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Machine-learning accelerated prediction of two-dimensional conventional superconductors†

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We perform a large scale search for two-dimensional (2D) superconductors, by using electron–phonon calculations with density-functional perturbation theory combined with machine learning models. In total, we screened over 140 000 2D compounds from the Alexandria database. Our high-throughput approach revealed a multitude of 2D superconductors with diverse chemistries and crystal structures. Moreover, we find that 2D materials generally exhibit stronger electron–phonon coupling than their 3D counterparts, although their average phonon frequencies are lower, leading to an overall lower T_c . In spite of this, we discovered several out-of-distribution materials with relatively high- T_c . In total, 105 2D systems were found with $T_c > 5$ K. Some interesting compounds, such as CuH₂, NbN, and V₂NS₂, demonstrate high T_c values and good thermodynamic stability, making them strong candidates for experimental synthesis and practical applications. Our findings highlight the critical role of computational databases and machine learning in accelerating the discovery of novel superconductors.

New concepts

This study introduces a large-scale computational approach to discover two-dimensional (2D) superconductors by combining density-functional perturbation theory (DFPT) with machine learning models. Unlike existing research, which often focuses on smaller datasets or specific material types, our work screens over 140 000 2D compounds from the Alexandria database, revealing numerous 2D superconductors with diverse chemistries and crystal structures. A key differentiation is the finding that 2D materials exhibit stronger electron–phonon coupling compared to their 3D counterparts, although lower average phonon frequencies result in generally reduced critical temperatures (T_c). Despite this, we identified several out-of-distribution materials with relatively high T_c , including CuH₂, NbN, and V₂NS₂, which also show good thermodynamic stability. This approach highlights the potential of leveraging computational databases and machine learning to accelerate the discovery of superconductors, offering a pathway to identify experimentally realizable materials with promising properties for practical applications.

1. Introduction

The discovery of superconductivity in 2D materials^{1–4} has opened up new possibilities for ultra-thin and flexible superconducting devices, essential for applications such as compact magnetic field sensors, efficient power transmission lines, and advanced quantum technologies. These materials can significantly enhance the performance of superconducting qubits, which are vital for quantum computing, owing to their stability and fault tolerance.^{5,6} Moreover, their high current density can lead to improved

efficiency in power transmission systems, high-field magnets, and nanoscale radiation detectors⁷.

Superconductivity in a variety of 2D transition metal dichalcogenides has been measured experimentally.^{8–13} In these systems, charge density wave^{10,14,15} and Ising pairing^{16–18} can coexist with the condensation of Cooper pairs.^{19,20} The competition and cooperation between these states forms an intriguing physical picture, for which numerous efforts have been made to give insights from the theoretical point of view.^{14,21–29} Superconductivity was also discovered in twisted bilayer graphite at low twisting angles,^{30,31} although at rather low transition temperature (T_c).

In conjunction with these advancements, numerous theoretical investigations have examined (hypothetical) 2D materials as potential conventional superconductors.¹⁹ Already in 2014 it was predicted that heavy electron doping could turn graphene into a superconductor.³² Density functional theory (DFT) calculations also showed that monolayer LiC₆ and CaC₆ could have a T_c of 8.1 K and 1.4 K.³³ Moreover, strained monolayer LiC₁₂ and AlC₈ could become high T_c superconductors, reaching 20.3 K³⁴

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and 41 K³⁵ under 10% and 12% strain, respectively. Li-adsorption is also predicted to convert the insulating mono-layer boron nitride (h-BN) to a superconductor.³⁶ Other graphene-related compounds formed by different ratios of squares, hexagons, and octagons could also become superconductors. Notably, octagraphene^{37,38} and biphenylene³⁹ are predicted to become conventional superconductors below 20.8 K⁴⁰ and 3.02 K,³⁹ respectively. Another interesting 2D compound is the fully hydrogenated form of graphene, the so-called graphane (CH),^{41,42} where all C-atoms are bonded to four neighbors (one hydrogen and three carbons). Although full hydrogenation of graphene is hardly achievable so far,^{43,44} graphane still attracts great interest due to its high predicted $T_c = 90$ K.⁴⁵ Various other “Xenes”, *i.e.* two-dimensional elementary structures (not limited to the honeycomb lattice), have been predicted to show superconductivity under electron or hole doping, namely, leadene,⁴⁶ silicene,⁴⁷ phosphorene,⁴⁸ arsenene,⁴⁹ aluminene,⁵⁰ gallenene,⁵¹ as well as antimonene.⁵²

