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First-principles NMR of oxide glasses boosted by machine learning†

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Solid-state NMR has established itself as a cutting-edge spectroscopy for elucidating the structure of oxide glasses thanks to several decades of methodological and instrumental progress. First-principles calculations of NMR properties combined with molecular-dynamics (MD) simulations provides a powerful complementary approach for the interpretation of NMR data, although they still suffer from limitations in terms of size, time and high consumption of computational resources. We address this challenge by developing a machine-learning framework to boost predictive modelling of NMR spectra. We use kernel ridge regression techniques (least-squares support vector regression and linear ridge regression) combined with smooth overlap of atomic position (SOAP) atom-centered descriptors to efficiently predict NMR interactions: the isotropic magnetic shielding and the electric field gradient (EFG) tensor. As illustrated in this work, this approach enables the simulation of magic-angle spinning (MAS) and multiple-quantum magic-angle spinning (MQMAS) NMR spectra of very large models (more than 10 000 atoms) and an efficient averaging of NMR properties over MD trajectories of nanoseconds for incorporating finite-temperature effects, at the computational cost of classical MD simulations. We illustrate these advances for sodium silicate glasses ($\text{SiO}_2\text{--Na}_2\text{O}$). NMR parameters (isotropic chemical shift and electric field gradient) could be predicted with an accuracy of 1 to 2% in terms of the total span of the NMR parameter values. To include vibrational effects, an approach is proposed of scaling the EFG tensor in NMR simulations with a factor obtained from the time auto-correlation functions computed on MD trajectories.

Introduction

Glasses are ubiquitous materials in modern life because of their low cost but good performances for a high diversity of usages.^{1–5} Glass indeed offers an infinite combination of compositions (but within a glass formability window) to match the properties of interest. The importance of glass was recognized in 2022 by

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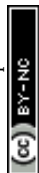


UNESCO, who declared it as the International Year of Glass.[‡] The fundamental challenge in glass science remains the establishment and the knowledge of the relationships between the composition-structure and the properties for the design of new formulations for specific applications. To this aim, molecular dynamics (MD) is the reference technique for building atomistic structural models of glasses and calculating the properties of interest.^{6–9} Spectroscopic data are, however, needed to assess the MD structural models, which have been mostly provided by neutron and X-ray diffusion experiments for decades.^{10–12} In this regard and in the context of oxide glasses, NMR remains underexploited and has been generally limited to its ability of providing quantitative information on the structural motifs building the glass network (such as SiO₄, AlO₄, BO₃, and BO₄) featuring the so-called short-range order (SRO).

NMR has clearly proven over the two last decades to be a key spectroscopy method for deciphering glass structure at various atomic length scale orders (from short to intermediate range order).^{13–22} Beside the direction of development of advanced radio-frequency pulse sequences for manipulating NMR interactions with an extremely high degree of accuracy,^{19,21} a second direction was proposed with the introduction of accurate and robust DFT computation methodologies, based on the popular DFT-GIPAW method.^{23–25} These two directions are of course complementary but both address the essential difficulty encountered in studying amorphous materials such as oxide glasses: the chemical and geometrical disorder introduces broadening of the lines resulting in a strong overlap between NMR peaks, which can persist despite the usage of sophisticated 2D high-resolution techniques. This spectral broadening is engendered by the NMR parameter distribution, a salient feature of glassy materials that cannot be ignored when fitting experimental data.^{16,26–31} With the help of relationships established either from known crystalline samples or DFT computations, NMR parameter distributions can be inverted to a distribution of a geometrical parameter, such as inter-atomic distances, bond lengths or bond-angle distribution (BAD).^{31–34} However, such approaches are limited to simple glass compositions and are difficult to extend when there is interplay between several parameters. A direct link between a 3D structural model and the NMR spectrum that can provide such information is therefore necessary.

The continuous increase of computational resources combined with the efficiency and accuracy the DFT-GIPAW method^{35–37} has enabled its fruitful combination with MD, so that a first-principles NMR approach has emerged as a new tool for investigating glasses.^{38–41} Within this framework, one can validate the interpretation of experimental data by prediction of NMR fingerprints of atomic species^{42,43} or assess the quality of MD structural models with a direct comparison with NMR data.^{44–46} According to our own experience, modern computational resources enable GIPAW-DFT calculations with MD models of up to ~800 atoms to be performed. DFT inherently limits applicabilities to representative models of glass of several thousands of atoms (a standard size is 5000–10 000 atoms for MD studies). In addition, investigations of dynamical effects (such as vibrations or diffusion of atoms) on NMR^{47–50} necessitates long MD trajectories of the order of ns to be considered. Consequently, the recent emergence of machine-learning (ML) methodologies in atomistic modelling⁵¹ offers appealing perspectives for

[‡] <https://www.iyog2022.org/>



accessing larger system sizes and time scales. In solid-state NMR, kernel ridge regression (KRR) techniques were applied to predict NMR shifts in organic molecular solids by Paruzzo *et al.*⁵² and in organic molecules by Rupp *et al.*⁵³ The first application to silicate glasses was provided by Cuny *et al.*⁵⁴ using a neural network and by Chaker *et al.*⁵⁵ in sodium aluminosilicate glasses with linear ridge regression (LRR). Gaumard *et al.*⁵⁶ studied the performances of different kernel regressions in zeolites. Recently, the positions of cesium in clays were refined by Ohkubo *et al.*⁵⁷ by using predicted NMR chemical shifts from LRR. In the context of amorphous molecular solids, Cordova *et al.*^{58,59} combined MD and KRR-SOAP predicted shifts (ML-Shift),⁵² to match structural models to experimental MAS NMR spectra. In the context of oxide glasses where quadrupolar nuclei are predominant, prediction of the EFG tensor is needed.

