

Cite this: *Nanoscale Adv.*, 2022, 4, 4131

Capillary-force-driven self-assembly of carbon nanotubes: from *ab initio* calculations to modeling of self-assembly†

Stefania Carapezzi,[‡] Gabriele Boschetto[‡] and Aida Todri-Sanial[‡]*

In elasto-capillary driven self-assembly of arrays of carbon nanotubes (CNTs) different factors play a role, from the mechanical properties of CNTs to the array geometry. In this work, we provide a multi-scale investigation where we first use density functional theory (DFT) to predict fully *ab initio* relevant mechanical properties such as Young's modulus, Poisson's ratio, and surface energy. To the best of our knowledge, we are the first to report DFT calculations of the surface energy of CNTs. Then, we feed the computed DFT parameters into a model for capillary-force-driven self-assembly of CNTs. By doing so, we are able to derive and predict cross-correlation between material parameters and array architecture.

Received 10th May 2022

Accepted 22nd August 2022

DOI: 10.1039/d2na00295g

rsc.li/nanoscale-advances

1 Introduction

The rational design of micro-/nano-scaled material architectures has recently attracted huge interest as a means to engineer their physical properties. For instance, vertically aligned nanowires (NWs) modulate the optical properties of surfaces because their geometry (diameter, height, pitch) can tailor light confinement and absorption. The consequent enhancement of light harvesting is greatly demanded in photovoltaic applications.¹ Arrays of carbon nanotubes (CNTs) allow to build highly-dense 3D integrated circuit architectures. The unprecedented increase in connectivity between different functional layers (*e.g.*, sensing, storing, processing)² is ideally suited to be exploited in data-intensive technologies like Internet-of-Things (IoT). For all the implementations mentioned above and others, the preservation of the vertical direction during processing of densely-packed arrays of 1D nano-structures is fundamental. However, different fabrication steps may deflect such a desired direction. The exposure to an electron beam, for instance, during characterization through scanning electron microscope, has been reported to bend semiconductor NWs with subsequent formation of NW bundles.^{3–6} Procedures involving wet etching or cleaning also result in reshaping of the vertical arrangement of NWs^{7–9} and CNTs. In all these cases, a drying step occurs where capillary menisci between adjacent nano-pillars induce lateral forces that may bring these in contact^{10,11} and eventually assemble together.

Although self-assembly could have a detrimental impact, its purposeful exploitation can also drive the fabrication of aggressively scaled devices. More specifically, self-assembly stands for a large family of bio-inspired strategies, where components organize autonomously into desired patterns or structures with no human intervention.^{12–15} The concept originated from the chemistry of molecular assemblies mediated by intermolecular bonds to build up supramolecular systems,¹⁶ and it has subsequently broadened its meaning to indicate programmed aggregation of non-molecular parts whose size ranges from nano to macroscopic scale. Indeed, the current extreme shrinkage of the operative regime in various technological fields can be severely hindered by material and engineering limitations at such scales, especially when the fabrication of non-planar 3D structures is involved. Thus, new paradigms such as self-assembly may become a game-changer to enable 3D small scale manufacturing.¹²

A key aspect of both avoiding undesirable sticking effects and, on the contrary, harnessing them to build smart architectures and/or devices is the ability to engineer and control such effects. In particular, the elasto-capillary driven self-assembly of arrays of 1D nano-structures is a multi-faceted phenomenon where many different factors play a role: (1) the mechanical properties of the involved nano-structures, (2) the geometry of the array (inter-distance, aspect-ratio), (3) the evaporation rate and the surface tension of the fluid in which the nano-scaled beams are immersed. Although a wealth of literature exists concerning the mechanism of clustering in arrays of 1D nano-structures, usually its analysis is mainly based on the elasticity theory alone,^{10,11,17,18} whereas the material properties are commonly taken from experimental literature. A multi-scale investigation able to integrate a rigorous calculation of mechanical properties into the established theoretical modeling of the phenomenon is still as yet missing.

