



Leveraging machine learning in porous media†

Cite this: *J. Mater. Chem. A*, 2024, **12**, 20717Mostafa Delpisheh, ^{*a} Benyamin Ebrahimpour, ^b Abolfazl Fattahi, ^c Majid Siavashi, ^d Hamed Mir, ^d Hossein Mashhadimoslem, ^e Mohammad Ali Abdol, ^e Mina Ghorbani, ^f Javad Shokri, ^g Daniel Niblett, ^a Khabat Khosravi, ^h Shayan Rahimi, ⁱ Seyed Mojtaba Alirahmi, ^j Haoshui Yu, ^j Ali Elkamel, ^{ke} Vahid Niasar ^{*g} and Mohamed Mamlouk ^{*a}

The emergence of artificial intelligence (AI) and, more particularly, machine learning (ML), has had a significant impact on engineering and the fundamental sciences, resulting in advances in various fields. The use of ML has significantly enhanced data processing and analysis, eliciting the development of new and improved technologies. Specifically, ML is projected to play an increasingly significant role in helping researchers better understand and predict the behavior of porous media. Furthermore, ML models will be able to make use of sizable datasets, such as subsurface data and experiments, to produce accurate predictions and simulations of porous media systems. This capability could help optimize the design of porous materials for specific applications and improve the effectiveness of industrial processes. To this end, this review paper attempts to provide an overview of the present status quo in this context, *i.e.*, the interface of ML and porous media in six different applications, namely, heat exchanger and storage, energy storage and combustion, electrochemical devices, hydrocarbon reservoirs, carbon capture and sequestration, and groundwater, stressing the advances made in the application of ML to porous media and offering insights into the challenges and opportunities for future research. Each section also entails a supplementary database of the literature as a spreadsheet, which includes the details of ML models, datasets, key findings, *etc.*, and mentions relevant available online datasets that can be used to train ML models. Future research trends include employing hybrid models by combining ML models with physics-based models of porous media to improve predictions concerning accuracy and interpretability.

Received 25th January 2024
Accepted 24th May 2024

DOI: 10.1039/d4ta00251b

rsc.li/materials-a

1. Introduction

Porous media play an important role in many natural and engineered systems, including subsurface reservoirs for energy resources such as oil, natural gas, and geothermal heat, as well as aquifers that store water for drinking and irrigation. In addition, porous media play a critical role in a variety of environmental and industrial processes, such as carbon capture and sequestration (CCS), water treatment, heat transfer, *etc.* which underscores the significance of porous media in diverse applications. The study of porous media is interdisciplinary, combining elements of physics, chemistry, mechanics, and geology. It involves understanding the transport and exchange of fluid, heat, and mass in porous media and the interactions between fluid, solid, and thermal components.¹

Current research on porous media covers various aspects of physics, chemistry, and engineering. In terms of transport phenomena, the transport of fluid, heat, and mass in porous media and the impact of fluid–fluid, fluid–solid, and solid–solid interactions on these processes are investigated. In materials science, researchers are developing new materials with improved properties, such as higher permeability, better mechanical strength, and improved thermal conductivity, for

^aSchool of Engineering, Newcastle University, Newcastle Upon Tyne, NE1 7RU, UK. E-mail: m.delpisheh2@ncl.ac.uk; mohamed.mamlouk@ncl.ac.uk

^bSchool of Mathematics and Physics, University of Portsmouth, Portsmouth, UK

^cDepartment of Mechanical Engineering, University of Kashan, Kashan, Iran

^dSchool of Mechanical Engineering, Iran University of Science and Technology, Iran

^eDepartment of Chemical Engineering, University of Waterloo, Waterloo, N2L3G1, Canada

^fSchool of Metallurgy and Materials Engineering, College of Engineering, University of Tehran, Tehran, Iran

^gDepartment of Chemical Engineering, University of Manchester, Oxford Road, Manchester, M13 9PL, UK. E-mail: vahid.niasar@manchester.ac.uk

^hSchool of Climate Change and Adaptation, University of Prince Edward Island, Charlottetown, PEI, Canada

ⁱDepartment of Chemical Engineering & Materials Science, University of Southern California, USA

^jDepartment of Chemistry and Bioscience, Aalborg University, Niels Bohrs Vej 8A, Esbjerg 6700, Denmark

^{ke}Department of Chemical and Petroleum Engineering, Khalifa University, Abu Dhabi, UAE

† Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d4ta00251b>



use in an assorted range of applications. In the context of energy resources such as oil and natural gas, researchers are studying the behavior of subsurface reservoirs and developing tools and techniques to improve the extraction of these resources.²

Over recent years, there has been a marked increase in interest in employing ML and data analysis techniques to uncover and elucidate the underlying mechanisms and interactions within porous media, thereby enhancing the ability to both understand and predict their behavior. Researchers are attempting to develop models that capture the composite interactions between fluid, solid, and thermal components and use these models for optimizing processes and augmenting predictions. In particular, ML techniques can particularly assist

in cases where traditional modeling methods are limited by the complexity of the system or the availability of data.³ Fig. 1 depicts the occurrences of the published research on the keywords “machine learning” (ML) and “porous media” over the past two decades together with the relevant fields. This rapport between the interface of ML and porous media is conspicuous to grow even more over the coming years, signposting the present review paper’s direction.

Chapter two provides a comprehensive description of different ML models employed in the study of porous media such as supervised and unsupervised learning methods. Additionally, it gives instances of particular models that have been



Fig. 1 The number of published articles containing the words [“porous” or “porous media” or “porous materials” or “porous medium”] and [“machine learning” or “artificial intelligence” or “deep learning” or “neural networks”] in the literature (a) annually and (b) by subject area, adopted from Scopus, (extracted on 14 April 2024).



deployed, such as decision trees, random forests, support vector machines, and neural networks, followed by evaluation metrics.

In chapter three, the review paper applies the different applications of ML to porous media, stratified in different sections, namely, heat exchanger and storage, energy storage and combustion, electrochemical devices, hydrocarbon reservoirs, CCS, and groundwater. In each section, the different variables involved are scrutinized which include fluid flow prediction and characterization of porous media, *i.e.*, permeability, porosity, pore size distribution, wettability, and transport properties. Furthermore, it underscores examples of particular applications, such as the prediction of permeability, pinpointing the optimal production and injection methods, and flood optimization.

A common and essential component of many porous media applications is heat transfer. The contribution of the various geometrical shapes, governing parameters, materials, and micro/macroscale flow in different forms (convection, conduction, and radiation) elicits challenges in analyzing, optimizing, and predicting such physics. In the field of heat exchanger and storage, ML allows for optimizing heat transfer processes and thermal management of porous media. In this scope, key thermal properties, such as thermal conductivity, diffusivity, and heat capacity, are crucial for ensuring efficient and safe heat transfer in thermal systems, especially high flux systems such as electronics, chemical reactors, *etc.* ML models can assist in interpreting large thermal data sets generated by monitoring these systems and provide critical information that will ultimately lead to the identification and mitigation of potential risks and better decision-making to ensure the desired operation.

ML models are commonly used in the energy storage field to predict and improve the performance of various energy storage systems, including thermal, electrochemical, hydrogen gas, and hybrid energy storage methods.⁴⁻⁶ This includes identifying optimal charging and discharging approaches for batteries and thermal storage systems, as well as controlling the operation of energy storage equipment such as inverters and charge controllers. Furthermore, ML models can predict and diagnose the state of energy storage systems, including identifying factors responsible for battery degradation. The use of ML models helps improve the performance and reliability of energy storage systems. These models can analyze data from weather forecasts, energy usage, and energy production to predict energy demand. This information is then used to optimize the use of energy storage systems and balance the energy grid through grid integration. Thermal energy storage (TES) systems, such as thermal batteries, can be improved using ML models. These models analyze data from experiments and monitoring systems, such as temperature and heat flux, to optimize the design and operation of TES systems. This results in improved efficiency for the system. In general, implementing ML in energy storage can enhance the effectiveness, functionality, and dependability of energy storage systems. This can also lead to the optimization of energy storage systems to manage the balance between energy supply and demand. The incorporation of ML models into combustion has led to many discoveries, particularly in the field

of optimizing and controlling combustion systems used in power generation, industrial heating, and transportation. These models are utilized to forecast and improve the performance of various combustion systems, such as by identifying the optimal fuel-air ratios and combustion conditions for maximum efficiency. They also help in controlling the operation of combustion equipment, such as burners and boilers, by considering factors such as ignition, flame propagation, and burnout. An important field of study involves the creation of fresh combustion technologies, specifically those that produce low levels of emissions. Using ML models, data from experiments and simulations can be analyzed to discover innovative strategies and technologies that can enhance performance while also reducing emissions. Finally, ML models can aid in predicting combustion-related problems. For instance, they can identify the root cause of combustion instability, leading to enhanced performance and reliability of combustion systems.

In the field of electrochemical devices, ML models have found various applications to analyze experimental data and improve the understanding and optimization of electrochemical processes. For electrocatalyst experiments, ML models are used to assess stability and activity, aiding in the development of more efficient catalysts for reactions such as the hydrogen evolution reaction (HER) and oxygen evolution reaction (OER).⁷ ML models are also valuable for battery research, predicting the performance and behavior of different battery types such as lithium-ion, alkaline, carbon zinc, redox flow, and zinc air. This information can guide battery design and optimization. Supercapacitors can also benefit from ML modeling. ML models are used in corrosion prediction to analyze experimental data and forecast the corrosion rate of various materials, contributing to corrosion mitigation strategies. Additionally, ML models can be employed in electrodeposition processes to control the microstructure of metal coatings, leading to improved properties. In the field of electrolysis, ML models explored the relationship between electrocatalyst synthesis conditions, structural properties, and catalytic performance.^{8,9} Specifically, in the PEM water electrolyzer, ML highlighted the key variables that influence current/power density and polarization of the electrolyzers. In fuel cells, both PEM and solid oxide, ML helps design porous media such as gaseous diffusion layers (GDLs) and catalyst layers (CLs) by optimizing porosity and pore size distribution and their impacts on fuel cell performance.¹⁰ Finally, ML models are employed in pore-scale modeling to predict electrochemical transport and reactions within porous media, providing accurate predictions of the behavior of charged species.

The review paper focuses on the ML models in hydrocarbon porous media, as a complex and dynamic system, to foremost raise the understanding and thereafter provide an overview of ways that optimize the recovery of hydrocarbons from the reservoir.¹¹ In reservoir characterization, ML models are used for analyzing data from reservoir cores, including porosity and permeability, for creating more accurate reservoir models. To this end, the location of wells can be optimized to improve the recovery of hydrocarbons from the reservoir. ML models in reservoir history matching are used for matching production



data from oil or gas reservoirs to numerical models, which allows for more accurate predictions of future production and its changes over time. In enhanced oil recovery (EOR), ML models may be employed for optimizing EOR methods including CO₂ injection and waterflooding,¹² by analyzing data from the reservoirs. In rock physics modeling, ML models are used for introducing rock physics models, whereby the connection between rock's physical properties, such as porosity and permeability, and the fluids' properties in the rock, such as oil and water are described. Here, pore-scale fluid flow and transport are also appraised allowing for better predictions of oil and gas behavior in porous media. Furthermore, in the subfield of fracture characterization, ML models can be used to analyze data from seismic surveys and well logs to eventually identify and characterize fractures in the reservoir, which are critical to the fluids' flow. Finally, by analyzing data from log measurements, *i.e.*, resistivity, porous media properties can be determined.

Many key applications of ML can be applied to CCS porous media. ML models can be used for analyzing data from experiments on the CCS process, for instance, porosity, pore structure, and permeability, and using this to discern the CO₂ behavior and thereafter optimize the CCS process.¹³ ML models in predictive modeling can be used for predicting CO₂ behavior in introducing a new framework for calculating the normalized effective permeability resulting from hydrate formation. Furthermore, ML models can be introduced for optimizing the CO₂-EOR process, by analyzing experimental data and optimizing the CO₂ injection rate, timing, and location in the reservoir. ML can make it possible to provide algorithms for developing new materials and has attracted a great deal of interest for its ability to accurately predict chemical and physical properties, establish structure–property relationships, synthesize activated carbon and porous materials adsorbents *via* several types of biomasses, and navigate the chemical space to direct chemical synthesis. To determine structure–performance correlations and choose the top descriptors that can precisely predict the CO₂ adsorption capacity, efficiency, and selectivity, ML is applied to discover different porous materials for carbon capture technologies. Furthermore, ML models could predict highly accurate process condition prediction allowing for quantifying the influence of CO₂ capacity variations on material ranking in adsorption process technologies.¹⁴ Nowadays, researchers present cases of ML algorithm development in various CO₂ capture, storage, transport, and utilization (CCSTU) systems. Adsorption, absorption, chemical looping, membranes, sequestration, and hydrates are a few examples of carbon capture or separation technology (CCST). Modeling and simulating solvent-based carbon capture would be a progressive effort towards the complicated governing processes of absorption, particularly chemical absorption, involving mass transfer and chemical reactions.¹⁵

The paper reviews ML models that can be applied to groundwater porous media to optimize the management of water resources and ensure water is used sustainably. The ML models are utilized for aquifer characterization, namely, analyzing experimental data on aquifers, which include their

porosity, pore structure, and permeability, to understand the aquifer water behavior and attempt to promote groundwater management. Parameters such as recharge, flow, and storage of aquifers can be studied over some time through ML models to better manage groundwater resources through predictive modeling. Concerning water quality, by analyzing data from water quality sensors in monitoring systems, the ML models can detect changes in water quality and therefore predict issues such as heavy metal removal, nitrates, pH variations, and contamination, aimed at mitigating potential risks. Data-driven decision-making is also addressed in this field. Regarding groundwater recharge prediction, ML models can examine parameters such as temperature, precipitation, and evapotranspiration and predict the groundwater recharge rate and hence identify optimal conditions for recharge. Finally, further assessments such as optimal pumping rate and drought prediction, *i.e.*, predicting the onset and severity of droughts, and flood prediction, by analyzing data from weather forecasts and water level monitoring systems, can be made using ML models for water management decisions.

The review paper sums up by addressing the challenges and outlook of ML in porous media. The article recollects the challenges and relevant limitations associated with using ML on porous media grounded on the findings of the prior section. With the authors' prior knowledge in this field, this may include issues such as the requirement for powerful computing, lack of data, the complexity of studying porous media, dimensionality, scaling, and validation and interpretability. The review paper attempts to signpost new techniques to overcome these challenges and to improve the accuracy and robustness of ML models for porous media. It additionally culminates future research outlook for the application of ML to porous media, such as integrating ML with other technologies such as simulation and imaging and developing state-of-the-art ML methods especially designed for porous media systems. Finally, as a further reading and better comprehension of the scope of the review, a list of available online databases that can be used as an exercise to train ML models and all the reviewed literature in the manuscript as a spreadsheet are given in the ESI.†

2. Background on machine learning and porous media

The integration of ML with porous media has been addressed extensively during the past 10 years and, as evidenced by the number of publications in this field, the field will be even more focused on in the years to come. The review synthesizes recent advancements and interdisciplinary applications by providing a detailed analysis of how different ML models can improve and innovate these applications, each of which is crucial to resource management and sustainable technology advancements. Additionally, the review enjoys the addition of a supplemental database of literature and datasets and discussions on current challenges and future outlook. Dynamic research in ML for porous media primarily focuses on data-based methods for predicting the characteristics of complex porous substances in



transportation and chemical reactions. This area finds utility in various sectors, including subsurface contaminant transport,¹⁶ geothermal power utilization,¹⁷ CO₂ and H₂ containment in geological formations,¹⁸ water purification,¹⁹ and lithium-ion batteries.²⁰

One of the main challenges in this domain involves accurately capturing the physical properties of pore-scale pores, dealing with the heterogeneity and uncertain nature of porous substances, and extrapolating these predictions to a larger scale. By employing ML techniques to learn from different types of data, such as visual representations or computer simulations of porous media, we can overcome these obstacles and provide rapid and accurate evaluations of relevant factors such as pore volume, flow capacity, pathway complexity, and reaction rates.

ML can extract insights from various data sources, including two or three-dimensional images, pore structure characteristics, computational fluid dynamics (CFD), or experimental findings.^{21,22} It can also incorporate fundamental physical constraints or existing knowledge into the learning process to enhance accuracy and applicability. The field of ML applied to porous media represents an innovative and stimulating area, offering fresh perspectives and solutions to numerous scientific and technical challenges related to fluid movement and distribution in complex materials. The following section briefly provides an overview various ML methods applicable to porous media.

2.1. Principles of porous media

Porous substances are characterized by two primary attributes: (1) the presence of unfilled voids or pores within the solid material that can be occupied by liquids such as air, water, oil, or a combination of different fluids and (2) the ability to allow various fluids to pass through at specific pressure differentials.²³

2.1.1. Relevant parameters

2.1.1.1. Permeability. Permeability, which refers to the flow of liquids through materials containing pores or cavities such as rocks, soils, or filtration devices, has been extensively studied by researchers and experts in porous media. Factors influencing permeability include pore volume, pathway complexity, pore shape and size, and other porous medium characteristics. Various methods exist to determine permeability, such as core analysis, interpretation of well logs, and well assessments. Permeability is commonly expressed in units of Darcy or milli-Darcy.²⁴

2.1.1.2. Porosity. Within the context of porous media, porosity represents the proportion of empty spaces within the material. It significantly influences the movement of liquids, heat, and solutes within the porous medium. Porosity is generally quantified as a dimensionless ratio or percentage. Furthermore, porosity can be categorized into different types: total porosity, effective porosity, primary porosity, and secondary porosity.²⁵

2.1.1.3. Capillarity. Capillarity refers to the phenomenon where fluids are drawn into tiny pores or porous materials due to surface tension driven by capillary pressure. The capillary pressure, influenced by interfacial tension, pore size and shape, and the wetting characteristics of the liquids and solid structure, is used to determine the pressure difference at the

interface of two immiscible liquids. Capillarity plays a crucial role in governing the flow, spreading, and confinement of liquids within porous media, with applications in areas such as oil extraction, CO₂ storage, groundwater decontamination, and fuel cells.²⁶

2.1.1.4. Sorption. Sorption, in the context of porous media, refers to the process by which a porous material adsorbs or absorbs a substance. This phenomenon significantly impacts the movement and fate of pollutants in soil and groundwater, as well as the sequestration and retrieval of gases such as CO₂ and CH₄. The properties of the substance, the porous material, and the environmental conditions all play a crucial role in influencing sorption. Sorption can exhibit nonlinearity, meaning that the sorbed substance amount does not correspond linearly to its concentration in the liquid phase. This nonlinearity arises from the heterogeneous nature of the porous material, the arrangement of sorption sites, and competition among different substances for the same sites. Additionally, sorption can exhibit disequilibrium, where the equilibrium between the solid and liquid phases is delayed or hindered in rate. This phenomenon is due to substance diffusion within the pores, mass transfer between distinct pore regions, and the kinetics of sorption reactions.²⁷

2.1.1.5. Fluid–solid interactions. The interaction between fluids and solids in porous media, known as fluid–solid interaction, explores the interplay at the pore scale and its implications for the macroscopic properties of the porous material. This interaction encompasses fluid flow, solid deformation, mass transfer, chemical reactions, and phase transitions. Fluid–solid interaction has significant applications and consequences in fields such as geomechanics, hydrology, petroleum engineering, environmental engineering, and biomedicine.²⁸

2.1.2. Relevant equations. The fundamental theories of porous media rely on mathematical formulations of equations that conserve mass, momentum, and energy for both the liquid and solid phases within the porous medium. Different models can be derived to describe porous media's flow and transport behavior, depending on the assumptions and simplifications employed. Some commonly used models include.

2.1.2.1. Darcy's law. Darcy's law, which serves as the foundational model, relates the fluid velocity to the pressure gradient within the porous medium. According to this law, the volumetric flow rate of the fluid is directly related to the cross-sectional area of the porous medium, its hydraulic conductivity, and the hydraulic gradient (pressure or head difference per unit length) along the flow direction. Mathematically, Darcy's law can be expressed as:²⁹

$$q = \frac{kA \Delta P}{\mu L} \quad (1)$$

In this equation, q represents the Darcy flux, k denotes the permeability, A is the cross-sectional area (m²), ΔP signifies the pressure difference, and L corresponds to the length of the porous medium. Darcy's law is applicable for low Reynolds number flows in homogeneous and isotropic porous media.

2.1.2.2. Brinkman's equation. Regarding porous substrates, the concept of Brinkman characterizes an advancement of



Darcy's law, encompassing the influence of fluid thickness on the flow through the porous material. An extension of Darcy's law, the Brinkman equation integrates a component reflecting the Laplacian of velocity in accordance with the Stokes equation for viscous movement. The Brinkman equation is expressed as follows:³⁰

$$-\nabla p + \mu \nabla^2 u = -\frac{\mu}{k} u \quad (2)$$

In this equation, p represents pressure, μ denotes the dynamic viscosity of the fluid, and u signifies Darcy's velocity. The first term on the left symbolizes the pressure gradient, the second term represents the Brinkman viscosity factor, and the resistance term of Darcy is depicted on the right side.

This Brinkman equation proves effective in modeling fluid movement within porous substances exhibiting low porosity, reduced permeability, or high velocity, where viscosity impacts are more evident. The Brinkman equation can also be combined with other elements to account for supplementary influences such as inertia, reactions, diffusion, and heat transfer within porous substances.

2.1.2.3. Forchheimer equation. In relation to porous substrates, the Forchheimer equation denotes a notion that encompasses a modification of Darcy's law, incorporating the inertial effects of fluid motion through the porous material. The Forchheimer equation, an expansion of Darcy's law, encompasses a term signifying the squared relationship between the pressure gradient and velocity, akin to the Bernoulli equation for non-viscous motion. The Forchheimer equation can be formulated as follows:³¹

$$-\nabla p = \left(\frac{\mu}{k} + \rho \beta |u| \right) u \quad (3)$$

In this equation ρ refers to the density of the fluid, β is the Forchheimer coefficient and u denotes Darcy's velocity.

The Forchheimer equation proves valuable in modeling the movement of fluid within porous substances featuring high porosity, increased permeability, or high velocity, where inertial effects become noticeable.

2.1.2.4. Richards' equation. In the case of porous substrates, Richards' equation represents a concept that encompasses a partial differential equation elucidating the movement of water in unsaturated soils, where gravitational and capillary effects play a significant role. This equation is based on the Darcy–Buckingham law, representing water flow in porous substances under varying saturation conditions, and the law of mass conservation for an incompressible porous substance with consistent liquid density. The equation can be formulated as follows:³²

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \times \left(K(h) \frac{\partial h}{\partial z} + k(h) \right) \quad (4)$$

In this equation, θ represents the volume-based water content, t denotes time, K represents the hydraulic conductivity,

h signifies the pressure head of the liquid, and z symbolizes the unit vector in the vertical direction.

Richards' equation proves effective in modeling the movement of water in the vadose zone, which is the region between the atmosphere and the aquifer, where saturated and unsaturated conditions can coexist. The equation can also be employed to investigate various phenomena such as water infiltration, drainage, evaporation, irrigation, plant transpiration, soil erosion, pollutant transportation, and heat transfer in porous substances.

2.1.2.5. Navier–Stokes. The Navier–Stokes equation is a crucial mathematical model that characterizes the motion of fluids by considering the conservation of mass, momentum, and energy. It can be expressed in the general form below:

$$\rho \left(\frac{\partial u}{\partial t} + u \times \nabla u \right) = -\nabla p + \nabla \times \tau + \rho f \quad (5)$$

Here, p signifies the fluid pressure, τ symbolizes the viscous stress tensor, and f stands for the body force per unit mass. The Navier–Stokes equation is applicable to various fluid types, including Newtonian, non-Newtonian, compressible, incompressible, laminar, and turbulent, among others. However, when fluid flows through porous media, the Navier–Stokes equation requires modification to incorporate the effects of the solid matrix. One common approach to achieving this is using Darcy's law. Nonetheless, Darcy's law is only valid for low Reynolds number flows, and it does not account for the effects of inertia, turbulence, or non-linearity of the fluid. Additionally, the permeability k is often difficult to measure or unknown, and it may vary spatially and temporally based on the properties of the porous medium and the fluid.

To address these challenges, ML techniques can be employed to enhance the modeling of fluid flow in porous media. ML can be utilized to approximate the solution of the Navier–Stokes equation in porous media. For instance, ML can predict steady-state velocity fields and permeability in porous media.³³

2.2. Types of learning

Fundamentally, ML operates by utilizing encoded instructions to analyze and evaluate input data, generating predictions within a permissible range. As new information is introduced, these algorithms adapt, improve their functionality, and gradually acquire knowledge, becoming more effective over time.

ML algorithms can be classified into four categories: supervised learning, semi-supervised learning, unsupervised learning, and reinforcement learning.

2.2.1. Supervised learning. Supervised learning involves learning from examples. A supervisor provides the algorithm with a dataset containing specific inputs and corresponding outputs, deciphers trends within the dataset, absorbs insights from noted instances, and establishes conjectures to imitate the preferred results. The supervisor continually adjusts the algorithm's predictive outputs until its accuracy or performance significantly improves. In supervised learning, the algorithm acts as a student meticulously studying a set of labeled examples. It analyzes the connection between the input data (pore



size distribution, permeability, *etc.*) and the corresponding labels (flow rate and transport behavior) to learn the trends. Supervised learning can be used in applications such as predicting fluid flow properties and classifying pore types. Supervised learning includes tasks such as classification and segmentation.³⁴

(1) Classification: during categorization functions, the ML application must deduce the group of fresh instances using the data.

(2) Segmentation: it is the process of classifying a given set of data into different groups. It is used in machine learning applications to determine similarities and differences in the data and to identify patterns and trends.

2.2.2. Semi-supervised learning. Obtaining fully labeled data in porous media research can be expensive and time-consuming, especially when characterizing complex properties or rare phenomena. This is where semi-supervised learning shines and combines labeled and unlabeled data. Labeled data contain meaningful tags that aid the algorithm's understanding, while unlabeled data lack such information. This combination enables algorithms to learn how to categorize unlabeled data.³⁵

Reservoir simulations pose a significant computational challenge due to their complexity. In this situation, semi-supervised learning offers a promising solution to this problem. By utilizing high-resolution simulations from a limited number of samples and combining them with lower-resolution data from a larger set, semi-supervised learning enables more efficient upscaling of simulations for reservoir characterization. Another application of semi-supervised learning in porous media is its use in identifying anomalous flow patterns. By training on labeled data containing examples of normal and anomalous flow patterns, a semi-supervised learning model can leverage unlabeled data to detect potential anomalies in new datasets.

2.2.3. Unsupervised learning. Unsupervised learning involves the algorithm examining data to identify patterns without guidance from an answer key or human intervention. It establishes correlations and relationships by scrutinizing the available data. Unsupervised learning tasks the algorithm with deciphering large volumes of data and organizing it in a structured manner.³⁶ In the context of porous media, this could be a vast dataset of images representing the microstructure of various samples, or extensive flow rate measurements without corresponding information on the specific characteristics of the porous media they originated from. As the algorithm processes more data, its decision-making capabilities regarding the data gradually improve. Techniques in unsupervised learning include clustering and dimension reduction.

(1) Clustering groups of similar datasets based on specific criteria allows for data segmentation into multiple groups to identify patterns within each group.

(2) Dimension reduction simplifies the consideration of variables by reducing their number, aiming to reveal the essential data required.

Unsupervised learning enables the analysis of unlabeled images of porous materials, allowing the quantification of pore network complexity metrics such as connectivity and tortuosity.

Moreover, unsupervised learning algorithms can detect anomalies in flow data, identifying deviations from typical flow patterns within large datasets. This capability is particularly useful for early detection of issues such as preferential flow paths or blockages, which can significantly impact porous media behavior. Overall, unsupervised learning has proven to be a promising tool for studying porous media, with various potential applications in both research and industry.

2.2.4. Reinforcement learning. Reinforcement learning encompasses organized learning methods, in which a ML algorithm adheres to a series of activities, instructions, and end consequences. Through pre-established regulations, the algorithm investigates various possibilities and assesses each consequence to identify the most appropriate selection. By including experimentation and correction, reinforcement learning allows the algorithm to acquire knowledge from prior encounters and adapt its strategy according to the situation, striving for the best outcomes.³⁶

2.3. Machine learning models

ML models can be seen as software programs designed to identify patterns in new data and make predictions. These models are represented as mathematical functions that take input queries, make conjectures, and produce corresponding outputs. Initially, the models are trained on a dataset, and an algorithm is applied to reason over the data, extract patterns, and acquire knowledge from it. Once trained, these models can be used to predict unseen data.

2.3.1. Decision trees. Decision trees are a prevalent choice for ML models that can handle both regression and classification challenges. A decision tree employs a tree-like diagram of decisions alongside their potential repercussions and results. In this, every internal node serves to represent a check on an attribute and each branch symbolizes the result of that test. The greater the number of nodes a decision tree possesses, the more precise the outcome will be.

Decision trees' merits lie in their simplicity and ease of implementation, but they fall short in precision. They find extensive application in operational research, especially in decision analysis, strategic planning, and primarily in ML.

