

Nanocrystalline silicon: lattice dynamics and enhanced thermoelectric properties

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Silicon has several advantages when compared to other thermoelectric materials, but until recently it was not used for thermoelectric applications due to its high thermal conductivity, $156 \text{ W K}^{-1} \text{ m}^{-1}$ at room temperature. Nanostructuring as means to decrease thermal transport through enhanced phonon scattering has been a subject of many studies. In this work we have evaluated the effects of nanostructuring on the lattice dynamics of bulk nanocrystalline doped silicon. The samples were prepared by gas phase synthesis, followed by current and pressure assisted sintering. The heat capacity, density of phonons states, and elastic constants were measured, which all reveal a significant, $\approx 25\%$, reduction in the speed of sound. The samples present a significantly decreased lattice thermal conductivity, $\approx 25 \text{ W K}^{-1} \text{ m}^{-1}$, which, combined with a very high carrier mobility, results in a dimensionless figure of merit with a competitive value that peaks at $ZT \approx 0.57$ at 973°C . Due to its easily scalable and extremely low-cost production process, nanocrystalline Si prepared by gas phase synthesis followed by sintering could become the material of choice for high temperature thermoelectric generators.

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1 Introduction

Silicon is the second-most abundant element in the Earth's crust after oxygen. Due to its abundance and widespread usage in the semiconductor industry, the material itself and also precursors for gas phase synthesis are available in industrial quantities, at exceptional purity and quality for a comparatively low price. Si is non-toxic and unproblematic from a safety, scarcity and environmental perspective, unlike other, lead or tellurium bearing, thermoelectric materials. Further, the entire technology around silicon – synthesis, machining, etching, doping – is well-established and it is one of the most studied and simplest model materials in solid state physics, for which reference data is widely available.¹ Si is therefore a material of choice to study the effects of nanostructuring on the lattice

dynamics and the thermal transport, which must be mastered in order to achieve good thermoelectric properties.

Single-crystalline and undoped silicon has a very high thermal conductivity, $156 \text{ W K}^{-1} \text{ m}^{-1}$ at room temperature,² related to its low density and high Young's modulus. In heavily doped silicon, the thermal conductivity is significantly reduced, though still very high, close to $80 \text{ W K}^{-1} \text{ m}^{-1}$, at room temperature.³ As a direct result of its lattice structure with stiff tetrahedral covalent bonds connecting the atoms, it is a hard but brittle material.

Nanostructuring as means to improve the thermoelectric properties of a material has been intensively studied,⁴ since such processing decreases the lattice thermal conductivity by creating additional scattering centers for phonons at grain boundaries. By influencing mostly the lattice contribution to the thermal conductivity without also decreasing the electronic contribution, which is directly related to the electrical conductivity, an improvement in the dimensionless thermoelectric figure of merit (ZT) – and ultimately the efficiency of a thermoelectric generator – can be achieved, since $ZT = S^2 \sigma T / \kappa$, where S is the Seebeck coefficient, σ the electrical conductivity, κ the thermal conductivity and T the temperature. Such approach is viable because phonons have usually a mean free path significantly larger than electrons, and the transport of the former can be disrupted without dramatically hindering the latter.

The effects of nanostructuring on the lattice dynamics were investigated by means of theoretical calculations^{5–12} and

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experimentally observed by methods such as inelastic neutron scattering,^{13–18} Raman spectroscopy,^{19,20} nuclear inelastic scattering (NIS)^{17,21} and measurements of the specific heat.^{22,23} Overall, these calculations and experiments reveal that an enhancement in the density of phonon states (DPS) at low energies and a broadening of the bands on the DPS is expected for nanocrystalline materials. These modifications in the vibrational modes are attributed to the vibrations of atoms located at the grain boundaries where the atomic structure is more open than within the crystalline grains, and result in a modified force field and a softening of the force constants.

Here we present a detailed experimental study on the effects of nanostructuration on the lattice dynamics and thermoelectric properties of nanocrystalline silicon which, except for the intentional doping, is virtually free of other impurities.

2 Experimental

2.1 Sample preparation

Silicon nanoparticles were synthesized by a plasma-assisted gas phase process, using a microwave reactor as described previously.²⁴ 1% of n-type doping was achieved by adding phosphine (PH₃) to the precursor gas. Two batches of powder were obtained by controlling the synthesis parameters: one with a nominal initial grain size of 14 nm and another with a nominal initial grain size of 52 nm confirmed by BET.[†] The nanopowder is functionalized at the surface by hydrogen during the synthesis, so that no oxygen impurities can attach at the surface of freshly synthesized powder. The nanopowder was bottled under inert conditions and kept within an inert atmosphere to prevent contamination with oxygen during further processing. Sintering was carried out immediately after synthesis with an absolute minimum time for filling the crucible and starting the sintering process. This effort is necessary, as a contamination of the nanopowder with oxygen can significantly influence the physical properties of the samples as reported previously.²⁵

The nanopowder was compacted into 2 cm diameter dense pellets with a spark plasma sintering furnace from FCT Systeme GmbH in a 1 mbar Ar atmosphere. For the first batch (14 nm), sintering was carried out during 3 min (sample A). The second batch (52 nm) was divided into two parts. One part was sintered for 3 min (sample B) and the other for 30 min (sample C). Heating and cooling rates for all samples were fixed to 100 K min^{−1}. The sintering temperature was 1150 °C and a 35 MPa pressure was applied during sintering.

