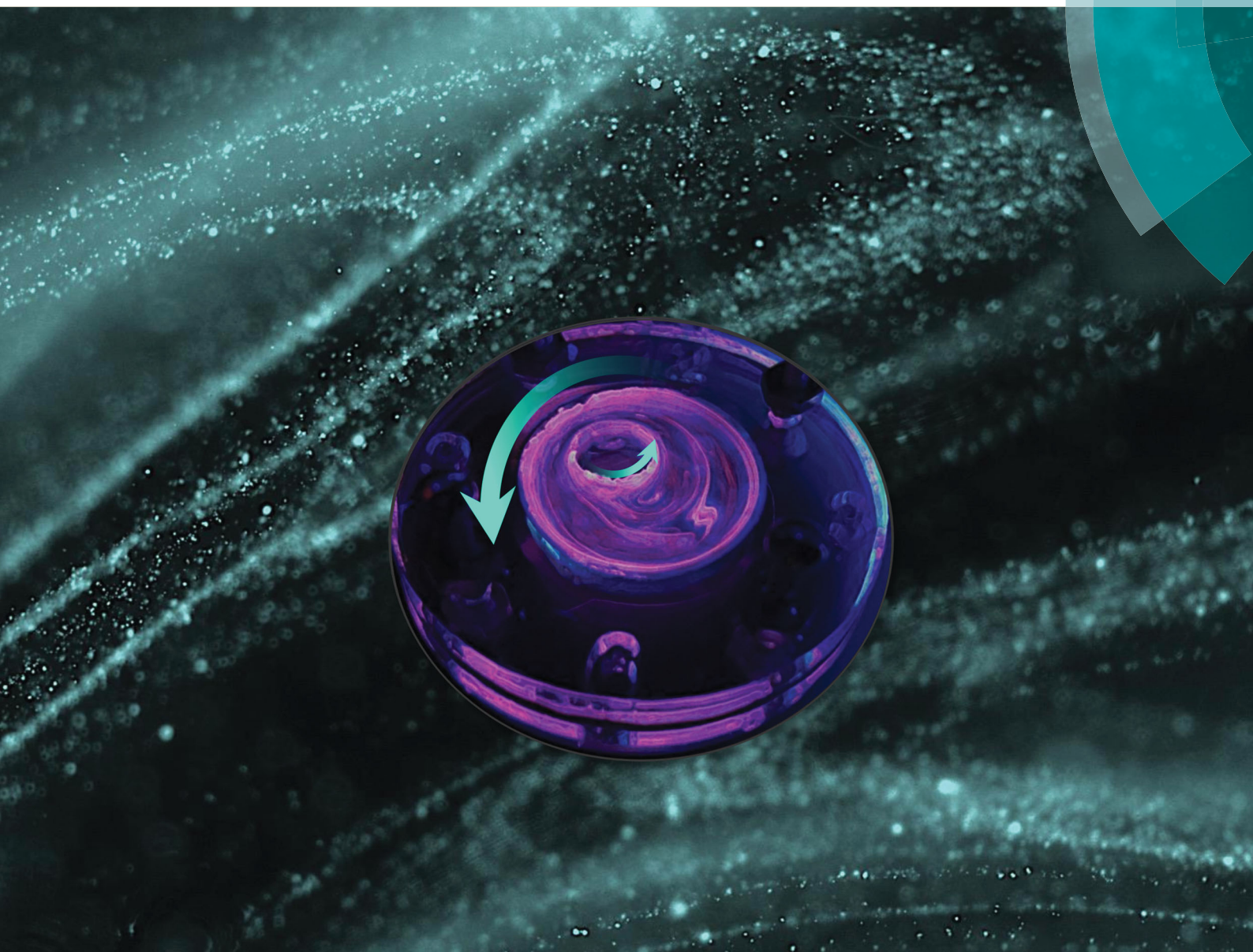


# Materials Horizons

rsc.li/materials-horizons



ISSN 2051-6347



## COMMUNICATION

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Cite this: *Mater. Horiz.*, 2018,  
5, 813Received 22nd March 2018,  
Accepted 11th June 2018

DOI: 10.1039/c8mh00344k

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# Chaotic printing: using chaos to fabricate densely packed micro- and nanostructures at high resolution and speed†

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Nature generates densely packed micro- and nanostructures to enable key functionalities in cells, tissues, and other materials. Current fabrication techniques, due to limitations in resolution and speed, are far less effective at creating microstructures. Yet, the development of extensive amounts of surface area per unit volume will enable applications and manufacturing strategies not possible today. Here, we introduce chaotic printing—the use of chaotic flows for the rapid generation of complex, high-resolution microstructures. A simple and deterministic chaotic flow is induced in a viscous liquid, and its repeated stretching and folding action deforms an “ink” (*i.e.*, a drop of a miscible liquid, fluorescent beads, or cells) at an exponential rate to render a densely packed lamellar microstructure that is then preserved by curing or photocrosslinking. This exponentially fast creation of fine microstructures exceeds the limits of resolution and speed of the currently available 3D printing techniques. Moreover, we show that the architecture of the microstructure to be created with chaotic printing can be predicted by mathematical modelling. We envision diverse applications for this technology, including the development of densely packed catalytic surfaces and highly complex multi-lamellar and multi-component tissue-like structures for biomedical and electronics applications.