Microelectronics Department, LIRMM, University of Montpellier, CNRS, 161 Rue Ada, Montpellier, France. E-mail: stefania.carapezzi@gmail.com; aida.todri@lirmm.fr

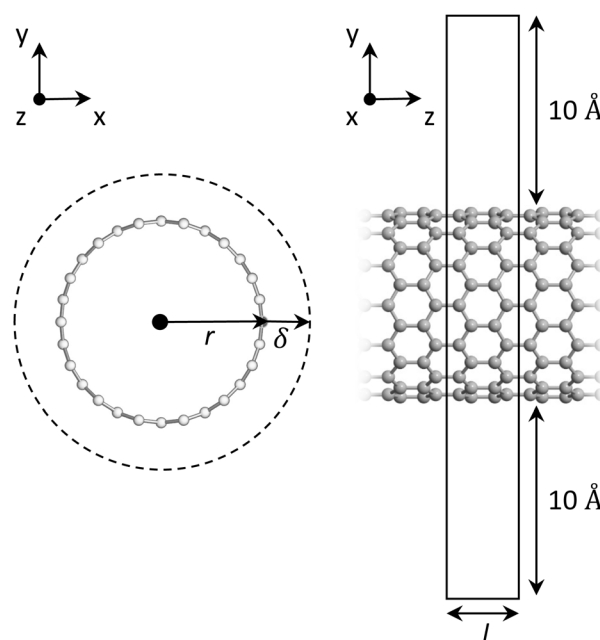
† Electronic supplementary information (ESI) available. See <https://doi.org/10.1039/d2na00295g>

‡ These authors contributed equally to this work.

Our paper is organized as follows: the first section is dedicated to predicting the relevant mechanical parameters of CNTs *via* DFT simulations; here, we describe the details of our simulations and present the results. Then, in the following section, the mechanism of capillary-force-driven self-assembly of CNTs is expressed through a simple model. The previously computed DFT parameters (Young's modulus, Poisson's ratio, and surface energy) are fed into such a model. Finally, inferences regarding the occurrence of self-assembly are consequently derived.

2.1 Simulation details

where r_0 and l_0 are the radius and the length of the CNT, respectively, at $\varepsilon = 0$. δ is the thickness of the tube. As per convention,³⁷ we chose $\delta = 3.35$ Å, which is the interlayer



© 2022 The Author(s). Published by the Royal Society of Chemistry

distance in graphite as obtained by our DFT simulations. We computed the Poisson's ratio (ν) as:

$$\nu = -\frac{1}{\varepsilon} \left(\frac{r_\varepsilon - r_0}{r_0} \right), \quad (3)$$

where r_ε is the radius of the CNT at each percentage of strain.³⁶ Finally, we extracted the surface energy per unit area (γ) by adapting the equation discussed by Medasani *et al.*:^{38,39}

$$\gamma = \frac{nE_{\text{graphene}}^{\text{coh}} - E_{\text{CNT}}^{\text{b}}}{2\pi r_0 l_0}, \quad (4)$$

where $E_{\text{graphene}}^{\text{coh}}$ is the cohesive energy of graphene, n is the number of atoms, $E_{\text{CNT}}^{\text{b}}$ is the total binding energy of the CNT, and the denominator is the surface area of the CNT.

2.2 Results and discussion

We computed the mechanical properties of CNTs as a function of both radius and chirality (armchair and zigzag). The results are shown in both Table 1 and Fig. 2.

First, our simulations predict Y to increase with respect to the tube diameter and to converge to ~ 1.02 TPa when $d \geq 12$ – 13 Å. However, we note that even at smaller diameters, Y is still reasonably close to 1 TPa. Our computed value of Y compares well with both experimental and theoretical data, although it is worth pointing out that there exists a rather large variability reported in the literature. Regarding experimental data, such variability is due to the employed measurement technique and the quality of the CNT samples, as it is known that defects can have a non-negligible effect. On the other hand, in theoretical models, the variability is primarily due to the CNT thickness (as previously mentioned, here we use $\delta = 3.35$ Å). Overall, typical values of Y for single-wall CNTs oscillate around 1 TPa.^{40,41} Chirality does not seem to have a major effect on Y , although the increasing trend with respect to the tube diameter is somewhat less smooth in armchair CNTs. Overall, our results suggest the stiffness of CNTs to slightly increase with respect to their diameter.

