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The first HyDRA challenge for computational vibrational spectroscopy†

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Vibrational spectroscopy in supersonic jet expansions is a powerful tool to assess molecular aggregates in close to ideal conditions for the benchmarking of quantum chemical approaches. The low temperatures achieved as well as the absence of environment effects allow for a direct comparison between computed and experimental spectra. This provides potential benchmarking data which can be revisited to hone different computational techniques, and it allows for the critical analysis of procedures under the setting of a blind challenge. In the latter case, the final result is unknown to modellers, providing an unbiased testing opportunity for quantum chemical models. In this work, we present the spectroscopic and computational results for the first HyDRA blind challenge. The latter deals with the prediction of water donor stretching vibrations in monohydrates of organic molecules. This edition features a test set of 10 systems. Experimental water donor OH vibrational wavenumbers for the vacuum-isolated monohydrates of formaldehyde, tetrahydrofuran, pyridine, tetrahydrothiophene, trifluoroethanol, methyl lactate, dimethylimidazolidinone, cyclooctanone, trifluoroacetophenone and 1-phenylcyclohexane-*cis*-1,2-diol are provided. The results of the challenge show promising predictive properties in both purely quantum mechanical approaches as well as regression and other machine learning strategies.

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1 Introduction

The 'Pauling point' is a term which has slowly faded out of use through the years, but which should be as relevant today as when it was first introduced. Its origins are discussed, for example, in ref. 1, 2. It refers to the point in a project where the theoretical predictions exactly match the experimental observables, but if one were to proceed and further improve on the calculations (*e.g.*, larger basis sets, remove approximations such as the harmonic approach, *etc.*...) such agreement would disappear. Whenever one resorts to numerical methods to solve a physical problem, it is often the case that there are enough buttons to push and knobs to turn in a way that a close to perfect cancellation of error arises. This can happen accidentally, but the 'Pauling point' is often times actively pursued when the target observables are known. So, instead of aiming for the most advanced description possible, one might use and/or recommend relatively low levels of theory which have shown promise in a known chemical subspace. However, the true test to quantum chemistry is its potential for prediction over a large chemical space. Aiming for cheaper solutions might be deterrent to this ultimate goal. This raises the question of how to foster better practices or discover computational protocols robust enough to be used for predictions in an unbiased way.

Blind challenges in the field of computational chemistry have become more and more popular over the past years. Particularly noteworthy examples thereof are the Statistical Assessment of Modeling of Proteins and Ligands (SAMPL) challenges initiatives^{3,4} and the Cambridge crystallographic database structure challenges.^{5,6} This is followed in smaller scale by individual groups initiatives,^{7,8} or even in structured round-robin tests.⁹ Whatever the case may be, these challenges provide unique opportunities to pit different methods to the same observable in a collegiate (optimally unbiased) fashion. A previous challenge^{8,10} promoted by some of the groups involved was the furan-methanol challenge, whereby the binding preferences of methanol and a series of modified furan molecules was under scope. The question posed to the theoretical groups was to identify the most stable binding motif, an OH...O or OH... π bound conformer. Although the experimental data for the challenge were jet-cooled vibrational spectra, the target quantities were energy differences. The latter were estimated from the relative heights of the observed absorption peaks for the different binding modes. Albeit this being an indirect measurement, conservative error estimates were still below 1 kJ mol⁻¹, well beyond the error bar of commonly accepted theory benchmarks.¹¹

In this new joint effort, the observable to be tested is no longer inferred from the spectra. The goal is to correctly predict the experimental red shift of the OH bond stretch in 1:1 monohydrate complexes relative to the free symmetric stretch. This builds a much more rigorous connection point between theory and experiment in the important field of micro-hydration,^{12,13} as a quantity that both sides of the table feel comfortable estimating with minimal modelling on the

experimental side. With its sensitivity to both electronic structure and nuclear motion aspects,¹⁴ it promises interesting error cancellation and thus Pauling point situations. As monohydrates are vibrationally¹⁵ far less characterised than rotationally,^{16,17} the topic also leaves enough playground for blind testing. As the layout of this blind test has been described extensively before,¹⁸ we refrain from repeating the experimental tools^{19–21} and caveats.²²

As detailed in our first publication introducing the challenge,¹⁸ a set of 10 hydrate systems were selected as 'training set', in order for the participants to fine tune or validate beforehand their approaches. The latter consisted of: acetone (ACE), acetophenone (APH), 1,2,4,5-tetrafluorobenzene (TFB), 1-phenylethanol (POH), imidazole (IMZ), aniline (ANL), dibenzofuran (DBZ), di-*tert*-butyl nitroxide (DBN), *o*-cyanophenol (OCP) and cyclobutanone (CBU). Another set of 10 structures was chosen¹⁸ and presented as the target of the challenge – from now on referred to as 'test set'. The latter consisted of: cyclooctanone (CON), 1,3-dimethyl-2-imidazolidinone (DMI), formaldehyde (FAH), methyl lactate (MLA), 1-phenylcyclohexane-*cis*-1,2-diol (PCD), pyridine (PYR), tetrahydrofuran (THF), tetrahydrothiophene (THT), 2,2,2-trifluoroacetophenone (TPH) and 2,2,2-trifluoroethan-1-ol (TFE), all previously uncharacterised in terms of the experimental water stretching vibrations in the vacuum-isolated complex. The participants were given 6 months between the test set reveal and a submission deadline. Following said deadline, any inconsistencies in the submissions were addressed. One issue we had to address was the use of different levels of theory within a single submission (*i.e.*, higher levels of theory for the smaller systems, computationally cheaper approaches for the larger cases). Our solution was in general to ask the participants to split the data into different sets. This was done to increase the amount of information about the different levels of theory featured, while ensuring a strict unique procedure (level of theory) per computational data set. There were also some issues with the definition of the reference – the symmetric water OH stretch. This was the only value which we allowed to be revised. Otherwise, all of the data was kept as submitted, even including mistakes in the molecular structure. TFE and PCD values in submission PH1 were based on the wrong molecules, same as with DMI in PH4 and FA3. These issues are discussed in further detail later in the text.

As previously discussed,¹⁸ the training and test sets covered roughly the same range of wavenumber downshifts, from a very low (10 and 8 cm⁻¹ for TFB and TFE respectively) to a rather high end (199 and 203 cm⁻¹ for IMZ and PYR respectively). Fig. 1 provides the Lewis structure of the compounds selected for both sets, as well as the experimentally obtained absolute position of the water OH donor stretch bands.

2 List of submissions

In order to facilitate the discussion of the computational submissions, we established four categories, depending on the methods used to produce predictions.