## Conceptual insights

This communication presents a simple, effective, and novel printing technique—one that is rooted in chaos theory and, more precisely, in the physics of chaotic mixing in a laminar regime. The main strength and differential attribute of this novel microfabrication strategy is its ability to create a densely packed microstructure at high resolution and speed in a predictable manner. Moreover, chaotic flows are deterministic, therefore, they are amenable to rigorous modeling and the microstructure resulting from them can be predicted using computational fluid dynamics platforms. In chaotic printing, a drop of “ink” (*i.e.*, a drop of a miscible liquid, nanoparticles, or cells) is injected into a viscous and Newtonian solidifiable liquid. A chaotic flow is then applied to generate a very complex microstructure at an exponential rate, which is then preserved by a crosslinking or curing step. This exponentially fast creation of a linear structure (meters), and the accompanying rapid decrease in the length scales of the micro- and even nano-structure, is not currently achievable by any other 3D printing technique. We envision the use of this platform for many relevant applications such as the fabrication of complex tissues, catalytic surfaces, supercapacitors, and highly reinforced materials, among others.

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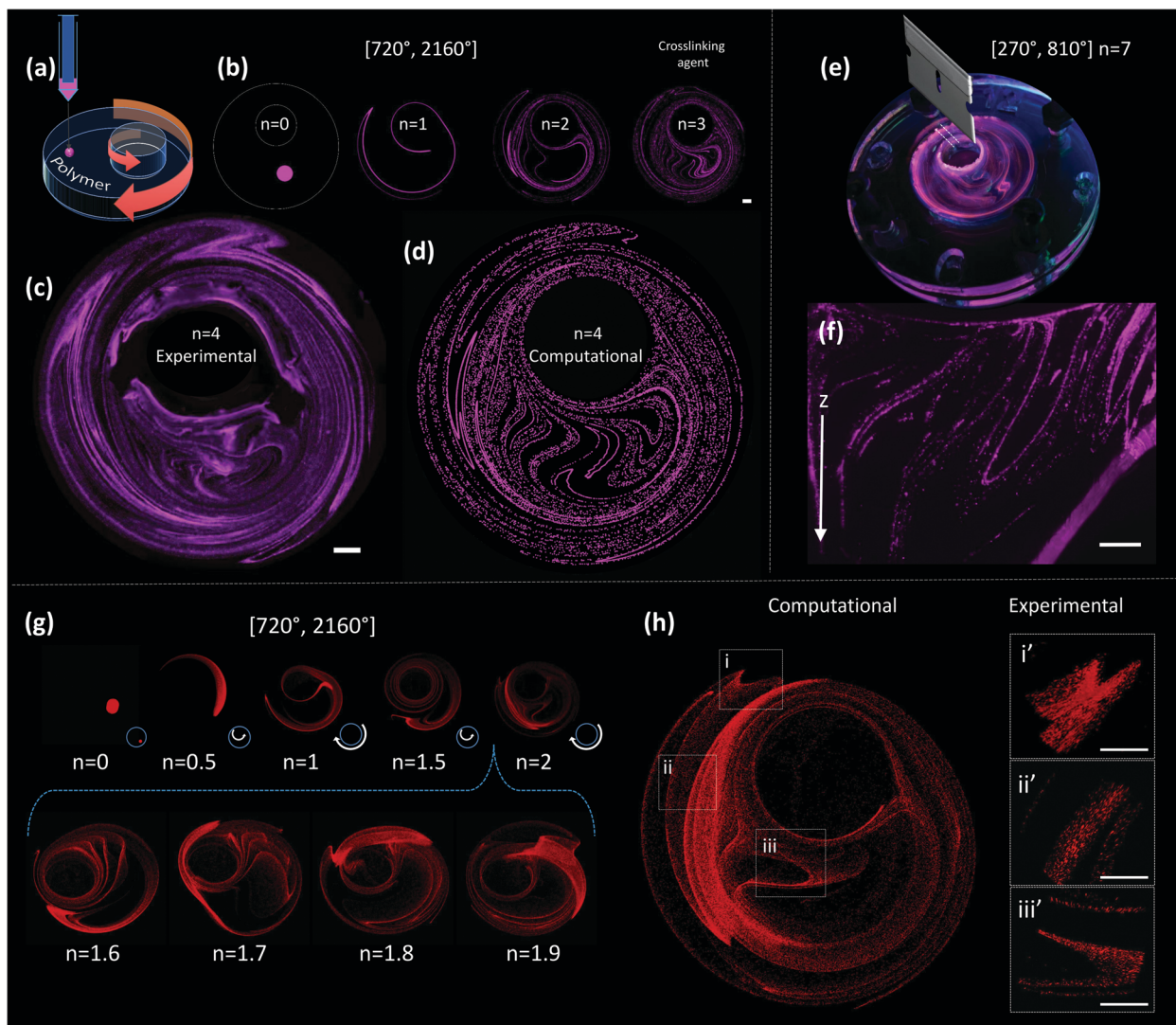
† Electronic supplementary information (ESI) available. See DOI: 10.1039/c8mh00344k



any given number of flow cycles (Fig. 2b). In our experiments, we used gelatin methacryloyl<sup>40</sup> (GelMA) and polydimethylsiloxane (PDMS) as liquid polymers.‡

