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Nucleation kinetics of lithium phosphate precipitation†

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Lithium phosphate is an important material today in battery technology and catalysis, the source of which is gradually depleting. In this work we provide insights into the kinetics of lithium phosphate precipitation in a supersaturated solution, by monitoring the turbidity of a well-stirred reactant mixture at different concentrations and temperatures. The analysis of experimental data has revealed that nucleation can be described by a power law resembling mass action kinetics. The constructed reaction kinetic model that includes consecutive reversible complex formation preceding the heterogeneous reaction provides data which quantitatively match the experimental results, allowing detailed explanation of the mechanism of nucleation. Classical nucleation theory applied for the homogeneous nucleation of sparingly soluble salts is also consistent with the experiments.

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1 Introduction

The importance of crystal shape and stability to industrial processes and pharmaceutical products^{1–4} prompted many research into the structural arrangement, physical and chemical properties, and medical activities of different crystals. The formation of crystalline materials through nucleation and growth is an intricate network in which a heterogeneous chemical reaction is coupled to various transport processes. The former brings in nonlinearity by the existence of positive feedback during growth, allowing self-organization and self-assembly. A rapid increase of reaction rate in such systems can be observed after an induction time characterized by small rates under suitable conditions. The control of transport processes involved hence provides the possibility of fine tuning the morphology of synthesized crystals. Microfluidic techniques due to their well-defined fluid flow have successfully been utilized in studying precipitation reactions.^{5–6} In droplet-based microfluidics in confinement, for example, calcium carbonate polymorph control^{7–10} has been achieved and protein crystallization⁵ has been studied to understand phase behavior. On a larger scale, flow-driven systems also provide morphology control.¹¹ The

dihydrate form of calcium oxalate, generally a by-product in well-stirred systems, can be formulated in the presence of spatial gradients generated by flow.^{12,13} Spatial separation of cobalt oxalate from a mixture has been achieved in a gravity-current-driven system in a Hele–Shaw crystallizer,^{14,15} and lysozyme crystallization has been studied using a meso-oscillatory flow reactor showing various morphologies at different concentrations.^{16,17} Biomimetic conditions have also been applied for calcium carbonate¹⁸ and guanine¹⁹ crystallization providing possible control. In many experiments the reactants are initially spatially separated and injection brings them into contact, in which case the pumping order can also change the morphology of the formed crystals, as observed for cerium phosphate²⁰ or in reverse chemical gardens.^{21,22} Hence, the method of mixing^{11–14,20,23} as well as the strength of agitation²⁴ significantly contributes to the reaction conditions that determine the resultant crystal properties. The external control of transport processes allows the fine tuning of the time scales associated with them. These, in turn, couple to the chemical time scale of precipitation; therefore, *a posteriori* knowledge of the latter is essential in interpreting the outcome of the resultant reaction–diffusion–advection system.

The rate of nucleation can be determined by monitoring the turbidity, focused beam reflectance count,²⁵ pH changes,²⁶ and conductivity.^{25,27} For small supersaturation classical nucleation theory is used to describe nucleation,^{28,4} whereas the kinetic approach is more often applied for barely soluble electrolytes at high supersaturation^{29,30} as well as for nanoparticle formation.³¹ In this work we go beyond binary

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electrolytes, where several kinetic studies have been performed,^{29,32} and investigate the nucleation of lithium phosphate in a well-stirred system.

Lithium phosphate is a key compound in the recycling of lithium ion batteries. Thorough knowledge of its precipitation may prove to be important in enhancing the technology. It can also maintain a chemical garden, a growing hollow structure that separates the inner liquid containing lithium ion from the outer phosphate solution. In earlier work, we have shown that in a microfluidic device, polycrystalline lithium phosphate particles grow with orientation dependent rates. This is a direct consequence of the coupling between diffusional and advective transport.

In this work, we aim at studying the kinetics of precipitation of lithium phosphate by determining the induction times obtained through turbidity measurements at different concentrations and temperatures in a well-stirred system. For the qualitative description we construct a reaction kinetic model applicable to nucleation at high supersaturation far from thermodynamic equilibrium. Finally a microscopy study of the crystals and their X-ray diffraction data are presented to determine the morphology of the solid particles.

