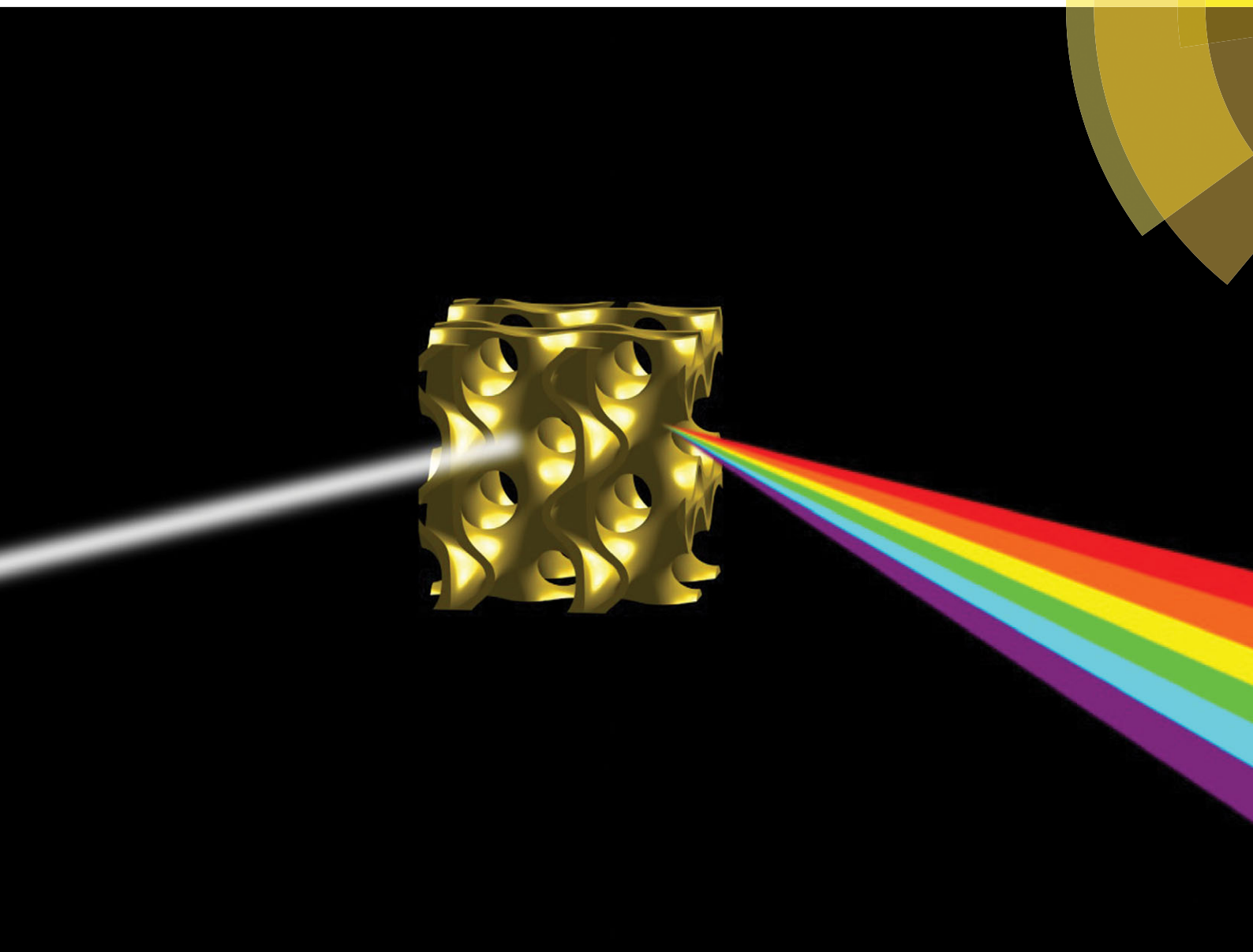


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Block copolymer self-assembly for nanophotonics

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The ability to control and modulate the interaction of light with matter is crucial to achieve desired optical properties including reflection, transmission, and selective polarization. Photonic materials rely upon precise control over the composition and morphology to establish periodic interactions with light on the wavelength and sub-wavelength length scales. Supramolecular assembly provides a natural solution allowing the encoding of a desired 3D architecture into the chemical building blocks and assembly conditions. The compatibility with solution processing and low-overhead manufacturing is a significant advantage over more complex approaches such as lithography or colloidal assembly. Here we review recent advances on photonic architectures derived from block copolymers and highlight the influence and complexity of processing pathways. Notable examples that have emerged from this unique synthesis platform include Bragg reflectors, antireflective coatings, and chiral metamaterials. We further predict expanded photonic capabilities and limits of these approaches in light of future developments of the field.

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1 Introduction

From informatics to alternative energy, the ability to control light–matter interactions on the nanoscale is crucial to a wide gamut of applications. Whether the goal is to trap or guide light within photonic bandgap materials, enhance certain reflections (e.g. for structural color), prevent reflections for enhanced light harvesting, or the polarization of light, the ability to control on the nanoscale the spatial organization of materials has progressed



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Morgan Stefik obtained a degree in Materials Engineering from Cal Poly SLO in 2005 before completing doctoral studies in Materials Science at Cornell University under Prof. U. Wiesner and Prof. F. J. DiSalvo in 2010. After two years of postdoctoral research at École Polytechnique Fédérale de Lausanne with Prof. M. Grätzel, he joined the University of South Carolina in 2013 as an Assistant Professor in the Department of Chemistry and Biochemistry. He is the founding director of the NSF supported South Carolina SAXS Collaborative. His research focuses on nanomaterials chemistry with emphasis on self-assembly techniques and atomic layer deposition.



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Stefan Guldin graduated in physics from the Technical University Munich and then pursued doctoral research with Prof. Ullrich Steiner at the University of Cambridge, where he obtained a PhD in 2012. He then moved to École Polytechnique Fédérale de Lausanne to work with Prof. Francesco Stellacci as a postdoctoral fellow of the German Academy of Sciences. Recently he has been appointed as a University Lecturer and now heads the Adaptive and Responsive Nanomaterials Group at University College London, Department of Chemical Engineering. His research interests include the self-assembly of soft & hybrid matter, adaptive and responsive materials architectures and light–matter interaction.



from a fundamental question to a technological need. With the promise of widespread benefits from this new generation of nanostructured materials, the main question today is: "How can we fabricate functional nanomaterials in a truly scalable fashion?". Historically materials science has focused on top-down lithographic approaches and on colloidal self-assembly to gain access to periodic material arrangements on the length scale of visible light. Supramolecular assembly provides a powerful alternative, where the structure formation is controllable on a smaller sub-wavelength 5–100 nm length scale that opens the possibility of mesoporous structures and metamaterials that are active at visible wavelengths. Such material architectures have a wide range of tunable symmetries and a remarkable range of accessible compositions.

Here we review promising block copolymer pathways for nanophotonics, covering a wide spectrum of processing conditions



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Silvia Vignolini studied physics at the University of Florence, Italy and in 2009 she was awarded a PhD in Physics. During her PhD, she studied light-matter interaction in the near-field regime in the group Prof. D. Wiersma at the European Laboratory for non-Linear Spectroscopy in Florence. In 2010, she joined the group of Prof. U. Steiner as a research associate at the Cavendish Laboratory in Cambridge, UK. After three years of work on optical properties of soft materials, she was awarded a BBSRC David Philip Fellowship. She joined the Chemistry Department in Cambridge as a Lecturer in 2014, and she has been awarded the ERC starting grant.

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Ulrich (Uli) Wiesner studied chemistry at the University of Mainz, Germany, and UC Irvine, CA, gaining his PhD in 1991 with work under Prof. H. W. Spiess at the Max-Planck-Institute for Polymer Research, Mainz. After a two year postdoc at the Ecole Supérieure de Physique et de Chimie Industrielle de la ville de Paris (E.S.P.C.I.) with Prof. L. Monnerie, he returned to the group of Prof. H. W. Spiess in 1993 where he finished his Habilitation in 1998. He joined the Cornell University, NY, MS&E faculty in 1999 as a tenured Associate Professor, became a Full Professor in 2005, and since 2008 is the Spencer T. Olin Professor of Engineering.