Fig. 2c shows a construct fabricated by injecting fluorescent microparticles into a liquid GelMA pre-polymer and allowing the flow to operate for 4 complete flow cycles ( $n = 4$ ). A chaotic flow was induced by a clockwise rotation of  $720^\circ$  of the outer cylinder, followed by a counter-clockwise rotation of  $2160^\circ$  of the inner cylinder [ $720^\circ, 2160^\circ$ ]. For the specific miniJB

geometry that we used, this protocol induces a globally chaotic flow (Fig. S2, ESI†) that creates a structure by the repeated reorientation and deformation of the fluid that promotes stretching and folding.<sup>33,41</sup> Such a simple iterative process drives the development of complex structures, and enables the creation of progressively finer patterns, moving from macro to micro and even nano-scales. The final structure was then solidified by simply exposing the GelMA pre-polymer to UV light for 30 seconds.



**Fig. 2** Chaotic printing of microstructures in curable polymers using a miniaturized journal bearing (miniJB) flow system: experiments and computational fluid dynamics (CFD) simulations. (a) The injection of a drop of ink between two eccentrically located cylinders rotating alternately in opposite directions; (b) results in the development of a complex microstructure after a few applications of the flow [ $\alpha^\circ, \beta^\circ$ ] that can be preserved by curing or crosslinking. The direct simulation of JB flows, by solving the Navier–Stokes equations (using 2D CFD simulations), enables the prediction of the microstructure at any time point. Predicted microstructure evolution for an experiment in which there is a drop of fluorescent particles in a JB flow for the first three flow cycles of a mixing protocol [ $720^\circ, 2160^\circ$ ]. (c) Chaotic structure experimentally produced after 4 cycles; and (d) 2D-CFD simulation of the dispersion of an injection of massless particles using the same mixing protocol. Scale bars: 1 mm. (e) The resulting microstructure is 3D in nature. A cross-section of a construct produced by chaotic mixing [ $270^\circ, 810^\circ$ ]  $n = 7$  is (f) examined under a microscope, revealing a complex 3D lamellar structure in the  $z$  direction. Scale bar:  $500 \mu\text{m}$ . (g) The evolution of the microstructure of any given JB flow recipe can be accurately predicted using 3D CFD simulations of the dispersion of a circular drop in a chaotic flow [ $720^\circ, 2160^\circ$ ]. The resulting microstructure is depicted at different times: after  $n = 0, 0.5, 1.0, 1.5, 1.6, 1.7, 1.8, 1.9$ , and  $2.0$  flow cycles, respectively. (h) 3D simulations accurately reproduce structural features of the microstructure obtained experimentally. Three sections in the simulation (i, ii, and iii) are compared with images, obtained by confocal microscopy, of an experimentally obtained construct (insets i', ii' and iii'). Scale bar: 1 mm.



Since the chaotic flows that we used to print are deterministic (*i.e.*, they are governed by the Navier–Stokes equations of motion), the process of particle convection and the generation of structures can be modelled (Fig. 2). Our simulations closely reproduce the behaviour of the actual experimental systems; therefore, they enable the prediction of microstructures with specific desired characteristics. For instance, the simple 2D simulations presented in Fig. 2b and d allow an accurate prediction, at a low computing investment, of the structure observed at the top layer of the experimentally obtained construct (Fig. 2c).

The sole observation of this top layer of the microstructure may convey the idea of the existence of a surface 2D flow. However, our miniJB flow is capable, by design, of producing highly complex 3D flows (and therefore 3D microstructures). The asymmetry in the boundary conditions at the top and bottom fluid layers—the top layer is a free surface while the bottom one is solid and rotates—creates a fully 3D flow.

Fig. 2e and f show a cross-sectional image of a PDMS-based construct fabricated through chaotic 3D printing (protocol  $[270^\circ, 810^\circ]$ ,  $n = 7$ )<sup>‡</sup>; the structure is evidently 3D, and a membrane-like structure is clearly depicted in the  $Z$  plane. Each layer of material, from top to bottom, is topologically different and the geometric features of the entire construct are continuous. The 3D nature of the microstructure generated by our miniJB flow system is described by the computational solution of the equations of motion in 3D (Fig. 2g and h). Fig. 2g shows the evolution of the shape of a drop of ink (a cylindrical array of 120 000 massless particles) into a highly convoluted 3D continuous micro-sheet that rapidly invades the flow domain. Our simulations are capable of reproducing, with high accuracy, the characteristic features observed in the experimentally obtained constructs (Fig. 2h).

## Printing at high resolution and speed

In chaotic flows, stretching proceeds at an exponential rate. Consequently, whereas regular flows produce interfaces that grow linearly (Fig. 3a), chaotic flows develop the structure at an exponential rate (Fig. 3b); in a chaotic flow, any material filament grows exponentially in time, closely following the following model:

$$(L/L_0) = \exp(\Lambda n), \quad (1)$$

where  $L$  is the length of the filament after  $n$  flow cycles,  $L_0$  is the length of the filament at an initial time, and  $\Lambda$  is the Lyapunov exponent of the flow.

