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Understanding the mechanism of the chiral phosphoric acid-catalyzed aza-Cope rearrangement†

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The first catalytic enantioselective aza-Cope rearrangement was reported in 2008 by Rueping *et al.* The reaction is catalyzed by a 1,1'-bi-2-naphthol-derived (BINOL-derived) phosphoric acid and achieved high yields and enantioselectivities (up to 97 : 3 er with 75% yield). This work utilizes Density Functional Theory to understand the mechanism of the reaction and explain the origins of the enantioselectivity. An extensive conformational search was carried out to explore the different activation modes by the catalyst and, the Transition State (TS) leading to the major product was found to be 1.3 kcal mol⁻¹ lower in energy than the TS leading to the minor product. The origin of this stabilization was rationalized with NBO and NCI analysis: it was found that the major TS has a greater number of non-bonding interactions between the substrate and the catalyst, and shows stronger H-bond interactions between H atoms in the substrate and the O atoms in the phosphate group of the catalyst.

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Introduction

In 2008, Rueping *et al.*¹ reported the first catalytic enantioselective aza-Cope rearrangement² (Fig. 1), which consists in a sigmatropic rearrangement^{3–6} involving a nitrogen-containing species of which a diastereoselective version had previously been reported.⁷ This important reaction provides a valuable route for the synthesis of chiral homoallylic amines, useful intermediates in the synthesis of natural products,⁸ and other organic compounds such as β -amino acids, aminoalcohols, aminoepoxides, pyrrolidines, and piperidines.^{9–11} The reaction is catalyzed by a 1,1'-bi-2-naphthol-derived (BINOL-derived) phosphoric acid. This kind of catalyst has been utilized in enantioselective versions of a wide range of reactions,^{12,13} and has been the focus of studies of several computational works,^{14–20} including many in our group.^{21–24}

In this work, we studied the mechanism of the reaction using Density Functional Theory (DFT). An extensive conformational search was carried out to explore the different activation modes by the catalyst and the transition states (TSS) of the C–C forming step were located, different activation modes were analyzed, and the origin of the enantioselectivity was explained. NCI plots showed a greater number of non-bonding

interactions and Natural Bond Analysis showed stronger H-bond interactions, between the substrate and catalyst for the TS leading to the major product.

Computational methods

We have performed DFT calculations with Gaussian 09²⁵ using the M06-2X²⁶ functional. An ultrafine integration grid was used for all calculations. Optimizations were carried out with the 6-31G* basis set in the gas phase. Single point energies²⁷ were obtained for the optimized structures using the M06-2X functional with the polarized, triple-zeta valence quality def2-TZVPP basis set²⁸ and the SMD²⁹ solvent model. Dibutylether was used as a model solvent for MTBE, since it was previously found to give valid results.³⁰ Reported energies refer to single point energies for the model system, and to free energies for the full system (*i.e.* single point energies with thermal corrections arising from translational, rotational, vibrational and electronic motions as implemented in Gaussian 09, calculated at the M06-2X 6-31G* level).

Conformational searches were carried out with MacroModel version 12.3³¹ using the OPLS3 force field³¹ in the gas phase and a mixed torsional Monte Carlo Multiple Minimum (MCMM) and low frequency mode (LMOD) sampling. A sufficient number of steps were chosen so as to obtain each conformation at least five times. In order to minimize the number of conformations of the full catalyst, the cyclohexyl rings were fixed in the lowest energy conformation, as was pre-

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Fig. 1 Reaction conditions for the phosphoric-acid catalyzed 2-aza-Cope rearrangement. Ar: 2-Naphthyl.

viously reported.²² The H-bond between the NH in the substrate and the phosphate in the catalyst was fixed at 1.8 Å, and the breaking and forming bonds were fixed at 1.7 Å and 2.0 Å respectively, which correspond to the TS distances consistent with previous work³² and model calculations. The Paton group have investigated sampling ion-pairs with explicitly solvated MD simulations to great effect.³³ We opted for constrained conformational sampling to enable us to proceed straight to TS optimization in Gaussian.

Results and discussion

A chiral phosphoric-acid catalyzed 2-aza-Cope rearrangement reaction has recently been reported.¹ The reaction has been tested with a variety of aldehydes (11 substrates) and amine **3a**. The largest er was observed with aldehyde **2j** leading to product **4j**, in the presence of 10% catalyst **1h**. The reaction was also evaluated in different solvents with substrate **2a**, leading to product **4a**, and the highest er was obtained in toluene (87.5 : 12.5 er) and methyl *tert*-butyl ether (MTBE, 91 : 9 er) (Table 1).

