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Phase transition engineering to break the symmetry of diamond-like chalcogenide for second-order nonlinear optics†

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Temperature-induced phase transitions offer a promising route to engineer nonlinear optical materials, particularly for infrared applications where conventional design approaches face fundamental limitations. Herein, a temperature-induced centrosymmetric (CS) to noncentrosymmetric (NCS) irreversible phase transition strategy was employed to successfully prepare a novel NCS diamond-like (DL) chalcogenide, β -Ag₄P₂S₇, which was derived from the CS phase α -Ag₄P₂S₇ transformation. Structural analysis reveals that this transformation involves a reorganization of [Ag₂PS₄]²⁻ layers from an AA'AA' to AA'A"AA'A" stacking pattern, facilitated by bridging [Ag₁S₄]⁷⁻ tetrahedra. β -Ag₄P₂S₇ has exceptional IR NLO properties, including a strong phase-matchable second-harmonic generation (SHG) response (1.02 × AgGaS₂) and a wide band gap of 2.90 eV (the largest one in ternary Ag-based DL chalcogenides), which balances excellent NLO response with a wide band gap. Further structure–property relationship analyses show that superior NLO properties and band gap broadening of β -Ag₄P₂S₇ mainly originate from the alteration of the [Ag₂PS₄]²⁻ layer stacking configuration, which is driven by a temperature-induced irreversible phase transition. This work not only presents a new paradigm for designing high-performance NLO materials through phase transitions but also significantly advances the potential of temperature-mediated crystal engineering for optical applications.

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Introduction

Inorganic infrared (IR) second-order nonlinear optical (NLO) materials are essential for all-solid-state laser systems, playing a crucial role in long-distance laser communication, laser diagnostics, quantum optics research, and environmental monitoring.^{1–10} These materials enable efficient frequency conversion by generating coherent light in regions of the electromagnetic spectrum that are difficult to cover. To achieve

high-performance frequency conversion, an ideal IR NLO material must possess a strong NLO effect ($>0.5 \times \text{AgGaS}_2$), a wide band gap to improve the laser damage threshold (LDT), and stable physicochemical properties conducive to bulk crystal growth. However, a fundamental challenge in material design lies in balancing a wide band gap with a strong NLO response, as enhancing one property often compromises the other.

The design of IR NLO crystals with outstanding NLO performance hinges on achieving a noncentrosymmetric (NCS) crystal structure, an essential yet highly challenging prerequisite.^{11–15} Molecular engineering strategies, which focus on the selection of functional motifs and spatial optimization of NLO-active chromophores, have been extensively employed to develop novel NCS crystals. Traditional approaches for constructing NCS structures often rely on the partial substitution of elements or functional motifs within the CS structure^{16–20} (e.g., CS: RbGaS₂ to NCS: [ABa₂Cl][Ga₄S₈] (A = Rb, Cs);²¹ CS: Rb₄P₂S₆ to NCS: RbBiP₂S₆;²² CS: ZnS to NCS: M[M₄Cl][Ga₁₁S₂₀] (M = A/Ba, A = K, Rb)).²³ However, these methods frequently introduce structural and functional complexity that hinders the simultaneous optimization of the band gap and NLO properties. Notably, strong second-harmonic

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nic generation (SHG) effect is often accompanied by a narrowing of the band gap, presenting a fundamental challenge in material design.

Overcoming this limitation requires innovative strategies to break centrosymmetry while maintaining a wide band gap. One of the promising approaches is phase transition engineering, which enables the formation of NCS structures through gradual structural modifications driven by high energy barriers. This method stabilizes metastable phases and generates diverse coordination environments for structural ligands under external stimuli such as temperature, pressure, or atmospheric changes.^{24,25} By leveraging phase transitions rather than chemical substitution, this strategy provides a more straightforward and controllable route to designing NCS materials.

Phase transitions can be classified as reversible and irreversible. Reversible phase transitions are predominantly explored in organic material systems, where they enable cyclic regulation of NLO switching function.^{26,27} In contrast, inorganic compounds tend to undergo irreversible phase transitions due to their high thermodynamic stability ($\Delta G < 0$) and significant phase transition barrier (>2 eV).^{28,29} Such irreversible transitions offer key advantages: they not only facilitate the growth of large-size single crystals *via* the Bridgman-Stockbarger method, but also enhance the structural and optoelectronic stability of devices under extreme operating conditions, such as temperature fluctuations, mechanical stress, and radiation environment.

In chalcogenides, even minor rearrangements of the tetrahedral ligands in diamond-like (DL) structures can induce phase transitions, leading to significant modification in crystal structures. For instance, $\text{Cu}_2\text{ZnSiS}_4$ undergoes a transition between the α -phase ($Pmn2_1$) and the β -phase (Pn),³⁰ and Ga_2Se_3 exhibits multiple transitions (α : $F\bar{4}3m$; β : Cc ; γ : $F\bar{4}3m$; σ : $C222_1$).³¹ Additionally, Ag^+ cations, possessing a d^{10} closed-shell configuration, can couple filled d orbitals and empty s orbitals of similar energy due to the second-order Jahn-Teller (SOJT) effect, lowering the energy barriers, which is easily overwhelmed by thermal perturbations.^{32–34}

Building upon those insights, we propose a high-temperature-induced irreversible phase transition strategy to construct an NCS chalcogenide based on the ternary Ag/P/S system. This approach successfully led to the transformation of CS $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$ into a novel NCS phase, $\beta\text{-Ag}_4\text{P}_2\text{S}_7$, both of which adopt DL structures. The synthesis, crystal structures, phase transitions, NLO properties, and structure-property relationship were systematically investigated. The resulting $\beta\text{-Ag}_4\text{P}_2\text{S}_7$ exhibits a strong and phase-matching SHG response ($1.02 \times \text{AgGaS}_2$), a wide band gap (2.9 eV), large birefringence ($\Delta n = 0.045$), and excellent thermal/chemical stability. Moreover, the ternary Ag/P/S system offers significant advantages over quaternary or quinary systems, particularly in terms of large-scale crystal growth. Its relatively simple composition facilitates better control over crystallization processes, making it a highly attractive platform for developing next-generation IR NLO materials.