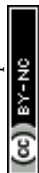
For atomistic modelling by ML, the so-called atom-centered descriptors (ACDs) play a central role. In the ML context, they were introduced in the seminal work of Behler *et al.*⁶⁰ and Bartók *et al.*⁶¹ The variety of descriptors that have been proposed in the literature is too vast to be covered here (see for, example, ref. 62–64). ACDs must provide a faithful and symmetry-adapted representation of the local environment of a central atom (chemically and geometrically): they must be invariant to translations and permutations, and equivariant to rotations and inversions with regard to the nature of the property of interest. Indeed, for prediction of a scalar property (such as the isotropic magnetic shielding, a charge or an energy), they must be invariant.⁶¹ In contrast, for tensorial properties (in our case the electric field gradient (EFG) tensor), they must respect the rotational properties of the second-rank tensors, as was first discussed by Grifasi *et al.*⁶⁵ In this work, we have chosen the popular smooth overlap of atomic positions (SOAP) descriptors, which have extensively been studied^{61,66–69} and shown to have excellent performances for NMR shifts prediction.^{52,55,56}

We present a fully-integrated methodology based on ML kernel tools (linear and kernel ridge regression, least-squares support vector regression, kernel density estimation, and dimensional reduction with incomplete Cholesky decomposition of the kernel Gram matrix) for simulation of the NMR spectra of structural models containing up to several thousands of atoms (calculations were performed on a standard workstation). Our strategy for building a database for ensuring a good transferability of the ML predictions (between various glass compositions and MD temperatures) is presented, as well as ideas for application to the study of the impact of local mobilities (vibrations, or diffusion of atoms) on the NMR spectrum. This opens an appealing perspective for the investigation of ionic conduction in glasses *via* NMR. Sodium-silicate glasses $\text{Si}_2\text{O}-\text{Na}_2\text{O}$ have been chosen as a representative model of oxide glasses: they contain both $I = 1/2$ (^{29}Si) and quadrupolar nuclei (^{23}Na and ^{17}O), one with a high local mobility (Na^+). Experimental data were taken from previous studies.^{27,29}

Theory and methods

SOAP descriptors for representing the local environment

To represent the local environment of an atom, the SOAP descriptors were chosen.^{61,66} They are constructed from the expansion of the smoothed atomic density $\rho_i(r)$ of a central atom i as:



$$\rho_i(\mathbf{r}) = \sum_{j \in N_i} g_\sigma(\mathbf{r} - \mathbf{r}_{ij}) f_c(r_{ij}) = \sum_{\mu, n, l, m} c_{n, l, m}^{i, \mu} Y_{lm}(\hat{\mathbf{r}}) R_{nl}(r) \quad (1)$$

N_i is the set of atoms j that are in the neighbourhood within a cutoff radius r_{cut} . g_σ is a (3D) Gaussian function of width σ and $f_c(r) = (1/2)\{\cos(\pi r/r_{\text{cut}}) + 1\}$ is the function used to smooth the density at the cutoff radius. $Y_{lm}(\hat{\mathbf{r}})$ are spherical harmonics ($\hat{\mathbf{r}} = (\theta, \phi)$ are the polar and azimuthal angles) and $R_{nl}(r)$ are radial functions. μ is an index that runs on the various atomic species (here, Na, Si and O). In this work, we employ real spherical harmonics (RSH) $Y_{lm}(\hat{\mathbf{r}})$ and spherical Bessel functions $R_{nl}(r) = j_l(\alpha_{nl}r/r_{\text{cut}})$. α_{nl} is the n th root of the Bessel function j_l . This choice ensures that the $R_{nl}(r)$ form an orthonormal set on the segment $[0, r_{\text{cut}}]$ (see Section S4 of the ESI†). With eqn (1), the local environment $\rho(\mathbf{r})$ of the central atom is represented by the set of parameters $c_{n, l, m}^\mu$. For computations, the expansion of eqn (1) is truncated to values $n \in [0, N_{\text{max}}]$ and $l \in [0, L_{\text{max}}]$. Thus, $(r_{\text{cut}}, N_{\text{max}}, L_{\text{max}})$, which are called hyper-parameters, have to be optimized during the training of the ML algorithm. The $c_{n, l, m}^\mu$ are invariant to permutations of the neighbouring atoms and to translations, and they behave like an l -rank tensor under rotations. They represent the local environment of a central atom X in terms of two body interactions. Indeed, for Na₂O–SiO₂ glasses, the expansion on the index μ yields X–Si, X–O and X–Na terms.

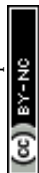
For the prediction of the scalar isotropic magnetic shielding value σ_{iso} (or equivalently, the isotropic chemical shift), we need rotation-invariant descriptors. The symmetry-adapted descriptors are therefore reduced to $c_{n, 0, 0}^\mu$ values, which severely limits the number of descriptors for an environment that can contain around ten atoms (in practice, N_{max} ranges from 2 to 12). To overcome this limitation in their seminal work, Bartók *et al.*⁶¹ introduced the power spectrum, a set of descriptors that combine the $c_{n, l, m}^\mu$ into a sum of rotationally invariant products:

$$p_{n_1, n_2, l}^{\mu_1, \mu_2} = \sum_m c_{n_1, l, m}^{\mu_1} c_{n_2, l, -m}^{\mu_2} \quad (2)$$

The power spectrum contains three-body terms, which account for the distribution of angles around the central atom (*i.e.*, Si–X–Si, Si–X–O, Si–X–Na, O–X–O, O–X–Na and Na–O–Na) as was explicitly shown in ref. 67. For tensorial properties of rank λ (*i.e.*, using the familiar notation in NMR, $T_{\lambda, m}$), eqn (2) can be easily generalized to become equivariant:

$$\left(q_{n_1, n_2, l_1, l_2}^{\mu_1, \mu_2} \right)_{\lambda, m} = \sum_{m_1, m_2} (\lambda, m | l_1 m_1 l_2 m_2) c_{n_1, l_1, m_1}^{\mu_1} c_{n_2, l_2, m_2}^{\mu_2} \quad (3)$$

where $(\lambda, m | l_1 m_1 l_2 m_2)$ are the Clebsch–Gordan coefficients. These descriptors, referred to as λ -SOAP, were introduced by Grifasi *et al.*,⁶⁵ generalizing thereby the SOAP power spectrum to represent a tensorial quantity. One can easily recognise that eqn (2) is a special case of eqn (3) with the choice $\lambda = 0$ (then $l_1 = l_2$). In the case of the EFG tensor or the symmetric part of chemical shift anisotropy (CSA) tensor, $\lambda = 2$. The NMR tensor (we consider only the EFG in this work) is then represented by a 5-dimensional vector denoted V_m in its spherical form (see Section S6 of the ESI†), which is the form that is used in our linear ridge regression (LRR) algorithm. Note that the dimensions of λ -SOAP descriptors can be very high (in our case, from 10^2 to 10^4), thus necessitating a large dataset for training the LRR algorithm.



