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2023, 16, 2550Multiple and nonlocal cation redox in
Ca–Ce–Ti–Mn oxide perovskites for solar
thermochemical applications†Robert B. Wexler,^a Gopalakrishnan Sai Gautam,^{ab} Robert T. Bell,^c
Sarah Shulda,^c Nicholas A. Strange,^d Jamie A. Trindell,^e Joshua D. Sugar,^e
Eli Nygren,^{cf} Sami Sainio,^d Anthony H. McDaniel,^e David Ginley,^c
Emily A. Carter^{id}*^a and Ellen B. Stechel^{id}*^g

Modeling-driven design of redox-active off-stoichiometric oxides for solar thermochemical H₂ production (STCH) seldom has resulted in empirical demonstration of competitive materials. We report the theoretical prediction and experimental evidence that the perovskite Ca_{2/3}Ce_{1/3}Ti_{1/3}Mn_{2/3}O₃ is synthesizable with high phase purity, stable, and has desirable redox thermodynamics for STCH, with a predicted average neutral oxygen vacancy (V_O) formation energy, $E_v = 3.30$ eV. Flow reactor experiments suggest potentially comparable or greater H₂ production capacity than recent promising Sr–La–Mn–Al and Ba–Ce–Mn metal oxide perovskites. Utilizing quantum-based modeling of a solid solution on both A and B sub-lattices, we predict the impact of nearest-neighbor composition on E_v and determine that A-site Ce⁴⁺ reduction dominates the redox-activity of Ca_{2/3}Ce_{1/3}Ti_{1/3}Mn_{2/3}O₃. X-ray absorption spectroscopy measurements provide evidence that supports these predictions and reversible Ce⁴⁺-to-Ce³⁺ reduction. Our models predict that Ce⁴⁺ reduces even when it is not nearest-neighbor to the V_O, suggesting that refinement of Ce stoichiometry has the possibility of further enhancing performance.

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Broader context

Sunlight is an abundant albeit low areal density source of renewable energy. Collecting and concentrating the sun's rays for its heat value can enable high-temperature endothermic reactions such as water splitting to produce clean hydrogen. Two-step thermochemical cycles with redox-active metal oxides are promising. However, technoeconomic analyses with state-of-the-art CeO₂ suggest that without a new active material, achieving the US Department of Energy's Hydrogen Shot \$1 per kg H₂ target is unlikely. Here, we introduce a previously unknown material predicted from theoretical considerations and experimentally validated. The material is a redox-active quinary oxide perovskite, CCTM, with solid solutions of Ca/Ce and Ti/Mn on the A- and B-sites, respectively. CCTM offers promising oxygen vacancy thermodynamics and exceptional H₂ yield, when reduced at moderate temperatures and cycled at relatively short reoxidation periods. Modeling reveals and experiment confirms that Ce⁴⁺ is the primary redox-active species, in contrast to other known reducible perovskites, where in all cases the active element sits on the B-site. Furthermore, even with B-site Ce⁴⁺, that element is not redox active. Hence this work reports the first perovskite with reducible A-site and reducible Ce⁴⁺, predicted entirely from theory, and subsequently validated with experiments that establish stability, reversibility, and high productivity.

^a Department of Mechanical and Aerospace Engineering and the Andlinger Center for Energy and the Environment, Princeton University, Princeton, NJ 08544-5263, USA. E-mail: eac@princeton.edu^b Department of Materials Engineering, Indian Institute of Science, Bengaluru, Karnataka 560012, India^c National Renewable Energy Laboratory, Golden, CO 80401, USA^d SLAC National Accelerator Laboratory, Menlo Park, CA 94025, USA^e Sandia National Laboratories, Livermore, CA 94550, USA^f University of California Santa Cruz, Santa Cruz, CA 95064, USA^g ASU LightWorks[®] and the School of Molecular Sciences, Arizona State University, Tempe, Arizona 85287-8204, USA. E-mail: ellen.stechel@asu.edu† Electronic supplementary information (ESI) available: Further details about the SCAN+U calculations, stability of CCTM2112, SQS construction for *Pnma* CCTM2112, V_O NN environment statistics, magnetic moment distribution by species in pristine CCTM2112, dependence of the V_O-induced magnetic moment changes by element on the V_O's NN environment, qualitative Ce and Mn oxidation state changes upon V_O formation, V_O-induced magnetic moment changes vs. distance, and projected density of states of pristine CCTM2112;^{40–47} additional synthesis details, comparison of H₂ produced by state-of-the-art redox-active perovskites, and XRD and XAS data from the reduced and re-oxidized CCTM powder; files containing crystal structures, total energies, magnetic moments, and projected densities of states. See DOI: <https://doi.org/10.1039/d3ee00234a>

Introduction

Combating climate change calls for decarbonized production of H_2 that can provide cost-effective, medium-to long-duration energy storage while also serving as a fuel¹ for transportation or industrial products and processes, or a feedstock.² However, the vast majority (95%) of commercial H_2 is produced today *via* steam-methane reforming (SMR), which consumes fossil fuels and contributes to direct CO_2 emissions (≈ 7 kg CO_2 per kg H_2 for the overall process of SMR³). Water splitting (WS) *via* renewable energy offers a simpler, more direct path to clean hydrogen with exceptionally low carbon intensity, albeit currently at greater expense. Given the magnitude of solar irradiance on the Earth's surface, solar thermochemical hydrogen (STCH) is potentially a cost-effective, sustainable, and carbon-neutral pathway to H_2 .⁴ However, functional STCH materials must meet an extraordinary set of requirements to be useful for large-scale hydrogen production. A STCH process that utilizes non-volatile metal oxides typically involves two steps,⁵ where the first is the thermal reduction (red) of a redox-active metal oxide (MO_x) at high temperatures generated by concentrated solar power⁶ or other solar sources of high-temperature heat and low partial pressures of oxygen (*i.e.*, at T_{red} and pO_2 where $\Delta G_{red} \leq 0$). The second step is the re-oxidation (ox) of the reduced metal oxide by steam at lower temperatures (where T_{ox} is typically several hundred degrees K less than T_{red} for spontaneous WS), thereby generating hydrogen.^{5–7}

