PCCP

PAPER



Cite this: Phys. Chem. Chem. Phys., 2022, 24, 5842

Received 2nd December 2021, Accepted 14th February 2022

DOI: 10.1039/d1cp05499f

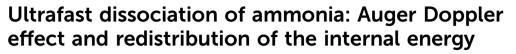
rsc.li/pccp

1 Introduction

Absorption of an X-ray photon by a molecule may lead to the excitation of a localized core electron to a specific unoccupied valence orbital. The created core–hole states are highly unstable and decay on a very short timescale emitting a photon (radiative

^a Sorbonne Université, CNRS, UMR 7614, Laboratoire de Chimie Physique-Matière et Rayonnement, F-75005 Paris, France.

- E-mail: oksana.travnikova@sorbonne-universite.fr
- ^b Department of Physics and Astronomy, University of Turku, FI-20014 Turku, Finland
- ^c Synchrotron SOLEIL, L'Orme des Merisiers, Saint-Aubin,
- F-91192 Gif-sur-Yvette Cedex, France
- ^d Fachbereich Physik, Freie Universität Berlin, D-14195 Berlin, Germany
- ^e Department of Theoretical Chemistry and Biology, KTH Royal Institute of Technology, 10691 Stockholm, Sweden
- ^f International Research Center of Spectroscopy and Quantum Chemistry IRC SQC, Siberian Federal University, 660041 Krasnoyarsk, Russia
- ^g Institute for Methods and Instrumentation in Synchrotron Radiation Research FG-ISRR, Helmholtz-Zentrum Berlin für Materialien und Energie, Albert-Einstein-Strasse 15, 12489 Berlin, Germany
- ^h Department of Physics and Astronomy, Uppsala University, SE-751 20 Uppsala, Sweden
- † Present address: Top Analytica, Ruukinkatu 4, FI-20540, Turku Finland.



Oksana Travnikova, 🝺 *^a Edwin Kukk,^b Farzad Hosseini, 🗓 ^{ac} Sari Granroth,^b Eero Itälä,†^b Tatiana Marchenko, 🗇 ^a Renaud Guillemin, 🗇 ^a Iyas Ismail, 🗇 ^a Roba Moussaoui,^a Loïc Journel, 🝺 ^a John Bozek,^b Ralph Püttner, խ ^d Pavel Krasnov, 🗇 ^{ef} Victor Kimberg, 🗇 ^{ef} Faris Gel'mukhanov, 🗇 ^{efg} Maria Novella Piancastelli 🗇 ^{ah} and Marc Simon 🗇 ^a

We study vibrationally-resolved resonant Auger (RAS) spectra of ammonia recorded in coincidence with the NH_2^+ fragment, which is produced in the course of dissociation either in the core-excited $1s^{-1}4a_1^1$ intermediate state or the first spectator $3a^{-2}4a_1^1$ final state. Correlation of the NH_2^+ ion flight times with electron kinetic energies allows directly observing the Auger-Doppler dispersion for each vibrational state of the fragment. The median distribution of the kinetic energy release E_{KER} , derived from the coincidence data, shows three distinct branches as a function of Auger electron kinetic energy E_e : $E_e + 1.75E_{KER} = \text{const}$ for the molecular band; $E_{KER} = \text{const}$ for the fragment band; and $E_e + E_{KER} =$ const for the region preceding the fragment band. The deviation of the molecular band dispersion from $E_e + E_{KER} = \text{const}$ is attributed to the redistribution of the available energy to the dissociation energy and excitation of the internal degrees of freedom in the molecular fragment. We found that for each vibrational line the dispersive behavior of E_{KER} vs. E_e is very sensitive to the instrumental uncertainty in the determination of E_{KER} causing the competition between the Raman ($E_{KER} + E_e = \text{const}$) and Auger ($E_e = \text{const}$) dispersions: increase in the broadening of the finite kinetic energy release resolution leads to a change of the dispersion from the Raman to the Auger one.

decay) or a so-called Auger electron (non-radiative or Auger decay). Core excitation of molecules by soft X-rays creates core holes with lifetimes of a few femtoseconds (typically, 3–8 fs), which is a sufficient duration for light nuclei to move away from their equilibrium geometry. This results in a competition between two dynamical processes: electronic relaxation of the excited system and its nuclear dynamics. Ultrafast dissociation (UFD) is an extreme example of such a competition, where electronic decay occurs after dissociation. UFD was observed for the first time for CS_2 and SF_6 molecules in 1978¹ and HBr in 1986.²

More complete information on molecular dynamics is obtained by performing electron-ion coincidence measurements, where the correlation of emitted electrons with ionic fragments allows disentangling dissociation mechanisms.^{3–9}

Furthermore, the so-called Auger–Doppler (AD) effect¹⁰ has been observed for the spectral lines pertaining to the atomic fragments formed after UFD for O_2 ,^{9,11–13} CH₃Cl,³ SF₆,^{14,15} O₃,¹⁶ HF/DF.¹⁷ The AD effect is the red/blue shift of kinetic energies for Auger electrons emitted from the fragments moving away/towards the detector, respectively. At the same time, an opposite shift can be observed for the corresponding ionic fragments, which are typically measured by an ion time-of-flight spectrometer facing an electron analyzer in a coincidence setup.^{5,9}



View Article Online

The maximum of the Doppler shift \mathcal{D}_{\max} can be described by a simple model:

$$\mathscr{D}_{\rm max} = 4\sqrt{E_{\rm e}E_{\rm KER}\mu m_{\rm e}}/m_{\rm A}$$

where E_{e} is the kinetic energy of the emitted Auger electrons, E_{KER} - the kinetic energy release, μ - the reduced mass of the system, $m_{\rm e}$ – the electron mass and $m_{\rm A}$ – the mass of the core-excited fragment, i.e. the Auger-electron emitter. For co-fragments with comparable atomic masses the AD shift can be sufficiently large to be observed for dissociative resonances by single-channel electron spectroscopy (for example, $\mathscr{D}_{\text{max}} \sim 0.5 \text{ eV for O}_2^{9,11}$). However, in heteroatomic molecules the Doppler shift will be small for the heavy fragment because the released kinetic energy is transferred mainly to the light co-fragment. In the latter case, the Doppler effect could be observed as broadening of the fragment lines. Advanced spectroscopic techniques allow simultaneous detection of energyresolved fast Auger electrons and ions in coincidence for each ionisation event. In such measurements, ions travelling in the opposite directions after dissociation can be distinguished and correlated to the kinetic energies of electrons emitted from them, which allows observation of small Auger-Doppler splittings, indiscernible by single-channel electron spectroscopy.³

In this work we demonstrate the first observation of the AD effect for a molecular fragment produced by UFD with a light co-fragment. In contrast to the previously studied AD effect for atomic fragments, electronic decay of molecular fragments is usually accompanied by vibrational excitations. Therefore, high kinetic energy resolution is required for such measurements. Using the newly available GPES (Gas-Phase End Station) coincidence setup,¹⁸ equipped with a high-resolution hemispherical electron analyser and permanently installed at the soft X-ray beamline FinEstBeAMS of the MAX IV synchrotron radiation facility in Sweden, we recorded resonant Auger decay spectra at the N 1s edge ($\sim 400 \text{ eV}$) for the NH₃ molecule in the gas phase following core excitation to the dissociative lowest unoccupied molecular orbital (LUMO, 4a₁) in coincidence with ions.

The core-excited $1s^{-1}4a_1^1$ state of NH₃ undergoes UFD on a few femtosecond (fs) timescale (N 1s lifetime $\tau = 5$ fs) leading to the ejection of a neutral hydrogen atom and a core-excited neutral NH₂^{*} co-fragment (eqn (1)), which relaxes by Auger decay, leading predominantly to the singly charged NH₂⁺ ion.

$$\begin{split} \mathbf{N}\mathbf{H}_{3} &+ \hbar \omega \rightarrow \mathbf{N}\mathbf{H}_{3}^{*}[\mathbf{1s}^{-1}\mathbf{4a_{1}}^{1}] \rightarrow \\ \begin{cases} \mathbf{N}\mathbf{H}_{3}^{+} + \mathbf{e}_{\mathrm{Auger}}^{-} & (\mathbf{1}) \\ \mathbf{H} + \mathbf{N}\mathbf{H}_{2}^{*} &\rightarrow \mathbf{H} + \mathbf{N}\mathbf{H}_{2}^{+} + \mathbf{e}_{\mathrm{Auger}}^{-}. \end{cases} \end{split}$$

Evidence of UFD in gas-phase ammonia molecules was first observed by resonant Auger electron spectroscopy in 2003 by Hjelte *et al.*¹⁹ as a series of peaks separated by ~390 meV, corresponding to the vibrational progression of the \tilde{a}^+ state of the NH₂⁺ ion. These lines stay constant at the kinetic energy of about 382 eV when the photon energy is tuned across the $1s^{-1}4a_1^1$ resonance, while the participator Auger-decay lines originating from the undissociated ammonia molecules

disperse linearly owing to the energy conservation law. This is explained in the previous works by the resonant Auger decay in the fragment taking place when the wave packet reaches a location on the potential energy surface where the curves for the intermediate and final states are parallel, and the residual energy goes to the nuclear motion.

Using GPES coincidence setup we achieved electron kinetic energy resolution, which is comparable to the single-channel resonant Auger spectroscopy measurements reported in ref. 19 allowing vibrational resolution for the a^+ state of the NH_2^+ ion. The AD shift, experimentally observed in our work, for the heavy counter-ion after N–H bond fission in the core-excited ammonia is comparable to the intrinsic N 1s core–hole lifetime broadening (~130 meV) and, therefore, cannot be resolved in single-channel photoemission spectroscopy.