Results and discussion

The synthesis of DL centrosymmetric $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$ can be found in the ESI,[†] and the crystal structure of $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$ is the same as that in the reference.³⁵ The structure of $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$, although previously reported, still needs to be analyzed for better comparison with that of $\beta\text{-Ag}_4\text{P}_2\text{S}_7$. Single-crystal X-ray diffraction indicates that $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$ crystallizes into the space group $C2/c$ (no. 15) (ESI Table S1[†]). Its asymmetric unit consists of two Ag, one P, and four S atoms, all of which are located at the Wyckoff position of 8f except S2 at 4e (Table S2[†]). The structure of $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$ is composed of the $[\text{Ag}_1\text{S}_4]^{7-}$ tetrahedra with $d(\text{Ag-S}) = 2.538(3)\text{--}2.876(3)$ Å, $[\text{Ag}_2\text{S}_4]^{7-}$ tetrahedra with $d(\text{Ag-S}) = 2.522(3)\text{--}2.719(3)$ Å, and the $[\text{PS}_4]^{3-}$ tetrahedra with $d(\text{P-S}) = 2.006(4)\text{--}2.119(3)$ Å (Table S3 and Fig. S1[†]), which are in accordance with those of related compounds.^{36–38} Specifically, $[\text{Ag}_2\text{S}_4]^{7-}$ tetrahedra are interconnected *via* corner-sharing to form one-dimensional (1D) $[\text{Ag}_2\text{S}_3]^{5-}$ chains, which are further bridged by isolated $[\text{P}_2\text{S}_7]^{4-}$ dimers consisting of two $[\text{PS}_4]^{3-}$ tetrahedra constructed by corner-sharing to construct two-dimensional (2D) $[\text{Ag}_2\text{PS}_4]^{2-}$ layers (Fig. 1a). The $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$ features three-dimensional (3D) anionic networks composed of $[\text{Ag}_2\text{PS}_4]^{2-}$ layers and $[\text{Ag}_1\text{S}_4]^{7-}$ tetrahedra interconnected by the sharing of S atoms. Remarkably, $[\text{Ag}_2\text{PS}_4]^{2-}$ layers can be viewed as reverse orientations stacked alternately in an AA' AA'... manner in the *ac* plane, incurring cancellation of their hyperpolarizabilities (Fig. 1b).

The thermal behavior of $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$ was studied by differential scanning calorimetry (DSC) measurements (Fig. 2a). It showed three absorption peaks at 421 °C, 463 °C, and 558 °C, and only one exothermic peak at 490 °C during the entire heating and cooling process. In addition, to gain a comprehensive insight into the relationship between the phase transitions and temperatures, a series of solid-state reactions at different calcination temperatures was performed in sealed silica tubes (Fig. 2b) based on the DSC results. For $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$, it is stable until 420 °C. Phase transition begins at 420 °C. The β -phase content increases progressively between 420–570 °C. Notably, $\text{Ag}_7\text{P}_3\text{S}_{11}$ emerges as a byproduct through peritectic reaction with the melt (Fig. S2[†]).³⁹ When the temperature exceeds 570 °C, a pure phase of $\beta\text{-Ag}_4\text{P}_2\text{S}_7$ is obtained. When the temperature begins to decrease, the $\beta\text{-Ag}_4\text{P}_2\text{S}_7$ fails to transform into the $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$, indicating the irreversible phase transition. Once the irreversible phase transition occurs, the system will move towards more stable thermal properties, leading to a decrease in the free energy, implying that the new phase $\beta\text{-Ag}_4\text{P}_2\text{S}_7$ is resistant to thermal perturbations and can maintain the stability of the phases and properties over a certain temperature range. In addition, irreversible phase transitions may lead to significant changes in the energy band structure of the material, such as an increase or decrease in the band gap. It is therefore necessary to probe the band gap of $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$, which has an absorption edge at 430 nm (Fig. S3[†]) and a band gap of about 2.65 eV (Fig. 2c), which fits well with the yellow color of the crystals.

Single-crystal XRD analysis indicates that $\beta\text{-Ag}_4\text{P}_2\text{S}_7$ crystallizes in the trigonal chiral space group $P3_21$ (no. 154) (cell

