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Compatibility issues between electrodes and electrolytes in solid-state batteries†

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Remarkable success has been achieved in the discovery of ceramic alkali superionic conductors as electrolytes in solid-state batteries; however, obtaining a stable interface between these electrolytes and electrodes is difficult. Only limited studies on the compatibility between electrodes and solid electrolytes have been reported, partially because of the need for expensive instrumentation and special cell designs. Without simple yet powerful tools, these compatibility issues cannot be systematically investigated, thus hindering the generalization of design rules for the integration of solid-state battery components. Herein, we present a methodology that combines density functional theory calculations and simple experimental techniques such as X-ray diffraction, simultaneous differential scanning calorimetry and thermal gravimetric analysis, and electrochemistry to efficiently screen the compatibility of numerous electrode/electrolyte pairs. We systematically distinguish between the electrochemical stability of the solid-state conductor, which is relevant wherever the electrolyte contacts an electron pathway, and the electrochemical stability of the electrode/electrolyte interfaces. For the solid electrolyte, we are able to computationally derive an absolute thermodynamic stability voltage window, which is small for Na₃PS₄ and Na₃PSe₄, and a larger voltage window which can be kinetically stabilized. The experimental stability, when measured with reliable techniques, falls between these thermodynamic and kinetic limits. Employing a Na solid-state system as an example, we demonstrate the efficiency of our method by finding the most stable system (NaCrO₂|Na₃PS₄|Na–Sn) within a selected chemical space (more than 20 different combinations of electrodes and electrolytes). Important selection criteria for the cathode, electrolyte, and anode in solid-state batteries are also derived from this study. The current method not only provides an essential guide for integrating all-solid-state battery components but can also significantly accelerate the expansion of the electrolyte/electrode compatibility data.

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Broader context

All-solid-state rechargeable batteries have seen a resurgence of interest from researchers in recent years, owing to their potential for enhanced safety and energy density. Many superionic conductors have been discovered and employed as solid state electrolytes with ionic conductivities close to or even higher than those of liquid counterparts. However, the compatibility between electrodes and solid-state electrolytes has not been systematically investigated. In this work, we present a simple yet powerful methodology which combines *ab initio* modeling and fast characterization tools to investigate the electrochemical stability of the solid-state electrolyte and the chemical stability of the electrode/electrolyte interfaces. Employing Na solid state batteries as an example, our combined theoretical and experimental investigation led us to identify the most stable system (NaCrO₂|Na₃PS₄|Na–Sn) within the selected chemical space (more than 20 different combinations of electrodes and electrolytes). We also provide possible solutions to the interfacial issues and important selection criteria for the cathode, electrolyte, and anode in solid-state batteries. With the focus of solid state battery research shifting toward cell integration, our timely system-level investigations provide a strong foundation.

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Introduction

Pioneered by the study of microbatteries, solid-state batteries have recently attracted significant attention^{1–9} because of their advantages compared with conventional batteries employing liquid electrolytes. The use of a ceramic solid-state electrolyte not only eliminates the safety hazards associated with flammable



organic liquid electrolytes but also opens up the possibility of using novel high-capacity electrodes, such as sulfur cathodes and Na or Li metal anodes. These high-capacity electrodes have proven problematic in liquid systems, partially because of reactivity and/or dissolution with the electrolyte, and poor metal deposition morphology in liquid electrolytes, often leading to dendrite growth.^{2,10,11} When built with stable interfaces, solid state batteries can also minimize the side reactions that occur in liquid electrolyte batteries, resulting in high Coulombic efficiency and ultra-long cycle life.^{12,13} Recently, all-solid-state batteries utilizing sulfide-based superionic conductors have even achieved superior performance in terms of power density compared with traditional Li-ion batteries (LIBs) thanks to the discovery of lithium superionic conductors with ionic conductivities of 25 mS cm^{-1} , one magnitude higher than those of state-of-art liquid electrolytes.^{14–19}

The main research focus in all-solid-state batteries has been on finding fast ionic conductors, which has resulted in many newly discovered conductors with ionic conductivities close to or even surpassing those of liquid electrolytes. Given that the basic structural and chemical features for high alkali ion conductivity are now reasonably well understood,^{20,21} it is likely even better conductors will be developed. In Li-ion systems, some NASICON, perovskite- and garnet-type oxides exhibit room-temperature (RT) conductivities of approximately 1 mS cm^{-1} or higher but suffer from poor contact with electrodes because of difficulties in pellet pressing and sintering.^{1,7,22–29} Sulfide-based solid electrolytes such as $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$ and $\text{Li}_2\text{S-P}_2\text{S}_5$ exhibit conductivities greater than 10 mS cm^{-1} ,^{8,21,30–33} but generally have limited voltage stability windows, which makes electrode selection a difficult task.^{6,34–36} In some cases, an electrode coating is applied to mitigate this issue; however, the coating process is often imperfect or difficult to scale.^{8,37–39} In parallel to the developments in solid-state lithium conductors, promising fast Na-ion conductors have also been recently discovered and applied in Na-ion batteries (NIBs).^{14,16,19,30,32,40–45} However, it is similarly challenging to find a Na conductor with all the desired properties for all-solid-state battery applications, namely high conductivity, compatibility with both anodes and cathodes, processability, and good mechanical properties.

Clearly, the bottleneck of all-solid-state battery development is no longer maximizing the ionic conductivity of solid electrolytes but has instead shifted toward the integration of the solid electrolyte and electrodes. This challenge of cell integration is largely associated with maintaining chemical and mechanical stability between the electrodes and electrolytes during battery operation, both of which are a major obstacle for solid-state battery development. The compatibility of electrodes and electrolytes is largely determined by the properties of the electrode/electrolyte interface. A good interface between a solid electrolyte and electrode requires fast ion transport, maximum contact area, and chemical stability during cycling. Indeed, in detailed studies, previously claimed stable electrolyte/electrode pairs have often found to degrade through chemical or electrochemical reactions.^{8,21,26,34,39,46–49}

In this work, we focus on the chemical aspect of the cell integration challenge, and present a methodology that combines

computational predictions with fast, simple experimental tests that can efficiently screen the compatibility of numerous electrode/electrolyte pairs. We use layered Na transition metal oxide cathodes (NaMO_2 , $M = \text{Cr, Mn, Fe, Co, Ni}$),^{50–54} Na metal or Na–Sn alloy anodes,^{55,56} and two recently reported solid electrolytes with high ionic conductivities (Na_3PS_4 ³⁰ and Na_3PSe_4 ^{15,41}) as examples to demonstrate our methodology. The Na ion system was selected for several reasons. First, NIBs have attracted significant attention because of the lower cost and greater abundance of their materials compared with those used in LIBs.^{57–59} Second, the Na system provides a wider chemical space to explore for cathode materials, enabling synthesis and cycling of many electrode materials for which the Li analogues are electrochemically inactive, such as layered NaFeO_2 .^{52,58–60} Finally, compatibility issues have not been systematically studied in the Na solid-state system, which provides us with an opportunity to demonstrate the efficiency of our screening method when applied to unknown systems.

In the following discussion, we will start by introducing the compatibility issues facing solid-state batteries as well as the methodology to examine these issues. Then, the results with respect to the electrochemical stability of the electrolytes and chemical compatibility between the electrodes and electrolytes will be presented. The manuscript concludes with a discussion of the (1) main chemical challenge associated with utilizing an oxide cathode and thiophosphate solid electrolyte, (2) importance of understanding both the chemical and electrochemical decomposition pathways of electrolytes and electrode/electrolyte composites, and (3) role of thermodynamics and kinetics in these reactions. Possible strategies and selection criteria to integrate all-solid-state battery components will also be proposed.

Methodology

Three factors mainly govern the choice of components for all-solid state batteries. Taking Na solid-state systems as an example, the three factors are graphically illustrated in Fig. 1 and are discussed in detail below:

(1) Voltage window of the solid electrolyte. The voltage window of the electrolyte determines the cycling range and selection of both electrodes and should thus be considered and determined first.

Prior experimental insights regarding the electrochemical stability of solid-state electrolytes may require reinterpretation. Determination of the stable electrochemical window of a solid electrolyte has been traditionally performed using cyclic voltammetry (CV).^{18,32,61,62} In this method, the solid electrolyte is pressed into pellets and cycled with Li or Na metal on one side and an inert metal (such as stainless steel, Au, or Pt) on the other side. However, CV often overestimates the electrochemical stability limits of electrolytes. The bulk electrolyte is likely not in equilibrium during a CV scan because of the fast scanning rate and/or imperfect contact with the metal electrodes. Furthermore, because of the poor electronic conductivity of solid electrolytes, the overall decomposition reaction is often slow or limited to a