Table 2 Listing of submissions and a short summary of the respective computational protocol

Submission	Computational protocol
PH1	B3LYP-D3(BJ)/def2-TZVPP harmonic values
PH2	PBE0-D3/aug-cc-pVTZ harmonic values
PH3	ω B97xD/def2-TZVP harmonic values
PH4	B3LYP-D3(BJ)/def2-TZVP harmonic values
PH5	MP2/6-31++G(2d,p) counterpoise-corrected harmonic values
PH6	CCSD-F12/aug-cc-pVDZ harmonic values
PH7	MP2-F12/aug-cc-pVDZ harmonic values
AC1	ω B97xD/def2-TZVP with 1D numerical differences along the donor OH stretch normal mode
AC2	Reproducing Kernel Hilbert Space+DVR3D based on B3LYP-D3(BJ)/aug-cc-pVTZ structures
AC3	B2PLYP-D3(BJ)/aug-cc-pVTZ with selected anharmonic modes calculations
AC4	MP2/6-311++G(d,p) counterpoise-corrected 2-D QFF cc-VSCF
FA1	Quasi-classical B3LYP-D3/aug-cc-pVDZ trajectories
FA2	VPT2 PBE0-D3(BJ)/aug-cc-pVTZ anharmonic values
FA3	VPT2 B3LYP-D3(BJ)/def2-TZVP anharmonic values
FA4	CCSD-F12/aug-cc-pVDZ harmonic+PBE0-D3(BJ)/aug-cc-pVTZ anharmonic corrections
FA5	MP2-F12/aug-cc-pVDZ harmonic+PBE0-D3/aug-cc-pVTZ anharmonic corrections
LS1	PAW PBE-D3 adjusted with a 2-parameter linear regression function extracted from the training set values
LS2	Kernel prediction of harmonic frequencies + delta learning correction with respect to the experiment
LS3	Neural network on B3LYP-D3(BJ)/aug-cc-pVTZ structures + transfer Learning to experiment
LS4	PBE0-D3(BJ)/aug-cc-pVTZ aug-cc-pVQZ adjusted with a 5-parameter linear regression function

band of the 1 : 1 complex emerges at 3474 cm^{-1} . Minor satellite contributions near 3477 and 3491 cm^{-1} may be due to traces of larger complexes or due to dark overtone and combination states stealing some intensity from the OH stretching fundamental by perturbation. If the latter is true, the deperturbed (zeroth-order) state which should be compared to a harmonic or low-order anharmonic prediction is slightly higher than the peak wavenumber, perhaps around $3475\text{--}3478\text{ cm}^{-1}$. However, this is not so relevant, because the Raman spectrum is most sensitive for the in-phase stretching of the two OH oscillators. The out-of-phase stretching mode is better seen in the Raman spectra of the more concentrated expansions (central traces) at 3524 cm^{-1} and it is very prominent in the IR spectra (lowest spectrum in Fig. 2), because it involves a larger change of the dipole moment. As shown in the ESI,[†] it is the only strong transition attributable to the monohydrate in this spectral window and therefore corresponds to the requested wavenumber for the challenge. However,¹⁸ O-substitution in the water molecule demonstrates that both the out-of-phase and the in-phase OH stretching signals involve some water character, because they both downshift (see ESI[†]). As the downshift is more pronounced for the 3524 cm^{-1} band (8 vs. 5 cm^{-1}), this is the band which should be compared to single theoretical predictions of the water OH stretch. Evidently, a comparison of both wavenumbers (listed in Fig. 1 for MLA) to their theoretical counterparts could be valuable as well in this particular case, but will be left for the future and the individual theory groups.

The OH group contained in TFE might have caused a similar mode mixing problem,²⁵ but here the coupling to the water OH is sufficiently weak for an unambiguous assignment. This is also the case for PCD,²⁶ where the monohydrate features a network of three coupled OH oscillators but only one of them shows a strong isotope shift upon ¹⁸O substitution (ESI[†]).

The experimental downshifts from the symmetric water monomer stretch in the test set span a range of $8\text{--}203\text{ cm}^{-1}$ and thus exclude the more challenging strong hydrogen bonds,

where the likelihood of anharmonic resonances increases substantially. None of the 10 test systems involves a proven b2lib resonance,²² where the water bending overtone (b2) and hydrogen bond libration (lib) ternary combination band steals intensity from the OH stretch fundamental. Therefore, the raw experimental data can be compared directly to the theoretical predictions, keeping in mind that there may be some mode mixing issue for the multi-chromophore systems MLA, TFA and PCD. Only in the MLA case is this mixing supported by experiment.

The experimental uncertainties of the OH stretches vary slightly. They only exceed $\pm 2\text{ cm}^{-1}$ for the MLA case due to satellite bands close to the MLA-centered mode and for the PCD case due to the convolution between the rotational contour and the resolution of the laser used in the IR-UV experiments. Therefore, the individual experimental uncertainties of the test systems do not enter the following analysis.

3.2 Uncertainties in computed values

When formulating the challenge, uncertainty estimates were requested for all submissions. However, very few of the entries included such estimates, somewhat reflecting a common practice in the theoretical chemistry community. There is a heavy reliance on established methodologies, but little information on how the performance of the method can be derived from the previous works. The only submissions which provided error estimates were LS1, FA1 and LS4.

Given that the training data was available for all the groups, any participant who also computed the training set (even if partially) would have been in a position to provide uncertainty estimates based on the performance of the method. Learning strategies heavily dependent on the latter would likely underestimate the uncertainty, but could provide this information nonetheless. LS1 provided a rather small uncertainty of 8 cm^{-1} , similar to that of LS4 (7 cm^{-1}). Both made use of linear fitting expressions, with comparable fitting quality for the test set.