2 Experimental section

We prepared filtered stock solutions of lithium chloride and sodium phosphate from analytical grade chemicals of LiCl (BDH) and Na₃PO₄·12H₂O (Sigma-Aldrich) using ion-exchanged water (Purite RO100, $\kappa = 2.1 \mu\text{S cm}^{-1}$ at 25 °C).

The precipitation was monitored by measuring turbidity at 340 nm with a UV-spectrophotometer (UV-3100PC) equipped with an in-built magnetic stirrer and a thermostated cuvette holder (VWR A-100). The background turbidity was set with 2 mL LiCl solution in a standard, commercially available quartz cuvette with 1 cm × 1 cm × 4 cm size, after which 1 mL solution was withdrawn. The reaction was started by pipetting 1 mL Na₃PO₄ solution into the cuvette and stirring it. The turbidity measurement was repeated at least four times for each set of concentrations with stoichiometric ratio $R = [\text{Li}^+]_0/[\text{PO}_4^{3-}]_0 = 3$, where the concentrations with 0 in subscript represent the initial concentrations of the reactants with the initial concentration of sodium phosphate ranging from 0.060 M to 0.20 M.

Thermal effects were studied at stoichiometric ratios with $[\text{Na}_3\text{PO}_4]_0 = 0.030 \text{ M}$ at different temperatures ranging between 25 and 50 °C with 0.01 °C precision. After each experiment, the cuvette was removed and placed in 1 M HCl for a 5 min-long sonication (Elmasonic S 60 H) to dissolve any precipitate from the cuvette wall and crevices prior to washing and rinsing with deionized water.

The changes in the crystal morphology and size were studied at temperatures of 25, 36, and 50 °C by mixing 100 mL 0.18 M LiCl with 100 mL 0.06 M Na₃PO₄. Aliquots of 60 mL of the reacting mixture were withdrawn at various times, filtered using a syringe filter cap (cellulose acetate

membrane, 0.2 μm), washed with ion-exchanged water, and air dried.

The density of the solid lithium phosphate powder was measured to be 2.397 g cm^{-3} by a helium gas multivolume pycnometer (Micromeritics 1305).

2.1 Characterization

Crystal samples were collected at temperatures of $(25.0 \pm 0.2) \text{ }^\circ\text{C}$, $(36.0 \pm 0.2) \text{ }^\circ\text{C}$, and $(50.0 \pm 0.2) \text{ }^\circ\text{C}$, at different stages of the crystallization process. The dried crystals were examined under a scanning electron microscope (Hitachi S4700) with a vacuum accelerating voltage of 20 kV to obtain higher resolution, after sputtering the sample with gold in a vacuum for 2 minutes to improve surface conduction. The sizes of at least 300 crystal particles from several SEM images were measured using ImageJ software and their distribution was also determined. X-ray diffractograms of the powdered Li₃PO₄ samples were recorded on a Philips X-ray diffractometer (PXRD) with $\text{CuK}\alpha = 0.1542 \text{ nm}$, as the radiation source at ambient temperature in the $2\text{--}70^\circ (2\theta)$ range in 0.02° steps. The crystallinity was determined using Match! software and the crystallite sizes were calculated from Scherrer's equation.

3 Results and discussion

3.1 Kinetics and thermodynamics

Upon mixing the reactants, the solution turbidity remains almost zero during the induction time (1) as shown in Fig. 1. This is followed by a rapid increase in turbidity, termed the growth region (2), during which growth is dominated by the increase in either the number of nucleation sites or crystal size until a maximum turbidity or plateau is reached. The solution finally becomes saturated with the precipitate (3) with only slow aggregation taking place beyond the time span of the experiment. The increase of reactant concentration not only shortens the induction time by increasing the reaction



Fig. 1 Turbidity profiles for lithium phosphate at different initial reactant concentrations and (inset) the determination of induction time at 25 °C with $R = 3$.



rate but also increases the turbidity at the end of the growth period due to the production of more precipitate.

The induction time, defined as the time at which the initial part of the turbidity curve starts to deviate from the linear background (see the inset of Fig. 1), is inversely proportional to the initial rate of nucleation. Hence the concentration dependence is sought as a power law in the form of

$$t_{\text{ind}} \propto \frac{1}{r} = a[\text{PO}_4^{3-}]_0^{-b} \quad (1)$$

as shown in Fig. 2 because the reactant ratio is kept constant ($R = 3$).