In relation to porous substances, decision trees can aid in determining the crucial features influencing CO₂ adsorption, such as textural characteristics, compositional properties, and adsorption parameters.³⁷

2.3.2. Random forest. The random forest represents an ensemble learning technique encompassing a considerable quantity of decision trees. Each tree within a random forest predicts a result, and the prediction receiving the most votes is deemed the final outcome.³⁸

A random forest model is versatile, being applicable to both regression and classification tasks. For classification tasks, the outcome from the random forest is derived from the majority voting. Conversely, the outcome in regression tasks originates from the mean or average of predictions produced by each tree.

2.3.3. Support vector machines. The support vector machine (SVM) is a prevalent ML algorithm predominantly



employed for classification and regression tasks. More specifically, it excels at resolving classification challenges. SVM's primary goal is to identify optimal decision boundaries within an n -dimensional space capable of segregating data points into distinct classes. The superior decision boundary is termed a hyperplane. The SVM employs the extreme vector to ascertain this hyperplane, which is why these vectors are dubbed support vectors.³⁹

2.3.4. Neural networks. Artificial neural networks (ANNs) or simply neural networks constitute a group of ML algorithms that derive inspiration from the human brain and, as per the Universal Approximation Theorem, can approximate any function.⁴⁰ Furthermore, due to their flexibility and modularity, neural network's structure can be customized for various supervised, unsupervised, and reinforcement learning applications. The construction of deep learning (DL) models is made possible by layering numerous levels in neural networks, which enhances the models' ability to extract features and learn intricate data representations. Hence, the neural network is a favorite algorithm across all domains of ML, consistently demonstrating remarkable results in all sorts of practical issues.

Numerous varieties of neural networks exist, each with varying complexity levels. All aim to emulate the human brain's functionality to tackle complex problems or tasks. The configuration of each neural network type somewhat mirrors neurons and synapses. However, they differ in complexity, applications, and structure. The differences extend to modeling artificial neurons within each type of neural network and the connections between each node. Other distinctions include the way data navigate through the neural network and the density of the nodes. The most common types of neural networks used in porous media are detailed in the following.

2.3.4.1. Multi-layer perceptron. A multi-layer perceptron (MLP) falls under the category of feedforward neural network (FFNN).⁴¹ It is a versatile and commonly used architecture for supervised learning tasks such as classification and regression. MLPs are the most fundamental deep neural network, consisting of a sequence of fully interconnected layers (an input layer, one or more hidden layers, and an output layer). Each neuron within the network processes input data using weighted connections and activation functions. MLPs can be utilized to circumvent the need for extensive computational resources required by modern deep learning frameworks.

2.3.4.2. Convolutional neural networks. Convolutional neural networks (CNNs) constitute a variant of neural networks predominantly utilized for processing image and visual data. They are designed to autonomously learn and extract hierarchical patterns and features from input images. CNNs encompass convolutional layers that apply filters to input data, followed by pooling layers for downsampling and fully connected layers intended for classification or regression tasks.

2.3.4.3. Recurrent neural networks. A recurrent neural network (RNN) represents another category of ANNs that leverages sequential data input. RNNs were conceived to tackle the time-series challenge posed by sequential input data. An RNN's input comprises the current input along with prior

samples. As a result, the connections between nodes form a directed graph that follows a chronological order. Additionally, every neuron in an RNN possesses an internal memory that preserves computational information from prior instances.

2.3.4.4. Physics-informed neural networks. Physics-informed neural networks (PINNs) are a groundbreaking fusion of artificial intelligence and mathematical physics, specifically tailored to address the complexities of partial differential equations (PDEs). Their modus operandi involves projecting solutions to these PDEs through the fine-tuning of a neural network aimed at minimizing a meticulously designed loss function. This loss function is imbued with critical elements representing the initial and boundary conditions within the space-time domain and the residual of the PDE at specific loci, known as collocation points. As PINNs function under the umbrella of deep learning models, they deliver a calculated approximation of a differential equation's solution at a specific point within the computational domain after completing their training. A revolutionary stride in the field of PINNs is the incorporation of a residual network that envelops the primary physics equations. In essence, the PINN's training process is viewed as an unsupervised learning approach, eliminating the necessity for pre-labeled data that typically originate from prior simulations or experiments.

The PINN algorithm is a grid-independent method that procures solutions to PDEs by recasting the task of directly solving governing equations into an optimization challenge for the loss function. This transformation becomes feasible by weaving the mathematical model into the fabric of the network and enriching the loss function with a residual term extracted from the governing equation. This residual term acts as a constraint that focuses on the range of acceptable solutions, ensuring more precise and reliable results.

2.4. Evaluation metrics

Evaluation metrics serve as tools to quantify the performance level of an algorithm or model. They offer a numerical indication of the model's success in meeting its objectives, such as precise prediction of results or data categorization. Diverse types of tasks might necessitate the application of different evaluation metrics.^{37,42}

2.4.1. Classification model. Evaluation metrics for classification models provide a quantifiable analysis of the model's ability to correctly categorize data into distinct groups. Common metrics for assessing classification models are accuracy, precision, recall, and F1-score. Accuracy quantifies the ratio of instances that were correctly classified out of the total number of instances. Precision is used to determine the fraction of positive instances that were correctly identified out of all instances the model predicted as positive. Recall measures the fraction of actual positive instances that the model correctly identified. The F1-score is the harmonic mean of precision and recall, providing a balanced measurement of both aspects. When evaluating a classification model, it's vital to consider multiple metrics as relying on one could fail to give a comprehensive view of the model's performance.



2.4.2. Regression model. Evaluation metrics for regression models provide a numerical estimation of the model's capability to precisely predict continuous or numerical outcomes. Commonly used metrics for evaluating regression models include mean squared error (MSE), root mean squared error (RMSE), mean absolute error (MAE), and *R*-squared. MSE measures the average of the squared discrepancies between predicted and actual values, while RMSE takes the square root of MSE to offer a metric in the same units as those of the predicted values. MAE calculates the average of the absolute discrepancies between predicted and actual values. *R*-squared quantifies the fraction of the variance in the dependent variable that can be explained by the independent variables in the model.

3. Applications of machine learning to porous media

This section presents a thorough review of the interface of ML and porous media in the six subsections, namely, heat exchanger and storage, energy storage and combustion, electrochemical devices, hydrocarbon reservoirs, CCS, and groundwater. Scientific research on porous media has traditionally been dominated by empirical and semi-empirical models which, while useful, often fail to capture the complex inherent interactions in such materials. In recent years, applications of porous media have been pronounced, especially in energy applications, including electrochemical devices^{43,44} (*i.e.*, batteries, fuel cells,⁴⁵ supercapacitors,⁴⁶ *etc.*), enhanced oil recovery, different energy storage technologies, and also environmental applications, such as carbon capture and water filtration. The advent of ML offers transformative potential in this regard, providing tools that can improve data processing, integrate large datasets, and uncover patterns that are not immediately discernable. ML's capability to adaptively learn from data without explicit programming leads to the assessment of porous media in exceptional detail. This facilitates a more refined understanding of physics such as flow and transport phenomena, adsorption and absorption, phase changes, and reactive dynamics within porous structures, which are critical for optimizing applications and poised to address some of the most important challenges in engineering and environmental science today. This discussion aims to engage readers by linking theoretical advancements in ML with practical, impactful applications in porous media, highlighting how these integrated approaches are transforming the assessments of porous media.

3.1. Heat exchanger and storage

Heat transfer represents a pivotal and foundational issue within thermal science, holding absolute significance in today's global economic and energy landscape. The efficiency of heat transfer systems is influential in mitigating energy waste and protecting the current fossil fuel reservoirs. It is conducted using energy recovery systems, such as economizers, and enhancing heat transfer methods, such as extended surfaces, turbulators,

microchannels, and phase change materials (PCMs). Moreover, the optimization of thermal systems, encompassing the extraction, transportation, and utilization of energy sources, particularly those facing challenges in temporal and spatial production, is imperative. Efficient heat transfer is needed using the methods of heat transfer increment, as well as the optimal input conditions. Another positive outcome of effective heat exchangers and storage devices is the reduction of pollution, contributing to improving adverse environmental impacts and climate change, especially for those systems that apply combustion flue gases.

The pursuit of a heat exchange system with superior thermo-hydraulic performance necessitates the use of tools for optimization and prediction. ML approaches, which initially emerged over half a century ago for pattern recognition, have evolved into sophisticated and professional methods. Consequently, tools for optimizing and predicting thermal system parameters are now readily available. The combined capabilities of optimization and prediction empower a thermal system to operate in a tuned mode, facilitating control systems a process that would be time-consuming with traditional analytical approaches. As well as the prediction of steady conditions, ML now takes advantage of transient estimation, enabling us to predict and respond to changes in real-time. This is particularly crucial in scenarios where thermal systems experience rapid variations, such as during startup and shutdown, or when subjected to varying external conditions. The ability to estimate transients allows ML models to adapt quickly and optimize control strategies, leading to enhanced energy efficiency, improved system performance, and increased reliability in thermal processes.

Accurately determining the conditions for the efficient operation of thermal systems requires handling large volumes of data, a task that becomes slow and hard without the aid of ML methods. This is because thermal systems are affected by both thermal and hydrodynamic conditions as well as the ambient status and energy resource quality. Recognizing the potential of ML, it emerges as a key tool not only in setting a thermal system at its desired operational point but also in the design phase. It is such that the optimum dimensions of the geometry can be determined using ML. This section aims to explore previous endeavors that utilized ML models in thermal systems and porous media. As the chronological trend indicates continuous improvement in prediction and optimization methods, there is confidence that future ML methods will reshape the current engineering system trends.

3.1.1. General heat transfer mechanisms. Numerous inquiries have delved into the underlying mechanisms of heat transfer, encompassing conduction, convection, and radiation. Within the realm of porous media, there has been a notable expansion in the application of ML. This expansion involves the utilization of a genetic algorithm to pinpoint the optimal operational point and/or the deployment of an ANN for predictive purposes across the three fundamental heat transfer mechanisms.

Moreover, recent studies have emphasized the role of ML in assessing the characteristics of convection heat transfer,



especially within porous media. Fig. 2 provides a visual representation, illustrating the integration of ML techniques to analyze and optimize the features of convection heat transfer processes in porous media. The incorporation of ML not only enhances our understanding of heat transfer phenomena but also paves the way for more efficient and targeted approaches to optimizing heat transfer characteristics within porous media.

Keykhah *et al.*⁴⁸ numerically simulated a tube with porous zone inserts filled with water–silver nanofluid, which is a suspension of a liquid and nanoparticles. The Darcy number left an increment and mitigation effect on the Nusselt number and friction factor, respectively. Furthermore, the nanofluid volume fraction made the heat transfer increase and the friction factor decrease. Particle swarm optimization (PSO) was applied to find the optimum conditions considering the Nusselt number and friction factor as the objectives in the tube of a heat exchanger. TOPSIS, LINMAP, and Shannon entropy were used to select the optimum point; however, Shannon entropy was the best decision-maker. It is worth noting that TOPSIS, LINMAP, and Shannon entropy are called decision-makers to find the best point of working conditions among the Pareto frontiers, showing the set of solutions having the best trade-off among the whole objectives.

Selimefendil *et al.*⁴⁹ proposed a 3D channel equipped with porous blocks for dehumidification and heat transfer of wet air. The constrained optimization by the linear approximation (COBYLA) method was used to optimize the geometrical features of the blocks concerning heat transfer. COBYLA is a derivative-free optimization method used to solve problems with bound and general constraints. It approximates the objective function and constraints using linear models and iteratively finds solutions that minimize the approximations while satisfying the constraints. The full simulation includes unsteady heat and mass transfer. The flow behavior between the blocks caused the temperature difference in the domain. A transient ANN was introduced using Levenberg–Marquardt (LM) with backpropagation (BP) by feeding the time and drying temperature as dependent variables and the liquid saturation as the output. However, the author recommended generating an ANN with time-dependent variables as the model inlet.

Khan *et al.*⁵⁰ numerically simulated porous fins with various shapes, called trapezoidal, rectangular, and dovetail, by considering convective and radiative heat transfer. Applying

1001 datasets, a neural network was constructed using the LM algorithm and cascade feedforward back-propagated approach. Using the inlet parameters, such as the inclination angle, tip tapering, and porosity, the temperature profile throughout the fins was predicted. A comparison between the captured results and those obtained by PSO and gray wolf optimization was accompanied and a negligible disparity was found. The results indicated that, in terms of having higher heat transfer, the fin shapes could be ranked as dovetail and rectangular followed by the trapezoidal fin profile.

Liu and Liu⁵¹ numerically simulated a heat-transferring tube involving porous ring inserts. The CFD results were coupled with an online multi-objective process, which was a non-dominating sorting genetic algorithm (NSGA-II), to find the optimum working conditions considering the Nusselt number and friction factor. The tube's radii, Damkohler number, and porosity were set as independent parameters. To reduce the undesirable populations in the genetic algorithm, they applied a penalty function, which removed the results with a higher friction factor. TOPSIS was used as a decision maker, showing more than a 40% increment in the Nusselt number and an 80% decrement in the friction factor.

Butt *et al.*⁵² tested an inverse multiquadric radial basis neural network for the problem of Casson nanofluid, which is a non-Newtonian fluid inherently, on a stretchable porous surface under an affecting magnetic force. The genetic algorithm was used for training and the solution method resulted in ODEs. The Casson parameter, Brownian motion parameter, Prandtl number, stretching parameter, and porosity parameter were some parameters to feed, and the velocity, temperature, and nanofluid concentration were predicted with an absolute error lower than 10^{-4} . However, the ability of the current method is required to test for stiff sets of equations.

Ahmad *et al.*⁵³ investigated a porous fin model through an analytical-numerical analysis. Two different porous types, which were silicon nitride and alumina, were compared and the prediction and optimization process was conducted respectively using an ANN and GA. It was concluded that silicon nitride had higher heat transfer than alumina. Therefore, alumina was highlighted with a higher temperature in the porous fin. The hybrid ANN-GA with the interior-point technique (IPT) showed more accurate and efficient optimum results.

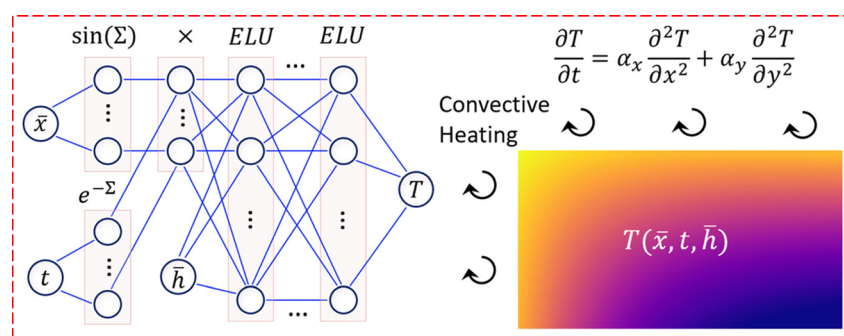


Fig. 2 Application of ML in the prediction of temperature using spacial and temporal parameters as independent variables in transient convection of a porous medium, Zobeiry and Humfeld,⁴⁷ reproduced with permission from Elsevier.



Su *et al.*⁵⁴ performed high-performance computing (HPC) coupled with an ANN for a double-diffusive problem, including mass and thermal diffusion. Furthermore, a multi-objective optimization for the functions of the Nusselt and Sherwood numbers was performed. The authors tried to solve the problem that needed a large volume of data to feed the ANN by applying the weighted objective functions, and aid from an HPC is required. The macroscopic porous properties and thermal features were fed to the ANN. It was shown that the random ordering of training data helped the accuracy of prediction when a sparse set of data is available, as the ANN's precision depended on the data distribution as well as the volume of data to feed.

Raja *et al.*⁵⁵ considered a three-dimensional hybrid nanofluid flow over a stretching/shrinking porous surface including radiative heat transfer using an analytical-numerical approach. The solution approach converted the PDEs to ODEs. The ANN was constructed using the input parameters of mass flux parameter, thermal relaxation parameter, stretching/shrinking parameter, and Prandtl number. The prediction was made on a hydrothermal field. The stretching/shrinking parameter changed the mass flow rate and velocity profile, while the variation in the radiation heat flux affected the temperature gradient. The author proposed a solution using AI based on infrastructure for future studies.

Ahmad *et al.*⁵⁶ used an ANN involving the Levenberg–Marquardt backpropagation to predict the temperature distribution of a fin attached to the heat sink. The fin was made of a functionally graded porous material to decrease the thermal gradient and three mechanisms of conduction, convection, and radiation heat transfer were considered through an analytical-numerical solution procedure. It was illustrated that the non-homogeneity of the fin increased heat transfer and the temperature gradient along the fin. It was such that the functionally graded materials made the temperature gradient negligible throughout the fin compared to the homogeneous materials.

Sajjad *et al.*⁵⁷ proposed an ANN to predict convective heat transfer for pool boiling with $R^2 > 0.97$ and MAE = 5.74%. Owing to the involvement of various parameters in problem physics, the prediction was hard using traditional methods. Therefore, a neural network could be beneficial and precise for predicting various fluids. Some input parameters were porosity, coating thickness, and particle size. Three hidden layers with neuron numbers of respectively 30, 15, and 1 were chosen.

The onset of convection cooling considering the rotation and magnetic field was studied in a horizontal bidispersive porous layer by Singh *et al.*⁵⁸ using a neural network with SVM type. The network was applied to find the marginal state and instability mode. Having the targets of the Taylor number, the Hartman number, and the Vadasz number, defined as the ratio of the thermal diffusivity of the base fluid to that of the nanoparticles, to determine the stationary zone, it was found that the rotation, inertia, and magnetic field postponed the instability beginning, and therefore, steady working conditions could be extended. The two hidden layers worked better than the neural network

with only one hidden layer. The Hartmann number could motivate the instability mode from the stability mode critically.

Increasing heat transfer in a proton exchange membrane fuel cell was simulated by Pourrahmani *et al.*⁵⁹ A series of wave-like porous ribs made of aluminum were mounted in the gas flow channel to increase heat transfer. The results indicated that the height of the first porous layer played a critical role in the Nusselt number and PEC. The latter indicates the ratio of the heat transfer improvement to the cost of the pumping. An ANN was also applied to produce a large amount of data to analyze the effects of the geometrical parameters on heat transfer and friction loss. The results showed the salient role of the friction factor in the investigated system. Furthermore, it was illustrated that the PEC could be an influential parameter in design geometry.

Alizadeh *et al.*⁶⁰ proposed an accurate estimator for the transport phenomena of a nanofluid passing through a cylinder in a porous medium using a support-vector regression (SVR) ANN. The semi-similarity technique by considering the local thermal non-equilibrium assumption was applied to find the results for training the ANN. As the problem involved a dozen parameters, the ANN decreased the time for a response by more than 90%. The correlations for the Nusselt number and shear stress using the PSO algorithm were derived.

Alhadri *et al.*⁶¹ analyzed a hybrid nanofluid flow with water base fluid over a stretching porous surface. The governing PDEs were converted into ODEs and then solved numerically using the shooting method. An ANN was produced to predict the Nusselt number and friction factor using the input parameters of porosity, Hartmann number, inertia coefficient, and suction/injection parameter. The coefficient of determination was found to be greater than 0.98. An optimization analysis was indicated using the response surface methodology (RSM). The main goal of RSM is to optimize a response variable, such as maximizing yield or minimizing cost, by exploring the relationship between this response and the input variables. RSM uses statistical models, often based on polynomial equations, to approximate the behavior of the response variable.

Mohebbi Najm Abad *et al.*⁶² instigated heat and mass transfer of a hybrid nanofluid in a porous medium. As the problem involves many parameters, conventional approaches to solving it might be complex and prone to failure. Therefore, they used an ANN. Furthermore, a PSO was also applied to derive some correlation to estimate the Nusselt and Sherwood numbers. Stemming from the dependency of the targets on various parameters, the feature selection process was performed. The results showed that the correlation involved at least five parameters that could reach an acceptable accuracy. Porous properties and the nanofluid volume fraction were among the most important ones.

Rajabi *et al.*⁶³ analyzed the accuracy and robustness of a deep learning method for the problem of natural convection. The porous media was selected as a heterogeneous type. The encoder–decoder convolutional neural network (ED-CNNs) was applied for image-to-image processing as the input-to-target for a porous cavity. The training was conducted through high-resolution imaging and the output generally showed good



accuracy. The zone with lower precision was found in the middle of the cavity where the temperature gradient fell. The training using a heat map in this method needed a large quantity of data, as they used 1000 samples. The method was beneficial for the uncertainty analysis of the meta-model.

The Brownian and thermophoresis effects were studied by Khan *et al.*⁶⁴ in a fluid flow passing through two parallel porous plates. Brownian motion refers to the random movement of particles suspended in a fluid (liquid or gas) due to collisions with the molecules of the fluid. Thermophoresis is the movement of particles in a fluid medium due to a temperature gradient. The governing PDEs were transformed into ODEs using the homotopy analysis method. Viscosity, porosity, Prandtl number, and some other parameters were used as input parameters to the ANN applied to predict the concentration and temperature profile. The accuracy of the method showed well as the MSE fell between 10^{-14} and 10^{-7} . The authors would like to test the applied ANN, which was a back-propagated neural network with the Levenberg–Marquard system to predict other fluid flow problems.

3.1.2. Heat exchangers. Various heat exchangers incorporating porous media find widespread application across industries such as oil refineries, power plants, and heating, ventilation, and air conditioning (HVAC) systems. Extensive research has been conducted due to the recognized advantages

of high efficiency in heat exchangers employing porous media, resulting in reduced energy consumption and costs. The first section investigates traditional heat exchangers, specifically time-tested shell-and-tube configurations, as the oldest category. Consequently, it is anticipated that greater emphasis will be placed on advancing this particular heat exchanger type.

The subsequent focus involves advancements in manufacturing technologies targeting the fabrication of micro and nanoscale structures, particularly within miniature channels filled with porous media relevant to heat and mass transfer. This exploration is detailed in the next section. Surprisingly, the integration of ML into micro/nanoscale heat transfer with porous media has not been extensively explored, as indicated in Fig. 3. It should include data set creation, which is expensively hindered in experiments as well as feature selection methods and data training. The last part of this section reviews earlier studies on solar applications where porous media play a crucial role. Recognizing the significant role of heat exchangers in renewable energy production, the final section explores the application of ML in heat exchangers within solar systems equipped with porous parts.

3.1.2.1. Conventional types. Siavashi *et al.*⁶⁶ numerically studied heat transfer augmentation and pressure loss increment in a tube of a heat exchanger by inserting gradient and multilayer porous media and applying the water-alumina



Fig. 3 The schematic diagram for application of the feed-forward algorithm in microchannel flows; the first step includes data preprocessing and normalization, the second one is feature selection for removing the weak related parameters, and the final step involves model tuning and validation for having an accurate prediction, Yang *et al.*⁶⁵ reproduced with permission from MDPI.



nanofluid. Six different porous types, including linear increasing particle size (LIPS), linear decreasing particle size (LDPS), stepwise increasing particle size (SIPS), stepwise decreasing particle size (SDPS), constant minimum particle size (CMIPS), and constant maximum particle size (CMAPS) were used. In LIPS structures, the pore size increases linearly and gradually along the length or depth of the material, while LDPS has a linear decrease in pore size. SIPS structures have discrete steps where the pore size increases abruptly rather than gradually; however, SDPS shows a similar structure when pore sizes decrease. CMIPS (CMAPS) structures maintain a constant minimum (maximum) pore size throughout the material. The maximum value of PEC (performance evaluation criteria) was captured by the PSO algorithm considering the independent parameters of porosity and grain size. The optimization for simultaneously considering particle size and porosity led to the same arrangement for independent parameters when considering each of them separately. Applying the nanofluid made the PEC three times higher.

Meng *et al.*⁶⁷ used porous fins to increase heat transfer in a heat exchanger equipped with thermoelectric modules by a numerical simulation. An NSGA-II algorithm along with the TOPSIS decision maker was employed to increase heat transfer and decrease pressure drop by feeding the variables of the position, number, and relative distance of porous fins. A higher power generation and lower pressure drop by respectively about 79% and 21% was achieved by introducing porous pin fins. The dense downstream distribution for pin fins was shown to have the best performance compared to other distributions. A novel index was introduced to aid in picking up the optimum solution from the Pareto frontiers, meaning the electrical power generated by considering the pressure drop penalty. The velocity profile in the solution was reduced by increasing the porosity factor, the volumetric concentration, and the magnetic field amplitude.

Abbasi *et al.*⁶⁸ numerically simulated a shell-and-tube heat exchanger with some segmental porous baffles. Inserting more baffles increased heat transfer, while it upgraded the pressure loss penalty. An ANN was trained to predict the crucial functions, which were the heat transfer rate and pressure drop to calculate the system performance. Furthermore, a multi-objective optimization along with a TOPSIS decision maker was performed to find the best values for baffles' features by minimizing the pressure drop and maximizing the heat transfer. The process recommended 10 porous baffles, a baffle angle of 111.9°, and a thickness of 16.69 mm, which led to a heat transfer rate and pressure drop respectively of 523.81 kW and 48.87 kPa.

Athith *et al.*⁶⁹ numerically simulated a heat exchanger partially filled with high porosity metal foams, made of aluminum, copper, and nickel with two pore densities, 20 pores per inch (PPI) and 40 PPI. The authors intended to find the best performance of the heat exchanger by maximizing heat transfer and minimizing the pressure drop. Therefore, a multi-objective optimization using the NSGA-II algorithm was performed linking with an ANN to predict the objectives, which were the heat transfer rate and pressure loss. Although the porous inserts

increased pressure drop, they could improve heat transfer significantly more than 5 times compared to the case without obstacles.

Chen *et al.*⁷⁰ conducted a transient numerical simulation for a vertical geothermal heat exchanger. Soil was considered a porous medium. The borehole depth was predicted through a three-layer ANN using the input parameters of the soil thermal conductivity, grout thermal conductivity, inlet water temperature, underground water velocity, and heat flux. They concluded that the porosity of soil and volumetric heat capacity had an insignificant effect on the results. The ANN worked with 10 neurons and $R^2 > 0.9999$; however, without using the Levenberg–Marquardt algorithm, the prediction error was critically enhanced.

Zheng *et al.*⁷¹ optimized the porosity of a multi-layer porous medium, ranging from 0.5 to 1.0, by coupling the ANSYS Fluent and MATLAB software. The application of their study was in the tubes of shell-and-tube heat exchangers. The multi-objective optimization found the appropriate porosity to have maximum performance evaluation criteria (PEC). The number of porous layers was also determined.

Mohammadi *et al.*⁷² numerically simulated a shell and tube heat exchanger equipped with porous baffles. An ANN was conducted coupled with an NSGA-II algorithm to find the optimum values of the porosity, permeability, and baffle cut for the objectives of heat transfer and pressure drop; each dependent parameter took six values. Additionally, the ANN was applied for sensitivity analysis, which showed that the baffle cut mostly contributed to the heat transfer enhancement and pressure drop decrement, respectively by 88% and 71%. The permeability was set in the next rank. The authors declared that, owing to steady state assumption, the fouling phenomenon was not considered a limitation of the simulation.

Baiocco *et al.*⁷³ numerically evaluated a heat exchanger using aluminum metal foam, electrically deposited with copper for increasing conductivity. A neural network was applied to predict the characteristics of the heat exchanger with a general error of less than 1%. Input temperature, airflow speed, and foam material were the inputs, while the outlet temperature was the output. An electroplating process increased heat transfer and enhanced efficiency by about 10%. The numerical simulation was performed considering non-local thermal equilibrium.

Deshamukhya *et al.*⁷⁴ used PSO to find the optimum design variables for a rectangular fin attached to a heat exchanger. The fin was made of porous materials and the porosity, the Damkohler number, and the ratio of thickness to length were selected as input parameters to find the maximum value of the heat transfer rate. PSO had a higher convergence speed, as it has a derivative-free nature. The tip temperature decreased by increasing the Damkohler number, while heat transfer increased. PSO elicited higher heat transfer while increasing the porosity decreased the heat transfer.

3.1.2.2. Micro/mini channels. Microchannels and mini channels are small-scale conduits through which fluids flow. Microchannels have dimensions in the range of micrometers to millimeters and exhibit a high surface-to-volume ratio, enabling enhanced heat transfer and fluid flow properties. They are



employed in applications such as microfluidics and electronics cooling. Mini channels are slightly larger, ranging from millimeters to centimeters, and are used in areas such as compact heat exchangers and cooling systems. Both micro and mini channels offer unique fluid dynamics and heat transfer characteristics due to their reduced size compared to conventional channels.

Wang *et al.*⁷⁵ performed a multi-objective optimization for finding a higher thermal resistance and a lower pumping power for a double-layered porous microchannel. Geometrical features were chosen as independent parameters. The numerical simulations showed an inverse trend for both objectives. The NSGA-II algorithm optimization results showed that the cooling performance increased by about 14% and pumping power decreased by nearly 16% compared to the reference case. The numerical results indicated that the upper channel was involved more in the pumping power and the lower channel was critical for improving heat transfer. The importance of various geometrical variables was derived.