The proposed mechanism of the 2-aza-Cope rearrangement (Fig. 2) starts with the formation of an imine by reaction between the starting amine and the aldehyde. The Brønsted-

acid catalyzed rearrangement proceeds *via* a six-membered transition state, activated by the formation of an H-bond between the intermediate imine and the catalyst, in which a new C–C bond is formed with the terminal alkene acting as the nucleophile and the imine as the electrophile, generating a new tetrahedral carbon center. The newly formed product then loses the association with the phosphoric acid, regenerating the catalyst.

In this work, the origin of the enantioselectivity in the **A** to **B** rearrangement step was studied using DFT. First, different activation modes of the transition state were located through a comprehensive conformational search followed by optimization, by using butadiene phosphoric acid as a model catalyst and a phenyl substituent as R' (Fig. 3). Only TS structures with a chair conformation of the six membered ring, and with the bulky R' group in equatorial position were considered, as both literature and our calculations showed that conformations in boat conformation or with the R' group in axial position were too high in energy.³⁴ 73 such conformations were located, in which different H-bond patterns are observed between the H atoms of the reacting substrate and the O atoms of the catalyst. The numbering of atoms is shown in Fig. 3. H-bonds were considered to be formed if the O–H distance was below 2.6 Å. The simplest activation pattern **TS-I** is observed by the formation of a single H-bond between the N–H atom and the negatively charged O atom, with a 1.52 Å distance (Fig. 4). However, this conformation was found to be 7.8 kcal mol⁻¹ higher in energy than the lowest energy conformation, therefore a substantial extra stabilization is observed by the formation of additional H-bonds. The lowest energy conformation **TS-A** shows four H-bonds, one between N–H and O1, two H-bonds between both H2 and H3 and O2, and a further H-bond between H2

Table 1 Selected reaction conditions

Entry	Aldehyde	Product	Solvent	Yield	er
1	2a	4a	Toluene	n/a	87.5 : 12.5
2	2a	4a	MTBE	77%	91 : 9
3	2j	4j	MTBE	75%	97 : 3





Fig. 2 Mechanism of the phosphoric acid catalyzed 2-aza-Cope rearrangement.



Fig. 3 Model catalyst and substrate to study the different activation modes in the TS.

and the bridging O3. All other activation modes show either three or four total H-bonds, with the highest energy conformation **TS-H** being 3.1 kcal mol⁻¹ above **TS-A**.

Once the different activation modes were investigated, a conformational search and optimization was carried out for the full catalyst **1h** and the transition state leading to product **4j**. 31 structures were located for the TS leading to the major product, and 32 for the TS leading to the minor product. The lowest energy TS structures leading to the major product (**TS-1-major**) and the minor product (**TS-1-minor**) are shown in Fig. 5 and 6. **TS-1-major** was found to be 1.21 kcal mol⁻¹ and 1.26 kcal mol⁻¹ lower in energy in toluene and dibutylether (as a model for MTBE) respectively than **TS-1-minor**.

An analysis of the activation modes observed for the major and minor TSs, in comparison with those observed for the model catalyst, can bring important conclusions. Firstly, all activation modes for the full catalyst show three or four

H-bonds between the phosphate and the C-H or N-H atoms. Activation mode **TS-I**, which showed only one H-bond, was not observed in the full catalyst system. However, as this conformation was found to be 7.8 kcal mol⁻¹ higher in energy, it is not expected to be significant in the full system. Given the higher steric hindrance of the full catalyst, and extra bromine atoms in the substrate, the relative order of the different activation modes changes. For instance, activation mode **TS-B** in the model catalyst ($\Delta\Delta E^\ddagger$ of 0.6 kcal mol⁻¹), which shows three simultaneous H-bonds between the O atom from the phosphate and the three H atoms from the substrate, was found to be much higher in energy in the full catalyst system: **TS-5-major** ($\Delta\Delta G^\ddagger$ of 3.79 kcal mol⁻¹) and **TS-6-minor** ($\Delta\Delta G^\ddagger$ of 2.77 kcal mol⁻¹).