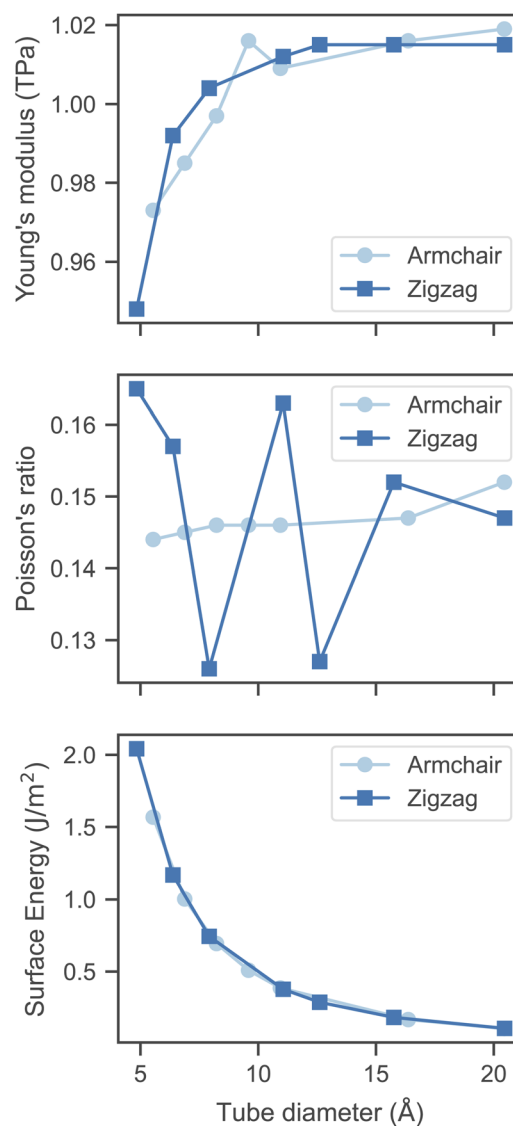


Fig. 2 Mechanical properties of the CNT structures considered in this work (armchair and zigzag) as a function of the tube diameter, as obtained *via* DFT simulations.

Table 1 Computed mechanical parameters of the CNT structures considered in this work by DFT. d is the tube diameter, Y the Young's modulus, ν is the Poisson's ratio, and γ is the surface energy

Structure	d (Å)	Y (TPa)	ν	γ (J m ⁻²)
(6,0)	4.84	0.948	0.165	2.042
(8,0)	6.38	0.992	0.157	1.167
(10,0)	7.92	1.004	0.126	0.744
(14,0)	11.06	1.012	0.163	0.377
(16,0)	12.61	1.015	0.127	0.287
(20,0)	15.76	1.015	0.152	0.182
(26,0)	20.46	1.015	0.147	0.106
(4,4)	5.54	0.973	0.144	1.568
(5,5)	6.88	0.985	0.145	1.003
(6,6)	8.23	0.997	0.146	0.694
(7,7)	9.59	1.016	0.146	0.509
(8,8)	10.94	1.009	0.146	0.386
(12,12)	16.37	1.016	0.147	0.167
(15,15)	20.45	1.019	0.152	0.105

The Poisson's ratio (ν) is the second parameter that we have computed. Interestingly, we observed that the chirality of the tube appears to have some effect on this quantity. As can be seen from Fig. 2, armchair CNTs possess roughly the same value of ν (0.14–0.15) regardless of the tube diameter, whereas, in zigzag CNTs, such a value oscillates between 0.125 and 0.165. However, for $d > 15$ Å, we observe that for both zigzag and armchair CNTs, the Poisson's ratio converges to ~ 0.15 . Once again, we point out that our results are consistent with published experimental data, in which ν was found to range between 0.149 and 0.340.⁴²

Finally, we computed the surface energy (γ) of CNTs, which, to the best of our knowledge, has never been previously computed *via* DFT simulations for this class of materials. As per its definition, surface energy is the energy required to create one unit of surface area. In this work, we computed γ by considering



graphene as the reference structure from which CNTs are derived (see Simulation details). Therefore, γ can be seen as a measure of the excess energy induced by the curvature of the C-C bonds in the structure of CNTs. Indeed, our results predict a decrease of γ with respect to the diameter of the tubes, regardless of the chirality. For $d \approx 5 \text{ \AA}$, we found a rather high value of $\sim 2.0 \text{ J m}^{-2}$, which reduces to $\sim 0.1 \text{ J m}^{-2}$ for diameters larger than 2 nm. It is worth noting that there exists a large variability in the experimental value of the surface energy of CNTs, although on average $\gamma = 0.26 \text{ J m}^{-2}$, larger and smaller values have also been reported.⁴³ Nevertheless, our results appear to be within the accepted range of values. The decreasing trend of γ with respect to the CNTs diameters can be easily explained by the amount of strain induced by the curvature to the sp^2 C-C bonds, which should normally be planar. Smaller diameters would lead to a larger distortion of the planarity of C-C bonds and, thus, increase the surface energy.