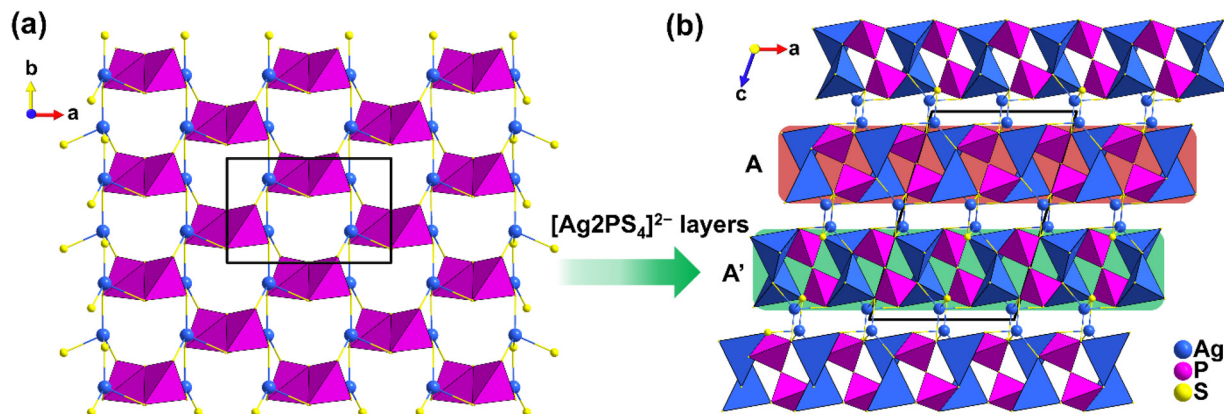


Fig. 1 (a) 2D $[\text{Ag}_2\text{PS}_4]^{4-}$ layer in $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$; (b) crystal structure along the b -axis of $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$.

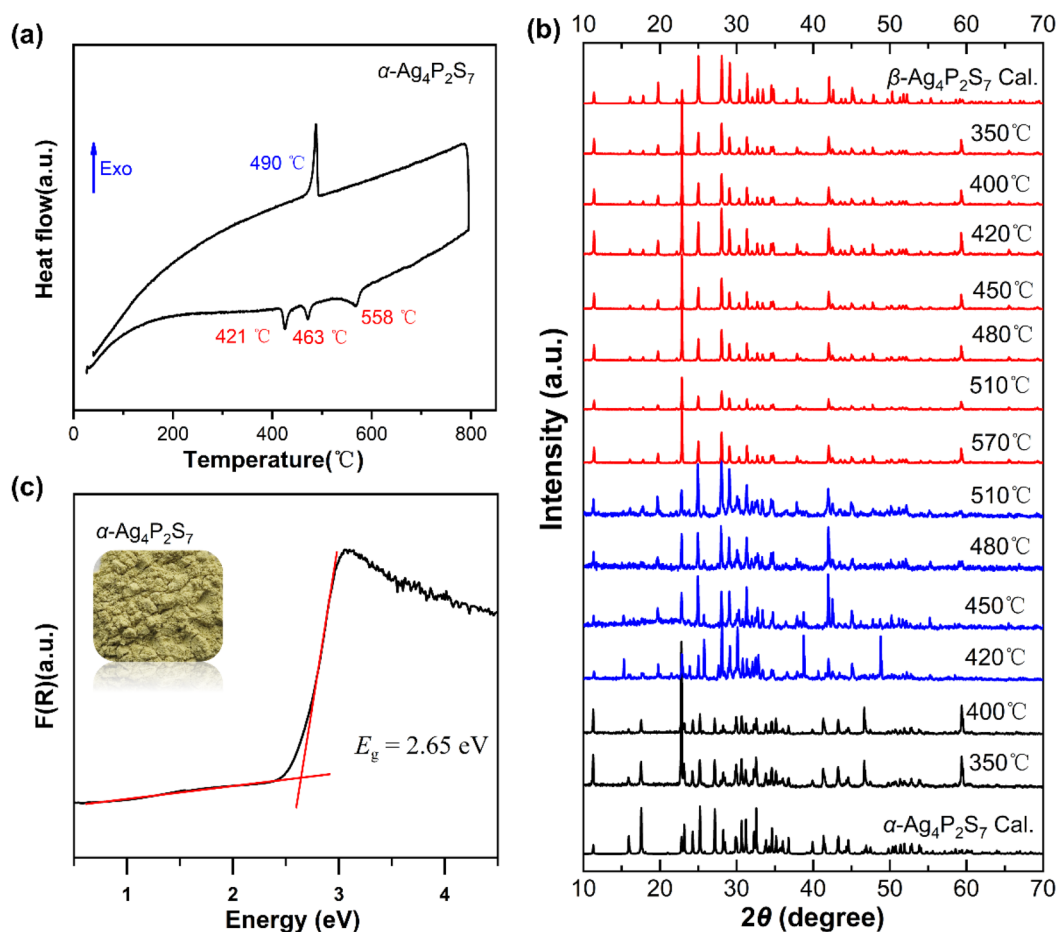


Fig. 2 (a) DSC curve of the $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$; (b) the variable-temperature powder X-ray diffraction patterns of the $\text{Ag}_4\text{P}_2\text{S}_7$; (c) E_g of $\alpha\text{-Ag}_4\text{P}_2\text{S}_7$.

parameters: $a = b = 6.3563(5)$, $c = 23.3477(18)$ Å and $Z = 3$). The energy-dispersive spectroscopy (EDS) measurement corroborated the homogenous distribution of Ag/P/S with an approximate molar ratio of 4 : 2 : 7 (Fig. S4†). Its asymmetric unit also consists of two crystallographically independent Ag atoms, one P atom, and four S atoms, all at the Wyckoff position 6c except

S2 at 3a (Table S4†). It is found that the structure of $\beta\text{-Ag}_4\text{P}_2\text{S}_7$ is composed of the typical $[\text{Ag}_4\text{S}_{12}]^{7-}$ tetrahedra with $d(\text{Ag-S}) = 2.51(3)\text{--}2.882(3)$ Å, $[\text{Ag}_2\text{S}_4]^{7-}$ tetrahedra with $d(\text{Ag-S}) = 2.526(3)\text{--}2.812(3)$ Å, and the $[\text{PS}_4]^{3-}$ tetrahedra with $d(\text{P-S}) = 1.996(3)\text{--}2.123(3)$ Å (Table S5 and Fig. S1†), which are in accordance with those of related compounds.^{36–38} The crystal structure of