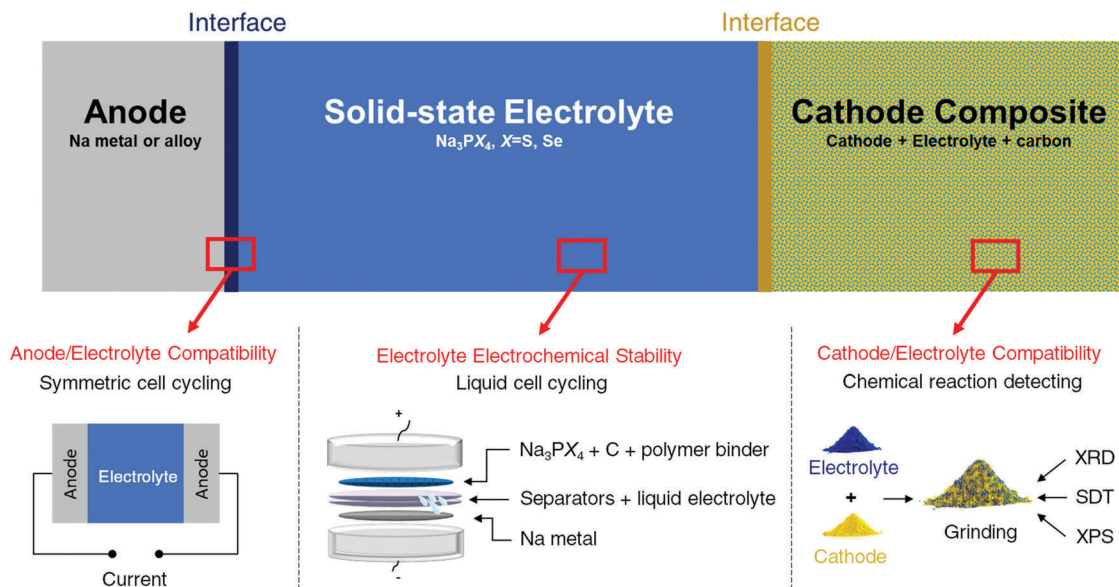


Fig. 1 Summary of compatibility and stability problems in all-solid-state batteries and the experimental methods for assessing these issues. The sodium system was selected as a specific example utilizing the methods.

thin region at the interface, thereby limiting the degradation current that can be observed in a CV scan. The situation is very different in a real cell configuration, where the electrolyte is mixed with carbon and the cathode material, providing a facile electron transfer pathway that promotes electrolyte redox reactions. Finally, the relatively small decomposition current detected by the CV method (sometimes less than $1 \mu\text{A}$) is difficult to notice compared with the large current created by metal deposition/stripping at low voltage and is often ignored in the CV method. However, this small current could have a catastrophic effect on the long-term cycling of the full cell. Indeed, solid electrolytes previously claimed to be stable based on CV scans⁶² were later upon more detailed investigation, found to be reactive at typical anode and cathode voltages,⁶³ in agreement with theoretical predictions.^{6,33,64}

Other electrochemical techniques, such as polarization experiments, should be complemented with CV methods to determine the stability window of the solid electrolyte more accurately. In such experiment, the electrolyte is made into electrode and polarized to a given potential or with a constant current. The electrolyte is considered stable at such potential if the capacity delivered below (or above) this potential is close to zero during a galvanostatic or potentiostatic charge (or discharge). In our work, the stability windows of selected electrolytes (Na_3PS_4 and Na_3PSe_4) were first computed using density functional theory (DFT) calculations.³⁴ The results were then compared with experimental results obtained from galvanostatic charging/discharging. A similar method was recently employed to evaluate the electrochemical stability windows of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ garnet and $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$, where the DFT computed and experimentally determined stability windows were in excellent agreement.⁶³ The synthesized solid electrolytes were ground into fine powders and then mixed with carbon and polymer binders to form film-type working electrodes, which were assembled in Swagelok cells with a liquid electrolyte

against Na metal. By slowly cycling this cell, the voltage experienced by the bulk electrolyte materials is much better represented by the cell voltage, and a more accurate estimation of the stability window of the materials can be provided. The corresponding charge (or discharge) capacities also indicate whether the electrolyte decomposition is self-limiting. A self-limiting decomposition reaction can be beneficial in widening the electrochemical stability of the electrolyte depending on the physical properties (*e.g.*, ionic and electronic conductivities) of the decomposition products.

(2) Possible reaction between cathode and solid electrolyte. Absolute stability between the cathode and electrolyte is difficult to achieve, and the products of the reaction between the cathode and solid electrolyte can form an interfacial layer between the two. Depending on its properties, this interfacial layer can be detrimental or beneficial to the ionic transport between the two components. A good interface between the electrode and electrolyte must be self-passivating while still being permeable to the working ions.

Based on this information, we tested the compatibility of electrodes and electrolytes by mixing the electrolyte and electrode powders at room temperature. Any bulk change detectable by X-ray diffraction (XRD) indicates that the selected electrolyte and electrode materials are incompatible. The possible reactions between electrodes and electrolytes at elevated temperatures were also evaluated using simultaneous differential scanning calorimetry and thermal gravimetric analysis (SDT) and XRD to determine the onset temperature of reaction and corresponding reaction products. Comparison of these results with the DFT-computed thermodynamic reaction products enabled us to assess the role of kinetics in the electrode/electrolyte reactions, providing additional mechanistic insights.

Besides testing the reaction of the electrolyte with the as-synthesized cathode, studying the compatibility with the



charged cathode at high voltages is also important. At higher potential the strong oxidative power of the charged cathode will likely promote the electrolyte decomposition for chalcogenide systems. This chemical compatibility, however, has not yet been systematically investigated.

To investigate the aforementioned issue, partially charged cathodes were prepared through chemical oxidation with highly concentrated iodine in acetonitrile (CH_3CN), resulting in cathode powders equivalent to being charged to approximately 3.7 V against Na metal.^{65,66} The reactions between the charged cathodes and electrolytes were then studied in a similar manner as discussed above.

(3) Possible reaction between anode and solid electrolyte. The compatibility between the anode and electrolyte was examined by cycling anode/electrolyte/anode symmetric cells. If the anode and electrolyte react to form a poorly ionic conductive interfacial layer, the cell potential will increase as the reaction progresses. To prevent possible potential increase due to the mechanical loss of contact, a specially designed pressure cell is used to ensure good contact between electrolyte and electrodes during cycling. Therefore, an increase in the charge and discharge voltages during galvanostatic cycling often signifies an unstable interface between the anode and electrolyte.

Results

I. Electrolyte electrochemical stability

The calculated voltage stability window and decomposition products of Na_3PS_4 and Na_3PSe_4 are shown in Fig. 2a and b, respectively. These figures indicate which products the conductor converts into when Na is supplied and extracted at a given potential. The x-axis represents the capacity generated when these decomposition reactions occur per gram of conductor consumed. The results in Fig. 2a indicate that Na_3PS_4 is electrochemically only stable from 1.55 to 2.25 V against Na metal. Below 1.55 V, Na_3PS_4 can be reduced and converted into Na_2S and other Na-P compounds. Above 2.25 V, in contrast, Na is extracted from Na_3PS_4 , leading to decomposition into Na-deficient phases such as P_2S_7 and S. Similarly, according to Fig. 2b, Na_3PSe_4 is stable from 1.80 to 2.15 V against Na metal and decomposes into Na_2Se and other Na-P compounds below 1.80 V and Na-deficient phases such as PSe and Se above 2.15 V. Of note is that our calculated stability window is much narrower than experimental values claimed from CV measurements, but in agreement with other theory work.^{30,41} This discrepancy results either from reaction kinetics, which would delay the onset of decomposition, or intrinsic limitations of the CV measurements. Based on our experimental results, as will be discussed below, the latter is more likely.

These calculated voltages assume that diffusion kinetics are not limiting, and thus provide a lower bound of the Na extraction voltage. To investigate the upper limiting case, the voltage for topotactic desodiation of the conductors was calculated. The calculated results indicate that Na_3PS_4 and Na_3PSe_4 lose Na at 3.05 V and 2.75 V, respectively. We found furthermore

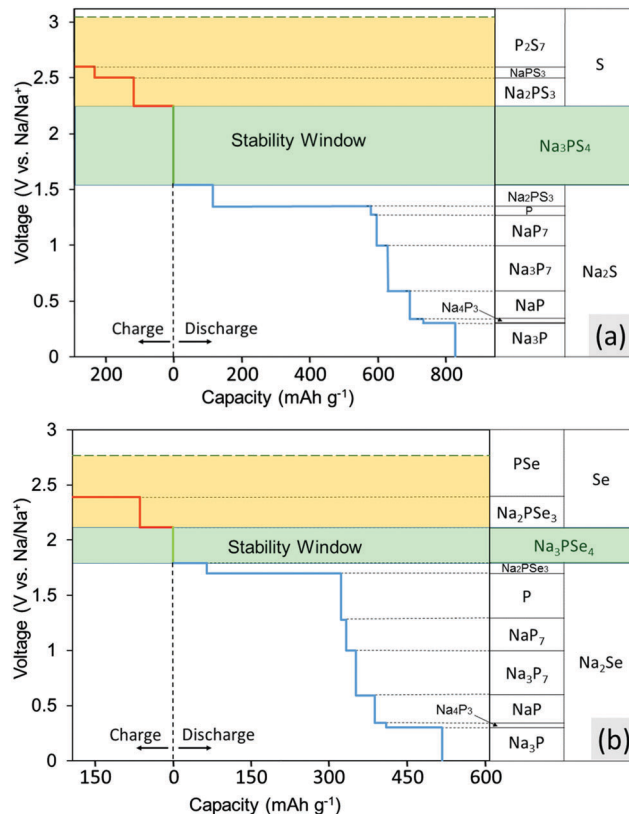


Fig. 2 Calculated stability window and decomposition products for (a) Na_3PS_4 and (b) Na_3PSe_4 . The green shaded region is the thermodynamically stable voltage window, and the yellow shaded region is the additional voltage range that could be kinetically stabilized.

that the voltage for subsequent extraction of Na is lower. Note that these two values indeed provide absolute upper bound for the Na_3PX_4 ($X = \text{S}, \text{Se}$) stability window, as the Na-ion and electron extraction are unlikely to be kinetically limited due to the faster Na-ion mobility in these materials.