3 Elastocapillary self-assembly of carbon nanotube arrays

The self-assembly of CNTs mediated by elasto-capillary forces is due to the combination of two different mechanisms (Fig. 3). First, (A) the process of bending the CNTs to favor the contact between their surfaces (Fig. 3a). To this aim, the CNTs are immersed in a liquid, whose evaporation induces their bending, provided that the capillary forces acting during the drying step defeat the elastic forces that would reset them back to the original vertical alignment. Second, (B) the process of CNT bundling (Fig. 3b). This occurs if the adhesion forces acting between the touching surfaces of CNTs are larger than the elastic forces that would tend to set them apart. In the following, we model the elasto-capillary self-assembly of CNTs by considering the simplest possible bundled unit composed of two CNTs. For simplicity's sake, we assume that both CNTs have the same geometry and physical properties. It has been demonstrated¹⁰ that the lateral forces resulting from capillary menisci interaction are those responsible for the clustering of micro-sized pillars after liquid evaporation. The capillary force between two cylindrical structures (F_C) when they are partially

immersed in a liquid can be estimated through Kralchevsky's asymptotic solution⁴⁴ as:

$$F_C = \frac{\pi \gamma_{\text{liq}} R^2 \cos^2(\theta)}{\sqrt{x^2 - R^2}}, \quad (5)$$

where γ_{liq} is the liquid surface tension, θ is the equilibrium contact angle between the cylindrical surface and the liquid, R is the cylinder's radius, and $2x$ is the inter-distance between axes of two structures (Fig. 3a). Regarding the elastic force that would restore each pillar to the original straight position, this can be estimated from the Euler-Bernoulli elementary beam theory⁴⁴ as the elastic force deflecting a beam clamped at one end, of height h , such that the free end is deflected of w :

$$F_{\text{el}} = \frac{3EIw}{h^3}, \quad (6)$$

where E is the pillar's Young modulus and I is its area moment of inertia.

We determine F_C from eqn (5) for all the CNTs considered, whose radii R_{CNT} are listed in Table 1. We use values of w ranging from 1 to 100 nm. We consider water as the liquid catalyzing the coalescence of CNTs, as frequently reported in literature. Consequently, we use θ equal to 86° ⁴⁵ and $\gamma_{\text{H}_2\text{O}} = 72 \text{ mN m}^{-1}$. Fig. 4 shows the behavior of calculated F_C vs. w for CNT armchair (4,4) (Fig. 4a; green dotted line) and for CNT armchair (15,15) (Fig. 4b; green dashed line). w is $x - R_{\text{ext}}$, for $R_{\text{ext}} = R_{\text{CNT}} + \delta$ being the external radius of CNT, where $\delta = 0.335 \text{ nm}$ is CNT thickness. The magnitude of F_C decreases from 8.36 to 0.124 pN for CNT armchair (4,4), and from 31.8 to 0.6 pN for CNT armchair (15,15), within the probed interval of w . We determine F_{el} from eqn (6) for all the CNTs, where the corresponding Young's moduli are reported in Table 1. We calculate I_{CNT} as the area moment of inertia of a tube, $\pi \times (R_{\text{ext}}^4 - R_{\text{int}}^4)/4$, with $R_{\text{int}} = R_{\text{CNT}}$. Fig. 4 shows calculated F_{el} vs. w for different values of CNT height h_{CNT} (from 24 nm to 10 μm). By comparing F_C and F_{el} values, we can assess when capillary forces are stronger than elastic forces. In case of CNTs armchair (4,4) (Fig. 4a) and h_{CNT} equal or smaller than 24 nm, F_{el} is larger than F_C for all probed w values. This means that CNTs are not brought into contact by capillary forces. For h_{CNT} larger than 24 nm and smaller than 500 nm, it exists a threshold value of w

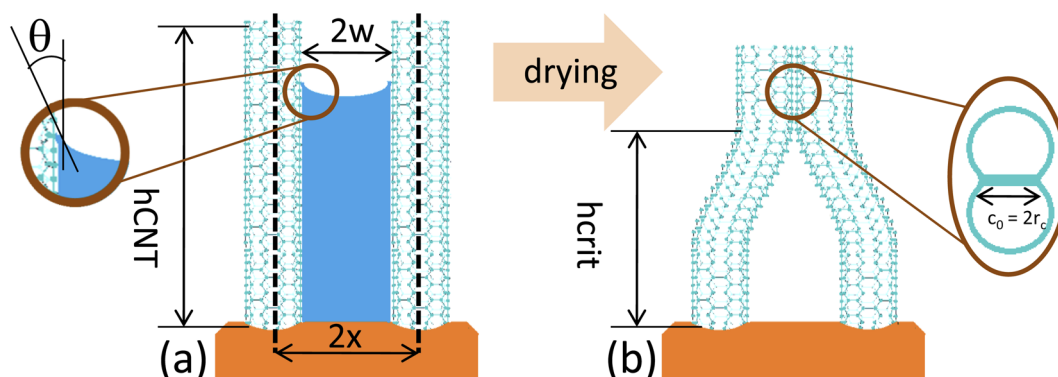


Fig. 3 (a) Capillary meniscus between two CNTs, the distance between whose axes being $2x$. In the inset is magnified the interface vapor/liquid close to the CNT surface, where θ is the contact angle. (b) Lateral collapsing between two adjacent CNTs.