Furthermore, we show that the measured kinetic energy release gives direct information about the redistribution of the internal energy left in the system among different vibrational and rotational modes. In the previous studies concerning ultrafast dissociation leading to an atomic fragment, E_{KER} follows linearly the photon energy across the resonance with the slope of 1, *i.e.* the total energy left in the system after resonant Auger decay is transferred to the kinetic energy of the atomic fragment.^{5,9} However, in the case of molecular fragments possessing several vibrational degrees of freedom, there are more ways to dissipate the internal energy as well as to excite recoil-induced vibrations and rotations.²⁰ Dispersion of the E_{KER} with the electron energy, extracted from the experimental data for the NH₂⁺-H dissociation channel, shows that about 43% of the internal energy remaining in the system after emission of the resonant Auger electron is transferred to vibrations, while recoil-induced rovibronic excitations are weak owing to the relatively high mass ratio of the co-fragments $(m_{\rm NH_*}/m_{\rm H} = 16:1).$

2 Experiment

2.1 Resonant Auger electron-ion coincidence measurements

The experiment was performed at the Estonian-Finnish beamline (FinEstBeAMS) of the MAX IV synchrotron radiation source in Lund, Sweden. The beamline²¹ is equipped with a SX700 type monochromator manufactured by FMB Feinwerk-und Messtechnik GmbH, receiving radiation from an Apple II type undulator. Horizontally polarized radiation was used in this experiment. Ammonia sample (99 999% purity) was introduced into the Gas-phase Endstation (GPES)¹⁸ through a needle via a dosing valve, to the experimental chamber (pressure of $4-5 \times$ 10^{-6} mbar). The molecular jet from the needle crossed the monochromatized photon beam at the centre of the sample region (Fig. 1), and photoelectrons were detected by a modified Scienta R4000 hemispherical electron analyzer, equipped with a fast 40 mm diameter microchannel plate (MCP) and a resistive anode (Quantar Inc.) position-sensitive detector. The electron detector provided triggers for the pulsed ion extraction voltage Us across the source region of a modified Wiley-McLaren

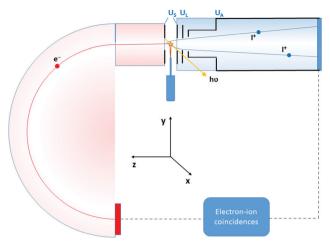


Fig. 1 Schematics of the electron-ion coincidence experiment at the Gas-phase Endstation (GPES).

type ion time-of-flight (TOF) spectrometer.¹⁸ The ions were then accelerated to the final energy by the drift tube voltage U_A , first passing a lens element with U_L , modifying the radial distribution and focusing. Ions were detected by a Roentdek 80 mm MCP and HEX-anode detector, recording ion flight times (TOFs) and radial hit positions. The electron energy and ion TOFs and ion positions of impact data were combined into a coincidence dataset. In addition, non-coincident "random" triggers for ion extraction were generated at a constant rate, interleaved with the electron triggers. The ions collected using the random triggers were added to the dataset and were used in the analysis for statistical subtraction of the false coincidence background from the electron–ion coincidence (PEPICO) maps, ion momentum and the E_{KER} distributions.

The electron energy window for a coincidence dataset is determined by the electron acceleration/retardation and the pass energy E_p of the analyzer, its width being about 8% of E_p . For different electron energy resolution/energy coverage optimization, data with $E_p = 50$, 100 and 200 eV were recorded, with the entrance slit of the spectrometer at 0.8 mm (for $E_p = 50$ and 100 eV) and 1.5 mm (for $E_p = 200$ eV), giving the estimated electron energy resolution of 160, 315 and 900 meV full-width at half-maximum (FWHM), respectively. The exit slit of the monochromator was set to 20–30 µm to give a sufficiently low electron rate of 10–20 el s⁻¹, which corresponded to the estimated photon bandwidth of 60–80 meV FWHM. Two sets of the ion extraction and acceleration voltages ($U_S = \pm 100$ V, $U_A = -620$ V and $U_S = \pm 200$ V, $U_A = -1240$ V) were used, to allow checking for consistency in ion momentum determination.

The resonant features in the N 1s photoabsorption spectrum were determined by measuring total ion yield as a function of photon energy just below the N 1s ionization threshold of NH₃. The spectrum, presented in Fig. 2, shows the first resonant transition N 1s \rightarrow 4a₁ at 400.66 eV (energy-calibrated according to ref. 22), and the strongest 1s \rightarrow 2e resonance at 402.33 eV. The two arrows denote the excitation energies at which the Auger electron–ion coincidence measurements were performed – at the

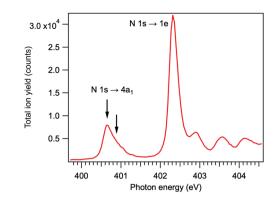


Fig. 2 Total ion yield spectrum of ammonia across the resonant excitations in the N 1s photoabsorption.

maximum of the $1s \rightarrow 4a_1$ resonance and at about +230 meV detuning. The energy for the positive detuning was chosen to be above the barrier which is present on the N $1s^{-1}4a_1$ potential energy surface of NH₃ (170 meV²³).

In the TOF spectrum of ammonia, recorded at the N 1s \rightarrow 4a₁ resonance, only the H⁺ and NH₂⁺ ions are present in coincidence with the resonant Auger electrons, detected in the kinetic energy range of 379–384 eV. Resonant Auger transitions at lower kinetic energies start to produce also the N⁺ and NH⁺ ions.

2.2 High-resolution resonant Auger measurements

Additionally, single-channel high-resolution resonant Auger decay spectra were recorded using a R4000 hemispherical electron analyser from Scienta-Omicron, which is permanently installed at the PLEIADES beamline of the synchrotron SOLEIL in Saint-Aubin, France.¹⁵ NH₃ was introduced to the homebuild gas cell and the pressure in the chamber was kept constant at about $2.5e^{-5}$ bar. A high flux grating containing 600 lines per mm with varied line spacing and varied groove depth was used for the measurements. The monochromator slit was set to 20 µm, which results in a soft X-ray beam with the bandwidth of about 56 meV around the N 1s edge ($\sim 400 \text{ eV}$). The estimated electron energy resolution was 40 meV for the used electron analyser settings (entrance slit 0.8 mm and pass energy 20 eV). The measurements were performed using circularly polarised light, as it delivers the highest flux around 400 eV. The possible drifts in photon energy position were monitored by recording an ion yield spectrum using a Channeltron detector, installed downstream from the electron analyser at the PLEIADES gas-phase end-station. The resonant Auger decay spectrum, presented in Fig. 3 was recorded during the total accumulation time of about 24 hours, at the photon energy of 400.86 eV, corresponding to the detuning of +200 meV from the top of the N 1s \rightarrow 4a₁ resonance. Additional angular resolved measurements were performed using linear vertical and horizontal X-ray light polarisation to observe a difference in the broadening of the fragment lines due to the Auger Doppler effect¹¹ for 0° and 90° polarisation relative to the electron emission axis. The analysis of the last measurements

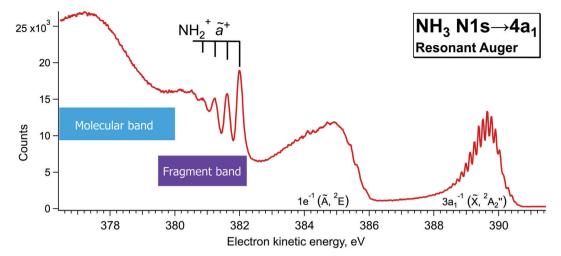


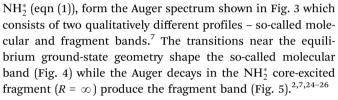
Fig. 3 High-resolution resonant Auger decay spectrum recorded at $\hbar \omega$ = 400.86 eV with hemispherical electron analyser at the beamline PLEIADES of the synchrotron SOLEIL.

confirmed that for the 0° light polarisation there is a small increase in the peak widths of the vibrationally-resolved lines of the NH₂⁺ fragment in the electron kinetic energy region of 381–382 eV.

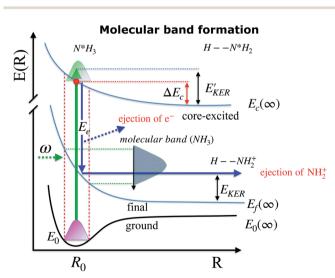
3 General features of resonant Auger spectrum of NH₃

When ammonia is core excited to the dissociative $1s^{-1}4a_1^1$ state it starts to decay to the manifold of the final cationic states emitting the Auger electron with momentum **k** and kinetic energy E_{e} .

The Auger transitions, occurring near the equilibrium geometry of the ground-state ammonia and in the UFD fragment



One can distinguish two qualitatively different spectral regions: the band below 382 eV, related to the first spectator molecular state $(3a_1)^{-2}(4a_1)^1$, see ref. 27; and the kinetic energy region comprising Auger decays to \tilde{X} and \tilde{A} participator final states with valence electron vacancy in the HOMO $(3a_1)$ and HOMO-1 (1e) molecular orbitals of NH₃, respectively. The sharp lines, which are seen in the electron kinetic energy region of $380 < E_e < 382$ eV, correspond to the



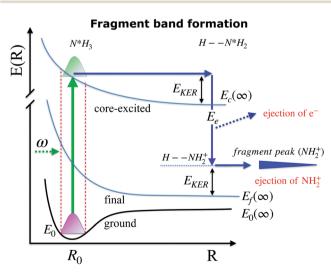


Fig. 4 Schematic depicting potential energy curves of the ground, coreexcited and final states, involved in the resonant Auger decay process. Ejection of the Auger electron near the equilibrium geometry (R_0) leads to the formation of the broad "molecular" band. Dissociation to the NH₂⁺ fragment occurs in the molecular final state NH₃⁺.

Fig. 5 Schematic depicting potential energy curves of the ground, coreexcited and final states, involved in the resonant Auger decay process. Late Auger decays occur at large internuclear distances (R_{∞}), which lead to the formation of the so-called "fragment" band. The narrow fragment line is formed by ejection of the Auger electron in the core-excited dissociated fragment N*H₂.