To experimentally determine the electrochemical stability window of the electrolyte materials, Na_3PX_4 cathodes were “charged” (oxidized) to 4.0 V or “discharged” (reduced) to 0.5 V at a constant current. Upon charging, Na_3PS_4 exhibited negligible capacity at the beginning of charging (Fig. 3a). However, as the voltage increased above ~ 2.65 V, a voltage dip followed by a substantial capacity delivered at approximately 2.7 V was observed. The initial voltage rise is likely due to a nucleation or other activation process, needed to generate the decomposition products of Na_3PS_4 . Therefore, we can assume that the voltage dip at approximately 2.5 V is the onset decomposition voltage of Na_3PS_4 . Approximately 2.5 Na per f.u. can be extracted from Na_3PS_4 until the cut-off voltage of 4.0 V is reached. The “fully charged” Na_3PS_4 cathode composite turns completely amorphous as observed in XRD (Fig. 3c).

During the discharging process, a sloping voltage region is first observed at approximately 1.8 V, followed by a redox reaction at approximately 0.9 V, suggesting that Na_3PS_4 is likely electrochemically unstable below this voltage. The sloping voltage region (1.8–0.9 V) is likely a result of the presence of a small



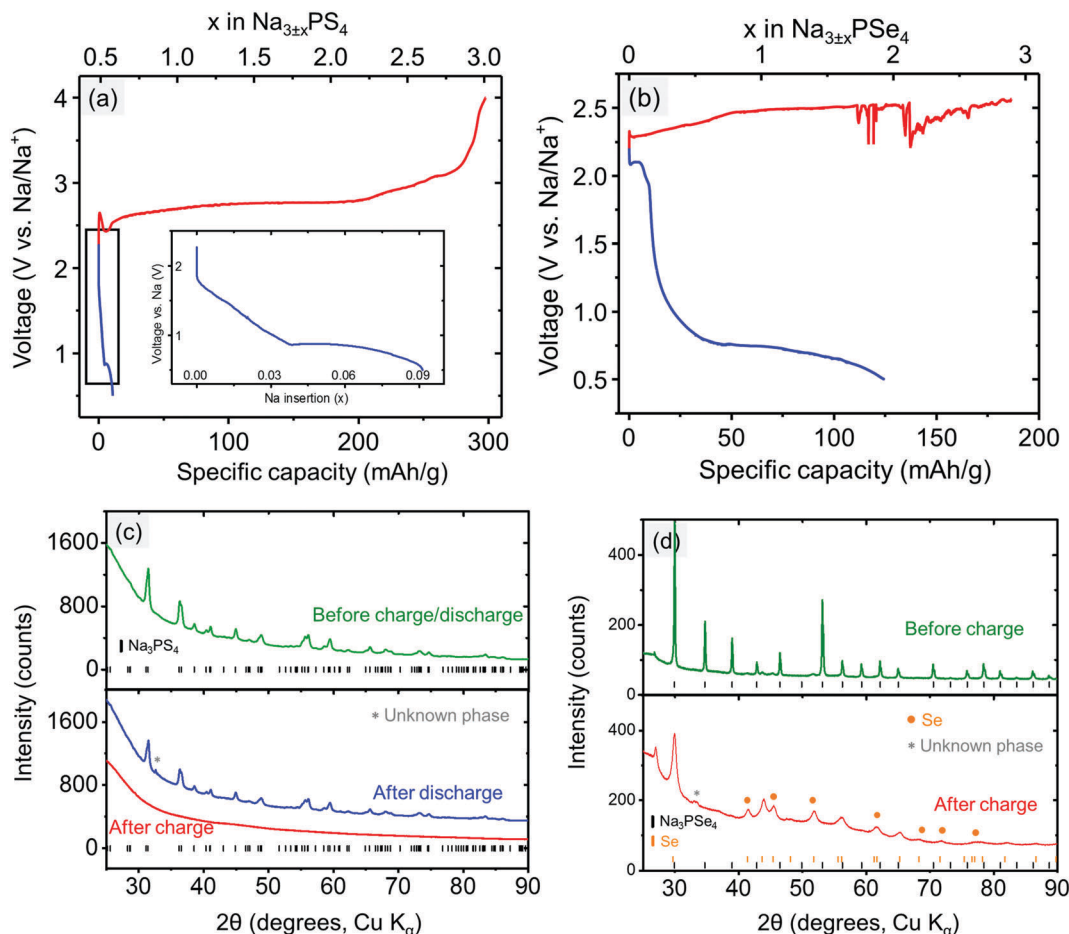


Fig. 3 Electrochemical cycling of the Na_3PX_4 (mixed with carbon) cathode composite at constant current (2.604 mA g^{-1} for Na_3PS_4 and 2.404 mA g^{-1} for Na_3PSe_4), showing the stability window of (a) Na_3PS_4 and (b) Na_3PSe_4 . Diffraction patterns of the (c) Na_3PS_4 cathode composite before and after being fully charged/discharged and (d) Na_3PSe_4 cathode composite before and after being fully charged.

amount of sulfur in the as-prepared Na_3PS_4 sample. The reduction of sulfur occurs at approximately 2 V.⁶⁷ Interestingly, fully discharging to the cut-off voltage of 0.5 V only results in a very low capacity (*i.e.*, 0.08 Na intercalation per formula), and the “fully discharged” Na_3PS_4 shows almost no structural change compared with the pristine cathode composite (Fig. 3c). One possible reason is that Na_3PS_4 might be passivated by the decomposition products upon discharging. This passivating process may prevent further decomposition of Na_3PS_4 and widens the apparent reduction limit of Na_3PS_4 . Based on the discussion above, we conclude that the electrochemical stability window of Na_3PS_4 lies within the range 0.9–2.5 V, which is in much better agreement with the DFT predictions than reported CV measurements, further underscoring the limited reliability of CV techniques to determine the stability limits of solid electrolytes.

Similarly, the stability window of Na_3PSe_4 was experimentally determined by charging and discharging the Na_3PSe_4 (mixed with carbon) cathode composite. During the charging process, the decomposition of Na_3PSe_4 starts at approximately 2.33 V, where a substantial capacity of 110 mA h g^{-1} or 1.5 Na per formula was delivered in the sloping voltage region of 2.33–2.50 V.

Based on DFT calculations, this decomposition process is most likely associated with the production of Se and Na_2PSe_3 . The decomposition products of the “fully charged” Na_3PSe_4 was experimentally determined by both *ex situ* and *in situ* XRD. In the *ex situ* XRD results presented in Fig. 3d, new Se peaks are observed after the Na_3PSe_4 cathode composite is “fully charged”, which is in almost perfect agreement with the DFT calculations; in the *in situ* XRD results (Fig. S1, ESI[†]), Se was detected to grow in quantity at the expense of Na_3PSe_4 , although the other predicted product (*i.e.*, Na_2PSe_3) is not observed. We suspect that Na_2PSe_3 might be present as an amorphous phase. The prolonged voltage plateau at approximately 2.50 V might be a result of the redox shuttle effect caused by dissolved polyselenide molecules,^{68,69} and the voltage fluctuation could be related to the reaction of the Na metal with the dissolved decomposition products. When the cell was opened after the charging process, the separators and Na metal had both become brown, indirectly supporting the above explanation of the voltage fluctuation. During the discharge process, a noticeable redox reaction occurs at approximately 2.10 V. Similarly, this is likely due to the presence of a small amount of the selenium in the as-prepared Na_3PSe_4 sample, which is reduced at approximately 2 V.⁶⁸ Since only



a small capacity is delivered in the voltage sloping region (2.10–1.25 V), it is unlikely to arise from the bulk reduction of Na₃PSe₄. Thus we tentatively assigned 1.25 V as the cathodic stability limit of Na₃PSe₄. Based on DFT calculations, this process is associated with the production of Na₂Se and Na₂PSe₃. Overall, the stability window of Na₃PSe₄ was determined to be 1.25–2.35 V, which is again closer to our theoretical predictions than to the CV measurement (Table 4).

II. Compatibility between cathode and electrolyte

(1) **DFT-predicted products of cathode/electrolyte reactions.** To obtain an estimate of the chemical stability of each interface, we used DFT calculations to calculate the maximum mixing energy of the cathode/electrolyte compositions using methodology similar to that of previous work.³⁴ The maximum mixing energies and their corresponding reaction products, were calculated for all combinations of the cathodes (NaMO₂, M = Cr, Mn, Fe, Co, Ni) and electrolytes (Na₃PX₄, X = S, Se). To show the compatibility at different status of charge, this procedure was repeated for partially desodiated cathodes Na_{0.5}MO₂. The calculation results, summarized in Table 1, indicate that none of the oxide and chalcogenide pairs are chemically absolutely stable. Because there are many possible reactions that result in similar mixing energies, and because which one actually forms depends on both thermodynamic and kinetic factors, a full list of the reaction products along the entire tie line is summarized in Table S1 (ESI[†]). Because these reactions require significant bulk diffusion, they can be expected to localize to a small interfacial region unless aided by high temperatures.

The reactions between the Na_xMO₂ ($x = 1.0$ pristine or $x = 0.5$ desodiated) cathode and Na₃PX₄ electrolyte can be broadly categorized into two classes (often occurring together):

(1) Anion exchange reactions. For instance, mixing NaCrO₂ and Na₃PX₄ (X = S, Se) can produce NaCrX₂ (X = S, Se) and Na₃PO₄. The exchange of some oxygen from the cathode with the chalcogenide from the electrolyte to form Na₃PO₄ and metal-chalcogenides is favorable for all the systems we investigated.