2.2 Microstructural characterization and composition

Transmission Electron Microscopy (TEM) was used for structural characterization of the sintered pellets in a FEI-Tecnaï microscope with a field-emission electron gun operating at 200 kV. TEM samples were prepared from the sintered pellets by a precision Focused Ion Beam (FIB) system using gallium ions. The grain size estimation was carried out measuring 75 grains on each sample in different regions. As the probe volume

is small, ~0.1 cubic micron, the microstructure was also investigated by scattering methods.

In order to verify the average crystallite size of the nanocrystalline pellets, X-Ray diffraction (XRD) was performed using synchrotron radiation at the high energy station 6-ID-D of the Advanced Photon Source (APS) at Argonne National Laboratory. The sample was 1 mm thick and the experiment was performed in transmission geometry in order to probe the bulk of the pellets. The X-ray wavelength was 0.124659 Å and a General Electric amorphous silicon detector was positioned at a distance of 1849 mm from the sample, a distance determined by a NIST640c Si standard. The data were reduced to diffraction patterns with the program FIT2D²⁶ and no preferential orientation was observed. Rietveld refinements were carried out using the program FULLPROF,²⁷ taking into consideration the Debye–Scherrer broadening of the diffraction peaks.

The average crystallite size was also investigated by Small Angle Neutron Scattering (SANS) measurements carried out using the instrument KWS1 operated by the Jülich Centre for Neutron Science (JCNS) at the FRM II (Garching, Germany).²⁸ In the present work, only the essential results concerning characteristic crystallite sizes will be presented, while further analysis based on Gaussian random fields²⁹ will be published elsewhere.

The elemental analysis was performed at the Prompt Gamma Ray Activation Analysis (PGAA) instrument positioned at the neutron guide NL4b of the Forschungs-Neutronenquelle Heinz Maier-Leibnitz (FRM II – Garching, Germany).³⁰ The cold neutron flux used for the measurement was 6.1×10^{10} n cm^{−2} s^{−1}. A high-purity germanium (HPGe) detector was used to detect the gamma rays produced in the sample by neutron capture reactions. The emitted gamma rays have a characteristic energy which depends on the element or isotope which absorbs the neutrons. The peak-area is proportional to the concentration of the element in the sample. This method is therefore a non-invasive way to chemically characterize the sample, which gives precise information about the impurities and its amount in percentages, and it is a method of choice which can give nondestructively information about elements such as hydrogen and boron.

2.3 Lattice dynamics

Resonant Ultrasound Spectroscopy (RUS) is a nondestructive technique which gives access to the elastic tensor by recording the frequencies of the natural modes of mechanical vibrations. Parallelepiped samples are positioned between two piezoelectric transducers, one driving and the other recording the response,³¹ in order to obtain the elastic constants C_{11} and C_{44} that fully characterize the elasticity in an elastically isotropic samples. The first 30 resonance frequencies were measured on samples with $\sim 2.0 \times 1.5 \times 1.5$ mm³ dimensions. The RMS errors between the calculated and measured frequencies were 0.29% and 0.21% for the samples with smaller and larger nanocrystallites, respectively.

The Density of Phonon States (DPS) of all samples was obtained by inelastic neutron scattering measurements performed on the Time of Flight (TOF) spectrometer IN6 at the

[†] BET (Brunauer, Emmett, Teller): surface area analysis.



cold source of the Institute Laue-Langevin (Grenoble, France). The incident wavelength was 5.12 Å with an elastic energy resolution of 0.13 meV, as determined by the elastic neutron scattering on a vanadium sample.

The specific heat, C_p , was obtained in a commercial Physical Property Measurement System (PPMS) from Quantum Design for all sintered pellets between 4 and 400 K. The specific heat of a polycrystalline Si sample was also measured for comparison.

2.4 Thermoelectric transport measurements

Thermoelectric transport characterization was carried out between room temperature and 1000 °C. The Seebeck coefficient S and the specific electrical conductivity σ were measured on a bar-shaped sample by a direct measurement technique using a commercial system (ZEM3 by Ulvac Technologies, Inc.). In contrast to ref. 32, we did not carry out a rapid thermal annealing to 1000 °C. However, all measurements were carried out upon slow heating at a rate between 1.5 and 2.5 K min⁻¹ in order to warrant comparison. The thermal diffusivity λ_0 was measured by a laser flash method on a sample of 10 × 10 × 1 mm³ size using a commercial system (LFA 457 MicroFlash by Netzsch Thermal Analysis GmbH). The thermal conductivity was then calculated with $\kappa = \lambda_0 \cdot C_p \cdot \rho$, using a value for the density of the pellets (ρ) obtained by the Archimedes method at room temperature. The bulk values of heat capacity were used for this calculation, since typically in this temperature range the heat capacity of bulk and nanocrystalline Si does not differ, as confirmed from the C_p results. In addition, charge carrier densities were determined at room temperature from Hall effect measurements carried out in the classical Hall bar geometry with magnetic fields ranging between -1 and 1 T and using alternating currents.