Research over the last decade has struggled to replace pure CeO_2 as the state-of-the-art redox-active MO_x for two-step STCH.^{8–10} Thermal reduction of CeO_2 -based redox-active materials leads to the formation of oxygen vacancies (V_O) and therefore off-stoichiometric compositions, ($CeO_{2-\delta}$), which are re-occupied by O upon re-oxidation by steam.¹¹ However, demonstrated solar-to-fuel conversion efficiencies (η) have plateaued between 5–8%^{12–14} for laboratory-scale STCH reactors running on ceria at power levels < 5 kW_{thermal}. To surpass the performance of these CeO_2 -based STCH reactors, researchers are exploring other redox-active metal oxides, with the ABO_3 perovskites being a popular choice due to their compositional and structural flexibility.¹⁵ Specifically, research over the last decade has identified Sr–La–Mn–Al¹⁶ and Ba–Ce–Mn¹⁷ oxide perovskites, among others, as potential next-generation redox-active MO_x s. However, metal-oxide perovskites have yet to supplant CeO_2 -based materials as the preferred redox-active MO_x for STCH production.¹⁸

To create a stable and cyclable redox-active metal-oxide system at temperatures below the 1773 K needed for CeO_2 is a challenge. The metal oxide must have the correct thermodynamics to be able to cycle with steam as the oxidant, the kinetics to do so rapidly, and long-term stability at both the reduction and re-oxidation temperatures. To date, theory alone has yet to design new materials that cycle under conditions milder than necessary for CeO_2 with higher H_2 productivity. This paper provides and discusses validating evidence for a computational methodology that has been able to achieve that, identifying a new, highly functional STCH material.

Increasing the η of metal-oxide-perovskite-based STCH toward that of the ideal Carnot cycle generally amounts to

optimizing the thermodynamics of both reduction and re-oxidation; or $\Delta G_{red} = \Delta H_{red} - T_{red} \Delta S_{red}$ and $\Delta G_{ox} = \Delta H_{ox} - T_{ox} \Delta S_{ox}$. For materials that undergo reduction *via* oxygen off-stoichiometry like CeO_2 and metal-oxide perovskites, V_O formation energies (E_v) of 3.4–3.9 eV correspond to optimal values of ΔH_{red} .¹⁹ The E_v of CeO_2 is too high (4.4 eV),⁴ hence the need for the design of off-stoichiometry metal oxides like oxide perovskites with a lower E_v . Here, we build on our previous theoretical prediction of $Pnma$ $Ca_{0.5}Ce_{0.5}MnO_3$ (CCM)²⁰ as a promising STCH candidate based on its E_v of 3.65–3.96 eV (within the target range¹⁹) and investigate a stabilized oxide perovskite with Ca and Ce on the A-site and Ti and Mn on the B-site.

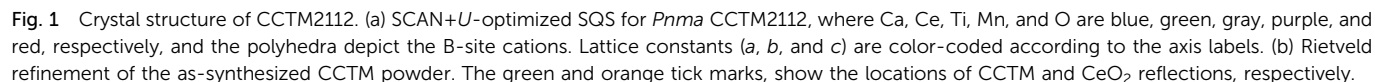
Results

Computationally predicted $Ca_{2/3}Ce_{1/3}Ti_{1/3}Mn_{2/3}O_3$ is stable experimentally

As is the convention in computational materials science, we quantify stability as the energy above the convex hull (E_{hull}), which is the energy change upon decomposition of a material into stable compounds at the same composition. Throughout, we performed density functional theory (DFT) calculations within the SCAN²¹+ U ^{22–25} framework (see Section S1 and S2 in the ESI† for additional details regarding the SCAN+ U calculations and E_{hull} computation, respectively).^{26,27} Based on this convex hull construction, CCM is thermodynamically metastable, with an $E_{hull} = 39$ meV per atom at 0 K. Experimental attempts to synthesize CCM perovskite were unsuccessful, with CeO_2 and Ca–Mn oxide phases predominating, and limited Ca–Ce–Mn oxide phase fraction decomposing during even gentle reduction (see Section S3 in the ESI†). We then tried to increase the stability by using the naturally abundant and highly stable $CaTiO_3$ perovskite as a template to then add a solid solution of Ce^{4+} and Mn^{3+} on the A- and B-sites, respectively. Beginning with the previously predicted CCM, we increased the fraction of Ca on the A-site (from 1/2 to 2/3) and Ti on the B-sites (from 0 to 1/3). The resulting structure is a $Pnma$ $Ca_{2/3}Ce_{1/3}Ti_{1/3}Mn_{2/3}O_3$ solid solution (CCTM2112, where the numbers indicate the relative composition of the material for three formula units or numerators of the fractional A- and B-site compositions for one formula unit), matching the $Pnma$ structure of $CaTiO_3$. For a preliminary check on stability, we used the τ tolerance factor of Bartel *et al.*²⁸ to predict whether CCTM2112 would form a perovskite. The τ value is 2.74, which gives a probability that the composition forms a perovskite structure of 94%, hence, high confidence. Additional support for this solid-solution approach came from reports of $CaTi_{0.5}Mn_{0.5}O_{3-\delta}$ ²⁹ and $CaTi_{0.2}Mn_{0.8}O_{3-\delta}$,³⁰ though, in our work, the A-site addition of Ce changes the predominant oxidation state of Mn in the fully-oxidized material from Mn^{4+} in the prior purely Ca-A-site perovskites to Mn^{3+} in CCTM2112 (see the section entitled Role of Ce^{4+} in Redox Activity). Independent simulation and empirical determination of the CCTM2112 crystal structure resulted in strong agreement in lattice parameters and atomic positions.

Simulated and empirical determination of the CCTM crystal structure resulted in strong agreement. The evidence for this agreement is the comparison of the Rietveld refined *Pnma* lattice parameters: $a = 5.61442 \text{ \AA} \pm 0.00013 \text{ \AA}$, $b = 7.55658 \text{ \AA} \pm 0.00018 \text{ \AA}$, $c = 5.35511 \text{ \AA} \pm 0.00013 \text{ \AA}$, to the simulated lattice parameters (extracted from supercell): $a = 5.567 \text{ \AA}$, $b = 7.640 \text{ \AA}$, and $c = 5.377 \text{ \AA}$, resulting in a deviation of simulation from empirical of -0.84% for a , $+1.10\%$ for b , and $+0.41\%$ for c . Small differences are expected as the composition was not identical. Additional comparison of simulated and empirically derived CCTM unit cells are included in Section S6.2 of the ESI,[†] which also shows an overlay of the computationally predicted structure onto the 300 K XRD data (Fig. S3, ESI[†]).