(2) Complex redox reactions involving multiple phases with significant structural rearrangements. For example, mixing NaNiO₂ and Na₃PX₄ (X = S, Se) leads to the production of more than three decomposition products and involves transition metal reduction.

(2) **Experimental verification of the reactions between the pristine cathode and electrolyte.** The compatibility of the pristine cathode and electrolyte was first investigated at room temperature. Diffraction patterns before and after mixing the selected electrode and electrolyte materials at room temperature are shown in Fig. S2 (ESI[†]). Fig. S2a–d (ESI[†]) shows that the diffraction patterns of NaCrO₂ and NaMnO₂ mixed with Na₃PS₄ or Na₃PSe₄ are almost the same as the sum the patterns of the individual components, suggesting that no bulk reaction occurs in these paired materials after mixing at room temperature. In contrast, peak shifts and/or peak shape changes are observed after mixing NaFeO₂, NaCoO₂, or NaNiO₂ with Na₃PSe₄ (Fig. S2e–j, ESI[†]), indicating a change in lattice dimension and/or symmetry. The majority of peaks that show noticeable differences are associated with Na₃PSe₄, which we believe is caused by either an anion exchange process creating intermediate Na₃PO_xSe_{4–x} phases or topotactic Na extraction from

Table 1 DFT calculations for the products of the reaction between Na_xMO₂ ($x = 0.5$ or 1.0) and Na₃PX₄

| | | NaCrO ₂ | NaMnO ₂ | NaFeO ₂ | NaCoO ₂ | NaNiO ₂ |
|----------------------------------|-------------------------------|---|--|--|---|--|
| Na ₃ PS ₄ | Reaction products | Na ₃ PO ₄ NaCrS ₂ | Na ₃ PO ₄ NaMnS ₂ ^a | Na ₃ PO ₄ Na _{3/2} (FeS ₂) FeS ₂ | Na ₃ PO ₄ NaCoS ₂ | Na ₃ PO ₄ Na ₂ S Na ₂ SO ₄ Na ₂ Ni ₃ S ₄ ^a |
| | Reaction energy (eV per atom) | –0.0970 | –0.2649 | –0.2652 | –0.3516 | –0.4394 |
| Na ₃ PSe ₄ | Reaction products | Na ₃ PO ₄ NaCrSe ₂ | Na ₃ PO ₄ NaMnSe ₂ ^a | Na ₃ PO ₄ Na ₂ Se FeSe ₂ FeSe | Na ₃ PO ₄ Na ₂ Se Co ₉ Se ₈ ^a Co ₅ Se ₈ ^a | Na ₃ PO ₄ Na ₂ Se Ni ₅ Se ₈ ^a Ni ₃ Se ₄ |
| | Reaction energy (eV per atom) | –0.1325 | –0.2138 | –0.2615 | –0.3695 | –0.4541 |
| | | Na _{0.5} CrO ₂ | Na _{0.5} MnO ₂ | Na _{0.5} FeO ₂ | Na _{0.5} CoO ₂ | Na _{0.5} NiO ₂ |
| Na ₃ PS ₄ | Reaction products | Na ₃ PO ₄ NaCrS ₂ S Cr ₂ O ₃ | Na ₃ PO ₄ Na ₂ SO ₄ MnS Na ₄ Mn ₃ S ₅ ^a | Na ₃ PO ₄ Na _{3/2} (FeS ₂) FeS ₂ | Na ₃ PO ₄ Na ₂ S Na ₂ SO ₄ Co ₉ S ₈ | Na ₃ PO ₄ Na ₂ SO ₄ Ni ₉ S ₈ Ni ₃ S ₂ |
| | Reaction energy (eV per atom) | –0.1429 | –0.3156 | –0.3514 | –0.4376 | –0.5580 |
| Na ₃ PSe ₄ | Reaction products | Na ₃ PO ₄ Na _{1/3} (CrSe ₂) Na _{2/3} (CrSe ₂) | Na ₃ PO ₄ Na _{1/3} (MnSe ₂) Na ₆ MnSe ₄ MnO | Na ₃ PO ₄ Na ₂ Se FeSe ₂ FeSe | Na ₃ PO ₄ Na ₂ Se Co ₅ Se ₈ ^a CoSe ₂ | Na ₃ PO ₄ Na ₂ Se Ni ₅ Se ₈ ^a NiSe ₂ |
| | Reaction energy (eV per atom) | –0.1985 | –0.2848 | –0.3730 | –0.4558 | –0.5463 |

^a Denotes compounds which are created through chemical substitution of compounds which are present in the Inorganic Crystal Structure Database (ICSD).



Table 2 Onset temperatures of the reactions between NaMO₂ and Na₃PX₄

| | NaCrO ₂ (°C) | NaMnO ₂ (°C) | NaFeO ₂ (°C) | NaCoO ₂ (°C) | NaNiO ₂ (°C) |
|----------------------------------|----------------------------|----------------------------|----------------------------|----------------------------|----------------------------|
| Na ₃ PS ₄ | 500 | 330 | 270 | 47 | 30 |
| Na ₃ PSe ₄ | 380 | 220 | 25 ^a | 25 ^a | 25 ^a |

^a When a bulk change was observed after mixing paired materials at RT, we tentatively assigned 25 °C as the onset temperature of the reaction.

Na₃PSe₄ accompanied by Se²⁻ oxidation. Through this simple test, our experiments already indicate that NaFeO₂, NaCoO₂, and NaNiO₂ cathodes are likely incompatible with Na₃PSe₄. The compatibility between the selected cathode and electrolyte materials at elevated temperatures were tested by SDT, and the onset temperatures of the reactions of the cathode/electrolyte pairs are summarized in Table 2. It is noted that the SDT results show that NaCoO₂ and NaNiO₂ are not compatible with Na₃PS₄ at very low temperatures, close to RT (47 °C and 30 °C, respectively), even though no peak change in XRD can be observed after mixing them at RT (Fig. S2f and h, ESI†). Unless other strategies such as protective barrier coatings are utilized to improve the compatibility of these electrodes (*i.e.* NaFeO₂, NaCoO₂, or NaNiO₂) with Na₃PX₄ electrolytes, alternative pairs should be sought.

According to the onset temperature of each reaction between NaMO₂ and Na₃PX₄ listed in Table 2, two reaction trends are observed:

(1) From NaCrO₂ to NaNiO₂, the onset temperature decreases, indicating a reduction of the kinetic barrier, which may be related to an increase of the driving force of each reaction (Table 1).

(2) From Na₃PS₄ to Na₃PSe₄, the onset temperature also decreases.

The cathode–electrolyte pairs for which no bulk reactions were observed close to RT (*i.e.*, NaCrO₂ and NaMnO₂ with Na₃PX₄) were subjected to combined SDT and XRD characterization. These simple tests were quite informative, as they provided insight into the intriguing interplay between thermodynamics and kinetics in the decomposition reactions. Taking NaCrO₂ and Na₃PX₄ as an example, when these mixtures were heated to below approximately 300 °C, no bulk reaction was observed in the XRD results (Fig. 4a and b). This finding suggests that NaCrO₂ and Na₃PX₄ should be a relatively stable pair that could be used in solid-state batteries at RT. When the reaction temperature was raised to 500 °C, NaCrSe₂ (along with excess NaCrO₂) was observed in the final products of the reaction between NaCrO₂ and Na₃PSe₄ (green line in Fig. 4b), which partially agrees with the DFT calculation result in Table 1. No other P-containing phases were observed in the XRD result. Because no substantial mass

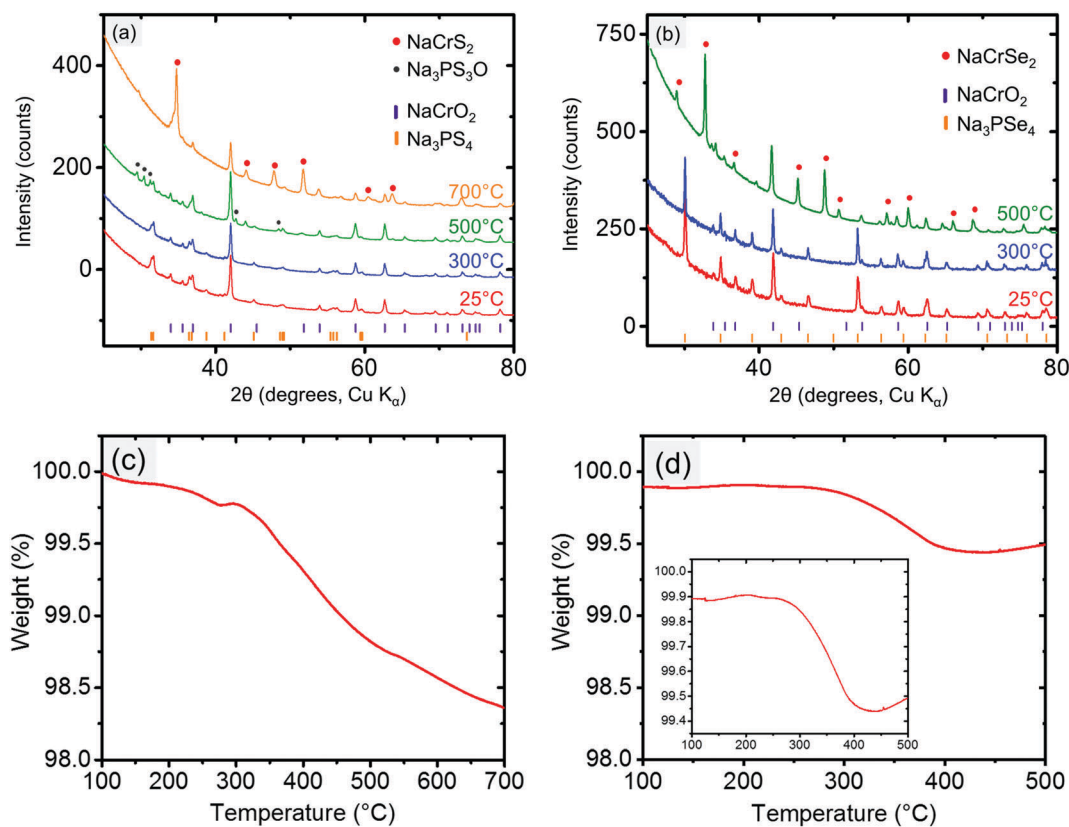


Fig. 4 XRD patterns of the reaction products of (a) NaCrO₂ and Na₃PS₄ at RT, 300 °C, 500 °C, and 700 °C, and (b) NaCrO₂ and Na₃PSe₄ at RT (25 °C), 300 °C, and 500 °C. The tick marks indicate the peaks for the reactants NaCrO₂ (purple, top) and Na₃PX₄ (orange, bottom). TGA measurements (total weight) of the reactions between (c) NaCrO₂ and Na₃PS₄ and (d) NaCrO₂ and Na₃PSe₄. The weight axis is shown in the same scale to emphasize the higher reactivity of S-based compound.