3 Results and discussion

3.1 Microstructural and chemical characterization

The average nanocrystallite diameters, D , as well as the strain in the sintered pellets was estimated by refinement of the X-ray diffraction pattern and the results were compared with images obtained from TEM, see Fig. 1(a) and (b), and with the results of the SANS data shown in Fig. 2 as a Kratky plot of the scattering intensity, $d\Sigma/d\Omega \cdot Q^2$ vs. Q , where Q is the scattering vector. The Kratky plot exhibits a maximum at q_{\max} , which can be used to estimate the average crystallite diameter D using the pseudo-Guinier radius $R_{pg} = D/2 = \sqrt{3}/q_{\max}$.³³ The values obtained by these three methods are summarized in Table 1.

Sample A had an average crystallite size of 40(2) nm from XRD and 42 nm from SANS whereas TEM reveals grains ranging between 48 and 264 nm with an average of 114 nm. Sample C had a slightly smaller crystallite size of 33(1) and 34 nm from XRD and SANS, respectively, and a grain size distribution obtained by TEM between 47 and 246 nm with an average of 112 nm, and also showed amorphous precipitates with average size of 29 nm. The differences seen between TEM, SANS and XRD analysis have their origin in sensitivity of the different methods. TEM is sensitive to the outer contour of grains, not

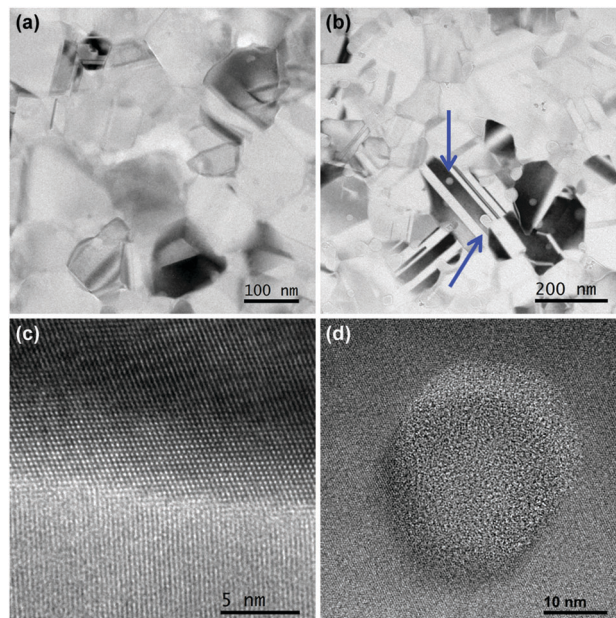


Fig. 1 TEM bright-field images of sample A (a) and sample C (b) and high resolution TEM of grain boundary between two nanocrystals of sample A (c) and of an amorphous precipitates on sample C (d). Arrows indicate amorphous precipitates.

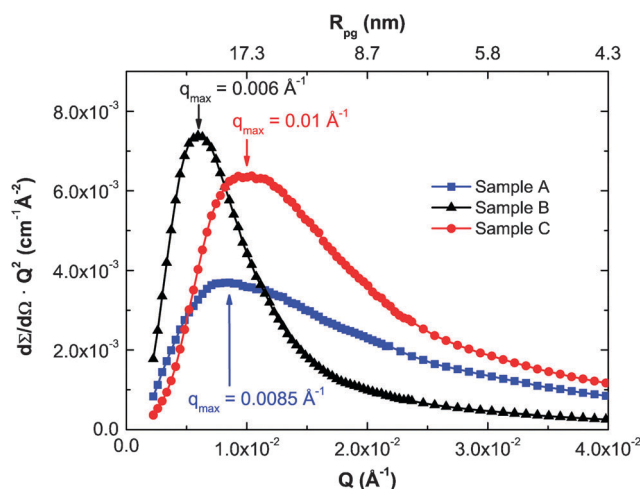


Fig. 2 Kratky plot of the SANS curves. Each curve exhibits a broad maximum, which yields the pseudo-Guinier radius R_{pg} .

Table 1 Summary of nanocrystallite sizes (D) and strain (ϵ) obtained by TEM analysis, XRD refinement and SANS

	TEM			XRD		SANS
	D_{\min} (nm)	D_{\max} (nm)	D_{av} (nm)	D (nm)	ϵ (%)	D (nm)
Sample A	48	264	114	40(2)	0.00138	42
Sample B	—	—	—	42(2)	0.00133	58
Sample C	47	246	112	33(1)	0.00150	34

taking into account possible twinning or intragranular effects. XRD is sensitive to the crystallite size, *i.e.* to limited correlation length, which is in general smaller than the grain size due to the



existence of planar defects and intra grain boundaries. Furthermore, SANS curves strongly depend on the size distribution of the scattering entities and may also be affected by inter-particle effects in the present case, though it still represents a measure of characteristic length scales.³³ Besides, XRD and SANS are methods averaging over a larger volume, whereas TEM only gives an impression of a very small sample volume, not necessarily fully representative for the complete pellet. Correlating the different methods and known behavior of nanocrystalline silicon, the presence of significant amounts of an amorphous cover of silicon, in excess of one or two atomic layers, can be ruled out, in particular because of the large charge mobility, see below, and because a change in contrast would be noticeable at the grain boundaries next to regions in diffracting condition and would appear black in bright field TEM images.