N–H symmetric stretching vibrations of the \tilde{a}^+ final state $((1a_1)^2(2a_1)^2(1b_2)^2(3a_1)^2)$ of the NH₂⁺ ion reached after Auger decay in the core-excited N*H₂ fragment.¹⁹ The width of the spectral lines constituting this so-called fragment band is defined by the lifetime broadening of the core-excited state Γ and the Auger Doppler broadening. In contrast, the $3a_1^{-1}$ band shows much narrower vibrational lines which correspond to the resonant Auger decays to the final bound state. The widths of the spectral lines in this case are defined by the photon bandpath width and lifetime broadening of the final state Γ_f which is usually much smaller than Γ .^{7,11,24}

In our high-resolution RAS spectrum, recorded with low signal-to-noise ratio (Fig. 3), we can clearly distinguish the NH_2^+ fragment lines up to $\nu = 3$ vibrational component in the 381–382 eV kinetic energy region. In Fig. 3 we can also notice hints of vibrational lines with $\nu > 3$ close to 380 eV. However, their relative intensities indicate that they might originate from a different vibrational progression than the one visible at 381–382 eV; however, attribution of those lines goes beyond the scope of the present paper.

Notably, the spectral resolution allows resolving the bending vibrational progression of the participator X final state for NH₃⁺ ($E_{\rm e} \sim 389-390$ eV), which is below the life-time broadening of $\Gamma \sim 130$ meV for N 1s. This is possible owing to the narrow bandwidth of the exciting X-rays resulting in the so-called Auger Resonant Raman (ARR) conditions, when the finite life-time Γ of the core-excited intermediate state does not contribute to the RAS cross section for molecular Auger decay. The width of the RAS lines is hence defined by the instrumental resolution (photon bandwidth and electron kinetic energy resolution) and lifetime broadening of the final state $\Gamma_{\rm f}$. Contrary, the spectral features of the fragment in Fig. 3 appear considerably broader. The width of the vibrational lines of this so-called fragment band is defined by the lifetime broadening of the core-excited state Γ and the Auger-Doppler broadening. Therefore, the Raman line narrowing below the core-hole lifetime width, which takes place for the molecular band, does not hold for the fragment band.^{24,26} The variation of the line widths can be used as a tool to distinguish molecular and fragment bands in RAS, which allows us confirming the fragment nature of the lines in the 381-382 eV region and removing the doubts in their attribution, raised in the theoretical work by Takahashi et al.27

In addition to the conventional resonant Auger decay spectrum shown in Fig. 3 we measured also the Auger spectra in coincidence with the NH_2^+ cation, which can be formed either following the dissociation in the intermediate neutral coreexcited state N^*H_3 or in the final molecular state NH_3^+ . The information provided by the coincidence experiment is much richer than in conventional single-channel Auger electron measurements, since both the momentum of the Auger electron **k** and the momentum of the cation **p** can be derived. One of the main advantages of the coincidence technique is that we know precisely the orientation in space of the dissociating H_2N-H bond, which is selected by the momentum of the fragment **p**. The photoelectron–photoion coincidence spectrum was measured in a relatively narrow electron kinetic energy

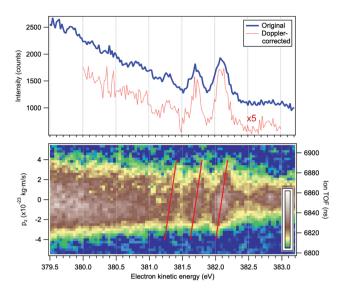


Fig. 6 Top panel: Resonant Auger electron spectrum following the N 1s \rightarrow 4a₁ excitation at the top of the resonance, at $\hbar\omega$ = 400.66 eV. The blue curve corresponds to all detected electrons and the red curve to the electrons detected in coincidence with a single NH₂⁺ ion and corrected for the Doppler energy shift. Bottom panel: Electron–ion coincidence (PEPICO) map of the Auger electrons and the NH₂⁺ ions. The tilted red lines were derived using a purely analytical expression for the Doppler shift (eqn (4)). The vertical scales give the flight times of the ions (right) and the corresponding values p_z of the ion momenta projected on the TOF spectrometer's axis (left).

range of the RAS spectrum and is shown in Fig. 6. The bottom panel of Fig. 6 will be discussed in more detail later in Section 4.1. The blue curve in the top panel of Fig. 6 is a resonant Auger electron spectrum, integrated for the $\rm NH_2^+$ ions, shown in the bottom panel. A series of 3–4 peaks, separated by about 390 meV and attributed to Auger decay in a fragment ion after ultrafast dissociation, can be clearly distinguished. To the best of our knowledge, this is the first vibrationally resolved coincidence measurement for such high electron kinetic energies.

As it will be explained below, knowing the NH_2^+ ion momentum and assuming momentum conservation in the course of the two-body dissociation process, we can obtain the kinetic energy release (E_{KER}) for the $NH_3^+ \rightarrow NH_2^+ + H$ and $NH_2^0 \rightarrow$ NH_2^+ channels, following 1s $\rightarrow 4a_1$ photoexcitation. The kinetic energy release E_{KER} as a function of Auger electron energy E_{e_1} based on the median momentum of the NH_2^+ ions, is presented in Fig. 7.

From Fig. 7 we can note three distinct features of the ion E_{KER} as a function of the kinetic energy of resonant Auger electrons: (1) a monotonous increase of the E_{KER} with the slope of -1.00(9) in the region preceding the fragment band ($E_e > 382 \text{ eV}$); (2) the presence of plateau in the region of the fragment band; and (3) a monotonous increase with the slope of -0.57(1) of E_{KER} with decrease of the Auger electron kinetic energy for the molecular band ($E_e < 380 \text{ eV}$). These different peculiar behaviours of kinetic energy release E_{KER} in the molecular and fragment band regions are discussed in the following Sections 4.2 and 4.3 together with the other new information provided by the coincidence measurements.

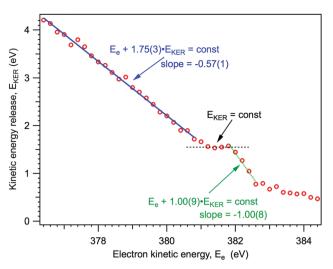


Fig. 7 Kinetic energy release in the dissociation events, based on the median momentum of the NH_2^+ ions.

4 Energetic and dynamic behaviour of the fragment band

Since the Auger electron is ejected with momentum **k** from the NH_2^+ dissociated fragment freely moving with the velocity **v**, each vibrational line of NH_2^+ , is Doppler shifted $(\mathscr{D} = \mathbf{k} \cdot \mathbf{v} = k_z v_z)^{7,10,11}$

4.1 Auger–Doppler effect for the NH₂⁺ fragment band

Contrary to the thermal Doppler effect, high values of the Auger electron (\mathbf{k}) and the fragment momenta (\mathbf{p}) lead to large AD shift and have a significant influence on the spectral shape of the fragment lines:

$$E_{\rm e} = \hbar\omega_{\rm cf} + \varepsilon_{\nu_{\rm c}} - \varepsilon_{\nu_{\rm f}} + \mathbf{k} \cdot \mathbf{v} \tag{2}$$

Here $\hbar \omega_{\rm ef}$ is the electron transition energy of the Auger decay, $\varepsilon_{\nu_{\rm e}}$ and $\varepsilon_{\nu_{\rm f}}$ are vibrational energies of core-excited and final states, respectively, $k = \sqrt{2m_{\rm e}E_{\rm e}}$ is the momentum of the electron while $\mathbf{v} = \mathbf{p}/M$ is the velocity vector of the NH₂⁺ fragments with mass $M \equiv m_{\rm NH_2}$ which is predominantly parallel to the dissociating H₂N–H bond. We choose the *z*-axis parallel to **k**. The AD effect was first observed in conventional Auger spectra of randomly oriented molecules as the splitting of the Auger spectral features when the Auger electron was detected along the polarization vector **e** of X-ray field¹¹.

Contrary to conventional Auger spectroscopy, energy selected Auger-electron-photoion coincidence technique allows to 'directly' observe the Doppler shift $\mathbf{k} \cdot \mathbf{v}$, because now both electron \mathbf{k} and cation \mathbf{p} momenta are well defined owing to the fixed geometry of the detection in the coincidence setup, where the electrons and ions are collected at opposite angles along the *z*-axis (Fig. 1).

In the following, we concentrate on the coincidence analysis of the electrons and ions, measured at the N 1s \rightarrow 4a₁ resonance.

The bottom panel of Fig. 6 is an electron-ion coincidence map of the NH_2^+ ions with the resonant Auger electrons. The width of the horizontal band reflects the broadening of the ion TOF peak at various coincident electron energies. One can observe an overall broadening towards lower electron kinetic energies indicating an increase in the momentum the ion obtains in the dissociation event. The momentum scale for the component p_z is attached to the PEPICO map, as discussed later. The fragment peaks in the electron spectrum correspond to specific features in the PEPICO map – a tilted pattern is observed for each peak. Next, we demonstrate that these are signature features of the Doppler effect in the Auger electron emission.

The acceptance angle for electrons is ≤ 15 degrees from the axis, whereas the ions were collected, in principle, from the full 4π solid angle. However, the initial momentum of the ions along the *z*-axis affects the flight time of the ions, broadening the peaks in the ion TOF spectrum. This deviation from the nominal flight time is in a good approximation proportional to the axial momentum component p_z , which then allows determining, from the actual flight time, the p_z value for each ion.

In a Wiley-McLaren type ion TOF spectrometer, the relationship between the change in the flight time, dT, and the initial momentum component of the ion, p_z , is in a good approximation given by the accelerating force F_s in the source region:

$$\frac{\mathrm{d}T}{\mathrm{d}p_z} \approx -\frac{1}{F_\mathrm{s}} = -\frac{L_\mathrm{s}}{U_\mathrm{s}q},\tag{3}$$

where U_s is the voltage applied over the source region of length L_s and q is the charge of the ion. For the experimental conditions of Fig. 6, $p_z[\text{kg m s}^{-1}] \approx (-1.07 \times 10^{-24}) \times \Delta T$ [ns]. A more accurate conversion is obtained by numerical ion flight trajectory simulations, which also include the effects of the delayed application of the ion extraction voltage U_s following the ionization event.¹⁸ The delay, caused by both the flight time of the coincident electron and the switching times in the electronics, was about 500 ns. According to the simulations, $p_z = (-9.14 \times 10^{-25}) \times \Delta T$, which is used for obtaining the p_z values of the ions from the coincidence dataset.