Ulrich (Uli) Wiesner studied chemistry at the University of Mainz, Germany, and UC Irvine, CA, gaining his PhD in 1991 with work under Prof. H. W. Spiess at the Max-Planck-Institute for Polymer Research, Mainz. After a two year postdoc at the Ecole Supérieure de Physique et de Chimie Industrielle de la ville de Paris (E.S.P.C.I.) with Prof. L. Monnerie, he returned to the group of Prof. H. W. Spiess in 1993 where he finished his

and morphologies as well as a range of optical constants and anisotropies. Despite the nuanced processing complexity, such block copolymer based nanophotonics remain in principle compatible with solution processing such as spin coating, dip coating, or roll-to-roll fabrication. Most polymers are commodity materials where the constituent monomers cost only pennies per gram and the controlled chain-growth synthesis techniques needed to make block copolymers are routinely deployed at the industrial scale.¹

2 Nanostructures for photonics

For a photonic bandgap or antireflective properties, the periodic spatial modulation of the refractive index has to be comparable to the incident wavelength. The scattering of photons occurs at interfaces of differing refractive index and the resulting constructive or destructive interference arises from the particular nanostructure geometry. The modulation of visible photons with 400–700 nm wavelengths is thus rarely accommodated directly by block copolymers due to the challenges of forming such large unit cells (Section 3.1.3) as well as the typically low refractive index contrast between the polymer blocks (Section 4). However, inorganic nanostructures generated from block copolymers enable access to larger refractive indices and higher refractive index contrasts. The tunability of refractive index with porous inorganic layers thus enables the modulation of refractive index with controlled layer thickness on the length scale of visible wavelengths (Section 3.2).

Although the typical 5–100 nm block copolymer unit cell dimensions are not suitable for visible photonic bandgaps, they are ideal scaffolds for the fabrication of metamaterials. The relevant optical parameters for metamaterials require spatial modulation on a sub-wavelength regime. In non-resonant dielectrics, light propagates across the material, averaging over its morphology, yielding a medium with designable permittivity and permeability.



Ullrich Steiner

Ullrich (Ulli) Steiner studied physics at the University of Konstanz, Germany. He gained his PhD in 1993, working with Prof. J Klein and Prof. G. Schatz at the Weizmann Institute, Israel. After post-doc positions at the Weizmann Institute and the Institute Charles Sadron, France, he returned to Konstanz where he finished his Habilitation in 1998. He joined the faculty of the University of Groningen as full professor in 1999 and became the John Humphrey Plummer Professor of Physics of Materials at the University of Cambridge in 2004. Since 2014, he holds the chair of Soft Matter Physics at the Adolphe Merkle Institute in Switzerland.

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This behavior is no longer determined by macroscopic structural parameters of material assemblies, but from their composition and geometries that act as “artificial atoms.” This effect, also termed “optical crowding,” is particularly useful for the creation of materials with very low refractive indices. Materials in which the electron system is resonant with respect to the incident light, such as in metals, the propagating resonant electronic modes (plasmon-polaritons) determine the optical properties of sub-micrometer structured materials. For example, efficient wave guide design requires sufficient propagating modes and limited energy dissipation, both of which may be improved by decreasing the local thickness of metallic nanostructures. Based on predictions by Pendry *et al.* in 1999,^{2,3} numerous examples of metamaterials have emerged with fascinating and unusual optical properties based upon the precise spatial arrangement of conventional materials into suitable architectures. The possibility of achieving a negative refractive index and super-lensing has intrigued many groups and caused a flurry of activity in this field.

The production of nanophotonics is often accomplished with complex and costly photolithographic techniques. Here, block copolymers are an ideal platform to develop tuned nanomaterials with a wide range of accessible structures and length scales. The reliance on self-assembly approaches considerably reduces overhead costs since they are widely based on solution processing and are thus directly compatible with future industrial upscaling. Below we outline how the particular block copolymer processing methodologies result in different types of nanostructure symmetries for particular photonic properties.

2.1 Fabrication and function

The assembly of pure block copolymers in the condensed matter state allows access to a range of highly ordered materials with unique nanostructure symmetries. The resulting assemblies may be directly used as photonic materials, or may be used as templates to produce complimenting inorganic nanostructures. The coassembly of inorganic nanoparticles with block copolymers provides a different pathway to generate highly ordered inorganic nanostructures in a more direct fashion. These approaches are based upon well-equilibrated assemblies (Section 3.1) resulting from the thermodynamics underlying supramolecular assembly. Equilibrated block copolymer derived materials uniquely yield a combination of uniform patterns with tunable symmetries that are amenable towards interactions with visible light, including photonic crystals and metamaterials. While this extent of 3D structure control is intriguing, the widespread adoption is somewhat challenged by the need to master polymer synthesis and processing conditions at which ordered phase separation occurs. Often equilibration is promoted through thermal or solvent annealing. Many photonic applications crucially depend on reliable morphology generation in thin films, where the bulk thermodynamic equilibrium is further perturbed by additional interfacial interactions and solvent evaporation kinetics as elaborated in Sections 3.1.1 and 4.

Subtly different solution processing routes result in non-equilibrated nanostructures with remarkably different characteristics

and photonic applications. Although pure polymer films are also processed from solutions, their equilibrium assembly in the condensed state is determined by the block copolymer thermodynamics alone, which is conceptually different from the assembly of solution structures. Polymer solution morphologies are often spherical micelles where the thermodynamics are additionally influenced by solvent interactions^{4,5} and the reorganization kinetics vary over many orders of magnitude.^{6–9} In the case of block copolymer coassembly with inorganic nanoparticles, the reorganization kinetics may be hampered by the presence of water to lead to kinetically trapped structures (Section 3.2). The resulting morphologies from this approach are uniform and usually have limited symmetries related to packed spheres. Porous inorganic materials are readily generated from such assemblies where the porosity serves to modulate the refractive index and may provide further advantages such as photocatalytic self-cleaning. Such non-equilibrium assemblies have been successfully demonstrated both for photonic bandgaps and anti-reflective properties.

3 Exploring the tool box of block copolymer self-assembly

Supramolecular assembly is the spontaneous aggregation of molecules towards an equilibrium condition, yielding well-defined assemblies based upon non-covalent interactions. The emergence of ordered and periodic structures indicates that the overall free energy change is often dominated by enthalpic terms such as the interaction strength of the different molecular segments. This free energy contribution is in concert with entropic terms, which are related to the molecular conformations induced by reorganization. Such assemblies are ubiquitous in biology, giving rise to highly ordered structures over many length scales.¹⁰ The direct evolution of assembled morphologies from the molecular structures affords a high level of control by adjusting molecular parameters during synthesis. Biological molecules such as DNA and the proteins derived therefrom are complex sequences of molecular segments that change motif frequently and without a simple pattern. While DNA sequences contain up to millions of repeated segments in a seemingly chaotic pattern, block copolymers are a much simpler molecular analog that also undergoes supramolecular assembly.

3.1 Block copolymer assembly near the thermodynamic equilibrium

Block copolymers are macromolecules with the different monomer segments organized into continuous blocks. Typical block copolymers are linear and contain two or three unique monomer chemistries organized into two to three blocks: AB, ABA, ABC. Although these provide idealized models for morphology studies, much more complex molecular structures are accessible, including non-linear polymers with various types of branches (star, H-shaped, comb, dendrimers) and more than three blocks.¹¹ The equilibrium self-assembly of pure AB diblock copolymers is well understood and leads to just four classes



of morphologies with spherical micelle packing (FCC or BCC), hexagonally packed cylinders, a 3D continuous double gyroid (G^D , space group $Ia\bar{3}d$), and a lamellar phase.¹² Notably, other morphologies are stabilized near the very limited region of phase space associated with the order-to-disorder transition. The prediction of the equilibrium phase morphologies of AB diblock copolymers is largely based on the volume fractions of the blocks and the product of their Flory–Huggins interaction parameter, χ , with the chain length, N , although further parameters contribute in non-ideal systems. Here, control over the chain length, and thus molecular weight, directly governs the periodic length-scale of the resulting assembly with an approximate relationship of $d \propto N^{2/3}\chi^{1/6}$ for the strong-segregation regime.¹³

The addition of a single additional block to form an ABC triblock terpolymer significantly expands the parameter space and complexity of the accessible morphologies with more than 30 reported so far.^{11,14–25} The use of ABC triblock terpolymers also enables access to several different 3D continuous network morphologies, including the chiral alternating gyroid network (G^A , space group $I4_132$) (Fig. 1).²² Chiral assemblies have important ramifications for optical metamaterials, *vide infra*. Although still significantly less complex than biological DNA and proteins, the further extension to block copolymers with four or more blocks opens a “Pandora’s box” of parameter space,²⁶ the exploration of which is only beginning.