The  $\Lambda$  value<sup>36,37,42</sup> is a quantity that can be used to estimate the speed of advance of the chaotic process. Therefore,  $\Lambda$  conveys a profound physical meaning for a chaotic flow: it describes, within a single value, the overall potential for the flow to stretch the material, cause elongation, and generate the structure. Fig. 3 describes the determination of  $\Lambda$ , based on 2D numerical simulations.

We calculated and recorded, every quarter-a-cycle, the evolution of the length of a filament initially located at the centre

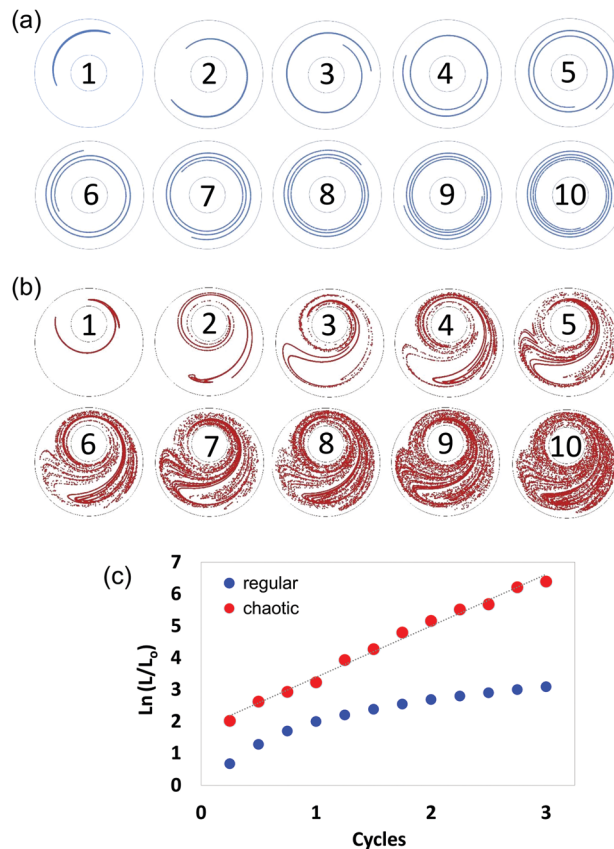


Fig. 3 Calculation of the Lyapunov exponent ( $\Lambda$ ) for 2D JB flows. A drop composed of 10 000 points is located at time  $t = 0$  in an initial position, in (a) a concentric or (b) an eccentric JB flow. In both cases, the mixing protocol used was  $[270^\circ$  and  $810^\circ]$ . The linear (blue) or exponential (red) evolution of the filament, as stretched and folded by the (a) regular or (b) chaotic flow, is depicted for 10 full flow cycles. (c) The length of the filament ( $L/L_0$ ), as deformed by the flow, is calculated at each  $\frac{1}{4}$  flow cycle and plotted. For the regular flow the advance of the length ( $L/L_0$ ) is linear (blue symbols), while for the chaotic flow this advance is exponential (red symbols). The  $\Lambda$  value of the flow can be calculated from the slope of the straight line ( $\ln(L/L_0)$  vs. time). For this particular 2D JB case  $\Lambda = 1.61 \text{ cycle}^{-1}$ .

line between the two cylinders as they rotated at 5 rpm—this was done both for a globally chaotic miniJB case  $[270^\circ, 810^\circ]$  and for a regular flow case  $[270^\circ, 810^\circ]$  (centred JB configuration). A Lyapunov exponent value of  $1.61 \text{ cycle}^{-1}$  was determined from the slope of the linear version of eqn (1) (Fig. 3c).

Once the  $\Lambda$  is known,<sup>§</sup> some simple additional calculations can be done. For example, Fig. 4a shows an estimation of the length of a progressively deformed filament that was produced by the repeated stretching and folding of a fluid segment of 1000  $\mu\text{m}$  in a 2D model chaotic flow characterized for  $\Lambda = 1.61 \text{ cycle}^{-1}$ . This segment could be elongated into a fibre of 3.13 m length after only 5 flow cycles (equivalent to 3 min at our operational speed of 5 rpm). By comparison, an extrusion-3D professional printer prints at a maximum speed of  $1.2 \text{ cm s}^{-1}$  for resolutions of 200  $\mu\text{m}$ .<sup>43</sup> The currently available nozzle-based bioprinting techniques exhibit a speed limit between 10 and 50  $\mu\text{m s}^{-1}$  for resolutions between 50 and 200  $\mu\text{m}$ .<sup>29</sup>



At maximum speed, an average professional 3D printer, and a nozzle-based 3D bioprinter, will print the same segment (3.13 m long) in 43.47 min and 17.38 h, respectively (Tables S1 and S2, ESI†).

Our calculations also suggest that chaotic printing can generate finer features faster than conventional linear printers. In our chaotic printing system, any growing segment of interface has to be accommodated within the finite volume between cylinders, which results in a densely packed microstructure.