We now examine the energetics of V_O formation in CCTM2112 and its dependence on the V_O 's nearest neighbors (NNs). Inspired by our recent finding that local chemistry governs V_O formation in ternary metal-oxide perovskites,³⁶ we categorized all 216 V_O s by their (NN) environment and randomly sampled one V_O (*i.e.*, we introduce one V_O in the SQS, corresponding to $\delta = 0.014$) from each of the 13 unique V_O NN environments (Fig. 2(a)). This categorization also gave a tractable number of SCAN+ U calculations from which to study the trends in the electronic and thermochemical properties of V_O s. We define NN V_O environments using x_{Ce} and x_{Mn} , where $x_{Ce} = N_{Ce}/(N_{Ca} + N_{Ce})$, $x_{Mn} = N_{Mn}/(N_{Ti} + N_{Mn})$, and x (N) is the fraction (number) of the V_O 's four NN A-sites and two NN B-sites occupied by Ce ($x_{Ce} = 1 - x_{Ca}$ and $N_{Ce} = 4 - N_{Ca}$) and Mn ($x_{Mn} = 1 - x_{Ti}$ and $N_{Mn} = 2 - N_{Ti}$), respectively. Note that the overall supercell structure maintains the same cation stoichiometry as that of bulk CCTM2112, with x_{Ce} and x_{Mn} in Fig. 2(a) strictly defining compositions that are local to the V_O considered. Predictably, the V_O with the highest frequency ($f = 44$ or $44/216 \approx 20\%$ of the SQS) is the one with a NN environment



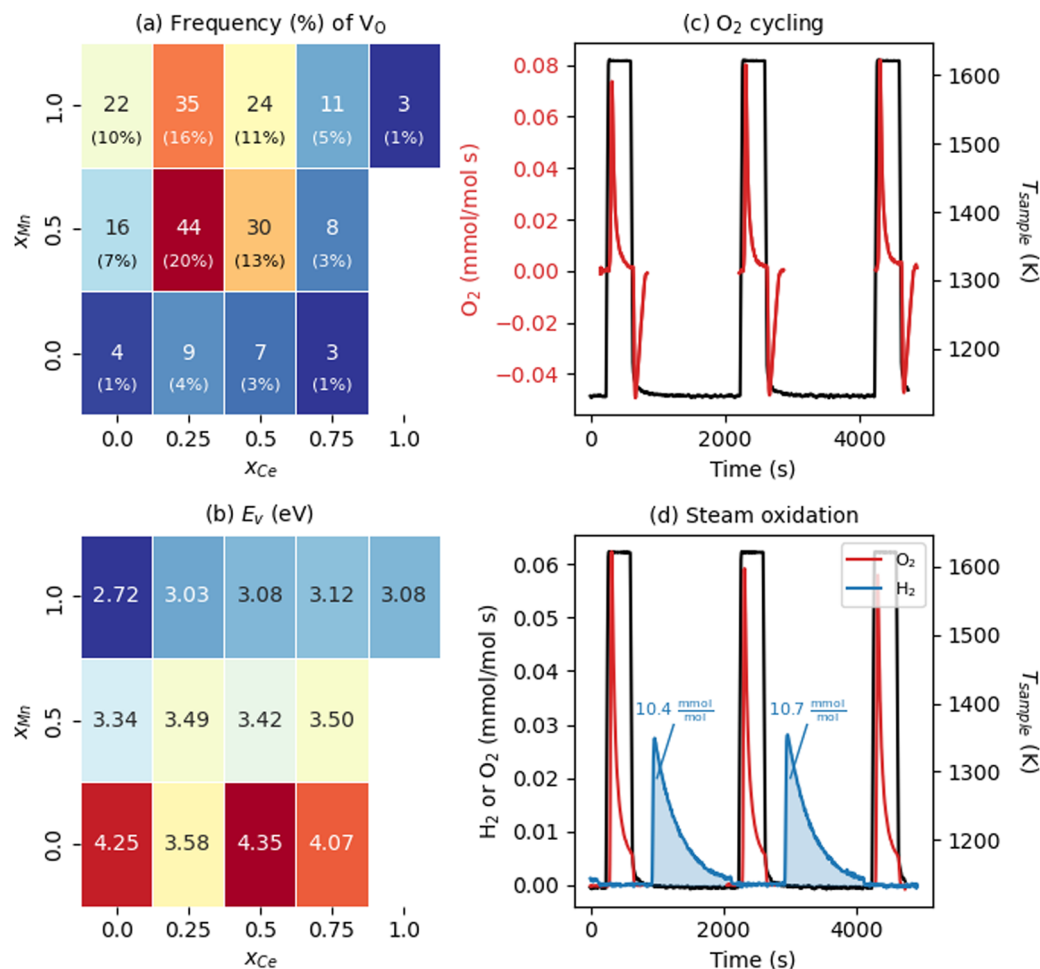


Fig. 2 Water-splitting properties of CCTM2112. (a) Frequency (color of and text in rectangles) and probability (percentages in parentheses rounded to the nearest integer) of all unique NN V_O environments in the calculated CCTM2112 360-atom cell (and, in Table S6, ESI† for the random alloy), with dark red and dark blue shading indicating higher- and lower-frequency environments, respectively. (b) NN- V_O -environment dependence of calculated E_v in CCTM2112. Color of and text in rectangles correspond to E_v in eV, where the minimum $E_v = 2.72$ eV is dark blue and maximum $E_v = 4.35$ eV is dark red. (c) O_2 evolution rate normalized to mole atoms in CCTM2112 (see ESI†, Section S5 for definition) measured as a function of time during heating and cooling between 1123 K and 1623 K in a constant background of 2000 ppm oxygen. (d) O_2 and H_2 evolution rates normalized to mole atoms in CCTM2112 measured as a function of time during two successive redox cycles where the sample temperature is raised to 1623.15 K while sweeping with high purity Ar, followed by exposure to 40 vol% H_2O in Ar at 1123.15 K. The area under the gas evolution features in (c) and (d) is used to quantify the redox capacity of CCTM2112 during oxygen and steam oxidation.

closest to the bulk composition allowed by the A and B site NN fractions ($x_{Ce} = 0.25$ and $x_{Mn} = 0.5$ for the V_O and $x_{Ce} = 1/3$ and $x_{Mn} = 2/3$ for the bulk). Two NN V_O environments do not appear in the optimized SQS for CCTM2112 (namely those for $x_{Ce} = 1$ and $x_{Mn} \leq 0.5$), however, V_O s with these NN environments are unlikely to influence significantly the macroscopic reduction of CCTM2112 due to their scarcity ($x_{Ce} = 1$ and $x_{Mn} = 0.5$, and $x_{Ce} = 1$ and $x_{Mn} = 0$ make up 0.5% and 0.1% of the random alloy, respectively).