To further investigate the mechanism of the enantiodetermining step, the structures of intermediates **A** and **B** were optimized. The energy profile of this step is shown in Fig. S1,† alongside the structures of the optimized intermediates. The obtained activation barrier of 21.9 kcal mol⁻¹ is compatible with the experimental results and reaction conditions of this reaction and it is consistent with other related phosphoric-acid catalyzed transformations.^{35–40}

In order to account for the difference in stabilization energy of **TS-1-major** vs. **TS-1-minor**, analyses of the intermolecular interactions between the substrate and the catalyst were carried out using the Non-Covalent Interactions (NCI) index method. Default parameters were used for the calculations and plots. **TS-1-major** (Fig. 7) shows a strong attractive interaction between the N-H group in the substrate and an O atom from the phosphate in the catalyst (shown in blue). Then, it





Fig. 4 Activation modes obtained for the model system consisting of a butadiene catalyst, diphenyl-substituted amine and benzaldehyde. Optimized with M06-2X 6-31G*, with single point M06-2X def2-TZVPP in toluene (SMD). Hydrogen bonds between the substrate and the catalyst below 2.6 Å are shown as dashed lines and distances in Å.

shows a number of weak attractive interactions (shown in green): (i) aliphatic interactions between the six membered ring in the substrate and the aromatic ring in one of the naphthyl groups in the catalyst, (ii) a halogen – aromatic interaction between one of the bromines in the substrate and the other naphthyl group in the catalyst, (iii) C–H aromatic interactions between one of the phenyl groups of the substrate and one of the naphthyl groups of the catalyst, (iv) C–H aromatic interactions between the other phenyl group from the substrate and one of the [H8]-ring from the catalyst, and (v) C–H...O interactions between one of the phenyl groups and

the bromine substituted aromatic ring in the substrate with the phosphate in the catalyst. The corresponding NCI plot for **TS-1-minor** (Fig. 7) also shows a strong interaction between the N–H group and the O from the phosphate and a number of weaker interactions: (i) a halogen aromatic interaction between one bromine atom from the substrate and one [H8]-rings from the catalyst, (ii) aliphatic interactions between the six member ring from the substrate and a naphthyl ring from the catalyst, and (iii) C–H...O interactions between one of the phenyl groups and the bromine substituted aromatic ring in the substrate with the phosphate in the catalyst. A comparison





Fig. 5 TS structures leading to the major product, optimized with M06-2X 6-31G*, single point with M06-2X def2-TZVPP in dibutylether (SMD), and thermal corrections with M06-2X 6-31G*. Hydrogen bonding interactions are shown as dashed lines and distances in Å.

between **TS-1-major** and **TS-1-minor** shows that the latter has a fewer number of interactions, since it does not show phenyl aromatic interactions. This is consistent with the greater stabilization energy present in **TS-1-major**.

The intermolecular interactions were further investigated using a Natural Bond Order (NBO) analysis of the second order perturbation energies. The greatest interaction was found between the H atoms in the reacting six membered ring in the substrate and the O atoms in the phosphate group in the catalyst. In total, the H bonds account for a stabilization of $36.8 \text{ kcal mol}^{-1}$ in **TS-1-major** and $34.4 \text{ kcal mol}^{-1}$ in **TS-1-minor**. The largest interactions are shown in Fig. 8. **TS-1-major** shows an interaction of $10.32 \text{ kcal mol}^{-1}$ between an empty N-H σ^* orbital and a partially-filled P-O1 σ^* orbital, an interaction of $3.88 \text{ kcal mol}^{-1}$ between an empty C-H3 σ^* orbital and a filled O3 lone pair n , and an interaction of

$2.34 \text{ kcal mol}^{-1}$ between an empty C-H2 σ^* orbital and a partially-filled PO1 σ^* orbital. **TS-1-minor** shows an interaction of $9.98 \text{ kcal mol}^{-1}$ between an empty N-H1 σ^* orbital and a partially-filled PO1 σ^* orbital, and interaction of $1.76 \text{ kcal mol}^{-1}$ between an empty C-H3 σ^* orbital and a filled O3 lone pair n , and an interaction of $1.53 \text{ kcal mol}^{-1}$ between an empty C-H2 σ^* orbital and a filled O2 lone pair. These interaction energies are consistent with the activation modes observed for these TS structures and provide a rationale for the greater stabilization of **TS-1-major** vs. **TS-1-minor**. These greater H bond energies, together with the greater intermolecular interactions observed using the NCI plot between the phenyl groups in the substrate and the aromatic rings in the catalyst, account for the origins of enantioselectivity of the reaction.

