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# Magnetic interactions in the $S = 1/2$ square-lattice antiferromagnets $\text{Ba}_2\text{CuTeO}_6$ and $\text{Ba}_2\text{CuWO}_6$ : parent phases of a possible spin liquid†

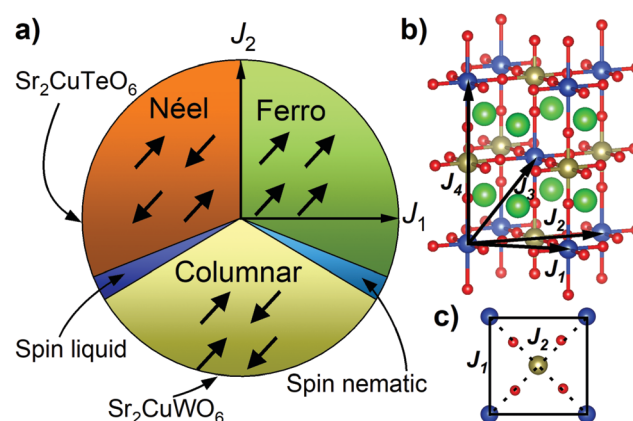
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**The isostructural double perovskites  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  are shown by theory and experiment to be frustrated square-lattice antiferromagnets with opposing dominant magnetic interactions. This is driven by differences in orbital hybridisation of  $\text{Te}^{6+}$  and  $\text{W}^{6+}$ . A spin-liquid-like ground state is predicted for  $\text{Ba}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  solid solution similar to recent observations in  $\text{Sr}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$ .**

Magnetic frustration can stabilise novel quantum ground states such as quantum spin liquids or valence bond solids.<sup>1</sup> Frustration occurs when not all of the magnetic interactions in a material can be satisfied simultaneously as a result of lattice geometry or competing interactions. We have recently shown that a quantum-spin-liquid-like state forms in the double perovskite solid solution  $\text{Sr}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  with a square lattice of  $\text{Cu}^{2+}$  ( $3d^9$ ,  $S = 1/2$ ) cations.<sup>2,3</sup> This was the first observation of a spin-liquid-like state in a square-lattice compound after 30 years of theoretical predictions.<sup>4–8</sup>

The parent compounds  $\text{Sr}_2\text{CuTeO}_6$  and  $\text{Sr}_2\text{CuWO}_6$  are frustrated square-lattice (FSL) antiferromagnets.<sup>9–13</sup> The FSL model (Fig. 1) has two interactions: nearest-neighbour  $J_1$  interaction (side) and next-nearest-neighbour  $J_2$  interaction (diagonal). Dominant antiferromagnetic  $J_1$  leads to Néel type antiferromagnetic order and dominant  $J_2$  leads to columnar magnetic order. Magnetic frustration arises from the competition of  $J_1$  and  $J_2$ , and a quantum spin liquid state has been predicted for  $J_2/J_1 = 0.5$  where frustration is maximised.<sup>4–8</sup>

$\text{Sr}_2\text{CuTeO}_6$  and  $\text{Sr}_2\text{CuWO}_6$  are the first known isostructural FSL systems with different dominant interactions and magnetic structures: dominant  $J_1$  and Néel order for  $\text{Sr}_2\text{CuTeO}_6$  and dominant  $J_2$  and columnar order for  $\text{Sr}_2\text{CuWO}_6$  respectively.<sup>9,10</sup> The two compounds have a tetragonal  $I4/m$  double perovskite structure with nearly identical bond distances and angles.<sup>11,13</sup> The magnetism becomes highly two-dimensional as a result of a Jahn–Teller distortion as the only unoccupied Cu orbital  $3d_{x^2-y^2}$  is in the  $ab$  square plane. The major differences in dominant magnetic interactions are due to the diamagnetic  $\text{Te}^{6+}$   $d^{10}$  and  $\text{W}^{6+}$   $d^0$  cations located in the middle of the  $\text{Cu}^{2+}$  square (Fig. 1c), which hybridise differently with O 2p allowing different super-exchange paths between the  $\text{Cu}^{2+}$  cations.<sup>14,15</sup> The spin-liquid-like ground state forms when these two perovskites are mixed into a  $\text{Sr}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  solid solution.<sup>2,3,16</sup> Muon spin relaxation