With this V_O categorization protocol, we predict that five of the 13 V_O s (shaded yellow and light blue in Fig. 2(b)), including those with the first- and third-highest frequencies ($f = 44$ or $44/216 \approx 20\%$ for $x_{Ce} = 0.25$ and $x_{Mn} = 0.5$, which is 17.6% in a random solid (Table S6, ESI†), and $f = 30$ or $30/216 \approx 14\%$ for $x_{Ce} = x_{Mn} = 0.5$, which is 13.2% of the sites in a random solid), have E_v s within (or within 0.06 eV of) the target range of 3.4–3.9 eV (see Fig. 2(b)).¹⁹ To quantify the macroscopic reducibility

of CCTM2112, we calculate the ensemble-averaged E_v , $\langle E_v \rangle = \sum_i f_i E_{v,i} / \sum_i f_i$, where f_i is the frequency of the i^{th} unique NN V_O environment given in Fig. 2(a), and $\sum_i f_i = 216$. We

obtain $\langle E_v \rangle = 3.30$ eV with a standard deviation of 0.36 eV based on the E_v values in Fig. 2(b), which overlaps with the target range for water splitting. We find that while E_v depends weakly on x_{Ce} , it systematically decreases with increasing x_{Mn} . This trend can be rationalized on the basis of crystal $O^{2-}-M^{n+}$ bond dissociation energies E_b , an extension of molecular O–M bond dissociation energies to the solid state,³⁶ defined as

$$E_b[O^{2-} - M^{n+}] = \frac{E_c[MO_{n/2}]}{N_b[O^{2-} - M^{n+}]} \quad (1)$$

where n is the oxidation state of the metal cation (M), $E_c[MO_{n/2}]$

is the cohesive energy of the ground-state polymorph of the binary metal-oxide crystal $\text{MO}_{n/2}$ containing M^{n+} , and $N_{\text{b}}[\text{O}^{2-}-\text{M}^{n+}]$ is the number of $\text{O}^{2-}-\text{M}^{n+}$ bonds per $\text{MO}_{n/2}$ formula unit. In short, $E_{\text{v}} \propto -x_{\text{Mn}}$ because $\text{O}^{2-}-\text{Mn}^{4+}$ (crystal bond dissociation energy $E_{\text{b}} = 2.25$ eV) and $\text{O}^{2-}-\text{Mn}^{3+}$ (1.97 eV) crystal bonds are weaker than $\text{O}^{2-}-\text{Ti}^{4+}$ (3.16 eV) and $\text{O}^{2-}-\text{Ti}^{3+}$ (2.62 eV).³⁶

Experiments demonstrate that CCTM2112 is a high-performance water splitter. The data presented in Fig. 2(c) and (d) were measured in a stagnation flow reactor dedicated to screening STCH materials.^{16,17} During dry redox cycling with O_2 (Fig. 2(c)) the material is continuously exposed to ≈ 2000 ppm O_2 while heating from a base temperature of 1123 K to 1623 K. During heating (*i.e.*, thermal reduction) the material evolves molecular oxygen as V_{O} s form in the crystal lattice, hence the positive rate of O_2 production. Upon cooling to 1123 K, the material uptakes an equivalent amount of O_2 from its surroundings as the V_{O} s are refilled, hence the negative rate of production. CCTM2112 is also redox active under the more stringent thermodynamic conditions of water splitting, as evidenced in Fig. 2(d). Here the sample is exposed to a high purity Ar sweep gas during thermal reduction followed by exposure to a mixture of 40 vol% H_2O in Ar. As with O_2 redox, molecular oxygen is produced by thermal reduction. However, in the water splitting case, O atoms stripped from H_2O fill V_{O} s such that H_2 evolves in the presence of steam. Finally, when reduced a second and third time (after steam re-oxidation), an equivalent amount of O_2 evolves from the material at levels indicative of the first cycle. The δ calculated from the oxygen reduction in the flow reactor is $\delta = 0.06$, with the cycling $\Delta\delta = 0.05$. Due to different operating regimes, this δ for the flow reactor is approximately twice that of the soft XAS ($\delta = 0.033$, *vide infra*) and four times the modeling conditions (one vacancy per 360 atom structure or $\delta = 0.014$, *vide supra*). The data in Fig. 2(d) demonstrates that CCTM2112 is reversibly redox active (for several cycles) in both O_2 and H_2O . Furthermore, the absolute amount of O_2 and H_2 produced during 40 vol% steam cycling (area under blue curve = 10.4 mmol H_2 per mol atom CCTM2112) exceeds that of other high-performing perovskite compounds such as $\text{BaCe}_{0.25}\text{Mn}_{0.75}\text{O}_3$ (7.3 mmol H_2 per mol atom BCM) and $\text{Sr}_{0.4}\text{La}_{0.6}\text{Mn}_{0.6}\text{Al}_{0.4}\text{O}_3$ (8.2 mmol H_2 per mol atom SLMA), and CeO_2 (2.9 mmol H_2 per mol atom CeO_2) under similar experimental conditions (see Section S5 in the ESI† for the calculation of the H_2 produced by these perovskite compounds). Note that CeO_2 does poorly under these conditions, *e.g.*, compared with thermal reduction at ≈ 1800 K.⁸ In future work, we will pursue a more thorough comparison between all of these materials in the context of “high conversion,” which is re-oxidation in a less oxidizing environment, such as 1:1000 H_2 : H_2O in the oxidizing stream. Normalizing to mole atom (see ESI† Section S5 for definition) makes these comparisons possible, without biasing one material over another.

Role of Ce^{4+} in redox activity

We aim to develop a mechanistic understanding of the high performance of CCTM2112 compared to the structurally related CTM and the Ce- and Mn-containing BCM perovskite water splitters. We therefore calculated and analyzed atomic magnetic

moments (μ), which are extremely sensitive measures of oxidation- and spin-state changes. For fully oxidized CCTM2112, the mean magnetic moments in Table 1 imply that, rounded to the nearest integer, the average oxidation states of Ca, Ce, Ti, Mn, and O are 2+, 4+, 4+, 3+, and 2−, respectively, which leads to a charge neutral formula unit (see Fig. S4 in the ESI† for the μ distributions). That said, Ce also can exist as Ce^{3+} and Mn as Mn^{4+} and Mn^{2+} (see min/max values in Table 1), where the latter suggests that disproportionation of two Mn^{3+} may occur in pristine CCTM2112.