Due to the high T_c of three dimensional MgB₂, that is driven by the in-plane stretching phonons of boron 2D layers, boron has attracted greater interest than any other element in the search for 2D superconductors. Borophene has a T_c as high as 24.7 K if vacancies are formed in stripes⁵³. Similarly, multiple 2D boron allotropes predicted from evolutionary algorithms have T_c ranging from 6.7 K to 27.6 K.^{54,55} Furthermore, doping with Sr was predicted to increase T_c of the boron Kagome monolayer up to 20.9 K.⁵⁶ Also several borides, where boron is combined with metallic elements, have been studied. Metals that were predicted to lead to superconductivity are alkaline-earth or Li,^{57–59} group III metals^{60,61} and transition metals.^{58,62–65} Interestingly, ferromagnetic 2D Mn-borides are predicted to be electron–phonon superconductors.^{66,67} Other boron related 2D compounds that are also predicted as conventional superconductors are hydrogenated borides (Ti₂B₂H₄⁶⁸ and TiB₂H⁶⁹), 2D boron carbides,^{70–72} boron silicides,⁷³ boron chalcogenides,⁷⁴ penta-structure 2D boron nitrides,⁷⁵ and boron phosphide.⁷⁶ Another interesting boron-related 2D system is the borophene oxide B₂O that, unlike the insulating B₂O₃,⁷⁷ is metallic and superconducting, with a T_c relatively high (10.3 K) comparing to other 2D borides.⁷⁸

Theoretical studies have also predicted several other 2D superconducting compounds, *e.g.* nitrides,⁷⁹ silicides,⁸⁰ metal silicon nitrides,⁸¹ phosphorus carbide,²⁷ 2D metal–organic frameworks (2D-MOFs),⁸² and MXenes.^{83–86} Unlike the other 2D-families, in MXenes the surface functional groups play an important role for superconductivity.^{83,87–89}

As we see, the theoretical search for new 2D superconductors has been very fruitful in the past decade. However, most of the searches rely on physical intuition and usually focus on a few structure prototypes and chemical elements. In such a way, the theoretical exploration of unknown chemical and structural spaces is limited. Fortunately, recently developed computational databases^{90–96} and machine learning methodologies,⁹⁷ enable a different approach to discover superconducting materials. Several high-throughput searches on three-dimensional (3D) inorganic conventional superconductors have been conducted,^{98–101}

unveiling thousands of potentially superconductors, some of them with potentially record T_c .^{102,103} Moreover, the models and workflow designed originally for the 3D worlds can be easily extended to 2D cases. This was already exemplified in ref. 104, where over 1000 2D structures from the JARVIS-DFT database¹⁰⁵ were screened. In total, 34 dynamically stable structures with $T_c > 5$ K were identified, including materials such as W₂N₃, NbO₂, ZrBrO, TiClO, NaSn₂S₄, Mg₂B₄C₂, and Mg₂B₄N₃, with T_c reaching as high as 21.8 K.

In this work, we take a step further by developing a large and accurate dataset of calculated electron–phonon and superconducting properties for 2D materials. This dataset is then used to train a reliable machine-learning model for predicting the transition temperature T_c of 2D superconductors. This model was then utilized to screen for superconductivity the 2D compounds present in the Alexandria⁹⁶ database, that includes more than 140 000 entries, unveiling numerous systems with interesting superconducting properties.

