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# A MoS<sub>2</sub>@SnS heterostructure for sodium-ion storage with enhanced kinetics†

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Layered metal sulphides are promising anode materials for sodium-ion batteries (SIBs) and capacitors owing to their distinctive crystal structures and large interlayer spacings, which are suitable for Na<sup>+</sup> insertion/extraction. However, low electronic conductivity, sluggish ion transfer and large volume variation of metal sulphides during sodiation/desodiation processes have hindered their practical application. In this work, we report the construction of a walnut-like core-shell MoS<sub>2</sub>@SnS heterostructure composite as an anode for SIBs with high capacity, remarkable rate and superior cycling stability. Experimental observations and first-principles density functional theory (DFT) calculations reveal that the enhanced electrochemical performances can be mainly ascribed to the boosted charge transfer and ion diffusion capabilities at the heterostructure interface driven by a self-building internal electric field. Our findings herein may pave the way for the development of novel heterostructure composite materials for beyond lithium-ion batteries and capacitors.

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## Introduction

Lithium-ion batteries (LIBs) with high energy and power densities have dominated the portable electronic device market and been targeted for (hybrid) electric vehicles, smart grids and storage of electricity from renewables.<sup>1</sup>

However, the limited resource of lithium in the Earth's crust has triggered intensive research on either novel electrode materials<sup>2</sup> or various beyond-LIBs.<sup>3</sup> In particular, sodium-ion batteries (SIBs) are regarded as a potential alternative energy storage device to replace or supplement LIBs owing to sodium's natural abundance and environmental friendliness.<sup>4,5</sup> SIBs have physiochemical properties (e.g., intercalation behaviour) similar to LIBs, but traditional electrode

materials for commercial LIBs cannot be simply transplanted into SIBs mainly owing to the larger ionic radius of Na<sup>+</sup> (1.02 Å) than that of Li<sup>+</sup> (0.69 Å), causing sluggish Na<sup>+</sup> diffusion, large volume variation and severe pulverization.<sup>6,7</sup> For instance, a graphite anode for LIBs is unable to accommodate a large portion of Na<sup>+</sup> because sodium can hardly form staged intercalation compounds with graphite. Therefore, developing suitable electrode materials for SIBs with high capacity, good rate and superior cycling stability to meet the increasing demands of practical applications is urgently desired.<sup>8</sup>

Recently, considerable effort has been devoted to searching for suitable anode materials for SIBs, including carbonaceous materials,<sup>9</sup> metals and alloys,<sup>10</sup> metal oxides/sulphides and so on.<sup>11–13</sup>

In particular, layered metal sulphides have attracted much attention due to the S–M–S sandwich-like structures bonded by weak van der Waals forces, which are beneficial for Na<sup>+</sup> diffusion with reversible intercalation/extraction.<sup>14–16</sup> For example, MoS<sub>2</sub> has been investigated as an anode for SIBs because of its large interlayer spacing (0.62 nm) to host Na<sup>+</sup> without a large volume variation.<sup>17–19</sup> However, the practical application of MoS<sub>2</sub> materials is limited by their poor intrinsic conductivity, low coulombic efficiency (CE), inferior cycling stability, and poor rate capability. Many efforts have been made to circumvent these issues through designing various nanostructured MoS<sub>2</sub> and combining with carbonaceous materials.<sup>18,20–22</sup> Besides, SnS is another promising anode material for SIBs because of its relatively weaker Sn–S bond

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resulting in higher initial CE and better reversibility.<sup>23–26</sup> But the serious volume variation in the sodiation/desodiation process leads to aggregation and pulverization of the SnS electrode, giving rise to quick capacity decay.<sup>27,28</sup>

Recently, a heterostructure electrode formed by coupling two dissimilar semiconductors that can enhance interface reaction kinetics and facilitate charge transfer between different components driven by the internal electrical field at the heterointerfaces has been studied.<sup>29–33</sup> Gong *et al.* demonstrated that a p-Co<sub>3</sub>O<sub>4</sub>/n-BiVO<sub>4</sub> heterojunction enhanced surface reaction kinetics and charge separation of BiVO<sub>4</sub> photoanodes.<sup>34</sup> Guo *et al.* reported a SnS/SnO<sub>2</sub> heterostructure as an anode for SIBs with superior electrochemical performance, displaying greater charge transfer capability and lower ion diffusion resistance.<sup>35</sup> Wang *et al.* proposed that the interface synergistic effect from layered metal sulphides of a MoS<sub>2</sub>/SnS<sub>2</sub> van der Waals heterojunction can induce more layer spaces for lithium-ion storage.<sup>36</sup>

Therefore, rational design and controlled synthesis of novel heterostructure electrodes with distinct morphologies, structures and compositions can considerably improve their electrochemical performances for various energy storage devices, which remains challenging. Herein, we reported a unique architecture of SnS nanocrystals decorated on MoS<sub>2</sub> nanospheres to form a hierarchical walnut-like MoS<sub>2</sub>@SnS core-shell heterostructure. Such a composite has several structural merits when used as an anode for SIBs: (1) the formation of the MoS<sub>2</sub>@SnS heterostructure promoted the electron/Na<sup>+</sup> transfer/separation at the interface with enhanced redox kinetics; (2) the spherical particles with high mobility facilitated electrode fabrication; (3) a small amount of carbon was incorporated into the composite, which improved the electrical transport and better buffered the structural variation during sodiation/desodiation. Electrochemical tests revealed that the resulting composites delivered excellent electrochemical performances with a high reversible capacity of ~697 mA h g<sup>-1</sup> at 0.1 A g<sup>-1</sup>, remarkable rate capability and superior cyclability derived from their unique structural features, thus confirming the potential of hierarchical walnut-like MoS<sub>2</sub>@SnS core-shell heterostructures as high-performance anode materials for SIBs. The strategy proposed in this work can potentially be extended to the design and interface engineering of a wide array of core-shell heterostructure electrodes for SIBs.