To gain greater insight into the nature of the electronic reorganization in CCTM2112 upon V_{O} formation in the thermal reduction step of STCH, we computed the V_{O} -induced changes in the absolute values of μ_{Ce} , μ_{Mn} , and μ_{O} (use of absolute values controls for changes in relative orientation, *i.e.*, ferromagnetic or antiferromagnetic; see Fig. S5 in the ESI† for a similar analysis of μ_{Ca} and μ_{Ti}). We then sum these $|\mu|$ changes separately for Ce, Mn, and O to quantify the extent to which the A, B, and O sub-lattices, respectively, are reduced (positive value) or oxidized (negative value) since changes in μ roughly correspond to changes in oxidation states, excluding Ca and Ti because we observe no more than marginal spin changes on these sites. Thus, the quantification of number of electrons added/removed from a species comes from our calculated changes in $|\mu|$. For example, when $x_{\text{Ce}} = 0$ and the change in $|\mu_{\text{Ce}}| \neq 0$, a V_{O} without a NN Ce has reduced a non-NN Ce, thus resulting in nonlocal or delocalized reduction.

Our results show that reduction occurs primarily on the A-site Ce sub-lattice (Fig. 3(a)) compared with that of Mn (Fig. 3(b)) and O (Fig. 3(c)), regardless of the V_{O} 's NNs. In particular, the Ce sub-lattice reduces by 0.75 to 2.23 electrons depending on x_{Ce} and x_{Mn} , corresponding to an average decrease in Ce oxidation state of 0.031 to 0.093 e, respectively (average reduction of the 24 Ce in the unit cell); whereas, for Mn, no obvious net reduction or oxidation occurs during the formation of the V_{O} , with both mild reduction (≤ 0.35 electrons accepted) and oxidation (≤ 0.42 electrons donated) of Mn occurring simultaneously (see Table S7 in the ESI† for a qualitative analysis of Ce and Mn oxidation state changes upon neutral V_{O} formation). During V_{O} formation, the remaining O sub-lattice experiences weak-to-mild reduction (≤ 0.52 electrons accepted in total by the O sub-lattice containing 216 atoms in the unit cell), reminiscent of the V_{O} -induced delocalized reduction of the O sub-lattice in the $\text{Sr}_2\text{Fe}_{2-x}\text{Mo}_x\text{O}_6$ double perovskites reported by Muñoz-García *et al.*³⁷ The reduction of the O sub-lattice is indicative of empty O states in the pristine material,

Table 1 Magnetic moment summary statistics for fully oxidized CCTM2112. σ is the first standard deviation. All values are in μ_{B} . Fig. S4 in the ESI shows the magnetic moment distributions

Element	Mean $\pm \sigma$	Minimum	Maximum
Ca	0.00 $\pm$ 0.00 (Ca^{2+})	0.00 (Ca^{2+})	0.00 (Ca^{2+})
Ce	0.28 $\pm$ 0.23 (Ce^{4+})	0.06 (Ce^{4+})	0.68 (Ce^{3+})
Ti	0.05 $\pm$ 0.02 (Ti^{4+})	0.03 (Ti^{4+})	0.08 (Ti^{4+})
Mn	3.77 $\pm$ 0.24 (Mn^{3+})	3.10 (Mn^{4+})	4.50 (Mn^{2+})
O	0.01 $\pm$ 0.01 (O^{2-})	0.00 (O^{2-})	0.05 (O^{2-})

