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Single-layer metal halides MX_2 ($\text{X} = \text{Cl}, \text{Br}, \text{I}$): stability and tunable magnetism from first principles and Monte Carlo simulations†

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Based on first-principles calculations, we investigate a novel class of 2D materials – MX_2 metal dihalides ($\text{X} = \text{Cl}, \text{Br}, \text{I}$). Our results show that single-layer dihalides are energetically and dynamically stable and can be potentially exfoliated from their bulk layered forms. We found that 2D FeX_2 , NiX_2 , CoCl_2 and CoBr_2 monolayers are ferromagnetic (FM), while VX_2 , CrX_2 , MnX_2 and CoI_2 are antiferromagnetic (AFM). The magnetic properties of 2D dihalides originate from the competition between AFM direct nearest-neighbor d–d exchange and FM superexchange via halogen p states, which leads to a variety of magnetic states. The thermal dependence of magnetic properties and the Curie temperature of magnetic transition are evaluated using statistical Monte Carlo simulations based on the Ising model with classical Heisenberg Hamiltonian. The magnetic properties of single-layer dihalides can be further tuned by strain and carrier doping. Our study broadens the family of existing 2D materials with promising applications in nanospintronics.

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1. Introduction

Tremendous research attention is currently focused on two-dimensional (2D) nanomaterials due to their rich physical properties and diverse technological applications.^{1–3} The possibility of designing magnetic 2D nanostructures is particularly intriguing and can be useful for spintronics and nanoscale magnetic memory devices.⁴ Most 2D nanomaterials, however, do not show any intrinsic magnetism with only rare exceptions.^{5–13} The strategies to induce magnetic moments in otherwise non-magnetic 2D materials include defect engineering,¹⁴ strain,¹⁵ adatom adsorption,^{16–22} and substitutional doping.^{23,24} However, the resulting materials lack experimental controllability and stability. Moreover, metal dopants tend to form clusters due to strong d–d interactions resulting in non-homogenous magnetization and low Curie temperature values. Identifying magnetic 2D nanomaterials thus has been a challenge.

Here, we examine a novel class of 2D nanostructures – single-layer metal dihalides (MX_2 , where $\text{X} = \text{Cl}, \text{Br}, \text{I}$). Surprisingly, this class of nanomaterials is relatively unexplored despite the presence of stable layered structures in the bulk. However, halides start

to attract research attention now, including the layered ones.^{25–28} For instance, the experimentally synthesized layered BiI_3 has a bandgap of 1.8 eV and demonstrates room-temperature band-edge photoluminescence.^{29–31} Layered ternary bismuth iodides show good photovoltaic performance with an extra advantage of the significantly reduced toxicity of Bi when compared with Pb.³² Theoretical calculations demonstrate that single-layer PbI_2 is stable and exhibits interesting exciton and spin–orbit coupling effects.^{33,34} Monolayer GaBiCl_2 , ZrBr and HfCl were identified as room-temperature quantum spin Hall insulators with large nontrivial band gaps.^{35,36} FeCl_2 displays a half-metallic ferromagnetic ground state.^{37,38} Recent experimental studies demonstrated that single crystals of CrI_3 can be cleaved very easily, possess a ferromagnetic order even in the monolayer form, and are stable in air/water, in the absence of CrI_2 contamination.^{39–41} The above studies show a high potential of 2D halides from both fundamental and applied perspectives.

In this work, we demonstrate that single-layer metal dihalides are energetically stable and possess intrinsic ferromagnetism. Their magnetic properties originate from the competition between antiferromagnetic (AFM) direct nearest-neighbor d–d exchange and ferromagnetic (FM) superexchange via halogen p states, leading to a variety of magnetic states. By using density functional theory (DFT) methods, we determine the ground-state magnetic ordering and calculate the exchange coupling constants in 2D dihalides. The thermal dependence of magnetic properties and the Curie temperature of magnetic transition are

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estimated using statistical Monte Carlo (MC) simulations based on the Ising model. We find that single-layer dihalides exhibit comparable or even slightly higher Curie temperatures than single-layer dichalcogenides. This can be attributed to the profound ionic bonding in halides, which enhances the super-exchange coupling between the magnetic metal ions *via* the halogen atoms, consistent with the Goodenough–Kanamori–Anderson rules.