## Results and discussion

The MoS<sub>2</sub>@SnS core/shell heterostructure was synthesized by step-by-step hydrothermal reaction procedures as schematically illustrated in Fig. 1. First, MoG solid spheres were fabricated through a hydrothermal method, followed by conversion into MoS<sub>2</sub> *via* reaction with Na<sub>2</sub>S. Next, SnS nanocrystals were deposited on the MoS<sub>2</sub> surface with the assistance of PVP as a capping agent,<sup>37</sup> forming a walnut-like core-shell MoS<sub>2</sub>@SnS heterostructure. The as-obtained composite was further annealed under a N<sub>2</sub> atmosphere to improve the crystallinity.

The crystal structure of the MoS<sub>2</sub>@SnS heterostructure was characterized by X-ray diffraction (XRD) as shown in Fig. 2a. The observed diffraction peaks can be readily indexed to orthorhombic SnS (JCPDS 65-3812; *Pnma* (62), *a* = 11.200 Å, *b* = 3.990 Å, *c* = 4.340 Å) and hexagonal MoS<sub>2</sub> (JCPDS 24-0513; *P6<sub>3</sub>/mm2* (187), *a* = 3.166 Å, *b* = 3.166 Å, *c* = 12.290 Å). The slightly weak intensity of the peaks of MoS<sub>2</sub> relative to that of SnS can be ascribed to the coating of SnS on MoS<sub>2</sub>. No additional peaks can be observed in the XRD pattern, suggesting high purity of the as-prepared MoS<sub>2</sub>@SnS heterostructure. For comparison, the XRD patterns of the as-synthesized pure MoS<sub>2</sub> and SnS (Fig. S1, ESI†) are in good accordance with those of the standard patterns of MoS<sub>2</sub> (JCPDS: 09-0312) and SnS (JCPDS: 65-3812), respectively. Next, the specific surface area and pore size distribution of MoS<sub>2</sub>@SnS were determined by N<sub>2</sub> adsorption-desorption analysis. As shown in Fig. 2b, the composite yields a Brunauer-Emmett-Teller (BET) surface area of 43.7 m<sup>2</sup> g<sup>-1</sup> and a pore size distribution mainly ranging from ~2 to ~6 nm (inset), which is beneficial for improving sodium-ion storage performance owing to a large contact area between the electrolyte and electrode. Next, the molar ratio of MoS<sub>2</sub> to SnS in the MoS<sub>2</sub>@SnS heterostructure was determined to be *ca.* 0.91 as measured by inductively coupled plasma-optical emission spectrometry (ICP-OES).

X-ray photoelectron spectroscopy (XPS) measurements (Fig. 3) were performed to further investigate the chemical composition and surface electronic states of the MoS<sub>2</sub>@SnS heterostructures. The full XPS survey scan spectrum (Fig. S2, ESI†) verifies the presence of Sn, O, N, C, Mo, and S elements in the composite sample. The existence of N and C elements can be ascribed to the carbonization of trace PVP residue during heat treatment process. The carbon shell creates abundant extrinsic defects, which can improve the overall conductivity and enhance electrochemical performance of the MoS<sub>2</sub>@SnS heterostructure. The existence of O can be attributed to the adsorbed oxygen species on the sample surface. The high-resolution XPS spectrum of Mo 3d (Fig. 3a) shows four peaks located at ~231.3, ~228.0, ~234.9 and ~225.2 eV. The former two peaks correspond to Mo 3d<sub>3/2</sub> and Mo 3d<sub>5/2</sub> of Mo<sup>4+</sup> in MoS<sub>2</sub>. The small peak at ~234.9 eV is ascribed to the presence of a small amount of Mo<sup>6+</sup> of MoO<sub>3</sub> due to surface oxidation.<sup>38</sup> The peak at ~225.2 eV originates from the S 2s component in the MoS<sub>2</sub>@SnS composites. The high-resolution XPS spectrum of the Sn 3d core level (Fig. 3b) displays two main peaks at ~494.3 and ~485.9 eV corresponding to Sn 3d<sub>3/2</sub> and Sn 3d<sub>5/2</sub> of Sn<sup>2+</sup> in SnS, respectively.<sup>27</sup> The high-resolution S 2p spectrum (Fig. 3c) can be deconvoluted into two peaks at ~161.9 and ~160.7 eV, which can be assigned to S 2p<sub>1/2</sub> and S 2p<sub>3/2</sub> of S<sup>2-</sup> in MoS<sub>2</sub>@SnS, respectively.<sup>39</sup> The high-resolution N 1s spectrum (Fig. 3d) suggests the presence of pyridinic N (398.5 eV) and pyrrolic N (400.2 eV) components in the MoS<sub>2</sub>@SnS heterostructure.

The structure and morphology of the MoS<sub>2</sub>@SnS heterostructure were characterized by scanning electron microscopy (SEM), transmission electron microscopy (TEM), and high-resolution TEM (HRTEM). The SEM image (Fig. 4a) shows that



Fig. 1 Schematic illustration of the synthesis of  $\text{MoS}_2@\text{SnS}$  heterostructure.