II. Results and discussions

A. Initial dataset

The first step in this work is the creation of an (unbiased) dataset. The objective is twofold: (i) to be able to compare directly electron–phonon and superconducting properties of 2D materials with their 3D counterparts; (ii) to allow for the training of machine learning models to perform an accelerated high-throughput study of 2D superconductors. To construct this dataset we select 2D materials from the Alexandria database,⁹⁶ choosing (*meta*)-stable ones with an energy above the convex hull (E_{hull}) of less than 250 meV per atom. To decrease the numerical cost, we discard compounds with a layer space group number of lower than 30. Furthermore, we restrict the search only to metallic materials by removing materials with a density of states at the Fermi level less than 0.1 states per eV (per unit cell). Finally, we only consider structures with up to 8 atoms in the unit cell. This initial dataset comprises 4383 compounds, belonging to a large diversity of chemical systems, space groups, and structural arrangements.

The next step is the calculation of the phonon spectrum and electron–phonon coupling within the framework of density functional perturbation theory (DFPT), as detailed in III. It turns out that the majority of the compounds studied exhibited imaginary frequencies in the Brillouin zone. We have found a similar situation for metastable 3D systems with distances to the convex hull comparable to the ones of the 2D systems studied here. Ultimately, this is a consequence of the symmetry-preserving prototype search used to build modern large material databases. For the ~900 dynamically stable materials, we calculated the superconducting critical temperature (T_c) using the Allen–Dynes modification¹⁰⁶ to the McMillan formula^{107,108} (see III).

In the top panel of Fig. 1 we show a periodic table indicating the number of occurrences of each element present in the initial dataset. We can see that almost the entire periodic table is well represented although with a larger weight towards systems with halogens, chalcogens and pnictogens. This can