Least-squares support vector and linear ridge regression

The kernel ridge regression (KRR) is a generalization of the popular linear ridge regression (LRR) by introducing non-linearities through a kernel function, which can be seen as a measure of the similarity between two environments, here denoted χ . For the isotropic magnetic shielding $\sigma_{\text{iso}}(\chi)$, the prediction is performed *via* a linear combination of similarities between the new environment χ_{new} and the training ones χ_i , as follows:

$$\sigma_{\text{iso}}(\chi_{\text{new}}) = \sum_{i \in \text{train}} K(\chi_{\text{new}}, \chi_i) \alpha_i \quad (4)$$

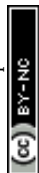
where $K(\chi_i, \chi_j)$ is the kernel function. In LRR, the kernel is the scalar product $K(\chi_i, \chi_j) = \chi_i \cdot \chi_j$. A standard choice is the Gaussian function (in this case KRR shares similarities with Gaussian Processes⁷⁰) $K(\chi_i, \chi_j) = \exp\{-\theta \|\chi_i - \chi_j\|^2\}$ where θ is a (hyper-)parameter that needs to be optimized. Note that considering all points in the dataset, eqn (4) can be rewritten in a “matrix form” as $\sigma = K\alpha$. Consequently, the determination of the regression parameters α (*i.e.*, the training phase) is obtained from $\alpha = (K + \varepsilon I)^{-1} \sigma$. ε is the ridge parameter that controls the norm of the regression parameters α in order to prevent the ML predictor from overfitting the training data. ε therefore has to be optimized from a second set of independent data (the validation set) in order to ensure a good transferability of the ML prediction to new data (the testing set).

Because of the high dimensionality of the training set, the resolution of the linear system eqn (4) can be cumbersome. The idea of the least-squares support vector regression (LSSVR)⁷¹ is to use a reduced set of representative data, denoted ξ , generally referred to as the inducing points or the landmark points. Restricted to this small set, the inversion of the kernel matrix $(K + \varepsilon I)^{-1}$ is then tractable. From a NMR perspective, it can be easily understood that many environments in the database are similar (and thus their NMR parameters are also very close), so that fewer points are necessary to support the linear regression eqn (4) (the support vectors). Mathematically, the kernel matrix is then approximated by $K_{\chi, \chi} \approx K_{\chi, \xi} K_{\xi, \xi}^{-1} K_{\xi, \chi}$ with $N_{\xi} \approx 103$, whereas $N_{\chi} \approx 105$ in our study. This is the Nyström approximation. Resolution of eqn (4) then only requires the diagonalization of $K_{\xi, \xi}$, as detailed in ref. 71, but the determination of the regression parameters α proceeds so as to account for all samples of the training set. To determine the inducing points ξ_i from the training set, we found that the incomplete Cholesky decomposition (ICD) of the kernel matrix $K_{\chi, \chi}$ (ref. 72) was very efficient and informative, as will be discussed below.

Concerning the EFG tensor, it was predicted in spherical form using the λ -SOAP descriptors, eqn (3), with LRR:

$$V_m = \sum_{\mu_1, \mu_2, l_1, l_2} \alpha_{n_1, n_2, l_1, l_2}^{\mu_1, \mu_2} \left(q_{n_1, n_2, l_1, l_2}^{\mu_1, \mu_2} \right)_{2, m} \quad (5)$$

Note that the summation over l_1 and l_2 is limited to values such that $(\lambda = 2, m | l_1 m_1 l_2 m_2) \neq 0$. In our work with $L_{\text{max}} = 4$, from the 25 (l_1, l_2) pairs, only 16 contribute in eqn (5).



NMR simulations with kernel density estimation

From DFT-GIPAW computations or ML predictions, the NMR parameters $x = (\delta_{\text{iso}}, C_Q, \eta_Q)$ for each atom (here ^{29}Si , ^{23}Na , and ^{17}O) are obtained. A simple approach for simulating the NMR spectrum consists in summing the individual NMR spectra for each atom. This would however be quite ineffective and time-consuming. As was discussed in earlier works,^{41,73} a better strategy for glasses consists in first reconstructing the NMR parameter distribution. The latter can of course be multi-modal if various species are present; in this case, a clustering algorithm can advantageously help to identify the speciations, an option that is left for future studies. Here a kernel density estimation (KDE)⁷⁴ approach is adopted for building the NMR parameter distribution $p(\delta_{\text{iso}}, C_Q, \eta_Q)$ on a 3D grid of pre-computed NMR spectra. In the case of silicon-29, quadrupolar parameters can be replaced by CSA values for an accurate modelling, but here a simple 1D approach is adopted so that only $p(\delta_{\text{iso}})$ is considered (for the reconstruction of anisotropic/isotropic 2D correlation with KDE, see for example ref. 41). In this work, we focus on MQMAS reconstruction of the two quadrupolar nuclei of interest, ^{17}O and ^{23}Na .

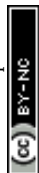
In the KDE formalism, the value of the distribution is estimated for each grid point $\mathbf{x}_g$ from the database points $\mathbf{x}_i$ as:

$$p(\mathbf{x}_g) = \frac{1}{N_i} \sum K_{\Sigma}(\mathbf{x}_g - \mathbf{x}_i) \quad (6)$$

where the kernel K_{Σ} is chosen as a Gaussian distribution of which the shape and width is controlled by the covariance matrix Σ (also referred to as the bandwidth matrix), which is calculated from the (training) $\mathbf{x}_i$ points. This matrix is essential to account for the correlation effects that exist between the NMR parameters, as was observed in oxygen-17 MQMAS NMR of silicate glasses.^{27,32,33} To lower the computational cost of eqn (6), numerous strategies exist to reduce the number of distance evaluations, such as an approximate nearest-neighbour search based on a graph.⁷⁵

From $p(\mathbf{x}_g)$ and precomputed spectra on the 3D grid, the simulation of the MAS and MQMAS spectra can then be reduced to simple matrix multiplications. In the case of a MQMAS simulation, equations were given in ref. 41. The pre-computed spectra can optionally account for the finite-pulse-width effects (intensity and lineshape distortion) and finite spinning rate. Denoting $I(\nu; \delta_{\text{iso}}, C_Q, \eta_Q)$ the pre-computed spectra on the grid and neglecting offset effects so that $I(\nu; \delta_{\text{iso}}, C_Q, \eta_Q) \approx I(\nu - \delta_{\text{iso}}; 0, C_Q, \eta_Q)$, only a 2D grid of (C_Q, η_Q) parameters is necessary. Typical grids have the following resolution (boundary values depend on the nucleus): C_Q 0.1 MHz, η_Q 0.05, and ν (or equivalently δ_{iso}) 0.2 ppm.