Bayer *et al.*⁷⁶ presented a microchannel with wavy double-layered porous walls to increase heat transfer as well as solve the problem of high-pressure loss. More than 3000 numerical tests were conducted to build an ANN based on the Levenberg–Marquardt backpropagation algorithm. The eight geometrical scales were used as independent parameters and convective heat transfer and pressure loss were the outputs of the ANN. Six neurons guaranteed the precision of the prediction. After validation of the proposed ANN using 30% of the data, the three best performers were introduced. The introduced patterns not only increased heat transfer but also decreased the temperature uniformity on the heat sink. The thermal efficiency factor was shown increase if the top wall became wavy and the bottom was straight instead of making a wavy shape on both walls.

Khosravi *et al.*⁷⁷ applied an ANN to predict entropy generation in a microchannel under a constant thermal flux with porous fins filled with the water–silver/graphene hybrid nanofluid. A neural network was constructed using the parameters, such as different porous medium thicknesses, nanoparticle concentrations, and inlet mass flow rates. Various neuron numbers for the ANN were tested and it was found that the ANN could be accurate with two hidden layers having 12 and 20 neurons. The Bejan number was reported to be 0.944, showing that the thermal irreversibility was salient. An increase in the inlet mass flow rate and nanofluid concentration diminished the strength of thermal entropy generation.

3.1.2.3. Solar systems. Solar systems utilize the principles of conduction, convection, and radiation to transfer heat from solar radiation to useful applications. Solar radiation is absorbed by solar collectors, which convert it into heat energy. This heat is then transferred through conduction within the system's components, such as metal tubes or fluid-filled panels. Convection allows for the movement of heated fluids, such as water or air, which carry thermal energy to desired locations. Additionally, radiation is involved in both the absorption and emission of heat. By combining these heat transfer processes in porous media, solar systems efficiently harness solar energy for various applications such as heating water or spaces.

Ghritlahre and Prasad⁷⁸ experimentally studied a solar air heater by inserting a porous bed. The prediction of thermal performance using a neural network using a multi-layer perceptron (MLP), generalized regression neural network (GRNN), and radial basis function (RBF) was conducted and compared with multiple linear regression (MLR) statistical models. The input parameters to the models were mass flow rate, wind speed, atmospheric temperature, inlet fluid temperature, fluid mean temperature, and solar intensity, collected during 96 tests. It was concluded that the neural models could predict better than the MLR. Furthermore, the GRNN was highlighted as the best predictive neural method; the MLP was set in the next rank.

Du *et al.*⁷⁹ investigated a porous volumetric solar receiver by considering silicon carbide as the fluid flow medium. Furthermore, non-equilibrium assumption was involved with convective-radiative heat transfer. A multi-objective optimization by coupling ANSYS Fluent and MATLAB was performed. The pressure drop and thermal efficiency were selected as objective functions. Although the pareto front was derived, decision-maker strategies were not investigated. Nonetheless, the single objective optimization showed that the higher the porosity and flow velocity, the larger the thermal performance would be.

Zheng *et al.*⁸⁰ evaluated a parabolic solar system by inserting porous fins in the shape of circular sectors and implementing a non-uniform heat flux on the tube. The Nusselt number, synergy angle, entransy dissipation, and exergy loss were the indices to appraise the heat transferring system. The porosity, thermal conductivity, and Reynolds number were the input parameters for the single objective genetic algorithm, while the Nusselt number was the target function. The results elucidated that optimum porous inserts made the receiver more efficient compared to the reference case with a lower exergy loss at the same pumping power.

Hosseini and Siavashi⁸¹ numerically scrutinized the steam reforming process to produce hydrogen gas in a thermochemical reactor aiding solar energy. A novel idea using a two-layer porous medium with different porosities was applied. Some parameters, such as permeability, pore size, and reactor length were chosen as input parameters for an ANN, coupled with the PSO algorithm, to find the optimum conditions. The objective was hydrogen production. The results showed that the optimization could enhance hydrogen production more than all the investigated cases. Additionally, the two-layer porous medium made an increment in hydrogen production.

Grosjean *et al.*⁸² optimized a glass with porous SiO₂ anti-reflective coating to enhance solar transmittance using GA. The porosity and angle were the inputs. The performance was found to be drastically dependent on the glass type. The optimization process showed that the angle below 30 degrees had no effect on the objective, while values higher than 45 degrees made it critically different. A low refractive index and high Abbe number were introduced for an acceptable glass for solar applications.

Du *et al.*⁸³ presented that a porous layer with small pore diameters was beneficial for uniform radiation heat flux in



a solar receiver in terms of higher convective heat transfer. However, it had an undesirable effect on the radiation penetration, such as having overheating zones. Therefore, they optimized the pore scales using a GA to have the highest thermal efficiency. The proposed radial-graded porous increased the thermal efficiency by 4.1% and decreased the flow resistance by 8.6%. It was made of super-alloy Inconel 718 and passed mythological post-processing.

The thermal efficiency of an air heater equipped with a porous bed was predicted using an ANN by Ghrithahre and Prasad.⁸⁴ Four training functions, such as one-step secant backpropagation, conjugate gradient backpropagation with Polak–Ribiere, and Levenberg–Marquardt were tested and it was illustrated that the latter performed the best. Thermal efficiency, heat gain, and temperature difference were chosen as targets for the input parameters of inlet velocity/temperature of the air, ambient temperature, and solar irradiance.

3.1.3. Cooling electrical systems or batteries. Contemporary focus is increasingly directed toward compact electrical systems, with ongoing efforts to enhance miniature CPUs and electrical power storage units. One notable challenge affecting the optimal performance of such systems is elevated operating temperatures, potentially causing system shutdown in the absence of effective thermal management control. To address this issue, numerous investigations have delved into the integration of porous media within the cooling system. By incorporating porous media, researchers aim to improve heat dissipation efficiency, mitigating the risk of overheating and system malfunctions.

The application of ML in the cooling systems of electrical devices further contributes to a more efficient design, enabling

a swifter and more resilient control system capable of responding adeptly to sudden thermal fluctuations. Moreover, the strategic use of porous media enhances the overall effectiveness of the thermal management system, providing a more stable operating environment for compact electrical systems. Additionally, as the diminished performance of vehicle batteries can compromise the power system's efficacy and competitiveness, maintaining precise temperature control within the desired range becomes crucial. This goal is easily attainable through optimization based on ML, as illustrated in Fig. 4, with the added advantage of porous media integration ensuring enhanced thermal regulation and reliability in challenging operational conditions.

Duan and Li⁸⁶ investigated transient heat transfer in a metal foam filled with a phase change material, applied for cooling electrical devices or batteries. An ANN was trained to predict the liquid fraction, temperature, and average Nusselt number using lab-based experimental data. The input data were the time series and the porous medium characteristics. However, the effects of geometrical features and environmental conditions were not considered. The importance of the porosity parameter on the changes in the melting process speed with passing time was reported. The latter was dependent on the temperature-dependent thermal features of the metal foam.

Tikadar and Kumar⁸⁷ predicted the thermo-hydraulic performance of a heat sink in conjugation with a metal foam using five ML algorithms, called k-nearest neighbors (KNN), random forest (RF), extreme gradient boosting (XGBoost), SVR, and ANN. The average Nusselt number and friction factor were chosen as the dependent parameters, while the porous zone density, porosity, two geometrical indices, and the Reynolds

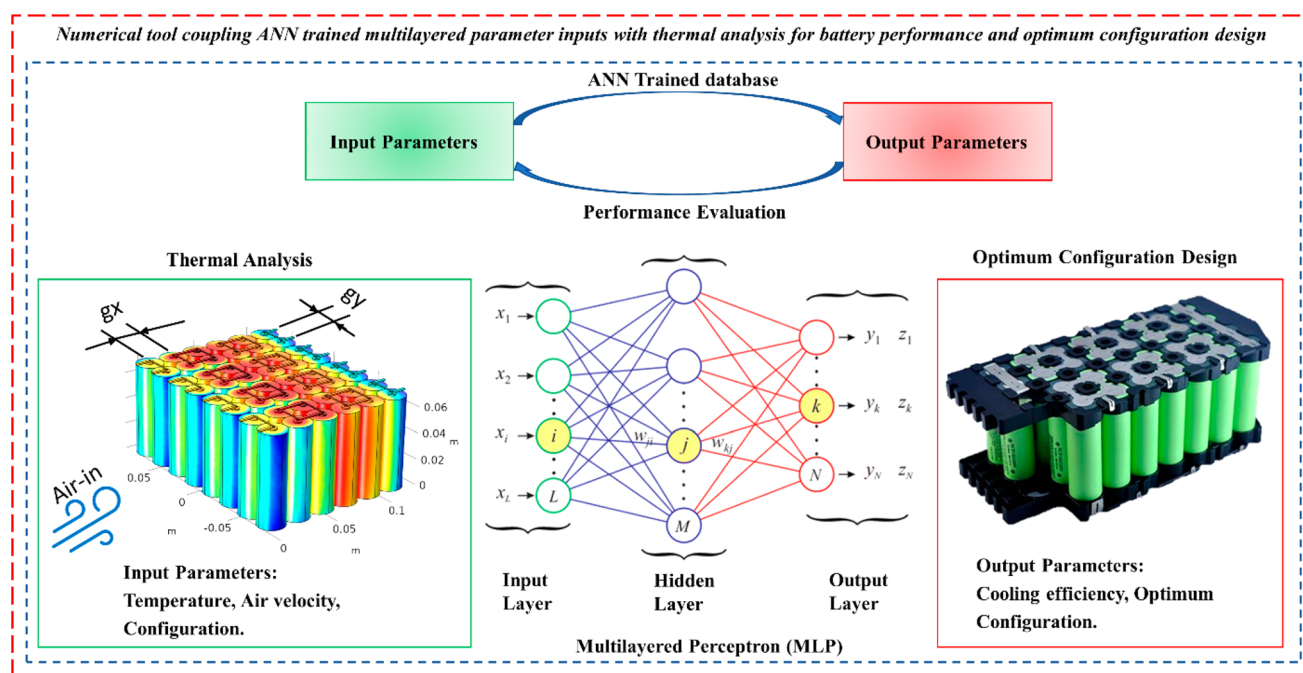


Fig. 4 Schematic view for applying combined CFD-ANN for battery cooling; temperature, air velocity, and geometrical features as input parameters and cooling efficiency as the output parameter in an MLP network aiming for prediction, Li *et al.*,⁸⁵ reproduced with permission from MDPI.



number were picked as the input parameters. SVR and the ANN showed a minimum mean absolute percent error of 3.1%. A data size of 1000 points was numerically collected, and the results indicated that the ML methods could capture the thermo-hydraulic performance of the heat sink well, despite its nature as a 'black box'.

Ilyas *et al.*⁸⁸ in an analytical-numerical study scrutinized the fluid flow and heat transfer of a hybrid nanofluid, as alumina-copper-water, over a rotating disk where a porous medium was attached and a magnetic field was imposed. Scaling group transformation converted the PDEs to ODEs. The thermo-hydraulic field was predicted by the Levenberg-Marquardt backpropagation neural network. The porosity factor, inertia coefficient, Prandtl number, Brinkman number, radiation parameter, magnetic parameter, and concentration of nanoparticles were selected as the feeding parameters for prediction. The validation performance was reported to be precisely a value lower than 10^{-10} .

Butt *et al.*⁸⁹ presented an amalgam procedure involving the inverse multiquadric (IMQ) radial basis neural networks (RBNNs) and a genetic algorithm, *i.e.*, IMQ-RBNN-GA. The hybrid proposed method was validated through the problem of cooling a wedge by passing a nanofluid in a porous medium considering the radiation, viscous effect, and magnetic field. The absolute error for the neural procedure was lower than 10^{-10} by comparing it with the Adams solution method. The dynamic properties of the nanofluid were the objective. The Eckert number and Brownian motion made the nanofluid temperature higher, while the radiation subsided it.

Bianco *et al.*⁹⁰ numerically simulated a cooling system for a heat sink involving finned and non-finned metal foams. As the heat transfer and pressure drop act in opposite directions, optimization was conducted in the study by linking the COMSOL Multiphysics and MATLAB modules. The results indicated a higher heat transfer by inserting fins about 3.3–3.5 times than that of simple configuration with constant pressure loss. In this case, the optimization could enhance the heat transfer by a factor of 3. The optimization concluded that a porosity of 0.85, 40 PPI and a number of fins of 8 were appropriate. Furthermore, correlations for Pareto fronts were provided.

Deshamukhya *et al.*⁹¹ studied the optimal heat transfer rate for stepped, convex and triangular porous fins attached to a heat sink. PSO and the firefly algorithm (FA) were employed to achieve optimal heat transfer *versus* the geometrical parameters, as well as the Damkohler number, Rayleigh number and porosity, keeping the fin volume constant. The stepped profile showed the highest heat transfer compared to the triangular and convex profiles by nearly 2% and 40%, respectively. PSO illustrated marginally better performance, while the FA indicated more acceptable suboptimal points. A porosity of 20% at a lower length ratio addressed optimal heat transfer.

A layered porous heat sink was scrutinized numerically for heat sink by Dathathri and Balaji.⁹² An ANN was used to predict the temperature and pressure drop using the input parameters of inlet velocity and pore scale. The applied ANN was fed to a multi-objective genetic algorithm (NSGA-II) to find a maximum temperature and minimum pressure drop. The

results elucidated that neglecting pressure drop could result in a major deviation from reality in genetic algorithm optimization.

Shoib *et al.*⁹³ investigated double-diffusive, free convective nanofluid flow in a porous medium numerically for cooling a hot plate. The prediction was performed using a Levenberg-Marquardt scheme in a backpropagation algorithm, in a novel application. Different cases with changing the Grashof number and various scenarios with varying variables, such as the Brownian motion parameter and thermophoresis parameter were studied. Various parameters, such as the Brownian parameter, inclination angle, and Dufour, Grashof, and Lewis number as well as magnetic strength were evaluated. The non-dimensional temperature and concentration were among the target parameters. The effect of governing parameters on the volume fraction of the nanofluid was critically investigated.

3.1.4. Heat storage. Heat storage involves the capture and retention of thermal energy for later use. It plays a crucial role in balancing energy supply and demand, particularly in renewable energy systems. Various methods are used for heat storage, including sensible heat storage, latent heat storage, and thermochemical storage. Sensible heat storage involves storing heat in a medium, such as water or rocks, and releasing it when needed. Latent heat storage utilizes PCMs to store and release heat during phase transitions, such as solid-liquid or liquid-gas. Thermochemical storage involves reversible chemical reactions that absorb and release heat energy. Heat storage systems enable the efficient utilization of excess or intermittent heat, increasing the overall energy efficiency and flexibility of thermal systems in various applications, including heating, cooling, and industrial processes. In this context, ML emerges as a valuable tool, contributing to the development of more efficient and sustainable heat storage systems.

Integration of porous media becomes particularly significant in enhancing the performance of these systems. The incorporation of porous media in terms of geometry, foam distribution, and flow path optimizes heat storage mechanisms, ensuring a more effective utilization of undemanding energy. This approach not only addresses the energy crisis but also promotes sustainable practices in energy management. Furthermore, the application of ML extends its benefits by enabling the prediction of thermal energy storage system performance under various operating conditions. This predictive capability enhances the overall efficiency of energy management strategies, providing valuable insights into system behavior under diverse circumstances. In summary, the synergy between ML and porous media contributes to the development of advanced heat storage systems that are not only more sustainable but also adept at meeting the evolving demands of energy consumption.

Yang *et al.*⁹⁴ tried to solve the problem of the low heat transfer rate and low thermal efficiency of a latent heat storage unit using metal foams, made of aluminum, nickel, and copper. A quasi-stationary approximation was considered to have a simple and accurate solution. A simplified model predicted the phase change time and a genetic algorithm optimized the metal foam distribution. The effect of various parameters on the porosity distribution and graded layer number was numerically



found to be negligible. Thermal performance was the objective function sought to find the best value with an average accuracy of 5–6%. Considering economical and engineering requirements, four metal foam layers were recommended.

Cui *et al.*⁹⁵ numerically and experimentally analyzed an inclined container equipped with a hybrid structure of metal foam and metal foam-fin hybrid. The metal foam-fin system aided in having more heat transfer. Furthermore, an increment in the fin number accelerated the phase change material (PCM) melting and heat accumulation. Using a proposed ANN, the melting time was predicted using the input parameters of the fin number, inclined angle, and melting time with an R^2 of about 0.9990. Applying the metal foam fin could make the melting process up to 60% quicker.

Anand *et al.*⁹⁶ used numerical results to feed a self-organizing map (SOM) to predict gas and solid phase temperature profiles in a porous medium including a PCM. The extinction coefficient and convective coupling were applied as inputs. Four pairs of temperature profiles were fed to the SOM, and it could predict various regimes correctly. The algorithm also succeeded in estimating precisely the PCM regime when it was trained using 1% noisy data. The proposed procedure could aid in the design process of thermal systems including porous PCMs, such as those working in a combustive aperture.

3.1.5. Thermal properties. Nowadays, various porous types have been synthesized, and determining their thermal

properties is an initial requirement for applying them in thermal systems. To do so, experimental or molecular dynamic methods are required, which are costly and time-consuming. ML can be a swift and accurate method to specify the thermal properties of such materials. Fig. 5 illustrates a view for finding the porous properties schematically. ML also helps in synthesis of porous media having high thermal conductivity and strength by proposing the micro-structure distribution.

Eghtesad *et al.*⁹⁸ applied an ANN to predict the radiation properties of a porous medium at a high temperature. The model could mitigate the burden of the numerical simulation of radiative models. Transmission and reflection were selected as the outputs. The authors introduced coupled geometrical and physical features, such as porosity, the void's refractive index, the particle's refractive index, and the particle radius. Three predictive categories, namely, whole-size, wall-wise, and point-wise were also considered by involving random overlapping and non-overlapping packed porous media; the latter was shown to be more accurate. The point-wise class, predicted independently from the emission angle, was of the least accuracy. It showed a promising prediction needed involving directional features of the porous media.

Wei *et al.*⁹⁹ tried to derive an ML method to predict porous thermal properties, considering morphology properties, owing to the high expense of numerical simulations. The effects of some parameters, such as the shape factor and channel factor,

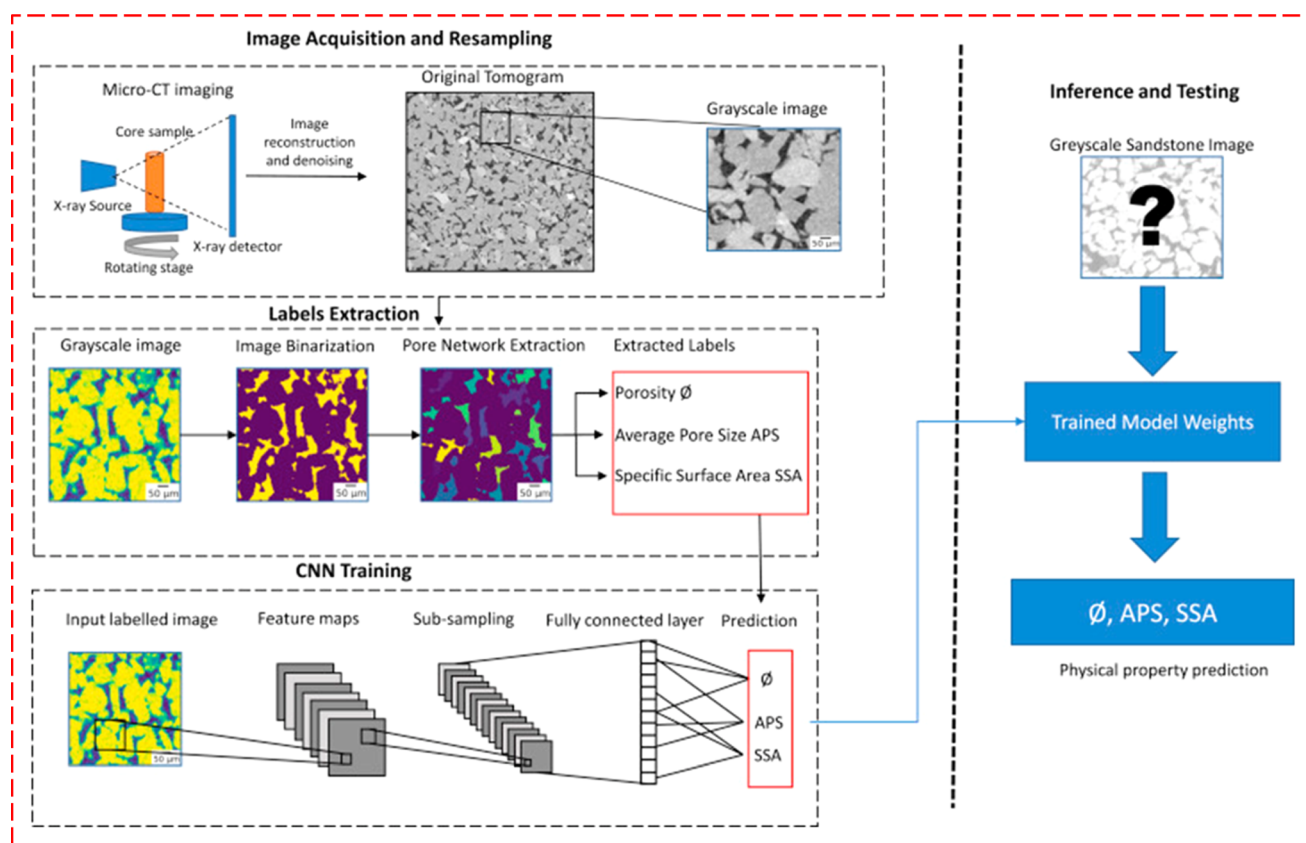


Fig. 5 A flow work to predict porous properties of porosity (ϕ), specific surface area (SSA), and average pore size (APS) by a CNN using image acquisition, visually/experimentally input parameter extraction, and construction of a tuned neural network for prediction, Alqahtani *et al.*,⁹⁷ reproduced with permission from Elsevier.



on the thermal conductivity were studied using an ANN. Then, the SVR could predict the anisotropy features of the pores and involve them in effective thermal conductivity. The results showed that the selected inputs were critical to have an accurate estimation of conductivity. The resultant ML could present an intuitive insight into the conductivity values out of the normal range.

Mishra *et al.*¹⁰⁰ used a global search algorithm (GSA) and GA to predict some thermal properties in a 2D rectangular porous matrix considering conduction, convection, and radiation. Scattering albedo, emissivity, solid conductivity, and heat transfer coefficient were tried to predict by capturing the solid and gas temperature distribution. Both direct and indirect approaches were applied using the finite volume method for solving energy equations. The results indicated that the GSA showed faster prediction with higher accuracy compared to the GA. However, the run time was affected by the starting points and the error.

Singh *et al.*¹⁰¹ tried to predict the effective thermal conductivity using six feedforward backpropagation ANN models for a moist porous medium by feeding the thermal conductivity and volume fraction. The complex structure and different thermal features of the substances in a moist porous material pushed the authors to use artificial intelligence. The model showed good accuracy against the experimental data. It was concluded that the fluid phase played a critical role in the prediction. The derived model could be used for complex moist porous structures.

3.2. Energy storage and combustion

As time passes, humans are facing a growing energy demand.¹⁰² Meeting the growing energy demand can be achieved by utilizing combustion systems such as boilers and gas turbines and renewable sources of energy, such as solar and wind energies, which are viable solutions.¹⁰³ In addition to addressing the growing energy demand, it is crucial to consider the storage of generated energy.¹⁰⁴ The industrial sector frequently stores energy to guarantee a consistent and uninterrupted power supply, as well as to regulate fluctuations in energy demand. Thermal energy storage (TES),¹⁰⁵ electrochemical energy storage (EES),¹⁰⁶ hydrogen gas energy storage,¹⁰⁷ and hybrid energy storage¹⁰⁸ are some prevalent methods for energy storage in industry. Optimal storage technology selection is performed using various factors, including the scale of storage required, the duration of storage needed, the specific energy demands, and the economic feasibility of the system.

Porous media can indeed be used for energy storage in various ways. For instance, metal–organic frameworks (MOFs) have found diverse applications as a porous medium across multiple industries such as solar cells, fuel cells, supercapacitors, white light emitting diodes, and lithium-ion batteries.¹⁰⁵ The porous nature of these materials provides a large surface area, which can enhance storage capacity and facilitate the movement of fluids or gases. Energy storage systems consist of various components that use porous media, including porous electrodes for batteries,¹⁰⁶ porous adsorbents

for gas storage,¹⁰⁷ and porous phase change materials (PCMs) for thermal energy storage.¹⁰⁸

The application of ML techniques in energy storage with porous media has gained significant attention.^{109,110} These techniques offer valuable tools to understand and optimize various aspects of energy storage systems based on porous media. ML has several applications in this field, such as the characterization of porous materials,¹¹¹ material design,¹¹² and optimization of energy storage systems.¹¹³ Through ML, researchers and engineers can analyze complex data, optimize system performance, and advance the field of energy storage with porous media. By leveraging these techniques, they can enhance the efficiency, reliability, and overall performance of energy storage systems based on porous media. Fig. 6 depicts several studies on energy storage systems utilizing porous materials, aided by ML.

In the upcoming section, we will delve into various processes of energy storage utilizing porous media and ML. We will present diverse thermal energy storage and electrochemical energy storage methods. Also, hydrogen gas energy storage, hybrid energy storage, and combustion will be reviewed. Fig. 7 illustrates some research on energy storage and combustion using porous media aided by ML.

3.2.1. Thermal energy storage. Thermal energy storage using porous media is a promising approach for storing and utilizing heat energy. Porous media can effectively store thermal energy in the form of sensible heat or latent heat, providing a means to store excess heat and release it when needed. It can be utilized in solar thermal systems, where excess heat from solar collectors is stored in porous media and released during periods of low solar availability.¹²⁶ It can also be applied in industrial processes, district heating and cooling systems, and energy-efficient buildings, enabling the utilization of waste heat and load shifting.¹²⁷

3.2.1.1. Phase change materials (PCMs). PCMs can be effectively combined with porous materials for energy storage applications.¹²⁸ The integration of PCMs with porous media enhances the storage and release of thermal energy. The combination of PCMs and porous materials offers advantages such as high energy storage density, improved thermal conductivity, and enhanced heat transfer characteristics. These hybrid systems have the potential to contribute to more efficient and sustainable energy storage solutions in various fields, including building and construction, renewable energy integration, and thermal management.¹²⁹ Furthermore, the combination of PCMs with porous materials for energy storage can be further enhanced through the application of ML techniques. In a study, Saboori *et al.*¹²⁰ utilized multi-layer calculation loops based on ML to examine the flow pattern and thermal behavior of pore scale porous media (PSPM) walls, which incorporated PCMs in Trombe walls. They introduced a new approach for predicting and optimizing the concentration of PCMs in Trombe walls, considering factors such as porosity, solar radiation, heat flux, and time. Based on the findings, the use of PCMs can lower the temperature of the outer side of the PSPM wall by 5.2% compared to not using PCMs during the day and night. In another study conducted by Selimefendigil and



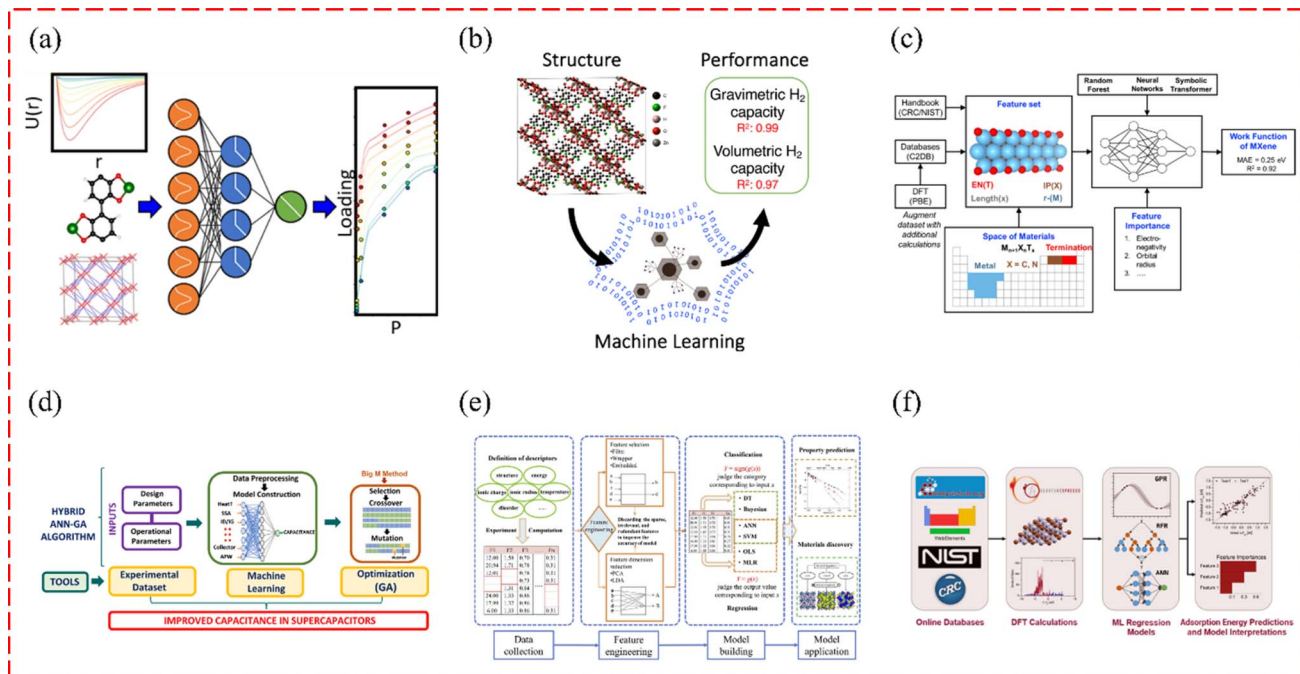


Fig. 6 (a) Determining achievable volumetric targets for adsorption-based hydrogen storage in porous crystals using ML,¹¹⁴ reproduced with permission from American Chemical Society, (b) predicting hydrogen storage in MOFs through ML techniques,¹¹⁵ reproduced with permission from Cell Press, (c) a computational framework that utilizes ML techniques to predict the work function of MXenes,¹¹⁶ reproduced with permission from IOP Publishing Ltd, (d) the construction of a hybrid framework that combines ANNs and genetic algorithms for optimizing capacitance in supercapacitors,¹¹⁷ reproduced with permission from Elsevier, (e) the process of utilizing ML for rechargeable battery materials involves four major stages,¹¹⁸ reproduced with permission from Elsevier, and (f) predicting the adsorption energies of hydrogen, carbon, and oxygen using online databases, density functional theory (DFT) calculations, and ML regression models,¹¹⁹ reproduced with permission from the AIDC-Italian Association of Chemical Engineering.