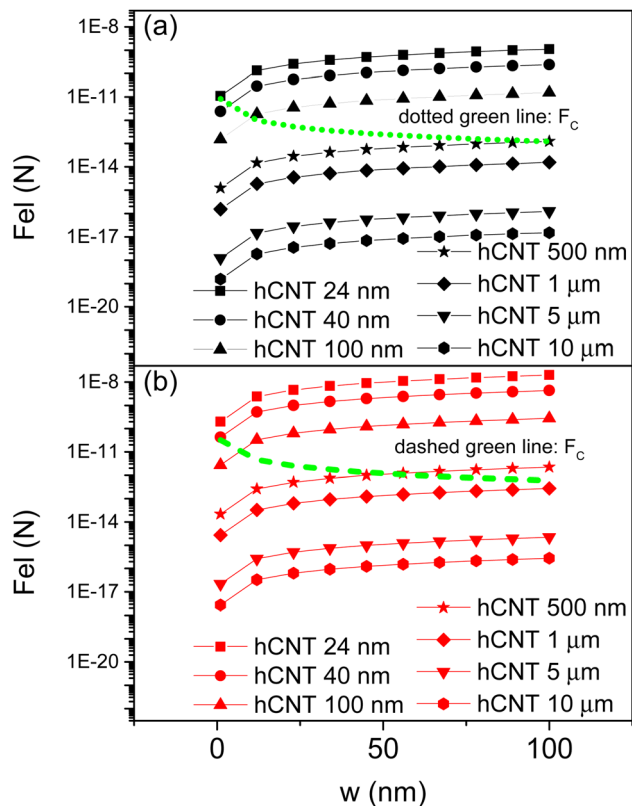


Fig. 4 Behavior with w of F_C from eqn (5) (green lines) and of F_{el} from eqn (6) (symbols), for (a) armchair (4,4) CNT and (b) armchair (15,15) CNT.

above which F_C becomes smaller than F_{el} . Finally, for CNTs taller than 500 nm capillary forces are stronger than elastic forces for all considered w values. The same analysis is qualitatively applicable to other armchair CNTs (results of armchair (15,15) are shown in Fig. 4b) and to zigzag CNTs (Fig. ESI† of the ESI†).

Once the conditions for capillary-forces-driven contact of CNTs are established, we also need to assess when the adhesion forces between their surfaces are such to keep them self-assembled. In this respect, we avail of a theoretical model obtained studying the contact behavior of fibrillar interfaces.^{17,46} Such model has been validated against experimental results for a variety of material interfaces, like arrays of poly(dimethylsiloxane) fibrils¹⁷ and gallium arsenide nanowires.³ It is important to note that fibrillar interfaces are intensively investigated to mimic the efficiency of adhesiveness of some natural contact surfaces, for example, the ones of lizards. These interfaces are simply modeled as arrays of pillars (called fibrils) extruding from a substrate. The surfaces of two next-neighbor pillars may stick together, once they are brought to touch each other, due to the influence of van der Waals forces. In this case, the elastic strain energy U_b of the system is concentrated into the noncontact region of length H , which is deformed by the bending (Fig. 3b). The increase of H by a small amount dH implies a consequent strain energy variation of $(9EIw^2) \times dH/H^4$. If the system is in equilibrium, then it must be equal to the

work dW necessary to shrink the contact area. For cylindrical-shaped pillars, the contact radius r_c is smaller than cylinder's radius. Also, some elastic deformation occurs near the contact region¹⁷ (inset of Fig. 3b). JKR theory¹⁸ allows to calculate the equilibrium contact width $c_0 = 2r_c$, and thus the energy to separate the two surfaces is determined to be $(2\gamma_{\text{sup}}c_0 - U_c) \times dH$, where U_c is the elastic energy stored into the deformed region of contact¹⁷ and γ_{sup} is the surface energy. c_0 and U_c are¹⁷ as follows:

$$\frac{c_0}{2} = r_c = \left(\frac{32R^2\gamma_{\text{sup}}}{\pi E^*} \right)^{1/3} \quad (7)$$

$$U_c = \frac{\pi E^* R^2}{32} \left(\frac{r_c}{R} \right)^4 \quad (8)$$

respectively, for $E^* = E/(1 - \nu^2)$, ν being the Poisson's ratio. The consideration of energy balancing yields a criterion of critical height for lateral collapse that reads as:

$$h_{\text{crit}} = \left[\frac{9EIw^2}{2\gamma_{\text{sup}}c_0 - U_c} \right]^{1/4} \quad (9)$$

where CNTs bundle if their height is larger than h_{crit} . It is noteworthy to observe that h_{crit} increases monotonically with w . Then, a stable bundling is obtained with taller and taller CNTs for arrays with larger and larger inter-distance between CNTs. Fig. 5 shows h_{crit} as determined from eqn (9) for all armchair CNTs considered, plotted against w . It can be seen that h_{crit} ranges from 5.7 to 57 nm for CNT armchair (4,4), up to from 25 to 255 nm for CNT armchair (15,15). The ranges in which CNT self-assembly is predicted to occur can be assessed by comparison between Fig. 4 and 5. Thus, in the case of CNT armchair (4,4), for h_{CNT} below $h_A = 24$ nm, capillary-force-driven self-assembly does not occur, given that capillary forces are not

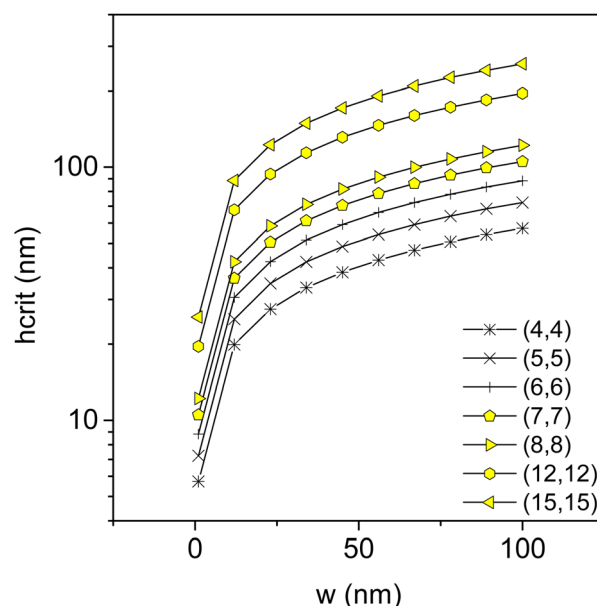


Fig. 5 Critical height h_{crit} of lateral collapse by eqn (9), from armchair (4,4) CNT to armchair (15,15) CNT.



able to overcome elastic forces. For h_{CNT} above h_A and below h_B , $= 500$ nm, capillary forces are able to bring CNTs into contact only for w below a threshold w_{th} , which depends on h_{CNT} . In this latter case, h_{CNT} results to be above h_{crit} , thus, the CNTs brought into contact form a bundle. For h_{CNT} above h_B the capillary-force-driven bundling of CNTs occurs for every value of w , and the adhesion forces are always able to keep the CNT bundle stable. The above discussion can be repeated for the other armchair (and zigzag) CNTs, where R_{CNT} modulates the value of h_A and h_B : for example, $h_A = 40$ nm for CNT armchair (15,15).

4 Conclusions

In this work, we show a rigorous approach integrating *ab initio* calculation of CNT mechanical properties into theoretical modeling of capillary-force-driven self-assembly of CNTs, with the purpose of providing guidelines to exploit this phenomenon. We use DFT to predict Young's modulus, Poisson's ratio, and surface energy of CNTs. We investigate the impact of both diameter and chirality on such properties. We find that (1) Young's modulus increases and (2) surface energy decreases with respect to CNT diameter. To the best of our knowledge, we are the first to report DFT calculations of CNT surface energy. Then, we feed the relevant DFT parameters into a model for capillary-force-driven self-assembly of CNTs. We find that there exists height values h_A and h_B such that (A) for $h_{\text{CNT}} < h_A$ capillary-force-driven self-assembly does not occur, (B) for $h_A < h_{\text{CNT}} < h_B$ capillary forces bend CNTs into contact only for w below threshold values w_{th} , and (C) for $h_{\text{CNT}} > h_B$ the capillary-force-driven bundling of CNTs occurs for every value of w . Finally, we find that such values h_A , h_B depend on R_{CNT} .