2. Computational methods

Spin-polarized first-principles calculations were performed within the density functional theory (DFT) framework, as implemented in the Quantum Espresso package.⁴² The core electrons were treated within the projector augmented wave (PAW) method.⁴³ Exchange–correlation effects were described through the generalized gradient approximation (GGA) and the PBEsol exchange–correlation functional.⁴⁴ PBEsol is a revision of the PBE functional, specifically tailored for solids, and has been shown to produce better agreement with experimental data.⁴⁴ For accurate electronic structure prediction, we used the HSE06 hybrid functional including 25% non-local Hartree–Fock exchange.⁴⁵ The total energy of monolayers was calculated using a Γ -centered $15 \times 15 \times 1$ Monkhorst–Pack k -point grid for a primitive cell. The plane-wave cutoff is 50 Ryd (680 eV). Test calculations with a larger number of k points and higher cutoff energies produced the same results. The optimized structures were obtained by relaxing all atomic positions and lattice parameters using the Broyden–Fletcher–Goldfarb–Shanno (BFGS) quasi-Newton algorithm until all forces are smaller than $0.01 \text{ eV } \text{\AA}^{-1}$. To account for the on-site Coulomb interactions between the 3d electrons, we performed DFT+ U calculations by adding an effective parameter, U_{eff} .⁴⁶ We have used U_{eff} values for transition metals suggested by Ceder *et al.*⁴⁷ We have also performed additional tests using other U_{eff} values from 1.0 to 6.0 eV, and found that the use of different U_{eff} values leads to qualitatively similar results.

3. Results and discussion

3.1. Crystal structure and stability

First, we examine the atomic structure of dihalides MX_2 ($\text{M} = \text{V}, \text{Cr}, \text{Mn}, \text{Fe}, \text{Co}, \text{Ni}$, and $\text{X} = \text{Cl}, \text{Br}, \text{I}$). As shown by experimental studies, bulk metal dihalides have a natural layered structure as shown in Fig. 1a. Therefore, similar to graphene and MoS_2 , individual layers of dihalides can be potentially extracted from the bulk using exfoliation techniques. For each monolayer, we have determined the minimum-energy structure by optimizing all atomic positions and lattice constants. The typical crystal structure of single-layer MX_2 is shown in Fig. 1b and c. The atomic geometry of monolayer dihalides is conceptually similar to the well-known transition-metal dichalcogenides (TMDCs). Namely, each metal dihalide is composed of three atomic planes: a layer of transition-metal (TM) atoms sandwiched between two layers of halogen atoms. Interestingly,

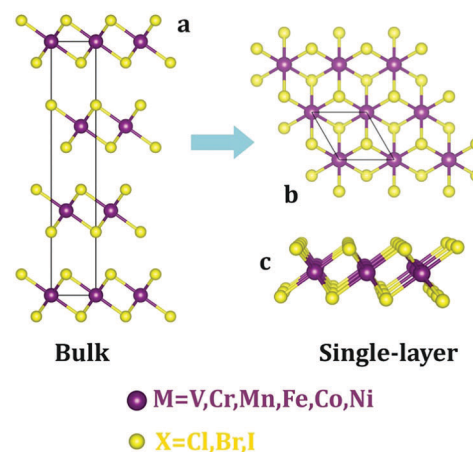


Fig. 1 Crystal structures of metal dihalides (MX_2) in the 1-T phase: (a) bulk and (b and c) single-layer. Top (b) and side (c) views are shown.

we find that all studied single-layer dihalides prefer the 1-T crystal structure (C_{3v} symmetry). Each metal atom is surrounded by 6 neighboring halogen atoms forming an octahedral $[\text{MX}_6]^{4-}$ unit. The 1-T crystal phase is also found in NbS_2 and TiSe_2 , in contrast to the H phase in MoS_2 and WSe_2 .⁴⁸ To assess the possibility of T–H phase transition, we computed the energy difference between these phases ($E = E_{\text{H}} - E_{\text{T}}$) for each monolayer (Fig. 2). We find that all relative energies are positive, indicating that 1-T is a ground-state structure. The energy associated with the T–H transition is considerable: several tenths of an eV per MX_2 formula unit. The computed absolute values are comparable to those in dichalcogenides, such as MoS_2 , WSe_2 and VS_2 .^{48,49} The smallest H–T energy difference is found in Fe dihalides and the largest in V and Ni dihalides.