The experimentally determined exponent in the power law b has a value of 4.22 ± 0.04 . This indicates that the association of reactant ions takes place in the apparent rate determining step for nucleation.

In our experiments we have not observed the dependence of induction time on the material of the cuvette as shown in the ESI† and the parallel runs have yielded reproducible results, indicating that the unavoidable dust particles have no significant effects. This suggests that homogeneous nucleation dominates the process in accordance with the very high supersaturation used ($S = 1.0 \times 10^4 - 2 \times 10^6$), where supersaturation S is defined as

$$S = \frac{[\text{Li}^+]^3 [\text{PO}_4^{3-}]}{K_{\text{sp}}} \quad (2)$$

with $K_{\text{sp}} = (1.3 \pm 0.2) \times 10^{-9}$ being the solubility product of lithium phosphate, determined from independent conductance measurements (for details see the ESI†). In such cases, induction times are short and nucleation is fast, with no time for inherent small particles, like dust, or the quartz surface to induce nucleation significantly.



Fig. 2 Induction time as a function of initial phosphate concentration at $T = 25$ °C. The black solid line shows the power-law fitting according to eqn (1). The red dashed line represents the calculated induction times from the kinetic model based on eqn (9)–(13).

This concentration dependence can also be related to the classical nucleation theory (CNT), according to which the nucleation rate J can be expressed as a function of supersaturation³³ as

$$J = A \exp\left(\frac{-B}{\ln^2 S}\right) \quad (3)$$

where A is the kinetic parameter, the concentration dependence of which is often neglected for small supersaturation not far from equilibrium. The thermodynamic parameter B is defined as

$$B = \frac{16\pi v^2 \gamma^3}{3k_B^3 T^3} \quad (4)$$

where v is the molecular volume of the solid particle, γ is the specific interfacial energy, k_B is the Boltzmann constant, and T is the absolute temperature. Since $t_{\text{ind}} \propto J^{-1}$, eqn (3) reduces to

$$t_{\text{ind}} = A' \exp\left(\frac{B}{\ln^2 S}\right). \quad (5)$$

In our system supersaturation is high; therefore, the fitting of eqn (5) to the measured data in Fig. 3 can only provide an estimation for the thermodynamic parameter B , from which the interfacial energy can also be estimated. The molecular volume of the solid particle is

$$v = \frac{M_w}{\rho_s N_A} = 8.021 \times 10^{-29} \text{ m}^3 \quad (6)$$

with $M_w = 115.79 \text{ g mol}^{-1}$, $\rho_s = 2.397 \text{ g cm}^{-3}$, and N_A is the Avogadro constant. Hence the calculation of interfacial tension from eqn (4) yields $\gamma_{\text{exp}} = 84 \pm 3 \text{ mJ m}^{-2}$. The value obtained falls in the range of 68–97 mJ m^{-2} found for weakly soluble inorganic salts like CaCO_3 , or various crystalline forms of CaHPO_4 and CaSO_4 .³⁴ The value also matches the



Fig. 3 The induction time as a function of supersaturation. The black line shows the dependence according to the classical nucleation theory.



estimation of solid–liquid interfacial tension by Mersmann's equation³⁵ according to

$$\gamma_{\text{SL}} = \frac{2k_{\text{B}}T}{(36\pi)^{1/3}} \left(\frac{1}{v}\right)^{2/3} \ln\left(\frac{C_{\text{S}}}{C_{\text{L}}}\right) \quad (7)$$

where $C_{\text{S}} = \rho_{\text{S}}/M_{\text{w}} = 20.7 \text{ M}$ is the concentration associated with the solid phase, while $C_{\text{L}} = 2.6 \text{ mM}$ is the solubility in the liquid phase, yielding $\gamma_{\text{SL}} = 82 \text{ mJ m}^{-2}$.

Because of the temperature dependence of the rate coefficients, the induction time is expected to increase exponentially with T^{-1} as

$$t_{\text{ind}} \propto \exp\left(\frac{E_{\text{a}}}{RT}\right) \quad (8)$$

with constant initial concentrations, since the solution density variation is negligible under the experimental conditions. Fig. 4 illustrates that a 10% increase in temperature results in a magnitude increase of reaction rate and, in accordance, a ten-fold decrease in the induction time.