β - $\text{Ag}_4\text{P}_2\text{S}_7$ is shown in Fig. 3b and can be regarded as 3D anionic networks consisting of 2D $[\text{Ag}_2\text{PS}_4]^{2-}$ layers and $[\text{Ag}_1\text{S}_4]^{7-}$ tetrahedra, which are interconnected by sharing S atoms. Similar to α - $\text{Ag}_4\text{P}_2\text{S}_7$, the $[\text{Ag}_2\text{PS}_4]^{2-}$ layers of β - $\text{Ag}_4\text{P}_2\text{S}_7$ are bridged by 1D $[\text{Ag}_2\text{S}_3]^{5-}$ chains of $[\text{Ag}_2\text{S}_4]^{7-}$ tetrahedra linked by corner-sharing and isolated $[\text{P}_2\text{S}_7]^{4-}$ dimers constructed from two $[\text{PS}_4]^{3-}$ tetrahedra *via* corner-sharing (Fig. 3d). Different from α - $\text{Ag}_4\text{P}_2\text{S}_7$, however, $[\text{Ag}_2\text{PS}_4]^{2-}$ layers adopt a more complex alternating stacking manner, *i.e.*, AA'A''..., leading to a superposition of microscopic SHG coefficients and macroscopically enhancing the NLO effect. So, a larger unit cell is necessary for β - $\text{Ag}_4\text{P}_2\text{S}_7$. In addition, the bond valence calculations resulted in values of 0.96–1.05 for the Ag^+ cation, 5.26 for the P^{5+} cation, and 1.97–2.13 for the S^{2-} anion (Table S4†). All of these are consistent with their respective ideal oxidation states.

Further structural comparisons of α - and β - $\text{Ag}_4\text{P}_2\text{S}_7$ were performed to gain insight into the phase transition behavior (Fig. 3). The density of high-temperature phase β - $\text{Ag}_4\text{P}_2\text{S}_7$ (4.377 g cm^{-3}) is lower than that of low-temperature phase α - $\text{Ag}_4\text{P}_2\text{S}_7$ (4.381 g cm^{-3}), which is consistent with the principle of thermal expansion and contraction. Moreover, the unit cells gradually decrease from α - to β - $\text{Ag}_4\text{P}_2\text{S}_7$, that is, $a_{(\alpha)} =$

$10.7634(8) \text{ \AA} \approx 1.69 \times b_{(\beta)}$, $b_{(\alpha)} = 6.5280(4) \text{ \AA} \approx b_{(\beta)}$, and $c_{(\alpha)} = 23.3477(18) \text{ \AA} \approx 0.69 \times c_{(\beta)}$. As shown in Fig. 3a and b, along the a -axis, the α - $\text{Ag}_4\text{P}_2\text{S}_7$ unit cell can accommodate two $[\text{P}_2\text{S}_7]^{4-}$ dimers, while that of β - $\text{Ag}_4\text{P}_2\text{S}_7$ can only accommodate one $[\text{P}_2\text{S}_7]^{4-}$ dimer. Along the c -axis, the unit cell of α - $\text{Ag}_4\text{P}_2\text{S}_7$ can accommodate two $[\text{P}_2\text{S}_7]^{4-}$ dimers, whereas that of β - $\text{Ag}_4\text{P}_2\text{S}_7$ can accommodate three $[\text{P}_2\text{S}_7]^{4-}$ dimers. Those indicate that the phase transition from α - to β - $\text{Ag}_4\text{P}_2\text{S}_7$ has an abnormal anisotropic thermal expansion, such as contraction along the a direction and expansion along the c direction. In addition, the Ag1–S distances of in the $[\text{Ag}_1\text{S}_4]^{7-}$ bridges of β - $\text{Ag}_4\text{P}_2\text{S}_7$ (2.551–2.882 $\text{\AA}$) are longer than the Ag1–S distances of α - $\text{Ag}_4\text{P}_2\text{S}_7$ (2.538–2.876 $\text{\AA}$) (Fig. S5†), facilitating the rotation of the $[\text{Ag}_2\text{PS}_4]^{2-}$ layer and constructing to NCS structure accompanied by a significant SHG response. Intriguingly, the $[\text{Ag}_2\text{PS}_4]^{2-}$ layer shows a higher symmetry of the 3_2 screw axis in β - $\text{Ag}_4\text{P}_2\text{S}_7$ compared to the 2-fold axis in α - $\text{Ag}_4\text{P}_2\text{S}_7$ (Fig. 3c and d). As can be seen in Fig. 3e and f, the spatial symmetry operation increases from four (in α - $\text{Ag}_4\text{P}_2\text{S}_7$) to six (in β - $\text{Ag}_4\text{P}_2\text{S}_7$).