Author contributions

SC and GB conceived the study concept and designed the simulations. GB performed DFT simulations and analyzed the data. SC performed elastic theory calculations and evaluated and interpreted the data. SC and GB drafted the manuscript. ATS critically revised the manuscript. ATS supervised the study. The manuscript has been read and approved by all authors.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

This project has received funding from the European Union's Horizon 2020 Research and Innovation Programme, EU H2020 SmartVista (<https://www.smartvista.eu>), grant agreement no. 825114.

References

- W. Chen and P. R. i Cabarrocas, *Nanotechnology*, 2019, **30**, 194002.
- M. M. Shulaker, G. Hills, R. S. Park, R. T. Howe, K. Saraswat, H.-S. P. Wong and S. Mitra, *Nature*, 2017, **547**, 74–78.
- S. Carapezzi, G. Priante, V. Grillo, L. Montès, S. Rubini and A. Cavallini, *ACS Nano*, 2014, **8**, 8932–8941.
- N. Senthilnathan and T. P. Radhakrishnan, *Chem. Mater.*, 2020, **32**, 8567–8575.
- L. A. Bitzer, C. Speich, D. Schäfer, D. Erni, W. Prost, F. J. Tegude, N. Benson and R. Schmechel, *J. Appl. Phys.*, 2016, **119**, 145101.
- V. M. Kaganer, S. Fernández-Garrido, P. Dogan, K. K. Sabelfeld and O. Brandt, *Nano Lett.*, 2016, **16**, 3717–3725.
- S. Carapezzi and A. Cavallini, *Beilstein J. Nanotechnol.*, 2019, **10**, 2094–2102.
- T. Ghosh, E.-C. Fritz, D. Balakrishnan, Z. Zhang, N. Vrancken, U. Anand, H. Zhang, N. D. Loh, X. Xu, F. Holsteyns, C. A. Nijhuis and U. Mirsaidov, *ACS Appl. Mater. Interfaces*, 2022, **14**, 5537–5544.
- N. Vrancken, T. Ghosh, U. Anand, Z. Aabdin, S. W. Chee, Z. Baraissov, H. Terry, S. D. Gendt, Z. Tao, X. Xu, F. Holsteyns and U. Mirsaidov, *J. Phys. Chem. Lett.*, 2020, **11**, 2751–2758.
- D. Chandra and S. Yang, *Langmuir*, 2009, **25**, 10430–10434.
- P. Kralchevsky, V. Paunov, I. Ivanov and K. Nagayama, *J. Colloid Interface Sci.*, 1992, **151**, 79–94.
- K. S. Kwok, Q. Huang, M. Mastrangeli and D. H. Gracias, *Adv. Mater. Interfaces*, 2020, **7**, 1901677.
- M. De Volder and A. J. Hart, *Angew. Chem., Int. Ed.*, 2013, **52**, 2412–2425.
- K. J. M. Bishop, C. E. Wilmer, S. Soh and B. A. Grzybowski, *Small*, 2009, **5**, 1600–1630.
- G. M. Whitesides and B. Grzybowski, *Science*, 2002, **295**, 2418–2421.
- J.-M. Lehn, *Science*, 1993, **260**, 1762–1763.
- N. J. Glassmaker, A. Jagota, C.-Y. Hui and J. Kim, *J. R. Soc. Interface*, 2004, **1**, 23–33.
- C. Y. Hui, Y. Y. Lin, J. M. Baney and A. Jagota, *J. Adhes. Sci. Technol.*, 2000, **14**, 1297–1319.
- Y. Che, H. Chen, H. Gui, J. Liu, B. Liu and C. Zhou, *Semicond. Sci. Technol.*, 2014, **29**, 073001.
- M. F. L. D. Volder, S. H. Tawfick, R. H. Baughman and A. J. Hart, *Science*, 2013, **339**, 535–539.
- G. Boschetto, S. Carapezzi and A. Todri-Sanial, *IEEE Open J. Nanotechnol.*, 2021, **2**, 120–128.
- M. Hartmann, J. Tittmann-Otto, S. Böttger, G. Heldt, M. Claus, S. E. Schulz, M. Schröter and S. Hermann, *ACS Appl. Mater. Interfaces*, 2020, **12**, 27461–27466.
- K. Chikkadi, M. Muoth, V. Maiwald, C. Roman and C. Hierold, *Appl. Phys. Lett.*, 2013, **103**, 223109.
- K. Chikkadi, M. Muoth, C. Roman, M. Haluska and C. Hierold, *Beilstein J. Nanotechnol.*, 2014, **5**, 2179–2191.
- S. Carapezzi, S. Reggiani, E. Gnani and A. Gnudi, *IEEE Trans. Electron Devices*, 2020, **67**, 4682–4686.
- A. Kamysny and S. Magdassi, *Chem. Soc. Rev.*, 2019, **48**, 1712–1740.
- A. S. Dahiya, J. Thireau, J. Boudaden, S. Lal, U. Gulzar, Y. Zhang, T. Gil, N. Azemard, P. Ramm, T. Kiessling,