Knowing the momentum p_z of the electron emitter ion along the emission direction allows us to calculate the Doppler correction to the electron's velocity and kinetic energy in the laboratory frame. When the kinetic energy of the electron from an emitter at rest is E_e , the change in its energy, when emitted from a moving ion, is

$$\mathscr{D} = \mathbf{k} \cdot \mathbf{v} \approx \frac{p_z}{M} \sqrt{2m_{\rm e}E_{\rm e}},\tag{4}$$

where M = 16 a.u. is the mass of the emitter NH₂⁺ ions. Here, we assumed that $\mathscr{D} \ll E_{\rm e}$ and neglected the deviation of the electron emission from the *z*-axis. Taking $E_{\rm e} = 382$ eV gives $\mathscr{D} [\rm eV] = (2.48 \times 10^{21}) p_z [\rm kg m s^{-1}]$. The tilted red lines in the bottom panel of Fig. 6 mark the changes due to the Doppler effect in the kinetic energy of the resonant Auger electrons emitted from a NH₂⁺ fragment. These lines were derived using the analytical relationship (4) derived above. As can be seen, they represent the observed patterns very well.

In the top panel of Fig. 6 the red dotted curve shows the "Doppler-corrected" spectrum, in which the Doppler shift was removed before generating the spectrum. Ideally, the Doppler energy correction should be done for each electron that was detected in coincidence with a NH₂⁺ fragment, on an event-byevent basis. The Doppler shift can be obtained using eqn (4) and the measured p_z value for the ion. However, in an actual measurement, events may contain false coincident NH₂⁺ ions originating from a different molecule than the one from which the detected electron was emitted, whereas the true coincident ion could remain undetected. Clearly, Doppler correction from false coincidences can not improve the spectral resolution and its effectiveness, therefore, depends strongly on the quality of the coincident dataset. In the present experiment, the requirement of high electron energy resolution reduced the transmission of electron spectrometer, which made it impractical to obtain coincidence data of high purity (minimal contribution from false coincidences). From comparison with the randomtriggered dataset, we estimated that 41% of all detected NH_2^+ ions were true coincidences with the resonant Auger electrons, and thus event-by-event Doppler correction would not be very efficient.

Instead, we performed the Doppler correction on histograms, in which case the false coincidence contribution can be eliminated. From the PEPICO map of Fig. 6, where the false coincidence background was first subtracted, a series of electron spectra were generated by slicing the ion TOF scale. Each slice spectrum then corresponds (within a narrow range) to a certain value of ΔT and p_z , and the Doppler shifts $\mathcal{D}(p_z)$ can be calculated for all slices. Then, the slices were shifted by $-\mathcal{D}(p_z)$ and added up, to obtain the red curve in the top panel of Fig. 6. As expected, the resulting "Doppler-corrected" spectrum exhibits narrowing of the peaks, as one source of broadening has been removed.

4.2 E_{KER} dispersion features of the fragment band

In this section we elaborate on the appearance of the following features observed in Fig. 7: (1) the plateau in the region of about 381–382 eV, which corresponds to the $\nu = 0, 1, 2, 3$ vibrationally excited \tilde{a}^+ state of the NH₂⁺ fragment ion (see the Auger spectrum Fig. 3); (2) monotonous decrease of E_{KER} with the slope = -1 in the region $E_e > 382$ eV. The last branch of the dispersion E_{KER} vs. E_e lying in the molecular region will be discussed in the next section. As we already clarified from the Auger spectrum (Fig. 3), the plateau region ($E_e = 381-382$ eV) can be almost exclusively attributed to the late Auger decay during the UFD process.

To give insight into the physical reason of the E_{KER} dependence on the energy of the Auger electron E_{e} let us write down the cross section of the coincidence process in the fragment region.

First, we derive the "coincidence" cross section. To avoid cumbersome analysis we neglected here the lifetime vibrational

interference (LVI) of intermediate vibrational levels^{7,24,28}

$$\begin{split} \sigma^{\text{fragm}}(E_{\text{e}}, E_{\text{KER}}, \omega) &= \sum_{\nu_{\text{c}}} \sigma_{\nu_{\text{c}}}^{\text{fragm}}(E_{\text{e}}, E_{\text{KER}}, \omega), \\ \sigma_{\nu_{\text{c}}}^{\text{fragm}}(E_{\text{e}}, E_{\text{KER}}, \omega) &= C \sum_{\nu_{\text{f}}} \mathscr{P}_{0E_{\text{KER}}} \mathscr{P}_{0\nu_{\text{c}}} P_{\nu_{\text{c}}\nu_{\text{f}}} \\ &\times \frac{\left\{ \left[E_{\text{KER}} + E_{\text{e}} + \varepsilon_{\nu_{\text{f}}} - (\hbar\Omega + \Delta E_{\text{c}} + \hbar\omega_{\text{cf}}) \right]^2 + \Gamma_{\text{f}}^2 \right\}^{-1}}{\left\{ \left[E_{\text{e}} - \hbar\omega_{\text{cf}} - (\varepsilon_{\nu_{\text{c}}} - \varepsilon_{\nu_{\text{f}}}) - \mathbf{k} \cdot \mathbf{v} \right]^2 + \Gamma^2 \right\}}. \end{split}$$
(5)

Here $C \propto |(\mathbf{e} \cdot \mathbf{d}_{oc})Q_{cf}|^2$, \mathbf{d}_{c0} and Q_{cf} are a transition dipole moment of core excitation and an amplitude of Auger decay, respectively, ε_{ν_c} and ε_{ν_f} are vibrational energies of the fragment in core-excited and final states, respectively. The FC factor of the dissociative mode is a broad function

$$\mathscr{P}_{0E_{\text{KER}}} \propto \exp\left(-\frac{(E_{\text{KER}} - \Delta E_{\text{c}})^2}{\Delta^2}\right), \quad \Delta = \mathscr{F}_{\text{c}}a_0.$$
 (6)

Moreover, $\mathscr{P}_{c0} = |\langle 0|\nu_c \rangle^{(\text{mol})}|^2$ and $P_{cf} = |\langle \nu_c|\nu_f \rangle^{(\text{fragm})}|^2$ are the FC factors of bound–bound photoabsorption transition in the NH₃ molecule and the Auger decay in core-excited fragment N*H₂, respectively, $\Omega = \omega - \omega_{V0}$ is the detuning of ω relative to the frequency of the vertical absorption transition $\omega_{V0} = (E_c(R_0) - E_0)/\hbar$, $\Delta E_c = E_c(R_0) - E_c(\infty)$, $\hbar \omega_{cf} = E_c(\infty) - E_f(\infty)$, $a_0 = \sqrt{\frac{\hbar}{\mu\omega_0}}$, and $\mathscr{F}_c = -dE_c(R)/dR$ is the gradient of the potential energy curve $E_c(R)$ of the core-excited state at the equilibrium R_0 . Since the dissociative broadening Δ of the studied core-excited state is much larger than Γ and Γ_f , the broad FC factor $\mathscr{P}_{0E_{\text{KER}}}$ (6) plays a minor role in the studied process. The RAS cross section

$$\sigma^{\text{fragm}}(E_{\text{e}},\omega) = \left\langle \int dE_{\text{KER}} \sigma^{\text{fragm}}(E_{\text{e}}, E_{\text{KER}}, \omega) \right\rangle$$
$$= \left\langle C \int dE_{\text{KER}} \sum_{\nu_{\text{c}}\nu_{\text{f}}} \frac{\mathscr{P}_{0E_{\text{KER}}} \mathscr{P}_{0\nu_{\text{c}}} P_{\nu_{\text{c}}\nu_{\text{f}}}}{\left[E_{\text{e}} - \hbar\omega_{\text{cf}} - (\varepsilon_{\nu_{\text{c}}} - \varepsilon_{\nu_{\text{f}}}) - \mathbf{k} \cdot \mathbf{v}\right]^{2} + \Gamma^{2}} \right\rangle$$
(7)

shows that the fragment band consists of narrow vibrational resonances (lines) with the width defined by Γ and Auger Doppler broadening.^{7,10,24,26} Here, angular brackets show the averaging over all directions of the momentum **p** of ejection of the dissociated fragment. Notably, the RAS cross section for *molecular* Auger decay in resonant Raman conditions does not include lifetime broadening of core-excited state,^{24,26} which was mentioned above and can be seen in Fig. 3: the vibrational progression with the spacing of about 110 meV of the participator \tilde{X} final state for NH₃⁺ ($E_e \sim 389$ –390 eV) is well resolved and the NH₂⁺ fragment lines at $E_e \sim 381$ –382 eV appear considerably broader owing to the contribution of $\Gamma \sim 130$ meV.