The microstructural characteristics of a material, such as atomic arrangement, crystal structure, phase composition, *etc.*, fundamentally determine the material's various physical and

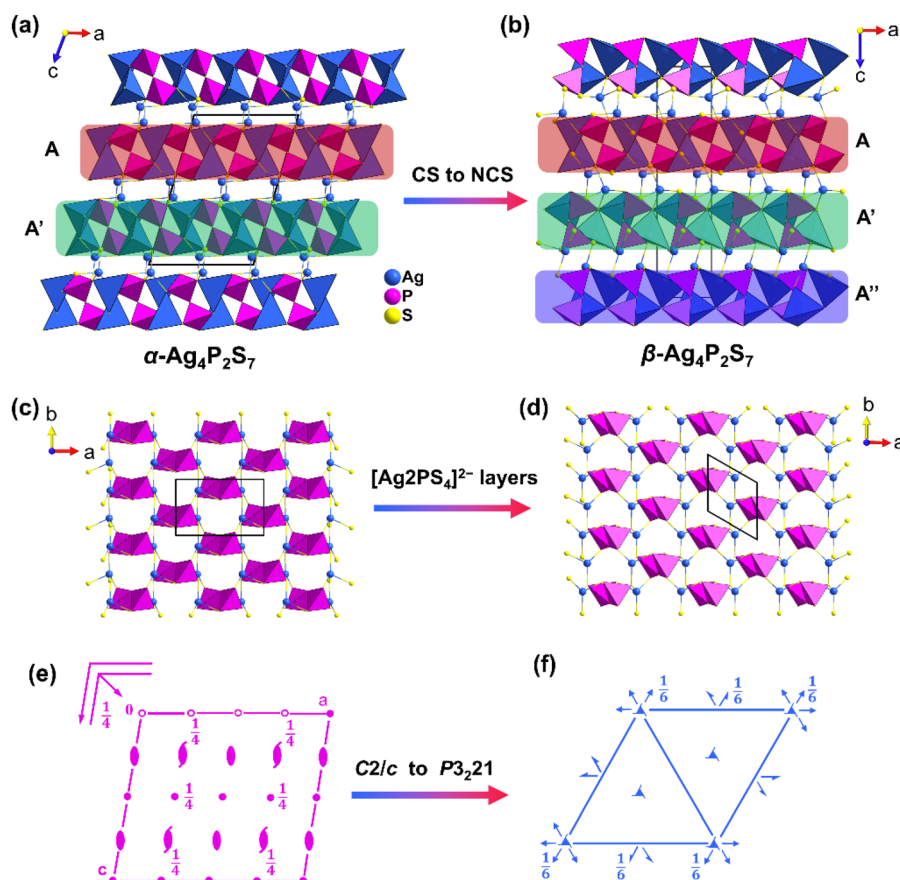


Fig. 3 The structural evolution from α - to β - $\text{Ag}_4\text{P}_2\text{S}_7$. (a) Crystal structure along the b -axis of α - $\text{Ag}_4\text{P}_2\text{S}_7$; (b) crystal structure along the b -axis of β - $\text{Ag}_4\text{P}_2\text{S}_7$; (c) 2D $[\text{Ag}_2\text{PS}_4]^{4-}$ layer in α - $\text{Ag}_4\text{P}_2\text{S}_7$; (d) 2D $[\text{Ag}_2\text{PS}_4]^{4-}$ layer in β - $\text{Ag}_4\text{P}_2\text{S}_7$; (e) spatial symmetry operation of α - $\text{Ag}_4\text{P}_2\text{S}_7$; and (f) spatial symmetry operation of β - $\text{Ag}_4\text{P}_2\text{S}_7$.

chemical properties. We evaluated the NLO properties of the β - $\text{Ag}_4\text{P}_2\text{S}_7$ by using the Kurtz-Perry method under the Q-switched 2100 nm laser.⁴⁰ As illustrated in Fig. 4a, the SHG intensity tended to attain saturation with an increase in the particle size of the sample, which indicated that β - $\text{Ag}_4\text{P}_2\text{S}_7$ was phase-matchable. β - $\text{Ag}_4\text{P}_2\text{S}_7$ demonstrates a strong SHG intensity of about 1.02 times that of AgGaS_2 at 150–200 μm (Fig. S6†), and is comparable to previously reported IR NLO materials $[\text{RbBa}_2\text{Cl}][\text{Ga}_4\text{S}_8]$ ($1.0 \times \text{AgGaS}_2$),¹⁹ NaAgPS_4 ($1.05 \times \text{AgGaS}_2$),⁴¹ $\text{NaMg}_3\text{Ga}_3\text{Se}_8$ ($1.0 \times \text{AgGaS}_2$),⁴² and $[\text{K}_4\text{Cl}][\text{CdGa}_9\text{S}_{16}]$ ($0.9 \times \text{AgGaS}_2$).⁴³ The large SHG response of β - $\text{Ag}_4\text{P}_2\text{S}_7$ will be favorable for generating high application conversion efficiencies. Note that the key scientific issue in the design of promising IR NLO crystals, especially for high-power laser applications, is how to strike a balance between strong SHG effects and high LDT, which have opposite structural requirements. In general, the barrier of photon absorption

increases with a larger optical band gap, and materials tend to have a higher LDT. However, Ag-based chalcogenides typically possess a shallow LDT further dramatically shortening the device longevity which stems from the 4d, 5s and 5p orbitals of Ag^+ always occupying the bottom of the conduction band (CB) and the top of the valence band (VB) leading to the narrow band gap and the photodarkening effect of silver. The absorption edge of β - $\text{Ag}_4\text{P}_2\text{S}_7$ is at 414 nm (Fig. S7†) and the band gap of β - $\text{Ag}_4\text{P}_2\text{S}_7$ is deduced to be 2.90 eV based on the Kubelka–Munk equation, which is in good agreement with the buff color of the crystals (Fig. 4b) and, to our knowledge, is the largest band gap in the ternary Ag-based DL chalcogenides (Fig. 4e and Table S6†).^{44–51} We hypothesize that the strong covalent P–S anionic frameworks promote the expansion of the band gap and drive the blue shift of the shortwave absorption edge, thus achieving high LDT, which is verified in subsequent theoretical calculations.