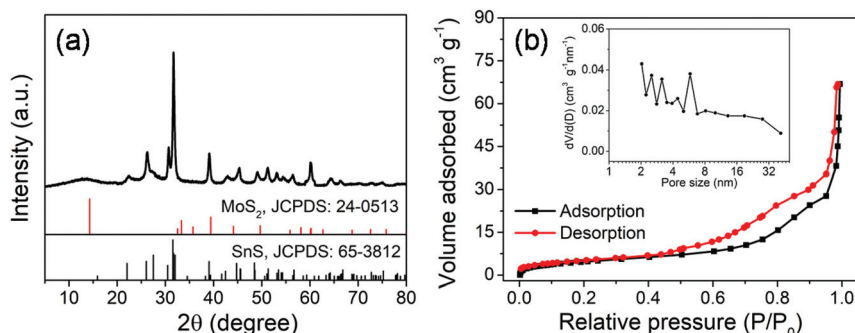


Fig. 2 (a) XRD pattern and (b)  $\text{N}_2$  adsorption/desorption isotherms and pore size distribution curve (inset) of the  $\text{MoS}_2@\text{SnS}$  heterostructure.



Fig. 3 High-resolution XPS spectra of the  $\text{MoS}_2@\text{SnS}$  heterostructure. (a) Mo 3d; (b) Sn 3d; (c) S 2p; and (d) N 1s spectra.

the as-prepared MoG nanospheres have a diameter of  $\sim 700$  nm and a smooth surface. After the sulfuration process, the  $\text{MoS}_2$  nanospheres possess similar particle shapes but a rough surface (Fig. S3a†). The SEM images (Fig. 4b and c) of the  $\text{MoS}_2@\text{SnS}$  heterostructure reveal the formation of a walnut-like heterostructure after decoration of SnS nanocrystals on  $\text{MoS}_2$  nanospheres during the hydrothermal process. The coating of SnS nanocrystals not only increases the contact area between the active materials and electrolyte but also

buffers the volume variation to maintain the electrode integrity during charge/discharge. The TEM micrograph in Fig. 4d further discloses that the  $\text{MoS}_2@\text{SnS}$  heterostructure has a diameter of  $\sim 800$  nm and a shell thickness of  $\sim 50$  nm. Fig. 4e and its inset show the HRTEM image of the edge of an individual  $\text{MoS}_2@\text{SnS}$  nanosphere and the corresponding fast Fourier transform (FFT) pattern. In Fig. 4e, an ultrathin amorphous carbon layer can be observed as indicated by the white arrow at the margin of  $\text{MoS}_2@\text{SnS}$ , which is consistent with the XPS

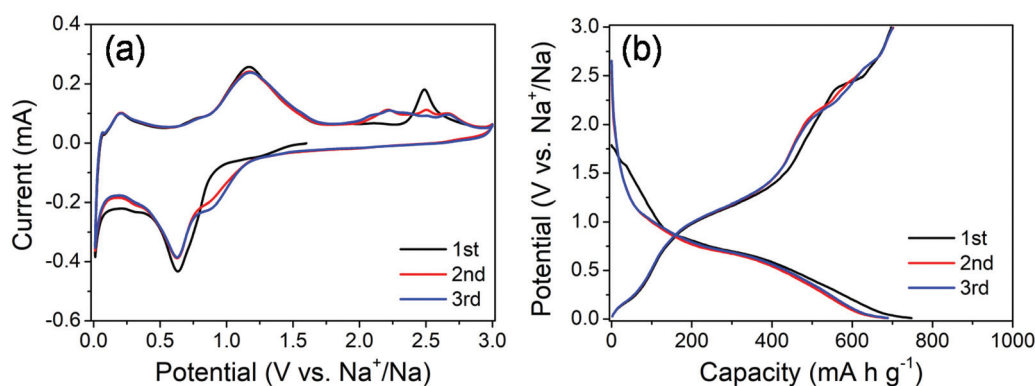


**Fig. 4** (a) SEM image of the MoG nanospheres; (b and c) SEM images of the  $\text{MoS}_2\text{@SnS}$  heterostructures with different magnifications; (d) TEM image of the  $\text{MoS}_2\text{@SnS}$  heterostructures; (e) HRTEM image of the  $\text{MoS}_2\text{@SnS}$  heterostructures with the corresponding fast Fourier transform (FFT) pattern (inset); EDS elemental mapping of (f) Sn, (g) Mo, (h) S and (i) N elements in the  $\text{MoS}_2\text{@SnS}$  composite.

result. The interplanar distance of 0.32 nm is in good agreement with the  $d$ -spacing of the (210) plane of orthorhombic SnS. The results confirmed the decoration of SnS nanocrystals on  $\text{MoS}_2$  nanospheres, leading to the formation of a hierarchical core-shell heterostructure. In contrast, the pure SnS sample is composed of nanosheet-constructed microflowers (Fig. S3b†). The energy-dispersive X-ray spectroscopy (EDS) mapping analysis of a single  $\text{MoS}_2\text{@SnS}$  sphere shown in Fig. 4f–i further demonstrates the uniform distribution of Sn, Mo, S and N elements in the  $\text{MoS}_2\text{@SnS}$  composite. The EDS mapping result suggests that the uniform coating of SnS on  $\text{MoS}_2$  helps to form a heterostructure.<sup>40</sup>

The electrochemical properties of the  $\text{MoS}_2\text{@SnS}$  heterostructure were evaluated by cyclic voltammetry (CV) and galvanostatic charge/discharge tests. The CV curves of the  $\text{MoS}_2\text{@SnS}$  electrode for the first three cycles at a scan rate of  $0.1 \text{ mV s}^{-1}$  in the potential range of 0.01–3 V (vs.  $\text{Na}^+/\text{Na}$ ) are