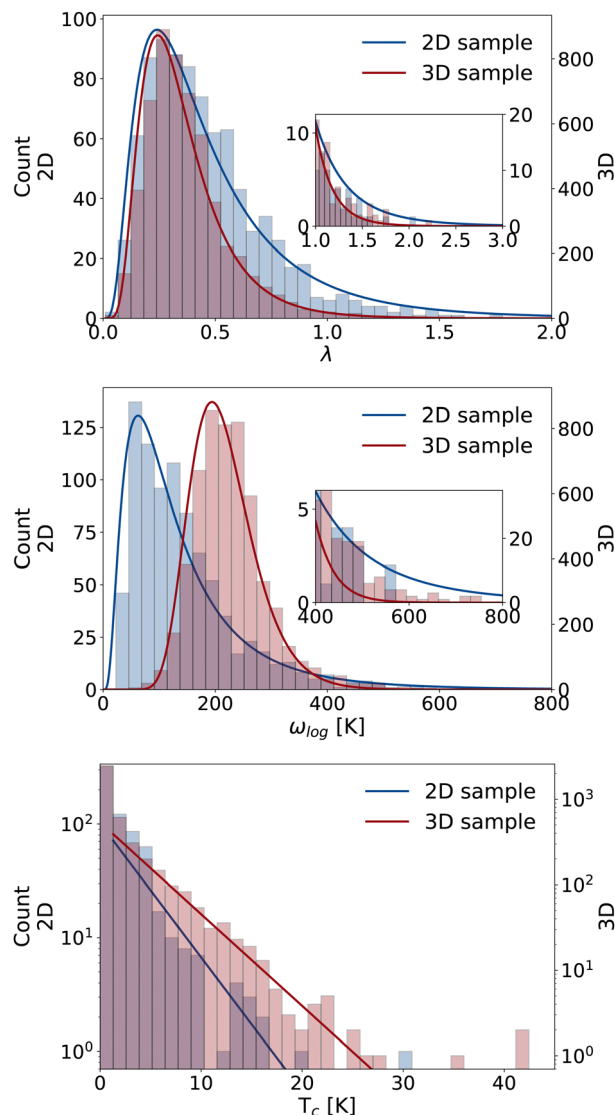


Fig. 2 (a) Histogram of the electron–phonon coupling constant λ . The blue and red lines are fits to a log-normal distribution with parameters $\sigma^{2D} = 0.6884$, $\mu^{2D} = -0.9532$, $N^{2D} = 50.59$, and $\sigma^{3D} = 0.5058$, $\mu^{3D} = -1.157$, $N^{3D} = 306.2$; (b) histogram of the logarithmic averaged phonon frequency $\omega_{\log}$. The blue and red lines are fits to a log-normal distribution with parameters $\sigma^{2D} = 0.7479$, $\mu^{2D} = 4.692$, $N^{2D} = 2.020 \times 10^4$, and $\sigma^{3D} = 0.2714$, $\mu^{3D} = 5.342$, and $N^{3D} = 1.206 \times 10^5$; (c) histogram of the values of the transition temperature T_c . Note the logarithmic scale on the y-axis. The blue and red lines are fits to an exponentially decaying distribution ($p(x) = N\kappa e^{-\kappa x}$) with parameters $\kappa^{2D} = 0.2717$, $N^{2D} = 374.4$, and $\kappa^{3D} = 0.2473$, $N^{3D} = 2172$. All fits were performed using scipy.¹⁰⁹ The number of bins in the distributions was set to 35.

In Fig. 2 we show the distribution of key superconducting properties, including the electron-phonon coupling constant (λ), the logarithmic average of the phonon frequencies ($\omega_{\log}$), and the T_c calculated with the Allen-Dynes formula (see III). To shed some light on the difference between 2D and 3D, we plotted also the histogram from our previous search of 3D compounds.¹⁰¹

even if the 2D systems generally have much smaller Fermi surfaces. Furthermore, as the position of the peak is close in the two cases, we can still expect that the mechanism that leads to electron-phonon coupling in most 2D materials is similar to 3D, in spite of the different bonding patterns and atomic coordinations. The most visible difference is observed in the $\omega_{\log}$ histogram, with the average $\omega_{\log}$ for 2D materials being 144 K, around 70 K lower than in 3D. Both the average increase of λ and the decrease of $\omega_{\log}$ can be understood by noticing that