3.1.1 Block copolymer self assembly at interfaces. While the self-assembly of amphiphilic macromolecules in the bulk is determined by the thermodynamic properties of the polymers

themselves, the presence of surfaces and interfaces gives rise to further complexities. Typically, preferential enthalpic interactions between some of the copolymer blocks may alter the phase diagram of Fig. 1 close to interfaces. A smaller contribution to the free energy arises from a change in entropy of molecules that are close to an interface, and thirdly, reptation kinetics may be strongly altered, depending on the nature of the surface. Since block copolymer based nanophotonic materials typically involve thin films in which self-assembly takes place, the consideration of effects that originate from the presence of a surface or interface is important.

The equilibration of block copolymers onto a substrate alters self-assembly in a way that may either be beneficial or detrimental for photonic applications. For a lamellar morphology, preferential interactions of one of the blocks with the substrate interface and/or the film surface typically orients the lamellae parallel to the surfaces,²⁷ which greatly facilitates the manufacture of Bragg reflectors (see Fig. 2). Care must however be taken to design the film thickness to be commensurate with the lamellar spacing. Otherwise the free surface may reconstruct into islands or troughs.²⁸ Sandwiched between two solid surfaces, the interplay of surface interactions and confinement controls the orientation of the lamellar structure.²⁹ Surface roughness also has an effect on the interfacial block copolymer morphology.³⁰

Beyond the mere reorientation of the self-assembled bulk phase, preferential block interactions are able to alter the phase morphologies near surfaces, for example from hexagonal to lamellar.³¹ For photonic applications, this change in symmetry may be significant, particularly because changes in surface morphology may affect the in- and out-coupling for light from the film. In extremely thin films, surface effects often lead to a rich block copolymer phase diagram that by far exceeds the complexity of the bulk phase space.^{32,33}

In cases where self-assembled morphologies are used as templates for electrochemical material synthesis, surface-induced polymer reorientation or surface reconstruction is often undesired,

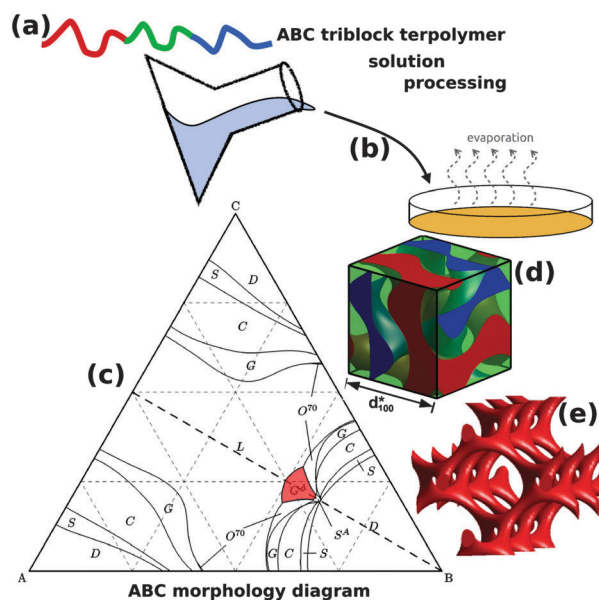


Fig. 1 Block copolymer self-assembled nanostructures for photonic applications. Block copolymers (a) are solution processable (b) to form self-assembled nanostructures. While AB diblock copolymers only form centrosymmetric morphologies, ABC triblock terpolymers (c) can enable non-centrosymmetric morphologies such as the alternating gyroid, G^A (d). The G^A contains two single gyroid networks that contain several helical axes, formed by the A and C blocks (e). (c) Adapted with permission from ref. 156. Copyright 2012 American Chemical Society. (d, e) Adapted from ref. 64 with permission from The Royal Society of Chemistry.

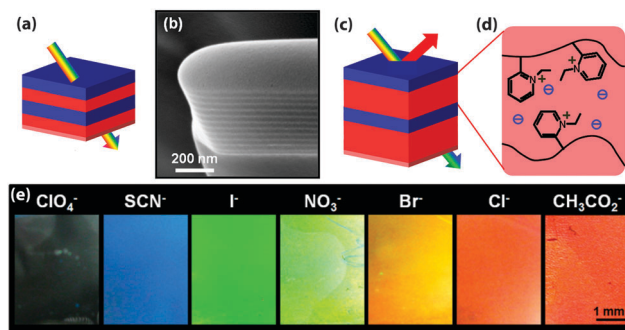


Fig. 2 Schematic representation of a color change mechanism in a photonic block copolymer multilayer modulated by an exchange of counterions (a). In the dry film, the modulation is too small to create an optical effect in the visible range as can be seen in the cross-sectional SEM image of the lamellar film (b). Schematic of the modified photonic response due to swelling (c and d). Depending on the hydration characteristics of the counterions, the selective swelling of the block copolymer lamellae can be controlled, causing a change in the optical response (e). Adapted with permission from ref. 89. Copyright 2012 American Chemical Society.



since this leads to morphologies that cannot be electrochemically replicated. The in-plane orientation of the lamellar or cylindrical phases cannot be accessed *via* either of the surfaces, but this can be overcome, *e.g.* by reorienting the phase morphology in an electric field.³⁴ The control over domain alignment in thin films has indeed been a subject of intense study. Meanwhile a number of effective and less complex methods have been developed, including the utilisation of solvent casting,³⁵ thermal and solvent annealing methods,^{36,37} photo-induced alignment,³⁸ as well as chemical templating,^{39–42} chemoepitaxy,^{43,44} and graphoepitaxy.^{45,46}

With gyroid-forming block copolymers, surface reconstruction into the lamellar phase is common, and causes a significant barrier to electrochemical replication. At the free film surface, plasma or ion etching may be necessary to expose the buried gyroid phase. At the substrate interface, typically a combination of surface and chemical modification by a self-assembled monolayer can be used to prevent the formation of a surface-induced lamellar phase.⁴⁷ Note that the successful replication of an interpenetrating network phase requires that all block copolymer phases make contact with a conducting substrate; while a lack of surface connectivity of the sacrificial phase will inhibit electrochemical processes, the preferential segregation of this material to the substrate will cause the film to float-off the surface during immersion into the electrolyte. The formation of sparse pore-interconnects at the surface leads to only localized replication.⁴⁸

3.1.2 Templating vs. coassembly. Photonic applications often rely upon high refractive index contrast or surface plasmon effects that are not yet accessible from pure block copolymers. Thus significant efforts have sought to combine the structure control from block copolymers with the range of functionalities available from inorganic materials. The synthesis pathways for such polymer–inorganic hybrid materials are either based on templating or coassembly strategies. With templating, a desired polymer morphology is transferred into an inorganic phase after the self-assembly process by the selective chemical removal of a polymer block followed by deposition of the inorganic species. Such strategies are widely generalizable since the morphology formation and inorganic deposition steps are separated.⁴⁹ Templating strategies however have a number of practical challenges associated with the crystallization of deposited amorphous materials such as oxides. The accumulation of strain caused by crystallization often limits the overall thickness of replicated layers to less than a micrometer.⁵⁰