The samples which were processed with the same sintering parameters, but with initially different nanoparticles sizes (14 and 52 nm for samples A and C, respectively), present only a small different average nanocrystallite sizes after sintering. Sample A presented strong grain growth during sintering. Sample C presented a large amount of defects such as twins and a certain amount, $\sim 6\%$, of amorphous precipitates, which energy-dispersive X-ray spectroscopy indicated to be essentially Si, both visible in Fig. 1(b), resulting in an increased strain as obtained from XRD refinement. A grain boundary between two nanocrystals in sample A with different relative orientation without any amorphous layer is shown in Fig. 1(c) and a high resolution image of an amorphous precipitate on sample C in Fig. 1(d). Those precipitates are rather spherical and are found on all images acquired on this sample, indicated by blue arrows in Fig. 1(b).

Overall, although the three different measurements yielded different values of nanocrystallite sizes, the same trend in sizes is observed, ranging from the smallest being sample C and the largest being sample B.

Samples B and C were investigated exemplarily by PGAA. The spectra reveal that the samples were 99.0(1)% Si with 1.0(7)% of P dopant as expected. A small amount of H (0.20(1)%) was detected on the sample with smaller initial nanocrystallite size (sample C). Furthermore, in both samples, a very small ppm contribution of boron was detected. This impurity could originate from a contamination of the precursor silane, which is prepared by fractional distillation, as it is not easy to completely separate silane from diborane.

3.2 Lattice dynamics

Samples A and B had the same properties in all measurements within their experimental errors: density of phonon states

Table 2 Summary of the elastic constants and sound velocities in nanocrystalline Si compared with bulk Si obtained by different techniques

	C_{11} (GPa)	C_{44} (GPa)	v_s (km s ⁻¹)		
			RUS	DPS	C_p , θ_D^{LT}
Bulk	160.1 ³⁴	80.0 ³⁴	5.94	6.73(5)	5.70(5)
Sample A	173(3)	59.0(8)	5.0(1)	5.0(3)	4.44(9)
Sample C	172(3)	58.2(7)	4.9(1)	4.3(3)	4.2(1)

(DPS), specific heat (C_p) and resonant ultrasound spectroscopy (RUS). Therefore, only the results for sample A are being discussed here.

The values obtained for the elastic constants C_{11} and C_{44} with RUS are summarized in Table 2. The speed of sound was then calculated: $3/v_s^3 = 1/v_{\text{long}}^3 + 2/v_{\text{trans}}^3$, where $v_{\text{long}} = \sqrt{C_{11}/\rho}$ and $v_{\text{trans}} = \sqrt{C_{44}/\rho}$ for the polycrystals are the longitudinal and transversal speed of sound, respectively. The values of speed of sound for single-crystalline Si were calculated previously (ref. 25) using the Hershey–Kröner–Eshelby average.

The elastic constant $C_{11} = 172(3)$ and $173(3)$ GPa for the samples with smaller and larger nanocrystallites sizes, respectively, corresponding to the bulk modulus (B) is $\approx 8\%$ larger than in single crystalline Si. The shear modulus, $G = C_{44} = 58.2(7)$ and $59.0(8)$ GPa, is $\sim 25\%$ smaller than in single crystalline Si. Such a decrease in the resistance to shear deformation (G) combined with an increase of the resistance to dilation (B) shows that the mechanical properties of a material with as many grain boundaries and defects are significantly modified when compared with the single-crystalline material, leading to a softening of the material. This is also confirmed by the decrease of the speed of sound calculated from the elastic constants. Such a decrease relates to a decrease in thermal conductivity.

The DPS of two samples of nanocrystalline Si obtained from inelastic neutron scattering are shown in Fig. 3 and compared with polycrystalline Si.²⁵ Note that the area under the DPS curve of all samples was normalized to 1 between 0 and 70 meV.