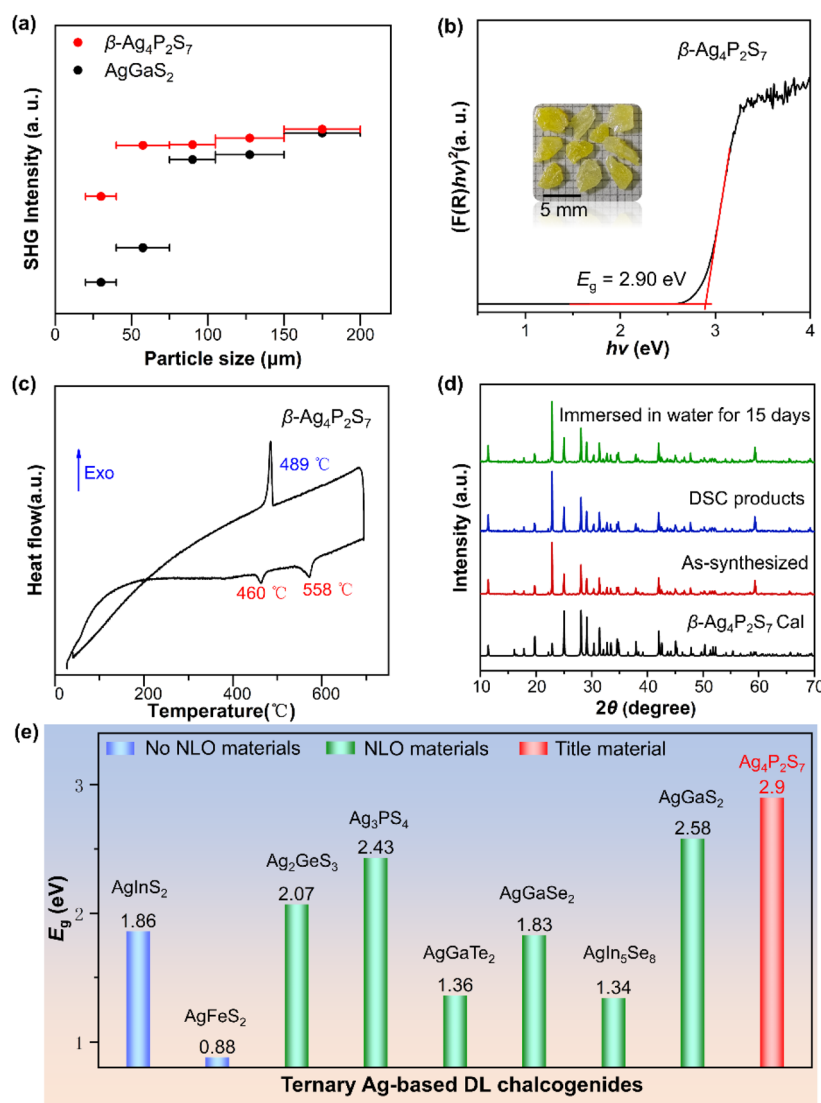


Fig. 4 (a) Size-dependent SHG intensities of β - $\text{Ag}_4\text{P}_2\text{S}_7$ and AgGaS_2 under 2100 nm radiation; (b) E_g of β - $\text{Ag}_4\text{P}_2\text{S}_7$. Inset: crystals of β - $\text{Ag}_4\text{P}_2\text{S}_7$; (c) DSC curve of the β - $\text{Ag}_4\text{P}_2\text{S}_7$; (d) PXRD patterns; (e) band gaps comparison of the Ag-based DL chalcogenides.

The thermal behavior of β - $\text{Ag}_4\text{P}_2\text{S}_7$ was investigated by DSC, as illustrated in Fig. 4c. There are two endothermic peaks at 460 °C and 558 °C, corresponding to the peritectic reaction of $\text{Ag}_7\text{P}_3\text{S}_{11}$ with the melt and melting point, respectively, and one exothermic peak at 489 °C during one heating/cooling cycle. In addition, the match of the powder X-ray diffraction (PXRD) patterns between the DSC measurement of β - $\text{Ag}_4\text{P}_2\text{S}_7$ and the β - $\text{Ag}_4\text{P}_2\text{S}_7$ sample further illustrates the melts congruence and the irreversible behavior of the phase transition (Fig. 4d). Thereby, β - $\text{Ag}_4\text{P}_2\text{S}_7$ is thermodynamically stable and can be grown as bulk single crystals by the Bridgman–Stockbarger method. With its stable DL crystal structure, β - $\text{Ag}_4\text{P}_2\text{S}_7$ possesses desirable water resistance. After being immersed in water for over two weeks, PXRD analysis showed that the crystalline structure of β - $\text{Ag}_4\text{P}_2\text{S}_7$ remained stable for further practical applications (Fig. 4d). The Raman spectrum recorded on the β - $\text{Ag}_4\text{P}_2\text{S}_7$ powder sample is displayed in Fig. S8.† The peaks located at 450–600 cm^{-1} correspond to

vibration modes of the P–S bond, while peaks existing between 200 and 450 cm^{-1} can be designated to vibrations of the Ag–S bond.^{52,53}

Electronic band structure calculations of α - $\text{Ag}_4\text{P}_2\text{S}_7$ and β - $\text{Ag}_4\text{P}_2\text{S}_7$ have been carried out to comprehensively understand the relationship between the structure and optical properties based on first principles. The α - $\text{Ag}_4\text{P}_2\text{S}_7$ undergoes an indirect transition from the M point to the other position points, corresponding to an indirect band gap value of 2.16 eV (Fig. 5a). The β - $\text{Ag}_4\text{P}_2\text{S}_7$ transitions directly from the M point to the M point, corresponding to a direct band gap of 2.42 eV (Fig. 5b). The calculated band gap value is significantly underestimated compared to the experimental result (2.65 eV and 2.90 eV, respectively) due to the discontinuity in the exchange–correlation potential.⁵⁴ It is generally accepted that optical properties are mainly determined by electronic transitions close to the band gap. To profoundly understand their band structure characteristics, partial densities of states (PDOS) are pre-