The calculated structural parameters of MX_2 are summarized in Table 1. The obtained lattice constants are in good agreement with experimental data on bulk structures.^{50,51} The M–X bond lengths increase as M changes from V to Mn and then decrease to Ni. Both lattice parameters and M–X bond lengths increase with the element number of X ($\text{Cl} \rightarrow \text{Br} \rightarrow \text{I}$). These trends are consistent with the variations of the radii of the TM atoms in their +2 valence states, as well as increasing the atomic radius of halogen. All M–X–M bond angles are $\sim 90^\circ$. The stability of single-layer dihalides can be evaluated from their formation

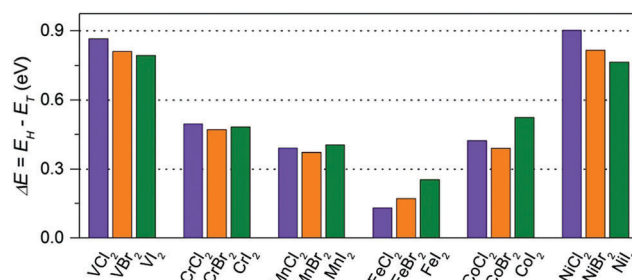


Fig. 2 The energy difference (per MX_2 formula unit) between H and T phases for all studied monolayers. The energies are computed at the equilibrium lattice parameters for each phase.



	E_{form}	a (DFT)	a (Exp.)	$d_{\text{M-X}}$	C
VCl ₂	-3.46	3.58	3.60	2.45	25.63
VBr ₂	-2.77	3.76	3.77	2.60	26.32
VI ₂	-1.93	4.04	4.06	2.80	30.86
CrCl ₂	-2.57	3.55	3.59	2.49	26.15
CrBr ₂	-2.00	3.74	3.81	2.61	24.95
CrI ₂	-1.28	3.99	4.08	2.81	22.01
MnCl ₂	-3.23	3.64	3.68	2.51	33.08
MnBr ₂	-2.65	3.80	3.82	2.66	29.77
MnI ₂	-1.83	4.06	4.16	2.86	28.73
FeCl ₂	-2.22	3.43	3.57	2.42	41.49
FeBr ₂	-1.61	3.63	3.74	2.57	39.41
FeI ₂	-0.83	3.91	4.04	2.77	37.92
CoCl ₂	-1.71	3.42	3.54	2.38	20.19
CoBr ₂	-1.15	3.62	3.68	2.53	21.74
CoI ₂	-0.67	3.80	3.96	2.62	27.14
NiCl ₂	-1.98	3.42	3.48	2.36	53.30
NiBr ₂	-1.50	3.61	3.70	2.50	49.42
NiI ₂	-0.96	3.88	3.89	2.69	46.64

energy as $E_{\text{form}} = E(\text{MX}_2) - \mu_{\text{M}} - 2\mu_{\text{X}}$. Here, μ_{M} and μ_{X} correspond to the energy per atom of the stable bulk (bcc-V, bcc-Cr, bcc-Mn, bcc-Fe, hcp-Co, fcc-Ni) and gas (Cl_2 , Br_2 , I_2) phases, respectively. We found that all calculated formation energies are negative in the range from -0.83 to -4.66 eV per M atom. These values are very close to the calculated formation energies of MoS_2 , VS_2 and WSe_2 (-2.49 , -2.79 and 1.86 eV per M atom, respectively).⁴⁸ Therefore, metal halide monolayers are energetically stable and could be potentially obtained by exfoliation.

To access the dynamical stability of single-layer dihalides, we calculated their phonon band structure using density functional perturbation theory (DFPT). The force constants were calculated for a $4 \times 4 \times 1$ supercell by using Phonopy package.⁵² Fig. S1 in the ESI† shows the phonon dispersions of all monolayers. We observe no imaginary (negative) frequencies, confirming the dynamical stability of single-layer dihalides.