In the incoherent scattering approximation, and because the sample essentially contains only one chemical element, the speed of sound can be obtained from the low energy limit of $g(E)/E^2$ with $1/v_s^3 = 2\pi^2 N_V / \hbar^3 g(E)/E^2$ where N_V is the number of atoms per unit volume.¹⁷ In the case of the nanocrystalline Si samples an increase on the Debye level, $\lim_{E \rightarrow 0} g(E)/E^2$, in the reduced DPS is observed. Note that the incoherent scattering approximation is not perfectly suitable for silicon, which is a strong coherent scatterer. Therefore, the speed of sound is

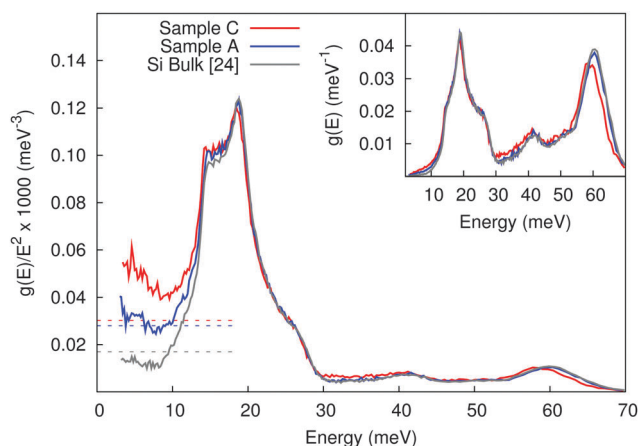


Fig. 3 Reduced Density of Phonon States (DPS) for two samples of nanocrystalline Si compared to previously reported results on polycrystalline Si, dotted lines indicate the asymptotic limits from RUS. Inset: DPS.



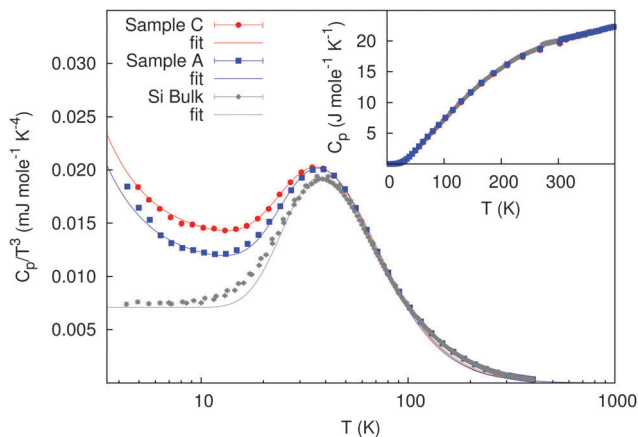


Fig. 4 Specific heat divided by T^3 for both nanocrystalline Si compared with polycrystalline Si. Inset: specific heat (error bars are smaller than the symbol size).

obtained by a second approach using RUS measurements, and the data is compared. An extrapolation using the asymptotic limit from RUS, considering the speed of sound summarized in Table 2, shown as dotted lines in Fig. 3, reveals a fair agreement of both methods.

On one hand, the sample containing a small amount of grain boundaries (sample A) presented the same results of speed of sound calculated from the reduced DPS and obtained with RUS, with only a small part of the reduced DPS data being above the asymptotic limit from RUS. On the other hand, the reduced DPS of the sample with larger amount of grain boundaries, defects, and amorphous contribution (sample C) is significantly above the asymptotic limit from RUS and has a pronounced increase for $E \rightarrow 0$. We therefore conclude that the excess states in the reduced DPS, which is probed only above 3 meV, are above the asymptotic limit and can be considered as contribution due to the larger amount of grain boundaries, defects and amorphous inclusions.

The specific heat, represented as C_p/T^3 vs. T , of the nanocrystalline silicon samples measured between 4 and 400 K compared to bulk Si is shown in Fig. 4. The nanocrystalline samples have the same C_p at high temperatures as bulk Si. Below 30 K an increased lattice contribution, related to the increased Debye level and decreased speed of sound, is observed. Further, an electronic contribution, linear in temperature, and thus $\propto 1/T^2$ in C_p/T^3 , is observed at the lowest temperatures, because with such high carrier concentrations, in the % range, there is no freeze-out of the charge carriers as would be expected in semiconductors.

At the lowest temperatures, a simple model of the heat capacity can be designed by considering an electronic contribution (γT) and a lattice contribution that can be described using the Debye model and an Einstein term to describe the excess C_p at approximately 45 K:²⁵

$$C_p(T) = \gamma T + dC_D(T) + eC_E(T) \quad (1)$$

where d and e are prefactors for the Debye and Einstein contributions, $C_D(T)$ and $C_E(T)$, respectively. More details about the Debye and Einstein models can be found in ref. 35–37. A fit to the data up to 90 K yields parameters as summarized in Table 3. The electronic contribution ($\gamma \approx 0.1 \text{ mJ mol}^{-1} \text{ K}^{-2}$) is close to that obtained on the specific heat of metals ($0.6\text{--}2.5 \text{ mJ mol}^{-1} \text{ K}^{-2}$),³⁶ and shows a significant presence of electronic contribution in the samples. The values obtained for the Einstein and Debye temperatures were also converted to energy ($1 \text{ K} = 0.0862 \text{ meV}$) and the Einstein energies are in very good agreement with the feature observed at this energy ($\approx 16 \text{ meV}$) in the reduced DPS (Fig. 3). The Debye temperature obtained from a fit in this temperature range (Θ_D^{HT}) differs from the temperature obtained considering only the low temperature Debye plateau (Θ_D^{LT}), as it probes higher energies phonon modes. For the calculations of the speed of sound from the specific heat, $v_s = k_B \Theta_D^{\text{LT}} / \hbar (6\pi^2 N_V)^{1/3}$, only the Debye plateau was considered, and yields values as summarized in Table 2.