**Fig. 1** (a) Phase diagram of the frustrated square-lattice model. Antiferromagnetic (negative)  $J_1$  stabilises Néel order and  $J_2$  columnar order respectively. A spin liquid state has been predicted for the Néel–columnar boundary at  $J_2/J_1 = 0.5$  where magnetic frustration is maximised. (b) The double perovskite structure of  $(\text{Ba},\text{Sr})_2\text{Cu}(\text{Te},\text{W})\text{O}_6$ .  $J_1$  and  $J_2$  are the in-plane interactions of the FSL model, whereas  $J_3$  and  $J_4$  are out-of-plane interactions. The blue, dark yellow, red and green spheres represent Cu, Te/W, O and Ba/Sr, respectively. (c) The  $\text{Cu}^{2+}$  square in the  $ab$  plane with  $J_1$  and  $J_2$  interactions.

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experiments revealed the absence of magnetic order or static magnetism in a wide composition range of  $x = 0.1$ – $0.6$ .<sup>2,3</sup> The specific heat displays  $T$ -linear behaviour suggesting gapless excitations in a similar composition range.<sup>2,3,16</sup> The ground state has been proposed to be a random-singlet state with a disordered arrangement of non-magnetic valence bond singlets.<sup>17,18</sup>

Motivated by these exciting findings in the  $\text{Sr}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  system, we have investigated the magnetic interactions of the isostructural barium analogues  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$ .  $\text{Ba}_2\text{CuWO}_6$  is known to have columnar magnetic order,<sup>19,20</sup> but little is known about  $\text{Ba}_2\text{CuTeO}_6$  as the perovskite phase requires high pressures to synthesise.<sup>21</sup> Here we use density functional theory (DFT) calculations and high-temperature series expansion (HTSE) fitting of experimental susceptibility data to show that these compounds are FSL antiferromagnets with opposite dominant interactions similar to  $\text{Sr}_2\text{CuTeO}_6$  and  $\text{Sr}_2\text{CuWO}_6$ . We predict a quantum-spin-liquid-like state in  $\text{Ba}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  with strong antiferromagnetic interactions.

Magnetic interactions and electronic structure in  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  were calculated using the DFT+ $U$  framework, where an on-site Coulomb repulsion term  $U$  was used to model electron correlation effects of localised Cu 3d orbitals. Interactions up to the fourth-nearest neighbour were evaluated, see Fig. 1b.  $J_1$  and  $J_2$  are the square plane interactions of the FSL model, and  $J_3$  and  $J_4$  are additional out-of-plane interactions. Energies of different spin configurations were mapped onto a Heisenberg Hamiltonian to obtain  $J_1$ – $J_4$ . We have previously shown this approach works well for  $\text{Sr}_2\text{CuWO}_6$ .<sup>10</sup> The  $J_1$  and  $J_2$  interactions were also determined from experimental magnetic susceptibility data using high-temperature series expansion fitting.  $\text{Ba}_2\text{CuTeO}_6$  was prepared by high-pressure synthesis and  $\text{Ba}_2\text{CuWO}_6$  by conventional solid state synthesis. Details of the DFT calculations, sample synthesis and characterisation are available in the ESI.†

The calculated magnetic interactions of  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  are presented in Table 1. The calculated values depend on the Coulomb  $U$  term as is typical with DFT+ $U$ , but the same

**Table 1** Exchange constants of  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  obtained by density functional theory using different on-site Coulomb  $U$  terms and by high-temperature series expansion fitting of magnetic susceptibility data. Negative (positive) values correspond to antiferromagnetic (ferromagnetic) interactions