This KDE approach underlines that, in the specific case of glasses, the primary goal of the ML prediction is to reconstruct the NMR parameter distribution $p(\delta_{\text{iso}}, C_Q, \eta_Q)$ from the set of environments generated with the MD model(s). Thus, in addition to the quantification of prediction error for each point of the dataset, it is important to compare the reconstructed NMR parameter distribution from predicted ML values (and simulated NMR spectra) with the one computed from the DFT values. Accordingly, many (small) structural models are used to provide a set of sufficiently densely distributed points to estimate $p(\delta_{\text{iso}}, C_Q, \eta_Q)$. The alternative of using larger models offered by ML prediction enables investigation of size effects (such a spurious



correlation effect can be induced by the periodic boundary conditions (PBC) in MD simulations).

Optimisation of the hyper-parameters: *k*-fold cross-validation

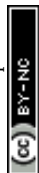
Beside the determination of the regression parameters in eqn (4) and (5), the SOAP, kernel and ridge parameters need to be optimized. They are generally referred to as hyper-parameters (with respect to the regression parameters α in eqn (4)). We use a *k*-fold cross-validation approach which consists in splitting the database into *k* subsets (in practice, $k = 5$): the testing set, the validation set and the remainder subsets are in the training set. In LSSVR and LRR, the regression parameters are determined with the training set and the ridge regression parameter is optimized by minimizing the error on the validation set. Note that the inducing points are restricted to being in the training set. The reported error is computed with the testing set. In order to have each point tested, the procedure is repeated *k*-times by shifting the *k*-folds. With an initial random shuffling of the database points, the whole procedure can be repeated so that each point can be a testing point more than once, and it provides a robust value of the error standard deviation value. The (hyper-)parameters of the descriptors and kernel width are optimized in an outer loop. Two errors are reported: the mean absolute error (MAE) and root mean square error (RMSE). The latter is sensitive to outliers so that both values are complementary.

Design of the NMR database

Structural models of Na_2O - SiO_2 glasses with % mol Na_2O ranging from 10% to 50% (by steps of 10%) were generated with classical MD simulations, as detailed in Sections S1 and S2 of the ESI.† For each composition, 20 independent small models of 300 atoms and 2 supplementary models of 600 atoms were generated for testing the transferability of ML algorithms to larger models when trained on small models. To investigate increased geometrical diversity, structures were extracted at 300 K, 1000 K (both forming the reference set), 1500 K and 2000 K. Long MD trajectories (up to 1 ns) were simulated to study the impact of vibrations on the NMR spectra. Additionally, for each composition, a model of 14 400 atoms was generated to demonstrate the applicability of machine learning NMR (ml-NMR) simulations to very large systems in short CPU times (here, ~ 2 s).

Part of the database was recently used for training a machine-learning potential (MLP).⁷⁶ Two compositions, denoted NS22.5 and NS43.1 (22.5 and 43.1% mol Na_2O , respectively) were chosen from this work (~ 700 atoms, see Table S2 of the ESI†) for the comparison of the ml-NMR spectra with experimental data (^{29}Si , ^{23}Na and ^{17}O).²⁷ To this end, *ab initio* MD simulations at 300 K were performed (with CP2K⁷⁷) for incorporating effects of vibrations at 300 K in the NMR simulations through the computation of correlation functions as detailed below. About 41 structures were extracted every 50 fs to build a NMR database from the first 2 ps of the trajectory. In the last 10 ps, 8 structures were extracted every 500 fs to check the accuracy of ML prediction.

The NMR properties, the magnetic shielding and electric field gradient tensors, were calculated with the DFT-GIPAW method²³ as implemented in VASP (version 5.3.x).³⁵ For referencing the NMR-GIPAW outputs σ_{iso} to the isotropic



chemical shift values δ_{iso} , SiO_2 (cristobalite and quartz), Na_2SiO_3 and α - and β - $\text{Na}_2\text{Si}_2\text{O}_5$ were used, but in a consistent approach with the MD models: for each system, a supercell of ~ 300 atoms was built, its geometry (atomic positions and unit cell parameters) was optimized with CP2K, and the NMR-GIPAW values computed with VASP. Details are given in Section S3 of the ESI.[†] Notably, the calibration parameters (α and σ_{REF}) of the linear regression $\delta_{\text{iso}} = -\alpha(\sigma_{\text{iso}} - \sigma_{\text{REF}})$ are given in Table S4 of the ESI.[†]

Results and discussion

Examination of the NMR database

We propose to examine the diversity of environments in the database by visualizing their respective NMR parameter distribution. For the quadrupolar nuclei, the NMR parameters were efficiently represented with the 2D distribution $p(\delta_{\text{iso}}, P_Q)$ using the quadrupolar product $P_Q^2 = C_Q^2(1 + \eta^2/3)$. Indeed, P_Q (in contrast to C_Q and η) is invariant to both the orientation and the ordering principal values of the EFG tensor (V_{xx}, V_{yy}, V_{zz}). This parameter should therefore be preferred for representing the EFG tensor strength rather than C_Q in glasses and during MD trajectories. As shown in Fig. 1, a broadening effect with increasing MD temperature is clearly seen in all data (resulting from a higher geometrical diversity). The aiMD data shows narrower distributions with more pronounced effects of correlation between the NMR parameters for oxygen-17 (note the opposite sign of the linear correlation between NBO and BO). As the MD and aiMD distributions do not overlap, it is therefore expected that MD data cannot predict the aiMD data well. This also points out that, even if less accurate, classical MD produces more disordered structures, and thus is more suitable for building a database with high transferability (a specialized database can be of course generated depending on the aim of the ML prediction). All datasets of the NMR database are given in Table S3 in the ESI.†