Öztop,¹³⁰ they explored the impact of a porous disk on the dynamic aspects of the phase change process. The study focused on a circular pipe with PCM integration during nano-liquid forced convection in discharging operation mode using the finite element method for various values of porous disk permeability, radius, and height. The disk achieves its best permeability value at a Darcy number of 5×10^{-3} , resulting in the shortest discharging time. In this research, a feed-forward neural network (FFNN) predictive model is utilized to provide precise results on the impact of a porous disk on the dynamic characteristics of the phase change process.

It's important to note that the integration of ML into PCM and porous material systems for energy storage is an emerging research area, and these are potential avenues where ML techniques can provide valuable insights, optimization, and control for enhancing the performance and efficiency of energy storage systems utilizing PCMs and porous materials.

3.2.1.2. Adsorption cooling and heating systems. Adsorption cooling and heating systems that utilize porous media can benefit from the integration of ML techniques. ML can aid in optimizing and improving the performance and energy efficiency of adsorption-based systems for cooling and heating.¹³¹ In a study conducted by Skrobek *et al.*,¹³² three deep learning techniques (long short-term memory (LSTM), bidirectional long short-term memory (BiLSTM), and gated recurrent unit (GRU)) were employed to predict the mass of an adsorption bed in both

fixed and fluidized beds. The purpose of utilizing this particular bed was to optimize the efficiency of adsorption cooling systems by enhancing heat and mass transfer *via* fluidization. The algorithms developed for the LSTM, BiLSTM, and GRU networks produced results that were highly consistent with experimental tests, with coefficient of determination (R^2) values exceeding 0.97. In the field of adsorption-driven heat pumps and chillers, Shi *et al.*¹³³ conducted a study on selecting effective adsorbents and working fluids. They utilized a high-throughput computational screening of 6013 computation-ready experimental MOFs to determine the best candidates for methanol-MOF pairs. The research resulted in the identification of the top 10 MOFs with the highest working capacity (ΔW) and coefficient of performance (COP) under the heat pump's operating conditions, which were found to be 512.86 mg g⁻¹ and 1.83, respectively. They also applied four ML algorithms (back propagation neural networks (BPNNs), decision trees (DTs), random forest (RF), and SVMs) to predict the relative significance of each MOF descriptor. Based on the comparisons, it has been determined that both RF and BPNNs can produce the most accurate predicted results. Using high-throughput screening and ML techniques, this computational work serves as a reliable guide for the development and design of MOF adsorbents in adsorption-driven heat pumps and chillers.

3.2.1.3. Thermochemical energy storage (TCES). Thermochemical energy storage (TCES) with porous media involves





Fig. 7 (a) The temperature behavior of the walls of pore scale porous media (PSPM) changes with the use of PCM encapsulation influenced by variations in porosity, (1) without and (2) with optimization,¹²⁰ reproduced with permission from Elsevier, and (b) the wetting of an electrode using real and predicted visualization of the electrolyte over time in a lithium-ion (Li-ion) battery. The electrolyte enters through the yz plane at $x = 0$. Refer to the web version for color explanations,¹²¹ reproduced with permission from Elsevier, and (c) comparing actual and predicted capacitance values for a supercapacitor during training and test phases. Circles represent real values and triangles represent predicted values,²⁴³ reproduced with permission from Elsevier. (d) performance of an ML model in predicting $\ln P_{eq}^0$ (the equilibrium pressure of H_2 at room temperature) in (1) training and (2) test processes, in which each plot contains overlaid data from 10-fold validation experiments,¹²³ reproduced with permission from ACS Publications, (e) comparing estimated and measured values of liquid fraction, entropy generation rates, and thermal management in battery systems using a gradient boosting decision tree (GBDT) model and scatter plots,¹²⁴ reproduced with permission from Elsevier, and (f) comparison of research results and experimental data for combustor wall temperature and reformer CH_4 conversion,¹²⁵ reproduced with permission from Elsevier.

utilizing chemical reactions within porous materials to store and release heat. It is a promising approach for high-density and long-duration energy storage. The reactions occur within the porous structure, allowing the storage and release of thermal energy.¹³⁴ TCES systems that utilize porous media can benefit from the integration of ML techniques which can aid in optimizing performance, improving control strategies, and enhancing system efficiency. A study by Chen *et al.*¹³⁵ has shown that calcium carbonate and calcium oxide ($CaCO_3/CaO$) can be excellent materials for storing thermochemical energy and can be used in renewable energy sources due to their high energy storage density and long storage time. This research delves into the impact of complex pore structures and different operating conditions on micro-flow diffusion mass transfer performance within CaO materials. The study discovered that the effective gas diffusion coefficient increases with porosity but decreases with fractal dimension. Moreover, an ML-based prediction model was proposed, with an average error rate of approximately 12% and a root mean square error (RMSE) of 0.04138. This model can be valuable in designing Ca-based materials with high performance, as well as in reactor design or system thermodynamic investigations. According to a study by Praditia

et al.,¹³⁶ the TCES system using calcium oxide and calcium hydroxide ($CaO/Ca(OH)_2$) is a promising energy storage technology due to its relatively high energy density and low cost. They implemented a PINN to predict the dynamics of the TCES internal state. They performed numerical simulations on an ensemble of system parameters to obtain synthetic data to train the network. The suggested approach provides results with an error of 3.96×10^{-4} , which is in the same range as the result without physical regularization but is superior compared to conventional ANN strategies because it ensures the physical plausibility of the predictions, even in a highly dynamic and nonlinear problem. A recent study by Tasneem *et al.*¹³⁷ discovered that reversible thermochemical reactions have significant potential for use in thermochemical energy storage systems. In this study, five powerful ML algorithms, including KNN, least absolute shrinkage and selection operator (LASSO), XGBoost, SVM, and Bayesian ridge, were utilized to develop accurate models that predict the dynamic behavior of a reversible thermochemical reaction-based system. The research utilized these ML algorithms to create the best formula and model for NH_4NO_3 and KOH . The study discovered that the polynomial regression degree 4 for the NH_4NO_3 temperature with KOH and



water temperatures provides the best R^2 of 0.938, with an MSE of 3.898504. The KNN ($K = 5$) is ideal for creating a model with polynomial regression degree 2, with an R^2 of 0.999 and an MSE of 0.009042. The KNN ($K = 5$) degree 3 had an R^2 of 0.984, with an MSE of 5.355852, making it the best method for creating a model. As KOH also has a time series dataset, XGBoost was used to compute the future KOH temperature.

3.2.2. Electrochemical energy storage. Electrochemical energy storage using porous media is a widely used approach in various electrochemical devices, including batteries and fuel cells. Porous media are instrumental in enhancing electrochemical processes, transport phenomena, and overall performance of electrochemical energy storage systems. Through careful design and optimization, porous media can significantly contribute to the efficiency, capacity, and durability of batteries, fuel cells, and other electrochemical devices.¹³⁸ The integration of ML techniques with electrochemical energy storage systems using porous media holds great potential for optimizing performance, improving control strategies, and accelerating materials development.¹³⁹

3.2.2.1. Battery energy storage. A battery stores electrical energy for later use. It has gained significant attention and adoption in various applications, including renewable energy integration, grid stabilization, electric vehicles, and backup power systems in the different types of Li-ion batteries,¹⁴⁰ lead-acid batteries,¹⁴¹ and so on. Battery energy storage systems typically do not utilize porous media directly in their operation. However, there are certain aspects where porous media can indirectly affect battery energy storage such as electrode structures.¹⁴² Ongoing research focuses on improving battery performance and durability through the design and optimization of porous electrode structures, advanced porous separators, and thermal management systems. These advancements aim to enhance energy storage capacity, cycling stability, and safety of battery systems. The integration of ML techniques with battery energy storage systems can enhance their performance, control, and optimization.¹⁴³ While the direct involvement of porous media in battery operation is limited, ML can be applied in several areas to improve battery energy storage. ML can aid battery energy storage systems in terms of state-of-charge (SoC) and state-of-health (SoH) estimation,¹⁴⁴ battery material design and optimization,¹⁴⁵ battery performance and lifetime prediction,¹⁴⁶ and optimal control and energy management.¹⁴⁷

Some researchers have utilized ML techniques in conjunction with battery energy storage. In a study, Ishikawa *et al.*¹⁴⁸ examined the structural characteristics of positive and negative electrodes in lithium-ion batteries. Using an ML model, they formulated a correlation equation for effective ion conductivity by considering the unique features of each electrode layer. The negative electrode is made up of graphite particles that have a flat shape, which means their aspect ratio is a significant factor in determining tortuosity. On the other hand, the positive electrode is a secondary aggregate, and the tortuosity is dependent on particle morphology, which makes it difficult to determine relevant parameters. Using the SVM, they predicted the tortuosity of the negative electrode in terms of the particle aspect ratio through nonlinear regression. All in all, this study

sheds light on the relationship between tortuosity and other structural properties or images and can be applied in various fields related to porous materials to help optimize structural designs. In a study by Weber *et al.*,¹⁴⁹ they efficiently approximate the macroscopic response of batteries. Some approaches, such as direct numerical simulations of transport at the pore-scale on reconstructed or synthetically generated images of electrodes that include detailed topological information about the pore structure, were employed. High-fidelity simulations have also been used to train CNNs to estimate effective battery properties directly from images of porous electrodes. In addition, they combined CNN methods with homogenization theory to take advantage of effective medium formulations and reduce the computational cost associated with individual pore-scale simulations. A noise sensitivity analysis is conducted to evaluate CNN's robustness, and it is shown to accurately predict the effective properties of real battery electrodes using both 2D and 3D images. Jiang *et al.*¹⁵⁰ presented a study to understand the behavior of battery particles in a lithium-ion battery which is a complex challenge. The microstructure of a composite electrode plays a crucial role in determining how these particles are charged and discharged. To tackle this challenge, they used a combination of experimental approaches, statistical analysis aided by ML, and mathematical modeling. They also explored the potential of using electron density as a proxy for SoC.

3.2.2.2. Supercapacitor energy storage. Supercapacitors, also known as ultracapacitors or electrochemical capacitors, store energy through the electrostatic adsorption of ions on the surface of electrodes. They have high power density, fast charge and discharge rates, and long cycle life. Supercapacitors are often used in applications requiring rapid energy storage and release, such as regenerative braking systems and power buffering in renewable energy systems.¹⁵¹ Porous media can play a crucial role in the design and performance of supercapacitors. Research efforts in supercapacitor technology often focus on optimizing the pore structure, pore size distribution, and surface area of the porous media to improve the energy density, power density, and cycling stability of supercapacitors.¹⁵² ML and computational modeling techniques are also employed to predict and optimize the performance of supercapacitors by considering the complex interactions between porous media, electrolyte, and electrode materials. ML can aid supercapacitors with porous media in different ways such as electrode material design, performance prediction, state of health monitoring, control, energy management, and material characterization.¹⁵³

Researchers have used ML techniques along with supercapacitors. In a study by Saad *et al.*,¹⁵⁴ they presented graphene-based nanocomposites that have emerged as promising active components for high-capacity supercapacitor electrodes in energy storage systems. For the sake of predictions, the ML models (KNN, decision tree regression (DTR), Bayesian ridge regression (BRR), and ANN) utilized various electrochemical measurements such as electrolyte ionic conductivity and electrolyte concentration and physicochemical features such as atomic percentages, pore size, and pore-volume. Among these, the ANN model demonstrated the highest accuracy, with RMSE and R^2 values of 60.42 and 0.88, respectively. Rahimi *et al.*¹²²



mentioned that the multi-physio-chemical features of the activated carbon (AC) material play a synergistic role in enhancing the capacitance performance of supercapacitors. A multi-layer perceptron neural network (MLP-NN) model predicts the *in-operando* performance of N/O co-doped AC, using electrode materials. The results show that the training algorithms in the MLP-NN model have high feasibility in predicting AC performance with minimal error. The model provides valuable insights into possible procedures for fabricating N/O co-doped porous carbon electrodes with maximized specific capacitance. Finally, the genetic algorithm predicts the optimal AC in 6 M KOH in a three-electrode system with a specific capacitance of 550 F g^{-1} at 1 A g^{-1} , which can be used for practical applications. In another study by Gosh *et al.*,¹⁵⁵ a combinatorial approach that leverages value and grade prediction ML models was used to predict the performance of a novel material, cerium oxynitride, for use in supercapacitor applications. The model predicts that this material will have a specific capacity of approximately 26.6 mA h g^{-1} and a capacity retention of over 90%. Experimental results have validated this predictive approach, with an observed specific capacity of approximately 26 mA h g^{-1} and 100% capacity retention. Lu *et al.*¹⁵⁶ introduced a novel ML approach for both electrochemical sensors and supercapacitors using a carbonized metal-organic framework (C-ZIF-67). An ANN algorithm is employed as a powerful tool to achieve intelligent analysis of niclosamide (NA) and incorporates theoretical calculations to optimize the structure of the sensing material and predict its adsorption and binding energy. Results show that the developed sensor exhibits excellent electrochemical response, with a 196.6-fold improvement compared to bare GCE for NA, wider linear ranges of intelligent analysis from 1 nm to 9 μm , and a low limit of detection of 0.3 nm. The ML model with the ANN algorithm is also utilized to predict the performance of the supercapacitor, which exhibits a capacitance of 336.67 F g^{-1} at a current density of 2 A g^{-1} and shows excellent prediction accuracy.

3.2.2.3. Fuel cell energy storage. Fuel cells are electrochemical devices that convert the chemical energy of a fuel, typically hydrogen, into electrical energy through an electrochemical reaction. While fuel cells themselves do not directly use porous media, they often incorporate porous materials to facilitate efficient reactions and enhance performance.¹⁵⁷ Research and development efforts in fuel cell technology often focus on optimizing the design and performance of porous media within fuel cell components. The combination of fuel cell energy storage and porous media with ML techniques offers several potential benefits for performance optimization, control, and system integration. ML can aid fuel cell energy storage systems utilizing porous media in terms of performance prediction and optimization, optimal control and energy management, design and material optimization, and system integration and sizing.¹⁵⁸ The application of ML to fuel cell energy storage systems with porous media is an active area of research and development.¹⁵⁹ Designing the flow field is crucial in proton exchange membrane (PEM) fuel cells as it greatly affects gas transfer, water discharge, electron conductance, and heat transfer. The use of porous media flow fields, such as metal

foam, shows potential for enhancing cell performance by providing uniform distributions of oxygen, liquid, current density, and temperature, particularly in the concentration polarization regime.

Scientists have employed ML methods in conjunction with fuel cells. Zhang *et al.*¹⁵⁹ utilized a data-driven surrogate model, supported by the SVM, to optimize the geometry of the porous media flow field. Results demonstrate that the SVM-based data-driven surrogate model yields similar predictions to the 3D physical model. Furthermore, the genetic algorithm (GA) is utilized for optimization, and the optimized values obtained from the surrogate model are validated using the 3D physical model, confirming the effectiveness of the proposed data-driven surrogate model in the design and optimization of the porous media flow field. In a study by Liu *et al.*,¹⁶⁰ they utilized the deep convolutional generative adversarial network (DCGAN) deep learning method to reconstruct the three-dimensional (3D) porous structure of the fuel cell catalyst layer using microstructure graphs obtained from focused ion beam scanning electron microscopy (FIB-SEM) as training data. The DCGAN with interpolation in latent space generates spatial-continuous microstructure graphs that are used to construct a unique 3D microstructure of the CL without the need for real FIB-SEM data. Different interpolation conditions in the DCGAN are also explored to optimize the ultimate structure by incorporating real data such as porosity, particle size distribution, and tortuosity. Additionally, the comparison between real and generated structural data shows that the data generated by the DCGAN have an adjacency relationship with real data, indicating its potential applicability in the field of electrochemical simulation with reduced costs.

3.2.3. Hydrogen gas energy storage. Hydrogen energy storage involves the use of hydrogen gas as a means of storing and releasing energy. Hydrogen can be produced through various methods, such as electrolysis of water or reforming of natural gas, and stored for later use in various applications.¹⁶¹ Porous media can be utilized for energy storage in the context of hydrogen gas. In both cases, the choice of porous media is critical to optimize storage capacity, adsorption/desorption kinetics, and overall system performance. The porosity, surface area, and adsorption properties of the media impact the storage capacity and release characteristics. Additionally, proper design, safety considerations, and system integration are crucial factors when implementing energy storage using porous media for hydrogen gas.¹⁶² ML techniques can play a significant role in optimizing and enhancing energy storage systems based on hydrogen gas. While the application of ML in the field of hydrogen gas energy storage is still emerging, it holds great potential for optimizing system performance, improving safety, enhancing operational efficiency, and facilitating the integration of these energy carriers into a broader energy landscape.¹⁶³ Hydrogen energy storage using porous media, aided by ML techniques, holds promise for optimizing storage performance, enhancing efficiency, and enabling intelligent control. Porous media can be employed for hydrogen storage, enabling the storage and release of hydrogen gas for various applications,



including fuel cells, transportation, and renewable energy integration.¹⁶⁴

Scientists have employed ML methods in combination with hydrogen energy storage with porous materials. Gopalan *et al.*¹⁶⁵ developed a highly efficient and accurate method for predicting hydrogen adsorption in porous materials. Their approach involves calculating the amount of adsorption at any given temperature and pressure by integrating the energy density of the adsorption sites (guest–host interactions) and adding an average guest–guest term. To calculate guest–host interaction energy, they use a classical force field with hydrogen modeled as a single-site probe. For guest–guest interaction energy, they approximate an average coordination number using Gaussian process regression (GPR). Their method was tested on 933 MOFs, ranging from 10^{-5} to 100 bar at 77 K. Their analysis showed that 13 MOFs exceeded the Department of Energy target of 50 g L^{-1} for adsorption at 100 bar, 77 K, and desorption at 5 bar, 160 K. In a study by Bucior *et al.*,¹⁶⁶ they developed a data-driven approach that accelerates material screening and learns structure–property relationships. They created new descriptors for gas adsorption in MOFs based on the energetics of MOF–guest interactions. The model parameters demonstrate that a slightly weak attraction between hydrogen and the framework is ideal for cryogenic storage and release. As a case study, they applied this method to screen a database of more than 50 000 experimental MOF structures and identified MFU-4l as one of the top candidates. Rahimi *et al.*¹⁶⁷ constructed and tested three ML models to predict the hydrogen adsorption of ACs. The data-based modeling considers crucial properties of ACs' structural characteristics, such as micropore surface area, pore volume, and pore-size distribution, as inputs for hydrogen adsorption. They found that the proposed models were highly feasible for predicting hydrogen uptake, with RMs ranging from 0.06 to 0.19. Among them, the SVM model demonstrated the highest accuracy in predicting hydrogen adsorption on ACs. Using the SVM-based GA technique, they optimized the effects of microstructure properties on hydrogen storage. By using the optimal structural properties obtained from GA, they were able to increase hydrogen uptake by 2.5 wt%.

3.2.4. Hybrid energy storage. Hybrid energy storage refers to the combination of multiple energy storage technologies or systems to create a hybridized energy storage solution. By integrating different storage technologies, hybrid systems aim to leverage the unique strengths and capabilities of each technology to achieve enhanced performance, improved efficiency, and optimized energy management. Hybrid energy storage systems are an evolving field, and ongoing research and development efforts focus on optimizing system configurations, improving control strategies, and exploring new combinations of storage technologies.¹⁶⁸ These efforts aim to further enhance the performance, flexibility, and scalability of hybrid energy storage for various applications, including renewable energy integration, grid support, and energy management. Hybrid energy storage systems that incorporate porous media can provide enhanced performance and flexibility in storing and utilizing multiple forms of energy.¹⁶⁹ Additionally, hybrid energy storage systems using porous media, aided by ML

techniques, have the potential to optimize energy storage performance, improve system control, and enhance overall efficiency. The integration of porous media and ML techniques in hybrid energy storage systems offers the potential for improved energy storage performance, system optimization, and intelligent control. Ongoing research and development efforts focus on advancing these technologies to enhance the efficiency, reliability, and scalability of hybrid energy storage for various applications, including renewable energy integration, grid support, and demand management.¹⁷⁰

3.2.4.1. Thermal-electrical hybrid energy storage. This hybrid system combines thermal energy storage (TES) with electrical energy storage (EES) using porous media. Excess electricity is first converted into thermal energy and stored in a porous medium, such as PCMs or hot water/steam in a thermal storage tank.¹⁷¹ When electricity demand is high, the stored thermal energy is converted back into electricity using a thermodynamic cycle or through a heat exchanger. This approach enables the efficient utilization of both electrical and thermal energy, making it suitable for applications such as combined heat and power (CHP) systems or district heating and cooling. The integration of porous media and ML techniques in thermal-electrical hybrid energy storage systems holds great potential for achieving enhanced energy storage performance, efficient energy management, and optimized system control. Ongoing research and development efforts aim to further advance these technologies and improve the scalability, reliability, and cost-effectiveness of thermal-electric hybrid energy storage systems.¹²⁴

3.2.4.2. Electrochemical-thermal hybrid energy storage. In this hybrid system, electrochemical energy storage, such as batteries or supercapacitors, is combined with thermal energy storage using porous media. Excess electrical energy is first stored in the electrochemical storage system. When there is a demand for thermal energy, the stored electrical energy is converted into heat using resistive heating or other means and stored in a porous medium, such as high-temperature PCMs or solid-state materials. The stored thermal energy can later be utilized for heating applications or power generation. This hybrid approach can provide a more flexible and efficient utilization of energy for both electrical and thermal requirements.¹⁷² Electrochemical-thermal hybrid energy storage systems that incorporate porous media, aided by ML techniques, offer promising solutions for efficient energy storage and management and hold great potential for achieving enhanced energy storage performance, efficient energy management, and optimized system control. Ongoing research and development efforts aim to further advance these technologies and improve the scalability, reliability, and cost-effectiveness of electrochemical-thermal hybrid energy storage systems.¹⁷³

3.2.5. Combustion. A combustion process refers to the chemical reaction between a fuel and an oxidizer that produces heat and light. It involves the rapid combination of fuel molecules with oxygen molecules, resulting in the release of energy in the form of heat and the production of combustion products.¹⁷⁴ Combustion using porous media refers to a process



where a fuel–air mixture is burned within a porous medium.¹⁷⁵ The porous media acts as a matrix that facilitates combustion by providing a large surface area for reaction and allowing for efficient mixing of fuel and oxidizer.¹⁷⁶ Combustion processes can be aided by ML techniques to enhance combustion efficiency, optimize performance, and improve control.¹⁷⁷ The integration of ML techniques with porous media in combustion systems holds promise for enhancing combustion efficiency, emission control, and system performance. Ongoing research and development efforts aim to further advance these technologies and optimize their application in various combustion processes, including power generation, heating systems, and industrial applications. To conduct a thorough study of micro-scale integrated hydrogen production systems, one must dedicate significant computational efforts to account for complex phenomena such as reaction kinetics.

Researchers have utilized ML techniques to enhance the efficiency of combustion systems. In a study by Pourali and Esfahani,¹²⁵ they developed an innovative approach that combines ML for data generation (pre-processing), analytical techniques for processing, and response surface methodology for post-processing to investigate an integrated hydrogen production system. They used the decision tree algorithm to establish appropriate correlations for the species' net rate, mixture properties, and heat of reactions based on a detailed reaction mechanism of methane steam reforming and combustion in the pre-processing step. The findings suggest that wall thickness is the most influential parameter in CH₄ conversion and system efficiency, while combustor height is the most critical parameter for sustaining combustion in the integrated system. Lastly, they propose five optimized designs of the integrated system for constructing experimental prototypes. In another study, Jiang *et al.*¹⁷⁵ utilized wheat straw, corn straw, and sorghum straw as raw materials. Using KOH and NaOH as catalysts, they prepared straw pyrolytic carbon (SPC) and analyzed the characteristics of combustion activation energy (AE) through thermogravimetric analysis. They proposed predictive models of combustion AE based on linear regression (LR), SVR, and random forest regression (RFR) and compared their results. In the LR, SVR, and RFR models, R^2 values reached 0.8531, 0.9048 and 0.9834, respectively. The RFR model was found to be more suitable for the AE prediction of alkali-catalyzed SPC compared to the LR and SVR models.

3.3. Electrochemical devices

The advancement of porous electrocatalytic materials primarily depends on empirical approaches, involving extensive trial-and-error methods.¹⁷⁸ Discovering optimal solutions for multicomponent catalysts across diverse reaction conditions demands substantial investments of time and effort. However, in recent years, the landscape has undergone a revolutionary transformation with the emergence of ML techniques. These powerful ML tools have revolutionized the development and exploration of materials designed for electrochemical devices.¹⁷⁹ This section presents a comprehensive review of ML-based techniques for discovering and developing porous media

for electrochemical devices. It also highlights practical applications in various fields such as electrocatalysts, proton exchange membrane water electrolyzers (PEMWEs), PEM fuel cells (PEMFCs), solid oxide fuel cells (SOFCs), batteries, and supercapacitors.