However, at higher temperatures there is a deviation from the simple exponential dependence because nucleation is found to be slower than expected. The apparent activation energy at temperatures above 35 °C is about half of that found at lower temperatures (86.3 kJ mol⁻¹ vs. 175 kJ mol⁻¹). This suggests that the rate determining step in the nucleation process is preceded by reaction steps so that the apparent rate coefficient contains several others with different activation energies.

3.2 Modeling the precipitation reactions

In our experimental study supersaturation is high, and the system is far from thermodynamic equilibrium; therefore, we follow a reaction kinetic approach for the description of the onset of precipitation. We first consider the stepwise

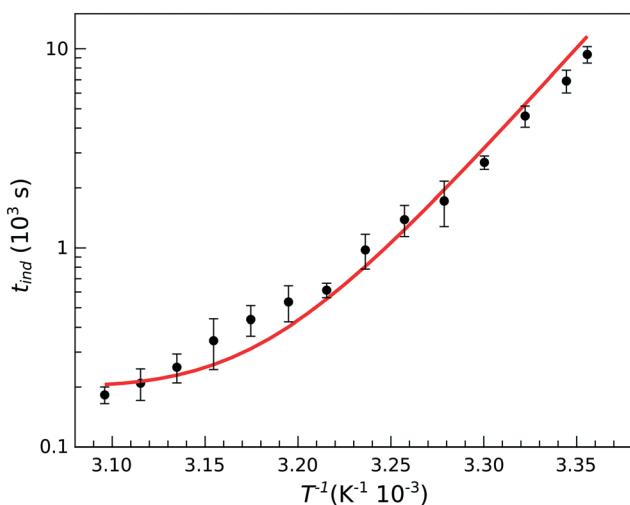
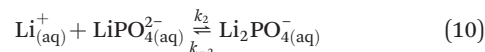
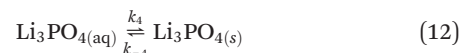


Fig. 4 Temperature dependence of the induction time for stoichiometric composition with $[\text{PO}_4^{3-}]_0 = 0.030 \text{ M}$. The solid line shows the results of modeling.

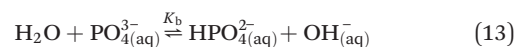
reversible reactions between lithium and phosphate ions according to



The neutral complex formed in eqn (11) will yield solid particles in a heterogeneous reaction as



Under the experimental conditions, the protonation of the phosphate ion as



is significant; therefore, eqn (13) has to be included in the model, while further protonation can be neglected, resulting in $[\text{HPO}_4^{2-}] \approx [\text{OH}^-]$. Based on these chemical reactions, we can construct the differential equations describing the temporal evolution of the species in a well-stirred system.

Lithium complexes are kinetically unstable and do not accumulate; therefore, the reverse directions of eqn (9)–(11) are favored, *i.e.*, $k_i c^0 \ll k_{-i}$ for $i \in [1,3]$ at room temperature. The overall equilibrium constant K is

$$K = \frac{k_1}{k_{-1}} \times \frac{k_2}{k_{-2}} \times \frac{k_3}{k_{-3}} \quad (14)$$

where we set $k_{-i} = 10^5 \text{ s}^{-1}$ for $i \in [1,3]$. In the heterogeneous reversible reaction of eqn (12), the backward step has zeroth order kinetics because it describes the dissolution of solid colloidal particles. The equilibrium constant associated with it can be obtained from the microreversibility condition as $K_4^{-1} = KK_{\text{sp}}$, hence k_{-4} is calculated as $k_{-4} = k_4 KK_{\text{sp}}$. The reaction between OH^- and HPO_4^{2-} is taken into account as a diffusion controlled step with $k_{\text{d}} = 10^8 \text{ dm}^3 \text{ mol}^{-1} \text{ s}^{-1}$ and $K_{\text{b}} = 0.0251$.³⁶

The differential equations are solved using the backward differentiation method of the CVODE package with a time step of 0.01 s, relative tolerance of 10^{-12} and absolute tolerance of $10^{-11} \text{ mol dm}^{-3}$. The induction time in the calculations is defined as the time required to form a sufficient amount of $\text{Li}_3\text{PO}_{4(\text{aq})}$ to make up a particle with 1 μm diameter in a $(200 \times 200 \times 200) \mu\text{m}^3$ unit volume corresponding to $1.3 \times 10^{-6} \text{ M}$ concentration.

Parameter fitting is obtained by applying the weighted least squares method on the induction times with respect to the experimentally determined values at various concentrations. For the room temperature parameter set, the values of k_i ($i = 1\dots3$) and k_4 are varied to find the best fit for all data points.