With coassembly, an amphiphilic block copolymer and inorganic nanoparticles are combined in solution.⁵¹ Coassembly relies on the selective interaction of the inorganic components with a single block of the copolymer *via* attractive intermolecular forces such as hydrogen bonding. The selective association of the inorganic component with one of the polymer blocks changes their relative volume fractions, thereby significantly altering the self-assembled morphologies.⁵² Coassembly strategies have been developed for highly ordered silicate,^{53,54} transition metal oxide,⁵⁵ and metal⁵⁶ nanostructures. Successful coassembly relies upon careful tuning of key enthalpic,^{52,57,58} entropic,⁵⁹

and kinetic⁶⁰ considerations. Although there are numerous reported coassemblies based on AB and ABA block copolymers, only very few reports have emerged on the coassembly of inorganic components with ABC polymers.^{61–65} Coassembled hybrids also have challenges associated with the shrinkage and cracking of amorphous assemblies during formation and crystallization. The use of thin films provides support from the substrate and may allow partial stress relaxation. Multiple coatings with subsequent crystallization cycles significantly lower the film strain and enable device-relevant film thicknesses up to several micrometers.⁶⁶ Bulk films typically detach from the casting container and can be processed as films or powders without a substrate. A method (termed “CASH”) was developed to crystallize bulk films by utilizing the *in situ* generation of carbon as a hard-template to preserve the nanostructure during crystallization at temperatures up to 1000 °C.⁶⁷ An elegant alternative is the direct coassembly of crystalline nanoparticles and block copolymers.^{68–72} While relatively new, the additional key parameter for this coassembly is the particle surface coverage by ligands.⁷³ Recent calculations suggest that under certain conditions the nanoparticles in coassemblies may form superlattices for novel photonic applications.^{58,74} Many block copolymer approaches to synthesize controlled inorganic nanostructures have been successfully applied towards a wide array of photonic materials.

3.1.3 Photonic crystals. Nanostructures based on block copolymer self-assembly have been employed in the fabrication of a large number of photonic crystal structures from one^{75–80} to three dimensions.^{81,82} Standard one dimensional periodic dielectric reflectors from self-assembled block copolymer–homopolymer blends were demonstrated in 1999 when the photonic crystals community had just started to develop.⁷⁵ Large ordered lamellar structures with relative low refractive index contrast were made of poly(styrene-*b*-isoprene) ($\Delta n = 0.08$) demonstrating remarkably high reflectivities ($\sim 70\%$) across the entire visible range.⁷⁶ The refractive index contrast can be improved at the cost of absorption by doping one of the blocks with metal nanoparticles creating metallodielectric composites.^{83,84} A remaining fundamental challenge is the access to ever larger structures with periodicities comparable to the wavelength of visible light. For instance, a 391 kg mol^{−1} poly(styrene-*b*-isoprene) was used to manufacture a lamellar stack with 200 nm lamellar spacing by the addition of a homopolymer to swell the periodic spacing.⁸⁵ Block copolymers with such high molecular weights introduce considerable processing challenges, *vide infra*. Recently, several different composite approaches were demonstrated that enabled dynamic, responsive devices. Stimuli such as temperature change,^{77,86} electric voltage, or the presence of counter ions^{87–90} create reversible expansion of the self-assembled periodicity, drastically changing the optical response (Fig. 2).^{79,80}

Increasing the unit cell size in two and three dimensionally continuous morphologies poses new challenges for block copolymer assembled photonic crystals. A photonic response in the visible requires reliable phase separation and a high degree of long-range order in very high molecular weight block copolymers. Although several 3D continuous block copolymer



network morphologies were predicted to exhibit complete photonic bandgaps,⁹¹ their demonstration at visible wavelengths has been hampered by slow relaxation kinetics of the required high molecular weight polymers. To the best of our knowledge, the largest 3D structure assembled from a block copolymer had a double gyroid morphology with a lattice parameter of 258 nm, requiring a 2 week casting process of a $\sim 750 \text{ kg mol}^{-1}$ poly(styrene-*b*-isoprene).⁸¹ Please note that this unit cell dimension corresponds to a 129 nm spacing from strut-to-strut. High molecular weight polymers are highly entangled and suffer from ever decreasing reptation rates as the molecular weight increases. This example demonstrates routes to reduce kinetic limitations by starting the structure formation process in the presence of a solvent.⁸¹ The solvent plays two roles: it plasticizes the glassy polystyrene block and swells the chains to reduce entanglements and facilitate reorganization by polymer reptation. The equilibration of networked morphologies from ABC triblock terpolymers are additionally limited by a bridging B-block conformation with limited reorganization pathways.⁹² Similarly, solution processing was shown as a viable route to also circumvent such kinetic challenges for network forming ABC polymers.⁹³ The additional challenge of inducing such long-range order with predictable alignment and on a macroscopic scale is discussed in Section 4.

A recent review highlights the use of soft materials for photonic crystal fabrication.⁹⁴ Although a strong candidate approach for the scalable production of nanoscale materials, the manufacture of photonic crystals by block copolymer self-assembly, in particular of ordered 3D geometries from molecular weights larger than 100 kg mol^{-1} , remains challenging. Examples are mostly limited to one-dimensional structures although there were recently several advances with photonic architectures based on block copolymer assembly within the confinements of both opal and inverse-opal templates.^{95,96} Block copolymer approaches have yet to demonstrate a complete photonic band-gap in the visible range.

3.1.4 Metamaterials. Among the many designs still waiting to be explored, gyroid morphologies are particularly interesting due to their potential to create metamaterials at visible wavelengths. Although theoretical predictions have debated candidate morphologies such as the double and alternating gyroid,^{97–99} there are only a few experimental realizations of gyroid based metamaterials, in which the optical properties were studied.^{100–104} The alternating gyroid is particularly interesting because of its chiral axes. Strong chirality can lead to a cross-coupling between electric and magnetic dipoles breaking the degeneracy between two circularly polarised waves. This is predicted to lead to a negative refractive index for some geometries and is generally interesting since these metamaterials can exhibit both linear and circular dichroism.

While AB diblock copolymers can generate double gyroid morphologies that are achiral and centrosymmetric, the use of ABC triblock terpolymers has a greatly expanded the range of accessible morphologies and space groups. In particular, the alternating gyroid (G^A , space group $I4_132$) is one of the most attractive ABC morphologies because it has chiral spirals along

six axes, $\langle 100 \rangle$ and $\langle 111 \rangle$ (Fig. 1e) and is predicted to exhibit a complete photonic bandgap for a sufficiently high refractive index contrasts and filling fractions.^{81,91,99,105,106} These non-centrosymmetric features are not found in more common double gyroid morphologies because the inversion center of symmetry provides equivalent helices of opposite chirality leading to an overall achiral structure (space group $Ia\bar{3}d$). ABC triblock terpolymers have been shown to form the G^A both in the neat melt^{16,107} and when coassembled with nanoparticles.⁶⁴ The use of compositions with similar A and C block fractions (near the dashed line in Fig. 1c) are crucial for the symmetry breaking that places the A and C blocks separately into a similar topology that alternates in composition. In the G^A , the A and C blocks each form a single gyroid that interweave each other without intersecting and have opposite chiralities.