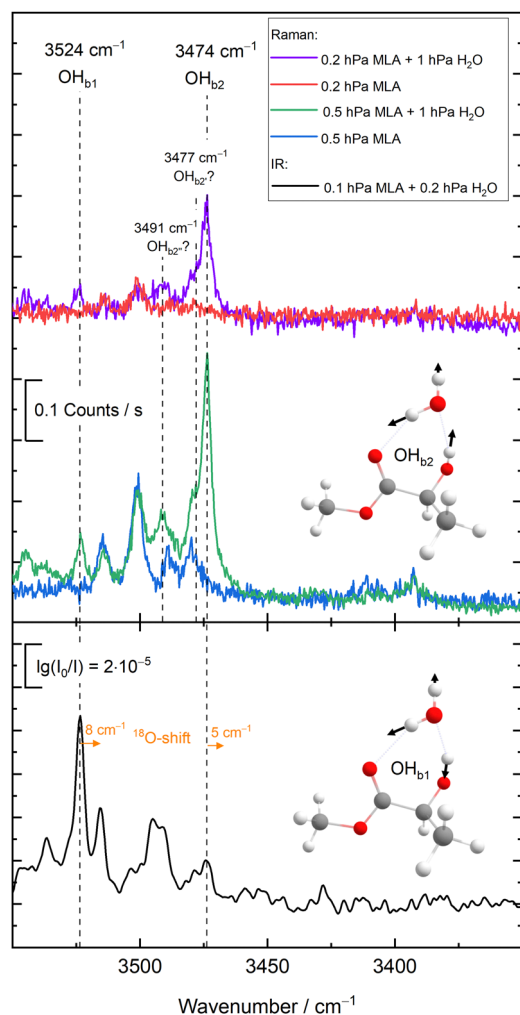


Fig. 2 Experimental Raman (top) and IR spectra (bottom) for the MLA monohydrate, showing by isotope substitution that the two OH stretching modes are coupled and that the higher-wavenumber transition OH_{b1} is dominated by water stretching motion. See text for details.

In the case of FA1, the only other submission with uncertainty quantification, the value was 16 cm^{-1} , taken to be slightly above the mean average error of the training set quasi-classical simulation results.

Finally, one should note that one could make use of other deviation measures instead of relying on the root-mean-square deviation (RMSD).²⁷ It is for example common to report the mean absolute error (MAE). However, the latter will give the smallest error estimates, as it tends to lessen the weight of outliers. Given that we are critically assessing the predictive power of computational protocols, a measure like RMSD seems a more natural choice. For fairness, we will also consider results when removing the largest outliers of each set, trying to set an equal footing for all submissions, whether complete or incomplete.

3.3 General performance

The full results are provided in the ESI,[†] as well as ref. 28. For the sake of clarity and ease of interpretation, most of our discussion will be based on general statistics and we will avoid

as much as possible to focus on single instances. Often times, we will compare the results to a null hypothesis, which is constructed by taking the average of the training systems shifts. This requires no computation and provides a single estimate of 99.7 cm^{-1} for all test systems. The RMSD of the null hypothesis for the measured test values is 62.3 cm^{-1} , which we will take as a general quality measure.

A close inspection of the individual submissions showed that a few submissions made in fact use of the wrong organic molecule. We will mention this in the text. Of less concern was the computation of different minima. The most problematic system in this respect was PCD, with two alcohol groups. Otherwise, only small deviations were observed. It was commonly found in the TPH and FAH geometries that the water molecule was binding out of plane, breaking C_s symmetry. This seems to have a minimal impact on the predicted wavenumbers. Independent calculations were carried out at the CCSD(T)/aug-cc-pVTZ^{29–31} level of theory, confirming that the global minimum for both complexes should localise the water molecule in plane.

In order to give an overview of the submitted values, we provide in Fig. 3 the errors for each entry. For ease of visualisation, a kernel density estimator has been used, showing in bright yellow value ranges with a large number of submissions. The RMSD of the null hypothesis ($\pm 62.3 \text{ cm}^{-1}$) is delimited by the dotted white lines. A few observations can be readily made. Most of the submitted values do outperform the null hypothesis. Although this is a low bar, it is not necessarily a given. If the quantity of interest had a low spread (small range of test values), the null hypothesis would be hard to compete with, as has been observed in other blind challenges (see for example ref. 32). Another observation to make is that there is no apparent systematic error (too small or too large shifts) with a fairly balanced distribution around 0. The density distribution readily highlights DMI, FAH and TFE as the systems with the best quality estimates, despite the fact that a few outliers (with errors beyond 62 cm^{-1}) are observed. Rewardingly, these three systems span relatively strong, intermediate and very weak hydrogen bonding.

It is rather hard to analyse the results bundling all submissions together. In Fig. 4 an overview of the performance for all submissions is provided, taking the RMSD in the test set as a measure. This choice is not without bias, given that not all submissions included all 10 test systems. Nonetheless, it does allow for some first general considerations in regard to the different types of calculations. The best fully anharmonic submission (FA3) still exhibits a RMSD of 38.5 cm^{-1} , a rather large value considering that the shifts only go up to 203 cm^{-1} . It is in general the class with the lowest performance. Only 6 submissions are below the 30 cm^{-1} mark (PH5, AC2, AC4, LS1, LS3 and LS4) and 4 below 15 cm^{-1} (PH5, AC2, LS3 and LS4). Somewhat surprisingly, this shows that a similar accuracy can be reached with wildly varying approaches to the problem. Learning strategies do show some advantage, but the differences are not so significant that one would immediately exclude other approaches to the problem.



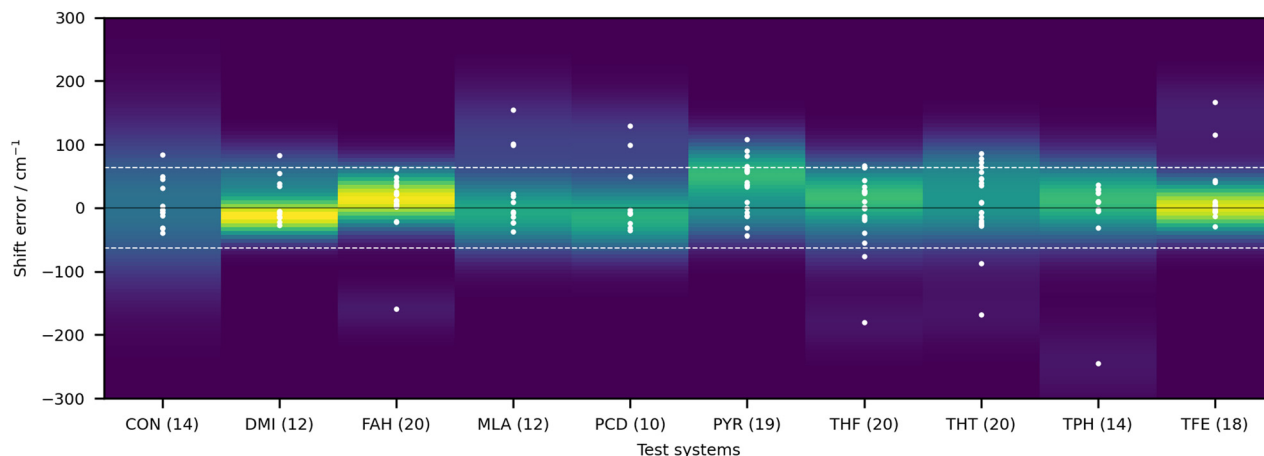


Fig. 3 Deviations of the submitted OH stretch shifts relative to the measured experimental values (raw values) in cm^{-1} for the 10 test systems. A positive error means that the predicted wavenumber downshift from the monomer is too large. Each value is represented as a white dot (only one value is outside of the visualisation window, AC1 submission for CON, with an error of 460.5 cm^{-1}). The color coding of the graph is provided by the probability density function of the error for each system. Yellow indicates larger density values, dark blue low density. The bandwidth selection has been made with Scott's rule.³³ The dotted line delimits the RMSD range of the null hypothesis (62.3 cm^{-1}), obtained as described in the text.