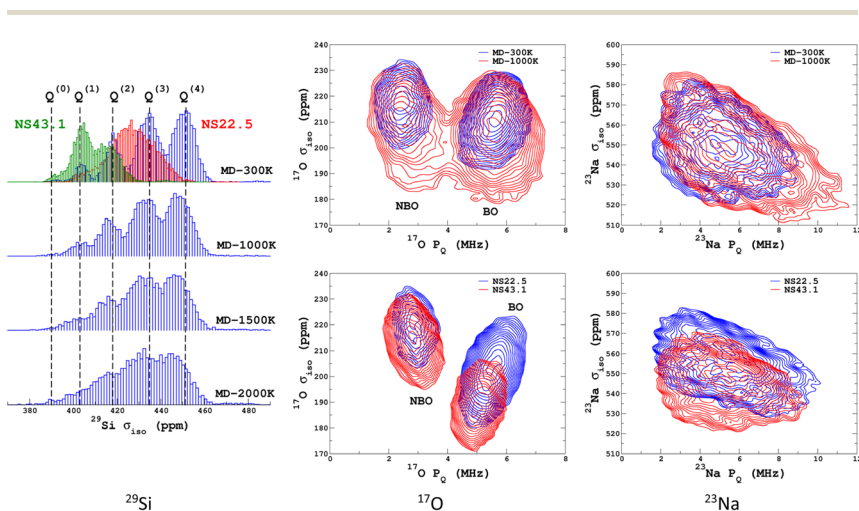


Fig. 1 ^{29}Si , ^{17}O and ^{23}Na NMR parameter distributions of datasets from the database. MD-xxx (xxx = 300 K, 1000 K, 1500 K and 2000 K) are classical MD models, and NS22.5 and NS43.1 are MLP models extracted from aiMD data at 300 K. For ^{17}O and ^{23}Na , $p(\delta_{\text{iso}}, P_Q)$ was calculated using KDE eqn (6).



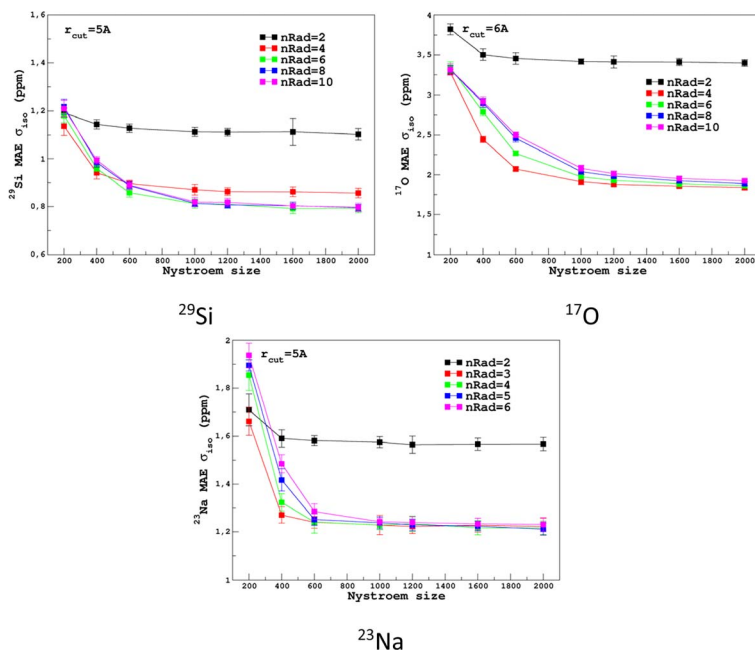


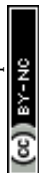
Fig. 2 Convergence of σ_{iso} MAE with respect to the Nyström size N_{ξ} and the number of radial functions ($n_{\text{Rad}} = N_{\text{max}}$) in the SOAP descriptors for the MD-300 K training set (other SOAP parameters are given in Table 1).

Learning the isotropic magnetic shielding

For the prediction of σ_{iso} (or equivalently δ_{iso}), we performed a systematic grid search on the SOAP hyper-parameters as follows: σ_{SOAP} in $[0.2, 1]$ Å (step 0.2 Å); $r_{\text{cut}} = 3, 4, 5$ and 6 Å; N_{max} from 2 to 12; L_{max} was fixed to 4. Details on the computation and optimization of the SOAP descriptors for the MD-300 K and MD-1000 K datasets are given in Sections S4 and S5, respectively, of the ESI.† For each set of $(\sigma_{\text{SOAP}}, r_{\text{cut}}, N_{\text{max}})$ values, the Nyström size (denoted N_{ξ}) was incremented until the MAE had converged (denoted N_{ξ}^{opt}). N_{ξ} strongly depends on the variety of environments present in the training set and N_{ξ}^{opt} can be therefore considered as a measure of the diversity of the database. An optimal value of σ_{SOAP} of 0.4 Å was obtained for all studied nuclei (^{29}Si , ^{17}O and ^{23}Na). Note that no attempt was made to set a different value for each atom. Representative MAE convergence curves are shown in Fig. 2 using MD-300 K as the training set. We observe that

Table 1 Parameters of SOAP descriptors $c_{n,l,m}^{\mu}$ (eqn (1)), and σ_{iso} mean absolute error (MAE) and root mean square error (RMSE) (with standard deviation values in parentheses)

Atom	σ_{SOAP} (Å)	r_{cut} (Å)	L_{max}	N_{max}	N_{ξ}^{opt} (MD-300 K + 1000 K)	MAE (ppm)	RMSE (ppm)
Si	0.4	5	4	4	2000	0.93 (0.02)	1.25 (0.03)
Na	0.4	5	4	6	1000	1.39 (0.02)	1.79 (0.03)
O	0.4	6	4	5	4000	2.25 (0.02)	3.15 (0.07)