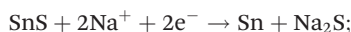
shown in Fig. 5a. During the initial cathodic scanning process, a shoulder at ca. 0.9–1.2 V corresponds to the conversion reaction of SnS to Sn and  $\text{Na}_2\text{S}$ <sup>24,26</sup> as well as intercalation of Na into the  $\text{MoS}_2$  interlayer.<sup>41</sup> The peak centered at  $\sim 0.63$  V can be ascribed to the alloying reaction of Sn and Na and conversion of  $\text{MoS}_2$  into Mo and  $\text{Na}_2\text{S}$  as well as the formation of a solid electrolyte interface (SEI) film.<sup>42</sup> Another peak appearing at  $\sim 0.03$  V suggests a multistep alloying reaction process of  $\text{Na}_x\text{Sn}$  and Na-ion storage at the Mo/ $\text{Na}_2\text{S}$  interface.<sup>43</sup> The formation of  $\text{Na}_x\text{Sn}$  alloys can effectively relieve the huge volume change during the multistep alloying reactions and thus improve the cycling stability. During charge, the peak at 0.2 V corresponds to the dealloying reaction of  $\text{Na}_x\text{Sn}$  into Na and Sn. Another peak centered at  $\sim 1.16$  V indicates the reverse conversion of Sn and  $\text{Na}_2\text{S}$  into SnS, while the peak at  $\sim 2.48$  V (which shifts to  $\sim 2.2$  V and becomes broad in the 2nd/3rd cycle) is caused by the reverse conversion of Mo and  $\text{Na}_2\text{S}$  into



**Fig. 5** (a) CV curves of the  $\text{MoS}_2\text{@SnS}$  heterostructure at a scan rate of  $0.1 \text{ mV s}^{-1}$  and (b) galvanostatic charge/discharge profiles of the  $\text{MoS}_2\text{@SnS}$  heterostructure at a current density of  $0.1 \text{ A g}^{-1}$ .



the MoS<sub>2</sub> phase.<sup>44</sup> The potential-dependent redox reactions involved in the whole charge/discharge processes can be summarized as follows:



The CV curves almost overlap in the subsequent cycles, indicating the formation of a stable SEI layer and high reversibility of electrochemical reactions in the MoS<sub>2</sub>@SnS electrode.

The galvanostatic charge/discharge profiles of MoS<sub>2</sub>@SnS at a current density of 0.1 A g<sup>-1</sup> for the first three cycles are shown in Fig. 5b. The MoS<sub>2</sub>@SnS heterostructure delivers an initial discharge capacity of ~747 mA h g<sup>-1</sup> and a charge capacity of ~697 mA h g<sup>-1</sup>, with a high initial coulombic efficiency (CE) of ~93.3%. Such a high CE could be ascribed to the formation of a uniform and stable SEI layer at the surface of SnS, resulting from the strong interface synergistic effect of the MoS<sub>2</sub> and SnS heterointerface for improved electrochemical activity.<sup>36</sup> From the second cycle, the discharge and charge curves overlap well and no obvious capacity loss can be observed, revealing the good capacity retention and cyclability of the MoS<sub>2</sub>@SnS electrode.

The rate capability of the SnS microflowers, MoS<sub>2</sub> nanospheres, and MoS<sub>2</sub>@SnS heterostructure is shown in Fig. 6a. The MoS<sub>2</sub>@SnS heterostructure electrode exhibits a high capacity of ~662 mA h g<sup>-1</sup> at 0.1 A g<sup>-1</sup>. As the current densities increase to 0.2, 0.5, 1.0 and 2.0 A g<sup>-1</sup>, the MoS<sub>2</sub>@SnS electrode can maintain reversible capacities of ~614, 600, 596 and ~586 mA h g<sup>-1</sup>, respectively. Even when the cycling current density increases to 5 A g<sup>-1</sup>, the MoS<sub>2</sub>@SnS electrode can still maintain a reversible capacity of ~556 mA h g<sup>-1</sup>. After switching the current density back to 0.2 A g<sup>-1</sup>, the MoS<sub>2</sub>@SnS electrode can maintain a reversible capacity of ~654 mA h g<sup>-1</sup>

again, indicating its good capacity reversibility, which makes it suitable as an anode material for SIBs. In comparison, the pure MoS<sub>2</sub> nanosphere electrode exhibits an inferior sodium-ion storage property with capacities of ~476, ~418, ~359, ~317, ~260, and ~160 mA h g<sup>-1</sup> at 0.1, 0.2, 0.5, 1.0, 2.0, and 5.0 A g<sup>-1</sup>, respectively. The SnS microflower electrode manifests an even lower rate capability under the same test conditions. The remarkable rate capability of the MoS<sub>2</sub>@SnS heterostructure can originate from the synergetic enhancement of electronic conductivity and sodium-ion transport kinetics, benefiting from the internal electric field at the heterointerfaces.<sup>34</sup> The long-term cycling stability of the SnS microflowers, MoS<sub>2</sub> nanospheres and MoS<sub>2</sub>@SnS heterostructures was further evaluated at 1.0 A g<sup>-1</sup> as shown in Fig. 6b. The MoS<sub>2</sub>@SnS heterostructure displays a high and stable reversible capacity of ~566 mA h g<sup>-1</sup> after 500 cycles, implying excellent cycling stability. In contrast, the MoS<sub>2</sub> nanospheres deliver a reversible capacity of ~295 mA h g<sup>-1</sup> after 500 cycles. Meanwhile, the SnS microflowers show a lower reversible capacity of ~198 mA h g<sup>-1</sup> after 300 cycles. These results further demonstrate the high sodium-ion storage capability and superior cycling stability of MoS<sub>2</sub>@SnS heterostructure anode materials for SIBs. To clarify the relationship between the architecture and electrochemical performance, the morphology of the MoS<sub>2</sub>@SnS heterostructures upon cycling was examined. The SEM images of the MoS<sub>2</sub>@SnS heterostructure after testing at 1 A g<sup>-1</sup> for 100 cycles are shown in Fig. S4†. It can be seen that the original morphology of the MoS<sub>2</sub>@SnS heterostructure has been well preserved during the cycling process. Table S1† compares the sodium-ion storage properties of the MoS<sub>2</sub>@SnS heterostructure electrode with some transition-metal sulphides reported in the recent literature, demonstrating its better electrochemical performance.