	$U = 7$ eV	$U = 8$ eV	$U = 9$ eV	HTSE
<b><math>\text{Ba}_2\text{CuTeO}_6</math></b>				
$J_1$ (meV)	−23.65	−20.22	−17.22	−16.54(3)
$J_2$ (meV)	0.13	0.23	0.06	−0.04(3)
$J_3$ (meV)	1.28	0.83	0.67	—
$J_4$ (meV)	−0.30	0.01	0.05	—
$J_2/J_1$	−0.01	−0.01	−0.003	0.002
<b><math>\text{Ba}_2\text{CuWO}_6</math></b>				
$J_1$ (meV)	−1.25	−1.17	−1.27	0.2(9)
$J_2$ (meV)	−14.71	−11.94	−9.56	−10.0(1)
$J_3$ (meV)	0.05	−0.01	0.01	—
$J_4$ (meV)	0.03	0.37	0.02	—
$J_2/J_1$	11.79	10.18	7.55	−50 <sup>a</sup>

<sup>a</sup> Significant uncertainty in this value due to error in  $J_1$ .

trends are observed for reasonable values of  $U$ . Despite being isostructural, the magnetic interactions in  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  are very different.  $\text{Ba}_2\text{CuTeO}_6$  has a very dominant antiferromagnetic  $J_1$  interaction with weak  $J_2$ ,  $J_3$  and  $J_4$  interactions. It is a near-ideal FSL Néel antiferromagnet.  $\text{Ba}_2\text{CuWO}_6$ , in contrast, has a dominant antiferromagnetic  $J_2$  interaction slightly frustrated by an antiferromagnetic  $J_1$  interaction with negligible  $J_3$  and  $J_4$  interactions. The strong  $J_2$  interaction is consistent with the known columnar magnetic structure of this compound.<sup>20</sup> Due to the weakness of the out-of-plane  $J_3$  and  $J_4$  interactions, magnetism in both compounds is highly two-dimensional and well described by the FSL model.

The significant differences in the magnetic interactions of  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  can be explained by their electronic structures. We have plotted total and partial densities of states for both compounds in Fig. 2.  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  are antiferromagnetic insulators: the band gaps open between the occupied Cu 3d states hybridised with O 2p (valence band) and the unoccupied Cu  $3d_{x^2-y^2}$  states hybridised with O 2p (conduction band). In  $\text{Ba}_2\text{CuWO}_6$  the conduction band is further hybridised



**Fig. 2** Total and partial density of states plots for  $\text{Ba}_2\text{CuTeO}_6$  (left) and  $\text{Ba}_2\text{CuWO}_6$  (right). Both compounds are antiferromagnetic insulators. The moderate Te 5p/5s–O 2p hybridisation and stronger W 5d–O 2p hybridisation are seen in the Te/W and O PDOS plots.



with unoccupied W 5d states. The W 5d states also hybridise with the Cu 3d/O 2p states in the valence band, which allows a  $180^\circ$  Cu–O–W–O–Cu superexchange pathway resulting in a strong antiferromagnetic  $J_2$  interaction. This hybridisation does not occur in  $\text{Ba}_2\text{CuTeO}_6$  and therefore  $J_2$  is negligible. In  $\text{Ba}_2\text{CuTeO}_6$  the Te 5p states hybridise to a lesser degree with the Cu 3d/O 2p states in the conduction band, which could explain the strong antiferromagnetic  $J_1$  interaction. However, the role of Te in the  $J_1$  superexchange in  $\text{Sr}_2\text{CuTeO}_6$  is under debate.<sup>9,14</sup> Overall, the electronic structures of  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  are similar to their strontium analogues  $\text{Sr}_2\text{CuTeO}_6$  and  $\text{Sr}_2\text{CuWO}_6$ , and the differences in magnetic interactions are driven by the same orbital hybridisation mechanism.