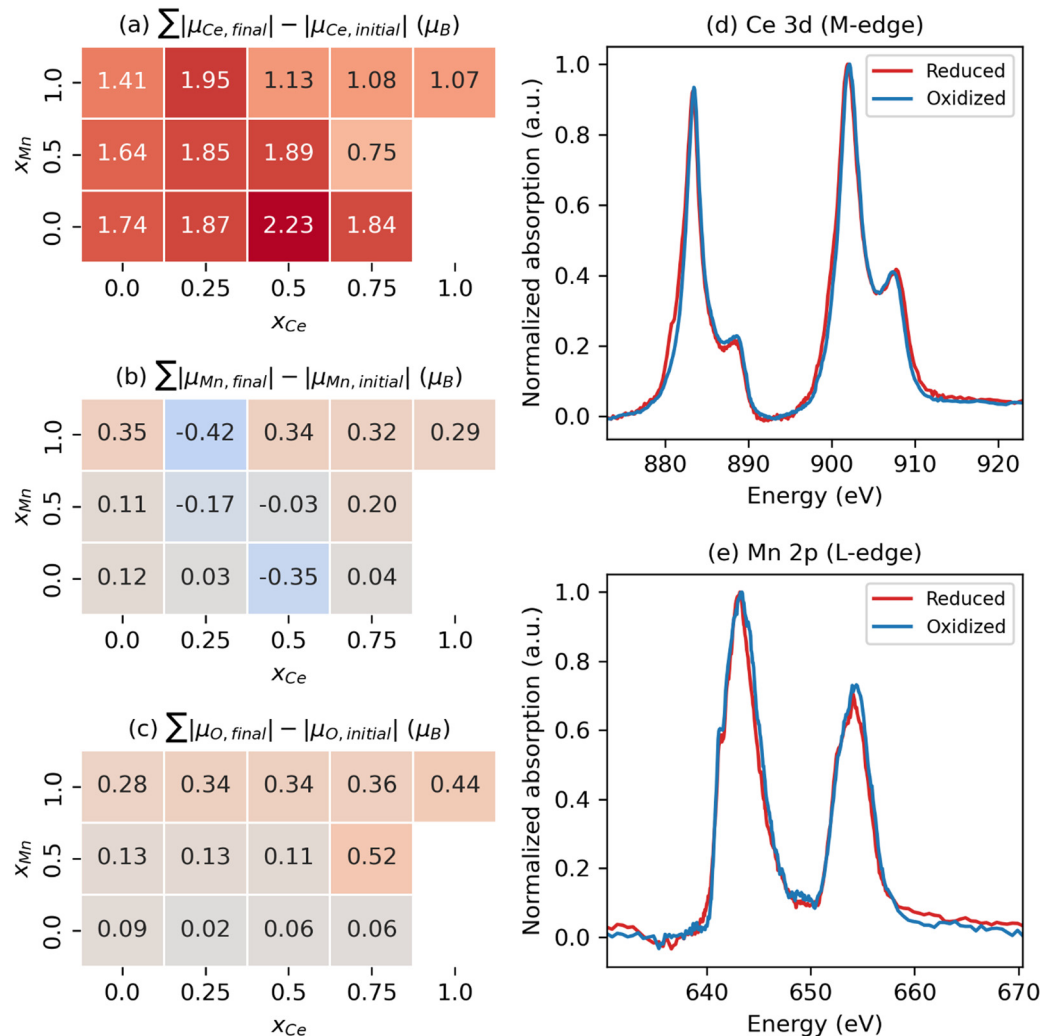


Fig. 3 Multiple cation redox in CCTM2112. Dependence of V_O -induced absolute magnetic moment ($|\mu|$) changes for the (a) Ce, (b) Mn, and (c) O sub-lattices on the V_O 's NN environment, where the mole fractions, x , refer just to the NN environment. Note that we sum these $|\mu|$ changes separately for Ce, Mn, and O to quantify the extent to which the A, B, and O sub-lattices, respectively, are reduced (positive value) or oxidized (negative value) since μ changes roughly correspond to fractional oxidation state changes, reserving Ca and Ti for Fig. S5 in the ESI† because we observe marginal spin changes on these sites. XAS spectra at the (d) Ce 3d_{5/2} and (e) Mn 2p_{3/2} edge for reduced CCTM2112 and re-oxidized CCTM2112 (see Fig. S8 in the ESI† for the complete spectra).

indicating that the Os are not fully ionized as O^{2-} (as seen by Bader charge analysis), with instead the M–O bonds exhibiting some singlet-coupled covalent character, which spin-averages the electrons on O to appear nonmagnetic.

X-ray absorption (XAS) synchrotron studies provide validating evidence supporting the predicted changes in average Ce and Mn oxidation states indeed occur during reduction of CCTM2112. We confirmed that, for oxidized CCTM2112 ($\delta \approx 0$), the predominant oxidation states of Mn and Ce are Mn^{3+} and Ce^{4+} by comparing the XAS spectrum of oxidized CCTM2112 (Fig. 3(d) and (e)) to standards. CCTM2112 was repeatedly reduced ($p_{O_2} \approx 1 \times 10^{-5}$ bar) and re-oxidized ($p_{O_2} \approx 0.2$ bar) in dry redox cycling conditions at 1473 K with 16 hours at each condition. CCTM2112 samples after both the third reduction and third re-oxidation were characterized. XRD confirms both the reduced and re-oxidized sample retained the CCTM structure with negligible secondary

phase formation (Fig. S6, ESI†). Mass change in the sample between re-oxidizing and reducing conditions is consistent with a $\Delta\delta = 0.033 \pm 0.003$, with near full oxidation of the re-oxidized sample ($\delta \approx 0$) giving the reduced sample $\delta = 0.033 \pm 0.003$. In comparison, the one V_O out of 216 oxygen sites modeled here (Fig. 2) corresponds to $\delta = 0.014$, conditions that are roughly half of the empirical reduction but still sufficiently close for comparing modeling results to observational data.

Soft XAS experiments at the Ce M-edge (*i.e.*, X-ray-induced electron transitions from 3d to 4f orbitals) and Mn L-edge (electron transitions from 2p to 3d orbitals) were used to identify cation-specific changes in oxidation state. Increases in oxidation state result in less electron shielding of the atomic nucleus. Hence, more energy is required to excite a core electron, moving the spectrum edge position to higher energy. Ce and Mn oxidation states were benchmarked against known

standards: CeO_2 for Ce^{4+} , CeAlO_3 for Ce^{3+} , MnO_2 for Mn^{4+} , Mn_2O_3 for Mn^{3+} , and MnO for Mn^{2+} . The soft XAS results for the Ce M-edge (see Fig. 3(d)) demonstrate reversible reduction of Ce (shift in edge positions at approximately 881 eV and 900 eV to lower energy upon reduction) to a fractional oxidation state of $\approx 3.90 \pm 0.03$, determined from a linear combination fit of the re-oxidized and reduced CCTM with the Ce^{4+} and Ce^{3+} standards (see Fig. S7 and S8 in the ESI†). This measured 1.1% decrease in the average Ce oxidation state $[(4 - 3.9)/4 = 2.5\% \text{ for } \delta = 0.033, \approx 2.5 \times 0.014/0.033 = 1.1\% \text{ for } \delta = 0.014]$ agrees well with the 0.8% decrease predicted by SCAN+*U* calculations $[(\langle q_{\text{ox}} \rangle - \langle q_{\text{red}} \rangle)/\langle q_{\text{ox}} \rangle = [3.72 - 3.69]/3.72 = 0.8\% \text{ for } \delta = 0.014]$, where $\langle q \rangle$ is the ensemble-averaged Ce oxidation state). Additionally, the Mn L-edge (see Fig. 3(e)) demonstrates no observable shift in edge positions (at approximately 641 eV and 652 eV), but does have evidence of Mn^{2+} oxidation to Mn^{3+} and Mn^{4+} reduction to Mn^{3+} (loss in intensity at the lower energy shoulder and higher energy side of the spectrum), supporting model predictions that simultaneous Mn oxidation and reduction occurs with modest net change in Mn oxidation state compared with that of Ce (see smaller values with positive and negative signs for Mn in Fig. 3(b) compared with larger positive values for Ce in Fig. 3(a)).

Discussion

Nonlocal Ce reduction

Surprisingly, we predict that Ce reduces even when it does not neighbor the V_O (see ≥ 1.41 electron reduction of the Ce sub-lattice for $x_{\text{Ce}} = 0$ in Fig. 3(a)). To explore this phenomenon further, we study the spatial dependence of the $|\mu|$ changes induced by a V_O with a Ca- and Mn-rich local environment (*i.e.*, $x_{\text{Ce}} = 0$ and $x_{\text{Mn}} = 1$). Fig. 4(a) shows that two Ce reduce, labeled α ($\Delta|\mu| = 0.44 \mu_\text{B}$) and β ($0.53 \mu_\text{B}$), at distances of 4.32 Å (for α) and 7.04 Å (for β) from the V_O . Note that Ca and Ti are not redox

active and only a few O are slightly reduced or become more ionic, mostly at distances of < 5 Å from the V_O , which accounts for the non-zero value in Fig. 3(c) for $x_{\text{Ce}} = 0$ and $x_{\text{Mn}} = 1$. Additionally, the Mn sub-lattice is both reduced and – to a slightly lesser extent – oxidized, leading to a net mild reduction of 0.35 electrons, corresponding to a disproportionation. Given the changes for Mn are modest, experimental validation is non-trivial. Ce reduction-at-a-distance also can be seen in Fig. 4(b), which displays the difference between the electron density (ρ) of CCTM2112 with and without (*i.e.*, in its pristine state) this same neutral V_O ($\Delta\rho = \rho_{\text{vacancy}} - \rho_{\text{pristine}}$), as yellow isosurfaces (indicating electron gain) emerging from and surrounding the two green Ce labeled α and β , respectively. There are a lot of cyan isosurfaces as well, which implies, in the cases where $\Delta\rho$ is p-like polarization rather than charge accumulation or depletion at those sites. This nonlocal reduction allows a substantial fraction of the Ce present in the material to participate in oxygen vacancy formation, and partially explains the high extent of Ce reduction in CCTM2112.