We then determine the mechanical properties of halide monolayers by calculating their in-plane stiffness – the analogue of Young’s modulus for 2D materials. This can be done by applying a series of small deformations on the material and monitoring its mechanical response. Starting with the fully relaxed structure of MX_2 , its lattice constants are imposed to small strains ε_x and ε_y within the harmonic range of ± 0.02 . For each $(\varepsilon_x, \varepsilon_y)$ pair, we fully optimize the structure and calculate the strain energy E_s . In the harmonic regime, the strain energy can be fitted to a two-dimensional quadratic polynomial expressed by

$$E_s(\varepsilon_x, \varepsilon_y) = a_1 \varepsilon_x^2 + a_2 \varepsilon_y^2 + a_3 \varepsilon_x \varepsilon_y \quad (1)$$

Through fitting of the strain-energy surface, we can derive the in-plane stiffness (C) of single-layer dihalides as follows

$$C_x = \frac{4a_1a_2 - a_3^2}{2a_2A_0} \text{ and } C_y = \frac{4a_1a_2 - a_3^2}{2a_1A_0} \quad (2)$$

Here, A_0 is the equilibrium area of single-layer MX_2 in the orthorhombic cell. Table 1 summarizes the obtained results ($C = C_x = C_y$). The calculated in-plane stiffness of metal dihalides ranges from 20.19 to 53.30 N m^{-1} , which is comparable to those of germanene (48 N m^{-1}), phosphorene (30–94 N m^{-1}), arsenene (58 N m^{-1}), CrSnTe_3 (60 N m^{-1}), and MnPSe_3 (36 N m^{-1}) monolayers.^{6,53–56} The single-layer dihalides demonstrate high flexibility with their in-plane stiffness being smaller than that of TMDCs, such as MoS_2 (140 N m^{-1}) and WSe_2 (130 N m^{-1}).⁴⁸ This may be attributed to the weaker ionic bonds in dihalides as compared to covalent bonds in TMDCs.

3.2. Electronic properties

Our spin-polarized calculations demonstrate that most transition-metal (TM) dihalides possess a large magnetic moment. The total magnetic moment forms a “volcano” curve (Fig. 3a) starting with V-halides ($3 \mu_B$ per TM atom), increasing to Mn-halides ($5 \mu_B$), and then gradually decreasing to $2 \mu_B$ for Ni-halides, in good agreement with the magnetic moments of free metal atoms, described by Hund’s rules. The calculated magnetic moments in 2D dihalides are higher than those in magnetic 2D dichalcogenides (*e.g.* VS_2 , NbS_2).^{5,15,57} The majority of the total magnetic moment

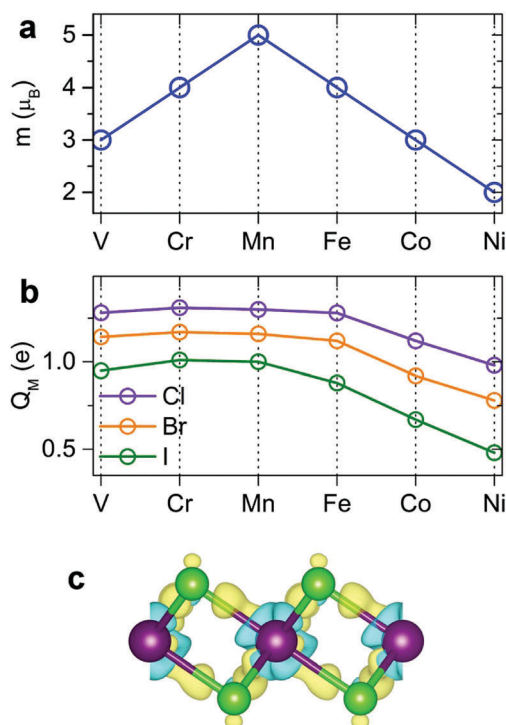


Fig. 3 Calculated magnetic and electronic properties of dihalide monolayers: (a) total magnetic moments per M atom, (b) Bader charges on M atoms, (c) charge density difference isosurface plot, showing charge accumulation and depletion (yellow and blue colors, respectively).

comes from the TM atoms, while the halogens have a small magnetic moment of only 0.16–0.40 μ_B . The detailed analysis indicates that the local magnetic moment on TM atoms increases with the atomic number of the X atom (Cl \rightarrow Br \rightarrow I). This trend is opposite to the amount of electron transfer between TM and X atoms. The Cl atom has the largest electronegativity and withdraws the most valence electron charge from TM atoms, decreasing their magnetization.