- C. O'Murchu, F. Sebelius, J. Tilly, C. Glynn, S. Geary, C. O'Dwyer, K. M. Razeed, A. Lacampagne, B. Charlot and A. Todri-Sanial, *J. Electrochem. Soc.*, 2019, **167**, 037516.
- 28 A. S. Dahiya, T. Gil, J. Thireau, N. Azemard, A. Lacampagne, B. Charlot and A. Todri-Sanial, *Adv. Electron. Mater.*, 2020, **6**, 2000547.
- 29 R. R. Pandey, J. Liang, D. Cakiroglu, B. Charlot and A. Todri-Sanial, *Electrochemical Glucose Sensor Using Single-Wall Carbon Nanotube Field Effect Transistor*, 2020, <https://arxiv.org/abs/2006.12973>.
- 30 G. Boschetto, T. Xu, M. Yehya, J. Thireau, A. Lacampagne, B. Charlot, T. Gil and A. Todri-Sanial, *2021 IEEE International Conference on Flexible and Printable Sensors and Systems (FLEPS)*, 2021, pp. 1–4.
- 31 S. Smidstrup, T. Markussen, P. Vancraeyveld, J. Wellendorff, J. Schneider, T. Gunst, B. Verstichel, D. Stradi, P. A. Khomyakov, U. G. Vej-Hansen, M.-E. Lee, S. T. Chill, F. Rasmussen, G. Penazzi, F. Corsetti, A. Ojanperä, K. Jensen, M. L. N. Palsgaard, U. Martinez, A. Blom, M. Brandbyge and K. Stokbro, *J. Phys.: Condens. Matter*, 2020, **32**, 015901.
- 32 *QuantumATK Version S-2021.06*, Synopsys QuantumATK, <https://www.synopsys.com/silicon/quantumatk.html>, last accessed, April 25, 2022.
- 33 J. P. Perdew, K. Burke and M. Ernzerhof, *Phys. Rev. Lett.*, 1996, **77**, 3865–3868.
- 34 M. J. van Setten, M. Giantomassi, E. Bousquet, M. J. Verstraete, D. R. Hamann, X. Gonze and G.-M. Rignanese, *Comput. Phys. Commun.*, 2018, **226**, 39–54.
- 35 H. J. Monkhorst and J. D. Pack, *Phys. Rev. B: Solid State*, 1976, **13**, 5188–5192.
- 36 E. Hernández, C. Goze, P. Bernier and A. Rubio, *Phys. Rev. Lett.*, 1998, **80**, 4502.
- 37 J. P. Lu, *Phys. Rev. Lett.*, 1997, **79**, 1297.
- 38 B. Medasani, Y. H. Park and I. Vasiliev, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2007, **75**, 235436.
- 39 B. Medasani and I. Vasiliev, *Surf. Sci.*, 2009, **603**, 2042–2046.
- 40 A. Krishnan, E. Dujardin, T. W. Ebbesen, P. N. Yianilos and M. M. J. Treacy, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1998, **58**, 14013.
- 41 R. S. Ruoff, D. Qian and W. K. Liu, *C. R. Phys.*, 2003, **4**, 993–1008.
- 42 Z.-C. Tu and Z.-C. Ou-Yang, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2002, **65**, 233407.
- 43 M. R. Roenbeck, X. Wei, A. M. Beese, M. Naraghi, A. Furmanchuk, J. T. Paci, G. C. Schatz and H. D. Espinosa, *ACS Nano*, 2014, **4**, 124–138.
- 44 R. C. Hibbeler, *Mechanics of Materials*, Prentice-Hall, Englewood Cliffs, NJ, 3rd edn, 1997.
- 45 H. Liu, J. Zhai and L. Jiang, *Soft Matter*, 2006, **2**, 811–821.
- 46 A. Jagota and C.-Y. Hui, *Mater. Sci. Eng., R*, 2011, **72**, 253–292.