Having explored the spatial dependence of V_O -induced reduction, we now are able to explain the subtle x_{Ce} dependence of E_v at $x_{\text{Mn}} = 0$. The E_v for $x_{\text{Ce}} = 0$ (*i.e.*, 4.25 eV) is the second highest value in Fig. 2(b), which we attribute to the localized reduction of Ce ($\approx$ two Ce reduced in Fig. S9 of the ESI†), and the electrostatic penalty associated with its distance (4.67–4.83 Å) from the holes localized on the V_O (see, *e.g.*, Fig. 4(b)). For $x_{\text{Ce}} = 0.25$, the $E_\text{v} \approx 3.58$ eV (Fig. 2(b)) is anomalously low because, while the reduction of Ce remains fairly localized (two Ce reduced at distances < 5 Å to the V_O , Fig. S9, ESI†), these electrons are closer to the V_O -generated holes and therefore electrostatically stabilize the V_O . Note that strain can have an indirect effect on E_v by inducing or relaxing Jahn–Teller distortions on Mn but the strain effect is difficult to quantify.

Interestingly, E_v reaches its highest value for $x_{\text{Ce}} = 0.5$ (*i.e.*, 4.35 eV; Fig. 2(b)), which we propose is the sum of (1) an electrostatic penalty for delocalized reduction of Ce (four Ce

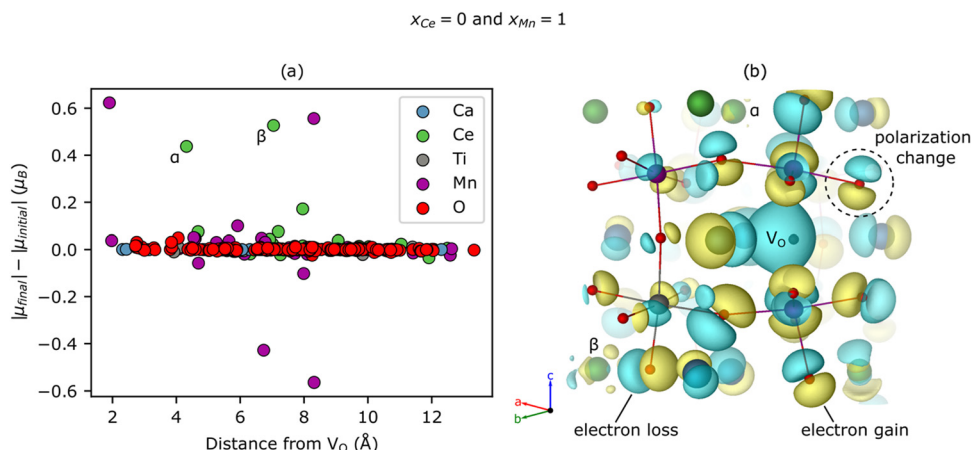


Fig. 4 Nonlocal Ce reduction in CCTM2112 upon formation of a V_O in a Ca- and Mn-rich local environment ($x_{\text{Ce}} = 0$ and $x_{\text{Mn}} = 1$). (a) V_O -induced magnetic moment changes vs. distance, with two Ce (α and β) highlighted. (b) Electron density difference upon V_O formation, $\Delta\rho = \rho_{\text{vacancy}} - \rho_{\text{pristine}}$, where ρ_{vacancy} and ρ_{pristine} are the electron densities of CCTM2112 with and without the V_O . Isosurfaces correspond to a $\Delta\rho$ value of $0.06 \text{ e } \text{\AA}^{-3}$, with yellow and cyan isosurfaces corresponding to regions of electron gain and loss, respectively.

reduced by >0.27 electrons at distances of $2.36 \text{ \AA}$ to $9.48 \text{ \AA}$ from the V_O , Fig. S9, ESI†) and the delocalized electrons' resultant screening of electron-hole interactions and (2) a penalty for oxidizing the Mn ($|\Delta\mu| = -0.55 \mu_B$) at a distance of $10.01 \text{ \AA}$ from the V_O . Finally, from $x_{Ce} = 0.5$ to $x_{Ce} = 0.75$, E_v decreases from 4.35 eV to 4.07 eV (Fig. 2(b)), which – considering the latter's fairly delocalized reduction of Ce (Fig. S9, ESI†) – seems to derive from the absence of oxidized Mn (*i.e.*, Mn for which $|\Delta\mu| < 0 \mu_B$). Therefore, we can explain the subtle x_{Ce} dependence of E_v at $x_{Mn} = 0$ by the nature (localized/delocalized) and location of V_O -generated charge carriers interacting electrostatically with the V_O .

What properties promote the high extent of Ce reduction?

Lastly, it is worth discussing an interesting question that our results provoke: why does Ce^{4+} function as the primary acceptor of electrons (Fig. 3(a)) if it is less reducible than Mn^{4+} and Mn^{3+} ? To quantify the reducibility of Ce^{4+} , Mn^{4+} , and Mn^{3+} , we calculate the enthalpy changes of the following solid-state reduction reactions: $CeO_2 \rightarrow 0.5 Ce_2O_3 + 0.25 O_2$, $MnO_2 \rightarrow 0.5 Mn_2O_3 + 0.25 O_2$, and $0.5 Mn_2O_3 \rightarrow MnO + 0.25 O_2$, respectively. Mn^{4+} is the most reducible cation ($\Delta H = 0.40 \text{ eV}$) followed by Mn^{3+} ($\Delta H = 1.02 \text{ eV}$) and then Ce^{4+} ($\Delta H = 1.82 \text{ eV}$). Additionally, since these reactions are normalized per one-electron reduction, their ΔH s are effectively crystal reduction potentials (V_r), which are a key factor governing E_v in ternary oxide perovskites.³⁶ While this simple analysis suggests that Ce should not reduce, the unoccupied states closest to the Fermi level in metallic CCTM2112 are Ce 4f states (see Fig. S10 in the ESI†). Therefore, even though Ce^{4+} is less reducible than Mn^{4+} and Mn^{3+} in their ground-state binary oxides, Ce does reduce in CCTM2112 because there is a lower energy penalty for the structure to put the V_O -donated electrons in the Ce 4f states, even if the Ce atom is physically farther from the V_O . Ce^{4+} reduction is also accompanied by delocalization of electrons (due to the degeneracy of 4f states contributed by several Ce atoms close to the Fermi level), while Mn reduction is almost always local, evidenced by the presence or absence of Jahn–Teller distortions associated with Mn^{3+} . The need for 4f states near the Fermi level to reduce Ce^{4+} in the presence of Mn^{3+} is consistent with the observation that Mn and not Ce reduces during thermochemical cycling of $Ba(Ce,Mn)O_3$ (BCM) perovskites (where Ba is on the A-site, and Ce and Mn occupy the B-site)¹⁷ because BCM has a band gap and thus V_O -induced reduction is driven by cation proximity and reducibility rather than the relative location of unoccupied states near the Fermi level. Thus, the density of states for CCTM2112 promotes Ce reduction, revealing a mechanism that quantum-based modeling can target to predict other formulations of Ca–Ce–Ti–Mn–O as well as other materials with enhanced Ce reduction and thus enhanced STCH performance.