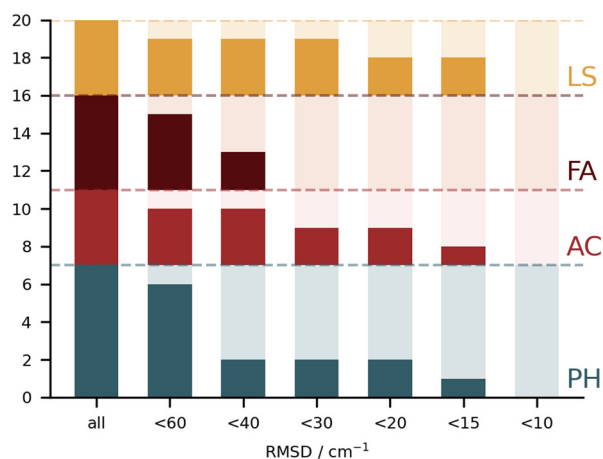


Fig. 4 Stacked bar chart showing the number of submissions which exhibit root-mean-square deviations below selected values, grouped according to the four general classes of calculations. Four submissions showed RMSD values below 15 cm^{-1} (PH5, AC2, LS3 and LS4) but none reached below 10 cm^{-1} .

In the following text, we mention correct and incorrect structures based on the large agreement observed for the best submissions. These are considered as reference global minima and are then used to evaluate the other entries. The organisers of the challenge have not independently confirmed all of the minima for their stability.

3.4 Purely harmonic (PH) submissions

On paper, purely harmonic estimates should be the class of calculations with the least chance of success. They stand as the most accessible calculations, but will carry the full error of anharmonic effects. However, we have already observed in previous blind challenges^{8,10} that harmonic approaches can be surprisingly effective. In the furan-methanol challenge,

the delicate energy balance between different conformers was critically dependent on the quality of the zero-point vibrational energy (ZPVE) estimates. However, the most successful entries in general only included harmonic estimates, while some anharmonic ZPVE corrections provided the wrong energetic ordering. It all boils down to the degree of error compensation in the model chemistry chosen. In the present case, most of the anharmonicity of an OH group is diagonal in nature and does not change much upon hydrogen bonding.^{34,35} By a quite significant margin, the best submission in this class was PH5, making use of MP2/6-31++G(2d,p)^{36,37} counterpoise-corrected harmonic values. The RMSD for all submissions in this class are depicted in Fig. 5. We provide values incrementally removing the worst prediction of each set, in order to compare in a more balanced way the different submissions.

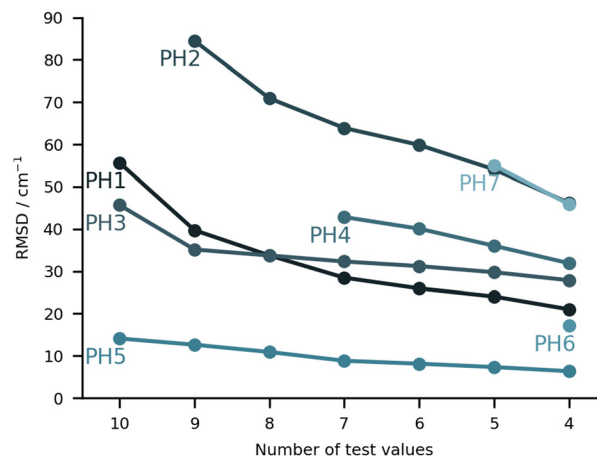


Fig. 5 RMSD values (in cm^{-1}) for the purely harmonic (PH) submissions. The values are provided incrementally removing the worst prediction of each set, in order to compare in a more balanced way the different submissions.



The largest deviations for PH1 and PH3 are due to wrong structures for the PCD minimum upon which the frequencies are based. In the case of PH1 the wrong organic molecule was used, 1-phenylcyclohexane-*cis*-2,5-diol instead of 1-phenylcyclohexane-*cis*-1,2-diol. In the case of PH3, a different minimum was found, leading to an error of 98.7 cm⁻¹ for PCD. The water is correctly pointing to the ring system, but also is hydrogen bonding to one of the alcohols (in the accepted global minimum it should be accepting a bond from the alcohol). We provide the overlap of two selected PCD complex structures in Fig. 6. Both sets are of relatively similar quality, with B3LYP-D3(BJ)/def2-TZVPP^{38–44} (PH1) and ω B97xD/def2-TZVPP⁴⁵ (PH3) delivering the overall same level of accuracy. Once the outliers are removed, the RMSD is found to be below 40 cm⁻¹ (Fig. 5).

The PH2 submission worst value (for MLA, error of 155 cm⁻¹) does not appear to be due to the minimum chosen, but solely the approach used. The PBE0-D3/aug-cc-pVTZ⁴⁶ level of theory reveals large errors for the whole set, at least as submitted by the participating group. The only geometry which was not correctly predicted was for TPH. The water binds to the side of the trifluoro group, when it should be docking to the carbonyl group from the opposite end. Despite the wrong geometry, and through error compensation, the deviation is only 23 cm⁻¹, the second best prediction in PH2. Curiously enough, despite the similarity in method between PH1 and PH4, the smaller basis set chosen in the latter submission seems to have a sizeable impact (an almost constant 15 cm⁻¹ increase in RMSD). All structures of PH4 were in line with the best results, with the exception of DMI, where 2,5-dimethylpyrrole was wrongly used. Attempting to build a summary for this class of submissions, and removing the impact of wrong structure submissions, there was a decisive advantage in the use of the MP2 method and a small basis set. This could be due to the well documented fact that MP2 will overcorrect Hartree-Fock in predicting OH stretching hydrogen bond shifts (too large downshifts).³⁴ By reducing the basis set, the amount of

electron correlation described decreases, compensating the harmonic and method errors. This is partly confirmed in the harmonic estimates underlying the AC4 submission, where the basis was expanded to 6-311++G(d,p) and the results were overall worst (if no anharmonic corrections were included).