For the forward steps ($i = 1\dots3$), we follow Logan's description of diffusion controlled reactions,³⁷ for which $E_{\text{a}} =$



$\mathcal{B} + RT$ where \mathcal{B} can be expressed from the temperature dependence of dynamic viscosity as $\eta = \mathcal{A} \exp(\mathcal{B}/(RT))$. This yields $E_{(a,i)} = 19.5 \text{ kJ mol}^{-1}$ ($i = 1 \dots 3$) for our model. The activation energies are linked to the reaction enthalpy of the net reaction ($\Delta_r H^0 = 16.5 \text{ kJ mol}^{-1}$),³⁶ which we have also taken into account. In the fitting procedure, therefore, the values of $E_{(a,-i)}$ ($i = 1 \dots 3$) and $E_{(a,4)}$ are varied to find the best match for the entire data set with different temperatures. The activation energies, similarly to the rate coefficients, do not decouple for the homogeneous consecutive reaction of eqn (9)–(11), so that we use one value for them, which represents a mean activation energy and rate coefficient, respectively.

For the induction times at room temperature, there is a linear relationship between $\lg k_4$ and $\lg k_i$, ($i = 1 \dots 3$) within the best fit obtained for the experimental data, as shown by the fit parameter (Σ) representing the goodness of fit in Fig. S2 in the ESI†. The individual fits for various k_4 here remain indistinguishable (see Fig. S3 in the ESI†).

When temperature dependence is considered, the results with different values of k_4 decouple, as seen by the deviating curves in Fig. S4 in the ESI†. In addition, the appearance of a well-defined minimum for the fitting function ensures the optimization of activation energies (see Fig. S5†). With the best set of parameters, the induction times can be reconstructed by the model with an average error of 17%, which falls in the range of experimental errors (13%). The high order with respect to the reactant concentration (see Fig. 2), the dependence of induction time on supersaturation

(see Fig. S1 in the ESI†) and the decrease in the apparent activation energy (see Fig. 4) are returned by our model calculations. This results from the relations $E_{(a,i)} < E_{(a,-i)}$ and $E_{(a,4)} > E_{(a,i)}$.

3.3 Microstructure

Two different crystalline structural forms can be distinguished in the SEM images of the final product of the precipitation process, as illustrated in Fig. 5. One of the forms is a flat-sheet-like crystal, and the other is a floral shaped crystal arising from the aggregation of fractured flat-sheet-like crystals because of the agitation *via* vigorous stirring. During fracturing, defects develop where oriented attachment is favored, changing the symmetry of the final morphology.

At the induction time, flat-sheet-like crystals appear mono-dispersed with a size of $\approx 0.1 \mu\text{m}$ and a polydispersity index $\text{PDI} = 0.07$ (for definition see the ESI†) at 36°C . The crystals then start to grow and aggregate resulting in polydispersed particles of size $\approx 1.0 \mu\text{m}$ and $\text{PDI} = 0.28$. By the end of the investigation time the crystals reach $\approx 2.0 \mu\text{m}$ with a polydispersity of $\text{PDI} = 0.27$ (see Fig. 6a). A similar



Fig. 5 SEM images of particles obtained at different temperatures and at different crystallization times: (a–c) 36°C , (d–f) 50°C with $[\text{Na}_3\text{PO}_4]_0 = 0.030 \text{ M}$ and $R = 3$. The red box indicates a fully developed flat-sheet-like crystal, while the green dashed box a floral shaped crystal from aggregation.