The electrode reaction kinetics were studied *via* electrochemical impedance spectroscopy (EIS) before cycling. The Nyquist plots are composed of a depressed semicircle in the high-to-medium frequency region and an inclined line in the low frequency region (Fig. S5†). The depressed semicircle in



Fig. 6 (a) Rate capability and (b) cycling stability of the SnS microflowers, MoS<sub>2</sub> nanospheres and MoS<sub>2</sub>@SnS heterostructures at the indicated densities.

the high-to-medium frequency region of the Nyquist plots corresponds to the SEI layer impedance ( $R_{\text{SEI}}$ ) and charge transfer impedance ( $R_{\text{ct}}$ ) between the electrode/electrolyte interface, and the sloping line at low frequency is related to  $\text{Na}^+$  diffusion in the solid phase.<sup>45,46</sup> From the Nyquist plots, the  $\text{MoS}_2@\text{SnS}$  heterostructure displays a smaller semicircle diameter, suggesting improved electrolyte/electrode interfacial characteristics after the formation of the  $\text{MoS}_2@\text{SnS}$  core/shell heterojunction. The calculated interfacial impedances ( $R_{\text{int}} = R_{\text{SEI}} + R_{\text{ct}}$ ) of the SnS microflowers,  $\text{MoS}_2$  nanospheres, and  $\text{MoS}_2@\text{SnS}$  heterostructure are  $\sim 106.9$ ,  $\sim 93.4$  and  $\sim 55.2 \Omega$ , respectively. The reduced interface impedances can be attributed to enhanced electronic conductivity and sodium-ion transportation in the  $\text{MoS}_2@\text{SnS}$  heterostructure. Moreover, EIS measurement of the  $\text{MoS}_2@\text{SnS}$  heterostructure electrode after testing at  $0.1 \text{ A g}^{-1}$  for 100 cycles was carried out and the Nyquist plot is shown in Fig. S6†. Compared with the fresh one, a smaller, high-frequency semicircle is noted after cycling, demonstrating stable Na-ion storage capability during cycling.

In order to further investigate the origin of reaction kinetics, the CV curves of the  $\text{MoS}_2@\text{SnS}$  heterostructure at various scan rates were recorded between 0.01 and 3 V (vs.  $\text{Na}^+/\text{Na}$ ), as shown in Fig. 7. The shapes of the CV curves are well preserved and a slightly positive shift for the anodic peaks and a negative shift for the cathodic peaks can be observed in Fig. 7a with increasing scan rates owing to polarization during the sodiation/desodiation process.<sup>47</sup> The degree of the capacitive effect can be qualitatively analysed according to the relationship

between the peak current ( $i$ ) and scan rate ( $v$ ) from the CV curves:  $i = av^b$ , where  $i$  is the peak current,  $v$  stands for the scan rate, and  $a$  and  $b$  are both adjustable parameters. The value of  $b$  is between 0.5 and 1.0, which is determined by the slope of the  $\log(i)$  vs.  $\log(v)$  plot. It is well known that the electrochemical behavior is dominated by a surface capacitive process when  $b$  is close to 1.0, whereas for a diffusion-controlled process,  $b$  approaches 0.5. In the current experiment, the adjustable  $b$  values for peak 1, peak 2, and peak 3 are  $\sim 0.84$ ,  $\sim 0.87$ , and  $\sim 0.89$ , respectively, as shown in Fig. 7b, indicating more significant capacitive storage kinetics of the  $\text{MoS}_2@\text{SnS}$  heterostructure.

The contribution from the pseudocapacitive effects (both surface pseudocapacitive and double layer capacitance) and diffusion-controlled process to the current response can be calculated based on the following equation:<sup>48</sup>

$$I(V) = k_1v + k_2v^{1/2} \quad (1)$$

where  $I(V)$  represents the total current response at a given potential  $V$ ,  $k_1v$  stands for surface capacitive effects, and  $k_2v^{1/2}$  represents a diffusion-controlled process. The above equation can be reformulated as follows:<sup>49</sup>

$$I(V)/v^{1/2} = k_1v^{1/2} + k_2 \quad (2)$$

The values of  $k_1$  (slope) and  $k_2$  (intercept) from the straight lines can be calculated by plotting  $I(V)/v^{1/2}$  vs.  $v^{1/2}$  at different potentials. The percentage of the capacitive contribution at different scanning speeds can be calculated, as shown in