3.5 Anharmonic corrected (AC) submissions

In this class of submissions (Fig. 7), we have partly anharmonically corrected values for the bonding OH stretch. AC1 makes use of the ω B97xD/def2-TZVP level of theory (the harmonic results built the PH4 set), and extends the prediction by including anharmonic corrections to the OH stretch mode. This was performed by computing numerical differences along the normal coordinates. The large errors found in this particular set are a direct consequence of the procedure used. When adding an anharmonic correction AC2 and AC4 are among the best submissions for this challenge. In the case of AC2, internal potentials for the water molecule in each monohydrated system were built from B3LYP-D3(BJ)/aug-cc-pVTZ calculations (a functional which was already confirmed to give good results in the PH category). The latter PESs were then used as reference to respectively fit three Morse potentials for the internal degrees of freedom of water adding a Reproducing Kernel Hilbert Space (RKHS) correction term^{47,48} which accounts for 2- and 3-mode coupling. The vibrational states are then computed with the Discrete Variable Representation Method (DVR) and the DVR3D program package,^{49,50} using the water molecule geometry as in the hydrated complex. This approach lays the focus on the treatment of the water internal potential, neglecting any coupling with the organic molecule vibrations. In case strong resonance effects or even harmonic mixing with alcohol groups would be present, this effect could not be captured, but this was not a point of concern for the set of molecules chosen in the challenge. It should be noted that the largest deviation in AC2 is found for the PYR system (36 cm⁻¹ error), which is also where the largest experimental shift is observed. Close in

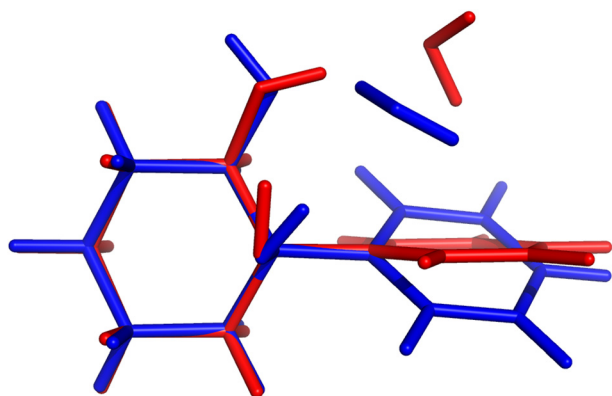


Fig. 6 Comparison of PCD hydrate complex structures submitted by LS1 (red) and PH3 (blue). In the latter case, the water molecule functions both as acceptor and donor to the alcohol moieties. In the structures featured in submissions with lower RMSD, the water is actually pointing towards the π -system, interacting with only one of the alcohols. This gives a much lower shift, in line with the experimental observations.

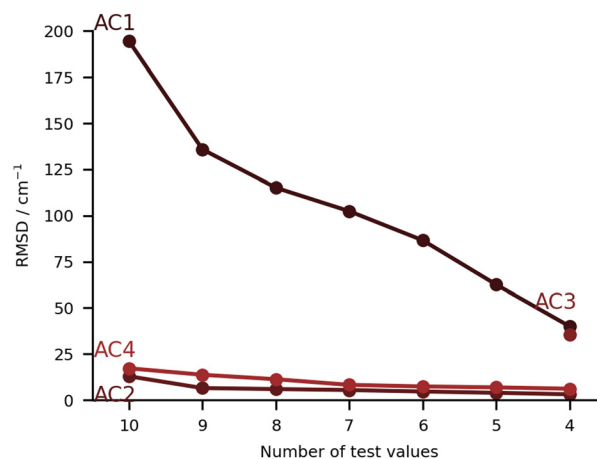
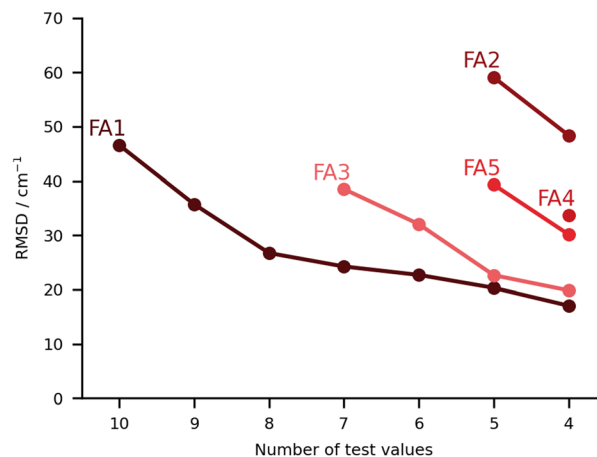


Fig. 7 RMSD values (in cm⁻¹) for the anharmonic corrected (AC) submissions. The values are provided incrementally removing the worst prediction of each set, in order to compare in a more balanced way the different submissions.



3.6 Fully anharmonic (FA) submissions

Finally, we have the best set of values under this category, the FA1 submission. It falls close to FA3 for the best predictions,



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with the largest errors for MLA and THF, 101 and 76 cm^{-1} in absolute deviations. The total RMSD falls significantly once the two outliers are removed (RMSD of 27 cm^{-1}). It is a unique set of calculations within the challenge. The authors carried out adiabatic *ab initio* molecular dynamics at the B3LYP-D3(BJ)/aug-cc-pVTZ level of theory. The fundamentals were taken from the power spectrum which is obtained by Fourier transform of the velocity autocorrelation function. Further details to the method are available in the corresponding FA1 ESI.† The single trajectories were started from optimised minima which fall in good agreement with the best predictions available, aside from a small difference in the conformation of the PCD hydrate. The source of the deviations should not be linked to the starting structures or the initial momenta. One should note that for this particular submission, the results for the training set were significantly better than for the test set, 18 vs. 47 cm^{-1} . Most of this difference is due to the two aforementioned outliers, and which the authors anticipated as problematic. MLA and THF spectra were characterized by complex power spectra and more investigations should have been undertaken to best identify the target spectroscopic signal. Clearly this task is eased in the case of the training set.