The experimental magnetic susceptibilities of synthesised  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  samples are shown in Fig. 3. The broad maximum observed in the susceptibility is due to the two-dimensional nature of the magnetism in these materials. Our maximum temperature of 400 K was not enough for reliable Curie–Weiss fits. Previous measurements<sup>21</sup> up to 800 K yielded the Curie–Weiss constants  $\Theta_{\text{CW}} = -400$  K for  $\text{Ba}_2\text{CuTeO}_6$  and  $\Theta_{\text{CW}} = -249$  K for  $\text{Ba}_2\text{CuWO}_6$  revealing strong antiferromagnetic interactions.

The magnetic susceptibilities were fitted to a high-temperature series expansion of the FSL model.<sup>22</sup> The molar magnetic susceptibility  $\chi_{\text{mol}}$  is given by:

$$\chi_{\text{mol}} = \frac{N_A g^2 \mu_B^2}{k_B T} \sum_n \beta^n \sum_m c_{m,n} x^m + \chi_0$$

where  $g$  is the effective  $g$ -factor,  $\beta = -J_1/k_B$ ,  $x = J_2/J_1$ ,  $\chi_0$  is a temperature independent diamagnetic correction and the coefficients  $c_{m,n}$  are from Table 1 in ref. 22. The model has four parameters:  $J_1$ ,  $J_2$ ,  $g$  and  $\chi_0$ , which were fitted to the experimental data using a least squares method. The model always produces two solutions due to internal symmetry: one with dominant  $J_1$

and one with dominant  $J_2$ .<sup>23</sup> Our DFT calculations allow us to select the correct dominant  $J_1$  solution for  $\text{Ba}_2\text{CuTeO}_6$  and the dominant  $J_2$  solution for  $\text{Ba}_2\text{CuWO}_6$ .

The best fits were obtained with the parameters  $J_1 = -16.54(3)$  meV,  $J_2 = -0.04(3)$  meV,  $g = 2.20(1)$  for  $\text{Ba}_2\text{CuTeO}_6$  and  $J_1 = 0.2(9)$  meV,  $J_2 = -10.0(1)$  meV,  $g = 2.26(5)$  for  $\text{Ba}_2\text{CuWO}_6$  in the temperature ranges 150–400 K and 90–400 K, respectively. The fitted exchange constants depend slightly on the minimum temperature used. For both compounds the calculated dominant interaction remains stable in a wide fitting range, but the weaker interaction cannot be accurately quantified. In  $\text{Ba}_2\text{CuTeO}_6$  the sign of  $J_2$  changes depending on the fitting range, whereas in  $\text{Ba}_2\text{CuWO}_6$  the error of  $J_1$  is much larger than its value. We can conclude, however, that the dominant interaction is much stronger than the weak one in both  $\text{Ba}_2\text{CuTeO}_6$  ( $|J_2|/|J_1| < 0.02$ ) and  $\text{Ba}_2\text{CuWO}_6$  ( $|J_1|/|J_2| < 0.12$ ) and that the DFT and HTSE results are in good agreement.

The magnetic properties of  $\text{Ba}_2\text{CuTeO}_6$ ,  $\text{Ba}_2\text{CuWO}_6$ ,  $\text{Sr}_2\text{CuTeO}_6$  and  $\text{Sr}_2\text{CuWO}_6$  are summarised in Table 2. Magnetic interactions in  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  are notably stronger than their strontium analogues. This is due to the smaller  $a^0a^0c^-$  tilt of the  $\text{CuO}_6$  octahedra in the barium phases, which leads to stronger orbital overlap in the  $ab$  plane as the Cu–O–Te/W angle is closer to  $180^\circ$ ,<sup>21</sup> see ESI† for further details. As long-range magnetic order is driven by the weak out-of-plane interactions which are of the same order in all compounds,  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$  are even closer to ideal two-dimensional antiferromagnets than their strontium analogues. The transition temperature of  $\text{Ba}_2\text{CuTeO}_6$  is not known, but we predict it to have the highest frustration index  $f = \Theta_{\text{CW}}/T_N$  of these compounds and the Néel magnetic structure due to the very strong  $J_1$  interaction. Magnetic excitations in  $\text{Sr}_2\text{CuTeO}_6$  and  $\text{Sr}_2\text{CuWO}_6$  have been observed at temperatures higher than  $2T_N$  driven by the two-dimensional magnetic interactions.<sup>9,10</sup> The stronger in-plane  $J_1$  and  $J_2$  interactions of the barium phases indicate the excitations survive to even higher temperatures.