Let us analyse the partial "coincidence" cross section $\sigma_{\nu_c}^{\text{fragm}}(E_{\text{e}}, E_{\text{KER}}, \omega)$ (eqn (5)) where the signal is collected from

different directions of **p**:

$$\sigma_{\nu_{c}}^{\text{fragm}}(E_{e}, E_{\text{KER}}, \omega) = \left\langle C \times \sum_{\nu_{f}} \mathscr{P}_{0E_{\text{KER}}} \mathscr{P}_{0\nu_{c}} P_{\nu_{c}\nu_{f}} \right.$$
$$\times \frac{\exp\left\{-\frac{\left[E_{\text{KER}} + E_{e} + \varepsilon_{\nu_{f}} - (\hbar\Omega + \Delta E_{c} + \hbar\omega_{cf})\right]^{2}\right\}}{2\gamma_{\text{inst}}^{2}}\right\}}{\left[E_{e} - \hbar\omega_{cf} - (\varepsilon_{\nu_{c}} - \varepsilon_{\nu_{f}}) - \mathbf{k} \cdot \mathbf{v}\right]^{2} + \Gamma^{2}}\right\rangle}.$$
$$(8)$$

For comparison with the experiment, the instrumental resolution in determining E_{KER} should be taken into account. E_{KER} is obtained from the momentum of the NH_2^+ ions, calculating their kinetic energy $E_{\text{NH}2^+}$ and converting it to E_{KER} with the coefficient $(1 + M_{\text{NH}2}/M_{\text{H}})$. The instrumental momentum resolution $\Delta p_{\text{NH}2^+}$ is approximately constant, therefore the kinetic energy resolution $\gamma_{\text{inst}} \propto \sqrt{E_{\text{KER}}} \Delta p$. Since this value is in fact much larger than the lifetime broadening of the final state Γ_{f} : $\gamma_{\text{inst}} \gg \Gamma_{\text{f}}$, we replaced the Lorentzian $\{[E_{\text{KER}} + E_{\text{e}} + \varepsilon_{\nu f} - (\hbar\Omega + \Delta E_{\text{c}} + \hbar\omega_{\text{cf}}]]^2 + \Gamma_{\text{f}}^2\}^{-1}$ in eqn (8) by a Gaussian that represents the experimental broadening.

Because of the averaging over the directions of the fragment momentum **p**, the peak position of the partial cross section $\sigma_{\nu_c}^{\text{fragm}}(E_e, E_{\text{KER}}, \omega)$ (see eqn (8)) does not depend on the Doppler shift and $\sigma_{\nu_c}^{\text{fragm}}(E_e, E_{\text{KER}}, \omega)$ exhibits a maximum when two resonant conditions are fulfilled

$$E_{\text{KER}} = -(E_{\text{e}} + \varepsilon_{\nu f}) + \hbar\Omega + \Delta E_{\text{c}} + \hbar\omega_{\text{cf}}, \quad E_{\text{e}} = \hbar\omega_{\text{cf}} + \varepsilon_{\nu c} - \varepsilon_{\nu f}.$$
(9)

Substitution of the expression for E_e in equation for E_{KER} results in expression $E_{\text{KER}} = -\varepsilon_{\nu c} + \Delta E_c + \hbar \Omega$. This equation says that the maximum of the partial cross section is lying on the horizontal ridge

$$E_{\rm KER} = -\varepsilon_{\nu \rm c} + {\rm const} \tag{10}$$

in agreement with the plateau observed in the experiment (Fig. 7). The total "coincidence" cross section $\sigma^{\text{fragm}}(E_{e,}E_{\text{KER}},\omega)$ (eqn (5)) is the sum of the partial cross sections for different vibrational levels ν_c of core-excited states. This means that the 2D map of $\sigma^{\text{fragm}}(E_{e,}E_{\text{KER}},\omega)$ is the set of the parallel horizontal lines for each $\varepsilon_{\nu c}$ (see eqn (10)), on which the maxima (eqn (11)) of the "coincidence" cross section (see Fig. 8) are lying as defined by equations

$$E_{\text{KER}} = -\varepsilon_{\nu c} + \Delta E_{c} + \hbar \Omega = \text{const}, \quad E_{e} = \hbar \omega_{cf} + \varepsilon_{\nu c} - \varepsilon_{\nu f}.$$
(11)

The distribution of the maxima (11) of the "coincidence" cross section (eqn (8)) displayed in Fig. 8 shows that the slope of the $E_{\text{KER}}(E_e)$ is 0 (horizontal) when the number of populated vibrational levels in the core-excited state is significantly smaller than the number of the final vibrational states. This is the case of the experimentally observed dependence in the electron kinetic energy region 381 eV $< E_e < 382$ eV (see Fig. 7). This result is fully in line with the RAS spectrum shown in Fig. 3

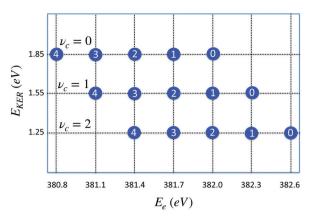


Fig. 8 Distribution of maxima of the total cross section $\sigma^{\text{fragm}}(E_{\text{er}}, E_{\text{KER}}, \omega)$ (eqn (8)) in the $(E_{\text{KER}}, E_{\text{e}})$ plane. Labels in circles show the vibrational quantum number of the final state $\nu_{\text{f}} = 0, 1, 2, 3, 4$. Calculation is performed using eqn (11) for $\nu_c = 0, 1, 2$ and harmonic potentials for core-excited and final states with vibrational frequencies $\omega_{\text{vib}} = 0.385 \text{ eV}$. $\omega_{\text{cf}} = 382 \text{ eV}$. $\Delta = 1$, $\Delta E_c = E_c(R_0) - E_c(\infty) = 2 \text{ eV}$, $\Omega = 0$. When ν_c increases the distribution is shifted to the right (to higher values of) $E_e = \omega_{\text{cf}} + \varepsilon_{\nu_c} - \varepsilon_{\nu_f}$ while $E_{\text{KER}} = -\varepsilon_{\nu_c} + \Delta E_c + \Omega$ decreases (see eqn (11)).

since the fragment decay shows a vibrational progression which is typical for starting at $\nu_c = 0$.²⁹ Progressions starting at $\nu_c > 0$ would show different intensity distributions; in particular a progression starting from $\nu_c = 1$ would show the $\nu_c = 1 \rightarrow \nu_f = 0$ transition at 382.3 eV. From the absence of such a peak we can conclude that contributions from $\nu_c > 0$ can be neglected.

In a general case, when the numbers of core-excited and final-state vibrational levels are comparable, the slope of the function $E_{\text{KER}}(E_{\text{e}})$ can deviate significantly from 0.

4.2.1 Dispersion law in the 'off-resonance' region of the $\nu_{\rm f}$ vibrational lines of the \tilde{a}^+ state of the NH₂⁺ fragment ($E_{\rm e} > 382$ eV). The experimental dispersion of $E_{\rm KER}$ as a function of $E_{\rm e}$ has different behavior in the region preceding the first vibrational line (here referred to as ' $\nu_{\rm f} = 0$ resonance') of the fragment band (Fig. 7). Above, we characterized it using the median distribution of the NH₂⁺ ion total momenta.

Additional details of the relationship between the kinetic energy release in the dissociation and the Auger electron energy can be obtained from the investigation of the E_{KER} distribution curves. In Fig. 9a and b, the experimental distributions $N(E_{\text{KER}})$ are presented as two-dimensional histograms, allowing to show their evolution with the electron energy $(E_{\rm e})$. Panel (a) shows the unnormalised distributions, thus reflecting also the variations of the intensity in the coincident Auger electron spectrum. Panel (b) gives all the distributions (vertical slices) as normalized to unity, and thus the variations seen reflect solely the changes in the shape of $N(E_{\text{KER}})$. As can be seen from the comparison of panels (a) and (b), the distinct vertical lines in (a) arise mainly from the increased cross section at these vibrational peak positions in the Auger spectrum, and the actual changes in the $N(E_{\text{KER}})$ are minor (panel b). The distribution $(N(E_{\text{KER}}))$ gradually broadens as the electron energy decreases (resulting in lower peak values and correspondingly less contrast in panel b).

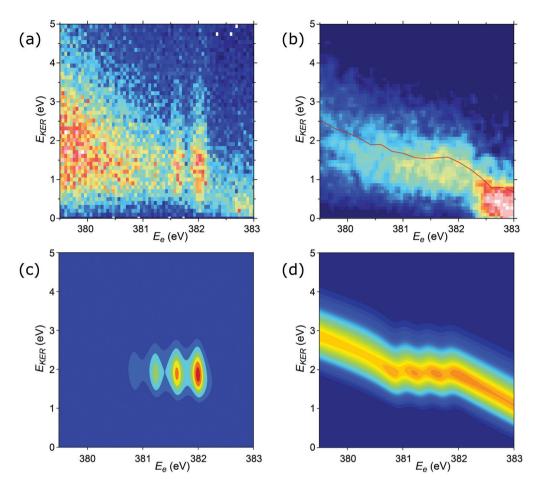


Fig. 9 2D plots for the distributions of E_{KER} as a function of resonant Auger electron energy E_e for the fragment band region. (a) Experimentally derived E_{KER} as a function of E_e measured at the top of the resonance, at $\hbar\omega = 400.66 \text{ eV}$. (b) Experimental data derived from the normalised momentum distribution as a function of E_e . The normalisation was done by the area for each bin of electron kinetic energy E_e . The red curve is the E_{KER} distribution, derived from the median momentum of the NH₂⁺ ion (see Fig. 7). The observed intensity at $E_e > 382.5 \text{ eV}$ corresponds to the high-binding-energy tail of the molecular participator state e^{-1} of NH₃⁺. (c) Theoretical cross section calculated by eqn (8) displaying four vibrational lines with the tails dispersing as $E_e = \text{const}$ in agreement with the experimental panel (a). (d) Normalised theoretical cross section $\sigma_{\text{frorm}}^{fragm}(E_e, E_{\text{KER}}, \omega)$ (12) featuring that the dispersion of the tails of the vibrational line $\nu = 0$ at $E_e > 382$ eV is close to $E_{\text{KER}} + E_e$ = const in agreement with the experimental panel (b) and Fig. 7. Calculations were performed for $\nu_c = 0$, $\nu_f = 0.12, 3$, $\Omega = 0$, $\Gamma = \text{HWHM} = 0.11 \text{ eV}$, $P_{00} = 0.4$, $P_{01} = 0.3$, $P_{02} = 0.2$, $P_{03} = 0.1$. Γ is the experimental HWHM broadening of the RAS vibrational lines. In simulations, we used experimentally derived dependence $\gamma_{\text{inst}}(E_{\text{KER}}) = 0.09 + 0.282E_{\text{KER}}^{0.6}$.