Fig. 8a depicts design parameters in an ANN for the prediction of SOFC cell performance. Fig. 8b shows a schematic of a PEMWE, Fig. 8c shows an SOFC voltage prediction using an ANN model, and Fig. 8d displays a PEMFC catalyst layer with SVM polarization curve prediction. In electrochemical reactions, two half-reactions take place: one at the anode, such as the oxygen evolution reaction (OER), and the other at the cathode, encompassing reactions such as carbon dioxide reduction, hydrogen evolution reaction (HER), nitrogen reduction, and the oxygen reduction reaction (ORR).¹⁷⁸ These reactions are powered by the flow of electrons. Effective catalysts play a crucial role in optimizing efficiency and minimizing overpotential during these processes.¹⁷⁸

3.3.1. Electrocatalysts. Electrocatalysts play a crucial role in shaping a sustainable future by facilitating the generation of clean fuels, mitigating the effects of global warming, and offering solutions to environmental pollution. The progress in ML offers a pathway to overcome the limitations of traditional approaches to discovering new electrocatalysts.¹⁸⁴ In this review, we emphasize the current advancements in ML-driven approaches that have facilitated the discovery and optimization of porous electrocatalysts at an accelerated pace. Xia *et al.*¹⁸⁵ investigated nanoporous carbon-based electrocatalysts for the ORR. They used k-nearest neighbor regression (KNN), SVR, and RFR methods to choose the best porous solid supports for anchoring metal particles. Various descriptors, including Brunauer, Emmett, and Teller (BET) surface area, nitrogen content, and the I_D/I_G ratio, were used as inputs and four descriptors, namely, half-wave potential, onset potential, current density, and electron transfer number, were employed to represent the ORR performance. Based on RSME and MAE results, RFR accurately predicted the best ORR performance by considering the most important materials descriptors which were BET surface area and nitrogen content. Defective nitrogen-doped graphene nanomesh was identified as a highly promising matrix for loading metal-based catalysts, exhibiting maximum onset potential and superior electrocatalytic performance for the ORR. Zhou *et al.*¹⁸⁶ investigated the OER process in covalent organic framework (COF)-based electrocatalysts which are an emerging type of porous crystalline materials. They presented a new methodology to select the best M-N_xO_y-based catalyst candidate among thousands of possible COF structures *via* combining ML and DFT methods. The GBR algorithm was used to find the most crucial factors affecting the adsorption properties. The RMSE and R^2 were employed to evaluate GBR which showed that ML methodologies can be applied in catalyst design. They also selected Ni-COF as the best candidate catalyst and experimentally synthesized it which showed the highest OER activity and stability among COF-based OER catalysts. Ebikade *et al.*¹⁸⁷ conducted a study that explored the relationship between catalyst synthesis conditions, structural properties, and performance. Their specific focus was on the synthesis



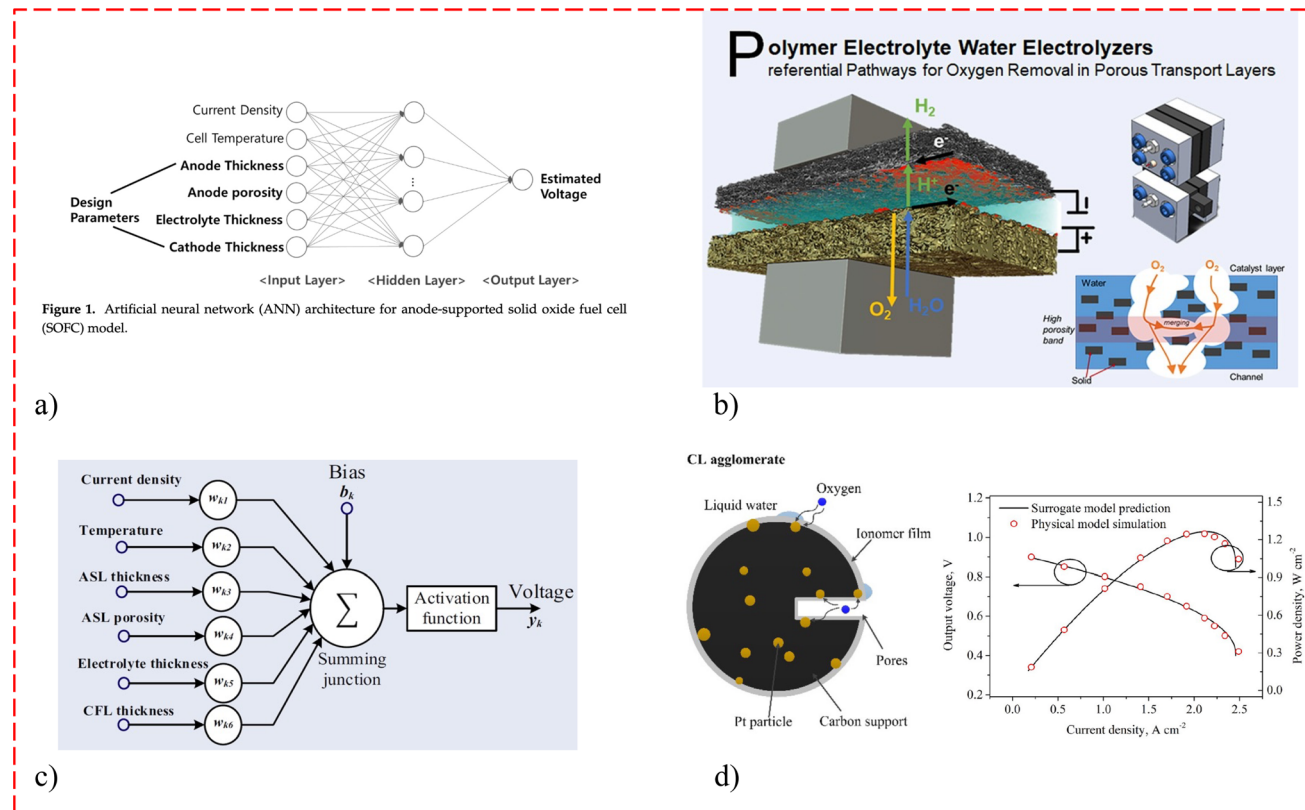


Fig. 8 (a) The optimization of multiple parameters such as anode and cathode thickness, anode porosity, and electrolyte thickness included in an ANN for the prediction of voltage of an SOFC and improve its performance,¹⁸⁰ reproduced with permission from MDPI. (b) In order to distinguish oxygen within the PTL, machine learning was utilized to analyze the amount of oxygen present in the PTL of the electrolyzers at varying flow rates and current densities which is shown in 3D representation of a conventional PEWE,¹⁸¹ reproduced with permission from Cell Press, (c) prediction of cell voltage in the SOFC using an ANN model using current density, temperature, anode, cathode, and electrolyte thickness,¹⁸² reproduced with permission from Elsevier, and (d) schematic of distribution of water, platinum, ionomer, and carbon support in the PEMFC catalyst layer, including prediction of the SVM for the polarization curve compared against a physical model,¹⁸³ reproduced with permission from Elsevier.

of nitrogen-doped catalysts (NDCs) for the HER. Using active learning-based optimization and ML techniques such as regression, partial least squares (PLS), and principal component analysis (PCA), they efficiently determined the optimal pyrolysis conditions. The ML models were trained using a dataset that comprised both structural features (such as micropore volume, BET surface area, and crystallinity) and synthesis conditions as inputs and current density and onset potential as outputs. An important discovery from their research is that the performance of NDCs was influenced by factors such as the pore structure, nitrogen dopants, and material disorder. Overall, their methodology offered valuable insights into the synthesis, structure, and performance of catalysts, providing a systematic approach for optimizing electrochemical catalysis. To achieve net-zero emissions, researchers are particularly interested in the electrochemical evolution of H₂ using catalysts. Given the difficulty of designing catalysts, Zheng *et al.*¹⁸⁸ presented a data-driven strategy for developing optimized catalysts for H₂ evolution. Based on previous studies, they created a database of Pt/C catalysts for H₂ evolution and used ML to reveal the significance of various features such as the properties of Pt, the pore volume, and the specific surface area of carbon support on catalytic performance. According to the algorithms, the Pt size

and content had the highest influence on the catalyst overpotentials. They created size-controllable Pt nanoclusters that are anchored on an N-doped mesoporous carbon nanosheet network which had higher catalytic activity in alkaline electrolytes than current commercial catalysts. Pourali *et al.*¹⁸⁹ examined hydrogen production through ammonia decomposition using a novel setup involving a porous catalytic shell and tube reactor. They investigated the correlation between eight process variables, which include factors related to the reactor's structure and operation, and their impact on the overall system performance. To achieve this, they utilized CFD, ANN, and response surface methodology (RSM). The study demonstrated that the porosity of the catalyst significantly affects the pressure drop along the reactor, emphasizing the need for optimization to minimize any detrimental effects on system performance. Chen *et al.*¹⁹⁰ devised a methodology combining laboratory experiments and the ML method to expedite the creation and development of catalysts through the example of selective catalytic reduction (SCR) of nitrogen oxides (NO_x). Their approach included training an ANN model using experimental data (62 variables including specific surface area, the pore volume, and size) from relevant publications, screening candidate catalysts using the trained model, experimentally synthesizing, and



characterizing the candidates, updating the ML model with the new experimental results, and reevaluating candidate catalysts with the updated model. This process was repeated to attain an optimized catalyst. By employing this iterative approach, an innovative SCR NO_x catalyst was discovered and successfully synthesized after four iterations, exhibiting desirable features. The versatility of this approach enabled its application to the screening and optimization of other catalyst designs, thereby presenting significant opportunities for the exploration of various materials.

3.3.2. PEM water electrolyzers. Sustainable and clean energy consumption is vital for technological development, necessitating the exploration of new energy vectors such as hydrogen, which can be produced through chemical and electrochemical processes.¹⁹¹ PEM water electrolysis remains the preferred choice for producing clean and pure hydrogen, as it offers sustainability and a carbon footprint-free solution.¹⁹¹ Günay *et al.*¹⁹² employed regression trees and classification modeling to analyze a large database from previous publications on PEM electrolyzers. Box and whisker plots revealed that the utilization of Ti porous structures in the electrodes contributed to enhanced performance. The classification tree models highlighted the key variables that influenced the performance of the electrolyzer, showcasing the crucial roles played by the mole fraction of Ni on the cathode surface and the mole fraction of Co on the anode surface, in addition to current density and potential. Furthermore, the regression tree method effectively captured and simulated the polarization behavior of the electrolyzer, showcasing a remarkable RMSE. In their new study, Günay *et al.*¹⁹³ employed local interpretable model-agnostic explanations (LIMEs) as a local surrogate model to investigate the impact of different factors on current/power density and polarization in PEM and anion exchange membrane (AEM) electrolysis systems. Their findings suggested that while material properties mainly influence power density, the catalytic properties of electrodes play a primary role in affecting current density and polarization. To enhance the performance of the PEM water electrolyzer, it is crucial to understand how the morphology of the porous transport layer (PTL) relates to the removal of oxygen. Satjaritanun *et al.*¹⁸¹ employed *operando* X-ray computed tomography and ML techniques on a model electrolyzer. Their objective was to examine the oxygen content within the PTLs and its correlation with both the current density and the water flow rate. Also, they determined whether oxygen exhibits preferential pathways while being transported through the PTL. The observed oxygen distribution was attributed to the PTL's low tortuosity and its high porosity which enabled preferential oxygen flow.

3.3.3. PEM fuel cells. Proton exchange membrane fuel cells (PEMFCs) play a vital role in achieving an environmentally friendly society by serving as energy conversion devices for hydrogen energy. However, their cost and performance still present challenges for large-scale commercialization. The complex nature of PEMFCs involves multiple simultaneous physical and chemical processes occurring at different scales. The gas diffusion layer (GDL) plays a crucial role in facilitating the movement of electrons, gases, and liquid water within

PEMFCs as it acts as a connecting component between the flow field and the catalyst layer.¹⁹⁴ ML and AI can be utilized to optimize the design of GDLs which includes optimizing factors such as porosity, pore size distribution, and permeability. Zhang *et al.*¹⁹⁵ successfully developed a data-driven surrogate model based on the SVM for optimizing the porous media flow field in PEMFCs. By training the SVM model on a small dataset obtained from a validated 3D physical model, they successfully established a relationship between the inputs (fiber distance, fiber diameter, and output voltage) and the output (current density). The surrogate model enabled accurate cell performance prediction at different porosities, closely matching the outcomes of a computationally taxing 3D physical model. They asserted that the use of SVM, specifically chosen for its suitability with small datasets, mitigates over-training issues and ensures reliable predictions. The study identified optimal porosity values with impressively high current densities and a negligibly small relative error by incorporating the SVM-based surrogate model into the GA optimization process. Wang *et al.*¹⁹⁶ conducted a comprehensive study on the effect of various factors, such as porosity, thickness, and electrical conductivity of GDL, on PEMFC performance. Both RSM and ANN models were employed to optimize the physical parameters of the GDL, aiming to maximize cell performance and achieve a uniform oxygen profile within the cathode electrode. Upon validation using average R^2 and RSME, as the training sample size grew, the prediction accuracy of ANN models surpassed that of RSM. Through the utilization of a physics-based model and experimental validation, the optimization of input parameters using the ANN and RSM resulted in notable enhancements in current density and the standard deviation of oxygen distribution. Pourrahmani *et al.*¹⁹⁷ conducted a study addressing water column formation in the gas GDL of PEMFCs, which can negatively impact performance. They explored the influence of GDL porosity and permeability on liquid water removal within the GDL and PEMFC performance. Increased GDL liquid removal rates were associated with enhanced PEMFC performance, including reduced degradation, extended lifespan, and improved cold-start capabilities. The study utilized variable parameters of GDL porosity and permeability, with maximum GDL liquid water removal as the output parameter. Error evaluation using MSE, RMSE, and R^2 confirmed the suitability of the developed ANN model. The findings demonstrated that increasing GDL porosity enhances liquid removal within the GDL, while a specific range of permeability values yields optimal water removal results. Notably, higher GDL porosity values reduce resistance to liquid and gas phase movement, resulting in improved power densities and more efficient water management in PEMFCs. Pourrahmani *et al.*¹⁹⁸ evaluated the impact of porous media as an inserted layer within the gas flow channel on PEMFC performance. Using 66 simulation datasets, ANN models were created to forecast the output values of the Nusselt number, voltage, pressure drops, and power density by considering the input parameters of thickness, current density, and viscous resistance. At high current densities, the study revealed that power densities were predominantly affected by viscous resistance,



whereas improved performance was achieved with thicker inserted porous layers. After confirming the accuracy of the ANN models through regression values and MSE, the study employed these models to define an evaluation criterion of the proton exchange membrane (ECPEM) that considered the simultaneous optimization of output parameters. Li *et al.*¹⁹⁹ developed a comprehensive framework integrating a 3D CFD model, kernel extreme learning machines (KELM), and an improved gray wolf optimizer (IGWO) for PEMFC modeling and optimization. KELMs exhibited superior generalization ability and rapid convergence and eliminated the need for manual parameter adjustment and local optimal solutions, providing a notable advantage in handling low-dimensional data. The framework considered operating parameters (cell voltage, oxygen flow rate, and operating pressure) and geometric parameters (GDL thickness and porosity) to collect reliable data. Higher GDL porosity improved reactant diffusion but increased ohmic resistance, impacting voltage drop and current density. The KELM model achieved excellent agreement with CFD simulation results, demonstrating high R^2 and a minimum of MSE and MAPE values. The proposed model determined optimal values for various parameters, resulting in a significant maximum power density. It is worth noting that the coupling of KELMs and the IGWO not only addressed critical challenges in the fuel cell field but also exhibited great potential for fuel cell design and control. Cawte *et al.*²⁰⁰ evaluated various ML methods to forecast the air diffusivity and water permeability in GDL porous media in a PEMFC system, under multiphase and single-phase flow conditions. The implemented algorithms were SVR, DTR, GBR, RFR, KNR, ANN, and ELN. Among the algorithms tested, GBR emerged as the most successful, while the ANN and SVR exhibited comparable performance in predicting single-phase transport properties. In single-phase properties, fiber orientation and the porosity of the material were identified as the most crucial parameters, while for multiphase transport conditions, saturation emerged as the predominant parameter across all models.

The composition and microstructure of the catalyst layer (CL), which serves as the central electrochemical reaction region in PEMFCs, play a pivotal role in determining the output performance of PEMFCs. Wang *et al.*¹⁸³ established an SVM model combined with a GA to globally optimize multiple variables and enhance the maximum power density of PEMFCs. The database was formed using simulation results from a CFD model coupled with a CL agglomerate model. After the surrogate model was developed, prediction performance was assessed using RMSE, R^2 , mean percentage error, and maximum percentage error to evaluate model performance. For verification, the optimal CL composition was returned to the physical model and a good agreement was achieved. Additionally, the porous structure of the CL in PEMFCs is crucial for oxygen transfer resistance and charge/discharge performance. Using microstructure graphs acquired from focused ion beam scanning electron microscopy (FIB-SEM), Liu *et al.*²⁰¹ employed a deep convolutional generative adversarial network (DCGAN) to reconstruct the 3D porous structure of the CL in PEMFCs. Different interpolation conditions in the DCGAN were explored

to optimize the generated structure, aligning it with real data in terms of particle size distribution, porosity, and tortuosity. Comparisons between generated structural and real data demonstrated the adjacency relationship, suggesting the potential application of DCGAN-generated data in electrochemical simulations with reduced costs. The cathode catalyst layer (CCL) in PEMFCs plays a crucial role in facilitating mass, charge, and heat transfer. Traditional methods are insufficient for a comprehensive understanding of the CCL. As a new approach, Lou *et al.*²⁰² employed an ML model to investigate the structure of the CCL. By integrating the XGBoost algorithm with the PEMFC physical model, this model effectively established a relationship between nine adjustable parameters (such as Pt loading, agglomerate radius, pore diameters, and CCL thickness) and optimization goals (power density, current density, and temperature uniformity of the CCL). The model achieved high accuracy, with an R^2 value greater than 0.95 and an RMSE value less than 0.05, indicating its strong predictive capabilities. Their results indicated that the critical parameters for multi-objective optimization are the Pt loading, agglomerate radius, ratio of Pt to carbon, and CCL thickness. Implementing an optimized CCL leads to improvements in power density and current density and a reduction in Pt loading. Vaz *et al.*²⁰³ employed an MLP model for multi-objective optimization analysis to assess the impacts of different compositions in the CCL on single-cell voltage and stack cost. Four important parameters of the cathode CL, namely Pt loading, ionomer to carbon weight ratio, Pt to carbon weight ratio, and cathode CL porosity, were treated as design variables. The 85 CFD simulation database from a comprehensive three-dimensional, multi-scale, two-phase PEMFC model was utilized to train and validate the MLP model. The accuracy of the MLP model was verified using metrics such as RSME and adjusted R^2 . The optimization process led to significant cost reduction by minimizing Pt usage and simultaneously resulted in noteworthy improvements in single-cell voltage.

3.3.4. Solid oxide fuel cells. SOFCs have garnered ongoing interest due to their numerous benefits, which include high power efficiency, fuel adaptability, environmentally friendly design, and relatively affordable production. Xu *et al.*²⁰⁴ introduced a methodology that leveraged CFD, ANN, and GA to enhance the performance of SOFCs. They compared 19 commonly used algorithms among which the ANN had the highest R^2 and lowest MAE, so the ANN was chosen to connect inputs and outputs. The impact of 10 inputs, namely, microstructure (anode, cathode, and electrolyte porosity), operating conditions (temperature, pressure, cathode, and anode mass flow rate, and molar fractions of H_2), and geometry (airway surface liquid (ASL) thickness and channel width) properties on power density output was investigated. Then, the optimal operating parameters were used to establish a CFD model for validation GA. Liu *et al.*²⁰⁵ introduced a homogenization framework that utilized DL to establish a link between the microstructures of porous nickel/yttria-stabilized zirconia anodes in SOFCs and their macroscopic properties. By employing the finite element method and mesoscale kinetic Monte Carlo method, they generated a range of 3D



microstructure images to discover the best SOFC anodes with a proper microstructure (porosity and Ni%) and effective mechanical properties (elastic properties, coefficient of thermal expansion, and the triple-phase boundary length density). Thereafter, these 3D images were used as inputs and macroscopic properties were used as outputs to train a DL model based on the CNN. The model successfully predicted the values of these properties for new samples, showcasing exceptional predictive performance compared to the actual values. Nassef *et al.*¹⁸² employed an ANN to simulate the SOFC by leveraging experimental data. The simulation was utilized to identify the optimal operating parameters of the SOFC by an efficient and reliable optimization algorithm known as the radial movement optimizer. The parameters considered during the optimization process included anode support layer thickness, anode porosity, electrolyte thickness, and cathode interlayer thickness. Meanwhile, the output variable of the ANN was the voltage. By adopting this approach, the power density greatly surpassed that achieved through experimental and genetic methods. Fathy *et al.*²⁰⁶ employed an ANN model to predict the terminal voltage of the SOFC using six inputs. They utilized a moth-flame optimizer (MFO) to estimate optimal values for various parameters of the SOFC model, including ASL thickness, ASL porosity, electrolyte thickness, and cathode functional layer thickness. The results demonstrated that their ANN-MFO approach significantly improved the SOFC power output, affirming the effectiveness of ML in enhancing the power generation of SOFCs. Sciazko *et al.*²⁰⁷ employed an ML-based image processing framework to accurately reconstruct the 3D structures of carbon deposition within the porous anode of SOFCs. By utilizing a U-net neural network with multiple inputs, they successfully identified unfilled pores, enabling the phase segmentation of unaltered SEM images without resin infiltration. The innovative microstructure evaluation framework significantly contributed to quantitative investigations of carbon deposition in pores, as well as the development of effective mitigation strategies for SOFC anodes. Song *et al.*¹⁸⁰ developed an anode-supported SOFC model using an ANN and optimized design variables. The model incorporated input parameters to estimate the voltage of the SOFC. They optimized four design parameters: electrolyte thickness, anode thickness, cathode thickness, and anode porosity using a multi-armed bandit algorithm. Golbabaei *et al.*²⁰⁸ introduced several ML approaches to forecasting the output voltage of anode-supported SOFCs. The MLP regressor stood out as the superior model among others for accurately predicting the output voltage of an anode-supported SOFC. The model considered key operational parameters such as temperature, anode-supported porosity and thickness, electrolyte thickness, cathode functional layer thickness, and current density.

Solid oxide electrochemical cells (SOCs) are versatile energy conversion devices that can function as either fuel cells or electrolysis cells. In the fuel cell mode (SOFC), they produce electricity by oxidizing fuel, while in the electrolysis mode (SOEC), they convert electricity into chemical energy stored as fuel. Wang *et al.*²⁰⁹ introduced a data-driven surrogate model that utilized the SVM regression algorithm to establish

a relationship between fabrication parameters (including volume fractions of NiO, YSZ, and pore former phases, as well as initial average particle size) and electrode overpotentials. The model demonstrated fast and accurate prediction of the electrochemical performance of heterogeneous porous electrodes. Specifically, the volume fractions of YSZ were identified as a crucial factor influencing the overall overpotential.

3.3.5. Redox flow batteries. Redox flow batteries (RFBs) have emerged as a promising solution for addressing the challenges of intermittent renewable energy sources. To enable the widespread adoption of RFBs, improvements are needed in various components, including the discovery of high-energy-density redox couples, optimization of electrode and membrane microstructures, and enhancement of flow field design. These improvements aim to enhance the overall performance, efficiency, and cost-effectiveness of RFBs.

The optimization of electrode microstructures has been investigated in the literature using a combination of ML methods, lattice Boltzmann method (LBM) simulations,²¹⁰ and pore network modeling (PNM).²¹¹ In one study, artificial fibrous electrode microstructures were generated using stochastic reconstruction methods and morphological algorithms, and their hydraulic permeability was evaluated using the LBM.²¹⁰ ML models such as linear regression, ANN, and random forests (RF) were utilized, along with the genetic algorithm NSGA-II, to identify microstructures with high specific surface area and hydraulic permeability. The workflow resulted in the discovery of microstructures exhibiting microstructures with significant improvements compared to commercial carbon felt electrodes. However, limitations were noted regarding assumptions made during microstructure generation, which may impact the realism of the optimized microstructures.²¹⁰ Another study employed PNM to optimize the pore and throat size distributions of an artificially generated microstructure using a genetic algorithm.²¹¹ The optimized microstructures showed a bimodal pore size distribution, leading to improved flow pathways and enhanced electrochemical performance. However, challenges were identified regarding the realism and manufacturability of the optimized microstructures, as well as the consideration of pore coordinate relocation during the optimization process.²¹¹

Furthermore, a multi-scale model was employed to investigate the relationship between pore-scale electrode structure reactions and device-scale electrochemical reaction uniformity.²¹² The study combined a deep neural network with a partial differential equation solver and utilized 128 pore-scale simulations to train and validate the deep neural network. The findings revealed that optimizing the electrolyte inlet velocity over time led to a significant reduction in pump power consumption while maintaining surface reaction uniformity, while the impact on electric power output during discharging was minimal.²¹² It is important to note that the limited number of simulations conducted in this study may restrict the generalizability of the results. Additionally, the characterization of electrode microstructure plays a crucial role in understanding its behavior. In another investigation,²¹³ a custom Weka three-dimensional segmentation technique²¹⁴ was employed to study the permeability and mass transport processes in various



carbon electrodes. This segmentation approach provided improved control over the known fiber thickness, potentially leading to more accurate estimations of specific surface area and porosity. However, it is worth mentioning that the disadvantage of the workflow was the small sample size used for training the classifier and the use of scanning electron microscope (SEM) images as the ground truth for adjusting fiber thickness.²¹³

The laser reduction process of poly(acrylonitrile) (PAN) membranes has been investigated using Bayesian optimization.²¹⁵ A dataset of 204 samples, including laser scan speed, laser power, focal point height, and image density, was utilized for this study. The results demonstrated the successful synthesis of laser-reduced PAN membranes in a single lasing step, leading to materials with low sheet resistance ($6.5 \Omega \text{ sq}^{-1}$). The suitability of these materials as membrane electrodes for vanadium RFBs was confirmed through electrochemical testing.²¹⁵ However, challenges were encountered, such as the system-specific nature of the optimized parameter set and the limitation imposed by electrode thickness. In another study,²¹⁶ an ANN was employed to develop polybenzimidazole (PBI)

membranes with high ion selectivity, proton conductivity, and low cost through solvent treatment. The dataset comprised 49 samples, with solvent properties and experimental parameters used as inputs. The predicted performance of the PBI membranes in vanadium RFBs, in terms of voltage efficiency (VE) and energy efficiency (EE), achieved a mean absolute prediction error (MAPE) within 1% of the experimental data as highlighted between the comparisons in chemicals (hexane, ethanol, *etc.*) as shown in Fig. 9a. Nonetheless, the relatively small dataset and the limited exploration of solvents could impact the generalizability of the model.²¹⁶

3.3.6. Lithium-ion batteries. Lithium-ion batteries (LIBs) have become an integral part of modern life, powering numerous portable electronic devices, electric vehicles, and renewable energy storage systems. The increasing demand for longer-lasting batteries with higher performance and efficiency has propelled research and development efforts in this field. By gaining insights into the intricate details of the electrode microstructure the development of advanced materials, manufacturing techniques, and computational models becomes possible. ML algorithms are used to enhance the



Fig. 9 (a) Predictable membrane performance of the ML model and membrane structure,²¹⁶ reproduced with permission from the Royal Society of Chemistry, (b) U-Net neural network used to enhance the quality of extracted microstructures from X-ray tomography images,²¹⁷ reproduced with permission from Elsevier, (c) coupled physical models for battery electrode manufacturing processes (drying and calendaring) to a deterministic learning method and subsequent property optimization,²¹⁸ reproduced with permission from Elsevier, and (d) correlation analysis between control variables for the cathode and anode,²¹⁹ reproduced with permission from Elsevier.



image segmentation outcome, estimation of the electrode microstructure properties, optimization of the electrode manufacturing process, and 3D microstructure reconstruction using 2D images.

Microstructure characterization plays a vital role in optimizing manufacturing processes and predicting the long-term performance of LIBs. In a recent study, researchers focused on $\text{LiNi}_{0.33}\text{Co}_{0.33}\text{Mn}_{0.33}\text{O}_2$ as the active material and employed coarse-grained molecular dynamics simulations and X-ray micro-computed tomography to investigate changes in electrode heterogeneity and the deformation of secondary particles during manufacturing.²²⁰ To analyze the obtained tomographic data, ML techniques, including the Weka plugin²¹⁴ and fast random forest class, were trained on real particle shapes. However, further improvements and validations are necessary to enhance the accuracy and applicability of the model in real-world scenarios. In a similar study, to minimize variation in quantifying the volume fraction of the active material, researchers utilized the open-source software Ilastik²²¹ and employed an iterative, manual training approach.²²² This method achieved reduced variation compared to unsupervised techniques, but additional refinements and validations were required to enhance accuracy and applicability when quantifying the active material volume fraction in LIB cathode tomograms. Moreover, researchers employed a DL-based U-Net architecture and StarDist²²³ for active particle segmentation, enabling rapid and accurate characterization of the electrode microstructure.²²⁴ Geometric analysis of the segmented data provided valuable information on particle size distribution, porosity, tortuosity, and particle system connectivity. Additionally, a stochastic reconstruction methodology was presented to generate statistically equivalent virtual microstructure designs. It is important to note that the limitations of this approach include its reliance on previously published tomographic data and the challenge of accurately representing non-spherical particle morphology.

For microstructure extraction from 2D scanning electron microscopy (SEM) images, researchers used a modified U-Net architecture²²³ based on the CNN²¹⁷ with an input to segmented output process on the images shown in Fig. 9b. They examined the relationship between porosity and thickness at different states of charge, demonstrating the effectiveness of the image segmentation method in improving microstructure extraction quality. Another investigation focused on the rapid characterization of microstructural effective properties of LIB graphite anode electrodes using ML models.²²⁵ Different supervised learning models, including linear, decision-tree, and ensemble-based models, were employed and trained on input parameters such as composition, active material shape, mean pore size, and particle orientation and alignment. The results exhibited high prediction accuracy for estimating effective properties, but the limitations included the use of artificially constructed porous electrodes and the complexity of accurately estimating the properties of real electrodes.

To estimate the tortuosity of the cathode and anode in LIBs, researchers used a combination of a CNN and support vector regression (SVR).²²⁶ Three-dimensional porous structures were

employed as input, and the study revealed a correlation between tortuosity and the particle aspect ratio, expanding the understanding beyond porosity alone. However, the limitations included the use of simulated electrode structures that may not fully represent real microstructures and the neglect of carbon black and binder in the models. Researchers developed a CNN model to predict the microstructural properties of a graphite| LiMn_2O_4 electrode based on voltage–capacity curves.²²⁷ Training the model on a large dataset allowed successful prediction of Bruggeman's exponent and shape factor. This study highlighted the potential of deep learning approaches for rapidly inferring microstructural properties for battery design optimization and performance evaluation. Limitations included the challenges of capturing particle–particle effects at high current densities and predicting the performance of highly aligned platelets with morphological anisotropy.

Advancements in 3D microstructure reconstruction have also been explored. One study developed a method using ANNs and the scaled conjugate gradient (SCG) method to construct 3D microstructures from limited morphological information obtained from 2D cross-sectional images.²²⁸ The results demonstrated that the workflow preserved statistical characteristics, geometrical irregularities, long-distance connectivity, and anisotropy observed in the 2D images. However, further research is needed to address and validate the limitations and challenges related to accuracy and efficiency. Another study focused on the reconstruction and analysis of anode and cathode electrodes using a neural network-based approach.²²⁹ The study employed an autoencoder–decoder framework for microstructure reconstruction and feature extraction. While the findings showed promise in optimizing microstructure reconstruction, incorporating additional computational layers such as pooling, batch normalization, and regularization, the model's inability to produce realistic reconstructions indicated the need for more data to enhance its performance. Additionally, researchers utilized CNNs to build 3D models of nickel–manganese–cobalt cathodes.²³⁰ This approach aimed to overcome the challenges associated with accessing 3D images by utilizing readily available 2D images and capturing the granular-like morphology of the battery system. The findings demonstrated the ability of the proposed method to generate synthetic 3D models that exhibited good agreement with the original models. However, differences in pore size distribution, permeability, and thermal conductivity compared to the original models indicated a limitation of the approach.