3.3 Thermoelectric and transport measurements

The general trend of the electrical conductivity (σ) of all samples between room temperature and 750 °C demonstrates a decrease with temperature as expected for degenerately doped semiconductors (Fig. 5(a)). This occurs due to the increase of the lattice vibrations in this range of temperature, *i.e.* electron scattering by phonons dominates the observed temperature trend, as in metals. Above this temperature an additional contribution is observed leading to a kink in σ which increases with temperature above temperatures of 750 °C. Such a kink in a n-type semiconductor might a priori be attributed to bipolar contributions,³⁸ when additional p-type charge carriers are thermally activated over the band gap of the semiconductor, but this explanation does not hold for silicon, which has a too large band gap. An alternative explanation for a similar kink previously observed on nanocrystalline Si by Bux *et al.*,³² is the kinetics of dopant precipitation related to the retrograde solid solubility of phosphorus in silicon.³⁹ As the temperature rises, additional phosphorus atoms are being incorporated at substitutional lattice sites and become electrically activated. This leads to a rapid increase in carrier concentration and

Table 3 Values of the electronic contribution (γ), Einstein and Debye temperatures as well as heat capacity prefactors (e and d) obtained with a fit of the eqn (1) for low temperatures (below 90 K)

	$\gamma \text{ (mJ mol}^{-1} \text{ K}^{-2}\text{)}$	$e \text{ (J mol}^{-1} \text{ K}^{-1}\text{)}$	Θ_E		$d \text{ (J mol}^{-1} \text{ K}^{-1}\text{)}$	Θ_D^{HT}	
			(K)	(meV)		(K)	(meV)
Bulk	—	3.8(3)	188(2)	16.2(2)	11.4(3)	501(17)	43(2)
Sample A	0.114(5)	2.76(7)	186(1)	16.0(1)	9.8(1)	410(5)	35.3(5)
Sample C	0.12(2)	2.02(3)	184(1)	15.9(1)	11.2(9)	402(11)	34.6(9)



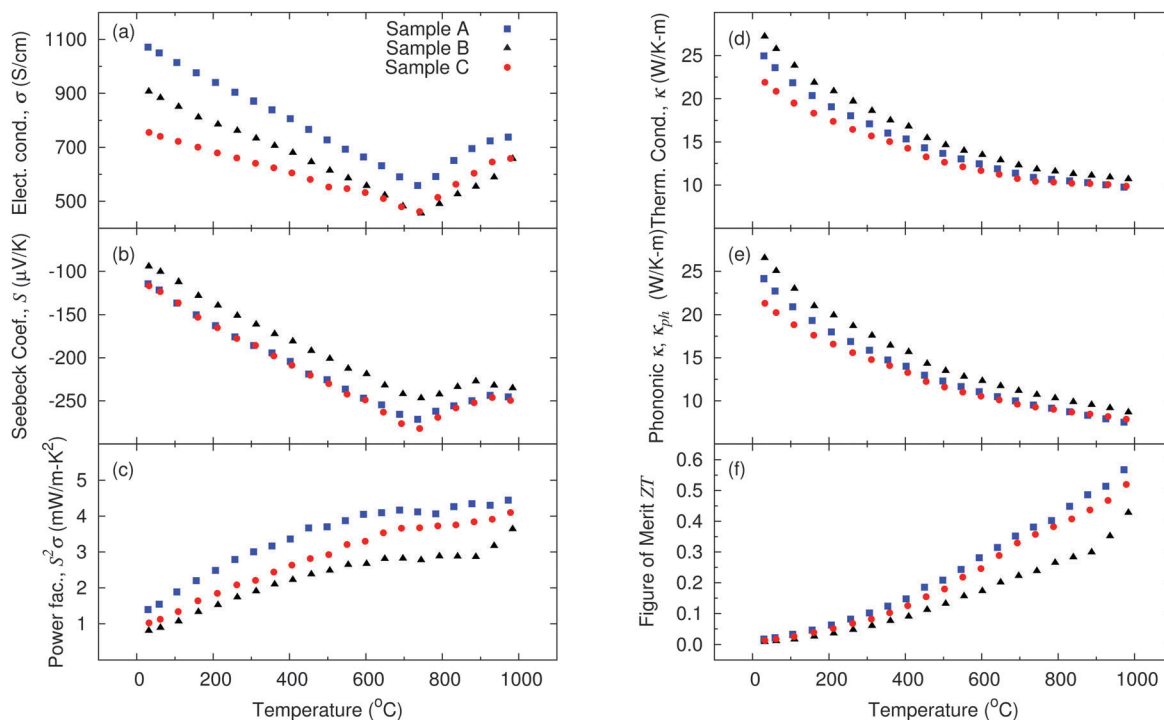


Fig. 5 Thermoelectric characterization of the 3 nanocrystalline Si samples: (a) electrical conductivity; (b) Seebeck coefficient; (c) calculated power factor; (d) thermal conductivity; (e) calculated lattice contribution to the thermal conductivity and (f) calculated dimensionless figure of merit.

consequently an increase of the electrical conductivity as well as a decrease of the Seebeck coefficient. This is possible because at low temperature less phosphorus atoms are electrically activated than chemically incorporated. The tendency towards hysteresis³⁹ in the heating and cooling cycles confirms dopant kinetic as an explanation of this kink rather than the bipolar effect.