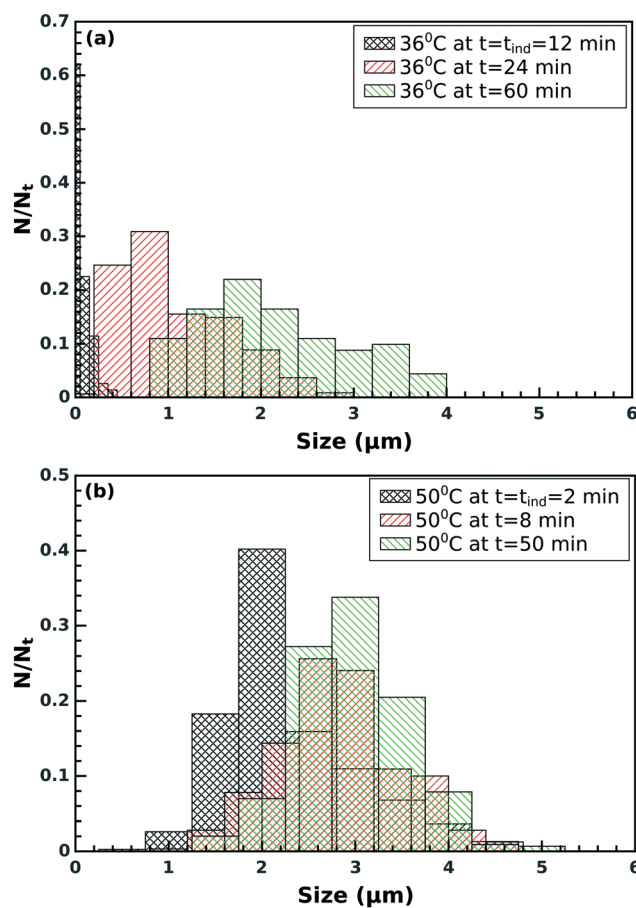


Fig. 6 Particle size distribution (a) at 36°C and (b) at 50°C at different times for flat-sheet-like crystals.



