feature points (points b to f) in the σ – ϵ curve are presented in Fig. 3(b)–(f), respectively. At $\epsilon = 0.135$, a dislocation nucleates from the surface, where the local energy is relatively high [Fig. 3(b)]. As ϵ increases to 0.137,

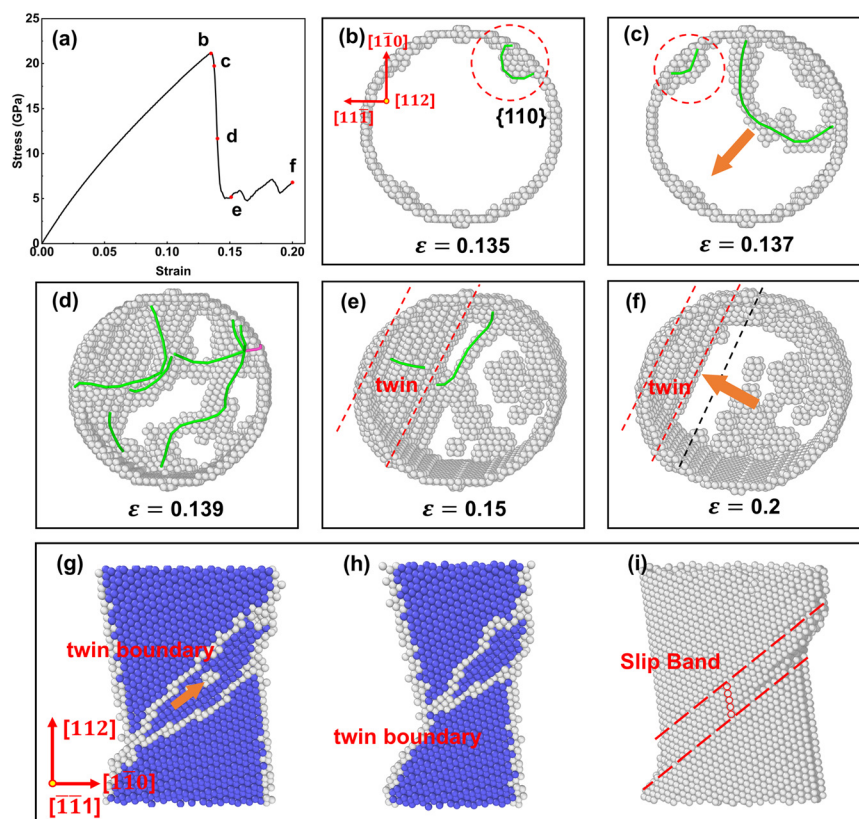


Fig. 3 (a) Stress-strain curve of a nanowire sample with $R = 4$ nm, with points b–f as feature points. (b)–(f) Top views of microstructures of the nanowire sample at points b–f in (a), illustrating the dislocation nucleation process. Atoms in the perfect BCC lattice have been removed for clarity, with white atoms indicating the surface or defect sites, green lines representing $\langle 111 \rangle$ dislocations, and pink lines representing $\langle 110 \rangle$ dislocations. (g) and (h) Slices of nanowires revealing twin boundaries at $\varepsilon = 0.15$ and $\varepsilon = 0.2$, respectively. (i) Formation of the slip band observed at $\varepsilon = 0.2$.