The Si sample with smaller nanocrystallite sizes presents a lower electrical conductivity between room temperature and 750 °C when compared with the two other samples. The sample which was sintered for a longer period of time has lower σ than the sample with large nanocrystallites sintered for a short time.

Both samples which were sintered for a short period of time presented similar values of the Seebeck coefficient (Fig. 5(b)), *i.e.*, likely a very similar charge carrier concentration. The sample with smaller nanocrystallites presented a lower σ than the sample with larger crystallites, due to a large amount of grain boundaries, defects and amorphous contribution leading to a more pronounced scattering of electrons. This results in a better power factor for the sample with large nanocrystallites, but sintered for a short period of time (Fig. 5(c)).

Although the sample which was sintered for a longer period of time (sample B) had a slightly higher density when compared with the other samples (only 1.1% higher, see in Table 4), its

Table 4 Summary of room temperature properties for all nanocrystalline Si samples, compared with previously published results on spark plasma sintered bulk nanocrystalline Si and single-crystal Si

	Single-cryst. ³²	Nanocryst. ³²	Nanocryst. ²⁵	Sample A	Sample B	Sample C
Nanoparticles production	—	Ball-milling	Gas phase synthesis		Gas phase synthesis	
SPS temperature (°C)	—	—	1050	1150	1150	1150
SPS hold time (min)	—	—	3	3	30	3
Additives/impurities	—	(From ball-mill)	P, SiO ₂ , H	P	P	P
Av. nanocryst. size (nm)	—	50–100	30	42	58	33
Density (g cm ⁻³)	2.329	—	2.189	2.259	2.284	2.257
S (μV K ⁻¹)	-86	-70	-81.2	-94.3	-116	-114
ρ (μΩ m)	3.3	9.1	23.7	9.3	11.0	13.2
n_{Mott} (×10 ²⁶ m ⁻³)	—	—	—	1.3	1.6	1.3
μ_{Mott} (×10 ⁻⁴ m ² V ⁻¹ s ⁻¹)	—	—	—	52	36	38
n_{Hall} (×10 ²⁶ m ⁻³)	4.5	4.6	—	1.1	2.3	1.0
μ_{Hall} (×10 ⁻⁴ m ² V ⁻¹ s ⁻¹)	42.8	15.1	—	61	25	47
κ_{Total} (W K ⁻¹ m ⁻¹)	89.3	7.0	14.8	25.0	27.2	21.9
κ_{Lattice} (W K ⁻¹ m ⁻¹)	87.3	6.3	14.5	24.3	26.6	21.4
$S^2\sigma$ (mW K ⁻² m ⁻¹)	0.3	0.5	0.2	1.4	0.8	1.0
ZT at RT	0.008	0.023	0.0055	0.017	0.009	0.014
ZT_{max} at 980 °C	—	0.68	—	0.57	0.43	0.52

electronic properties were not better. During the long sintering period (30 minutes) at high temperatures (1150 °C), diffusion processes occur. Those do not only lead to a healing of defects, which rather improve the crystalline quality of the sample as seen by higher values of thermal conductivity (Fig. 5(d)) and by the higher density, but also to diffusion of the impurities (dopants). The latter have a tendency to aggregate on grain boundaries. This agglomeration of dopants can be seen in the weak increase in σ for $T > 750$ °C. Overall, the power factor of this sample is lower than for the two samples sintered within only 3 minutes (samples A and C), see Fig. 5(c).

The charge carrier concentration (n) can be estimated from the slope of the Seebeck coefficient (for $T < 750$ °C):³⁸

$$S = \frac{8\pi^2 k_B^2}{3eh^2} m^* T \left(\frac{\pi}{3n} \right)^{2/3} \quad (2)$$