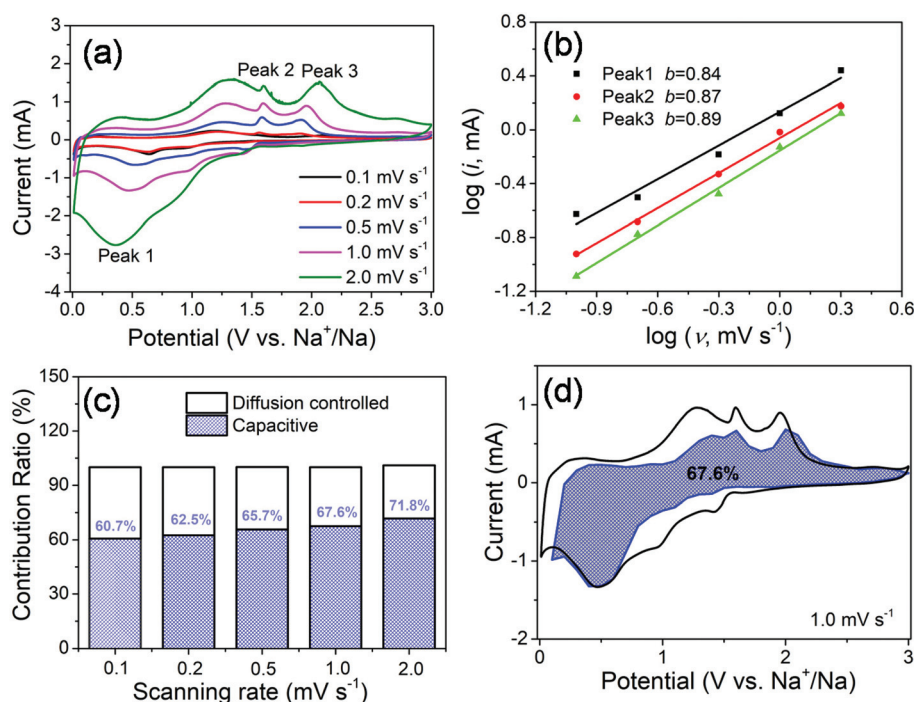


Fig. 7 (a) CV curves at various scan rates ranging from 0.1 to 2.0  $\text{mV s}^{-1}$ ; (b) plots of  $\log(i)$  vs.  $\log(v)$  at the sharp cathodic/anodic peak pair (peak current:  $i$ , scanning rate:  $v$ ); (c) capacity contributions at different scan rates; and (d) capacitive charge storage contribution at a scan rate of 1.0  $\text{mV s}^{-1}$ . The estimated pseudocapacitance contribution is shown in the blue region.

Fig. 7c, demonstrating the percentages of the capacitive contribution can be improved with the increase of the scan rate, which may account for the high rate capability and superior cycling stability of  $\text{Na}^+$  storage in the designed  $\text{MoS}_2@\text{SnS}$  heterostructure. Fig. 7d shows the typical voltage profile for the pseudocapacitive contribution (blue shaded region) in comparison with the whole area (black line). A large part of the pseudocapacitive contribution of  $\sim 67.6\%$  was achieved at a scan rate of  $1 \text{ mV s}^{-1}$ , indicating favorable charge transfer kinetics of the  $\text{MoS}_2@\text{SnS}$  heterostructure. Therefore, a large portion of the stored charge stems from the pseudocapacitive effect, which is in good agreement with the calculated  $b$  value.

More mechanistic insights are further gained from first-principles density functional theory (DFT) calculations. Fig. 8a shows the structure of  $\text{MoS}_2@\text{SnS}$  after geometry optimization. From the charge difference contour plot, the red and green colors denote the electron gain and loss regions, respectively, indicating the charge redistribution at the  $\text{MoS}_2@\text{SnS}$  interface and formation of the heterostructure. The optimized geometry structures of  $\text{MoS}_2$ ,  $\text{SnS}$  and  $\text{MoS}_2@\text{SnS}$  heterostructure after intercalation of one Na are shown in Fig. 8b–d. The corresponding binding energies ( $E_b$ ) are calculated to be ca.  $-2.25$ ,  $-1.05$  and  $-2.82 \text{ eV}$  for  $\text{MoS}_2$ ,  $\text{SnS}$  and  $\text{MoS}_2@\text{SnS}$ , respectively. The computational results indicate that Na insertion in all three structures is feasible and the intercalation in  $\text{MoS}_2@\text{SnS}$  is more favored in energy. During Na insertion, the Na can donate most of its electrons to the  $\text{MoS}_2@\text{SnS}$  framework as revealed by the charge difference plot.

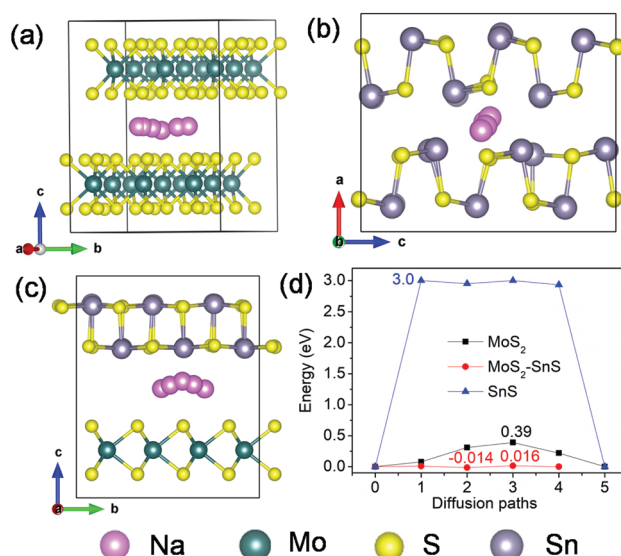


Fig. 9 Possible diffusion pathways of Na in (a)  $\text{MoS}_2$ , (b)  $\text{SnS}$  supercells and (c)  $\text{MoS}_2@\text{SnS}$  heterostructure, and (d) the corresponding energy barriers for Na diffusion in  $\text{MoS}_2$ ,  $\text{SnS}$  and  $\text{MoS}_2@\text{SnS}$ .