Since  $\text{Ba}_2\text{CuTeO}_6$  has a dominant  $J_1$  interaction and  $\text{Ba}_2\text{CuWO}_6$  has a dominant  $J_2$  interaction, we predict a spin-liquid-like state will form in the  $\text{Ba}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  solid solution similar to  $\text{Sr}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$ . In the  $\text{Sr}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  system the Néel order is destabilised already at  $x = 0.1$ , and spin-liquid-like state exist in the composition region  $x = 0.1$ – $0.6$ . Columnar order is observed for  $x = 0.7$ – $1$ . Since the  $J_1$  interaction of  $\text{Ba}_2\text{CuTeO}_6$  is so strong even compared to  $J_2$  in  $\text{Ba}_2\text{CuWO}_6$ , we predict the Néel order remains more stable against W substitution. For the same reason, the columnar order near  $x = 1$  is likely to be less stable in  $\text{Ba}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$ . The extent of the spin-liquid-like region depends also on disorder, and is difficult to predict just from the properties of the end phases. Finally, the stronger antiferromagnetic interactions in the barium phases indicate that the quantum disordered ground state will remain stable up to higher temperatures.

The previous discussion concerns a double perovskite  $\text{Ba}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  solid solution, which near  $x = 0$  will require high-pressure synthesis to form. The ambient pressure form of  $\text{Ba}_2\text{CuTeO}_6$  is triclinic with a tolerance factor higher than 1.03.<sup>24</sup> Therefore, a  $\text{Ba}_2\text{Cu}(\text{Te}_{1-x}\text{W}_x)\text{O}_6$  solid solution prepared in

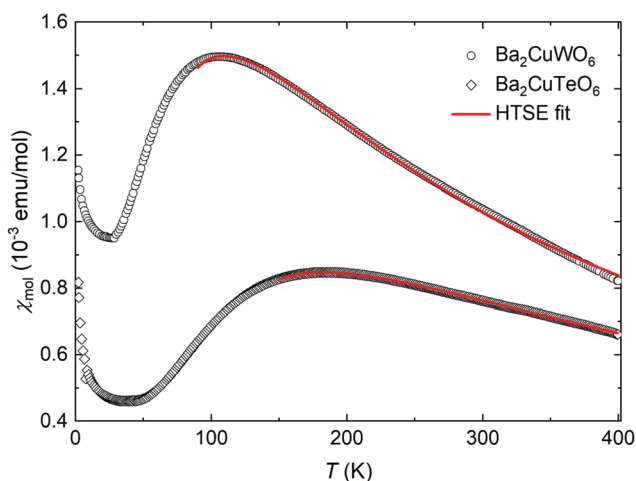


Fig. 3 Magnetic susceptibility and high-temperature series expansion fits for  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$ . Open symbols represent experimental data and the lines are HTSE fits with the parameters  $J_1 = -16.54(3)$  meV,  $J_2 = -0.04(3)$  meV,  $g = 2.20(1)$  and  $J_1 = 0.2(9)$  meV,  $J_2 = -10.0(1)$  meV,  $g = 2.26(5)$  for  $\text{Ba}_2\text{CuTeO}_6$  and  $\text{Ba}_2\text{CuWO}_6$ , respectively. The ZFC and FC curves overlap and therefore only ZFC data is shown.



<sup>a</sup> Predicted based on magnetic interactions.

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