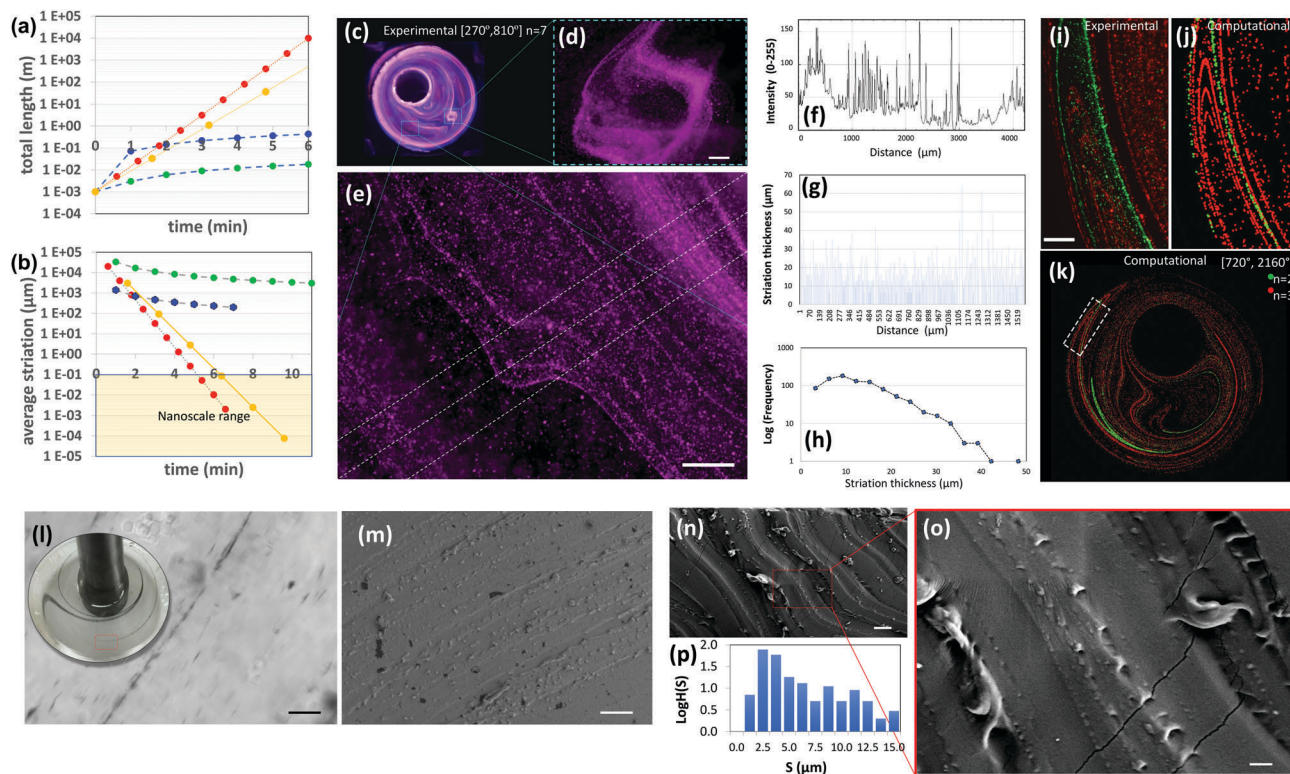
Therefore, this exponential growth rate implies the creation of a great expanse of interface<sup>33,37</sup> in a small area and in a few flow cycles (Fig. 2c and Fig. S3, ESI†).

In Fig. 4b, we have calculated the evolution in time of the average striation thickness resulting from the repeated operation of an ideal 2D chaotic printer characterized by  $\Lambda = 2.68 \text{ min}^{-1}$ , an average speed professional 3D printer printing at  $1.2 \text{ mm s}^{-1}$ ,<sup>43</sup> and a nozzle-based state of the art

3D bioprinter printing at  $50 \mu\text{m s}^{-1}$ <sup>29</sup> on a square section of  $1 \text{ cm}^2$ . Remarkably, our simple chaotic printer will produce an average striation thickness of 10 nm after 10 flow cycles (6 minutes) (Fig. 4b; Fig. S3 and Table S1, ESI†).

Fig. 4c–e show a PDMS construct obtained by 3D chaotic printing using an ink composed of fluorescent microparticles suspended in PDMS. The multiple sheets of particles were observed in remarkable alignment and packed in a nearly parallel fashion (Fig. 4e).

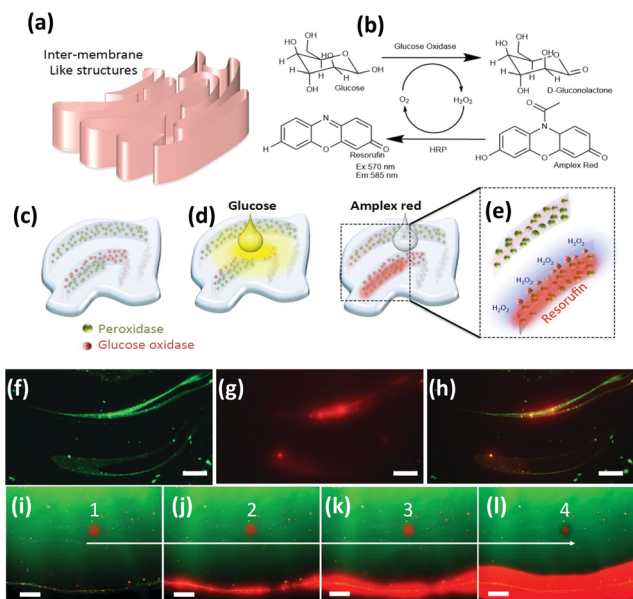
Based on a simple image analysis conducted by measuring the sum of the length of particle lines per unit of surface area in that particular plane,  $\sim 7.10 \text{ m per cm}^2$  of interface was developed in a few flow periods ( $n = 7$ ). The resolution of this microstructure is exceptionally fine. In agreement with our theoretical estimates, in some regions of the flow, the distance between adjacent lamellae (striation thickness) is less than  $10 \mu\text{m}$  (Fig. 4e–h), a value that equals or exceeds the resolution