Next, we investigated Na diffusion in the three structures. As shown in Fig. 9a, Na can readily diffuse in the  $\text{MoS}_2$  (001) planes with a relatively small energy barrier ( $\sim 0.39 \text{ eV}$ ) (Fig. 9d). For  $\text{SnS}$ , the diffusion of Na along the (100) plane experiences a much higher energy barrier ( $3.0 \text{ eV}$ ) (Fig. 9d), possibly due to the scattering of  $\text{Sn-S}$  chains in this plane. In contrast, the diffusion of Na within the interface of  $\text{MoS}_2(001)/\text{SnS}(100)$  is the fastest with the smallest energy barrier ( $\sim 0.016 \text{ eV}$ ). The much enhanced Na diffusion behavior further suggests that the existence of a built-in electric field at the interface can considerably propel the electronic/ionic transport and charge transfer, thus boosting the rate capability.

## Conclusions

In summary, a hierarchical walnut-like  $\text{MoS}_2@\text{SnS}$  core-shell heterostructure has been designed and synthesized *via* a simple yet effective hydrothermal method. The heterostructure is comprised of  $\text{MoS}_2$  spheres wrapped by  $\text{SnS}$  nanocrystals. When evaluated as an anode material for SIBs, the  $\text{MoS}_2@\text{SnS}$  heterostructure exhibited high capacity and initial coulombic efficiency, remarkable rate capability, and superior cycling stability, much superior to those of pure  $\text{SnS}$  microflowers and  $\text{MoS}_2$  nanospheres. The improved sodium-ion storage properties mainly stem from the increased charge transfer capability and ion diffusion kinetics due to the presence of an internal built-in electric field at the heterointerfaces during charge/discharge. It is believed that the unique core-shell architecture designed herein can pave the way for the development of novel heterojunction-based electrode materials for high-performance SIBs and other electrochemical energy storage and conversion devices.

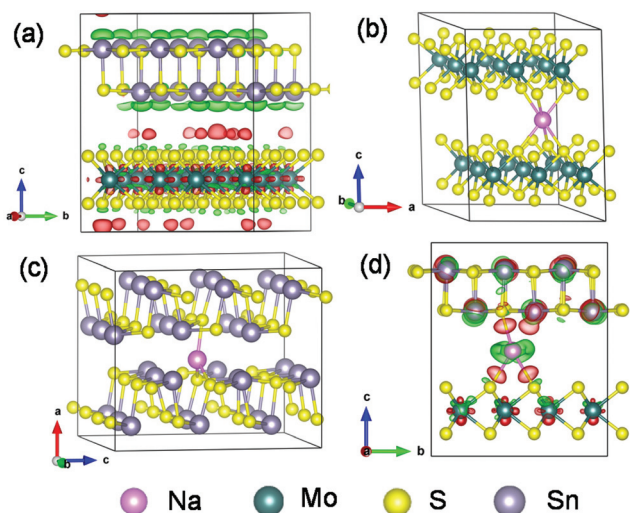


Fig. 8 (a) The  $\text{MoS}_2@\text{SnS}$  heterostructure after geometry optimization and the optimized geometry structures of (b)  $\text{MoS}_2$ , (c)  $\text{SnS}$  supercells and (d)  $\text{MoS}_2@\text{SnS}$  heterostructure after insertion of one Na atom. The corresponding binding energies ( $E_b$ ) of one Na atom in (b)  $\text{MoS}_2$ , (c)  $\text{SnS}$  and (d)  $\text{MoS}_2@\text{SnS}$  are calculated to be ca.  $-2.25$ ,  $-1.05$  and  $-2.82 \text{ eV}$ , respectively. The red and green colors in the charge difference contour plots of (a) and (d) represent the charge accumulation and depletion regions, respectively. The isosurface levels are  $3.5 \times 10^{-4} \text{ e bohr}^{-3}$  in (a) and  $2 \times 10^{-3} \text{ e bohr}^{-3}$  in (d).



## Experimental

### Synthesis of the Mo-glycerate (MoG) precursor

Typically, 10 mL of H<sub>2</sub>O, 10 mL of glycerol, and 35 mL of isopropanol were mixed and stirred to form a homogeneous solution. Then, 150 mg of molybdenyl acetoacetonate was added into the resulting solution under magnetic stirring to obtain a transparent solution. The resultant solution was transferred to a Teflon-lined stainless steel autoclave (100 mL in volume) and maintained at 190 °C for 3 h. After cooling down to room temperature, the obtained product was centrifuged and washed with ethanol three times, and then dried at 60 °C for 12 h under vacuum.

### Synthesis of MoS<sub>2</sub> nanospheres

Briefly, 100 mg of the as-prepared MoG solid spheres were dispersed in 25 mL of ethanol with the assistance of ultrasonication for 30 min to form a homogeneous suspension. Then, 10 mL of ethanol and 100 mg of Na<sub>2</sub>S were added into the above suspension and stirred for 10 min. The solution was transferred into a Teflon-lined stainless steel autoclave (100 mL in volume) and maintained at 200 °C for 10 h. The obtained MoS<sub>2</sub> was centrifuged and washed with deionized water and ethanol three times, and then dried at 60 °C for 12 h under vacuum.