the dislocation grows and glides along the slip plane [Fig. 3(c)]. Simultaneously, a second dislocation nucleates from the surface on the other side [Fig. 3(c)], leading to the interconnection and intertwining of multiple dislocations within the nanowires as ε reaches 0.139 [Fig. 3(d)]. At this stage, twin nucleation begins, accompanied by a significant drop in stress [from points b to d in Fig. 3(a)]. As ε further increases to 0.15, the dislocation count decreases, and the stress falls to the bottom of the valley [point e in Fig. 3(a)]; the twin becomes more distinct [Fig. 3(e)]. At $\varepsilon = 0.20$, dislocations nearly disappear, the edges of twin boundaries (TBs) gradually migrate towards the surface, and numerous scattered defects appear within the nanowires [Fig. 3(f)]. Slicing the nanowires and observing the TBs along the $\langle 111 \rangle$ direction reveals that the TBs noticeably shorten from $\varepsilon = 0.15$ to $\varepsilon = 0.2$, with their positions migrating from the center towards the periphery of the nanowires [Fig. 3(g) and (h)]. Substantial deformation is observed, with the $\{110\}$ plane identified as the slip plane, forming a slip band comprising five atomic layers [Fig. 3(i)]. This deformation mode aligns well with the experimental result of W nanowires subjected to tension in the same direction.⁵²

The Young's modulus E is defined as the slope of the stress-strain (σ – ε) curve prior to dislocation nucleation. In our work, the Young's moduli of the nanowires with different radii are calculated with the σ – ε curves in the strain range

from 0 to 0.05. It can be seen in Fig. 4 that E decreases gradually with the decrease of the nanowire radius. The E of the nanowires with different radii can be described using the rule of mixture (ROM):⁵³

$$E = f_0 E_0 + f_1 E_1 \quad (1)$$

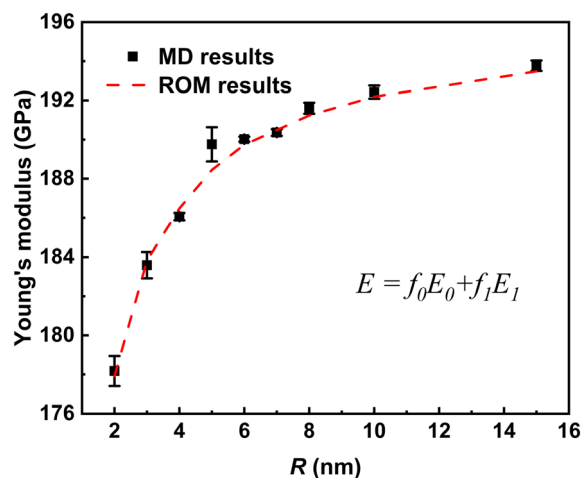


Fig. 4 Comparison of Young's moduli (E) of nanowires with varying R from eqn (1) and MD results.

where E_0 and E_1 are the Young's moduli of the surface and inner core of the nanowire, respectively, and f_0 and f_1 are the volume fractions of the surface and inner core, respectively. It can be solved from eqn (1) using the MD results of nanowires with $R = 2$ nm and $R = 15$ nm that $E_0 = 128$ GPa and $E_1 = 196$ GPa, where E_1 is close to the Young's modulus of $E_{\text{block}} = 210$ GPa obtained using a block model. The E of the nanowires at different radii obtained using eqn (1) is shown in Fig. 4, which is a good description of the change of E with R .

The microstructure evolutions of the nanowires with other R under tension are also analyzed. Due to the absence of internal defects, the surface atoms of the nanowires have higher energy compared with the internal atoms, leading to dislocation nucleation initiating from the surface. Throughout the simulation, twin nucleation consistently follows the nucleation of dislocations, indicating that the deformation mechanism is mainly dislocation-dominated. This is because twinning typically involves the $\{112\}\langle 111 \rangle$ slip system, while in BCC metals, slip systems are temperature-dependent, and at low temperatures, the $\{110\}$ plane is often preferred.⁵⁴ In this work, tension tests on nanowires are conducted at a low temperature of 10 K, favoring the $\{110\}\langle 111 \rangle$ slip system, thus facilitating the generation of dislocations. Slip occurs when the resolved shear stress on a slip system exceeds a critical value. The Schmid factor can describe the relation between the applied tensile stress and the resolved shear stress, and the Schmid factor for the two slip systems can be calculated: the $\{110\}\langle 111 \rangle$ slip system corresponding to dislocation nucleation has a Schmid factor of $\mu_1 = 0.41$, and the $\{112\}\langle 111 \rangle$ slip system corresponding to twinning has a Schmid factor of $\mu_2 = 0.39$.⁵⁵ Since $\mu_1 > \mu_2$, dislocation nucleation should be the dominant deformation mechanism. As R increases, the number of dislocations nucleating from the surface increases, along with the capacity to store dislocations. The number of dislocations increases rapidly after yield, and subsequently decreases with the increase of strain. As $\varepsilon = 0.2$, dislocations in the nanowire samples with smaller radii tend to annihilate, while some dislocations may persist in the samples with larger radii.