- 6 Q. Wang and O. Steinbock, Chemical garden membranes in temperature-controlled microfluidic devices, *Langmuir*, 2021, **37**, 2485–2493.
- 7 A. Yashina, F. Meldrum and A. Demello, Calcium carbonate polymorph control using droplet-based microfluidics, *Biomicrofluidics*, 2012, **6**, 22001–22011.
- 8 Y. Wang, M. Zeng, F. C. Meldrum and H. K. Christenson, Using confinement to study the crystallization pathway of calcium carbonate, *Cryst. Growth Des.*, 2017, **17**, 6787–6792.
- 9 L. Li, J. R. Sanchez, F. Kohler, A. Røyne and D. K. Dysthe, Growth of calcite in confinement, *Crystals*, 2017, **7**, 361.
- 10 L. Li, J. R. Sanchez, F. Kohler, A. Røyne and D. K. Dysthe, Microfluidic control of nucleation and growth of CaCO₃, *Cryst. Growth Des.*, 2018, **18**, 4528–4535.
- 11 B. Bohner, G. Schuszter, D. Horváth and Á. Tóth, Morphology control by flow-driven self-organizing precipitation, *Chem. Phys. Lett.*, 2015, **631–632**, 114–117.
- 12 B. Bohner, G. Schuszter, O. Berkesi, D. Horváth and Á. Tóth, Self-organization of calcium oxalate by flow-driven precipitation, *Chem. Commun.*, 2014, **50**, 4289–4291.
- 13 G. Laffite, C. Leroy, C. Bonhomme, L. Bonhomme-Coury, E. Letavernier, M. Daudon, V. Frochot, J. P. Haymann, S. Rouzière, I. T. Lucas, D. Bazin, F. Babonneau and A. Abou-Hassan, Calcium oxalate precipitation by diffusion using laminar microfluidics: toward a biomimetic model of pathological microcalcifications, *Lab Chip*, 2016, **16**, 1157–1160.
- 14 E. Tóth-Szeles, G. Schuszter, A. Tóth, Z. Kónya and D. Horváth, Flow-driven morphology control in the cobalt-oxalate system, *CrystEngComm*, 2016, **18**, 2057–2064.
- 15 E. Tóth-Szeles, B. Bohner, A. Tóth and D. Horváth, Spatial separation of copper and cobalt oxalate by flow-driven precipitation, *Cryst. Growth Des.*, 2017, **17**, 5000–5005.
- 16 F. Castro, A. Ferreira, J. A. Teixeira and F. Rocha, Protein Crystallization As a Process Step in a Novel Meso Oscillatory Flow Reactor: Study of Lysozyme Phase Behavior, *Cryst. Growth Des.*, 2016, **16**, 3748–3755.
- 17 F. Castro, A. Ferreira, J. A. Teixeira and F. Rocha, Influence of mixing intensity on lysozyme crystallization in a meso oscillatory flow reactor, *Cryst. Growth Des.*, 2018, **18**, 5940–5946.
- 18 G. Zhang, C. Verdugo-Escamilla, D. Choquesillo-Lazarte and J. M. García-Ruiz, Thermal assisted self-organization of calcium carbonate, *Nat. Commun.*, 2018, **9**, 5221.
- 19 F. Chen, D. Guo, J. Gao and Y. Ma, Bioinspired crystallization of guanine, *J. Phys. Chem. Lett.*, 2021, **12**, 11695–11702.
- 20 P. Pusztai, E. Tóth-Szeles, D. Horváth, A. Tóth, A. Kukovecz and Z. Kónya, A simple method to control the formation of cerium phosphate architectures, *CrystEngComm*, 2015, **17**, 8477–8485.
- 21 J. J. Pagano, T. Bánsági Jr. and O. Steinbock, Tube formation in reverse silica gardens, *J. Phys. Chem. C*, 2007, **111**, 9324–9329.
- 22 F. Haudin, J. H. E. Cartwright and A. De Wit, Direct and reverse chemical garden pattern grown upon injection in confined geometries, *J. Phys. Chem. C*, 2015, **119**, 15067–15076.
- 23 M. Emmanuel, D. Horváth and Á. Tóth, Flow-driven crystal growth of lithium phosphate in microchannels, *CrystEngComm*, 2020, **22**, 4887–4893.
- 24 S. Ivan and M. Egon, Homogeneous precipitation of calcium carbonates by enzyme-catalyzed reaction, *J. Colloid Interface Sci.*, 2001, **238**, 208–214.
- 25 J. Schöll, L. Vicum, M. Müller and M. Mazzotti, Precipitation of L-glutamic acid: Determination of nucleation kinetics, *Chem. Eng. Technol.*, 2006, **29**, 257–264.
- 26 N. Spanos and P. G. Koutsoukos, Kinetics of precipitation of calcium carbonate in alkaline pH at constant supersaturation. Spontaneous and seeded growth, *J. Phys. Chem. B*, 1998, **102**, 6679–6684.
- 27 T. Maqbool, P. Srikiratiwong and H. S. Fogler, Effect of temperature on the precipitation kinetics of asphaltenes, *Energy Fuels*, 2011, **25**, 694–700.
- 28 C. Brandel and J. H. ter Horst, Measuring induction times and crystal nucleation rates, *Faraday Discuss.*, 2015, **179**, 199–214.
- 29 N. P. Das, B. Müller, A. Tóth, D. Horváth and G. Schuszter, Macroscale precipitation kinetics: Towards complex precipitate structure design, *Phys. Chem. Chem. Phys.*, 2018, **20**, 19768–19775.
- 30 M. A. McDonald, H. Salami, P. R. Harris, C. E. Lagerman, X. Yang, A. S. Bommaris, M. A. Grover and R. W. Rousseau, Reactive crystallization: a review, *React. Chem. Eng.*, 2021, **6**, 364–400.
- 31 A. Forgács, K. Moldován, P. Herman, E. Baranyai, I. Fábrián, G. Lente and J. Kalmár, Kinetic model for hydrolytic nucleation and growth of TiO₂ nanoparticles, *J. Phys. Chem. C*, 2018, **122**, 19161–19170.
- 32 N. P. Das, R. Zahorán, L. Janovák, A. Imre-Deák, A. Tóth, D. Horváth and G. Schuszter, Kinetic characterization of precipitation reactions: Possible link between a phenomenological equation and reaction pathway, *Cryst. Growth Des.*, 2020, **20**, 7392–7398.
- 33 J. W. Mullin, *Crystallization*, Butterworth-Heinemann, Oxford, 2001.
- 34 O. Söhnel and J. Mullin, A method for the determination of precipitation induction periods, *J. Cryst. Growth*, 1978, **44**, 377–382.
- 35 A. Mersmann, Calculation of interfacial tensions, *J. Cryst. Growth*, 1990, **102**, 841–847.
- 36 *Handbook of Chemistry and Physics*, ed. R. C. Weast, CRC Press Inc., Cleveland, 2005.
- 37 S. Logan, Arrhenius activation energy of reactions that are almost diffusion-controlled, *J. Chem. Soc., Faraday Trans. 1*, 1977, **73**, 592–595.
- 38 C. Keffer, A. D. Mighell, F. Mauer, H. E. Swanson and S. Block, Crystal structure of twinned low-temperature lithium phosphate, *Inorg. Chem.*, 1967, **6**, 119–125.