G^A polymer templates were recently used to produce the first 3D chiral metamaterials made by self-assembly.¹⁰⁰ The template was a G^A -forming poly(isoprene-*b*-styrene-*b*-ethylene oxide) that was self-assembled onto a conductive substrate (Fig. 3). The polyisoprene was selectively removed by UV ozone etching, followed by a rinse. The resulting pores were filled by electrodeposition of gold into the voided template. A subsequent plasma etch was used to selectively remove the surrounding polymer template, leaving behind a free-standing single gyroid network of gold that replicated the original structure of the

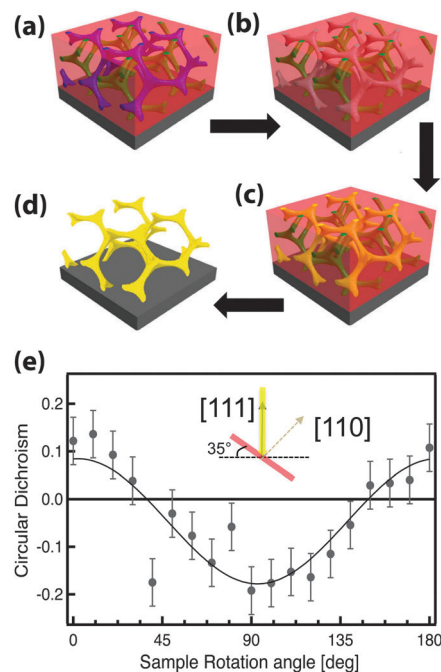


Fig. 3 Self-assembly of a 3D chiral metamaterial using a block copolymer template. An ISO polymer was assembled into a G^A morphology (a) followed by selective UV etching of polyisoprene (b). The resulting pores were back-filled by electrodeposition of gold (c). Subsequent removal of the polymer template by plasma etching (d) resulted in a free-standing single-gyroid network of gold. The anisotropic sample exhibited gyrotropic transmission that selectively allowed the passing of circularly polarized light corresponding to the structural chirality (e). Adapted with permission from ref. 104 and 100. Copyright John Wiley and Sons.



minority polyisoprene block. Because of the “polycrystalline” self-assembly of poly(isoprene-*b*-styrene-*b*-ethylene oxide), the resulting G^A domains had a random distribution of handedness. Measurements of individual G^A domains showed evidence of the internal chirality by exhibiting an anisotropic gyrotropic transmission. Along one of the chiral axes, either left or right circularly polarized light was preferentially transmitted, depending to the chirality of the morphology.¹⁰⁰ A follow up study, showed that these structures are highly tunable with several easily adjusted parameters.¹⁰¹ Control over the d_{100}^* unit cell dimension from 35 to 50 nm was demonstrated by changing the molecular weight of the block copolymer from 33 to 53 kg mol⁻¹. The increasing d_{100}^* unit cell dimension allowed a systematic variation of the transmission and reflection spectral response (Fig. 4a–c). Remarkably, about 20% of the incident light transmitted through a 300 nm thick film with 30 vol% gold, clearly indicating that the optical energy flux was transmitted by plasmon resonances propagating

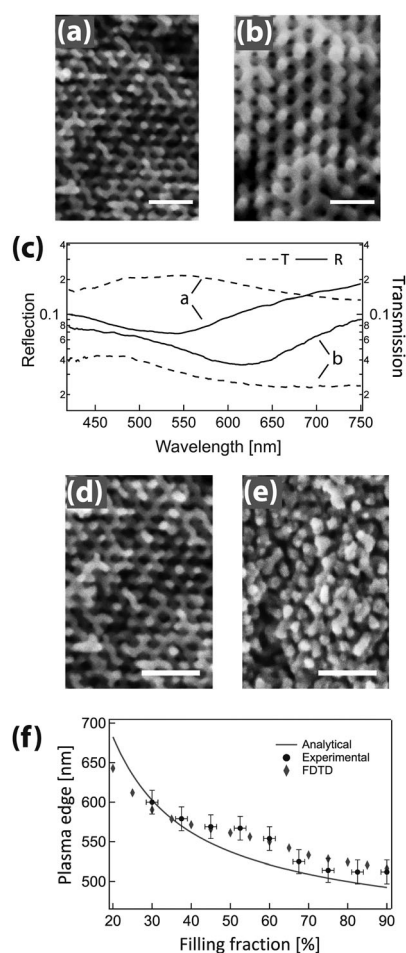


Fig. 4 Tunable chiral metamaterials. The G^A unit cell size is adjustable by changing the molecular weight of the poly(isoprene-*b*-styrene-*b*-ethylene oxide) template (a, b) to modulate the spectral wavelength dependence (c). After gold replication of the isoprene phase and template removal, the strut width of the replicated G^A network was increased by further Au electro-deposition (d, e). This modified the unit cell filling fraction, causing a variation of the plasma edge wavelength (f). Adapted with permission from ref. 101. Copyright John Wiley and Sons.

along the gold struts, confirming the well established fact that plasmon resonance frequencies are tunable by varying the structural dimensions. This allows the tuning of the metamaterial characteristics of a given G^A unit cell by changing the diameter of its gold struts. This was demonstrated by the electrodeposition of gold radially around the conductive struts of an initially replicated gold gyroid (Fig. 4d–f). The resulting filling fraction of gold in the G^A unit cell was tuned in this fashion from the initial value of 30% up to 90%, yielding systematic control over the blue shift of the plasma edge.¹⁰¹ Correspondingly, the strength of linear dichroism decreased monotonically, reaching 0 at 60 vol% gold.

Although this approach has not yet demonstrated a negative refractive index, gold gyroid metamaterials strongly affect light propagation beyond standard dichroism. For example, the nonlinear optical response of these structures provides an enhancement larger than ten fold when compared to all other metallic nanomaterials, including bulk gold. This remarkable increase of nonlinearity can be attributed to the metamaterial effect.¹⁰² The interconnected nanostructured network confines light, making the nonlinear response dominant. The fact that the structures are truly three dimensional and easily tunable makes this type of metamaterial the perfect platform for a new sensing principle as well as nonlinear and active devices.

Additional flexibility in the optical response can also be introduced by fabricating coaxial geometries (Fig. 5).¹⁰³ Here, similar to the discussion above, the porous scaffold after polyisoprene removal was backfilled with nickel by electrodeposition. The remaining polymers were subsequently removed by plasma etching, resulting in a freestanding Ni single gyroid. This structure was then used as the working electrode for the electrodeposition of coaxial gold. Finally, the inner nickel core was etched away by immersion in FeCl₃, providing a hollow

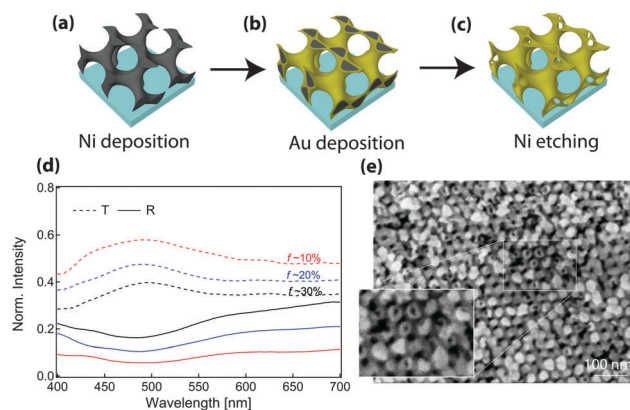


Fig. 5 Hollow alternating gyroid. Hollow G^A structures were templated from poly(isoprene-*b*-styrene-*b*-ethylene oxide) by first electroplating nickel into the free-volume generated by etching polyisoprene (a). The polymer template was removed and the resulting nickel network was used as the working electrode for the deposition of a coaxial gold layer (b), followed by selectively etching the nickel (c). The final hollow single gyroid structure (e) exhibited a 3-fold enhancement of photonic transmission compared to a structure consisting of solid struts with the same filling fraction (d). Adapted from ref. 103 with permission from The Royal Society of Chemistry.



single gyroid morphology (Fig. 5c and e). This metamaterial design provides a substantial transmission enhancement by nearly a factor of 3 when compared to the solid alternating Au gyroid with the same amount of gold per unit cell. The presence of a hollow guide geometry increases the number of propagating modes across the wave-guide structure. At the same time, the hollow geometry increases the efficiency of light in-coupling while also reducing the dissipation by decreasing the Au-volume involved in plasmon mode propagation to values much below the Au skin-depth. These conclusions are probably valid not only for hollow gyroid structures but also for the diamond or column morphologies. These findings are likely to pave the way for novel designs of metamaterials with low losses.