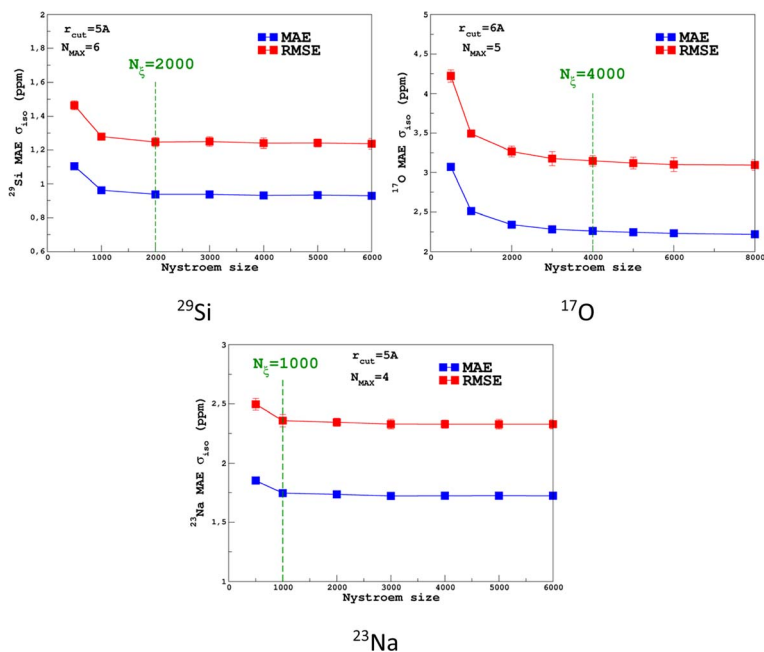


Fig. 3 Convergence of the σ_{iso} MAE with respect to the Nyström size N_{ξ} for MD-300 K + 1000 K training sets (SOAP parameters are given in Table 1).

increasing the number of radial functions (to better capture the diversity of the environment) effectively requires an increase in N_{ξ}^{opt} . The final optimal values that were determined from the dataset MD-300 K + MD-1000 K (the sets used to build the final LSSVR predictors) are given in Table 1 and convergence curves (MAE and RMSE) are shown in Fig. 3. Note that a higher value of N_{ξ}^{opt} is necessary with this composite set *versus* the individual set (for example, $N_{\xi}^{\text{opt}} = 1200$ for ^{17}O in MD-

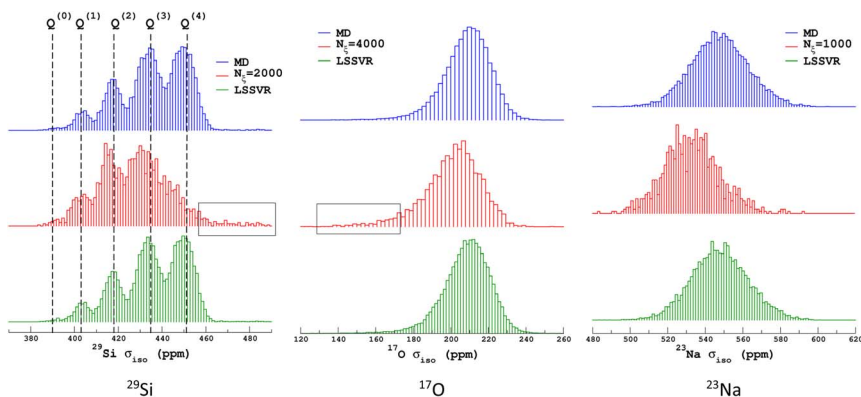
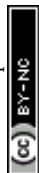


Fig. 4 Distribution of isotropic magnetic shielding σ_{iso} values from MD-300 K + 1000 K datasets, with inducing points selected by ICD and the LSSVR predictions. Distributions are normalized to the same area. Black boxes highlight the weak intensity regions that are well-captured by ICD.



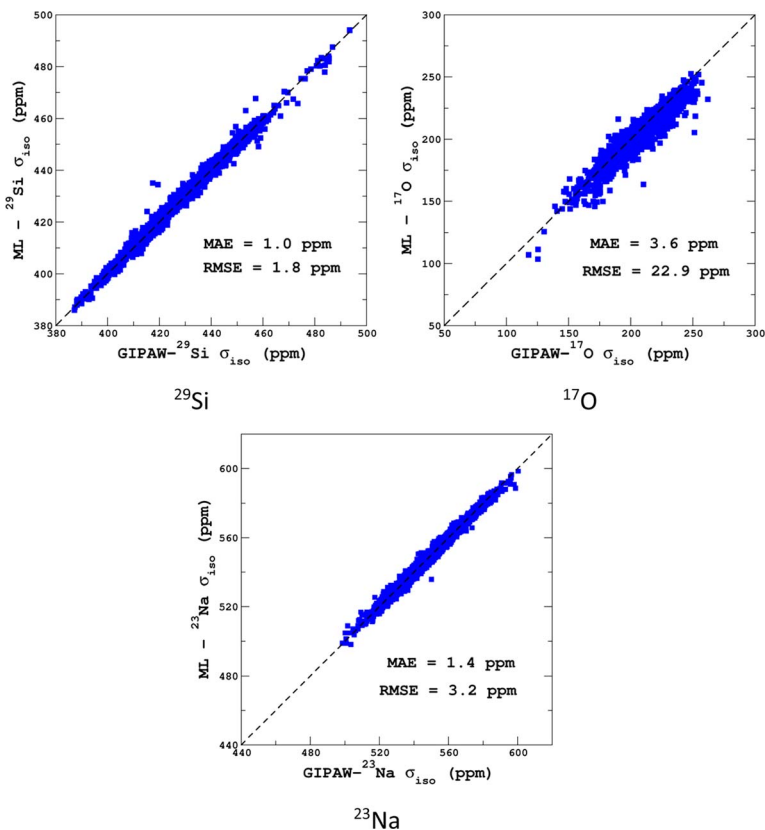


Fig. 5 LSSVR versus DFT-GIPAW σ_{iso} values for ^{29}Si , ^{17}O and ^{23}Na in the 600-atom MD datasets (300 K + 1000 K). Training was performed on the 300-atom data.

300 K and MD-1000 K, see Section S5 of the ESI†) showing the complementarity of the two datasets.

Similarly to Fig. 1, the selection of the inducing points ξ by ICD can be effectively visualized by examination of the NMR parameter distribution, as shown in Fig. 4. We first note the excellent prediction by LSSVR. Interestingly, ICD produces a distribution that differs from the original datasets by enhancing, for example, regions in the tails. Taking as an example the ^{29}Si data, clearly the $Q^{(3)}$ and $Q^{(2)}$ regions are significantly enhanced (which thus suggests a higher local structural diversity) *versus* the (more regular) $Q^{(4)}$ region. Note that the weak region $Q^{(0)}$ is well-retained by ICD. These results also confirm that the SOAP descriptors combined with a kernel-ICD approach are providing an efficient procedure for extracting the representative set of environments in a database. Attempts to force the selection of inducing points uniformly distributed on σ_{iso} did not improve the LSSVR predictions.