loss (<0.6%) was observed upon heating to 500 °C (Fig. 4d), P-containing phases should still be present in the mixture but in amorphous form. Taken together with the DFT prediction (Table 1), we suspect that amorphous Na_3PO_4 is present in the heated mixture. However, when the conductor was changed to Na_3PS_4 , the calculated reaction products between NaCrO_2 and Na_3PS_4 with the highest driving force (*i.e.* NaCrS_2 and Na_3PO_4) were not observed after heating to 500 °C. Instead, $\text{Na}_3\text{PS}_3\text{O}$ (together with both precursors NaCrO_2 and Na_3PS_4) was observed (green line in Fig. 4a). It is not until 700 °C that the predicted product NaCrS_2 (together with excess NaCrO_2) starts to appear with the disappearance of $\text{Na}_3\text{PS}_3\text{O}$ (orange line in Fig. 4a). Although the predicted NaCrS_2 might be present in the 500 °C heated mixture in amorphous form, the presence of $\text{Na}_3\text{PS}_3\text{O}$ in lieu of the predicted product Na_3PO_4 may indicate a preference for intermediate reaction products over the stable thermodynamic states unless the temperature is very high (*e.g.* 700 °C). We also note from Table 1 that the reaction energy between NaCrO_2 and the selenide conductor is substantially higher than with the sulfide conductor.

(3) Chemical reactions between desodiated cathode and electrolyte. The compatibility between the partially desodiated cathode Na_xMO_2 ($x < 1.0$) and electrolyte Na_3PX_4 is equally important for the stable cycling of all-solid-state batteries and was also investigated. We first prepared the chemically desodiated

NaCrO_2 , NaCoO_2 , NaFeO_2 , and NaNiO_2 samples using a highly-concentrated iodine solution in acetonitrile, which is equivalent to oxidation at ~ 3.7 V.⁷⁰ The same process always yields amorphous desodiated NaMnO_2 , likely due to Mn dissolution into the acetonitrile solvent.⁷¹ Desodiated NaMnO_2 was therefore excluded in our study. The diffraction patterns for desodiated NaCrO_2 , NaCoO_2 , NaFeO_2 , and NaNiO_2 are presented in Fig. 5. The products after chemical desodiation were $\text{Na}_{0.5}\text{CrO}_2$, $\text{Na}_{0.5}\text{FeO}_2 + \beta\text{-NaFeO}_2$, $\text{Na}_{0.5}\text{CoO}_2$, and $\text{Na}_{0.5}\text{NiO}_2 + \text{Na}_{0.4}\text{NiO}_2$, respectively. The Na compositions of Na_xMO_2 compounds were estimated based on comparisons of the refined lattice parameters and electrochemical capacity with previous literature. Interestingly, $\beta\text{-NaFeO}_2$ was generated after chemical desodiation of NaFeO_2 , which may be one of the causes of the observed irreversibility in NaFeO_2 ,^{52,60} as $\beta\text{-NaFeO}_2$ is not electrochemically active according to our electrochemical measurements (Fig. S4, ESI†).

When the partially desodiated samples were mixed with Na_3PX_4 , only $\text{Na}_{0.5}\text{CrO}_2$ was observed to be compatible with Na_3PX_4 at RT (*i.e.*, no bulk reaction was observed in the XRD results, see Fig. 6a and b). All of the other partially desodiated samples reacted with the electrolyte, and some of the reactions were rather violent. For example, when partially desodiated NaNiO_2 was mixed with Na_3PX_4 in an Ar glove box, sparks were immediately generated and the powder color changed to dark red.

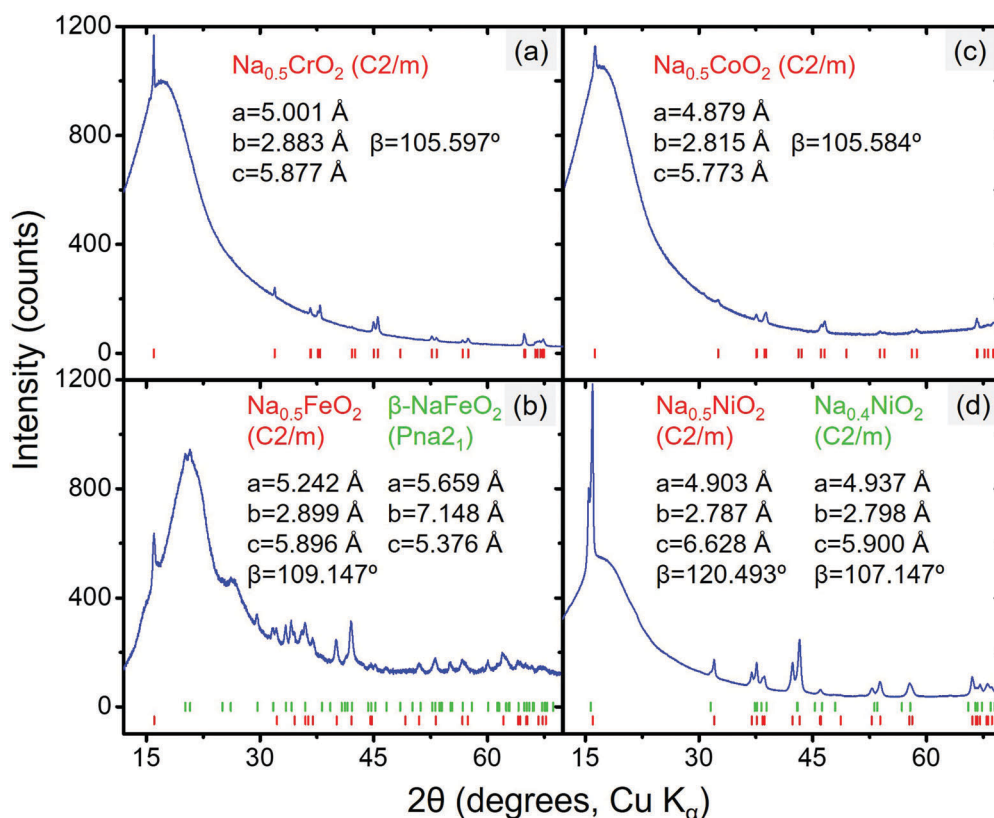


Fig. 5 Diffraction patterns of desodiated compound(s) of (a) NaCrO_2 , (b) NaFeO_2 , (c) NaCoO_2 , and (d) NaNiO_2 . The peak positions and refined structure data are also displayed; the hump at $\sim 15^\circ$ in all four figures originates from the Kapton sample holder (the diffraction pattern of the empty sample holder is presented in Fig. S3, ESI†).





Fig. 6 XRD results for reaction between (a) $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PS_4 and (b) $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PSe_4 at RT (25 °C) and 300 °C. DSC results for reaction between (c) $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PS_4 and (d) $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PSe_4 .

Because $\text{Na}_{0.5}\text{CrO}_2$ is the only compound compatible with Na_3PX_4 at RT among our observations, further studies with XRD and SDT at elevated temperatures were performed. In the XRD of mixed $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PX_4 , we observed that fully sodiated NaCrO_2 was regenerated after heating the mixture to 300 °C in reactions with both Na_3PSe_4 (Fig. 6a) and Na_3PS_4 (Fig. 6b), suggesting that Na is extracted from the Na_3PX_4 electrolyte and inserted into $\text{Na}_{0.5}\text{CrO}_2$, consistent with the thermodynamic anodic potentials predicted for the Na_3PX_4 electrolytes (2.25 V for Na_3PS_4 and 2.15 V for Na_3PSe_4), which are well below the $\text{Na}_{0.5}\text{CrO}_2$ voltage (~ 3.7 V vs. Na/Na^+).

This Na insertion to $\text{Na}_{0.5}\text{CrO}_2$ is similar to a self-discharge reaction, as often observed in rechargeable batteries, leading to decomposition of the electrolyte (*i.e.* Na_3PX_4). As shown in Fig. 2, S or Se is likely generated in the decomposition products by oxidizing Na_3PX_4 . In the reaction between $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PSe_4 , the generation of Se can indeed be observed in our differential scanning calorimetry (DSC) measurements (Fig. 6c), where an endothermic peak is observed at approximately 220 °C, corresponding to the melting point of Se (220.8 °C). The following exothermic peak is attributed to the heat generation of the bulk reaction. In contrast, the generation of S cannot be observed in the reaction between $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PS_4 . In the DSC result for the reaction between $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PS_4 in Fig. 6d, only one

exothermic peak is observed at approximately 260 °C reflecting the heat generation of the reaction.