Recent simulations suggest that simpler manufacturing routes based on polymer coassembly with ligated metallic nanoparticles may directly form 3D chiral structures involving fewer processing steps.⁷⁴ Following this prediction, the coassembly of metallic nanoparticles with a different ABC polymer, poly(isoprene-*b*-styrene-*b*-dimethylaminoethyl methacrylate), led to the direct fabrication of G^A structures with platinum and gold nanoparticles.¹⁰⁸ The use of a different hydrophilic block, PDMAEMA, is key to provide for sufficiently enthalpic interactions with the metal nanoparticles. These advances lay a path to the broader development of optical metamaterials prepared by block copolymer self-assembly.

3.2 Block copolymer assembly away from equilibrium

The use of block copolymers for photonic applications can also be powerful from persistent solution morphologies under robust and simple fabrication conditions. Most solution processing routes for block copolymers are at least partially selective for one of the polymer blocks thereby inducing micellisation. Depending on the processing kinetics and conditions, these micelles may be translated into the final morphology rather than transitioning to the classical condensed matter state behavior of pure block copolymers. Please note that in the strictest sense, solution phases can exist in equilibrium with a reversible dependence on thermodynamic parameters,^{4,5} however the kinetics for the rearrangement of highly amphiphilic block copolymers are often extremely slow,^{6,7} with few exceptions.⁹ In recent years, protocols that allow the use of block copolymer coassembly in thin films have been developed. It has been demonstrated that the spontaneous dense packing of copolymer micelles allows detailed control over porosity^{71,109,110} and pore sizes⁷¹ in a fully interconnected and accessible porous network.^{109,111} The architecture closely resembles an inverse opal morphology, well known on 10 times larger length scales and typically created by colloidal self-assembly. While inverse opal architectures by colloidal assembly have become a well studied and widely used materials route, a similar architecture on the 10 nm length scale opens up a number of potential applications in optical coatings, photocatalysis, water cleaning or photovoltaic devices.

As schematically shown in Fig. 6a, the polymer acts as a structure-directing agent for the inorganic material. With proper chemical design, the inorganic guest can preferentially interact and coordinate with the hydrophilic block and thereby

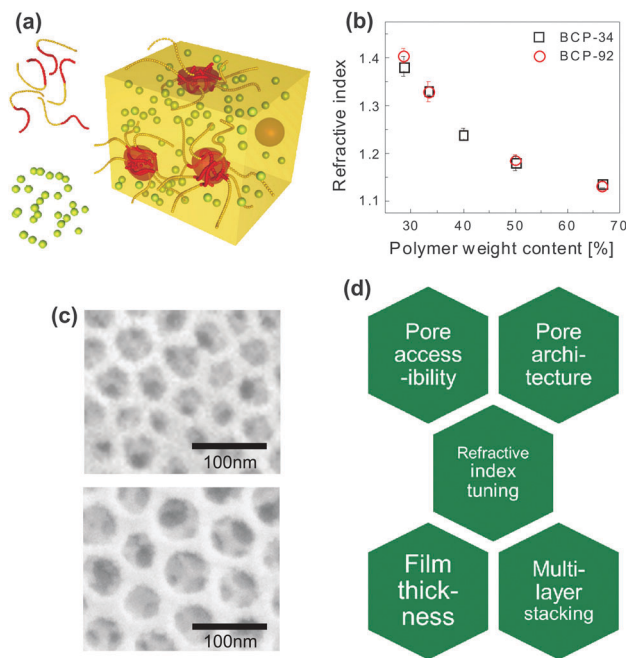


Fig. 6 Inorganic photonic nanoarchitectures by block copolymer coassembly. Schematic of block copolymer coassembly (a). The block copolymer (indicated as yellow and red chain strands) acts as a host for the inorganic material (yellow-green spheres) during block copolymer self-assembly. Film processing, solvent evaporation, annealing of the inorganic material and subsequent removal of the organic host gives rise to a nanoscopic inverse opal-type structure of densely packed pores in an inorganic matrix. Dependence of the refractive index of the resulting porous film as a function of polymer weight content in the initial mixture for two different block copolymers (b). Resulting pore size in silica-type films is dependent on the molecular weight of the polymer (c). A molecular weight M_n of 24.8 kg mol^{-1} led to a pore size distribution of $33 \pm 6 \text{ nm}$, while $M_n = 63.2 \text{ kg mol}^{-1}$ resulted in $52 \pm 6 \text{ nm}$. Overview of key requirements for porous thin film architectures with tunable photonic responsive (d). (a) Adapted with permission from ref. 112. Copyright 2010 American Chemical Society. (b, c) Adapted with permission from ref. 71. Copyright 2013 American Chemical Society. (d) Adapted with permission from ref. 113. Copyright 2014 Society of Photo Optical Instrumentation Engineers.

participate in the supramolecular coassembly process. In selective solvents, amphiphilic block copolymers form micelles in solution with cores that consist of the solvophobic block. Film processing, solvent evaporation, annealing of the inorganic material and subsequent removal of the organic host gives rise to a nanoscopic inverse opal-type structure of densely packed pores in an inorganic matrix. It is important to note that the effectiveness of this approach relies on the nature of the block copolymer. Poly(isoprene-*b*-ethylene oxide) (PI-*b*-PEO) was employed, which differs largely from the widely established Pluronic structure-directing agent (PEO-*b*-PPO-*b*-PEO) that acts like a surfactant, forming small $\sim 10 \text{ nm}$ structures that often collapse during high temperature processing.^{114,115} The high Flory–Huggins interaction parameter of the isoprene and ethylene oxide blocks,¹¹⁶ their low glass-transition temperatures, and the ability to synthesize high molecular weights with low polydispersities¹¹⁷ enable fast micro-phase separation, high polymer mobility during processing, and uniform structure control, respectively.



The coassembly route enables the manipulation of the refractive index of porous film over a wide range. Fig. 6b shows this variation as a function of the organic-to-inorganic mixing ratio in the initial solution. The refractive index window of $1.4 > n > 1.13$ corresponds to porosity values ranging from 20% to 73%. The resulting porous architectures in Fig. 6c are highly ordered and well interconnected. Their average pore size is a direct consequence of the molecular weight of the PI block in the organic host and can thus be finely controlled. In the example of Fig. 6c, a molecular weight M_n of 24.8 kg mol^{-1} led to a mean pore size of $33 \pm 6 \text{ nm}$, while $M_n = 63.2 \text{ kg mol}^{-1}$ resulted in a pore size distribution of $52 \pm 6 \text{ nm}$. This is in good agreement with scaling laws for the radius of gyration of the polyisoprene block in the melt.

One core challenge in a coassembly route to porous thin films is the material shrinkage that occurs during the processing, mostly due to the evaporation of the solvents and the condensation of the inorganic network. Processing protocols have however been developed to accommodate material shrinkage. This involves layer-by-layer processing combined with a specific annealing protocol which prevents the formation of cracks even in several μm thick films.⁶⁶

3.2.1 Mesoporous Bragg reflectors. The concept of block copolymer Bragg stacks is discussed in Section 3.1.3. Typically, high and low refractive index components of the dielectric stack are defined by individual blocks of the block copolymer and then driven into lamellar arrangements by annealing near the thermodynamic equilibrium. In contrast, mesoporous dielectric Bragg reflectors (MDBRs) are essentially porous multilayer stacks of alternating high and low refractive index. The characteristic reflection and transmission behavior can be tuned by varying the refractive index, the thickness and the number of the alternating layers.^{118,119} Fabrication is typically carried out in a layer-by-layer fashion. The combination of a MDBR with accessible pores on the 10 nm length scale opens up a number of new and unique applications, ranging from enhanced light absorption in photovoltaics to hybrid lasers as well as chemical and biochemical sensing.