The bonding mechanism is examined by plotting the electron density distribution. The distinctive feature of 2D metal halides is a significant charge transfer. The bonding has a profound ionic character. Halogen atoms have strong affinity for acquiring an extra electron to fill its outer shell, and the Bader charge analysis shows that 0.48–0.65 e is transferred from M to each Cl, 0.39–0.58 e from M to each Br, and 0.24–0.50 e from M to each I atom (Fig. 3b). The direction of charge transfer can be rationalized by much larger electronegativity of Cl, Br and I atoms *versus* metal atoms. The amount of charge transfer decreases going as Cl \rightarrow Br \rightarrow I. The charge distribution in dihalides was visualized by calculating the charge density difference ($\Delta\rho$) plots as shown in Fig. 3c. Here, $\Delta\rho$ is obtained as the difference between the charge density of the MX_2 monolayer and the superposition of the charge densities of the constituent atoms. The blue and yellow isosurfaces represent charge depletion and accumulation regions, respectively. There is noticeable electron depletion in the region of M atoms, consistent with electron affinities and Bader analysis.

We compare the densities of states (DOSs) calculated using GGA, GGA+ U and HSE methods on the example of NiCl_2 .

The GGA spin-polarized DOS of monolayer NiCl_2 is shown in Fig. 4a. The electronic structures of different dihalides share several common features. The valence band is formed by halogen p bands, while the bottom of the conduction band mainly originates from metal s states. The TM atoms transfer their 4s electrons to halogens and have a +2 oxidation state; therefore, TM 4s states are completely unoccupied. The spin-polarized 3d states of TM atoms are located within the band gap. We can observe significant hybridization between TM 3d and halogen p orbitals. Each TM atom is surrounded by six halogen neighbors (“ligands”) which form a nearly spherical octahedral coordination. The octahedral crystal field splits the 3d orbitals of TM atoms into upper e_g ($d_{x^2-y^2}$, d_{z^2}) and lower t_{2g} (d_{xy} , d_{xz} , d_{yz}) states. The e_g orbitals point directly at the six negatively charged halogens, which increases their energy due to the electrostatic repulsion with halogens. In contrast, t_{2g} orbitals lie between the halogens, making them relatively more stable and lowering their energy. Halogens are weak ligands from the spectroscopic series; therefore, 3d TM atoms in the octahedral field are expected to prefer the high spin state. This is consistent with the large exchange splitting of the TM 3d states, as observed in Fig. 4.

The addition of on-site Coulomb repulsion (GGA+ U , Fig. 4b and c) increases the exchange splitting between filled and empty orbitals in the TM 3d manifold. Consequently, the occupied spin-up TM 3d states now move towards the valence band and hybridize more strongly with the halogen p states. The unoccupied spin-down TM 3d states shift towards the CBM. GGA+ U reduces the width of the TM 3d peak inside the