Finally, we have studied the distortion⁴¹⁻⁴³ of the catalyst and substrate upon the formation of the transition states, a



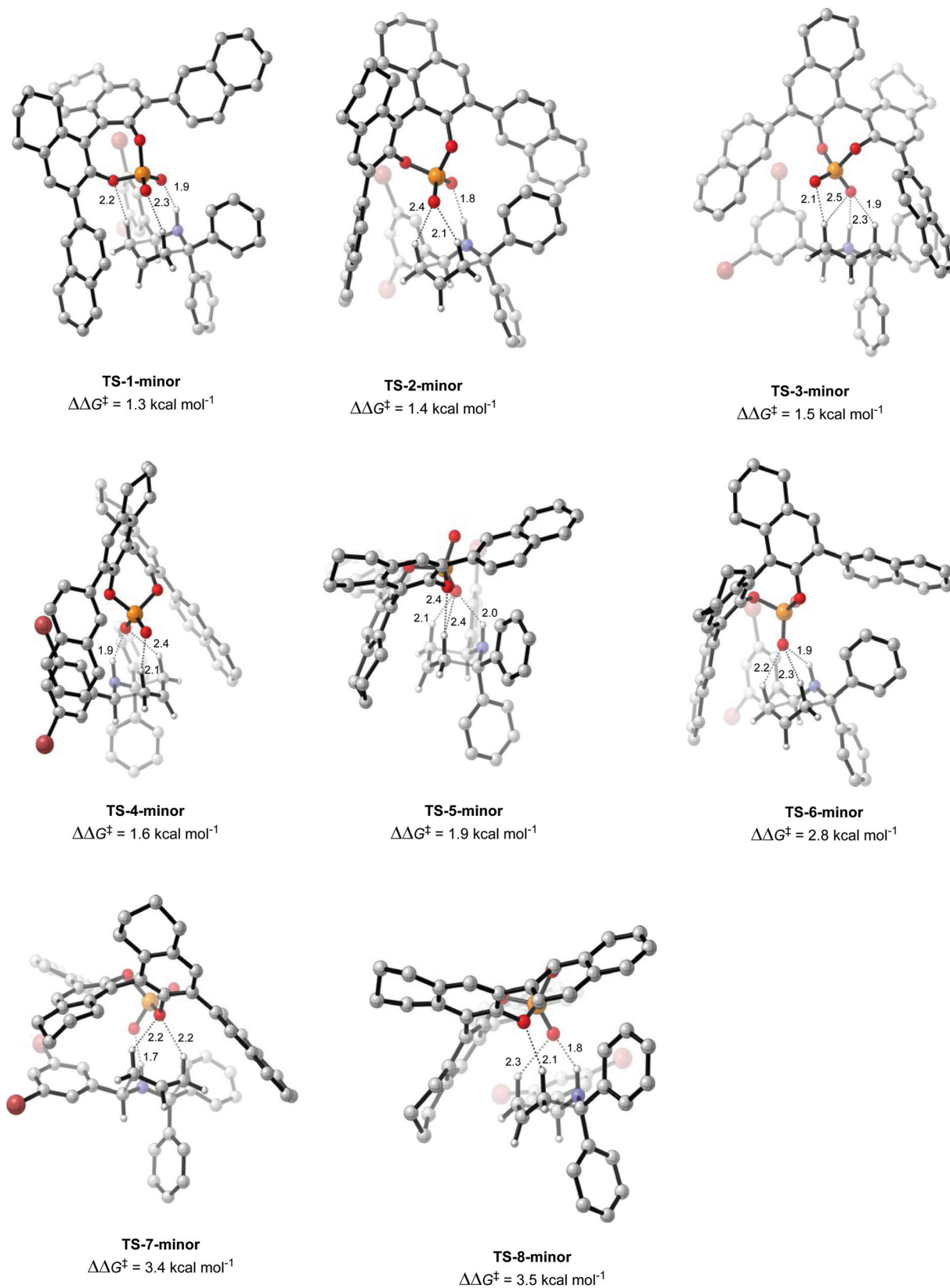


Fig. 6 TS structures leading to the minor product, optimized with M06-2X 6-31G*, single point with M06-2X def2-TZVPP in dibutylether (SMD), and thermal corrections with M06-2X 6-31G*.



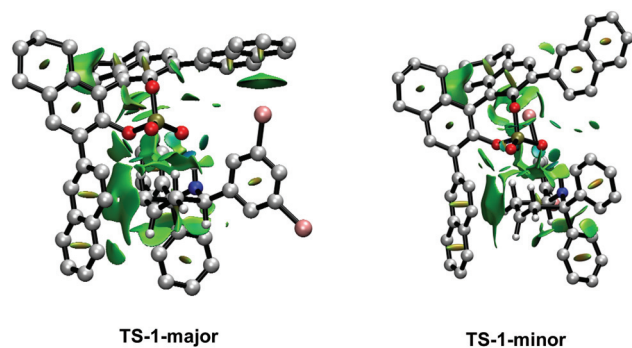


Fig. 7 NCI plots showing intermolecular interactions between the substrate and catalyst. Strong attractive interactions shown in blue, and weak attractive interactions shown in green. Obtained with M06-2X def2-TZVPP in the gas phase.