Transferability tests between the different training sets were performed and are reported in Section S5 of the ESI†. As expected, high-temperature sets give better accuracy when tested on a lower temperature, compared to the opposite



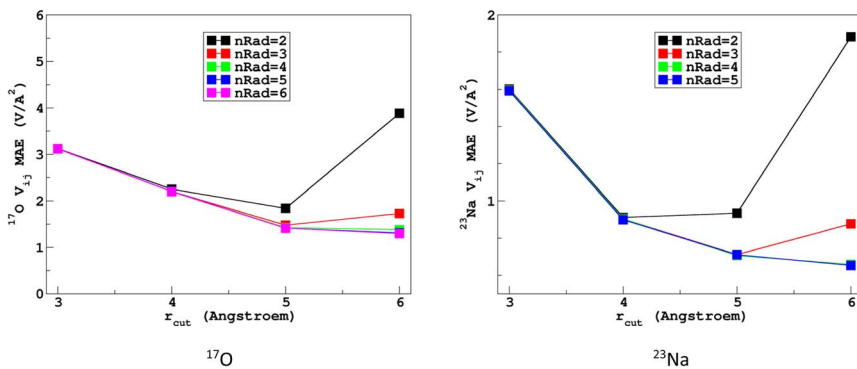


Fig. 6 Variations with the cutoff radius of the LRR λ -SOAP mean absolute error (MAE) of the EFG tensor components in the MD-300 K datasets.

case. Transferability to larger systems (*i.e.*, from 300 to 600 atoms) was also excellent and is illustrated in Fig. 5.

Learning the EFG tensor

It would be tempting to use LSSVR to predict the scalar quadrupolar parameters (C_Q , η). However, both quantities depend on the ordering of the eigenvalues of the EFG tensor and are therefore discontinuous. Effectively, they are very poorly predicted by LSSVR, as shown in Section S6 of the ESI.[†] Other ML algorithms (not investigated here) that are robust to discontinuities (such as neural networks or random forests) could be better adapted, but their investigation is out of the scope of the present study. Better LSSVR results are obtained for P_Q (which is invariant to rotation), but still show some discrepancies. For these reasons, the option of predicting the full EFG tensor appeared to be the best one.

Optimizations of the λ -SOAP descriptors for ^{23}Na and ^{17}O EFG tensors are summarized in Fig. 6. Despite contributions from long-range coulombic

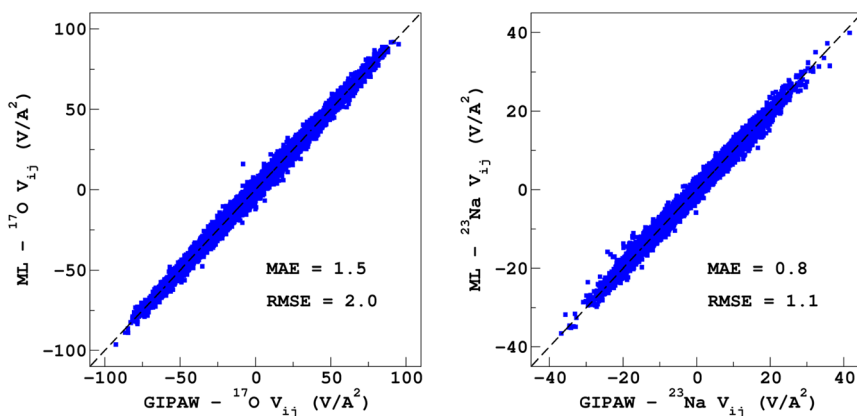
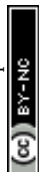
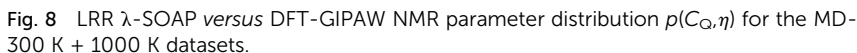


Fig. 7 LRR λ -SOAP versus DFT-GIPAW EFG tensor components of the 600-atom MD datasets (300 K + 1000 K).





KDE simulation of the MAS and MQMAS NMR spectra

Focusing first on the ^{23}Na NMR data and classical MD models, we observe a discrepancy between the large- and small-model spectra. This is indicative of the effect of the PBC on the structure of the small models, but without impacting the transferability of the ML predictors (Fig. 5 and 7). The comparison with experimental data shows a good agreement, except for the width of the spectra, which is due to an overestimated mean value of the quadrupolar coupling constant, as already observed.²⁹ As will be shown below, accounting for short-time-scale averaging by vibrations significantly reduces the discrepancies. Considering the

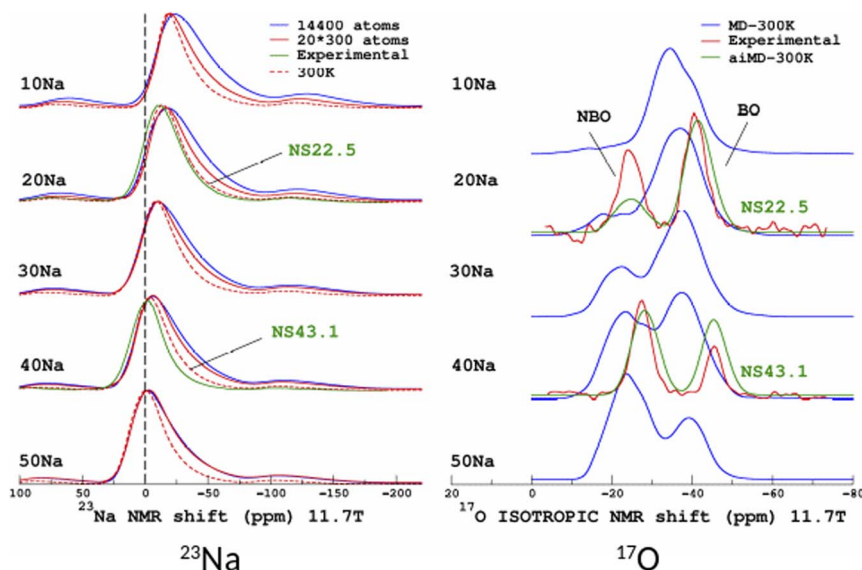


Fig. 9 ML simulations of ^{23}Na (left) and ^{17}O (right) MAS and isotropic (isotropic projection of the MQMAS spectra) NMR spectra of the $\text{SiO}_2\text{--Na}_2\text{O}$ glasses from 10% to 50% mol. Na_2O (denoted ^{10}Na to ^{50}Na). For the purpose of comparison, experimental data from ref. 27 are shown (22.5% and 43.1% mol. Na_2O , denoted NS22.5 and NS43.1, respectively). For ^{17}O , ML simulations from aiMD structural models (aiMD-300 K) are also shown.