4. Model construction and validation

As discussed in section 3, the primary deformation mechanism for the yield of the NbMoTaW nanowires is the nucleation of dislocation from the surface, followed by dislocation slip and the formation of the slip band as strain increases. The grain size effect, characterized by the fact that the smaller the grain size, the higher the grain boundary fraction, would significantly affect the mechanical properties of polycrystalline materials. Similarly, in nanowires, a reduction in the sample radius would also result in a higher proportion of the surface area. The surface, which would increase the energy of a system due to the introduction of additional surface energy, would lower the energy barrier for dislocation nucleation, accounting for the observed IHP-like

relation. Therefore, the surface proportion should be considered as a crucial factor in evaluating the influence of the surface on the mechanical properties of nanowires.

The local microstructure of the samples is examined using DXA⁵⁶ in OVITO, revealing that the surface proportion of the nanowires increases from approximately 5% at $R = 15$ nm to around 25% at $R = 2$ nm. To determine the surface proportion, the outermost atoms of the nanowires are defined as the surface layer atoms, with a layer of atoms perpendicular to the axis being intercepted. The interatomic distance ranges from $0.707a$ to $0.866a$ (a is the lattice constant), and a thickness of $0.866a$ is selected for the outermost surface layer thickness. This method enables the calculation of the surface proportion of nanowires in the cross-section for different radii and lattice constants (more details are available in section S1 in the ESI†). The results obtained are consistent with those by DXA in OVITO, supporting the selection methodologies outlined in the relevant literature.⁵⁷

Chandross *et al.*⁴⁴ proposed a theoretical model to predict the strength of materials through thermal activation theory, which is based on the energy barrier associated with the transition between crystalline and amorphous phases. The model can be expressed as:

$$\dot{\varepsilon}_{\text{GBS}} = \dot{\varepsilon}_{\text{tot}} \exp\left(-\frac{\Delta G - \tau V^*}{kT}\right) \quad (2)$$

where $\dot{\varepsilon}_{\text{GBS}}$ is the strain rate related to GB sliding, which can be viewed as the strain rate related to GB behavior here; $\dot{\varepsilon}_{\text{tot}}$ is the total (applied) strain rate; ΔG is the activation energy; τ is the shear stress; V^* is the activation volume; k is the Boltzmann constant and T is the temperature. By applying the Taylor expansion to eqn (2), one obtains:

$$\tau = \frac{\Delta G}{V^*} + \left(\frac{\dot{\varepsilon}_{\text{GBS}}}{\dot{\varepsilon}_{\text{tot}}} - 1\right) \frac{kT}{V^*} \quad (3)$$

In MD simulations, it is usually assumed that the two strain rates ($\dot{\varepsilon}_{\text{GBS}}$ and $\dot{\varepsilon}_{\text{tot}}$) are approximately equal,⁴⁴ and thus, eqn (3) can be simplified to:

$$\tau = \frac{\Delta G}{V^*} \quad (4)$$

To predict the strength of nanotwinned metals, Xiao *et al.*⁴⁵ considered their yield as the result of combined contributions of grain boundary melting and phase transition, and introduced an innovative energy activation model to quantify the energy required for phase transitions. Drawing inspiration from their work, in this work, we also treat the nucleation of dislocation and the formation of a stacking fault from the surface of nanowires as a phase transition. During the yield of the nanowires, dislocation activation and glide lead to the formation of a stacking fault, while new surfaces are formed. Therefore, the activation energy of these behaviors can be expressed in terms of the stacking fault energy (γ_{SFE}) and surface energy (γ_{SUR}) as:

$$\Delta G = \Delta G(\gamma_{\text{SFE}}, \gamma_{\text{SUR}}) \quad (5)$$

We then calculate the required γ_{SFE} and γ_{SUR} . The calculation of γ_{SFE} involves the construction of a bulk sample and the determination of the maximum energy needed for sliding along the $\langle 111 \rangle$ direction on the $\{110\}$ plane (further details can be found in section S2 of the ESI†). On the other hand, γ_{SUR} is directly calculated by using the established nanowire sample (more details are provided in section S3 of the ESI†). As a result, the values of γ_{SFE} and γ_{SUR} of the nanowires are determined to be 1.363 J m^{-2} and 2.615 J m^{-2} , respectively. Notably, compared with γ_{SFE} , the higher γ_{SUR} supports our hypothesis that the surfaces of the nanowires with smaller radii may exert a more significant influence on their yield stress.

The activation process of dislocation is illustrated in Fig. 5(a). To facilitate the construction of the model, we set the height of the model to be perpendicular to the $\{110\}$ plane. First, we assume that the area of dislocation nucleation is much smaller than the surface of the nanowire sample. Therefore, at the site where dislocation nucleates, we simplify the curved surface as a plane. The orange plane represents the simplified surface, and plane A is concaved into the nanowire under the influence of the dislocation nucleation, which form the curved surface B, and the top and bottom of surface B are semicircles C with radius r . The contribution of γ_{SFE} and γ_{SUR} to the activation energy corresponds to the change of their relevant area in the activation model. The area corresponding to the contribution of γ_{SFE} is $S_1 = (\pi - 2)rh$, which is the increased area from plane A to curved surface B, and the area corresponding to the contribution of γ_{SUR} is $S_2 = \pi r^2/2$, which is the area of the new surface C. Here, r is the distance at which the stacking fault occurs and is set to $0.433a$, and h is the atomic distance in the $\langle 110 \rangle$ direction and is set to $0.707a$. Smoluchowski *et al.*⁵⁸ suggested that the presence of a surface on nanowires could lower the energy barrier for dislocation nucleation, making nucleation easier. By using the surface proportion

suggested previously as the influence factor for reducing the stacking fault energy barrier, the corresponding contribution of γ_{SFE} is weakened, with the degree of weakening being dependent on the radius of nanowires. Hence, the activation energy can be expressed as:

$$\Delta G = (\gamma_{\text{SFE}} - \alpha\gamma_{\text{SUR}}) \frac{\pi r^2}{2} + \gamma_{\text{SUR}}(\pi - 2)rh \quad (6)$$

where α is the surface proportion of nanowires with radius R . The activation volume is a semi-cylinder created by concave surface B. Assuming that the formation of surface B affects a wider range, the height of the activation volume is set to $H = 2h$. Therefore, the activation volume can be expressed as $V^* = \pi r^2 H/2$. From eqn (4), the shear stress can be expressed as eqn (6) divided by the activation volume V^* . Additionally, there is an angle between the loading direction and the dislocation glide direction. The Schmid factor, $\mu = 0.41$,⁵⁵ is used as a conversion factor in the model to link the predicted shear stress (τ) and the simulated yield stress (σ). Therefore, the yield stress σ of a nanowire with radius R can be expressed as:

$$\sigma_y = \frac{1}{\mu} \frac{(\gamma_{\text{SFE}} - \alpha\gamma_{\text{SUR}})\pi r + 2.28\gamma_{\text{SUR}}h}{\pi r H} \quad (7)$$

Substituting the parameters into eqn (7) and comparing the results with the MD results, as shown in Fig. 5(b), one can see that the predicted curve aligns well with the MD simulation results. With the increase of R , the stress increases initially, then flattens out gradually. The yield stress predicted aligns well with the MD results at the IHP stage, specifically, in the range of $2 \text{ nm} < R < 6 \text{ nm}$.