**Fig. 4** Highly aligned micro and nano structures produced by chaotic printing. (a) The growth of surface area and, (b) the reduction in striation thickness achievable by a chaotic printing process characterized by  $\Lambda = 1.61 \text{ cycle}^{-1} = 2.68 \text{ min}^{-1}$  at 5 rpm (red symbols); by chaotic printing characterized by  $\Lambda = 3.50 \text{ cycle}^{-1} = 2.18 \text{ min}^{-1}$  at 5 rpm (yellow symbols); by a state-of-the-art extrusion 3D printer<sup>43</sup> (blue symbols), and by a state-of-the-art extrusion bioprinter<sup>29</sup> (green symbols). (c) Fluorescent microparticles (2–15  $\mu\text{m}$  in diameter), chaotically printed in PDMS using the protocol  $[270^\circ, 810^\circ] n = 7$ , are aligned to the chaotic flow manifold to reveal a complex 3D microstructure; (d and e) close-ups of two regions within the construct. After seven flow iterations, repeated folding and stretching yields alignment at the micro scale, and (e and f) develop a densely packed microstructure composed of parallel lamella; (g) in some regions of the flow, after three flow iterations, this separation is on the order of tens of microns. (h) The striation thickness distribution (STD) can be calculated from the estimation of the space between neighbour striations using image analysis techniques. (i) The microstructure resulting from the injection of two different types of microparticles at two different time points ( $n = 2$ , green;  $n = 3$ , red) and locations; both particle sets are aligned to the flow manifold to produce a highly aligned microstructure, as revealed by experiments and (j and k) CFD simulations. Scale bars: 500  $\mu\text{m}$ . (l) The injection of a drop of a silver nanowire suspension into GelMA under a chaotic miniJB flow  $[270^\circ, 810^\circ] n = 4$ . The chaotic flow rapidly stretches the pointwise injection into strings of nanowires aligned on the micro-scale. A close-up of a particular region of the construct reveals a high level of alignment and resolution. Individual nanowires rotate and align to the flow manifold. (m) Parallel strains of carbon nanoparticles in a PDMS construct  $[720^\circ, 2160^\circ] n = 4$ . Similarly, (n and o) gold nanoparticles chaotically printed in PDMS align to the flow manifold  $[720^\circ, 2160^\circ] n = 4$ . (p) STD ( $\log H(S)$ ) of the microstructure as determined by image analysis techniques. Scale bars: (l) 50  $\mu\text{m}$ ; (m) 20  $\mu\text{m}$ ; (n) 10  $\mu\text{m}$ ; (o) 2  $\mu\text{m}$ .



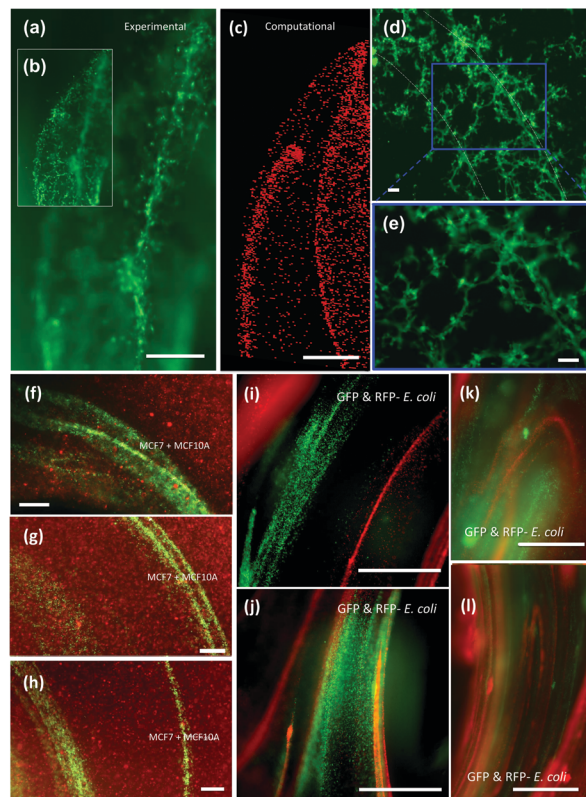




**Fig. 5** Chaotic bioprinting of enzymes. Microfabrication of (a) catalytic surfaces inspired by internal cell membranes. (b) Schematic of a sequential reactive enzymatic system composed of glucose oxidase and peroxidase (c) immobilized into nanoparticles and chaotically printed in GelMA hydrogels. (d) Glucose is added to the constructs and (e) the local reaction rate and extent is visualized by the change in colour (colorless to red). (f) Experiment in which green nanoparticles functionalized with either enzyme were co-injected; (g and h) the extent of the local reaction is denoted by the development of red fluorescence in the membrane sections. (i–l) Reaction front as revealed after 5, 15, 30 and 60 seconds, respectively. Scale bars: 500  $\mu$ m.