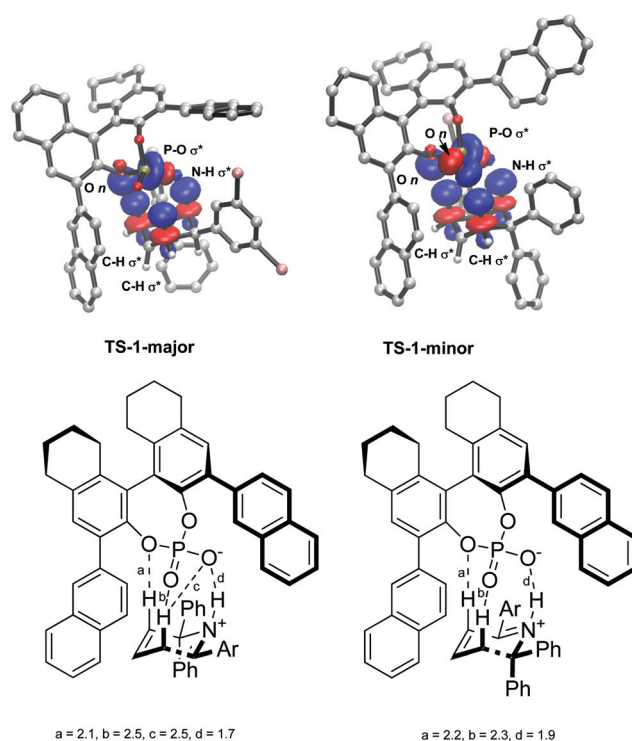


Fig. 8 NBO analysis of hydrogen bonding interactions between the substrate and the catalyst. Obtained with M06-2X def2-TZVPP in the gas phase. H-Bond distances *a*, *b*, *c* and *d* shown in Å.

process that has been reported as being fundamental to some related reactions, such as chiral phosphoric-acid catalyzed oxetane desymmetrizations⁴⁴ and ring-openings of *meso*-aziridinium and episulfonium cations.³³ We have calculated the single point energy of the catalyst and substrate in the **TS-1-major** and **TS-1-minor** conformations using M06-2X def2-TZVPP in dibutylether (SMD). The substrate conformation in **TS-1-major** is in fact 0.26 kcal mol⁻¹ higher than in **TS-1-minor**, and the catalyst conformation is 0.88 kcal mol⁻¹ higher, accounting for a total distortion energy of 1.15 kcal

mol⁻¹, so in fact the conformation of the constituents leading to **TS-1-major** are disfavored over **TS-1-minor**. These results highlight the significance of the intermolecular interactions described above, which account for the origin in the stabilization of **TS-1-major** over **TS-1-minor**, consistent with the experimental results.

Conclusions

In conclusion, DFT calculations were carried out on the chiral phosphoric-acid catalyzed 2-aza-Cope rearrangement reaction. Different activation modes of the C–C bond forming step model TS were located, and **TS-A** was found to be lowest in energy. It shows four H-bonds, one between N–H and a phosphate O atom, and three C–H...O bonds between the substrate and the phosphate group in the catalyst. Then, the origin of the enantioselectivity was evaluated by locating the TSs for the full catalyst **1h** and substrate leading to product **4j**. The lowest energy conformations were found to be **TS-1-major** and **TS-1-minor**. The full energy reaction profile was investigated and the obtained reaction barrier of 21.9 kcal mol⁻¹ is consistent with the experimental results. NCI and NBO analyses were performed in order to rationalize the difference in stabilization energy between **TS-1-major** and **TS-1-minor**. The NCI plot showed that **TS-1-minor** has a lower number of interactions and it does not show interactions between the phenyl groups in the substrate and the aromatic rings in the catalyst. The NBO analysis showed stronger H-bond interactions between the H atoms in the substrate and the O atoms in the phosphate group from the catalyst. Finally, the distortion of the catalyst and substrate upon TS formation was explored but was not found to account for the stabilization of the preferred reaction pathway. These results provide valuable insights into the mechanism of the reaction and the different stabilization modes in the TS and can be used for the design of more effective catalysts for this and related reactions.

Conflicts of interest

There are no conflicts to declare.

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