We also computed normalised theoretical cross sections, which were derived from eqn (8):

$$\sigma_{\text{norm}}^{\text{fragm}}(E_{\text{e}}, E_{\text{KER}}, \omega) = \frac{\sigma^{\text{fragm}}(E_{\text{e}}, E_{\text{KER}}, \omega)}{\int dE_{\text{KER}}\sigma^{\text{fragm}}(E_{\text{e}}, E_{\text{KER}}, \omega)}$$
(12)

This normalisation allows observing the non-resonant tail of the $\nu_{\rm f} = 0$ vibrational line which, according to experiment (Fig. 7), has a linear dispersion with the slope = -1: $E_{\rm KER}$ + $E_{\rm e}$ = const. To explain this dispersion we take into account the expression for the FC factor $\mathcal{P}_{0E_{\rm KER}}$ (eqn (6)) in eqn (8) for the cross section:

$$\sigma_{\nu_{\rm c}}(E_{\rm e}, E_{\rm KER}, \omega) \propto \exp\left(-\frac{(E_{\rm KER} - \Delta E_{\rm c})^2}{\Delta^2}\right) \times \exp\left\{-\frac{\left[E_{\rm KER} + E_{\rm e} + \varepsilon_{\nu_{\rm f}} - (\hbar\Omega + \Delta E_{\rm c} + \hbar\omega_{\rm cf})\right]^2}{2\gamma_{\rm inst}^2}\right\}$$
(13)

where we neglected the Lorentzian because the electron kinetic energy region $E_{\rm e}$ > 382 eV is beyond the $\nu_{\rm f}$ vibrational resonances. This equation asserts that the dispersion in the off-resonance region is lying between the lines

$$E_{\text{KER}} = \text{const}, \text{ and } E_{\text{KER}} + E_{\text{e}} = \text{const}$$
 (14)

In the case of ammonia, the dissociative broadening Δ of the N 1s \rightarrow 4a₁ resonance is significantly larger than the instrumental broadening γ_{inst} , therefore the dispersion law is defined by the sharpest Gaussian resulting in $E_{KER} + E_e = \text{const.}$ This conclusion is in agreement with both theory and experiment (Fig. 9b and d).

4.2.2 Rotation of the (E_{KER}, E_e) dispersion of the vibrational lines vs. Γ , γ_{inst} . Fig. 9 shows the dispersion E_{KER} as a function of E_e . Both experiment (Fig. 9a) and theory (Fig. 9c) show that each vibrational line of the fragment band displays almost vertical dispersion E_e = const. In fact, the tilt of the

PCCP

 $E_{\text{KER}}(E_{\text{e}})$ dispersion is very sensitive to the ratio $\gamma_{\text{inst}}/\Gamma$ (see eqn (8)) and is not related to the Doppler effect. The reason for this is that E_{KER} depends on p_z^2 (see the text above eqn (9)) in contrast to the Doppler effect which depends on the sign of p_z as it is seen from Fig. 6.

The cross section (eqn (8)), being the product of the Gaussian and the Lorentzian, has two resonant features given by eqn (11). The maximum of the Lorentzian evolves along the vertical line E_{e} = const, while the maximum of the Gaussian follows the dispersion along the tilted line $E_{\text{KER}} = -E_{\text{e}} + \text{const}$ with the slope equal to -1. Apparently, when $\gamma_{inst} \leq \Gamma$ the Gaussian plays a major role, which results in a tilted dispersion $E_{\text{KER}} = -E_{\text{e}} + \text{const.}$ With increase of the ratio $\gamma_{\text{inst}}/\Gamma$ the horizontal dispersion starts to compete with the tilted dispersion and the dispersion line $E_{\text{KER}}(E_e)$ rotates clockwise (Fig. 10) and approaches the vertical line $E_{\rm e} = {\rm const}$ when $\gamma_{\rm inst}/\Gamma \gg 1$. The instrumental broadening γ_{inst} is dependent on E_{KER} and is larger in average than Γ . We computed the dispersion of each vibrational spectral line using eqn (8) neglecting the Doppler effect and taking into account the experimental dependence of γ_{inst} on E_{e} . The calculated dispersion $E_{\text{KER}}(E_{\text{e}})$ is close to the vertical one in agreement with the measurements (see Fig. 9a).

4.3 Molecular band: redistribution of available energy

The molecular band is formed by the Auger transitions near the equilibrium ground state geometry R_0 of NH₃ (Fig. 4), contrary to the Auger decays in the core-excited already dissociated fragment far away from R_0 which produce the fragment band (Fig. 5).

The region below $E_e < 381$ eV is largely dominated by molecular Auger decay, taking place at the NH₂–H bond distances close to the ground-state geometry of ammonia, where the NH₂⁺ fragment is formed by the dissociation in the final state after emission of the Auger electron. In this case, the partitioning of the internal energy left in the system after Auger decay occurs in the final molecular state of the NH₃⁺ ion.

To describe the coincidence measurements of the molecular band with the dissociative final state we should use the following expression for the cross section:

$$\begin{split} \sigma^{\mathrm{mol}}(E_{\mathrm{e}}, E_{\mathrm{KER}}, \omega) \\ &= |F_{\nu_{\mathrm{f}}}|^{2} \exp\left\{-\frac{\left[E_{\mathrm{KER}} + E_{\mathrm{e}} + \varepsilon_{\nu_{\mathrm{f}}} - (\hbar\Omega + \Delta E_{\mathrm{c}} + \hbar\omega_{\mathrm{cf}})\right]^{2}}{2\gamma_{\mathrm{inst}}^{2}}\right\},\\ F_{\nu_{\mathrm{f}}} &= (\mathbf{e} \cdot \mathbf{d}_{0c}) \mathcal{Q}_{\mathrm{cf}} \\ &\times \int \mathrm{d}E_{\mathrm{KER}}^{'} \sum_{\nu_{\mathrm{c}}} \frac{\{\langle 0|E_{\mathrm{KER}}^{'} \rangle \langle E_{\mathrm{KER}}^{'}|E_{\mathrm{KER}} \rangle \langle 0|\nu_{\mathrm{c}} \rangle \langle \nu_{\mathrm{c}}|\nu_{\mathrm{f}} \rangle\}^{(m)}}{E_{\mathrm{e}} - (\hbar\omega_{\mathrm{cf}} + \varepsilon_{\nu_{\mathrm{c}}} - \varepsilon_{\nu_{\mathrm{f}}}) + E_{\mathrm{KER}} - E_{\mathrm{KER}}^{'} + i\Gamma'}, \end{split}$$

$$\tag{15}$$

where the upper index (*m*) indicates that all Franck–Condon amplitudes are calculated in the region of molecular transitions near the equilibrium ground state geometry R_0 ; ν_c and ν_f are bound vibrational modes in core-excited and final states, respectively; and E'_{KER} and E_{KER} correspond to the dissociative nuclear state along the reaction coordinate. The kinetic energy release E'_{KER} and E_{KER} are depicted in Fig. 4.

In the case explored in this work for dissociative core-excited and final states, the spectral width of the RAS amplitude $F_{\nu_{\ell}}$ is defined by the spectral width of the continuum–continuum FC amplitude $\langle 0|E_{\rm KER}'\rangle^{25}$

$$\gamma = \left|\frac{\hbar^2}{2\mu}(F_{\rm f} - F_{\rm c})\sqrt{F_{\rm f}F_{\rm c}}\right|^{1/3} \tag{16}$$

which is defined by the difference of the slopes $F_{\rm f}$ and $F_{\rm c}$ of potential energy curves of final and core-excited states, respectively. This broadening is much larger (see Fig. 3) than $\gamma_{\rm inst}$. Thus the narrowest function in cross section (15) is the Gaussian which asserts that $E_{\rm KER} + E_{\rm e} + \varepsilon_{\nu_{\rm f}} = {\rm const.}$ This equation neglects rotational degrees of freedom which often contribute to Auger spectra.^{7,30–33} Including all internal degrees of freedom gives a general equation:

$$E_{\text{KER}} + E_{\text{e}} + \varepsilon_{\text{f}}^{\text{in}} = \text{const}, \quad \varepsilon_{\text{f}}^{\text{in}} = \varepsilon_{\nu_{\text{f}}} + \varepsilon_{\text{rot}}$$
(17)

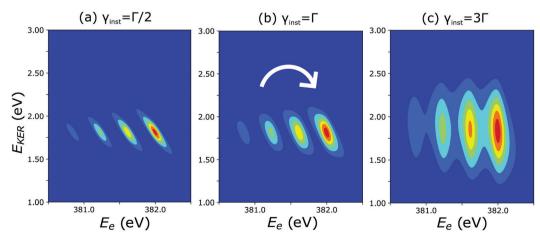


Fig. 10 Theoretical 2D plots of E_{KER} as a function of E_{e} calculated by eqn (8): the dispersion of vibrational lines 'rotates' clockwise with increase of the ratio $\gamma_{\text{inst}}/\Gamma$ (see text for more details).

where the total internal energy $\varepsilon_{\rm f}^{\rm in}$ is introduced as a sum of energies of vibrational $\varepsilon_{\nu_{\rm f}}$ and rotational $\varepsilon_{\rm rot}$ excitations of NH₃, occurring in the course of the ultrafast dissociation.

Neglecting internal degrees of freedom gives the equation

$$E_{\rm KER} + E_{\rm e} = \rm const.$$
 (18)

This linear correlation between electron energy E_e and kinetic energy release E_{KER} with a slope of 1 was experimentally observed for the diatomic molecules (O_2^9 , HCl⁵) when atomic fragments are formed following dissociation. However, in our work on ammonia we observe a strong deviation from eqn (18), which is discussed in more detail in the last part of the paper. The correlation extracted from our measurements is

$$E_{\rm e} + 1.75(3) \times E_{\rm KER} = \text{const} \tag{19}$$

The reason for this disagreement with eqn (18) is that the internal degrees of freedom (see eqn (17)) of the NH_2^+ fragment play an important role in the course of the molecular dissociation in the final state.