with the currently available bioprinting techniques, but this level of precise control is an indispensable requirement for the creation of multilayered tissue-like constructs. Our miniJB flow allows the printing of multi-layers of one or more particle type (single or multiple bio-inks), within the same matrix and in a single operation (Fig. 6a–c and Fig. S4, ESI<sup>†</sup>). Each injection rapidly aligns to the manifold of the flow, due to the property of AD. We used inks composed of HUVEC suspensions and GelMA-VEGF (GelMA covalently functionalized with vascular endothelial growth factor or VEGF<sup>51</sup>) to print layers of cells in GelMA matrices. This alignment yields a highly ordered structure that closely resembles the multi-layered tissue structures of complex mammalian tissues (e.g., skin, cancerous tissue encapsulated in healthy organs, pancreatic tissue, and brain pathways).<sup>52</sup> Chaotic bioprinting is cell friendly. The cells are minimally exposed to shear forces during injection with conventional pipettes and later during exposure to laminar flows. We observed mammalian cell viability in the range of 90 to 97% after printing. Cells preserved their original seeding position during the first 96 hours of culture (Fig. 6a and b), spread at later times, using the flow structural template, and reached across lines to establish connections between neighbouring lamellae to develop complex tissue-like structures (Fig. 6d, e and Fig. S4, S5, ESI<sup>†</sup>). As shown earlier, the resulting structure can be accurately predicted by CFD simulations (Fig. 6c).

The microstructure fabrication strategy proposed here can be applied to many relevant biological and biomedical engineering



**Fig. 6** Chaotic bioprinting of cells. (a) Sheets of HUVECs expressing green fluorescent protein (HUVEC-GFP) were chaotically printed in a GelMA construct and observed using optical fluorescence microscopy; (b) a different focal plane of the same region of the construct reveals the three-dimensional nature of the structure. (c) Simulations show similar features within the same region. Scale bars: 500  $\mu$ m. (d and e) HUVEC-GFP, chaotically co-printed in GelMA containing VEGF (VEGF-GelMA). The cells first spread along a string defined by the chaotic flow manifold, and they subsequently connect across lines after 96 hours of culture, as observed by optical microscopy. Scale bars: 100  $\mu$ m. (f–h) Different degrees of intimacy of MCF7 cancerous (red) and MCF10A healthy (green) cells co-printed in the same construct [ $270^\circ$ ,  $810^\circ$ ]  $n = 3$ . Scale bars: 500  $\mu$ m. (i–k) Bioprinting of GFP + RFP *E. coli* (green and red fluorescent bacteria) using the protocol [ $270^\circ$ ,  $810^\circ$ ]. Different degrees of intimacy between lines of the green and red bacteria appear as time advances: (i)  $n = 3$ ; (j)  $n = 4$ ; (k)  $n = 7$ . (l) Bioprinting of GFP + RFP *E. coli* (green and red fluorescent bacteria) using a globally chaotic protocol [ $720^\circ$ ,  $2160^\circ$ ] at  $n = 2$ . Scale bars: 500  $\mu$ m.

scenarios, ranging from the study of fundamental questions related to cell–cell interactions at microbial communities or tissue interfaces to the development of organ-on-a-chip platforms.

Fig. 6f shows a 3D printed construct containing both MCF7 (breast cancer cells, red stained) and MCF10A (noncancerous breast tissue fibroblasts, green stained). A significant amount of interface between the cancerous and normal cells develops after 3 flow cycles. At low cycles, the different degrees of intimacy between cancerous and normal tissue can be observed at different locations within the same construct (Fig. 6f–h). This enables the study of the effect of a variety of degrees of spatial interaction between cancerous and healthy tissue under the same experimental conditions. Greater intimacy between different types of cells can also be achieved simply by increasing





the number of flow applications. For example, we printed bacterial communities of red (the producers of red fluorescent proteins [RFP]) and green (the producers of green fluorescent proteins [GFP]) *Escherichia coli* with different degrees of proximity by varying the number of printing cycles. At  $n = 3$ , *E. coli*-GFP and *E. coli*-RFP are planted along different branches of the flow manifold. At  $n = 4$ , sections populated by the lines of GFP-bacteria are flanked by RFP-bacterial lamella. At higher cycles, a great amount of interface is shared between both cell types (Fig. 6k). Also, the STD (and the degree of intimacy between cell types) can be tuned by selecting different mixing protocols; protocols with higher  $\lambda$  generate greater intimacy in fewer cycles (Fig. 6l). The results can be anticipated through simulations or experiments using simpler model systems, such as particles and PDMS. The use of two or more polymers to fabricate composites with long embedded sheets (and therefore high interfacial surfaces) might also have diverse and relevant applications. We conducted chaotic printing experiments in which a drop of gelatin was dispensed in the GelMA pregel in our miniJB flow. In these constructs, only the GelMA fluid pregel is crosslinked after exposure to UV light; the gelatin sheet, rhodamine stained, remains as a soft gel and serves as a sacrificial component that melts rapidly at 37 °C, leaving a convoluted empty space in the form of an embedded continuous microstructure (Fig. S4, ESI†). We envision the use of this simple technique for the fabrication of convoluted sacrificial microstructures that might improve the mass transfer within thick cell-laden constructs or for the design and fabrication of micro-vasculature in tissue engineering applications.