where k_B is the Boltzmann constant, h is the Planck constant, e is the elementary charge and $m^* = 1.13m_{e,0}$ ⁴⁰ is the reduced band effective mass of electrons in silicon. Band transport in one parabolic band as well as an energy independent scattering time were assumed to derive this relatively simple transport model from the Mott equation,⁴¹ strictly valid only in metals but useful also for the analysis of degenerated doped semiconductors. A comparison between Hall data and an evaluation of the Seebeck coefficient for nanocrystalline silicon showed a decent agreement for electron mobility and charge carrier concentration,⁴² so that this simple approximation is used here to compare nano silicon transport data. From the combined measurement of the Seebeck coefficient and the electrical conductivity, we estimated the mobility of the charge carriers, μ , with $\sigma = ne\mu$. In addition, as the Mott equation is not strictly valid for doped semiconductors, we have determined the charge carrier density in sample A and B from the Hall coefficient, R_H , $n = 1/R_H e$ assuming a Hall factor value of 1. The obtained charge carrier densities from the latter method are in reasonable agreement with those obtained from the Mott formula. The values obtained are summarized in Table 4 and compared with literature data. The difference between the lattice thermal conductivity and total thermal conductivity, *i.e.* the electronic contribution, κ_e , has been estimated using $\kappa_e = LT/\rho$, where $L = 2.2 \times 10^{-8} \text{ W } \Omega \text{ K}^{-2}$ is the estimated Lorentz factor for highly doped Si.³² The mobility obtained for the samples under investigation is larger than in heavily doped bulk single crystalline silicon,³² which might seem surprising. However, as the mobility is dependent on the charge carrier concentration and decreases with increasing concentration at very large doping level,⁴³ this observation is reasonable.

Comparing the samples produced from different nanoparticle batches (14 nm vs. 52 nm), but sintered for the same short period of time (3 minutes), no significant decrease of the thermal conductivity was observed, since sample A showed a more pronounced grain coarsening during sintering. The sample with initially smaller nanocrystallite size has a thermal conductivity κ which is 12% lower at room temperature than the sample with initially larger nanocrystallite size, but at high temperatures the thermal conductivity data of both samples converges.

The lattice contribution to the thermal conductivity accounts for up to 97% of the total thermal conductivity at room temperature and decreases to around 77% at the highest measured temperature. In single crystalline silicon, 90% of the heat is transported by phonons with mean free path larger than 100 nm.⁴⁴ Therefore, an average grain size around 100 nm or slightly smaller is already effective in lowering the lattice thermal conductivity as can be seen from the investigated samples.

The thermal conductivity of the pure nanocrystalline samples studied in this paper is still large when compared with previously reported results on nanocrystalline Si,^{25,32,42} but in those samples, several impurities were present either from exposing the nanopowder to air before sintering^{25,42} or due to additives used for nanopowder preparation with ball-milling.³² These impurities may significantly affect the mobility of charge carriers, μ , leading to a smaller power factor for the samples in earlier reports than for the samples discussed herein, see Table 4. Next to impurities, a second possible cause for both the higher mobility and thermal conductivity for the samples investigated here, is the fabrication method. Where the bottom up gas phase synthesis followed by sintering is expected to lead to well crystallized particles, the top down approach using ball-milling³² is more prone to lead to a strained lattice, and thus, smaller mobility but also smaller thermal conductivity.

Overall, despite the large thermal conductivity, the dimensionless figure of merit of the silicon nanocomposites investigated herein still reaches competitive values due to a very high carrier mobility resulting in comparatively high power factors. With a ZT of 0.57 at 973 °C, the sample produced with 52 nm nanoparticles and sintered for 3 minutes can compete with other results published so far,³² with the advantage of a more easily scalable production process.

4 Conclusions

The three different nanocrystalline Si samples which were analyzed in this work showed interesting lattice dynamics and thermoelectric properties depending on their synthesis parameters. Both samples which were prepared with the same nanoparticle size, but sintered for different periods of time, presented same results on the study of their lattice dynamics: a decrease in the speed of sound when compared to single-crystalline Si. The sample which was sintered for a longer period (30 min) showed also a decrease in the thermoelectric properties with a lower power factor and an elevated thermal conductivity due to improved crystallinity.

The sample with small initial nanoparticle size showed a significant grain growth during sintering as analyzed by XRD refinement and TEM, and also a larger amount of defects and a certain amount of amorphous precipitates, leading to a further decrease on the speed of sound and to an excess of vibration modes at low energies. It also presented slightly worse electronic properties, which compensates the lower thermal conductivity and leads to a similar dimensionless figure of merit as the



sample prepared with larger nanoparticles and same sintering parameters.

A systematic trend in the decrease of the speed of sound obtained from the density of phonon states, resonant ultrasound spectroscopy, and specific heat, combined with the large amount of grain boundaries in nanostructured Si materials, resulted in a thermal conductivity four times lower than for a single-crystal.

When compared with previously reported results on nanocrystalline Si, the samples still present a somewhat large thermal conductivity, which is compensated by a very high power factor and results in competitive values of the dimensionless figure of merit with a peak ZT of 0.57 at 973 °C. When compared to other materials which are used in this temperature range such as nanocrystalline SiGe, Si has a ZT which is approximately half of the results reported so far (1.3 at 900 °C⁴⁵), with the advantage of being approximately 14 times cheaper than SiGe.

Since the thermal conductivity of the nanocrystalline Si samples presented in this work is still large when compared to other thermoelectric materials, further optimization of the parameters leading to the reduction of the thermal conductivity could lead to an even better ZT value.

Furthermore, studies have shown that the energy cost of Si nanopowder production through gas phase synthesis is drastically reduced with increasing production amount.⁴⁶ Therefore, when compared with other methods such as ball-milling, gas phase synthesis has the great advantage of being a continuous and a more easily scalable method.

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