3.7 Learning strategy (LS) submissions

The final category of submissions were computational protocols which made use in one way or the other of learning strategies, either to correct computed harmonic frequencies, or to overall predict the position of the bands in the hydrate complexes. The worst performing set of values under this category was LS2 (see Fig. 9), with very large deviations for MLA, THT and TFE, 99, 88 and 166 cm^{-1} absolute errors respectively. We will discuss this set of values together with one of the best performing sets (LS3), since these originate from the same group and make use of the same training data. This consisted of the training and test set molecules, expanded by over 200 other organic molecules retrieved from the GDB11 dataset.^{64,65} The latter were chosen based on a similarity search, in an

attempt to better cover the chemical space of the test set. For further details in the molecule selection, please consult the LS3 ESI.† The molecular geometries are available for download in <https://github.com/MMunibas/Hydra/>. The harmonic frequencies for the full set of hydrates were calculated at the B3LYP-D3(BJ)/aug-cc-pVTZ level of computation, which together with the measured hydrate frequencies (when available) served as data for both LS2 and LS3 learning approaches. In the case of LS2 (the worst performing submission in the LS category) a kernel was trained to reproduce the harmonic frequencies. The descriptors were generated from the Faber-Christensen-Huang-Lilienfeld (FCHL19) representation (total length 33 by 486).⁶⁶ Using the same representation, the harmonic values were corrected to the known (experimental) training set values following the Δ -learning method.⁶⁷ The two kernels were used in combination to arrive at the final predicted values, using the experimental OH symmetric stretch wavenumbers for water (3657 cm^{-1}). In the case of LS3, the same underlying data was used, but this time a neural network was trained on the basis of the optimised geometries to provide the corresponding harmonic wavenumbers. The descriptors were also based upon FCHL19 (total length 193 after reduction by a principal component analysis, as described in the LS3 ESI.†). The test set molecules were included in the training of the aforementioned neural network. Transfer learning was then used to replicate the experimental values for 9 hydrate complexes of the training set (the radical case was excluded). Further details on the architecture and algorithms used are provided in the respective ESI.† As one can observe comparing the LS2 and LS3 values, the transfer learning strategy was far more successful than the kernel approach. However, one should not necessarily pin this on the methods. After disclosing the results, a re-assessment of LS2 revealed that there was a mistake in the scaling of the standardised predictions. Instead of the anharmonic average and variance, the harmonic values were used, leading to an overestimation of the fundamentals values. With the correct procedure the root mean squared difference decreases from 74 to 54 cm^{-1} . For further details, see “Re-evaluation of the Hydra results for Method LS2 (Δ -learning)” in the ESI.† It would be interesting to revisit both models with knowledge of the final target quantities.

The other two submissions (LS1 and LS4) approached the problem making use of computed harmonic frequencies corrected by an empirical function. In the case of LS1, the base harmonic predictions were obtained at the PBE-D3 level of theory using the projector augmented wave approach (PAW). For calculation details please consult the corresponding ESI.† Eight complexes from the training set were used to fit a linear regression formula (two were excluded due to issues in the optimisation), the latter being applied to the harmonic predictions of the test set. The training and test sets roughly covered the same range of OH shifts, with similar types of interactions, providing a reasonable basis for the correction function. Albeit LS1 was not among the top group of submissions, the RMSD was still overall below 30 cm^{-1} . Lastly, LS4 used a somewhat more complex linear correction function. The geometries and

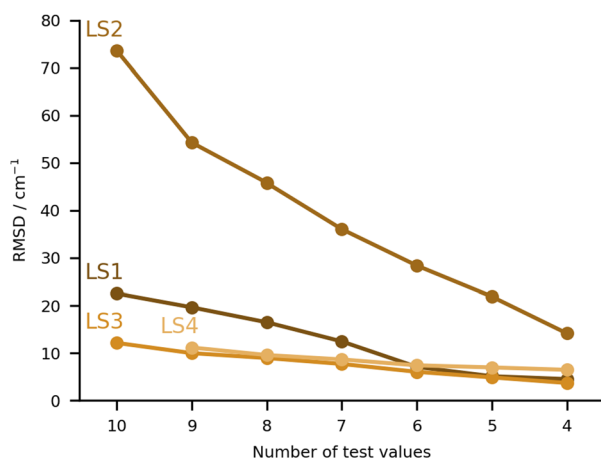


Fig. 9 RMSD values (in cm^{-1}) for the learning strategy (LS) submissions. The values are provided incrementally removing the worst prediction of each set, in order to compare in a more balanced way the different submissions.

corresponding harmonic wavenumbers were obtained with the PBE0-D3(BJ) functional. The basis sets used were may-cc-pVTZ for the organic molecules, aug-cc-pVQZ for the water molecule in the complex. An empirical linear function was then used to correct the harmonic predictions to target experimental values. The training data consisted of 42 hydrate complexes with published spectroscopic data. The linear function included two parameters which were fitted to the aforementioned data, weighing in the OH bond elongation. Further details are provided in the LS4 ESI.† The performance of this approach was very similar to that of LS3 (Fig. 9).

4 Revisiting the training set

At this point it is worth revisiting the training set, both experimentally and in terms of theory performance. The latter is limited to those submissions which have provided training performance data. As the training set also included cases with a proven or speculated higher-order anharmonic resonance²² which shifts around the OH stretching energy levels by up to $\pm 10\text{ cm}^{-1}$, one can now check whether submissions without regression step fit better the raw or the deperturbed experimental data, to learn more about the impact of this resonance. Finally, one can check whether a method performs better for the training set than for the test set or more or less equally well for both. Because the spread of wavenumber values turned out to be quite similar for the test and training data set, a balanced performance would not be too surprising.

4.1 Reference experimental values and deperturbation

The case of ANL was experimentally revisited in the present work (see ESI,† and ref. 23 for details), because there was a hypothesis of an anharmonic perturbation in place.²² The size-selected literature spectrum of the monohydrate of ANL⁶⁸ exhibits a very strong, partially saturated signal at 3524 cm^{-1} and a sharp satellite at 3547 cm^{-1} with unclear origin. To account for the possibility of an intensity stealing by this satellite, 3526 cm^{-1} with an uncertainty of $\pm 3\text{ cm}^{-1}$ was proposed for the best deperturbed band position estimate.¹⁸ Comparison with the FTIR spectra in the present work confirms the main peak at 3525 cm^{-1} , *i.e.* within 1 cm^{-1} . It rules out a relative intensity of 10% or more for any weak satellite contribution near 3547 cm^{-1} . Therefore, the resonance hypothesis can be dropped and the new best estimate is 3525 cm^{-1} with an uncertainty of $\pm 1\text{ cm}^{-1}$, in line with the original raw result.⁶⁸

For all the other training set members, there is no new evidence which would cause a revision of the originally proposed fundamental wavenumbers, with or without deperturbation, although the DBN case is currently under reinvestigation. Hence, the following training set wavenumber alternatives remain, depending on whether raw results for the strongest signal or deperturbation for the high order anharmonic resonance²² is attempted. For ACE, the raw/deperturbed alternatives are $3538/3531\text{ cm}^{-1}$, for APH $3536/3530\text{ cm}^{-1}$, for DBN $3484/3487\text{ cm}^{-1}$. Note that Fig. 1 only lists the raw values.