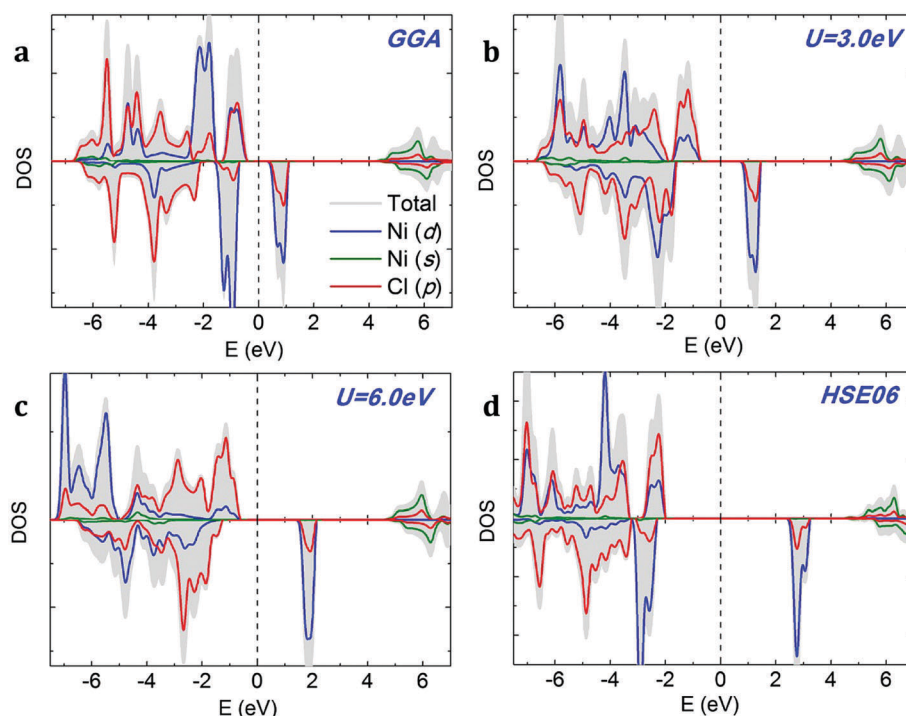


Fig. 4 Density of states (DOS) of monolayer NiCl_2 calculated using (a) GGA, (b and c) GGA+ U , and (d) HSE06 methods. The Fermi level is indicated by a dashed vertical line.



	E_{ex}	J	T_{C}^{MC}	MS	m
VCl ₂	−81.80	−3.03	—	AFM	3.0
VBr ₂	−41.25	−1.53	—	AFM	3.0
VI ₂	−14.85	−0.55	—	AFM	3.0
CrCl ₂	−63.30	−1.32	—	AFM	4.0
CrBr ₂	−32.09	−0.67	—	AFM	4.0
CrI ₂			—	AFM	4.0
MnCl ₂	−18.63	−0.25	—	AFM	5.0
MnBr ₂	−15.65	−0.21	—	AFM	5.0
MnI ₂	−15.43	−0.21	—	AFM	5.0
FeCl ₂	122.58	2.55	109	FM	4.0
FeBr ₂	90.05	1.88	81	FM	4.0
FeI ₂	47.48	0.99	42	FM	4.0
CoCl ₂	53.05	1.96	85	FM	3.0
CoBr ₂	14.35	0.53	23	FM	3.0
CoI ₂	−12.83	−0.48	—	AFM	3.0
NiCl ₂	38.55	3.21	138	FM	2.0
NiBr ₂	37.33	3.11	132	FM	2.0
NiI ₂	36.28	3.02	129	FM	2.0

Figure 2 consists of two panels, (a) and (b), showing the temperature dependence of the magnetic moment m (in units of μ_B) for different materials.

Panel (a) shows the data for FeCl_2 (purple squares), FeBr_2 (orange circles), and FeI_2 (green triangles). The x-axis is Temperature T (K) from 0 to 150, and the y-axis is m (μ_B) from 0 to 4. FeCl_2 shows a sharp drop in m around 110 K. FeBr_2 shows a sharp drop around 80 K. FeI_2 shows a sharp drop around 40 K.

Panel (b) shows the data for FeCl_2 (purple squares), strain (green diamonds), and strain+doping (magenta triangles). The x-axis is Temperature T (K) from 0 to 350, and the y-axis is m (μ_B) from 0 to 4. FeCl_2 shows a sharp drop in m around 110 K. The strain data (green diamonds) shows a sharp drop around 210 K. The strain+doping data (magenta triangles) shows a sharp drop around 280 K.

In summary, we have investigated the structural, electronic and magnetic properties of single-layer metal dihalides using first-principles calculations with the GGA, GGA+*U* and hybrid HSE06 functionals. We found that single-layer dihalides prefer the 1-T

crystal phase and are energetically stable. The magnetic properties of 2D dihalides are governed by the competition between AFM direct nearest-neighbor d-d exchange and FM superexchange *via* halogen p states, which leads to different magnetic states. Thus we found that 2D FeX_2 , NiX_2 , CoCl_2 and CoBr_2 monolayers are ferromagnetic (FM), while VX_2 , CrX_2 and MnX_2 are antiferromagnetic (AFM). Using the DFT derived spin exchange parameters, we estimated the Curie temperature of magnetic transition from the Monte Carlo simulations based on the Ising model and Heisenberg Hamiltonian. We find that single-layer dihalides exhibit comparable or even slightly higher Curie temperatures than single-layer dichalcogenides. This can be attributed to the profound ionic bonding in halides, which enhances the superexchange coupling between the magnetic metal ions *via* the halogen atoms. Overall, single-layer dihalides represent a new addition to the family of 2D materials with promising applications in nanoscale devices. We expect that our theoretical results will inspire further experimental studies.

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