Adsorption and desorption of gas molecules in the pores results in reversible changes of the refractive index of the porous layers and thus in a modification of the characteristic optical properties.^{114,120} When functionalized to bind specific molecules, MDBRs have been successfully used as biosensors to detect pico- to femtomolar concentrations of small organic molecules, DNA oligomers and proteins.^{121,122} 2D principal component analysis¹²³ or the coupling of MDBRs to surface layers¹²⁴ and resonance cavities¹²⁵ facilitates sensing with even greater accuracy. The ability to manipulate and control the flow of light in one dimension make MDBRs a powerful component in optoelectronic devices. When infiltrated with light emitting polymers, MDBRs have been successfully used for distributed feedback lasing.^{126,127} Incorporated into excitonic solar cells, MDBRs can lead to the localization of light in specific parts of the spectrum, while retaining the cell's transparency in others.^{119,128–131}

There are numerous material routes towards MDBRs. Initial attempts were based on porous silicon where the etching

conditions were periodically changed to realize a dielectric 1D lattice with alternating porosity. A first block copolymer-based route to coassemble alternative layers of porous TiO_2 and SiO_2 was introduced by Ozin and coworkers.¹¹⁴ This approach provided a greatly improved structure control of the porous networks. Yet, due to the slow phase separation and very limited thermal tolerance of the Pluronic surfactant, processing was extremely time consuming with fabrication times up to several days for each individual layer of the stack.¹¹⁵ A less complex route to form inorganic porous networks in thin films is the random packing of nanoparticles.^{132,133} While the optical properties of the stack can be tuned by film thickness and choice of the materials used in the individual layers (*e.g.* TiO_2 and SiO_2), control over other key parameters as discussed in Fig. 6d remains difficult. The random-close packing of somewhat polydisperse nanoparticles results in a rather random pore size distribution and allows only limited control over the porosity by changing the nanoparticle size and the addition of sacrificial fillers.^{134,135}

A fabrication route to MDBRs that makes use of solution-based block copolymer assembly far from equilibrium is illustrated in Fig. 7. The coassembly interplay between the structure-directing polymer and inorganic particles allows the fine tuning of porosity and thus the refractive index in the porous material by simply

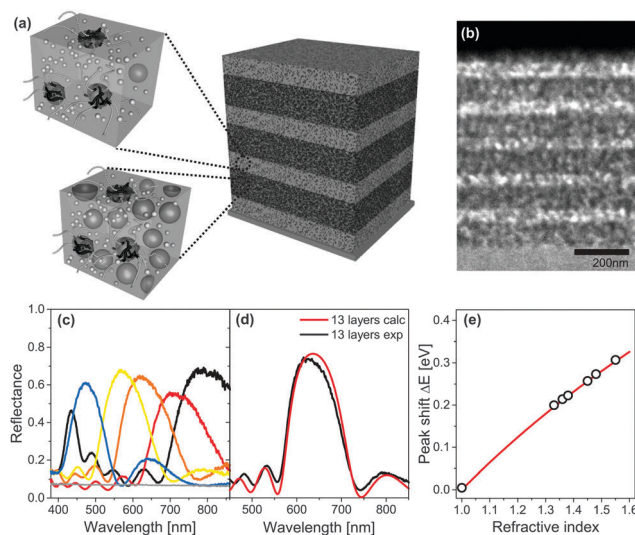


Fig. 7 Mesoporous Bragg reflectors based on block copolymer coassembly. Two stock solutions with a different TiO_2 to polymer weight ratio serve for the fabrication of high and low porosity layers in a multilayer architecture (a). Stacks are built-up by the alternating deposition and annealing of layers, followed by a final calcination step to reveal the mesopores. Cross-sectional view of a 11-layer TiO_2 stack by transmission electron microscopy (TEM) (b). Reflectance of 9-layer MDBRs, where the thickness of the five high refractive layers was kept constant while the thickness of the low refractive layers was varied to manipulate the optical response across the visible spectrum (c). Comparison of experimental reflectance (black) with calculations of an ideally regular stack comprised of 13 layers (red) (d). Corresponding shift of the Bragg peak position after pore infiltration with a variety of different liquids (e). The grey line corresponds to the theoretical shift of the Bragg peak calculated by a Bruggeman effective medium approximation. (a, d) Adapted with permission from ref. 136 and 110. Copyright 2011 Society of Photo Optical Instrumentation Engineers. (b, c, e) Adapted with permission from ref. 109. Copyright John Wiley and Sons.



changing the ratio between organic and inorganic components in the initial solution. As shown in Fig. 7a, sequential film deposition and annealing enables multilayer stacking and the build-up of a MDBR. A cross-section of the multilayer stack after removal of the organic material by high temperature calcination imaged by TEM is shown in Fig. 7b. Note that the contrast in electron density within the TiO₂ stack is caused exclusively by the alternating porosity. Experimental results of MDBR performance are shown in Fig. 7c–e.

The block copolymer coassembly route presented here offers several advantages over the state-of-the-art. It decouples important parameters in MDBR stack design, porosity and pore size, and allows the tuning of both properties in a wide parameter range. Furthermore the pore size distribution is narrow and controllable in comparison to random networks of nanoparticles. The control of the molecular weight of the pore-forming polymer block directly determines the resulting pore size.⁷¹ As previously discussed, the refractive index lattice in the nanoparticle-based MDBRs is realized by the sequential deposition of TiO₂ and SiO₂ nanoparticle layers.¹³³ The use of SiO₂ as the low refractive building block makes the stack non-conducting and thus prevents contributions to light absorption and conversion in photovoltaic devices. While certain nanoparticle-based routes allow the fabrication of conducting MDBRs,^{134,137} the lack of control over pore size and pore accessibility limits mass transport through the porous network and infiltration for solid state dye-sensitized solar cells.¹³⁸ This is covered in more detail in recent reviews on MDBRs¹¹⁹ and on the bottom-up assembly of photonic crystals in general.^{94,139}

3.2.2 Antireflective coatings. As illustrated in Section 3.1, block copolymer self-assembly away from equilibrium is a powerful route to the creation of highly porous and uniform thin films. This protocol is therefore ideal for the manufacture of optical coatings, particularly antireflective coatings. Antireflective coatings reduce unwanted light reflection at interfaces and rely upon amplitude and phase matching of light to achieve this effect. This requires an optical thickness of $\lambda/4$ for a given wavelength and angle of incidence and an effective refractive index of the antireflective coating (n_{AR}) of the square root of that of the underlying substrate.¹⁴⁰ Common substrates such as glass or polyethylene terephthalate (PET) with refractive indices of around 1.5 therefore require unrealistically low values of $n_{\text{ARC}} \approx 1.22$. This is typically solved by introducing porosity on the sub-wavelength scale. Block copolymers are ideal candidates for the fabrication of antireflective coatings as they allow fine control over pore dimensions on the 5–50 nm length scale, *i.e.* much below the diffraction limit of visible light.¹⁴¹

Critical parameters for the manufacture of antireflective coatings are the porosity and to a smaller extent the pore size, both of which may be controlled by block copolymer coassembly far from thermodynamic equilibrium as described above, yielding a simple and scalable approach. The block copolymer acts as a porogen which is typically combined with sol–gel chemistry.¹⁴² Mild conditions (*i.e.* through wet chemical etching or plasma etching) to remove the organic hosts allow to process antireflective coatings on plastic-based flexible substrates.¹⁴³

Block copolymer routes to antireflective coatings are diverse. Appealing concepts include the use block copolymer-functionalized gold nanoparticles or block copolymer patterns as lithographic masks in a reactive ion etching process, resulting in gradient refractive index surfaces that resemble the moth eye.^{144,145} Gradient refractive index antireflective coatings may also be achieved by exploiting domain rearrangement through surface reconstruction by block copolymer deposition on surface treated substrates followed by annealing.¹⁴⁶ Block copolymer assembly near the thermodynamic equilibrium and subsequent use as a sacrificial template for gyroid-structured thin inorganic films is also a successful strategy for the manufacture of optical coatings with exceptionally low refractive indices.¹⁴⁷

While numerous material routes lead to high performance optical coatings under laboratory conditions, commercial implementation is held up by their susceptibility to contamination and thus decay in functionality. This could be prevented by photocatalytic self-cleaning, *i.e.* the decomposition of organic contaminants by light-induced redox-reactions.¹⁴⁸ The inclusion of photocatalytic hot spots is challenged by their high refractive index ($n_{\text{TiO}_2} > 2.5$ ¹⁴⁹), which limits the amount of photocatalytic material that can be included in a self-cleaning antireflective coating while still reaching sufficiently low values of n_{ARC} .