In the following, we discuss the possible ways of partitioning of the internal energy between rotational and translational degrees of freedom.

We consider the dissociation of AB_3 molecule (NH_3 in the present study) which has a trigonal pyramidal shape

$$AB_3 \rightarrow AB_2 + B$$
 (20)

with the angle $\alpha = \angle (BAB)$.

The total available energy

$$E_{\rm av} = \omega - \omega_{\rm f0} - E_{\rm e} = E_{\rm KER} + \varepsilon_{\rm f}^{\rm in} \tag{21}$$

of the AB₃ molecule in the final state partitions into translational energy E_{KER} of both products AB₂ and B, as well as internal energy $\varepsilon_{\text{f}}^{\text{in}} = \varepsilon_{\nu_{\text{f}}} + \varepsilon_{\text{rot}}$ of the fragment AB₂, namely into vibrational $\varepsilon_{\nu_{\text{f}}}$ and rotational energy ε_{rot} .

4.3.1 Recoil-induced rotation. We implement the impulsive model to compute the rotational energy $E_{\rm rot}$ of the AB₂ fragment due to the recoil from the dissociating A atom. The impulsive model^{34–36} assumes that (1) the fragment B dissociates along the equilibrium bond direction AB, (2) the bond between the fragment atom B and the central atom A breaks instantaneously, and that after the bond breaking the fragment AB₂ rotates freely. Employing the conservation of energy, momentum and total angular momentum

$$\mathbf{P}_{AB2} + \mathbf{P}_{B} = 0, \quad \mathbf{J}_{AB2} + \mathbf{J}_{B} = 0 \tag{22}$$

one can obtain the following expression for the rotational energy

$$E_{\rm rot} = \eta^2 \rho E_{\rm KER},$$

$$\rho = \frac{(1+2\eta)^2}{(1+3\eta)^2 \cos^2(\alpha/2)} \left\{ \sin \frac{\alpha}{2} \sqrt{1+2\cos \alpha} - \frac{\sqrt{|(1+2\eta)(1+6\eta)-4\eta(2+3\eta)\cos^2(\alpha/2)|}}{2(1+2\eta)} |\sin \zeta| \right\}^2.$$
(23)

where the angular momenta J_{AB2} and J_B are defined with respect to the center of gravity of the AB₂ fragment and of the AB₃ molecule, respectively, E_{KER} is the kinetic energy release which is the total translational energy of AB₂ and B fragments in the center of gravity of the AB₃ molecule. Here

$$\cos \theta = -\frac{\cos \alpha}{\cos(\alpha/2)},$$

$$\cos \kappa = \frac{\sqrt{2}[\eta - (1+\eta)\cos \alpha]}{\sqrt{1+4\eta+6\eta^2+\cos \alpha - 2\eta(2+3\eta)\cos^2 \alpha}},$$
(24)

Since the dimensionless mass parameter

$$\eta \equiv \frac{M_{\rm B}}{M_{\rm A}} = \frac{M_{\rm H}}{M_{\rm N}} = \frac{1}{15} = 0.0667, \quad \eta^2 = 0.0044, \quad \zeta = \theta - \kappa$$
(25)

is too small in the ammonia molecule, studied in this work, the recoil-induced rotational excitations of the fragment NH_2^+ can not explain the deviation of the experimental coefficient 1.75 (eqn (19)) from 1 (eqn (18)).

Conclusion: the recoil-induced rotational excitation is small for molecules with a light dissociating atom (for example, the hydrogen atom, B = H). However, $E_{\rm rot}$ can become approaching $E_{\rm KER}$ when masses $M_{\rm A}$ and $M_{\rm B}$ are comparable; in this case the recoil-induced rotational heating is important and has to be taken into account.

4.3.2 Rotational excitation induced by the possible change of the pyramidal geometry to planar. In the previous experimental studies of VUV photodissociation of water³⁷ and ammonia^{38–40} molecules, it was shown that extensive rotation is excited upon a vigorous and rapid change of the molecular geometry in the course of dissociation (the change of the bending angle in the case of water and transition from pyramidal to planar geometry in the case of ammonia).

The physical mechanism of this important dynamical effect is briefly described along the following lines. The core-excited NH₃ molecule is pyramidal in its equilibrium geometry with the angle $\alpha \sim 108^{\circ}$, similar to the one of its ground state.^{19,23} We can assume that it may decay to the final state with the planar equilibrium geometry, which is dissociative along the H₂N-H bond. When the planar final state is reached after the Auger decay, the NH₂ group rotates from pyramidal to planar geometry at the same time as the H₂N-H bond elongation starts to proceed. When the N-H bond is "suddenly" broken, the NH₂⁺ fragment becomes free but it continues the free rotation. In this case, the rotational energy is then borrowed from the energy of the chemical bond.

As an example, it was demonstrated that for the photodissociation of valence-excited H_2O^{37} 94% of the bond dissociation energy is transformed into the rotational energy ($E_{\rm rot} \approx$ 0.94 $E_{\rm KER}$) of the OH fragment. Thus we can not exclude that the observed 43% loss of the dissociation energy might be related to the rotational excitation of the NH₂⁺ caused by the transformation from pyramidal (in the ground or core-excited state) to planar geometry in the final dissociative state. **4.3.3** Vibrational excitation caused by the coupling between translational (dissociative) and vibrational modes. Excitation of vibrations in the course of dissociation in the final state can be another reason for "borrowing" the internal energy from the kinetic energy release E_{KER} . To exemplify this mechanism let us consider the dissociation of the AB₂ molecule

$$BAB \rightarrow BA \cdots B$$
 (26)

The full potential energy surface (PES) can be approximately presented as the sum

$$E(R,r) \approx V_{\rm tr}(R) + V_{\rm vib}(r,R) \tag{27}$$

of the potential $V_{tr}(R)$ along the dissociative coordinate *R* and the BA potential along the vibrational coordinate *r*. The vibrational potential $V_{vib}(r,R)$ changes the shape when *R* changes. If $V_{vib}(r,R)$ depends only on the vibrational coordinate *r*, energy can not "flow" between the translational (*R*) and vibrational (*r*) modes. The Schrödinger equation separates in this case into two uncoupled equations and the motions along *R* and *r* evolve independently of each other. In real situation the *R* dependence of vibrational potential $V_{vib}(r,R)$ is usually significant.⁴¹ This dependence couples translational and vibrational degrees of freedom.³⁶ Due to this, the part of translational energy E_{KER} is transformed to excitation of vibrations.

5 Conclusions

We have performed a coincidence study of the ultrafast dissociation process occurring in ammonia upon excitation of the N 1s core electron to the antibonding LUMO $(4a_1)$ orbital. The new coincidence setup GPES, permanently installed at the FinEstBeAMS beamline of the MAX IV synchrotron radiation facility in Lund, Sweden, allows achieving high resolution for resonant Auger electrons which are correlated to ion momenta measured simultaneously for each ionisation event.

Correlation of NH_2^+ ion flight times with Auger electron kinetic energy shows directly a dispersion of each vibrational resonance of the UFD fragment, which is attributed to the Auger–Doppler effect caused by ejection of the electron from the moving NH_2^+ radical in the core-excited state.

Furthermore, the median distributions of kinetic energy release as a function of electron kinetic energy show prominent dispersion behaviors in different regions of the corresponding RAS spectrum, particularly in the regions of the so-called molecular and fragment bands: molecular band $E_e + 1.75E_{KER} = const$, fragment band $E_{KER} = const$ and $E_e + E_{KER} = const$ for the region preceding the fragment band. These dispersions are explained with the help of theory and trends for more general cases are provided in this work. A particularly interesting dispersion is observed in the molecular-band region, corresponding to the Auger decays to the first spectator $(3a_1^24a_1^1)$ state, which deviates significantly from $E_{Auger} + E_{KER} = const$, previously observed in all the coincidence studies of UFD cases, exploiting ejection of an atomic fragment. The 'loss' of translational energy of the NH₂⁺ ion is attributed to the redistribution

of the available energy to the dissociation energy and excitation of the internal degrees of freedom of the fragment in the course of the dissociation in the final state.

An unusual distribution of E_{KER} within each vibrational state of the fragment is demonstrated to be caused by the competition between the Raman $E_{\text{KER}} + E_{\text{e}} = \text{const}$ and Auger dispersion $E_{\text{e}} = \text{const}$: when the broadening by the finite kinetic energy release resolution increases, the slope of the linear dispersion rotates from the Raman to the Auger dispersion.

Moreover, we have recorded an ultra-high-resolution singlechannel RAS spectrum with low signal-to-noise ratio, where very different line widths are observed for the vibrational components of the fragment and molecular bands. Auger decays to the final bound \hat{X} state $(3a_1^{-1})$ form much narrower vibrational lines with the spectral width limited by the instrumental resolution, while the fragment band consists of lines with the width defined by the lifetime broadening of the coreexcited state and the Doppler broadening.

To conclude, this work demonstrates a great potential of the high-resolution Auger electron – ion momenta imaging technique for the future studies of the partitioning of the excess energy between internal degrees of freedom in dissociating molecular fragments.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

We acknowledge MAX IV Laboratory for time on Beamline FinEstBeAMS under Proposal 20180420. Research conducted at MAX IV, a Swedish national user facility, is supported by the Swedish Research council under contract 2018-07152, the Swedish Governmental Agency for Innovation Systems under contract 2018-04969, and Formas under contract 2019-02496. We acknowledge SOLEIL Synchrotron in France for time on the PLEIADES beamline under Proposals No. 20201704. We are grateful to MAXIV and SOLEIL staff for smoothly running the facility. V. K. acknowledges the Swedish Research Council, Project No. 2019-03470. F. G also acknowledges support by Helmholtz-Zentrum Berlin für Materialien und Energie GmbH. F. G. P. K. and V. K. acknowledge also the Russian Science Foundation, Project No. 21-12-00193. O. T. acknowledges financial support from the French Agence Nationale de la Recherche (ANR) through the MUSTACHE project (ANR-18-CE30-0015).