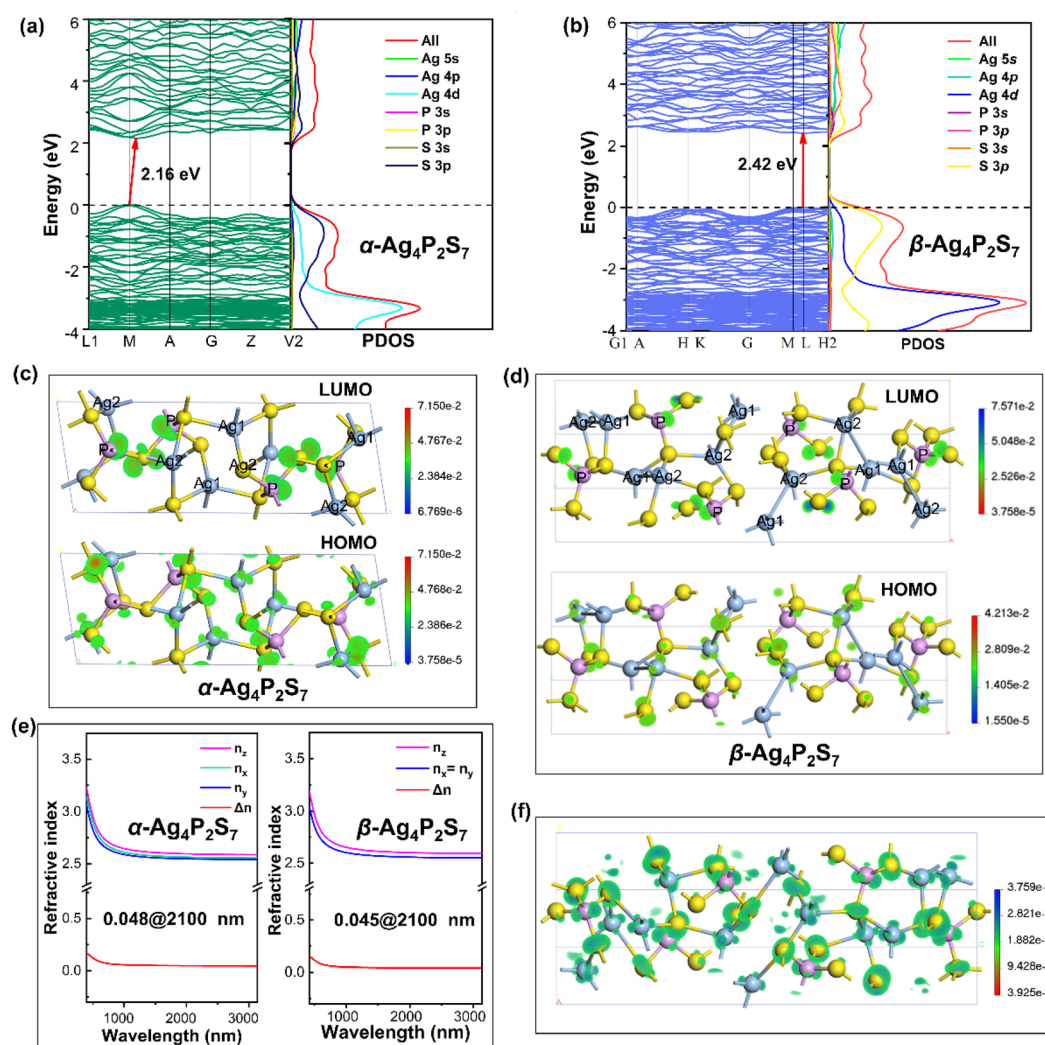


Fig. 5 (a) Electronic band structure and PDOS of α - $\text{Ag}_4\text{P}_2\text{S}_7$; (b) electronic band structure and PDOS of β - $\text{Ag}_4\text{P}_2\text{S}_7$; (c) HOMO and LUMO of α - $\text{Ag}_4\text{P}_2\text{S}_7$; (d) HOMO and LUMO of β - $\text{Ag}_4\text{P}_2\text{S}_7$; (e) the calculated refractive indices of α - $\text{Ag}_4\text{P}_2\text{S}_7$ and β - $\text{Ag}_4\text{P}_2\text{S}_7$; and (f) SHG density map. The blue, violet, and yellow balls represent Ag, P, and S atoms, respectively.