^{17}O NMR data, we note a strong deviation of the classical MD NMR model spectra from the experimental data. This is due to the approximate Si–O and Si–O–Si bond angle values predicted in classical MD, in contrast to aiMD (DFT) data, which yields an excellent agreement in the position of the NBO and BO peaks (intensities differ because the impact of the MQMAS pulse sequence was not taken into account for the sake of simplicity). Those simulated spectra can be useful for many purposes. One of them is the assessment of analytical models of

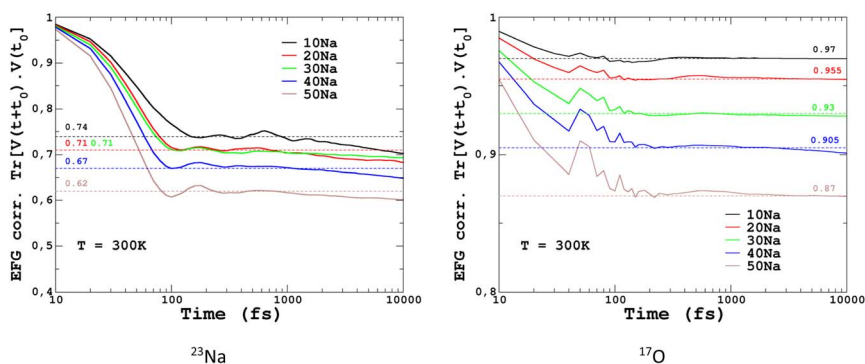


Fig. 10 ^{23}Na and ^{17}O EFG correlation functions $G_{\text{EFG}}(\tau) = \langle V(\tau + t_0)V(t_0) \rangle_{t_0}$. In the left and right panels, plateauing values used as EFG scaling factors for finite-temperature simulations are indicated.

NMR parameter distributions, such as the Gaussian Isotropic Model^{80,81} (GIM) for fitting the ^{23}Na NMR data, for example.

To quantify the impact of atomic vibrations on the NMR parameters, we investigated the auto-correlation functions of the two NMR interactions of interest in this work, $G_\delta(\tau) = \langle \delta(\tau + t_0)\delta(t_0) \rangle_{t_0}$ and $G_{\text{EFG}}(\tau) = \langle V(\tau + t_0)V(t_0) \rangle_{t_0}$, calculated on MD trajectories at 300 K. $\langle \rangle_{t_0}$ denotes the ensemble average that includes here the averaging over all initial times t_0 and over all atoms. At short-time scales, $G_\delta(\tau)$ is a constant function (~ 1) at 300 K, thus meaning a very minimal impact of vibrations. In contrast, $G_{\text{EFG}}(\tau)$ is decaying on the typical time-scale of vibrations (10–100 fs), with a stronger effect for ^{23}Na in contrast to ^{17}O , as illustrated in Fig. 10. After that first decay, the EFG time-correlation function reaches a plateau that can be considered, in a first approximation, as the time-averaged EFG that really contributes to the NMR spectra (whereas the initial decaying part controls the relaxation times,⁵⁰ but this will be not discussed here). Using the plateauing value as a scaling factor of the frozen EFG tensors (we assume an isotropic scaling), vibrations can then be simply incorporated into the NMR spectra, as shown for ^{23}Na (left panel in Fig. 10, dashed lines). This clearly improves the simulations (see especially ^{20}Na). We note that for ^{40}Na , the experimental width is still overestimated. Indeed, a longer time-scale would be needed to account for the diffusion of Na atoms at 300 K (Na-rich glasses show a higher Na mobility⁸²). The time-scale of the MD simulations is still well below the typical Larmor period for ^{23}Na (here ~ 8 ns at 11.7 T). Interestingly, aiMD simulations gave very close curves for the EFG correlation functions, as shown in Section S10 of the ESI.† This means that classical MD potentials are able to capture the vibrational averaging with a good accuracy.

Conclusion

We have described in this paper new computational methodologies for modelling NMR spectra of oxide glasses, combining prediction of NMR properties by ML kernel methods with efficient simulations using KDE of the NMR parameter distribution. We have shown that the SOAP descriptors are very efficient and symmetry-adapted for representing the local environment in the prediction of NMR interactions, be it a scalar (isotropic magnetic shielding value) or a matrix (the EFG second-rank symmetric tensor). Our strategy to build an NMR database that embraces a sufficiently large variety of environments (in terms of both geometrical and chemical disorder) was based on MD simulations at various temperatures and for various glass compositions. It was shown that small models were suitable to build ML predictors that are transferable to much larger systems (here, more than 10 000 atoms). Most representative environments could be extracted with incomplete Cholesky decomposition of the kernel Gram matrix of the dataset, providing an efficient tool for analysis of the database, as confirmed by the examination of the NMR parameter distributions. Appealing perspectives for an easy incorporation of finite-temperature effects (vibrations) in NMR simulations were presented. Because of its fundamental importance in glass science, ml-NMR will clearly enable NMR investigations of melts (with high-temperature NMR²⁰) to be now more closely connected to MD simulations by computation of the underlying correlation functions of NMR observations. The next step is the incorporation of NMR spectra as direct constraints in the



reconstruction of the 3D glass structure of glasses, in the Reverse Monte-Carlo simulations widely used in glass science.^{11,12,83}

Data availability

The data that support the findings of this study (DFT-GIPAW data for structures of the NMR database) are available at <https://doi.org/10.5281/zenodo.12314395>.

Conflicts of interest

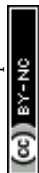
There are no conflicts to declare.

Acknowledgements

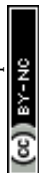
This work was granted access to the HPC resources of TGCC under the allocation DARI-A0110906303, DARI-A0130906303, and DARI-A0150906303 attributed by GENCI (Grand Equipement National de Calcul Intensif).

Notes and references

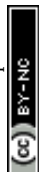
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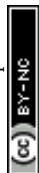
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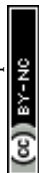
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