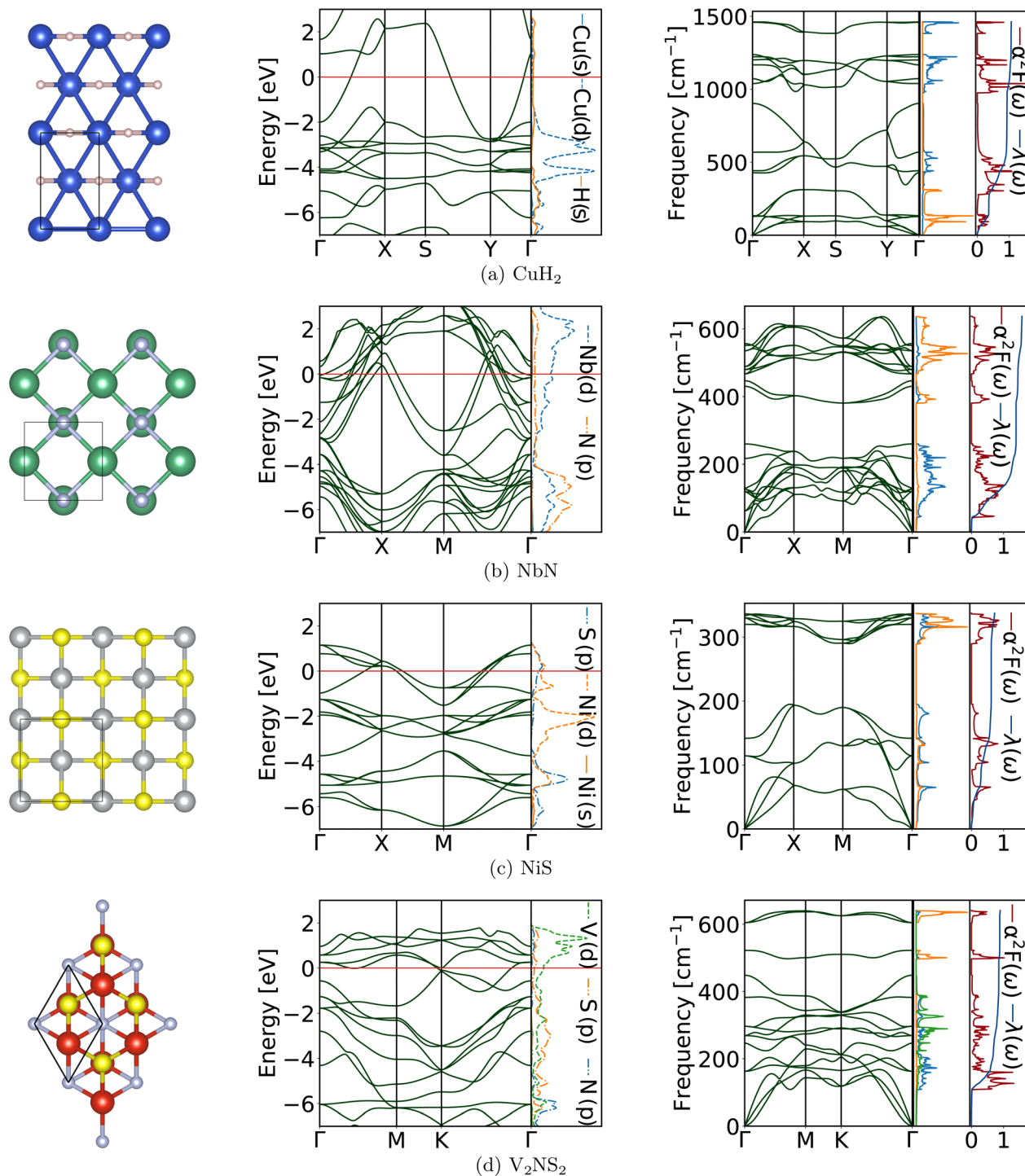


Fig. 3 Example 2D superconductors found in this work. The columns represent the chemical composition, a depiction of the crystal structure seen from the direction of the aperiodic axis, the electronic band structure and density of electronic states, and the phonon band structure, density of phonon states, and Eliashberg spectral function $\alpha^2F(\omega)$. In (a), Cu atoms are in blue and H in white; in (b), Nb atoms are in dark green and N in gray; in (c), Si atoms are in yellow and N in gray; in (d), V atoms are in red, N in gray and S in yellow. The primitive unit cell is also indicated.

the symmetry breaking due to the presence of the four layers – that cross the Fermi energy, leading to a very complicated Fermi surface. The phonons are well separated in two groups due to the very different masses of N and Nb. Most of the value of λ arises from the very strong coupling of the acoustic and

low-lying optical modes that have mostly Nb character. This leads to the very large $\lambda = 1.56$ but a relatively modest $\omega_{\log} = 177$ K, resulting in a T_c of 24.1 K. The energy above hull of 0.307 eV per atom indicates moderate thermodynamic stability, suggesting that NbN might be difficult to synthesize experimentally,



above the hull. This suggests good thermodynamic stability and a strong likelihood of being experimentally synthesizable. For V_2NS_2 we found that the Ir (110) facet is a good substrate candidate with 2.29% mismatch. The electronic band structure of V_2NS_2 features a doubly degenerate Dirac point at K and extra crossing of the Fermi surface between K and Γ . Furthermore, the Fermi level touches the conduction band between M and Γ . The lowest-energy electrons originate from both S and V, while above the Fermi level, the electrons come predominantly from V. The phonon band structure reveals a high density of medium-frequency modes, primarily stemming from vibrations of the V and S atoms. Additionally, two high-frequency modes are observed, originating from the vibrations of the inner N atoms. These high frequency N modes are expected due to the lower mass of N compared to S and V, as well as its spatial constraints. The high density of low-frequency modes contributes to an electron-phonon coupling constant of $\lambda = 0.88$, while the high-frequency modes from nitrogen contribute significantly to the value of $\omega_{\text{log}} = 246$ K, resulting in a critical transition temperature of $T_c = 14.4$ K. We note that a calculation including anisotropy reveals that V_2NS_2 is indeed a single gap superconductor, but with a slight increase of T_c to about 19 K.