To evaluate the predictive capability of the model for the mechanical properties of various BCC metal nanowires, we select the constituent metals of RHEAs and other metals or alloys for verification. To ensure the accuracy of the results for single-component metals and minimize the influence of the difference in sample size,⁵⁹ samples with a predefined

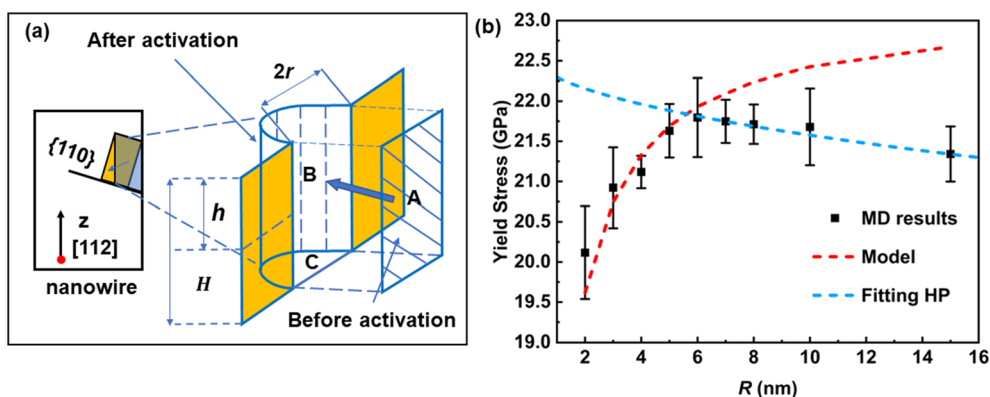


Fig. 5 (a) Schematic of dislocation activation from the surface of the nanowire (orange plane). (b) Comparison of yield stresses of NbMoTaW nanowire samples with different R obtained using theoretical model predictions [red curve, eqn (7) for the IHP stage; blue curve, fitting curve using the HP relation] with that simulated using MD (black points).

radius and a radius deviation of ± 0.1 nm are built (*e.g.*, $R = 2$ nm represents the average of $R = 1.9$ nm, 2.0 nm and 2.1 nm). The average value of the three sets of simulations is taken as the yield stress, WTa alloys are treated similarly to RHEAs, and their yield stress, γ_{SFE} , and γ_{SUR} are obtained under the same simulation conditions. Although the deformation mechanisms of some metals are dominated by twinning rather than dislocation nucleation, it is important to note that both dislocation nucleation and twinning are initiated by partial dislocations.^{7,60} Therefore, using γ_{SFE} as a consistent descriptor for yield stress is justified.

Two types of results are obtained: one exhibits the IHP relation and the other does not;¹⁸ here we only choose the former for discussion (other results can be found in section S4 of the ESI†). Several metals show the IHP relation, including W, Mo, Fe, and WTa; a verification range of $2 \text{ nm} \leq R \leq 7 \text{ nm}$ is selected for the comparison of the results predicted using eqn (7) with those obtained using MD simulations, as shown in Fig. 6. The yield stress obtained using MD simulations also takes the average of the results of the three samples. The γ_{SUR} and γ_{SFE} used in eqn (7) for each metal are calculated and shown in section S4 and Table S1 in the ESI†.