Researchers have explored the optimization of manufacturing parameters in LIBs using ML techniques. A combination of ML methods with physics-based simulations was employed for multi-objective optimization and inverse design of LIB electrode properties and manufacturing parameters²¹⁸ as shown in the flow chart in Fig. 9c. The ML-assisted pipeline utilized a synthetic dataset generated from physics-based simulations to train ML models, to find a balance between minimizing the electrode tortuosity factor and maximizing effective electronic conductivity, active surface area, and density, all crucial factors influencing Li^+ (de-) intercalation



kinetics and transport properties. The study revealed the interconnected nature of these properties and their impact on optimal electrode performance. However, limitations include reliance on simulation data, limited dataset volume impacting generalizability, and exclusion of certain manufacturing steps in the simulation process. Nonetheless, the successful experimental fabrication of an electrode based on the model's predictions validated the physical relevance of the modeling pipeline.²¹⁸ In predicting electrolyte infiltration in LIB electrodes, a multi-layer perceptron (MLP) approach was used.²³¹ The model was trained on a database generated from a 3D-resolved physical model based on the LBM and X-ray micro-computer tomography. The MLP model accurately predicted the rate of saturation, filling time, and direction of electrolyte flow in porous electrodes. It enabled quick and accurate predictions, facilitating the screening of different conditions to optimize the infiltration process. However, limitations of the model included the exclusion of certain geometrical parameters influencing the fluid distribution and the reliance on simulated data that may not fully capture the complexity of real-world systems.²³¹

In another study, to optimize electrolyte infiltration conditions, random forest (RF), neural network, and SVM models were employed.²³² Exploratory data analysis (EDA) identified influential electrolyte parameters affecting saturation descriptors. Lower kinematic viscosity led to higher wetting degrees and rates, while higher inlet applied pressure reduced the electrolyte filling time. The study showcased the potential of ML as a surrogate model for optimizing multi-parameter processes in battery manufacturing. However, the computational cost associated with physics-based approaches such as the LBM poses a limitation.²³² Gradient-boosted trees and random forest models were used to identify key parameters in the manufacturing process of LIB electrodes.²¹⁹ Coating process factors such as the comma bar gap, coating speed, and the coating ratio were considered input parameters. The study demonstrated a data-driven approach to predicting electrode quality and identified key parameters and control variables affecting the manufacturing process as shown in Fig. 9d. A systematic design of experiments was proposed to generate representative data for ML activities, reducing waste and resource demand. However, the limited number of experiments and consideration of only a subset of parameters restricted the general applicability of the model.²¹⁹

A deep-learning-based prediction algorithm combines adaptive dropout long short-term memory-Monte Carlo (ADLSTM-MC), for early prediction of battery remaining useful life (RUL) in LiFePO₄/graphite and LiNi_{0.8}Co_{0.15}Al_{0.05}O₂/graphite batteries,²³³ with reduced degradation data. The method achieves precise early prediction with only 25% of the degradation data, outperforming existing models. The proposed method demonstrates high accuracy with an R^2 value of 0.957–0.982 for capacity prediction and low prediction errors (RMSE and MAE). However, the computational efficiency of the LSTM network needs improvement for real-time battery management systems. Moreover, the Bayesian optimization (BO) strategy was employed to optimize rapid charging

protocols in graphite/LiCoO₂ batteries.²³⁴ The goal was to reduce charging time while limiting battery degradation. The probability-of-improvement acquisition function showed the best performance. Limitations include computational cost, limited applicability of the electrochemical model used, simplified assumptions, and a lack of experimental validations. Another study employed particle swarm optimization (PSO) to optimize highly ordered laser-patterned electrode (HOLE) architectures for fast-charging LIBs.²³⁵ The study used experimentally obtained voltage vs. capacity data for galvanostatic charging at different C-rates as input. The optimal spacing between channels for improved fast-charging performance was identified, with the Damkohler number (Da) serving as a metric. The optimal configuration maintained a $Da \approx 1$ throughout charging. Limitations include the oversight of pore-scale changes due to continuum modeling and the small dataset used in the study.

3.3.7. Supercapacitors. Supercapacitors are electrochemical energy storage devices that have fast charging capabilities, high power density, and cycle lifetimes. They can either store their charge *via* the electrical double layer (by ion adsorption) or reversible redox reactions.²³⁶ This means that electrode structures or chemical composition could alter the performance, such as by the change in active surface area or the connectivity of the pore network.²³⁷

Ions must flow from the separator region towards or away from the electrodes which is influenced by diffusion and migration, where the electrode structure may facilitate or resist each transport mechanism as shown in Fig. 10a. To determine the optimal properties for supercapacitor electrodes (typically activated carbon-based materials as shown in the figure, where the performance metrics are often specific capacitance ($F\ g^{-1}$)),^{236–243} ML tools using experimental data can be used.

ML models are empirical, meaning that high-quality datasets are needed for the models generated to be predictive outside of the experimental region of interest. For example, in one case²⁴³ 400 raw datasets were condensed to 259 defect-free results. The inclusion of inaccurate experimental data could bias the prediction of the ML models.

In the literature on supercapacitors, it is stated that theoretical models are not reliable enough to predict the state of supercapacitors away from equilibrium so to optimize the electrode structure currently, ML techniques must be used.^{237,242} The ML methods that have been used for supercapacitor optimization have used ANNs, MLP, LR, XGBoost, RF, and DTs^{236–243} to name a few; however, of these the ANN and XGBoost are often the more accurate performance models. The evaluation metrics used to study the predictive capability of the models include R^2 , RMSE, and MAPE.

As shown in Fig. 10b, the ANN can be used to create material design operating maps which provide a design space to choose specific surface area for mesoscale and microscale pores^{237,242} allowing for next-generation material design.

Some of these studies have used ML to optimize the chemical composition or preparation structure for bio-mass-derived electrodes for supercapacitors, including jackfruit-derived.²⁴¹ Here, using a design of experiment (Box-Behnken design), 15



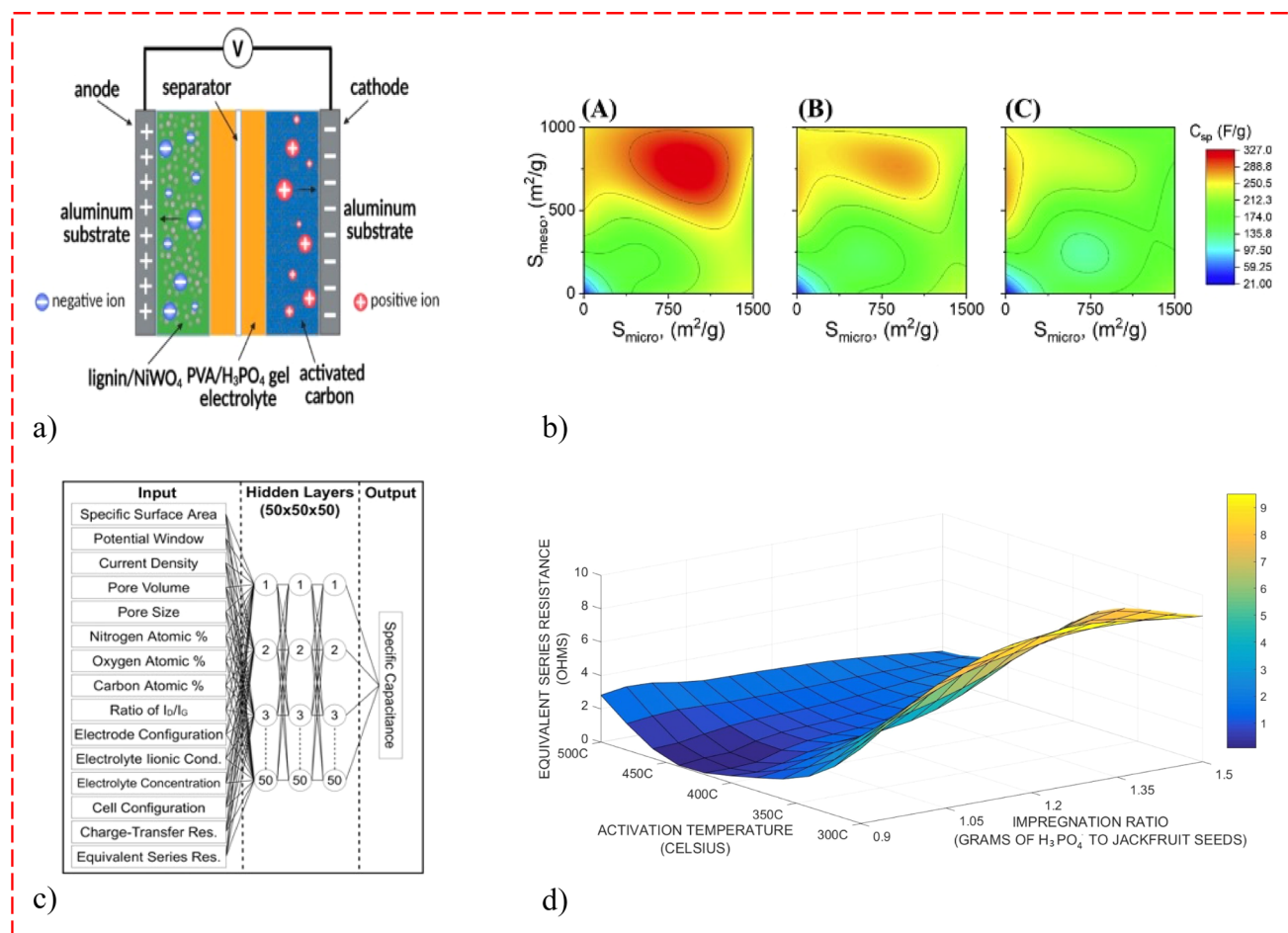


Fig. 10 (a) Schematic of an asymmetric supercapacitor showing different materials that can be used for the anode (lignin/NiWO₄) and cathode (activated carbon),²⁴² reproduced with permission from American Chemical Society, (b) specific capacitance design maps predicted by ANNs, allowing meso and micropore surface area to be optimized at different scan rates,²³⁷ reproduced with permission from Elsevier, (c) selection of input variables taken from 200 experimental publications allowing for prediction of specific capacitance of graphene doped electrodes,²³⁸ reproduced with permission from Elsevier, and (d) ANN used along with particle swarm optimization to predict and optimize specific capacitance (color bar) based on activation temperature and the impregnation ratio,²⁴¹ reproduced with permission from Elsevier.

experimental datasets were extracted and an ANN was trained on this limited dataset. The ANN model was able to predict and optimize the amount of phosphoric acid and activation temperature required, obtaining a maximum specific capacitance of 56.12 F g⁻¹. However, in this scenario, the microstructural properties were not used as inputs to the trained model.²⁴¹ As shown in Fig. 10d, this method was able to provide the response of specific capacity as a function of activation temperature, impregnation ratio, and series resistance, which could lead to improvements in specific capacitance of over 9 times. Similarly, lignin-based electrodes have been investigated *via* ML methods (LR, SVG, and ANN) using an 80/20 training/test split on cycle data, where performance data did not use microstructure data but could predict specific capacitance change over time.²⁴²

Other studies, where BET data for surface area have been acquired, have looked at using microstructural properties as inputs for ML models. This can include the surface area for the micro and macroporous structure^{237,239,240,243} or operating

parameters such as electrolyte conductivity, cell configuration, and charge transfer resistance²³⁸ as shown by the inputs to the neural network in Fig. 10c.

The impact of ML models on the development of next-generation electrode materials was highlighted by Rahimi *et al.*²⁴³ They used 259 defect-free datasets for experimental values in 6 M KOH and with three electrode configurations to train an ANN. The surrogate model was used for a genetic algorithm to optimize the input parameters which could predict the optimal properties of an AC supercapacitor electrode to reach 550 F g⁻¹.

ML approaches using empirical data as input may miss some critical features as the relationships between parameters may be highly non-linear. However, without this, there has been some success in optimizing input parameters or macroscopic parameters. However, there is still no approach that considers a mix of theoretical models, ML, perhaps as surrogate models to the theory (which contains no noise), leading to ML algorithms for optimization.



ML applied to electrochemical engineering has been shown to be able to predict the complex interaction between operating and material parameters that a physical-based model is currently unable to resolve. There are readily available data regarding the manufacturing methods that lead to certain electrode microstructures, and these could be leveraged by ML methods through surrogate modeling or optimization strategies to choose optimal manufacturing conditions. Generally, between fuel cells, electrolyzers, batteries, and supercapacitors, the role of the microstructure of electrodes, separators, and electrolytes plays a key role in performance and durability.

3.4. Hydrocarbon reservoirs

Central to the efficacy of oil and gas reservoirs is the intricate matrix of porous media, a labyrinthine network of interconnected spaces within rock formations that house hydrocarbons. These porous structures, comprising varying permeabilities and porosities, act as repositories for vital resources. ML algorithms play a pivotal role in unraveling the mysteries held within these porous domains. By harnessing ML models, the characterization and understanding of these porous media undergo a profound transformation.²⁴⁴

ML is a subset of artificial intelligence that enables computers to learn from data without being explicitly programmed. It involves developing algorithms to identify patterns in large datasets and make predictions based on those patterns. In oil and gas reservoirs, ML can analyze geological data, well logs, seismic surveys, production data, and other relevant information to enhance reservoir characterization, improve production efficiency, and reduce costs. One of the key benefits of ML in the oil and gas industry is its ability to handle large amounts of complex data. Traditional methods for analyzing geological data involve manual interpretation by geologists or engineers. However, this process can be time-consuming and prone to errors. ML methods can quickly analyze vast amounts of data from multiple sources to identify patterns that may not be apparent to human analysts. Another advantage of ML is its ability to make accurate predictions based on historical data.²⁴⁵

As technology continues to evolve, we will likely see more widespread adoption of ML in the exploration and production of oil and gas reservoirs. However, it is essential to note that ML is not a silver bullet solution and requires careful consideration of data quality, model accuracy, and ethical considerations. Nonetheless, the benefits of ML in the oil and gas industry are clear, and its application will undoubtedly continue to grow in the years to come.

This section focuses on the ML models in oil and gas porous media, as a complex and dynamic system, to foremost raise the understanding and thereafter provide an overview of ways that optimize the recovery of hydrocarbons from the reservoir. In reservoir characterization, ML models are used for analyzing data from reservoir cores, including porosity and permeability, for creating more accurate reservoir models. To this end, the location of wells can be optimized and improve the recovery of hydrocarbons from the reservoir. ML models in reservoir history matching are used for matching production data from oil or gas

reservoirs to numerical models, which allows for more accurate predictions of future production and its changes over time. In EOR, ML models may be employed for optimizing EOR methods including CO₂ injection and waterflooding, by analyzing data from the reservoirs. Towards rock physics modeling, ML models are used for introducing rock physics models, whereby the connection between rock's physical properties, such as porosity and permeability, and the fluids' properties in the rock, such as oil and water is described. Here, pore-scale fluid flow and transport are also appraised allowing for better predictions of oil and gas behavior in porous media. Furthermore, in the subfield of fracture characterization, ML models can be used to analyze data from seismic surveys and well logs to eventually identify and characterize fractures in the reservoir, which are critical to the fluids' flow. Finally, by analyzing data from log measurements, *i.e.*, resistivity, the porous media properties can be determined.

In this section, the application of ML techniques in hydrocarbon reservoirs is described in four subsections: pore-scale modeling, reservoir characterization, reservoir modeling, and reservoir management (Fig. 11).

3.4.1. Pore-scale modeling. Pore-scale simulation is a computational technique used to study the behavior of fluids in porous media at the microscopic level. Using numerical methods involves simulating fluid flow and transport through individual pores and throats of a porous material, such as a rock or soil. The process of pore-scale simulation typically begins with obtaining high-resolution X-ray images of the porous media. These images are then processed to create a three-dimensional digital representation of the pore space. The digital model is then used to simulate fluid flow and transport through the pore network using mathematical models that describe the physics of the fluid flow (Fig. 12). Pore-scale simulation can provide valuable insights into the behavior of fluids in complex geological formations, which can help improve our understanding of subsurface processes such as oil and gas production, groundwater management, and carbon sequestration.²⁵⁰

3.4.1.1. Image resolution enhancement. One of the primary applications of ML in pore-scale modeling is image resolution enhancement. Due to hardware constraints, pore images obtained from micro-CT scans or other imaging techniques are often limited by low resolution and size. There is a trade-off between image resolution and field-of-view (FOV), meaning that a wider FOV covers a larger area but reduces the pixel density (low resolution) and *vice versa*. ML algorithms can be trained for image resolution enhancement by using deep learning techniques while capturing a larger FOV, which improves realistic fluid flow simulation, and estimating rock-effective properties at desired scales.²⁵² Super-resolution (SR) reconstruction methods have shown outstanding performance in converting low-resolution (LR) images to high-resolution (HR) images by lowering the difference error between these two types of images. As mentioned earlier, deep learning approaches such as generative adversarial networks (GANs) and CNNs are utilized regularly with SR for tackling problems. Jackson *et al.*²⁵³ used an enhanced deep-super resolution (EDSR)





Fig. 11 The workflow of the hydrocarbon reservoir engineering section. The input data, such as seismic, well logs and micro-CT images, are used for reservoir characterization, Xie *et al.*,²⁴⁶ reproduced with permission from Elsevier, and petrophysical property prediction through pore-scale modeling, Ma,²⁴⁷ reproduced with permission from Elsevier, and then static and dynamic models are constructed for reservoir simulation, Fornel and Estublier,²⁴⁸ reproduced with permission from Elsevier. The final step is reservoir management, where production strategies, optimization, and EOR selection are conducted, Hutahaean *et al.*,²⁴⁹ reproduced with permission from Elsevier.

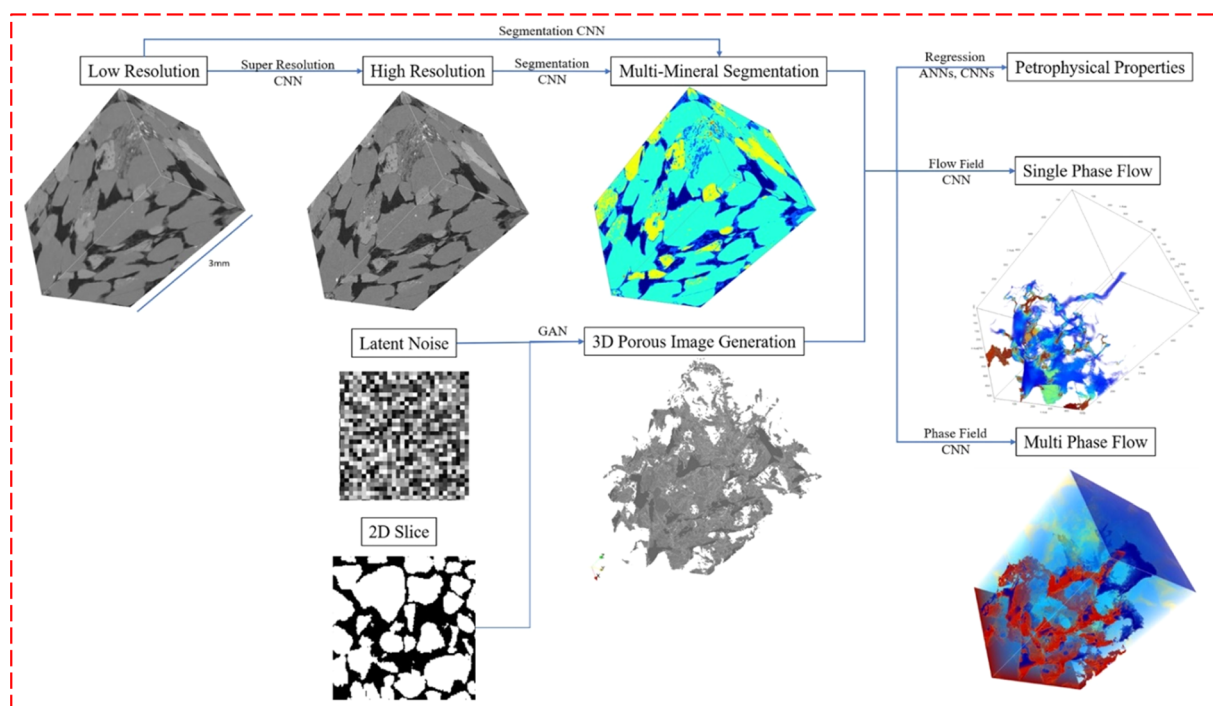


Fig. 12 A depiction of ML approach utilization in pore-scale imaging and modeling workflow. Gray-scale images obtained from scanners can undergo segmentation or super-resolution through CNNs, while GANs enable synthetic image reconstruction from latent or 2D/3D information. Petrophysical property prediction in pore-scale modeling can be enhanced using ANNs and CNNs to forecast parameters such as permeability and fluid phase distributions, Wang *et al.*,²⁵¹ reproduced with permission from Elsevier.



convolutional neural network to generate high-quality images from low-resolution (LR) images. This methodology reduces the common flaws in micro-CT imaging and generates realistic HR images for pore network modeling (PNM) and continuum modeling. In the image resolution enhancement field, two types of image data are used as input variables for the ML models, paired and unpaired images. In paired images, input and the ground-truth image domains are aligned, while the unpaired image refers to the data collected from various sample locations. Although paired images usually produce better results, they are challenging to acquire. The convolutional neural network (CNN) requires paired data as input, but methods based on generative adversarial networks (GANs) use unpaired images. Niu *et al.*²⁵⁴ probed the performance of these two approaches utilizing a micro-CT sample for creating HR images from LR images. They concluded that the unpaired GAN method performs the same as the paired CNN approach in creating HR images, but the unpaired GAN does not require image registration in the data processing stage. Compared to the paired CNN method, this feature reduces computational costs by up to 22.5%. In another study,²⁵⁵ the enhanced deep super-resolution generative adversarial network (EDSRGAN) showed remarkable visual similarity in texture regeneration over other approaches. Also, it reconstructs high-frequency texture, while the super-resolution convolutional neural network (SRCNN) retrieves large-scale edge features. Also, Liu and Mukerji²⁵⁶ utilized style-based GAN and cycle-consistent GAN to regenerate high-resolution images with a large FOV, which is the ultimate purpose of using ML for digital rock resolution enhancement. Their study used the style-based GAN to tackle the overfitting problem and cycle-consistent GAN for integrating the unpaired image data from various sources.

3.4.1.2. Pore geometry generation. Another important application of ML in pore-scale modeling is generating realistic pore geometries. Traditional methods for generating pore geometries involve manual segmentation or random generation based on statistical parameters. However, these methods may need to capture real-world porous media's complex geometry and heterogeneity accurately. ML methods can be conducted on large datasets of micro-CT scans to learn the statistical distribution of pores' shapes and sizes. This information can then be used to generate realistic 3D models that accurately represent the geometry and heterogeneity of porous media. Due to the high cost of 3D microscopy imaging, 3D microstructure reconstruction from 2D cross-sectional images using deep learning approaches is recommended as a cost-effective and accurate solution. Fu *et al.*²⁵⁷ used a supervised ML procedure for 3D pore reconstruction purposes. The proposed method showed superior results to conventional approaches, such as stochastic optimization-based reconstruction and Gaussian random field, regarding the accuracy and maintaining microstructural complexities within 2D images. Zheng and Zhang²⁵⁸ proposed a deep learning-based method called RockGPT to generate several types of rocks simultaneously using a single 2D image. Hybrid superposition approaches have shown promising performance in reconstruction problems, but they are complex, and both low and high-resolution images are required as the

input images. Hence, Yang *et al.*²⁵⁹ utilized a cGAN-based method to overcome the complexity of the proposed approach and prevent human factors that may cause severe problems. This method used low-resolution core images as the input for multi-scale digital rock reconstruction, while high-resolution images with a narrow FOV opted for the training stage. In another study, Zhang *et al.*²⁶⁰ introduced a framework named LGCNN based on the GAN and CNN for 3D porous media reconstruction. The LGCNN approach proved to be faster and more precise compared to traditional reconstruction methods with a higher construction speed (6003 voxels) and lower time (10 min).

3.4.1.3. Pore-scale simulation. ML has also been applied to simulate fluid flow and transport properties at the pore scale. Conventional numerical simulations involve solving partial differential equations (PDEs) that describe fluid flow through porous media. Direct numerical simulation (DNS) and pore network modeling (PNM) are the primary approaches for flow simulation at the pore-scale. DNS solves Navier–Stokes equations on the realistic 3D pore geometry reconstructed from high-resolution micro-CT images of rock samples. Using DNS leads to accurate but computationally expensive results. However, PNM uses a simplified ball-and-stick network obtained from real pore geometry to reduce the model complexity and computational costs of the DNS approach. However, the main drawback of PNM is that it may not accurately capture complex phenomena such as fluid–solid interactions and pore-scale heterogeneity as DNS. ML methods are also used in numerical simulations to learn the relationship between input parameters and output properties. This information can then be used to develop surrogate models that accurately predict fluid flow and transport properties such as temperature, pressure, and permeability at a fraction of the computational cost of traditional simulations. Ting *et al.*²⁶¹ applied a convolutional neural network (CNN) in a fluid flow simulation through the fracture problem. The priority of the researchers was avoiding simplified assumptions used in PNM, as it neglects the realistic geometry of the fractures and, consequently, the effect of capillary phenomena at the pore scale. However, the computational demands of DNS methods were also a significant challenge. Hence, they suggested using a data processing algorithm and CNN to tackle the disadvantages of the DNS method (LBM). The results illustrated that the accelerated LBM effectively simulated multiphase flow through 3D fractures in a shorter time. Ishola and Vilcáez²⁶² utilized a stochastic pore-scale simulation method for permeability estimation, and then they used the gradient boosting algorithm to reduce the number of simulations. The outcomes exhibited that using the gradient boosting algorithm reduced the number of simulations from 4400 to 28 while achieving the same results of rock core data with an MAE of 10%. Sun *et al.*²⁶³ proposed a deep learning-based approach for estimating permeability as a substitute for conventional pore-scale simulation and experimental methods, which are assumed to be time-consuming. They concluded that the proposed framework was 100 times faster than DNS. Tian *et al.*²⁶⁴ evaluated the performance of six different ML algorithms in a permeability prediction study. These algorithms



were optimized by using particle swarm optimization (PSO) to enhance the performance of the ML algorithms. The results showed that PSO's hyperparameter tuning of the ML algorithm improved their performance. Among all the ML algorithms, the ANN-PSO approach exceeded other algorithms regarding permeability prediction accuracy (R -value of 0.9985). Also, the application of feature selection in ML algorithms improved their performance and proved their supremacy over the empirical equations in permeability prediction. Bu *et al.*²⁶⁵ used five different linear regression algorithms for permeability prediction from CT images of core samples. The outcomes revealed that the Gaussian process regression (GPR) models achieved the highest R -squared values (minimum of 0.87), outperforming other methods in estimating permeability accurately. In addition, using ML-based methods overcomes the computational cost issues, which makes them an excellent alternative approach to conventional pore-scale simulation methods such as PNM.

3.4.2. Reservoir characterization. Reservoir characterization involves the analysis of geological, geophysical, and petrophysical data to determine the properties of subsurface reservoirs critical for estimating the total hydrocarbons present in a reservoir. Traditionally, reservoir characterization relied on manually interpreting logs, seismic data, and core samples. However, human biases made these approaches time-consuming and prone to errors. ML algorithms can be applied to seismic and logging data to improve image quality, remove noise, and extract more information from the data. They can also be trained on CT scan data to predict petrophysical properties such as mineralogical brittleness,^{266,267} total organic carbon (TOC),^{268,269} microorganism growth,²⁷⁰ shear wave velocity,²⁷¹ and minimum miscible pressure (MMP).^{272–275} However, ML models have been applied to predict permeability and porosity as the essential properties affecting fluid flow in reservoir engineering (Fig. 13).