The surface reaction at RT between $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PX_4 was investigated by X-ray photoelectron spectroscopy (XPS). After mixing $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PX_4 at RT, XPS measurements were performed on the Cr 2p peaks of the mixture. The Cr 2p reference peak positions in Cr^{3+} and Cr^{4+} were obtained by fitting the Cr 2p_{1/2} and 2p_{3/2} peaks in NaCrO_2 (Cr^{3+} only) and $\text{Na}_{0.5}\text{CrO}_2$ ($\text{Cr}^{3+}:\text{Cr}^{4+} = 1:1$), respectively (Fig. 7c and d). The XPS spectrum of the Cr 2p peaks in the mixture of $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PSe_4 is presented in Fig. 7b, and the fitting result indicates that the $\text{Cr}^{3+}/\text{Cr}^{4+}$ ratio changed from approximately 1.0 in $\text{Na}_{0.5}\text{CrO}_2$ to 2.423 in the mixed material (Table 3). The reduction of Cr^{4+} indicates an insertion of Na to $\text{Na}_{0.5}\text{CrO}_2$. This surface reaction between $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PSe_4 at RT cannot be detected in XRD (Fig. 6a), reflecting a slow kinetics and/or a self-passivation reaction mechanism. It is likely that the reaction products form a passivation layer and prevent further reaction, which explains why no bulk reaction is observed at RT in XRD. Based on the above discussion, the surface reaction is likely associated with the production of Se. As the temperature increases to the melting point of Se, the passivation layer becomes unstable and further reaction is activated, which is in good agreement with our observation in DSC (Fig. 6c). When $\text{Na}_{0.5}\text{CrO}_2$ was





Fig. 7 XPS spectra of Cr 2p from the surfaces of (a) mixture of $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PS_4 at RT (25°C), (b) mixture of $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PSe_4 at RT (25°C), (c) $\text{Na}_{0.5}\text{CrO}_2$, and (d) NaCrO_2 .

Table 3 XPS data fitting results for Cr 2p peaks

| Sample | Component | Peak position (eV) | | Area (a.u.) | | $\text{Cr}^{3+}/\text{Cr}^{4+}$ ratio |
|---|------------------|--------------------|------------|-------------|------------|---------------------------------------|
| | | $2p_{3/2}$ | $2p_{1/2}$ | $2p_{3/2}$ | $2p_{1/2}$ | |
| $\text{Na}_{0.5}\text{CrO}_2/\text{Na}_3\text{PS}_4$ | Cr^{3+} | 577.03 | 586.52 | 299 | 149 | 1.869 |
| | Cr^{4+} | 579.09 | 588.52 | 160 | 80 | |
| $\text{Na}_{0.5}\text{CrO}_2/\text{Na}_3\text{PSe}_4$ | Cr^{3+} | 577.03 | 586.52 | 344 | 172 | 2.423 |
| | Cr^{4+} | 579.09 | 588.52 | 142 | 71 | |
| $\text{Na}_{0.5}\text{CrO}_2$ | Cr^{3+} | 577.03 | 586.52 | 470 | 234 | 0.997 |
| | Cr^{4+} | 579.09 | 588.52 | 484 | 242 | |
| NaCrO_2 | Cr^{3+} | 577.03 | 586.52 | 661 | 331 | — |

mixed with Na_3PS_4 , a lower $\text{Cr}^{3+}/\text{Cr}^{4+}$ ratio increase (*i.e.* less Cr^{4+} reduction) was observed (Table 3), indicating that less Na was extracted from Na_3PS_4 in the reaction between $\text{Na}_{0.5}\text{CrO}_2$ and Na_3PS_4 . This observation is likely due to the slightly lower reactivity of Na_3PS_4 compared with Na_3PSe_4 , which is in line with the onset temperatures of the reaction between NaMO_2 and Na_3PX_4 (Table 2).

III. Compatibility between anode and electrolyte

The compatibility between the electrolyte and anode was investigated by cycling the Na/electrolyte/Na symmetric cells under a constant current density (typically 0.1 or 0.2 mA cm^{-2}). The symmetric cell was first galvanostatically cycled at 1 min per cycle. An increasing voltage during cycling is observed in Fig. 8a even at very low current density (0.1 mA cm^{-2}), suggesting an unstable metal/electrolyte interface. The cell failed after approximately 11.4 h of cycling, when Na_3PSe_4 was fully decomposed into amorphous phases (Fig. 8b), likely Na_3P and Na_2Se based on our DFT calculations (Fig. 2b). Thus, we conclude that Na_3PSe_4 is not compatible with a Na metal anode.

To improve the compatibility between the anode and electrolyte, a “ Na_2Sn ” alloy with higher potential ($\sim 0.3\text{ V vs. Na/Na}^+$) was synthesized. According to the Na–Sn binary phase diagram,^{72,73} the two stable phases near this composition are NaSn and Na_3Sn_4 , with the latter being the majority phase. The $\text{Na}_2\text{Sn}|\text{Na}_3\text{PSe}_4|\text{Na}_2\text{Sn}$ symmetric cell was galvanostatically cycled at 60 min per cycle. A relatively stable voltage during cycling at low current density (0.1 mA cm^{-2}) is observed in Fig. 9a, indicating enhanced interface stability. However, at a higher current density (0.2 mA cm^{-2}), the interface becomes unstable, and Na_2Se was observed after cycling for 40 h (Fig. 9b).

Because Na metal is reported to be incompatible with Na_3PS_4 forming Na_2S and Na_3P decomposition products,⁷⁴ consistent with our DFT calculation results shown in Fig. 2a, only the compatibility between the Na_2Sn anode and Na_3PS_4 was then investigated by cycling a $\text{Na}_2\text{Sn}|\text{Na}_3\text{PS}_4|\text{Na}_2\text{Sn}$ symmetric cell. A stable anode–electrolyte interface was obtained, signified by the approximately constant voltage during cycling at both low and high current densities (Fig. 10). We thus concluded that the “ Na_2Sn ” alloy is a promising anode candidate for use in solid-state batteries employing Na_3PS_4 solid electrolytes.

Discussion

We distinguish the pure electrochemical stability of the solid-state electrolyte at various Na chemical potentials (and in contact with Na reservoir) from the chemically-enhanced instability when solid-state electrolyte and cathode chemically interact. The pure electrochemical stability is relevant wherever the solid electrolyte is in contact with the electron reservoir. Hence this occurs at the cathode/electrolyte interface, at a direct contact with the current collector, or through the carbon network present in the electrode. Since Na^+ is highly mobile in the solid-state electrolyte, the conductor experiences the full chemical potential of Na applied at these electron contact interfaces. Computationally, we calculate the stability of the conductor in this condition by evaluating the thermodynamic grand potential of the compound under various applied Na chemical potentials, as described in prior work.³⁴ This analysis requires the availability of thermochemical information on a number of competing phases in the phase diagram of the conductor. Such information can for example be found in online resources such as the Materials Project.⁷⁵ This thermodynamic analysis for the electrochemical stability of the conductor provides





Fig. 8 (a) Electrochemical cycle for Na|Na₃PSe₄|Na symmetric cell; a short circuit (s/c) occurred after cycling for 11.4 h. (b) XRD results for Na₃PSe₄ before and after cycling for 12 h (1 min per cycle); the tick marks indicate Na₃PSe₄ peaks.

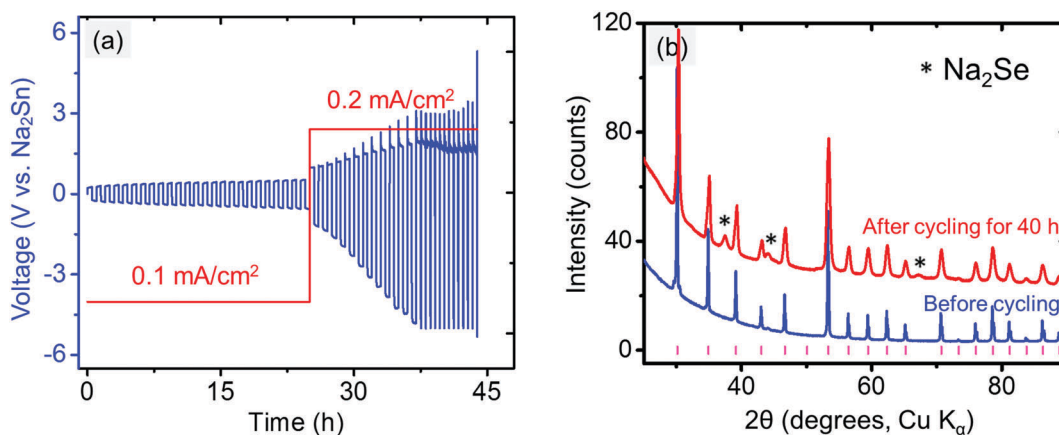


Fig. 9 (a) Electrochemical cycling of Na₂Sn|Na₃PSe₄|Na₂Sn symmetric cell. (b) XRD patterns of Na₃PSe₄ before and after cycling for 40 h (60 min per cycle); the tick marks indicate Na₃PSe₄ peaks.