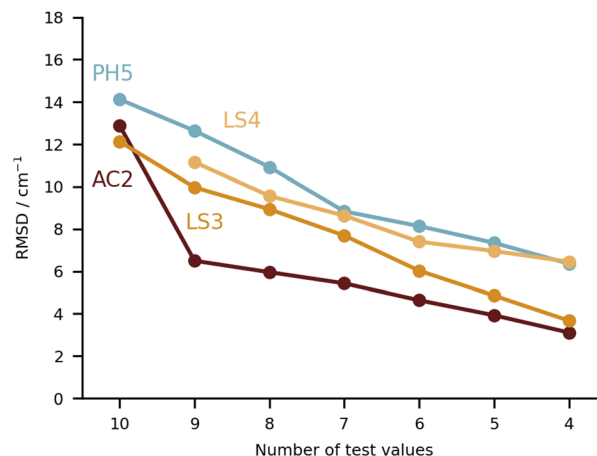


Fig. 10 RMSD values (in cm^{-1}) for the four submissions with the lowest RMSD overall (PH5, AC2, LS3 and LS4). Note that the ordinate axis has a much smaller range than in the previous plots, with all four sets of values remaining below an RMSD of 15 cm^{-1} .

The methods shown in Fig. 10 would profit by at most 10% in their RMSD when switching to deperturbed reference values. Other deficiencies of the models clearly dominate. Still, it is rewarding to see that none of the discussed methods deteriorate with the deperturbation. On the other hand, none of the submissions has attempted to model the high-order resonance explicitly. Therefore, this subtle anharmonic aspect²² is left for future iterations of HyDRA, with better performing theoretical methods.

Keeping the discussion on the best performing methods, it is interesting to consider the individual errors plotted in Fig. 10. PH5, LS3 and LS4 predominantly underestimate the stretch frequencies shifts, whereas AC2 is more balanced in this regard. The major flaw in the AC2 prediction is PYR for which a large shift overestimation is found. The accumulated negative errors (underestimates) are -97.1 , -18.6 , -85.0 and -62.6 cm^{-1} compared with accumulated shift overestimates of 25.6 , 68.6 , 12.0 and 28.6 cm^{-1} for PH5, AC2, LS3 and LS4, respectively. For the case of AC2 it is interesting to note that PYR has the farthest red shift (*i.e.* strongest interaction between water and probe molecule) which is consistent with results on the training set (see AC2 ESI†) for which the bands shifted most to the red are typically captured least reliably. This points towards a genuine deficiency of B3LYP for the calculation of the PES, which is required in the DVR3D calculations.

4.2 Training set performance vs. test set performance

A global comparison of the training set performance is not straightforward, because the submitted methods differ widely in their system coverage. However, the group of methods which achieve a test set RMSD better than 15 cm^{-1} (PH5, AC2, LS3, LS4) overlaps well with the methods achieving a training performance better than 15 cm^{-1} (PH5, LS3, LS4). AC2, the only outlier in this correspondence, is unusual because it actually shows a 25% better performance for the (blind) test set than for the (known) training set. The other three methods



Table 3 Predicted fundamental band position and (down)shift (in cm^{-1}) for the OH donor bond stretch in the water dimer, as provided by the best performing protocols in this challenge. This evaluation was carried out during manuscript preparation and after the challenge was finished. Comparison is made to a recent full-dimensional anharmonic treatment⁷⁴ and the most recent experimental^{22,70–73} reference values

Protocol	Position	Shift	Reference	Position	Shift
PH5	3770.9	79.1	IR-VUV ⁷⁰	3549	108
AC2	3561.8	95	IR-VUV ⁷⁰	3537	120
LS3	3581	76	FTIR ^{22,71}	3602	55
LS4	3580.7	76.7	IR-IR ⁷²	3601	56
12-D ⁷⁴	3599	58	review ⁷³	3601	56

perform better for the training set, which is expected for learning methods and for a purely harmonic approach (PH5) which has been manually tuned to achieve a good agreement with the training data.

5 Future extensions

It will now be important to substantially and dynamically⁶⁹ extend the HyDRA database in different directions such as larger downshifts, other compound classes, dihydrates, charged systems or spectral ranges, before another blind challenge might follow. Such a second generation blind challenge may decide more clearly between purely harmonic, anharmonically corrected, fully anharmonic and learning strategies. It may also reach a prediction quality which helps to better understand newly discovered anharmonic resonances in hydrate complexes.

As an example for the power of this collaborative approach, we suggested to the authors of the best submissions to compute the results for the OH donor vibration in the water dimer, which has been a rather controversial observable over the last few years.^{22,70–73} A well-converged full-dimensional variational treatment of the donor OH stretch band origin on a high quality analytical potential energy hypersurface is now available⁷⁴ yielding a value of 3599 cm^{-1} . This calculation matches the experimental consensus of about 3601 cm^{-1} well within the $\approx 10 \text{ cm}^{-1}$ spread due to quantum tunneling of

indistinguishable nuclei present in this floppy dimer. It is of interest how close different local strategies without such tunneling contributions come to experiment. The results are summarised in Table 3. One can see that none of the predictions from this work supports the multiply refuted^{22,71–73} recent IR-VUV result and interpretation.⁷⁰ AC2 comes closest but its focus on monomer anharmonicity is likely to perform poorly for the lightest, strongly librating hydrates, *i.e.* water dimer. All others consistently predict the water donor OH stretching downshift some 20 cm^{-1} above experiment and above the full-dimensional variational treatment, perhaps again a consequence of the particularly light and thus delocalised nature of the binding partner. This is also qualitatively true for the second-lightest case of formaldehyde (FAH, Fig. 11). It is encouraging that the three particularly successful independent approaches based on a harmonic reference are so consistent for such an extreme testing case.

6 Conclusions

Despite the manifold challenges posed to the participants, there are good reasons to be optimistic. We start with the positive points. In Fig. 10 and 11, a closer look is taken at the four submissions with the lowest RMSD overall (falling below 15 cm^{-1}). The differences among these sets are statistically not significant and we see no point in crowning a unique winner. They show how quite different strategies can be across the board successful, with RMSDs reaching close to the 10 cm^{-1} value. This would be an interesting milestone for the future. If one would have to select winning categories, these would be perhaps the learning strategies (LS) and the anharmonic corrected (AC) submissions. These are the procedures which most strongly focus on the quantity of interest, and inherently carry an advantage for such a specific quantity. Nonetheless, as some results show, this is not at all a guarantee for success.

The other side of the coin are the purely harmonic (PH) calculations, which heavily rely on error compensation. PH5 is built on a very conscious decision of using the 'Pauling point'.