Notes and references

- 1 H. Ågren, J. Nordgren, L. Selander, C. Nordling and K. Siegbahn, *Phys. Scr.*, 1978, **18**, 499.
- 2 P. Morin and I. Nenner, Phys. Rev. Lett., 1986, 56, 1913.
- 3 C. Miron, P. Morin, D. Céolin, L. Journel and M. Simon, J. Chem. Phys., 2008, **128**, 154314.

- 4 M. N. Piancastelli, R. Guillemin, M. Simon, H. Iwayama and E. Shigemasa, *J. Chem. Phys.*, 2013, **138**, 234305.
- 5 H. Sann, T. Havermeier, C. Müller, H.-K. Kim, F. Trinter, M. Waitz, J. Voigtsberger, F. Sturm, T. Bauer, R. Wallauer, D. Schneider, M. Weller, C. Goihl, J. Tross, K. Cole, J. Wu, M. S. Schöffler, H. Schmidt-Böcking, T. Jahnke, M. Simon and R. Dörner, *Phys. Rev. Lett.*, 2016, **117**, 243002.
- 6 T. Jahnke, V. Mergel, O. Jagutzki, A. Czasch, K. Ullmann, R. Ali, V. Frohne, T. Weber, L. P. Schmidt, S. Eckart, M. Schöffler, S. Schößler, S. Voss, A. Landers, D. Fischer, M. Schulz, A. Dorn, L. Spielberger, R. Moshammer, R. Olson, M. Prior, R. Dörner, J. Ullrich, C. L. Cocke and H. Schmidt-Böcking, in *High-Resolution Momentum Imaging-From Stern's Molecular Beam Method to the COLTRIMS Reaction Microscope*, ed. B. Friedrich and H. Schmidt-Böcking, Springer International Publishing, Cham, 2021, pp. 375–441.
- 7 F. Gel'mukhanov, M. Odelius, S. P. Polyutov, A. Föhlisch and V. Kimberg, *Rev. Mod. Phys.*, 2021, **93**, 035001.
- 8 K. Le Guen, C. Miron, D. Céolin, R. Guillemin, N. Leclercq, M. Simon, P. Morin, A. Mocellin, O. Björneholm, A. Naves de Brito and S. L. Sorensen, *J. Chem. Phys.*, 2007, **127**, 114315.
- 9 X.-J. Liu, Q. Miao, F. Gel'mukhanov, M. Patanen, O. Travnikova, C. Nicolas, H. Ågren, K. Ueda and C. Miron, *Nat. Photon.*, 2014, **9**, 120.
- 10 F. Gel'mukhanov, H. Ågren and P. Sałek, *Phys. Rev. A: At., Mol., Opt. Phys.*, 1998, 57, 2511.
- O. Björneholm, M. Bässler, A. Ausmees, I. Hjelte, R. Feifel, H. Wang, C. Miron, M. N. Piancastelli, S. Svensson, S. L. Sorensen, F. Gel'mukhanov and H. Ågren, *Phys. Rev. Lett.*, 2000, 84, 2826.
- 12 O. Björneholm, J. Chem. Phys., 2001, 115, 4139-4149.
- 13 R. Guillemin, M. Simon and E. Shigemasa, *Phys. Rev. A: At.*, *Mol., Opt. Phys.*, 2010, 82, 051401.
- M. Kitajima, K. Ueda, A. De Fanis, T. Furuta, H. Shindo, H. Tanaka, K. Okada, R. Feifel, S. L. Sorensen, F. Gel'mukhanov, A. Baev and H. Ågren, *Phys. Rev. Lett.*, 2003, 91, 213003.
- 15 O. Travnikova, J.-C. Liu, A. Lindblad, C. Nicolas, J. Söderström, V. Kimberg, F. Gel'mukhanov and C. Miron, *Phys. Rev. Lett.*, 2010, **105**, 233001.
- 16 L. Rosenqvist, K. Wiesner, A. Naves de Brito, M. Bässler, R. Feifel, I. Hjelte, C. Miron, H. Wang, M. N. Piancastelli, S. Svensson, O. Björneholm and S. L. Sorensen, *J. Chem. Phys.*, 2001, **115**, 3614.
- K. Wiesner, A. Naves de Brito, S. L. Sorensen, F. Burmeister, M. Gisselbrecht, S. Svensson and O. Björneholm, *Chem. Phys. Lett.*, 2002, 354, 382–388.
- 18 K. Kooser, A. Kivimäki, P. Turunen, R. Pärna, L. Reisberg, M. Kirm, M. Valden, M. Huttula and E. Kukk, J. Synchrotron Radiat., 2020, 27, 1080–1091.
- I. Hjelte, M. N. Piancastelli, C. M. Jansson, K. Wiesner, O. Björneholm, M. Bässler, S. L. Sorensen and S. Svensson, *Chem. Phys. Lett.*, 2003, 370, 781–788.
- 20 E. Kukk, D. Céolin, O. Travnikova, R. Püttner, M. N. Piancastelli, R. Guillemin, L. Journel, T. Marchenko, I. Ismail, J. Martins, J.-P. Rueff and M. Simon, *New J. Phys.*, 2021, 23, 063077.

- 21 R. Pärna, R. Sankari, E. Kukk, E. Nõmmiste, M. Valden, M. Lastusaari, K. Kooser, K. Kokko, M. Hirsimäki, S. Urpelainen, P. Turunen, A. Kivimäki, V. Pankratov, L. Reisberg, F. Hennies, H. Tarawneh, R. Nyholm and M. Huttula, *Nucl. Instrum. Methods Phys. Res., Sect. A*, 2017, **859**, 83–89.
- 22 J. Schirmer, A. B. Trofimov, K. J. Randall, J. Feldhaus,
 A. M. Bradshaw, Y. Ma, C. T. Chen and F. Sette, *Phys. Rev.* A: At., Mol., Opt. Phys., 1993, 47, 1136–1147.
- 23 N. Walsh, A. Sankari, J. Laksman, T. Andersson, S. Oghbaie, F. Afaneh, E. P. Månsson, M. Gisselbrecht and S. L. Sorensen, *Phys. Chem. Chem. Phys.*, 2015, **17**, 18944–18952.
- 24 F. Gel'mukhanov and H. Ågren, Phys. Rep., 1999, 312, 87-330.
- 25 F. Gelmukhanov and H. Ågren, Phys. Rev. A: At., Mol., Opt. Phys., 1996, 54, 379–393.
- 26 O. Björneholm, S. Sundin, S. Svensson, R. R. T. Marinho, A. Naves de Brito, F. Gel'mukhanov and H. Ågren, *Phys. Rev. Lett.*, 1997, **79**, 3150–3153.
- 27 O. Takahashi, K. Matsuyama, K. Tabayashi and K. Yamasaki, J. Phys. B, 2009, 42, 245102.
- 28 F. Gel'mukhanov, L. Mazalov and A. Kondratenko, *Chem. Phys. Lett.*, 1977, **46**, 133–137.
- 29 O. Travnikova, C. Miron, M. Bässler, R. Feifel, M. Piancastelli, S. Sorensen and S. Svensson, *J. Electron* Spectrosc. Relat. Phenom., 2009, 174, 100.
- 30 D. Céolin, J.-C. Liu, V. Vaz da Cruz, H. Ågren, L. Journel, R. Guillemin, T. Marchenko, R. K. Kushawaha, M. N. Piancastelli, R. Püttner, M. Simon and F. Gel'mukhanov, *Proc. Natl. Acad. Sci. U. S. A.*, 2019, **116**, 4877–4882.
- 31 Q. Miao, O. Travnikova, F. Gel'mukhanov, V. Kimberg, Y.-P. Sun, T. D. Thomas, C. Nicolas, M. Patanen and C. Miron, *J. Phys. Chem. Lett.*, 2015, 6, 1568–1572.
- 32 Y.-P. Sun, C.-K. Wang and F. Gel'mukhanov, *Phys. Rev. A: At., Mol., Opt. Phys.*, 2010, 82, 052506.
- 33 J.-C. Liu, V. Vaz da Cruz, S. Polyutov, A. Föhlisch and F. Gel'mukhanov, *Phys. Rev. A*, 2019, **100**, 053408.
- 34 K. E. Holdy, L. C. Klotz and K. R. Wilson, J. Chem. Phys., 1970, 52, 4588–4599.
- 35 H. B. Levene, J. Nieh and J. J. Valentini, *J. Chem. Phys.*, 1987, 87, 2583–2593.
- 36 R. Schinke, *Photodissociation Dynamics: Spectroscopy and Fragmentation of Small Polyatomic Molecules*, Cambridge University Press, 1993.
- 37 H. Wang, Y. Yu, Y. Chang, S. Su, S. Yu, Q. Li, K. Tao, H. Ding, J. Yang, G. Wang, L. Che, Z. He, Z. Chen, X. Wang, W. Zhang, D. Dai, G. Wu, K. Yuan and X. Yang, *J. Chem. Phys.*, 2018, **148**, 124301.
- 38 R. Dixon, Mol. Phys., 1989, 68, 263-278.
- 39 J. D. Rodrguez, M. G. González, L. Rubio-Lago and L. Bañares, *Phys. Chem. Chem. Phys.*, 2014, 16, 406–413.
- 40 C. Xie, J. Ma, X. Zhu, D. H. Zhang, D. R. Yarkony, D. Xie and H. Guo, *J. Phys. Chem. Lett.*, 2014, 5, 1055–1060.
- 41 R. C. Couto, V. V. Cruz, E. Ertan, S. Eckert, M. Fondell, M. Dantz,
 B. Kennedy, T. Schmitt, A. Pietzsch, F. F. Guimarães, H. Ågren,
 F. Gel'mukhanov, M. Odelius, V. Kimberg and A. Föhlisch, *Nat. Commun.*, 2017, 8, 14165.