sented in Fig. 5a and b. Both structures have similar PDOS; the top of the valence band (VB) is predominantly dominated by Ag 4d and S 3p orbitals, while the bottom of the conduction band (CB) is primarily contributed by P 3p and S 3p orbitals. In addition, orbital analyses are carried out to understand the structure-performance relationship more intuitively. The partial charge density distributions of the highest occupied atomic orbitals (HOMO) and the lowest unoccupied atomic orbitals (LUMO) of α -Ag₄P₂S₇ and β -Ag₄P₂S₇ are plotted in Fig. 5c and d, respectively. It is observed that the HOMO states of α -Ag₄P₂S₇ are mainly composed of Ag 4d and S 3p orbitals, and the LUMO states of α -Ag₄P₂S₇ consist of unoccupied P 3p, and S 3p orbitals. The HOMO state of β -Ag₄P₂S₇ consists mainly of Ag 4d and S 3p orbitals and the LUMO state consists mainly of unoccupied P 3p and S 3p orbitals. The stacking mode of the [Ag₂PS₄]²⁻ layer change selectively strengthens the covalency of the anionic framework (*e.g.*, P-S) and weakens the Ag 4d-S 3p orbital hybridization. Therefore, the band gap increase induced by the CS to NCS structural phase transition is mainly altered by the stacking mode of the [Ag₂PS₄]²⁻ layer. In addition, the charge transitions responsible for the SHG efficiency in β -Ag₄P₂S₇ are mainly dominated by the charge transfer from Ag 4d and S 3p to P 3p and S 3p orbitals in the [Ag₂PS₄]²⁻ layer. The calculated SHG coefficients of $d_{16} = d_{22} = 6.7 \text{ pm V}^{-1}$ are much smaller than second-order nonlinear optical coefficient ($d_{36} = 13.7 \text{ pm V}^{-1}$) of the reference material AgGaS₂⁵⁵ and the experimental value ($d_{\text{eff}} = 13.8 \text{ pm V}^{-1}$) of β -Ag₄P₂S₇, and a similar underestimate of the second-order susceptibilities has also been observed in other reports.^{56,57} Furthermore, the birefringence of α -Ag₄P₂S₇ is slightly larger than that of β -Ag₄P₂S₇ at 2100 nm, which is consistent with the general rule that low crystal symmetry usually leads to higher birefringence (Fig. 5e).⁵⁸ The birefringence of β -Ag₄P₂S₇ is suitable for a mid-infrared material to achieve phase-matching conditions. To understand the contribution of NLO active electron states and units, the SHG-weighted electron density analysis of β -Ag₄P₂S₇ was adopted with electron-including occupied and unoccupied states (Fig. 5f).⁵⁹ The result shows that SHG efficiency in β -Ag₄P₂S₇ is mainly determined by the synergistic effect of the anionic groups [Ag₂S₄]⁷⁻, [PS₄]³⁻, and the small contribution of [Ag₁S₄]⁷⁻ tetrahedra. Furthermore, the dipole moments calculations for [Ag₁S₄]⁷⁻, [Ag₂S₄]⁷⁻, and [PS₄]³⁻ tetrahedra in the unit cell were calculated based on the bond valence method⁶⁰ to analyze the origin of the strong SHG effect, as displayed in Table 1. For per cell, the z components

of the [Ag₁S₄]⁷⁻, [Ag₂S₄]⁷⁻, and [PS₄]³⁻ tetrahedral polarizations almost cancel out. The [PS₄]³⁻ tetrahedra possess a very large net dipole moment of 45.43 Debye (D), followed by [Ag₂S₄]⁷⁻ tetrahedra with a net dipole moment of 18.78 D, whereas [Ag₁S₄]⁷⁻ tetrahedra has the smallest net dipole moment of 4.35 D. Overall, the synergistic action of the [Ag₂S₄]⁷⁻ and [PS₄]³⁻ tetrahedra in [Ag₂PS₄]²⁻ layer contribute mainly to the net dipole moment, which facilitates the superposition of their polarizations. In other words, the temperature-induced changes in the alternating stacking pattern of the [Ag₂PS₄]²⁻ layers contribute to the superposition of microscopic SHG coefficients and macroscopically enhance the NLO effect.

Conclusions

In summary, a novel NCS chalcogenide with the DL structure, β -Ag₄P₂S₇, was successfully obtained through an irreversible temperature-induced phase transition from the CS α -Ag₄P₂S₇. This transformation induces a structural evolution from AA' AA'-type to AA'A''AA'A"-type stacking of [Ag₂PS₄]²⁻ layers, where the [Ag₁S₄]⁷⁻ tetrahedra serve as adaptive bridges to accommodate the symmetry breaking. The phase transitions from low-temperature to high-temperature are systematically analyzed based on a series of solid-state reactions. β -Ag₄P₂S₇ exhibits outstanding IR NLO properties, including a phase-matchable SHG response ($1.02 \times \text{AgGaS}_2$) and a record-wide band gap (2.90 eV) among Ag-based DL chalcogenides, achieving an optimal synergy between strong nonlinearity and wide band gap. The detailed theoretical analysis illustrates that the temperature-induced change in the alternating stacking mode of the [Ag₂PS₄]²⁻ layers contributes to the increase of the band gap, the superposition of microscopic NLO coefficients, as well as macroscopic enhancement of the NLO effect. This study demonstrates that controlled layer-stacking modification through temperature-induced phase transitions provides an effective strategy to tune both the electronic structure and NLO response in DL chalcogenides, without requiring chemical composition changes. Future efforts will focus on growing bulk β -Ag₄P₂S₇ single crystals *via* the Bridgman method and exploring their device-oriented properties (*e.g.*, LDT, thermal conductivity).

Data availability

The data supporting this article have been included as part of the ESI,† for example, experimental procedures, the structural data, crystal photographs, PXRD, EDS, Raman, UV-vis-IR spectra, and comparison of properties.

Conflicts of interest

There are no conflicts to declare.

Table 1 Local dipole moment calculation for β -Ag₄P₂S₇

Units	Dipole moment			Magnitude	
	x(a)	y(b)	z(c)	Debye	esu cm Å ⁻³
[Ag ₁ S ₄] ⁷⁻	-2.1760	-3.7696	0	4.35	0.016
[Ag ₂ S ₄] ⁷⁻	9.3872	16.2600	0	18.78	0.069
[PS ₄] ³⁻	22.7225	39.3409	0	45.43	0.167
Per cell	29.9337	51.8312	0	59.85	0.220

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