D. Discussion

We showed how using machine learning models, combined with standard density-functional based methods, can be used to explore, in a very efficient manner, 2D superconductors. It turns out that in 2D the electron-phonon coupling is stronger than in 3D, but the average phonon frequency decreases, due to the lower frequency of out-of-plane modes. Even if this leads to a decrease of the average transition temperature of 2D compounds with respect to 3D compounds, we still find a number of out-of-distribution systems with considerably higher T_c . As in 3D, the presence of hydrogen, nitrogen, or niobium are advantageous for superconductivity in 2D, but we also find systems with many other chemical elements. From our workflow, several interesting compounds, emerged, not only with relatively high- T_c , but also with rather low distances to the convex hull of thermodynamic stability suggesting that they are good candidates for experimental synthesis.

In spite of these advancements, we still face a number of challenges. The training set for the machine learning models still contains a relatively small number of 2D compounds, that translates into sizeable errors in the predictions. The solution to this problem is straightforward, specifically running electron-phonon calculations for more 2D compounds, so we expect significant improvements in the near future. We note that the prediction of superconducting properties will also benefit from any advances in machine learning methods for the prediction of structure-property relationships.

Another issues arises from the fact that we have a much smaller knowledge of 2D materials, both experimentally and theoretically, than of 3D compounds. For example, there are around 140 thousand 2D compounds in Alexandria while this database contains 5 million 3D compounds. Furthermore, the large majority of the 2D compounds contain non-metallic chemical elements, leading to a reduced number of intermetallic

Finally, in Fig. 3(d) we show V_2NS_2 , a representative of the family of 2D superconductors for which we found more compounds. This prototype (A_2BC_2) features a thick-layered structure composed of five atomic layers arranged in a sandwich-like configuration. At the center of the slab we find a layer of B-atoms (here N), surrounded on both sides by layers of A-atoms (V), which are further capped by C-atoms (S) layers. Viewed from above, the structure forms a hexagonal pattern, crystallizing in the trigonal space group $\bar{P}3m1$ (#72). The primitive unit cell contains 5 atoms, with the A and C atoms occupying the 2c Wyckoff positions while the B atom occupies the 1a Wyckoff position. In this family we identified 7 superconductors, namely Mo_2BSe_2 , V_2BSe_2 , Nb_2CO_2 , Ta_2NS_2 , V_2NS_2 , Ti_2NSE_2 , and Nb_2NSE_2 . The highest T_c in this family belongs to Nb_2CO_2 ($T_c = 20.2$ K), however this system has larger E_{hull} (0.124 eV per atom) than V_2NS_2 that was found to be merely 0.050 eV per atom

compounds, many of them potentially superconducting. An exploration of the 2D space, for example by using machine-learning-accelerated high-throughput searches that were extremely successful in the 3D world, is therefore a necessity to find novel 2D superconductors with interesting and unexpected properties.