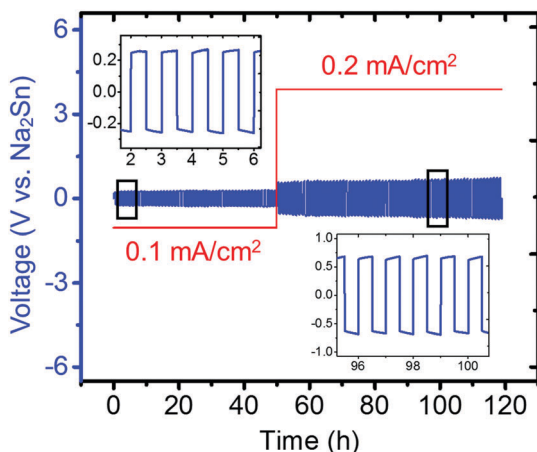


Fig. 10 Electrochemical cycling of Na₂Sn|Na₃PS₄|Na₂Sn symmetric cell (60 min per charge and discharge). The insets present zoomed-in voltage profiles during cycling from 2–6 h and 96–100 h.

a “safe” voltage window, in which there is no driving force at all for decomposition of the conductor. Because the thermodynamic decomposition of the conductor may sometimes require

complete bond breaking in the material to form multiple other phases, it may be kinetically inhibited at the operating temperature of the battery. Hence, we also provide a kinetic anodic stability limit by evaluating at which potential, Na⁺ can simply be extracted topotactically from the conductor together with the oxidation of the anion (S²⁻ or Se²⁻ in our case). Because the material is by definition a fast Na-ion conductor, and anion oxidation is easy, one expects there to be no kinetic barrier for this process. Hence, this topotactic Na extraction voltage can be considered an absolute upper bound for the voltage at which the conductor can operate. To test these computed stability limits we evaluated the conductor as an electrode in an electrochemical cell using liquid electrolyte so that contact problems, often present in full solid state devices, will not mask instabilities. The computational and experimental results summarized in Table 4 clearly indicate that the measured upper voltage limit lies between the thermodynamic upper voltage and the topotactic Na extraction limit, in agreement with our understanding. Table 4 also clearly shows that CV is a poor tool to measure electrochemical stability of solid-state conductors. The poor reliability of CV measurements has led for example to claims that some sulfide conductors have 5 V or even 10 V stability,^{18,32,76,77}



Table 4 Comparisons of the various stability windows obtained theoretically and experimentally for Na₃PX₄

| | Thermodynamic window (V) | Kinetic upper limit (V) | Experimental (liquid cell charging) upper limit (V) | Experimental (CV measurement) upper limit (V) |
|----------------------------------|--------------------------|-------------------------|---|---|
| Na ₃ PS ₄ | 1.55–2.25 | 3.05 | 2.50 | > 5 V ³² |
| Na ₃ PSe ₄ | 1.80–2.15 | 2.75 | 2.33 | 2.6 V ^a |

^a Data shown in Fig. S6 (ESI).

which is counterintuitive, given that a sulfide ion can in general be oxidized between 2–3 V.

In contact with the cathode, the conductor (*i.e.*, solid-state electrolyte) can also undergo chemical reactivity. To determine this reactivity, we used a combination of XRD, SDT and XPS to evaluate the reaction products in mixed cathode/electrolyte powders. Through the study of more than 20 cathode/electrolyte reactions between layered Na transition metal oxides (NaMO₂, M = Cr, Mn, Fe, Co, Ni) and two solid electrolytes (Na₃PX₄, X = S, Se), we were able to determine trends and understand the mechanisms behind these reactions. We first determine the thermodynamic driving forces and end-products of the cathode/electrolyte reaction, and then discuss what may happen under more kinetically constrained conditions. There are some common trends that can be understood from Table 1:

(1) On the cathode/conductor interface P strongly prefers bonding to O, resulting in the exchange of O and S/Se between the cathode and conductor, and the formation of PO₄ groups. As a result, Na₃PO₄ is produced for all reactions listed in Table 1.

(2) Some transition metals, even in the discharged redox state can oxidize the chalcogenide anion leading to reaction products that are metallic, have per-sulfide or per-selenide ions, or even sulfate ions. This is the case for the NaFeO₂ and NaNiO₂ cathodes against both conductors and for the NaCoO₂ cathode against the selenide conductor. The fact that the NaCoO₂ seems redox stable with the sulfide but not with the selenide is likely due to the fact that the Se²⁻ ion is easier to oxidize than S²⁻.

Once the cathodes are charged (bottom part of Table 1) oxidation of the anion by reduction of the transition metal is favorable for all cathode/conductor couples, and only local passivation with an electron-insulating layer will protect the conductor. The reaction products that form at the interface are however dependent on chemistry of each cathode. In some cases, elemental S is predicted to occur (*e.g.* Na_{0.5}CrO₂ with Na₃PS₄) while for other cathode/conductor couples reduced metal sulfides are usually predicted (MnS, FeS₂, *etc.*). The reaction products for the Co and Ni cathode deserve particular attention. Compounds such as Ni₉S₈ and Co₉Se₈ are in the pentlandite family and have a structure containing an excess of metal atoms and short metal-metal distance.^{78,79} Similar metal-metal bonding also exists in other metal-rich chalcogenides such as Ni₃S₂.^{80,81} These compounds are metallic and hence will not provide any passivation protection.

Though it is useful to understand the thermodynamic end-points of the cathode/conductor reaction as shown in Table 1, comparison with the experimentally observed products clearly indicates that these phases do not always form, as would be expected under conditions where kinetics may be limited.

First, when the electrode and electrolyte are in contact, arbitrary amounts of these phases can react, forming an interface layer of decomposition products that can take on, in principle any average composition between the cathode and electrolyte composition depending on the ratio in which they react. This renders many possible reaction pathways plausible. In our previous modeling approach, a mixing parameter x ($0 < x < 1$) between the electrode and electrolyte was introduced in our calculations.³⁴ By scanning a range of x from 0 to 1, we calculated the reaction enthalpies for all possible reactions and determined the mostly likely reaction as the one with the largest thermodynamic driving force. This approach was largely successful in predicting the decomposition products between electrodes and electrolytes, and indeed, many of the predictions have recently been verified by experiments.^{48,82–84} However, it is important to keep in mind that in principle all reactions with positive driving force can take place spontaneously, and which ones occur first depends on their kinetics. To make a broader comparison with future experiments possible we have listed in Table S1 (ESI[†]) possible reaction products that can be formed for each cathode/electrolyte couple. Given these constraints, it is remarkable that many of the experimentally observed products are the ones predicted in the thermodynamic calculations.^{82,85} This finding may result from the very thin interface layer (nanometer scale) formed, requiring only very short diffusion lengths.

Several of the experimental products we observed can be explained by adding at least a qualitative layer of kinetic constraints on top of the predictions. For example, in the reaction between NaCrO₂ and Na₃PS₄, the theoretically predicted product (Na₃PO₄) was not observed at temperatures below 700 °C. Instead, the intermediate Na₃PS₃O was formed at lower temperatures, which may be thought of as an intermediate towards the exchange of S and O in the conductor.

One reaction that however cannot be kinetically limited is the exchange of Na ions between the electrolyte and cathode. As a result, cathodes that are charged above the anodic voltage limit of the conductor will always extract Na from the solid-state electrolyte, at which point the electrolyte will degrade and decompose. This concept rationalizes our experimental observation when Na_{0.5}CrO₂ and Na₃PSe₄ come in contact. The results in Table 1, assuming diffusion is not limited, predicted the formation of Na_{1/3}(CrSe₂), Na_{2/3}(CrSe₂), and Na₃PO₄ decomposition products. However, experimentally a more limited reaction is observed whereby Na is extracted from the electrolyte, causing electrolyte decomposition, and producing fully sodiated NaCrO₂.

In the two cases discussed above, instead of taking the reaction pathway with the largest thermodynamic driving force, which involves diffusion and rearrangement of elements, a reaction



via anion and Na exchange processes is observed. This finding is not surprising as reactions involving well-known mobile species (*e.g.*, Na⁺) are fast and kinetically favored. Overall, in the analysis of electrode/electrolyte reactions, our results suggest that in addition to the ones with the largest driving forces, other reactions with similar thermodynamic driving forces but faster kinetics (*e.g.*, topotactic Na extraction/insertion) should also be considered in electrode/electrolyte reactions.

With the driving forces that may degrade the cathode/electrolyte interface better understood, one can develop strategies to alleviate these issues. The anion-exchange reaction is mainly driven by the tendency to form the stable phosphate group. Therefore, this type of reaction may be prevented by fully or partially replacing P in the solid electrolytes with other suitable elements that do not exhibit strong bonding preference with O, such as Sb, Ge, Sn, or As. Interestingly, recent studies suggest that a NaCrO₂ cathode can be cycled reversibly using a Na₃SbS₄ solid-state electrolyte, indicating that replacing P with Sb in the sulfide electrolyte resulted in improved compatibility with the oxide cathode.^{16,19,42} We expect that a similar effect will be observed for Na₄SnS₄,⁸⁶ Li₄SnS₄,⁸⁷ Li₄GeS₄,⁸⁸ Li₃AsS₄,⁸⁹ and similar materials. Another possible strategy to prevent the anion exchange is to use polyanion cathodes with stable anion groups such as PO₄. Since the O is already in a stable configuration, it is unlikely to participate in the anion exchange reaction. Changing from an oxide-based cathode to a sulfide-based cathode will also mitigate the interface issue, although sulfide-based cathodes will operate at a lower voltage than their oxide counterparts, thus reducing the overall energy density of the batteries. The redox degradation pathway requires transition metal reduction in the cathode. While this seems inevitable in a charged cathode, it may be preventable in the discharged cathode by selecting transition metals that are difficult to reduce (*e.g.*, Cr³⁺, Mo³⁺, V³⁺, Nb³⁺ and Ti³⁺). The thermodynamic stability requirement between the conductor and discharged cathode is often more stringent as processing of a solid-state battery may bring this system to elevated temperature. This is not the case for the charged cathode which is usually only exposed to the conductor during room temperature operation.