In several types of research, well-logging data are used as input since data obtained from core samples highly rely on core experiments and have limitations in uncored areas.²⁷⁷ Yang *et al.*²⁷⁸ used a deep learning approach based on the combination of a 1-D convolutional neural network (CNN) and bidirectional LSTM network to predict reservoir parameters such as permeability and porosity from logging data. In their study, optimization algorithms and self-attention mechanisms were conducted to find the optimum network architecture and weights for accuracy enhancement. The results showed that the proposed framework accurately predicts despite using input data from various reservoir regions. Masroor *et al.*²⁷⁹ established the supremacy of a novel multiple-input deep residual convolutional neural network (MIRes CNN) with single-input deep residual CNN methods and baseline methods such as random forest (RF) in the permeability estimation task. Two types of data, numerical well-logs (NWLs) and graphical feature images (GFIs) were fed to the network. It was concluded that the MIRes CNN's ability to handle mixed data as input features reduced the overfitting issue and computational costs compared to conventional methods. The computational costs and convergence problems related to ANNs have been addressed in some

studies. Matinkia *et al.*²⁸⁰ suggested that MLP neural network-heuristic hybrid approaches optimize the network architecture for predicting rock permeability. They compared the effectiveness of the social ski-driver (SSD) algorithm-MLP combination with two commonly used hybrid methods, such as particle swarm optimization (PSO)-MLP and genetic algorithm (GA)-MLP. It was illustrated that SSD-MLP had the highest accuracy with a correlation coefficient (R) of 0.9928, while GA-MLP converged faster than the other two approaches. Chao *et al.*²⁸¹ proposed a new ML model that can predict the stress-dependent gas permeability of shales with different moisture contents. The model combines the mind evolutionary algorithm (MEA) and adaptive boosting algorithm-back propagation ANN (ADA-BPANN) and has higher prediction accuracy and shorter training time than traditional ML algorithms. In another study, Pan *et al.*²⁸² used a grid search approach and genetic algorithm for hyperparameter tuning and optimizing the XGBoost algorithm in a porosity prediction problem. The proposed method illustrated excellent generalization performance and adaptability, and compared to the five other approaches, it showed the most accurate porosity estimation. Wang and Cao²⁸³ combined the 1-D CNN and bidirectional gated recurrent unit (BiGRU) neural network to take advantage of both models and overcome their drawbacks for porosity prediction from well-logging data. The CNN network was used for learning hierarchical local features, and the BiGRU neural network was used to learn global features. The porosity prediction results proved that the novel integrated neural network outperformed other models, such as LSTM and RNN. Despite the efficiency of the ML models in reservoir property prediction, the "black box" nature of these models hinders their enhancement in some points. Water saturation, a crucial property in reservoir characterization, can be determined using various correlations. However, there are several obstacles, such as the faultiness of presumptions and high computational demand, to using these equations. Ibrahim *et al.*²⁸⁴ fed various types of well-logs to ML approaches, such as random forest (RF), function network (FN), and SVM, for the training and testing of a model that forecasts water saturation. Compared to empirical correlations, the introduced models showed excellent performance in water saturation determination, with an average absolute percentage error (AAPE) of less than 8%.

Some other researchers fed data from rock samples and micro-CT images to ML models for training and testing. Zhao *et al.*²⁸⁵ introduced a digital quantum mechanism-based neural network (DQNN) to estimate rock permeability and pore-scale variables are opted as input variables. The results showed that pore length, size, and throat size are more important variables than the coordinate number and porosity for predicting permeability. Also, the evaluation results of the DQNN were compared with those of the classical ANN and experimental permeability in terms of computational costs and accuracy. dos Anjos *et al.*²⁸⁶ utilized a CNN and CNN with spatial pyramid pooling (CNN-SPP), two convolutional neural network models, to predict petrophysical properties such as permeability from micro-CT images. Also, an easy-to-implement model, named the ImageNet pre-trained model, was tested and compared with



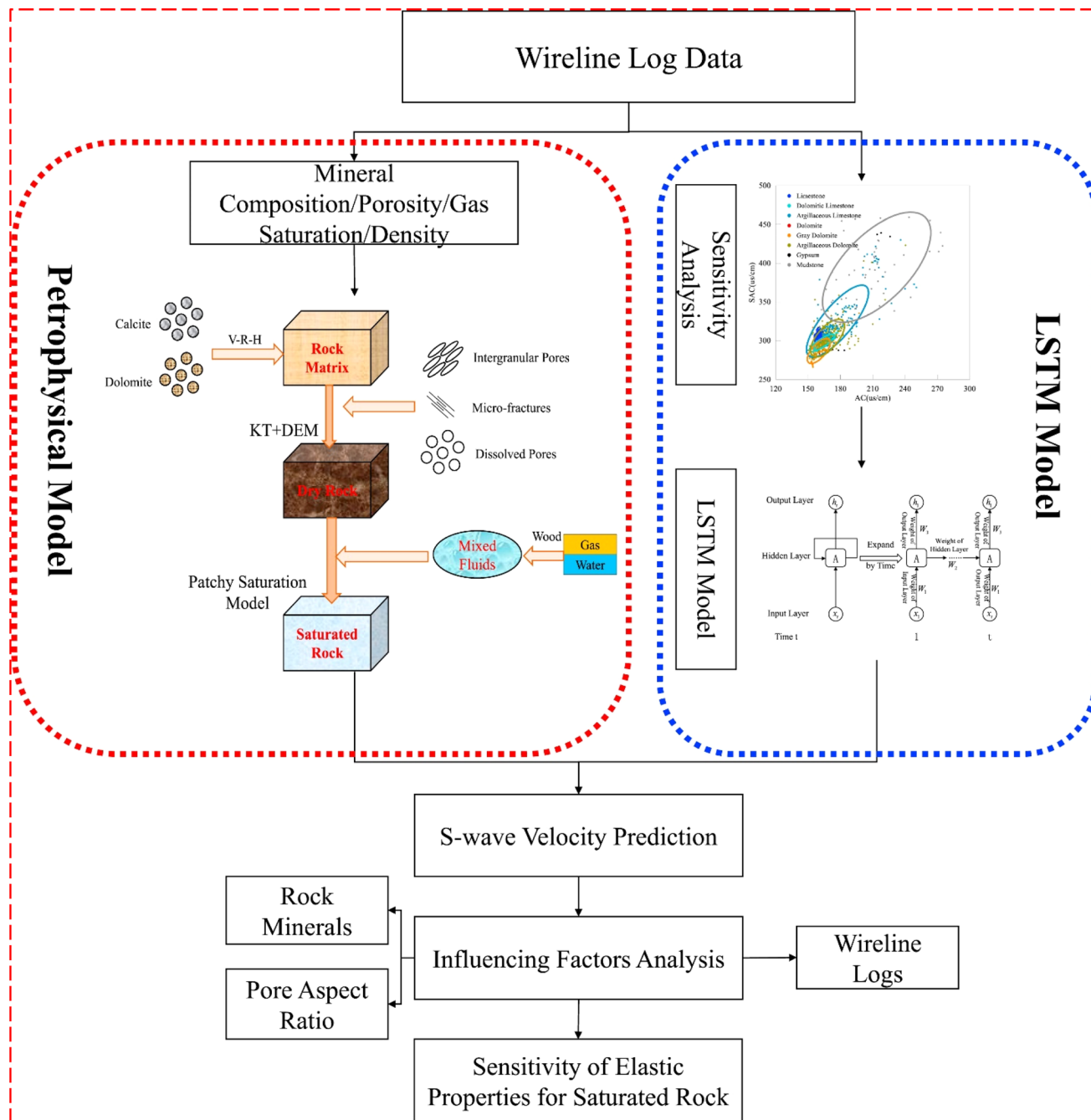


Fig. 13 Workflow for S-wave velocity prediction, utilizing a petrophysical model and employing a long short-term memory (LSTM) model based on wireline logs, Zhang *et al.*,²⁷⁶ reproduced with permission from Elsevier. The LSTM model begins by analyzing relationships between conventional wireline logs and measured S-wave velocity, selecting sensitive logs for prediction. Subsequently, an optimal LSTM model is established to predict the S-wave velocity. Then, the two models are compared based on factors such as rock mineral content and wireline log combinations, with the most accurate method selected for elastic modulus calculation.

the CNN models. It was shown that the pre-trained model could achieve the most accurate prediction, although CNN models reached satisfactory results. In addition, by using the prediction tools, absolute permeability was obtained 100 times faster than the Swanson method. Yet, the authors declared that the major problem for model training was not only the quality of the input data but also the quantity and amount of data. Alqahtani *et al.*²⁸⁷ conducted CNN models to estimate reservoir properties, such as

specific surface area, porosity, and average pore size. These are the most crucial in permeability calculation using 2D slices generated from rock sample images. The model training and testing images are categorized as binary and grayscale images. The outcomes indicate that model training based on binary images leads to the minimum value of average relative error and maximum accuracy.



3.4.3. Reservoir modeling. ML has revolutionized the oil and gas industry by providing a powerful tool for reservoir modeling. Reservoir modeling creates a mathematical representation of an oil or gas reservoir to predict its behavior over time. This process is crucial for optimizing production and maximizing recovery. ML algorithms have been applied to various aspects of reservoir modeling, including upscaling, history matching, and reservoir simulation²⁴⁵ (Fig. 14).

3.4.3.1. Upscaling. Upscaling refers to converting fine-scale properties, such as permeability and porosity, into coarser-scale data that can be used for reservoir simulation. The main goal of upscaling is to conserve the crucial properties and effects of heterogeneity at a lower computational cost and shorter time, which is necessary because simulating a reservoir at high resolution requires significant computational resources. Traditionally, flow-based methods are used to simulate fine-scale grids corresponding to the coarse cell and extract the property value that imitates the same flow value. However, this method highly relies on boundary conditions, and it is also considered to be time-consuming. ML algorithms can identify which parts of the model are most important for accurate predictions and simplify those areas while maintaining accuracy in other areas. Pal *et al.*²⁸⁹ presented an ML approach called the neural upscaling method that is more accurate than traditional analytical and numerical upscaling methods. They proved the superiority of the mentioned method over analytical and numerical upscaling methods. Also, they discussed the limitation of the neural upscaling method, which is the need for a substantial amount of training data. To overcome this limitation, the authors generated pseudo-training data using classical upscaling approaches. Wang *et al.*²⁹⁰ used an ML-assisted

upscaling (MLAU) approach to reduce the computational cost of two-phase upscaling for large-scale reservoir models. The procedure involves using a CNN-based clustering model to select representative coarse blocks and a regression algorithm to predict two-phase upscaled functions for the rest of the blocks. They showed that the MLAU method can reach the same coarse-scale outcomes as accurately as the full flow-based upscaling while achieving significant speedups compared to flow-based upscaling and fine-scale simulations. In another study by Wang *et al.*,²⁹¹ an ML-assisted relative permeability upscaling method was utilized to quickly compute upscaled relative permeability functions for coarse blocks using ML algorithms. The method was tested for generic flow problems using 2D models and showed similar accuracy to full numerical upscaling while achieving significant speedups. The outcomes suggest that the mentioned approach can be a promising alternative to traditional upscaling methods for subsurface uncertainty quantification or optimization. Santos *et al.*²⁹² proposed an artificial intelligence approach for upscaling geological properties in reservoir simulation models. The method uses ML to apprehend patterns from a portion of datasets and extrapolate them to all other scenarios, resulting in faster and more accurate upscaling. They concluded that the introduced method outperformed other conventional approaches since it reached the same results as the fine model with less computational effort. Siavashi *et al.*²⁹³ presented an upscaling method using CNNs and downsampling techniques to predict low-resolution model properties. The results showed a significant reduction in computational cost and time while maintaining a close match between the dynamic behavior of the upscaled model through CNNs and high-resolution properties.



Fig. 14 AI-assisted history matching workflow for reservoir property tuning. First a high-resolution model with suitable grid cells, zones, and layers is constructed from seismic data. Then the facies model was built using the SGS technique to select the most suitable fluvial channel distribution. After that, an ANN is employed to optimize the selection of seismic attributes for porosity and permeability prediction. Through multiple trials and testing iterations, ANNs rank the attributes based on their correlation with well-log values. Finally, the efficiency of the integrated ANN technique and object-based modeling is evaluated through history matching, Thanh and Sugai,²⁸⁸ reproduced with permission from Elsevier.



The proposed method can be used for predicting multiphase flow characteristics in low-resolution large-scale models.

3.4.3.2. History matching. History matching is a crucial step in reservoir modeling that involves adjusting the uncertain parameters of a model to match observed data. It is a challenging and time-consuming task that requires expertise and experience. History matching can be performed using the computer assistant, known as automatic history matching (AHM). ML algorithms can automate this process by identifying which parameters need to be adjusted to match historical data and reducing the problem's computational costs. Alolayan *et al.*²⁹⁴ introduced a new approach for solving the history matching problem in reservoir simulation using reinforcement learning. They introduced a Markov decision process formulation of the problem, which allows an artificial deep neural network agent to collaborate with the simulator and speed up the process considerably. Jo *et al.*²⁹⁵ used a deep-learning-based history-matching method in fluvial channel reservoirs without conventional calibration processes. The method outperforms non-convolution-based methods regarding geological constraints and computational resources. The convolutional denoising autoencoder (CDAE) as a post-processor of the proposed method enhances the uncertainty assessment of posterior production behaviors. Ma *et al.*²⁹⁶ exploited a hybrid recurrent convolutional network (HRCN) model for surrogate modeling conducted in automatic history matching (AHM). The proposed model significantly reduces the computational cost of AHM. They illustrated that the introduced surrogate model can obtain reliable predictions, and the surrogate-based AHM workflow can considerably reduce the computational cost. Ma *et al.*²⁹⁷ utilized a history-matching method using a recurrent neural network (RNN) surrogate model to estimate the parameters of spatially varying geological properties in large-scale reservoirs. The proposed multilayer RNN surrogate model with the gated recurrent unit (GRU) is used to estimate mapping from the feature vector of geological realizations to the production data. Numerical experiments on a 2D reservoir model and the Brugge benchmark model demonstrate the performance of the proposed surrogate model and history matching method. Xiao *et al.*²⁹⁸ proposed an efficient surrogate-assisted deterministic inversion framework for large-scale history matching problems in reservoir modeling. The framework uses a deep neural network surrogate to approximate the gradient and stochastic gradient optimizers for quick convergence. The proposed method is compared and evaluated with a previously submitted projection-based subdomain called the proper orthogonal decomposition and trajectory piecewise linearization (POD-TPWL) approach regarding computational costs and accuracy. Both models have illustrated outstanding capacity in carrying out history-matching problems.

3.4.3.3. Reservoir simulation. Dynamic modeling involves simulating the flow of fluids through the reservoir over time, which requires considering factors such as pressure change, fluid movement, and production rates. ML algorithms can optimize these simulations by predicting how different variables will affect the behavior of the reservoir. For example, neural networks can be trained on historical production rates

based on changes in pressure or fluid properties. Qubian *et al.*²⁹⁹ discussed using a hybrid reservoir simulation model that combines artificial intelligence and numerical models. The study uses a neural network called LSTM to learn order dependence in sequence prediction problems. The study results suggest that the hybrid model can be a valuable tool in reservoir simulation. Behl and Tyagi³⁰⁰ explored using data-driven reduced-order models (ROMs) as an alternative to detailed physics-based simulations for reservoir simulation. The study found that the case with stateless LSTM achieved the most accurate forecasting. Also, by applying a walk-forward validation strategy, the proposed framework decreased estimation error by 95% on average with less computational costs compared to the conventional simulation. The physical realism was also enhanced by adding a capacitance resistance model (CRM) constraint, demonstrating the ROM's ability to detect spatial irregularities. Huang *et al.*³⁰¹ proposed an improved E2C model for faster predictions of subsurface flow in complex reservoirs with many wells. The proposed model significantly enhances the deep-learning network structure, well quantity calculation, and loss function specification, resulting in highly accurate predictions with substantial speedups. The results proved the accuracy of the improved E2C model, with a median average error of 3.1% for production, 1.0% for saturation, and 5.9% for pressure. Saberali *et al.*³⁰² introduced a new method for constructing a grid-based surrogate reservoir model (SRM) using a hybrid data source based on finite differences and streamline data. The outcomes showed that the mentioned hybrid database allows the SRM to be utilized by fast-supply inputs from streamline data and generate results as accurate as the finite difference-based simulation. The fidelity of the introduced approach was also approved by testing it on the 10th SPE model. Shuaibi *et al.*³⁰³ discussed testing a new tool on a brownfield with over 30 years of production history. The tool can potentially improve brownfield development and optimization for future developments. The paper concluded that the AI simulator, which utilizes an AI-physics hybrid reservoir simulator, could generate a reasonable production forecast for the tested brownfield. The AI simulation results were compared to the actual field data, and it was found that the predictions from the AI simulator compared better than the reference case conventional simulator forecast. Manasipov *et al.*³⁰⁴ presented different approaches that follow the concepts of physics-informed models. They found that incorporating physics into ML models can increase their accuracy and predictive power. However, in cases where physics-based models perform poorly, history matching or tuning of the model should be performed in a globally constrained optimization formulation. The study also found that generalized additive models (GAMs) can produce comparable results to popular ML methods such as neural networks and gradient boosting. GAMs offer flexibility in considering inter-well connectivity, inter-well distances, production and injection rates, and average reservoir properties.

3.4.4. Reservoir management. ML has transformed the oil and gas industry by providing advanced tools for reservoir management. Applying ML in oil and gas reservoir



management has enabled companies to optimize production, design well placement, screen for IOR/EOR, and increase recovery rates while reducing costs, ultimately increasing profitability. As technology continues to advance, the application of ML in reservoir management will continue to evolve, providing even more advanced tools for the industry.

3.4.4.1. Production forecasting. Production forecasting is critical to reservoir management as it helps companies plan their operations, estimate reserves, and optimize production. ML algorithms can examine substantial amounts of data from various sources, such as well-logs, seismic data, production history, and geological models, to generate accurate production forecasts. ML models can also optimize production by identifying the best operating conditions for wells. These models can analyze real-time data from sensors installed in wells to predict the optimal flow rate, pressure, and temperature for maximum output. Kong *et al.*³⁰⁵ used a hybrid prediction model for oil production based on two-stage decomposition, sample entropy reconstruction, and LSTM forecasts. The model performed more accurately than traditional approaches and proved to be a useful tool for reservoir evaluation and oilfield management. Chu *et al.*³⁰⁶ utilized a data-driven proxy model using deep learning to assess the production performance of horizontal wells with complex fracture networks in shale gas reservoirs. The model considers production time, variable bottom hole pressure, and fracture network properties as input variables to forecast production for the future period. Ibrahim *et al.*³⁰⁷ introduced a new approach to estimating the estimated ultimate recovery (EUR) for oil production wells in the Niobrara shale formation using ML techniques. The study shows that ML tools can accurately predict EUR from completion design parameters and initial well production rates. Although conventional empirical decline curve analysis (DCA) models need multiple months of production to estimate the EUR, the developed models demand only an initial flow rate and the completion design for EUR prediction with high certainty. Osah and Howell³⁰⁸ investigated the use of supervised ML methods to forecast the performance of oil fields on the United Kingdom continental shelf. The study tests five different algorithms and finds that support vector regression is the most effective method for predicting recovery factor and the maximum field rate. Al-Ali and Horne³⁰⁹ discussed using a transformer-based deep learning model called the temporal fusion transformer (TFT) to predict the oil production rates of wells in the Norwegian Volve field. It was concluded that the TFT model is a promising approach for accurate oil rate prediction. The model was more precise than traditional block recurrent neural network architectures (BlockRNNs) in predicting complex trends in oil rates. The ability of the TFT model to provide a range of forecasting uncertainty using quantile regression is vital for making critical decisions in well intervention and field development. Liu *et al.*³¹⁰ presented a new approach for evaluating the complex characteristics and production optimization of shale oil reservoirs using an ANN. The introduced quantitative evaluation approach is based on source-reservoir assemblage types, source rock quality, reservoir quality, migration dynamics, and conduit conditions. The study concludes that

increased liquid hydrocarbon, mud gas, total organic carbon (TOC), and normal fault percentage positively affects shale oil production. In contrast, the increase in reverse fault percentage negatively affects shale oil production. Ullah *et al.*³¹¹ proposed using ML models to predict bio-oil yield from microalgae pyrolysis. The best-performing model was GPR-GA with a high *R*-squared value and low RMSE, and an interface was developed for predicting bio-oil yield. Du *et al.*³¹² proposed an ensemble framework for coalbed methane (CBM) production forecasting using supervised and unsupervised learning. An LOF-Xgboost governance system autonomously detects outliers and supplies missing values. At the same time, the improved Bi-LSTM method establishes a forecasting model of CBM production for both long-term and short-term prediction. The experimental analysis shows that the proposed framework improves the short-term prediction performance and considerably increases the long-term estimation capability.

3.4.4.2. Operational parameters and well placement optimization. Optimal well placement and operating conditions are other critical aspects of reservoir management that determine the success of oil and gas operations. ML algorithms can analyze geological data to identify the best locations for drilling new wells and optimum operating parameters, such as pressure, rate, and temperature. These algorithms can also predict the impact of drilling on existing wells by analyzing data from nearby wells. Tang and Durlofsky³¹³ presented an optimization framework for well placement in 3D models using low-fidelity (LF) models and ML error correction. LF models are constructed using a global transmissibility upscaling procedure and tree-based ML methods to predict the error in the net present value (NPV) associated with the LF models. In the off-line stage, preliminary optimizations are conducted using LF models, and a clustering approach is used to opt for a representative set of well configurations for training. In the online stage, optimization with LF models, with the ML correction, is performed using differential evolution. The results show that the proposed method provides a significant speedup factor compared to optimization using high-fidelity (HF) models, with the best-case NPV within 1% of the HF result. Using ML algorithms, Bertini *et al.*³¹⁴ explored a methodology to efficiently estimate the NPV of oil production strategies. The proposed methodology considers binary data representation, indicating the presence or absence of a given well in a production strategy, reducing data dimensions and model complexity. The simulations conducted in a benchmark case, based on a real field, showed that some regression algorithms could be used as a surrogate model to the simulator to perform well placement optimization considering binary data efficiently. The best results were obtained with MLP, whose estimations covered a wide range of NPV with a small and constant error. Zhou *et al.*³¹⁵ utilized an efficient multi-objective optimization framework for well placement and hydraulic fracture parameter optimization. The framework uses a novel hierarchical surrogate-assisted evolutionary algorithm and multi-fidelity modeling technology. The NPV and cumulative gas production (CGP) are the bi-objective functions to be optimized. The proposed approach is validated on a naturally fractured shale



gas reservoir and is found to be accurate and efficient. The ML model used in the approach only needs to run 100 or 500 reservoir numerical simulations, making it highly efficient. Nasir and Durllofsky³¹⁶ proposed a closed-loop reservoir management framework that uses deep reinforcement learning to train control policies for optimal well settings. The framework incorporates operational and economic constraints, including relative-change requirements and project life optimization. The purpose is to maximize the NPV while ensuring the practical applicability of the control policy results. The framework is applied to waterflooding cases involving 2D and 3D geological models. The results show that the control-policy approach provides comparable or superior solutions to deterministic and robust optimization approaches. The optimal well settings provided by the control policy display gradual ramping, consistent with operational requirements. Chen *et al.*³¹⁷ presented a new method called InterOpt for optimizing operational parameters in petroleum exploration and development. This method uses interpretable ML to assess the impact and importance of various parameters. The experiment showed that by modifying operational parameters, InterOpt presented various optimization scenarios and attained an average cost reduction of 9.7%. The transferability and scalability of InterOpt to different optimization objectives are also verified based on the optimization of test production. Yao *et al.*³¹⁸ discussed using surfactants to enhance oil recovery by altering the wettability of carbonate rock surfaces. ML models are used to predict and optimize surfactant performance. The Shapley additive explanations approach is used to interpret the results and provide insights into the effects of different parameters on surfactant performance. Fabbri *et al.*³¹⁹ discussed a screening code that helps reservoir engineers identify potential locations for new oil wells. The code uses data from existing wells, production and pressure data, and geological information to create polygons representing areas with high potential for oil production. The code was tested by comparing the results to a base case with no new wells and a case with a combination of hand-picked and code-identified locations for new wells. The results showed that the code-identified locations provided additional value compared to the hand-picked locations alone. Overall, the paper suggests that the screening code can be a useful tool for optimizing oil well placement.

3.4.4.3. Screening for IOR/EOR technique selection. Improved oil recovery (IOR) and enhanced oil recovery (EOR) are techniques used to increase recovery rates from hydrocarbon reservoirs. ML algorithms can screen potential IOR/EOR techniques by analyzing geological data to identify suitable candidates for these techniques. ML models can also predict the effectiveness of IOR/EOR techniques by analyzing historical data from similar projects. Screening potential IOR/EOR techniques increases recovery rates while costs associated with unsuccessful projects are reduced. Pirizadeh *et al.*³²⁰ proposed a novel method for ranking EOR processes based on predicting the EOR-PR values. EOR-PR is a new production rate that represents the performance of EOR processes on particular reservoir characteristics. The proposed approach uses multi-gene genetic programming (MGGP), a practical ML approach,

to predict EOR-PR values and rank EOR methods based on their efficiency under specific reservoir conditions. The results show that MGGP has a significant performance in predicting EOR-PR values, and it can be used for EOR decision-making strategies. Pavan *et al.*³²¹ proposed a PIML approach to forecasting the performance of the *in situ* microbial-enhanced oil recovery process and screening suitable microbe-nutrient combinations based on inadequate experimental data. The method evaluates the impact of microbial kinetic, operational, and reservoir parameters as input variables on oil recovery and assesses their weightage factors to screen a suitable microbe-nutrient-reservoir combination. Mahdaviara *et al.*³²² aimed to study potential EOR scenarios for low permeability reservoirs. The databank included essential parameters such as permeability, porosity, API, viscosity, lithology, depth, and temperature for each reservoir. They developed EOR screening tools based on statistical and intelligent procedures such as RF, GBM, XGBoost, and gene expression programming (GEP). The introduced EOR screening tools were valuable for this study's scope, with RF outperforming the alternatives.

3.5. Carbon capture and sequestration

3.5.1. Adsorption and absorption. Global CO₂ emissions from the burning of fossil fuels have increased during the 1970s by more than double and currently surpass 32 Gt of CO₂ per year, driven by economic and population development. The conclusion is that human activities are thought to have led to an estimated 0.8–1.2 °C increase in the world's temperature, and the Intergovernmental Panel (IPCC) predicts that present trends will end up resulting in 1.5 °C of warming from 2030 to 2052.³²³ The ocean level increase, catastrophic storms, the disappearance of species, and concerns for human health, stability, food, and water supplies are just a few of the elevated hazards that warming at these rates has been linked to both the world's people and ecosystems.³²⁴ By creating innovative technologies for the effective management of carbon emissions, the materials sector could play a significant role in these initiatives. Recent years have seen an increase in worry over climate change, which is brought on by the release of greenhouse gases, particularly CO₂.^{325,326} Technologies that capture carbon could be thought of as an effective CO₂ emission reduction technique. Generally, CO₂ removal from point sources (such as industrial exhaust gases – power plants) or the environment using direct air capture is referred to as carbon capture.^{327–329} When CO₂ is captured, it can either be kept indefinitely (for example, underground) or utilized to create high-value goods such as fuels or specialty chemicals.^{330,331} To meet the objectives of emission reduction, carbon capture techniques are currently being developed.

Several porous organic, inorganic, and chemical-organic composites have been suggested for adsorptive CO₂ collection.^{332–335} In addition to activated carbons (ACs), MOFs, and zeolites, porous organic polymers (POPs) have also been used as porous materials for CO₂ capture, as depicted in Fig. 15a–e. The selectivity of an adsorbent for CO₂ in the presence of other gases, the adsorbent's CO₂ swing capacity during adsorption–desorption cycling, the kinetics of adsorption and desorption, the energy



needed to cycle or regenerate the adsorbent, the adsorbent's resistance to mechanical and chemical stresses during recycling, and the adsorbent's economic and environmental potential are important metrics for evaluating its utility. In Fig. 15e, radar plots for important sorbent criteria for choosing are shown. The key performance indicators for selecting materials in carbon capture applications have been qualitatively evaluated.

The development of adsorbents for carbon capture has seen significant advancements in the materials community. Nevertheless, more resources are required to meet requirements along the way to industrialization. In general, lifespan issues require more focus, and as materials move along in their development, more thorough evaluations must be undertaken.^{340–342} In particular, suggested synthetic methods must be scalable and safe, with few steps and good space-time yields, and starting materials must be feasible at the goal scale (especially for MOFs, given restricted extraction rates and deposits of specific metals).³⁴³ It is also important to consider how easily biomass can be recycled, utilizing both experimental and computational waste streams.^{344–347} ML, which makes it possible to provide algorithms for developing new materials,³⁴⁸ has attracted a great deal of interest recently for its ability to accurately predict chemical and physical properties, establish structure–property relationships,^{349,350} synthesize AC adsorbents *via* various types of biomass,³⁵¹ and navigate the chemical space to direct chemical synthesis.^{352,353} Designing and implementing process strategies that successfully extract CO₂ from

a gas composition with a minimal energy cost is the main objective of ML for carbon capture deployment.

At both the molecular and process levels, ML techniques have been effectively used in absorption and adsorption-based processes to address the issues that these techniques are now experiencing.³⁵⁶ A schematic of the ML implementation at different resolutions for a carbon capture technology based on multiple sources is shown in Fig. 16a. Fig. 16a illustrates the application of ML for carbon capture techniques in several stages, from adsorbent syntheses through adsorption steps, using experimental and computational data. External (published papers/databases) or internal sources (experimental/computational data) are used as feeds for ML algorithms. One of the applications of gas (air) separation in the power plant industry is oxyfuel, one of several solutions that reduce the percentage of CO₂ released from the combustion chamber output. Additional carbon cannot be produced if the air is separated, and additional oxygen is injected into the combustion chamber. One technique used in this industry to select the right adsorbent for gas separation technology is the prediction of the adsorption process using ML algorithms. To forecast gas absorption using porous carbon adsorbents, Fig. 16b depicts the architecture of the gray wolf multilayer perceptron optimizer meta-heuristic algorithm.