III. Methods

We chose the parameters of our *ab initio* calculations in order to ensure compatibility (whenever possible) with our previous work on 3D superconductors.¹⁰¹ All density-functional calculations were performed using version 7.1 of Quantum Espresso^{112,113} with the Perdew–Burke–Ernzerhof functional for solids (PBEsol)¹¹⁴ generalized gradient approximation. We used the PBEsol pseudopotentials¹¹⁴ from the pseudodojo project,¹¹⁵ specifically the stringent, scalar-relativistic norm-conserving set. Geometry optimizations were performed using uniform Γ -centered k -point grids with a density of $1.5 \times (6\pi)^2$ k -points per $\text{\AA}^{-2}$. If this resulted in an odd number of k -points, the next even number was used instead. We ensured that a vacuum region of 15 $\text{\AA}$ separated the layers, and we truncated the Coulomb interaction in the z -direction following the method of ref. 116. Convergence thresholds for energies, forces, and stresses were set to 1×10^{-8} a.u., 1×10^{-6} a.u., and 5×10^{-2} kbar, respectively. For the electron–phonon coupling, we used a double-grid technique, with the same k -grid used in the lattice optimization as the coarse grid, and a k -grid quadrupled in each direction as the fine grid. For the q -sampling of the phonons, we used half of the k -point grid described above. For all k - and q -point samplings, we used a single point in the aperiodic direction. The double δ -integration to obtain the Eliashberg function was performed with a Methfessel–Paxton smearing of 0.05 Ry. For the higher precision calculations, we repeated the previous steps by changing the initial k -point grid density to $3 \times (6\pi)^2$ k -points per $\text{\AA}^2$ and by setting the k -grid used as the coarse grid to double the k -grid used for the geometry optimization.

For the machine learning part, we trained the Alignn¹¹⁷ model using, as targets, λ , ω_{log} , and T_c simultaneously, with the error for each property weighted equally. The dataset used contained both 3D and 2D data, and we employed a random split of 90%/5%/5% for training/validation/test sets. The mean absolute error (MAE) on the test set for the final model was 0.151, 31.9 K, and 2.51 K for λ , ω_{log} , and T_c , respectively. For reference, the mean values on the test set for λ , ω_{log} , and T_c are 0.533, 277 K, and 6.16 K. When considering only the 2D materials present in the test set, the corresponding MAEs are 0.204, 31.3 K, and 1.65 K, for mean values of 0.495, 147 K, and 1.36 K. While the error on T_c is significant, we can still see its usefulness for screening new 2D superconductors. When examining the values obtained with DFPT for the 2D materials recommended by the model, we observe that 33% of the calculated T_c values are above the 5 K threshold. This value should be compared to 13% success rate for our initial dataset.

The values of

$$\lambda = 2 \int \frac{\alpha^2 F(\omega)}{\omega} d\omega, \quad (1a)$$

$$\log(\omega_{\text{log}}) = \frac{2}{\lambda} \int \frac{\log(\omega)}{\omega} \alpha^2 F(\omega) d\omega, \quad (1b)$$

$$\omega_2^2 = \frac{2}{\lambda} \int \omega \alpha^2 F(\omega) d\omega, \quad (1c)$$

where $\alpha^2 F(\omega)$ is the Eliashberg spectral function, were used to calculate the superconducting transition temperature using the Allen–Dynes modification¹⁰⁶ to the McMillan formula^{107,108}

$$T_c^{\text{McMillan}} = f_1 f_2 \frac{\omega_{\text{log}}}{1.20} \exp \left[-1.04 \frac{1 + \lambda}{\lambda - \mu^* (1 + 0.62\lambda)} \right], \quad (2)$$

where

$$f_1 = \left\{ 1 + \left[\frac{\lambda}{2.46(1 + 3.8 \times \mu^*)} \right]^{3/2} \right\}^{1/3} \quad (3a)$$

$$f_2 = 1 + \frac{\lambda^2 (\omega_2 / \omega_{\text{log}} - 1)}{\lambda^2 + [1.82(1 + 6.3\mu^*) \omega_2 / \omega_{\text{log}}]^2} \quad (3b)$$

We took arbitrarily $\mu^* = 0.10$ for all materials studied, a value that has become rather standard in this kind of studies.

Author contributions

T. H. B. S. and T. C. developed the high-throughput workflow; T. F. T. C. trained the machine learning model and performed the predictions; H.-C. W. and M. A. L. M. performed the response calculations and directed the research. All authors participated equally in the interpretation of the results and in the writing of the manuscript.

Data availability

The data produced in this work can be downloaded from the Alexandria database⁹⁶ at <https://alexandria.icams.rub.de/>. The workflow, and the model together with the dataset used for its training is available on GitHub at <https://github.com/hyllios/utis/>.

Conflicts of interest

The authors declare that they have no competing interests.

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