Although one always has the option to coat the electrode to protect it chemically from the electrolyte,^{38,39,90} we believe that passivating solid-state electrolytes is equally important and should be explored in future studies. Because the coating is a thin layer, it has less stringent requirements for ionic conductivity than for the bulk electrolyte. This allows many more materials choices than for bulk electrolytes, making the selection of a chemically and electrochemically stable coating material more likely.³⁷ Coating only the cathode still exposes the electrolyte to electronic pathways created by carbon in the cathode. According to our electrolyte stability testing results, it is clear that electronic pathways promote the decomposition of the electrolyte *via* the extraction of Na⁺ and oxidation of the anion in the conductor. Therefore, the electrode coating method only solves the cathode/electrolyte interface problem and cannot prevent electrolyte decomposition at voltages beyond its stability window. This issue might not be critical for the cell initially,

especially when the cell is cycled at a very high rate, because breakdown of the electrolyte at places other than the cathode interface will initially not degrade cell operation. However, this issue is likely to be detrimental for the long-term cyclability of all-solid-state batteries. We believe that electrolyte coating provides a more effective approach to prevent both electrolyte decomposition and electrolyte/electrode reaction.

Conclusion

We presented a methodology that combines computational and experimental tools to investigate the compatibility between solid electrolytes and electrodes. Relatively simple and rapid XRD and SDT experiments were proven to be very effective in describing the interfacial reactions between electrolytes and electrodes. By applying our method to the Na solid-state system, we were able to determine the voltage windows of the electrolytes (both the thermodynamic-driven lower bound and kinetic-stabilized upper bound), understand the thermodynamics and kinetics behind the reactions between incompatible electrolyte/electrode pairs, and select the most stable components (NaCrO₂/Na₃PS₄/Na–Sn) within our chemical space for an all-solid-state battery. We believe that these data provide crucial information for new solid electrolyte design and electrolyte/electrode interfacial modification and serve as an essential guide for integrating these components. The methodology and insights obtained in this study can also be applied to other electrochemical systems of interest, such as Li-ion solid-state batteries.

Experimental

Synthesis of NaMO₂

All the NaMO₂ cathode materials were prepared by solid-state synthesis. Stoichiometric amounts of the precursors (typically ~1.0 g) were mixed by ball milling (tungsten carbide ball mill jar, Spex 8000 M mixer per mill) and pressed into 1/2-in pellets. The pellets were then placed in alumina boats and heated at a rate of 10 °C min⁻¹ in appropriate atmospheres until the reaction was completed. The corresponding precursors and heating conditions are listed in Table S2 (ESI[†]). The samples (except NaMnO₂) were cooled to 150 °C at a rate of 30 °C min⁻¹ and immediately transferred to an Ar glovebox. NaMnO₂ was quenched to RT after synthesis and then immediately transferred to an Ar glovebox.

Synthesis of Na₃PX₄

Na₂X (X = S, Se, Alfa Aesar, 99.8%), red phosphorus (Sigma-Aldrich, ≥99.99% trace metal basis), and S/Se (Sigma-Aldrich, 99.99% trace metal basis) powder were mixed in a stoichiometric ratio in an Ar-filled glovebox. The mixture of the three compounds was then loaded into a BN tube (3 mm inner diameter and 4 mm outer diameter). The tube was wrapped with Al foil and sealed with a stainless steel Swagelok cap (3/8 in) at the open end. The synthesis was performed in a sealed alumina tube furnace, which was purged with Ar gas for 20 min, rapidly ramped to 300 °C within 10 min, and held at the same



temperature for 16 h for the reaction. Continuous Ar gas with a flow rate of $\sim 30 \text{ mL min}^{-1}$ flowed into the sealed furnace during the entire synthesis process. The final products were collected after the furnace was naturally cooled down to RT and were immediately transferred into the glovebox.

Synthesis of chemically desodiated $\text{Na}_{0.5}\text{MO}_2$

Synthesized pristine NaMO_2 powder, over-stoichiometric (ten-fold excess) iodine (GSS, 99.8%, beads), and $\sim 15 \text{ mL}$ of acetonitrile (Sigma-Aldrich, 99.8%, anhydrous) were placed in a glass sample vial containing an octagonal magnetic stirring bar. After being wrapped with Al foil to prevent light exposure, the sealed vial was placed on a stirrer and stirred at a speed of 1200 rpm in a Ar glovebox for 4 days. The solution was then centrifuged at 5000 rpm for 7 min. The solid residue was separated from the supernatant and washed with acetonitrile ~ 6 times until no iodine was observed in the solvent. After drying in the vacuum chamber of the Ar glovebox for $\sim 12 \text{ h}$, the final product was transferred into the glovebox and ground into a powder for further characterization.

Experimental characterization

XRD analysis was performed using a Rigaku Miniflex diffractometer and Cu K α radiation. The powder sample was first sealed into a Kapton tube (0.9 mm in diameter, Cole Parmer) in the glovebox and then characterized in the diffractometer, which was equipped with a capillary stage to limit air exposure.

SDT measurements were performed using a TA Instruments SDT Q600. Approximately 15 mg of the powder sample was first placed into an alumina sample pan in the glovebox. The filled pan was then placed on the pre-tared cantilever of the analyzer. SDT standard measurements were then performed under continuous Ar flow with a flow rate of 100 mL min^{-1} . The measurement procedure usually involves heating and cooling processes. After equilibrating at $25 \text{ }^\circ\text{C}$, the sample was heated to the set temperature at a heating rate of $5 \text{ }^\circ\text{C min}^{-1}$. The temperature was held for at least 1 h to complete the reaction before cooling was initiated at a rate of $2 \text{ }^\circ\text{C min}^{-1}$. The sample was rapidly transferred to the glovebox after measurement for further characterization.

The working electrode composites were prepared by mixing the synthesized Na_3PX_4 powder, carbon black, and poly(tetrafluoroethylene) (PTFE) in a weight ratio of 80:15:5 with a mortar and pestle in an Ar glovebox. This powder mixture was rolled into a thin film using a stainless steel plate and roller. Circular disks of 5/16-in diameter were then punched with a loading of approximately 3–5 mg. These electrodes were assembled into Swagelok cells with Na metal as the counter electrode and 1 M NaPF_6 in a 1:1 (volumetric ratio) ethylene carbonate/diethyl carbonate (EC/DEC) solvent mixture as the liquid electrolyte. Two glass fiber separators were used in the cells. The charging and discharging of the Swagelok cells were performed with an Arbin battery cycler.

Cyclic voltammetry measurements were conducted to investigate the electrochemical stability window of the solid electrolyte Na_3PSe_4 . A platinum foil as the working electrode and a

sodium foil as the counter electrode were attached to each face of the pellet. The potential sweep was performed by using a potentiostat/galvanostat device with a scanning rate of 5 mV s^{-1} at room temperature.

XPS measurements were performed on a PHI 5400 ESCA/XPS system with a monochromatic Al K α X-ray source. The powder samples were mixed with PTFE binder (5 wt%) and rolled into thin films in the Ar glovebox. The films were transferred into the XPS system and cleaned using Ar ion milling (3 kV, 25 mA) to remove surface-absorbed C and O. The core-level spectra were fitted using the commonly applied Gaussian peak shapes and Shirley background correction to extract the transition metal valence states based on the ratio of scaled peak areas.

Computational

The calculations for voltage and interfacial stability generally followed the methodology described in greater detail in ref. 34.

Phase diagrams and bulk energies

Zero Kelvin phase diagrams were constructed using the pymatgen software package⁹¹ and a database of DFT-computed bulk phase energies of materials with crystal structures obtained from the Inorganic Crystal Structure Database (ICSD)⁹² or generated by applying data-mined chemical substitutions.⁹³ To obtain these bulk energies, we employed DFT within the projector augmented wave (PAW) formalism⁹⁴ using the generalized gradient approximation (GGA)⁹⁵ to the exchange–correlation energy as implemented in the Vienna ab initio simulation package (VASP)⁹⁶ to calculate the formation energy of each electrolyte from the nearest phases present in the NIST-JANAF⁹⁷ or Kubaschewski⁹⁸ thermochemical tables or from the elements. To treat the sulfides and selenides equally, we added the formation energy of Na_2Se to this dataset.⁹⁹ We uniquely define the nearest phases as those that define the Gibbs triangle (the low-energy facet) containing the desired composition in the phase diagram. As a result of this methodology, the formation energy input to the phase diagram calculation is exactly the experimentally determined enthalpy for compounds that are present in these thermochemical tables. For other compounds, we use the sum of the experimental formation enthalpies of the nearby phases and the DFT calculated reaction energy from these nearby phases to form the compound of interest. This reduces the formation energy error by minimizing electron transfer in the DFT calculated reactions.

For all the VASP calculations, a cutoff energy of 520 eV and a k -point grid of at least 500 per number of atoms were used. We applied the mixing scheme of Jain *et al.*¹⁰⁰ to combine GGA calculations with/without the rotationally invariant Hubbard (+U) correction^{101,102} to properly treat insulators and metals.

Voltage stability calculations

To calculate the voltage stability of each electrolyte, we calculated the range of Na chemical potential (μ_{Na}) over which each electrolyte was observed to be on the convex hull and therefore



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