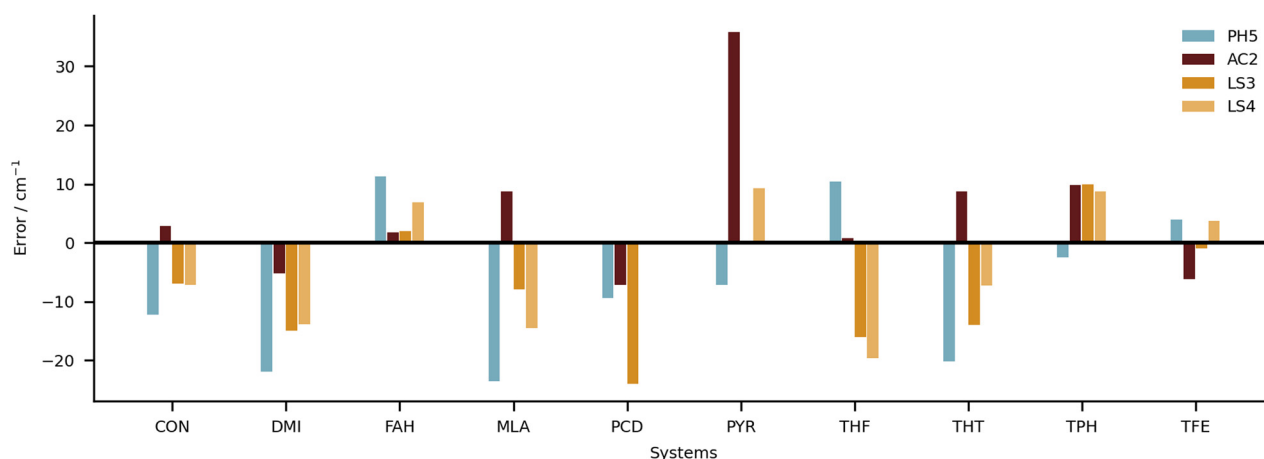


Fig. 11 Individual errors in predicted shifts for the four submissions with the lowest RMSD overall (PH5, AC2, LS3 and LS4).



Albeit calculations with larger basis sets were available (and provide the basis for AC4), cutting the number of functions leads to an improved error compensation. The robustness is impressive given the amount of approximations involved. We find two questions of interest for the future. The first one is whether this robustness will still hold when increasing the number or diversity of systems under study. This could be verified in future editions of the challenge or simply calculating some of the other systems which were suggested for the training set. The other question is whether this type of error cancellation can be found in other (relatively cheap) electronic structure methods, in particular DFT functionals. The three models used in this category (B3LYP, PBE0 and ω B97xD) seem to not hold to the task. However, the PH data sets are mostly subproducts of other computational protocols, and the 'Pauling point' was not being explicitly sought for. There could be alternatives.

The fully anharmonic submissions were perhaps the biggest upset overall. Some submissions were able to break below an RMSD of 40 cm^{-1} , but they were far from reaching the top 4. One should say that this is partly due to the way the challenge was conceived. The test set consisted of both large and small systems, significantly limiting the level of theory that could be applied across all (or at the least the majority of) systems. It would have been perhaps of interest to have a few higher-level calculations for the smallest hydrates. This can be a task for future studies, although one will miss the blind character of the challenge. In future editions, one could also attempt to include more groups with a focus on *ab initio* vibrational spectroscopy which could potentially restrict themselves to the smallest systems featured. Another deciding factor was to estimate the shift in the OH frequency, *i.e.* to estimate a difference of frequencies instead of the absolute value. This decreases the importance of anharmonic effects and strongly favours methods which most heavily rely on error compensation (*e.g.*, the PH submissions). The fully anharmonic (FA) methods have a much better comparative performance when looking at absolute fundamental band positions.

Finally, one should note that the conditions were not the best for machine learning approaches. Only a very small training set was made available. All LS submissions (with the exception of LS1) compensated for this fact by performing additional calculations on molecular datasets. Moving forward, it would be well-advised to combine the experimental information (*e.g.*, for the 20 systems featured in this challenge) and libraries of computed vibrational spectra, even if just under the harmonic approximation. The curated data should reduce the overhead in building such models, besides significantly improving their accuracy.

Author contributions

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investigation, validation, visualization, writing – review & editing. Sophie M. Schweer: investigation, validation, visualization, writing – review & editing. Jennifer Dupont: investigation, data curation, formal analysis, validation, visualization. Valéria Lepère: investigation, visualization, validation. Anne Zehnacker-Rentien: conceptualization, formal analysis, investigation, supervision, validation, writing – review & editing. Martin A. Suhm: conceptualization, formal analysis, funding acquisition, project administration, supervision, validation, writing – review & editing. Benjamin Schröder: investigation, formal analysis, validation, writing – review & editing. Tobias Henkes: investigation, formal analysis. Diego M. Andrada: supervision, project administration, resources, writing – review & editing. Roman M. Balabin: investigation, formal analysis, project administration, resources, writing – review & editing. Haobam Kisan Singh: investigation, formal analysis. Himangshu Pratim Bhat-tacharyya: investigation, formal analysis. Manabendra Sarma: conceptualization, formal analysis. Silvan Käser: investigation, data curation. Kai Töpfer: investigation, data curation. Luis I. Vazquez-Salazar: investigation, data curation. Eric D. Boittier: investigation, data curation. Markus Meuwly: supervision, project administration. Giacomo Mandelli: investigation, data curation, writing, review and editing. Cecilia Lanzi: investigation, data curation, writing, review and editing. Riccardo Conte: supervision, project administration, resources, writing – review & editing. Michele Ceotto: supervision, project administration, resources, writing – review & editing. Fabian Dietrich: data curation, formal analysis, investigation, methodology. Vicente Cisternas: investigation, formal analysis. Ramachandran Gnasekaran: investigation, formal analysis, project administration, resources, writing – review & editing. Michael Hippler: investigation, formal analysis, project administration, resources, writing – review & editing. Mahmoud Jarraya: investigation, formal analysis. Majdi Hochlaf: supervision, project administration, resources, writing – review & editing. Narasimhan Viswanathan: investigation, formal analysis, writing – review & editing. Thomas Nevolianis: investigation, formal analysis. Gabriel Rath: investigation, formal analysis. Wassja A. Kopp: investigation, formal analysis. Kai Leonard: supervision, project administration, resources, writing – review & editing. Ricardo A. Mata: conceptualization, data curation, formal analysis, project administration, validation, visualization, writing – original draft, writing – review & editing.

Conflicts of interest

The authors have no conflicts of interest to declare.

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