Since the chaotic flows we used are deterministic, the dynamics of the printing processes is governed by the equations of motion that are solvable numerically for laminar regime conditions. Therefore, the outcome of the printing process, the resulting microstructure, is predictable for any given chaotic flow system.

Chaotic printing might be a powerful enabler. Remarkably complex microstructures can be fabricated, in a predictable manner, within solidifiable polymers and hydrogels, using chaotic flows generated in a simple “lab-made” printer composed of stepper motors and an Arduino-based controller (Fig. 1 and Fig. S6, ESI†). We conducted experiments and simulations using another chaotic flow. In principle, any research group would easily be able to produce a version of a chaotic printer with a minimum investment. We have mainly presented 3D printing experiments and simulations using different JB protocols. However, in principle, any realizable chaotic flow could be used as a chaotic printer.

We envision chaotic printing as a versatile micro- and nanofabrication platform that can be applied for the facile creation of constructs with unique properties: composites containing hundreds of meters of interface per area unit between materials, long filaments or sheets with a highly defined geometry embedded within hydrogels, thin and conductive sheets within insulating polymeric matrices, catalytic surfaces bioinspired in the architecture of internal cellular membranes, and tissue-like living structures.

## Conclusions

Chaotic printing is a technological platform rooted in strong fundamental concepts. Chaotic flows exhibit an ability to create a self-similar microstructure at an exponential rate<sup>33,36</sup> due to their inherent properties, which include the existence of a unique flow intrinsic template and AD. The iterative character of a chaotic flow enables the creation of progressively finer patterns, moving from macro to micro and nano-scales. Ink drops will rapidly elongate by the action of the chaotic flow to produce 3D sheets with a total length that will grow exponentially and rapidly to reach hundreds of centimetres after a few flow cycles. In volume preserving systems, this exponential increase in length aligned to the flow manifold will necessarily imply a contraction in other dimensions.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

GTdS acknowledges the funding received from CONACyT (scholarship 234713) and Fundación México en Harvard in the form of postdoctoral scholarships. MMA acknowledges the institutional funding received from Tecnológico de Monterrey (GEE-002EICIN01), and funding provided by CONACyT (Consejo Nacional de Ciencia y Tecnología, México) in the form of a sabbatical scholarship (262130, SNI-26048). AK acknowledges funding from the National Science Foundation (EFRI-1240443), IMMODGEL (602694), and the National Institutes of Health (EB012597, AR057837, DE021468, HL099073, AI105024 and AR063745). NA acknowledges the support from the American Heart Association (AHA, 16SDG31280010), FY17 TIER 1 Interdisciplinary Research Seed Grants, the Northeastern University, and the startup fund provided by the Department of Chemical Engineering, College of Engineering at Northeastern University. YSZ acknowledges funding from the National Cancer Institute of the National Institutes of Health (K99CA201603). This research has been partially funded by the Tecnológico de Monterrey and the Massachusetts Institute of Technology (MIT) Nanotechnology Program, and the MIT International Science and Technology Initiatives (MISTI). We gratefully acknowledge the experimental contribution of Patrick Boisvert, Research Specialist in the Electron Microscopy Facilities at the Centre for Material Sciences and Engineering (CMSE) at MIT, and Sara Cristina Pedroza-González, Everardo González-González, Alan Roberto Márquez-Ipiña, Brenda Giselle Flores-Garza, David Choy-Buentello, Felipe López-Pacheco, and Ricardo García-Ramírez at Tecnológico de Monterrey. We sincerely thank Professor Troy Shinbrot, at Rutgers University, for repeatedly reading and extensively commenting on this work.

## Notes and references

‡ Gelatine methacryloyl (GelMA) is a UV cross-linkable material that has been widely used in tissue engineering applications; it contains cell



binding domains, and it is biodegradable, and amenable to micro-fabrication. Polydimethylsiloxane (PDMS) is arguably the most widely used silicon-based organic polymer. In our PDMS experiments, solidification was achieved by slowly curing on a vibration-free surface at room temperature overnight.

§ The units of the Lyapunov exponent ( $\lambda$ ) can be converted from cycles to seconds simply by considering the speed of rotation of the cylinders [rpm] and the angle of rotation of the mixing protocol. For instance, at 5 rpm (the rotational speed used in our experiments),  $\lambda = 1.61 \text{ cycle}^{-1} = 2.68 \text{ s}^{-1}$  for the mixing protocol [270°, 810°]. At 5 rpm,  $\lambda = 3.50 \text{ cycles}^{-1} = 2.18 \text{ s}^{-1}$  for the mixing protocol [720°, 2160°].

¶ For example, in an ideal chaotic flow occurring on a surface, the mean distance between consecutive lamellae (striation thickness) decreases proportionally to  $S^{0.5}/L_n$ , where  $S$  is the surface area of the system and  $L_n$  is the length of the stretched and folded filament at any given flow cycle (Fig. S3, ESI†).

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