The high reducibility of Ce^{4+} in CCTM2112 is both key to its high water-splitting performance and substantially different than the behavior of CeO_2 and other previously demonstrated Ce^{4+} -containing off-stoichiometric redox-active materials. The existence of Ce^{4+} reduction is observed directly in both modeling

and XAS. The most obvious structural distinction of CCTM2112 is the 12-fold coordination of Ce^{4+} on the A-site, compared to the 8-fold coordination of Ce^{4+} in the CeO_2 fluorite structure and 6-fold coordination on the B-site of BCM. As discussed above, the redox activity of Mn on the B-site is less clear, which suggests that other electronically similar elements may be able to substitute on the B-site and enable A-site Ce^{4+} reduction.²⁰ These results further suggest that a heretofore under-investigated family of Ce^{4+} A-site perovskites may exist with comparably high performance, across a range of alternate A-site and B-site elemental substitutions and ratios.

Conclusions

Perovskite $Ca_{2/3}Ce_{1/3}Ti_{1/3}Mn_{2/3}O_3$ (CCTM2112) offers potential to have greater solar thermochemical H_2 (STCH) production capacity than two other high-performing perovskite compounds, specifically $Sr_{0.4}La_{0.6}Mn_{0.6}Al_{0.4}O_3$ (SLMA4664) and $BaCe_{0.25}Mn_{0.75}O_3$ (BCM), and greater than CeO_2 at operating temperatures of 1623.15 K for the thermal reduction step and 1123.15 K for the water-splitting step. Additionally, the more general Ca–Ce–Ti–Mn–O phase space provides possibilities for supplanting CeO_2 -based materials as the preferred redox-active MO_x for STCH. Ce being the dominant acceptor of the electrons left behind by neutral oxygen vacancy formation, unlike other Ce-containing oxide perovskites for STCH like BCM, suggests that refinement of the Ce stoichiometry is a particularly promising avenue for future research. Finally, the electronic-structure-based mechanism that promotes Ce reduction with lower vacancy formation energies than in CeO_2 reveals novel physics and redox-active materials design considerations for realizing the climate-change-mitigation potential of STCH. As such, this work does not just introduce one high-performing material but instead uses the modeling-driven and experimentally verified discovery of a new water splitter with a distinct mechanism of action to introduce a new family of water-splitting materials.

Experimental details

Synchrotron powder X-ray diffraction data were acquired at the Stanford Synchrotron Radiation Lightsource (SSRL), beam line 2-1. The incident X-ray wavelength used was $0.730 \text{ \AA}$ as determined by a refinement of data from a NIST 660C LaB_6 diffraction standard. CCTM powders were prepared in 0.028 inch outer diameter Kapton capillaries with 0.002 inch wall thickness and rotated (≈ 1 rotation per second) during data acquisition. 2D diffraction images were obtained with a Pilatus 100 K hybrid photon counting detector, and subsequently integrated into a 1D pattern using a python script developed at SSRL for beam line 2-1. The diffraction pattern used to compare the experimental XRD data to the DFT model was simulated from the “CCTM2112” model, subjected to the ADDSYM routine within PLATON.³⁸ The XRD data was indexed using NTREOR, contained

within the EXPO2014³⁹ suite of crystallographic tools. Rietveld refinements were performed using GSAS-II.³³

X-Ray absorption spectroscopy data was acquired at SSRL, beam line 10-1. For analysis of each sample, a thin layer of CCTM powder was spread on carbon tape. Total fluorescence yield spectra were obtained with a silicon diode AXUV100 detector at the Ce 3d and Mn 2p edges. A Mn reference spectrum was collected simultaneously with data collection at the Mn edge for all samples. Specific to this beamline, an agglomerate of chemical species resides permanently within the beam path for reference collection. The reference material does not contain Ce, so no Ce reference was available. However, the Mn references collected throughout the experiment well align ensuring the monochromator was stable and data could be directly compared. Data was analyzed with Igor Pro (Wave-metrics, Lake Oswego, Oregon, USA). For each spectrum, the average value of the pre-edge region is subtracted, and the spectrum normalized to the Mn 2p_{3/2} or Ce 3d_{5/2}. Powder CCTM2112 samples were redox cycled in a laser-heated stagnation flow reactor.^{16,17} Approximately 100 mg of sample is placed in a shallow, loosely packed bed within the stagnation plane of the reactor flow field such that transport of gaseous species to and from the sample surface is governed by 1-D diffusion. The reactor operates at 75 Torr and the sample environment (*i.e.*, gas flow rate, gas composition, temperature, pressure) is fully controlled using appropriate hardware and software. The gas composition in the reactor effluent is measured by mass spectrometry at a rate ~ 4 Hz, which is important because the re-oxidation and reduction chemistries are inherently transient. Since the reactor flow field is well behaved, physical processes such as gas-phase dispersion, reactant mixing, and detector time lag that normally confound the extraction of material-specific behavior from the as-measured transient signal are easily resolved using numerical methods. One unique feature of the experimental system is the use of a 500 W, continuous-wave, near-IR laser to rapidly heat the material during thermal reduction. This heating method mimics the radiative environment encountered in an ultra-high temperature concentrating solar receiver and allows exploration of the effects of rapid thermal cycling, such as crystallographic and morphological instabilities, on macroscopic water splitting behavior.

Conflicts of interest

There are no conflicts to declare.

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