Overall, the model can predict more accurately the yield stress of nanowires with smaller radii ($2 \text{ nm} < R < 7 \text{ nm}$ in Fig. 6). It can be seen in Fig. 6 that W has the highest yield stress, ranging approximately from 27 to 28 GPa, while eqn (7) gives a prediction from 27 to 30 GPa. Fe has the lowest yield stress, around 17 to 18 GPa, with a critical transition radius of about 3 nm [Fig. 6]; in the IHP stage, the yield stress predicted by eqn (7) lies between 17 and 18 GPa. The yield stresses of the Mo and WTa nanowires fall within these ranges. Compared to NbMoTaW [Fig. 5(b)], these metals/alloys exhibit relatively stable yield stresses across the radius range we adopt, limiting our ability to identify the critical radius where the HP relation transitions to the IHP relation. Additionally, examining the error bars in Fig. 6, one can find that for each target radius, the calculation results for the three sample groups are relatively consistent, indicating that although minor size variations affect the yield mechanism,

their impact is less pronounced than the effect of random component distribution in RHEAs. The error bars for WTa alloys suggest that the random distribution of components in more complex alloys may influence the yield stress more significantly, implying that the size effect might be more substantial in RHEAs.

The orientation of a nanowire is also an important factor affecting its strength.^{35,51} We investigate the size effect on the yield stress of NbMoTaW nanowires with different orientations. The results indicate that the results of the [110] and [111] oriented nanowires are similar to those of the [112] oriented nanowires, both showing a transition from the HP relation to the IHP relation. In contrast, the [001] oriented nanowires exhibit consistently the HP relation (more details are given in section S5 in the ESI†). This difference can be attributed to variations in surface energy, atomic arrangement, and deformation mechanisms associated with different orientations. The theoretical model based on the [112] oriented nanowires still have room for improving the description capabilities to include these orientations, which implies the significance of establishing a unified theoretical expression.

5. Conclusion

In this work, we investigated the deformation behavior and mechanical response of NbMoTaW nanowire samples with different radii subjected to tensile deformation using molecular dynamics simulations, aiming to uncover the size effect and develop the corresponding model for the prediction of their yield stress. The main conclusions are drawn as follows:

(1) The yield stress of NbMoTaW nanowire samples exhibit significant variation with the sample radius, showing a transition between the Hall-Petch (HP) and inverse Hall-Petch (IHP) relations at a critical radius of about 6 nm.

(2) The dominant deformation mechanism observed was the nucleation and glide of dislocation from the surface, with twin nucleation typically occurring after the formation of dislocations. Although multiple dislocations form rapidly, yield generally occurs with the nucleation of the first dislocation and the emergence of a twin on the $\{110\}$ plane before transitioning to the formation of a slip band.

(3) A thermal activation-based theoretical model was developed for the prediction of yield stress, making use of stacking fault energy and surface energy as pivotal parameters. This model can effectively predict the yield stress of NbMoTaW nanowires at the IHP stage. The validity of the model in predicting the yield stress of other BCC metal nanowires was evaluated. It was found that although the metals verified exhibited both dislocation nucleation and twinning as the primary deformation mechanisms, they are consistently initiated by partial dislocation slip, allowing for consistent application of the model. Different verification approaches were employed for the prediction of the yield

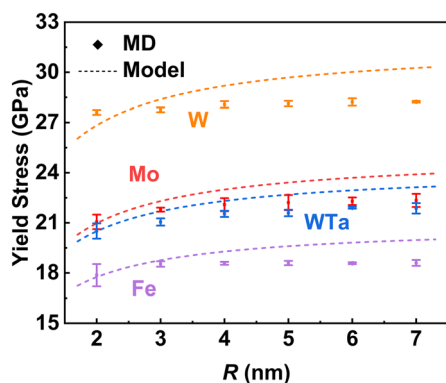


Fig. 6 Comparison of yield stresses for metals predicted using eqn (7) with that obtained using MD simulations, exhibiting the IHP relation.

stresses of BCC metal nanowires. The results demonstrated the validity of the model.

This study may contribute to the understanding of the deformation mechanism and size dependent mechanical properties of BCC refractory high entropy alloy nanowires.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Conflicts of interest

There are no conflicts to declare.

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