### Synthesis of SnS microflowers

500 mg of polyvinyl pyrrolidone (PVP, molecular weight of 40 000) were dissolved in 50 mL of ethylene glycol followed by stirring and ultrasonication. Then, 225 mg of SnCl<sub>2</sub> and 75 mg of thioacetamide were added into the solution and stirred for 10 min. Finally, the mixed solution was transferred into a sealed Teflon-lined stainless-steel autoclave (100 mL in volume) and maintained at 160 °C for 12 h. After cooling down, the product was centrifuged and washed with ethanol three times and then dried at 60 °C for 12 h under vacuum.

### Synthesis of MoS<sub>2</sub>@SnS heterostructures

In the first step, 500 mg of PVP (molecular weight of 40 000) and 50 mg of MoS<sub>2</sub> nanospheres were successively added into 50 mL of ethylene glycol (EG) followed by stirring and ultrasonication to form a homogeneous solution. In the second step, 144 mg of SnCl<sub>2</sub> and 288 mg of thioacetamide (TAA) were dissolved in 3.2 mL of ethylene glycol, respectively. Then, the two solutions were added into the above solution under stirring for 15 min. Subsequently, the mixed solution was transferred into a Teflon-lined stainless-steel autoclave (100 mL in volume) and kept at 160 °C for 12 h. After cooling down to room temperature, the MoS<sub>2</sub>@SnS heterostructures were centrifuged and washed with ethanol three times and then dried at 60 °C for 12 h under vacuum. Finally, the product was sintered at 400 °C for 2 h under a high-purity N<sub>2</sub> atmosphere to increase the degree of crystallinity.

## Characterization

The morphology and structure of the samples were characterized using a field-emission scanning electron microscope (FESEM; JEOL, Model JSM-7800F), a transmission electron microscope (TEM; Philips, CM20 operated at 200 kV), and a high-resolution TEM (HRTEM; CM200 FEG operated at 200 kV) with energy-dispersive X-ray spectroscopy (EDS). The X-ray diffraction (XRD) pattern was recorded on a Bruker D8 Advance X-Ray Diffractometer with Cu-K $\alpha$  as the radiation source ( $\lambda$  = 0.154 nm). X-ray photoelectron spectroscopy (XPS) measurement was performed by using a VG ESCA-LAB 220i-XL UHV surface analysis system with a monochromatic Al K $\alpha$  X-ray source (1486.6 eV). The Brunauer–Emmett–Teller (BET) method was used to evaluate the surface area and porous size distribution with N<sub>2</sub> adsorption–desorption isotherms at 77 K.

## Electrochemical measurements

Electrochemical performances of the MoS<sub>2</sub>@SnS heterostructures were tested by assembling CR2032 coin-type cells in a high-purity argon-filled glovebox with sodium metal foils as counter and reference electrodes. The working electrode was fabricated by mixing the active materials (MoS<sub>2</sub>@SnS, MoS<sub>2</sub>, SnS), acetylene black, and binder (sodium alginate) in a weight ratio of 7:2:1 to form a uniform slurry in deionized water. The slurry was coated on copper foil and vacuum-dried at 70 °C for 12 h. The typical mass loading for the active materials was  $\sim 1.5$  mg cm<sup>-2</sup>. A solution of 1.25 M NaPF<sub>6</sub> dissolved in ethyl methyl carbonate was used as the electrolyte. A glass fiber (Whatman, GF/D) was used as the separator. The galvanostatic discharge/charge measurements were performed on a LAND CT2001A test system at various current densities within a potential window of 0.01–3.0 V *vs.* Na<sup>+</sup>/Na. Cyclic voltammetry (CV) was carried out on a CHI 760E electrochemical workstation at a scanning rate of 0.1 mV s<sup>-1</sup>. Electrochemical impedance spectra (EIS) both before and after testing at 0.1 A g<sup>-1</sup> for 100 cycles were measured on a ZAHNER-elektrok IM 6 electrochemical system in a frequency range from 100 kHz to 5 mHz. All the electrochemical tests were performed at room temperature.

## Computational details

All the calculations were based on first-principles density functional theory (DFT) using plane-wave pseudopotentials with an exchange–correlation of Perdew–Burke–Ernzerhof (PBE) formation implemented in Vienna *ab initio* simulation package (VASP).<sup>50,51</sup> An energy cutoff of 400 eV was used for plane wave expansion of the wavefunctions. The Brillouin zone was sampled with a 1  $\times$  1  $\times$  1 gamma-centered Monkhorst–Pack *k*-point mesh. The convergence criteria for the total energy and ionic forces were set to 10<sup>-5</sup> eV and 0.03 eV Å<sup>-1</sup>, respectively. The binding energies ( $E_b$ ) for Na intercalation in the respective structures were determined by  $E_b = E_{\text{total}} - E_{\text{Na}} - E_{\text{MS}}$ , where  $E_{\text{total}}$ ,  $E_{\text{Na}}$ , and  $E_{\text{MS}}$  represent the calculated energies of the whole system, single Na atom in a vacuum, and host structure (MoS<sub>2</sub>, SnS or MoS<sub>2</sub>@SnS), respectively. The Na diffusion in



the three host structures (MoS<sub>2</sub>, SnS and MoS<sub>2</sub>@SnS) was calculated *via* the climbing-image nudged elastic band (CI-NEB) method. During the calculations, van der Waals interactions (DFT-D3) were considered. The drawing of the calculated results was carried out using VESTA software.<sup>52</sup>

## Conflicts of interest

There are no conflicts to declare.

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