A simple method for the manufacture of robust antireflective coatings with greatly improved self-cleaning properties was recently reported.⁷¹ As shown in Fig. 8a, the process relies on the block copolymer coassembly of a mixture of silica-based sol and preformed TiO₂ nanocrystals. The spontaneous dense packing of copolymer micelles during the film formation process, followed by condensation of the silica-based matrix during film annealing and subsequent removal of the organic host, results in an inverse opal-type silica morphology that is loaded with TiO₂ photocatalytic hot-spots. The arrangement of micelles represents the densest packing of sacrificial material, *i.e.* pores. The resulting ultra low volume fraction of the inorganic material (down to 27%) enables a high loading of the network with TiO₂ nanocrystals and thus a simultaneous matching of the requirements for self-cleaning and antireflection. This method requires only moderate annealing temperatures (<150 °C) and processing can therefore be accomplished onto plastic substrates. The resulting optical properties are shown in Fig. 8b, where the reflectance of an uncoated PET foil (PET-0s) is compared to a sample that was coated on one side with a self-cleaning antireflective coating (PET-1s). By simple interfacial analysis with $R_{\text{PET-0s}} = A + ((1 - A)A)$ and $R_{\text{PET-1s}} = B + ((1 - B)A)$, one can derive the reflectance R of an uncoated (A) and a coated PET interface (B). The spectral traces suggest a near ideal broad-band antireflective response with up to $\approx 5.2\%$ reduction in reflectance for each coated interface. The photocatalytic self-cleaning efficiency can be studied by the decomposition of stearic acid as a function of irradiation time under simulated sunlight (AM1.5). Stearic acid is a widely used model molecule which assembles as a monolayer onto the coating and can be monitored by Fourier transform infrared spectroscopy (FTIR), shown in Fig. 8c for an antireflective coating with 50 wt% TiO₂. The role of TiO₂ loading is further evidenced in Fig. 8d, where the decay in normalized absorbance is compared for



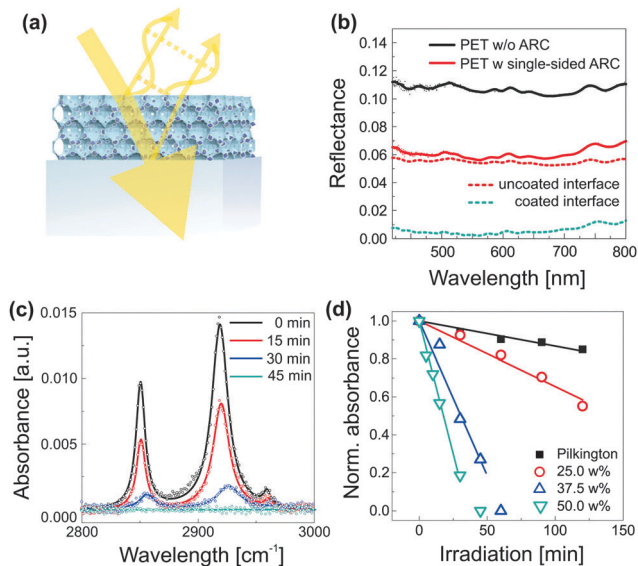


Fig. 8 Self-cleaning antireflective optical coatings. Compatibilized photocatalytic TiO_2 nanocrystals are coassembled with PI-*b*-PEO block copolymer and silica-based sol (a). Phase and amplitude matching of the optical coating results in destructive interference of reflected light, *i.e.* enhanced transmission, while the embedded photocatalytic hot spots prevent contamination of the antireflective coating. The low temperature fabrication route ($<130\text{ }^\circ\text{C}$) allows film processing onto flexible and low-cost PET substrates with near optimum optical properties (b). FTIR spectra, illustrating the decomposition of stearic acid as a function of irradiation time under simulated sunlight (AM1.5) (c). Decay of the integrated peak area with time for different TiO_2 loadings (d). The decay of the commercially available self-cleaning Pilkington active glass (not antireflective) is shown for comparison. (a–d) Adapted with permission from ref. 71. Copyright 2013 American Chemical Society.

antireflective coatings containing 25–50 wt% TiO_2 . Interestingly, these coatings clearly outperform commercially available self-cleaning glass that is not antireflective and thus less constrained in coating composition.

4 Outlook for block copolymer nanophotonics

Although the control of multiple length scales and structures by block copolymer self-assembly has been demonstrated, a number of important challenges remain, preventing the exploitation of their full potential as a nanophotonics platform. In the case of photonic crystals, an increase in refractive index contrast between blocks would be beneficial not only to shift the optical response to larger wavelengths but also to increase the bandgap width. A second benefit of an improved contrast is the reduced amount of material needed to effectively reflect the desired wavelength. For a one-dimensional periodic stack, a simple transfer matrix calculation directly shows that only 20 layers (overall thickness of less than $3\text{ }\mu\text{m}$) are sufficient to achieve 100% reflection when using refractive index contrast of $\Delta n = 0.279$, while with lower contrast $\Delta n = 0.071$ the reflectivity blue-shifts and is reduced to 50% (Fig. 9).

Since the dimension of the unit cell is defined by the block copolymer molecular weight, longer blocks with higher refractive

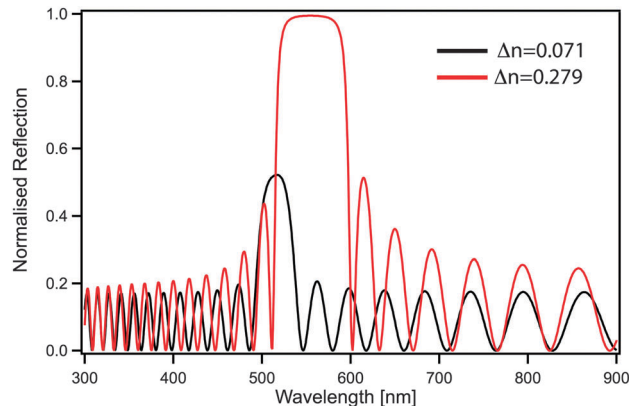


Fig. 9 Refractive index dependence of one-dimensional stacks. The black line shows the calculated spectrum of a multilayer stack composed of 40 alternating 70 nm thick PS and PI layers (typical values for block copolymer based multilayers) obtained by the transfer matrix method. The red line corresponds to a multilayer stack with the same layer dimensions, where the PS layers are replaced by guanine.

indices are also beneficial in the 3D case, where continuous morphologies such as the alternating gyroid or alternating diamond are predicted to provide a full photonic band-gap.^{150,151}

The production of ever increasing molecular weights comes however with a significant kinetic penalty from increasing polymer entanglements. It is important to note that continuous morphologies such as the gyroid phases are mechanically self-supporting and therefore enable templating to further increase in refractive contrast through the complete removal of the organic template, thus replacing the organic matrix by air. In the case of the alternating gyroid, a refractive index of about 2.5 is large enough to open up a complete photonic band gap with a filling fraction of 50%, while for the alternating diamond a refractive index of only 2 would suffice. The optimization of geometry and refractive index are however not sufficient. The precise control of the filling fraction is required through a careful design of polymer self-assembly.¹⁰⁴ Polymer materials exhibit a somewhat narrow range of refractive indices. Common building blocks, such as polystyrene, polyisoprene, poly(ethylene oxide) or poly(methyl methacrylate) all lie in the range of 1.4–1.6, see Table 1.

Table 1 Refractive index of organic and inorganic materials with low absorption in the visible spectrum

Material	Refractive index (at 589.3 nm)
Poly(ethylene oxide), (PEO)	1.4539
Silicon dioxide	1.458
Poly(methyl methacrylate), (PMMA)	1.481
Indium oxide	1.487
Cellulose	1.46–1.55
Polyisoprene, (PI)	1.521
Chitin	1.56
Polycarbonate, (PC)	1.586
Polystyrene, (PS)	1.592
Tin oxide	1.82
Guanine	1.83
Zirconia	2.1588
Niobia	2.316
Titanium dioxide	2.890



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