3.5.2. Adsorption technology and adsorbents. Alternative carbon capture systems based on adsorption are promising. Large interior surface areas in porous material structures allow



Fig. 15 (a) Activated carbons (ACs), Palmer *et al.*,³⁵² reproduced with permission from Elsevier, (b) IRMOF-5, Cai *et al.*,³⁵⁶ reproduced with permission from American Chemical Society, (c) Zeolites Rho, Lozinska *et al.*,³⁵⁷ reproduced with permission from American Chemical Society, (d) porous organic polymers (POPs), Bandyopadhyay *et al.*,³⁵⁸ reproduced with permission from American Chemical Society, and (e) radar plot for evaluation of adsorbent selection in CO₂ adsorption applications using various material class features. The radar plot is depicted in terms of different scores for adsorption of gases through porous adsorbents, Mashhadimoslem *et al.*,³⁵⁹ reproduced with permission from Elsevier.



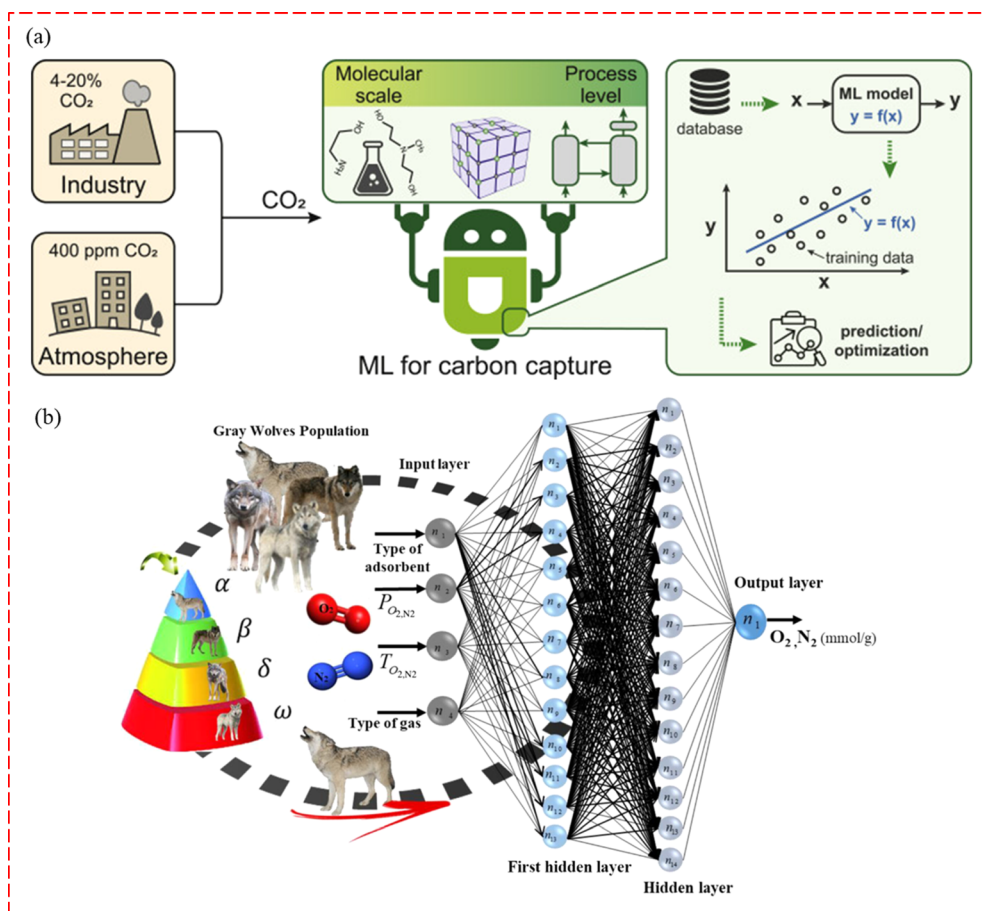


Fig. 16 (a) Schema of ML deployment for carbon capture systems, Rahimi *et al.*,³⁵⁴ reproduced with permission from Cell Press, (b) schema structure of the gray wolf-multilayer perceptron optimizer (GWO-MLP) meta-heuristic ML algorithm for predicting gas absorption using porous carbon adsorbents, Mashhadimoslem *et al.*,³⁵⁵ reproduced with permission from The Canadian Journal of Chemical Engineering.

for the efficient collection and storage of gas molecules, making them attractive replacements for solid adsorbents in carbon capture industries. Adsorbents must be capable of effective capture, regeneration, and ensuring sustainability. The processes of vacuum swing adsorption (VSA), pressure swing adsorption (PSA), and temperature swing adsorption (TSA) can all involve porous material-based technologies.³⁵⁷ Because of their large specific surface areas (S_{BET}) and pore volumes, strong chemical and thermal stability, ability to be made at low cost *via* readily available raw materials, customizable textural characteristics, and surface functions, porous carbons are the most extensively investigated adsorbents for carbon capture. The prediction of CO₂ capture capacity and S_{BET} was performed using MLP and RBF algorithms. The MLP model has been presented in a comparison of numerous networks to estimate diverse biomass syntheses, and the suggested method by Mashhadimoslem *et al.*³⁵¹ forecasted both CO₂ adsorption and S_{BET} of various biomass precursors *via* various temperatures of syntheses (see Fig. 17e and f). Zhang *et al.*³⁵⁸ and Wang *et al.*³⁵⁹ offered CO₂ adsorption capacity alongside textural characteristics such as S_{BET} , micropore, and mesopore volumes (V_{micro} and V_{meso}) as input features utilizing deep neural networks (DNNs). Pressure, as well as temperature, was incorporated into the

input features to retrain the model after using all the textural characteristics described above for algorithm training. To determine the gas–solid (N₂/CO₂) interactions and therefore CO₂ capture capabilities, S_{BET} is an independent textural parameter that could be dynamically linked with other textural factors. CO₂ adsorption depends on the intricate interaction of textural characteristics with each parameter's sensitivities that could be calculated. Yuan *et al.*³⁶⁰ used ML to systematically map the relationship between CO₂ adsorption and the textural and compositional properties of BWDPs (biomass waste-derived porous carbons), along with adsorption parameters. In this research, the gradient boosting decision tree (GBDT), light gradient boosting machines (LGB), and XGBoost algorithms using experimental datasets were used. Permutation importance plots of the entire dataset revealed that the pressure and temperature of the adsorption experiments had the most significant impact on the model's predictions. Textural properties, including S_{BET} , total pore volume (TPV), and micropore volume (MPV) also played a significant role in decreasing the order of importance. Compositional features ranked in decreasing order of significance were N > O > H > C. The feature importance test was also performed on RPCs (regular porous carbons) and HDPCs (heteroatom-doped porous carbons) sub-





Fig. 17 Contour maps of (a) S_{BET} ($\text{m}^2 \text{g}^{-1}$), and (b) CO_2 adsorption capacities (mmol g^{-1}) at 298 K and 1 bar,³⁵⁹ reproduced with permission from the American Chemical Society, the contour maps of CO_2 capture and micropore and mesopore volume under the same adsorption conditions, (c) at 298 K and 1 bar and (d) at 5 bar,³⁵⁸ reproduced with permission from Wiley, (e) 3D response surface of CO_2 adsorption prediction using the MLP from different precursor biomass and activators and, and (f) prediction of S_{BET} ($\text{m}^2 \text{g}^{-1}$) synthesized from different biomass materials and activators at different temperatures using RBF algorithms,³⁴⁶ reproduced with permission from American Chemical Society.

datasets. For the RPC dataset, the top three important input features for model prediction were pressure, temperature, and MPV. Likewise, in the HDPC dataset, the most dominant factors were adsorption temperature, pressure, and S_{BET} . In another research study, Ma *et al.*³⁶¹ developed the RF algorithm to study the effects of the pore structure, chemical properties, and

adsorption conditions on CO_2 adsorption performance. Their results indicated that at low pressure (0–0.15 bar), the pressure was a significant factor in CO_2 adsorption capacity. However, as pressure increases, the relative importance of pressure in CO_2 adsorption capacity decreases. Chemical properties and pore structure are also key factors in CO_2 adsorption, with pore



structure having a greater impact on adsorption capacity than chemical properties. In terms of the pore structure and chemical properties of porous carbon, N groups have the largest impact on adsorption capacity at low pressure, followed by ultra-micropore volume (V_u). Xie *et al.*³⁶² developed an ML model using the RF, SVM, LR, MLP, and SHAP (Shapley Additive Explanations) algorithms that were effectively trained to forecast CO_2 adsorption capacity. The SHAP algorithm has been utilized to gain insights into the unclear relationship between each physicochemical property and adsorption capacity. The findings revealed that textural properties are more influential than chemical composition in determining CO_2 uptake. The SHAP analysis revealed that the highest CO_2 adsorption capacity occurred at low pressure and a temperature of 298 K, with an S_{BET} of 1100–1300 $\text{m}^2 \text{g}^{-1}$, micropore volume (V_m) of 0.4–0.6 $\text{cm}^3 \text{g}^{-1}$, mesopore volume (V_{me}) of <0.1 $\text{cm}^3 \text{g}^{-1}$, carbon content (C) of 72–86 wt%, hydrogen content (H) of 1–4 wt%, oxygen content (O) of <16 wt%, and nitrogen content (N) of <1 wt%.

Wang *et al.*³⁵⁹ developed an ML model using the DNN algorithm and trained the algorithm using experimental data on CO_2 and N_2 uptakes in porous carbons. The training algorithm was based on textural features such as micropore volume, mesopore volume, S_{BET} , temperature, and pressure adsorption conditions. The trained DNN model was then used to screen porous carbons and predict their CO_2 and N_2 uptakes and CO_2/N_2 selectivity. In this study, 2500 hypothetical combinations of micropore volume (V_{micro}) and mesopore volume (V_{meso}), ranging from 0.02 to 1.00 $\text{cm}^3 \text{g}^{-1}$, were created. The trained DNN-3 model was then employed to predict their S_{BET} . Additionally, another neural network (DNN-3) was trained to predict S_{BET} from V_{micro} and V_{meso} and was used to generate 2D maps of adsorption uptakes and selectivity (see Fig. 17a and b). The results of this analysis suggest that introducing more mesopores in microporous carbons can disrupt and decrease N_2 adsorption, ultimately leading to better CO_2/N_2 selectivity. Their research results discovered that the highest CO_2/N_2 gas selectivity is not necessarily obtained in the regions with the highest CO_2 uptake, but rather in the regions with the lowest N_2 uptake where mesopores can disrupt N_2 adsorption. Moreover, it was found that the best features for high CO_2 uptake may not necessarily be optimal for achieving high CO_2/N_2 selectivity.

Zhang *et al.*³⁵⁸ developed an ML model using S_{BET} , V_{micro} , V_{meso} , temperature, and pressure parameters for CO_2 adsorption prediction. In this study, a DNN was trained as a generative model to establish the relationship between the CO_2 adsorption of porous carbons and their corresponding textural properties. Then, the neural network was utilized as an implicit model to evaluate its ability to predict the CO_2 adsorption capacity of unknown porous carbons. It was found that when the V_{micro} , V_{meso} , and S_{BET} are used as input neurons simultaneously, the trained neural network was able to achieve a remarkable agreement between experimental and predicted CO_2 adsorption capacity values (see Fig. 17c and d). The investigations confirmed that V_{meso} is important in controlling gas uptake, contrary to the previous belief that V_{micro} is the only parameter. Additionally, S_{BET} is an independent textural parameter that can work with other parameters to determine gas-uptake capacities.

Finally, gas uptake in solid adsorbents depends on the complex interplay of textural parameters, and the sensitivity of each parameter can be estimated.

A further interesting possibility for carbon capture, separation, and storage is MOF adsorbents, which have a variety of porosities, high S_{BET} , low densities, and an extensive variety of pore size diameters.^{363,364} To determine structure–performance correlations and choose the top descriptors that can precisely predict the CO_2 adsorption capacity, efficiency, and selectivity, ML is applied in MOFs for carbon capture technologies.^{365,366} Deep generative models, such as the supramolecular variational autoencoder (SmVAE), were created by Yao *et al.*³⁶⁶ for the converse design of MOFs exhibiting improved CO_2 capacity selectivity and separation from other gases. The autoencoder, which was jointly trained on several top adsorbent materials found for better gas separation, demonstrated promising optimization potential in this study.

Over 14 000 new CoRE MOF 2014 database structures have been proposed, and the MOF's structure came from several types of sources. By compiling the new structure data to feed the database, the full set of structures for the presence of open metal sites (OMSs), examining the impact of bond energy on the calculated geometric attributes, and considering real MOFs that could be discovered in a set of computer-generated, hypothetical MOFs, the understanding of the molecular fingerprint strategy was illustrated. With the aid of the distribution of data from experiments, the mentioned model could begin to produce a new dataset.³⁶⁷ Given the assistance of data from experiment distribution, this model could begin to produce new data. Using the 372 MOF edges acquired through CoRE MOF identification, this study produced an edge dataset of over 300 000. When simultaneously trained using several top suggestions for improved gas separation and verified by atomistic Monte Carlo (MC) simulations, this model demonstrated excellent predicting and optimizing capabilities.

Researchers provide cases of ML development in various CO_2 capture, storage, transport, and utilization (CCSTU) systems. Adsorption, absorption, chemical looping, membranes, sequestration, and hydrates are a few examples of carbon capture or separation technology (CCST). Any research project incorporates a synergistic approach (sequestration plus absorption).³⁶⁸ Modeling and simulating solvent-based carbon capture requires extensive effort and time owing to the complicated governing processes of absorption, particularly chemical absorption, involving mass transfer and chemical reactions.^{356,369} The measurement of parameters such as the mass flow rate using differential pressure-based flowmeters is unable to attain adequate precision in the measurement of mass flow, and their substantial complexity and cost limit their use in carbon capture, utilization, and storage (CCUS) industries. Recently, low-cost sensing methods that include ML techniques to increase the accuracy of flowmeters have been developed.³⁶⁸ In oxyfuel combustion for CO_2 collection, ML is also used in applications including forecasts of combustion characteristics and pollutants' emissions, as well as controlling the process of combustion using flame images.³⁷⁰ The use of ML algorithms for chemical looping combustion for CO_2 capture



has been investigated in a few investigations, although this subject still needs further research.³⁷¹ The novel modeling and analysis work that has been performed to examine various elements of the CO₂ adsorption, absorption, and separation processes in porous media is the main topic of our review study. Adsorbent materials, the adsorption process, optimization, and simulation of the process are all included.

Zhang *et al.*³⁷² developed ML techniques using experimental and simulation datasets that revealed the most significant factors affecting CO₂/N₂ selectivity and CO₂ permeability in the MOF composite. The RF model revealed that AV is a key factor in predicting membrane selectivity and GASA is a key factor in predicting CO₂ permeability. Guan *et al.*³⁷³ developed RF models trained on literature experimental data for CO₂/CH₄ separation to identify suitable MOFs for constructing Mixed Matrix Membranes (MMMs). The resulting membranes showed CO₂ separation performance beyond the 2008 Robeson upper bound and agreed well with model predictions. Moosavi *et al.*² developed and trained the ML model (using the XGBoost algorithm) using DFT simulations to predict the heat capacity of solid nanoporous sorbents, including MOFs, zeolites, and COFs. The ML model's highly accurate heat capacity prediction allows for quantifying the influence of heat capacity variations on material ranking in a TSA process. Yao *et al.*³⁶⁶ developed a platform using experimental data for nanoporous material discovery using a super molecular variational autoencoder (SMVAE) to create reticular frameworks with optimized properties. The MOF structures generated using the SMVAE model showed significant competitiveness against some of the best-performing MOFs/zeolites reported to date. The platform was employed to design new MOFs with improved CO₂/N₂ and CO₂/CH₄ separation capacity and selectivity. The developed platform has wide-ranging applicability for various materials, such as COFs, metal-organic polyhedra (MOP), hydrogen-bonded organic frameworks, and coordination polymers. It serves as a basis for creating reticular frameworks for diverse applications. Gao *et al.*³⁷⁴ employed ML using XGBoost, RF, Gradient Boosting Machine (GBM), and MLP algorithms and simulation datasets to gain a comprehensive understanding of the adsorption behaviors, and an ML-assisted analysis was employed to pinpoint the preferred CO₂ adsorption sites for each framework at various four distinct temperatures. The center-of-mass coordinates of 800 CO₂ molecules were randomly selected and labeled with their corresponding binding site types. Various well-known ML algorithms were applied to learn the relationship between the CO₂ molecule's C atom coordinates and the corresponding adsorption site types. Krokidas *et al.*³⁷⁵ for the first time used the ML using DFR and DTR algorithms to investigate how the substitution of basic MOF building blocks affects the pore structure and molecular diffusivity. While the ML approach is general, the focus was specifically on ZIFs with SOD topology. Due to the lack of a relevant ZIF database, an ensemble of 72 new and existing ZIFs has been created through systematic sub-unit replacement. Forcefields were developed for each structure, and fully flexible MD simulations were conducted to determine the framework properties and molecular diffusivity of various molecules.

Another study was presented by Yang *et al.*³⁷⁶ which used ML-assisted MC computational screening to identify optimal secondary building units (SBUs) for wet flue gas separation using COFs. They used the DT, RF, XGBoost, and CatBoost algorithms for the training of the experimental dataset. It has been found that tetraphenyl porphyrin units enhanced CO₂ adsorption uptake, while functional groups improved CO₂/N₂ selectivity. Based on these findings, 1233 COFs were assembled using the optimal SBUs. This research analyzed the quantitative relationship between input descriptors and COF separation performance. Their results showed that the IS and S_{BET} features had the greatest impact on CO₂ uptake, whereas the IS and DF features had the most significant impact on CO₂/N₂ selectivity. Cheng *et al.*³⁷⁷ proposed a multi-scale design framework using an MD simulation dataset for CO₂/CH₄ separation *via* MOF-based membranes. In this research, ANN prediction models were created and trained using MD and GCMC simulations to characterize the adsorption capacity and self-diffusivity of MOF membranes. The models were subsequently employed to determine permeability. The tanks-in-series model of a hollow fiber membrane separation process was combined with the ANN models and simulated using the finite volume method. Zhu *et al.*³⁷⁸ using the DFT calculations dataset developed ML models that were employed to predict the ΔG and pressure of all possible reaction intermediates and products, including methanol, methane, and formaldehyde, during the reduction of CO₂ on 26 single-atom catalysts (SACs) in zeolites. The multi-ML models proposed using XGBoost, gradient boosting regression (GBR), extra trees, KNN, DT, ANNs, SVR, multi-linear regression (MLR), linear ridge (LR), and least absolute shrinkage and selection operator (LASSO) algorithms exhibited good transferability and can be utilized to predict the performance of MOFs, 2D materials, and molecular complexes. After a comparison of the selected algorithms, the XGBoost algorithm demonstrated the strongest performance with an MAE of 0.36 eV and an R² value of 0.87. Kriesche *et al.*³⁷⁹ integrated a new ML model, the ANI-2 neural network potential (NNP) with an MD framework to model the behavior of two COF systems, HEX COF1 and 3D-HNU-5, which share the same linking unit. Their results indicated that the ANI-2x NNP could accurately describe the structures of macromolecules such as COFs and their interactions with CO₂ guest molecules. The main innovation of this research was the use of a DFT-based neural network approach and a suitable MD simulation protocol to simulate a relatively large system over an extended period. This approach provides access to correlated properties within the long-time limit, with a particular focus on estimating the system's diffusion coefficient. The exceptional efficiency of this approach was demonstrated by the extensive total simulation time of over 0.4 μs, which cannot be achieved using traditional DFT methods. The use of minimum distance distribution functions (MDDFs) can provide valuable insights into the nature of interactions between host-gas molecule systems. In this study, MDDFs were employed to identify similarities and differences in the host-CO₂ interactions of HEX-COF1 and 3D-HNU5. Feng *et al.*³⁸⁰ created an intelligent system for materials, which utilized the DeepFM approach to predict multiple adsorption properties of



the hMOF database by integrating descriptors. The mentioned research investigated the importance of various descriptors on the CO₂ capture capabilities of MOFs. Their results revealed that MOFID is an extremely crucial descriptor. Excluding MOFID, the top five important descriptors for CO₂ uptake and CO₂/N₂ selectivity were the same, which included topology, metal linker, functional group, S_{BET} , and porosity, although their ranking differed slightly. The DM model presented in this study was used to predict 28 adsorption properties of 8206 screened hMOFs database. Sturluson *et al.*³⁸¹ proposed a COF recommendation system that matches COFs with specific adsorption tasks. This model was achieved by training a low-rank model of an incomplete COF-adsorption-property matrix constructed from simulated uptakes of CH₄, H₂O, H₂S, Xe, Kr, CO₂, N₂, O₂, and H₂ using experimental data under various conditions. This model was developed by fitting a model of the COF-adsorption-property matrix to the observed (COF, adsorption property) values. The mentioned research results were able to provide predictions for missing (COF, adsorption property) values. Additionally, this approach generated a “map” of COFs, where COFs were represented as points and those with similar or dissimilar adsorption properties congregated or separated, respectively. The COF recommendation system developed in this research was found to be capable of effectively ranking COFs for most adsorption properties. However, the imputation performance of the system decreased significantly when the fraction of missing entries in the COF-adsorption-property matrix exceeded 60%. A knowledge engineering technology was utilized by Kondinski *et al.*³⁸² to automate the development of MOP formulations using existing knowledge as a database. In this study, an ontological MOP was created to establish a clear definition of MOP and its essential properties. Raji *et al.*³⁸³ developed ML models, which use experimental temperature and pressure CO₂ adsorption. The main goal of this study was to develop efficient prediction models using soft computing methods, specifically hybrid-ANFIS, particle swarm optimization-adaptive neuro-fuzzy inference system (PSO-ANFIS), and least-squares support vector machine (LSSVM), for estimating CO₂ adsorption on five distinct types of zeolite adsorbents (5A, 13X, T-Type, SSZ-13, and SAPO-34). This research aimed to provide an alternative to the costly and time-consuming laboratory experiments currently used for this purpose. Based on the results, it was demonstrated that all the proposed models are reliable and precise for estimating CO₂ adsorption on various types of zeolites. Zhang *et al.*³⁸⁴ utilized the ML using RF, XGBoost, and SHAP algorithms to investigate the correlation between the CO₂ adsorption performance of amine-functionalized adsorbents and input descriptors. It was found that amine loading was the most crucial factor affecting CO₂ adsorption capacity, followed by pore volume. Pore size was the primary factor influencing amine efficiency, while the cycle stability of the adsorbent was mainly related to the type of amine used. This research illustrated, that to attain the highest possible CO₂ adsorption capacity for the adsorbents, the pore volume required for amine loading should account for 40–50% of the support's pore volume for TEPA (Tetraethylenepentamine) and 65–75% for PEI (polyethyleneimine). Yan *et al.*³⁸⁵

presented a deep learning (DL) workflow for predicting the pressure evolution of fluid flows in large-scale 3D heterogeneous porous media. This research developed an efficient feature technique to extract the most representative information for DL training and prediction at the coarse scale. The mentioned technique also allowed for the recovery of resolution at a fine scale through spatial interpolation. By using a pre-defined stride, feature coarsening was employed to extract the most representative information about geology and well controls, resulting in reduced memory consumption of feature arrays and improved training efficiency. The effect of feature coarsening on DL performance was investigated, and it was discovered that it not only cut training time by more than 74% and memory consumption by more than 75% but also maintained an average temporal error of 0.63%. Another research study focused on the gas permeability database, to address missing values in the database. Yuan *et al.*³⁸⁶ utilized the ML model to impute or fill in the missing data. For systems with limited experimental data, sparse feature ML was utilized. The study suggests that once the permeability of CO₂ and/or O₂ for a polymer has been measured, most other gas permeabilities and selectivity, including those for CO₂/CH₄ and CO₂/N₂, can be quantitatively estimated through ML techniques. The research results suggested that KAUST-PI-1 may exhibit potentially high CO₂/CH₄ selectivity and good CO₂/N₂ selectivity. This prediction was later confirmed by experimental work that was not originally recorded in the database. The multivariate imputation by chained equations (MICE), Bayesian linear regression (BLR), and extremely randomized tree (ERT) algorithms were used to simulate datasets (1387 datasets). The ERT algorithm showed the best results in predicting CO₂/CH₄ and CO₂/N₂ adsorption selectivity, based on the CO₂ permeability data.

3.5.3. Carbon sequestration. The ML models created could be used for precisely calculating the experimental data crucial for carbon sequestration. The assessment outcomes show how well the trained ML model performed on a carbon sequestration site with comparable geology but varied permeability distributions for the geologic strata. We could assess the feasibility of ML models on different CO₂ storage sites by employing flow simulations with various permeability parameters using ML algorithms. Yamaguchi *et al.*³⁸⁷ developed an ML model in sequestration industries. In this research, a novel multiscale numerical method was proposed to estimate the permeability of hydrate-bearing sediments in reservoir-scale simulations spanning several hundred meters. The method utilizes an ML technique based on a database of results from microscopic pore-scale simulations of a couple of hundred micrometers. This study aimed to introduce a new framework for calculating the normalized effective permeability (kH) resulting from hydrate formation. The novelty of this study was in the development of a new framework for multi-scale two-phase flow simulation with CO₂ hydrate formation, utilizing an ML approach. Two neural networks were utilized to establish a connection between hydrate growth on the reservoir scale and permeability based on hydrate morphology on the pore scale. The mentioned networks were the hydrated shape recurrent neural network (RNN) and the permeability neural network. The



hydrated shape RNN was adopted to represent hydrate morphology. The use of RNNs was appropriate, as the temporal changes of geometrical parameters were strongly related to physical parameters for hydrate shapes (S_{BET} and tortuosity in X , Y , and Z directions). The hydrate shape RNN was designed to extract temporal information from the reservoir scale, which was then used to obtain microscale geometrical parameters. Meanwhile, the permeability neural network utilizes the outputs of the hydrate shape RNN, along with hydrate saturation and porosity, to predict the changes in permeability resulting from hydrate formation. Among all geological storage possibilities, deep saline aquifers tend to be the best choice for CO_2 storage. Storage aquifer properties including the temperature, pressure, water's salt, porosity, heterogeneity, permeability, and the rate of CO_2 injection all affect how much energy can be stored in saline aquifers.³⁸⁸ Another research study on the CO_2 sequestration field by Thanh *et al.*³⁸⁹ was performed. This study developed three supervised ML-based models (RF, SVR, and XGBoost algorithms) to predict the trapping efficiency of CO_2 sequestration in saline formations. The ML models were ranked according to their accuracy, with XGBoost being the most accurate, followed by RF and SVR. The proposed model could serve as a valuable and practical template for predicting CO_2 trapping indices in other saline formations around the world. The input features, in order of decreasing importance to storage efficiency, are permeability, thickness, injection time, injection rate, porosity, depth, salinity, residual gas saturation, and post-injection time. Permeability, formation thickness, time, and injection rate were the most critical parameters that affected the volume of CO_2 stored, as well as its residual and solubility. The proposed XGBoost model has significantly reduced training, testing time, and computational cost compared to previous models, making it more efficient for evaluating the feasibility of CO_2 storage projects.

3.6. Groundwater

Finding proper, cost-effective, and efficient models in hydrology and groundwater is always challenging. On the one hand, hydrologic cycle phenomena such as flood and streamflow, evapotranspiration, precipitation, infiltration, groundwater modeling, *etc.*, have a complex process on a catchment scale and cannot be predicted using simple/linear models.³⁹⁰ On the other hand, developing and implementing a model that involves all catchment phenomena, such as distributed and semi-distributed hydrologic models/physically-based models *i.e.*, MIKE-SHE and SWAT (soil and water assessment tool) is time-consuming and needs a vast amount of high-quality input data according to ref. 391–393. Owing to substantial advancements in computational power, ML algorithms have recently achieved notable breakthroughs in managing and processing intricate and voluminous datasets. Due to high computational power, user-friendliness, handling big data, handling data with different dimensions, not needing a vast amount of data like numerical models, and high prediction/forecasting power of any complicated process such as water resource phenomena by formulating the relationship between inputs and output

variables,^{394–396} application of ML/DL algorithms has recently been increasing, especially in the field of hydrology and groundwater resources. In addition, by expanding the application of big data, which is available from numerous sources such as satellite images, reanalysis data, drones, sensors, and geophysical data,³⁹⁷ the use of ML/DL model has significantly increased. Within this context, groundwater issues have consistently been a focal point for researchers seeking to harness these technological strides for diverse applications. These applications encompass areas such as hydrological modeling, fluid flow and transport in porous media, and the characterization of geo-systems. Consequently, there exists pervasive interest in the development of ML techniques tailored to capitalize on the burgeoning availability of substantial datasets from the varied above-mentioned sources. Khosravi *et al.*³⁹⁸ compared the prediction accuracy of hybrid ML models, including random forest (RF) and Dagging-RF (DA-RF), simple and well-known approaches of sediment rating curve (SRC), and the SWAT model for prediction of suspended sediment load at Talar catchment, in the north of Iran. They revealed that the Dagging-RF model outperformed traditional and physically based models. Therefore, complicated models such as distributed and semi-distributed models don't guarantee higher prediction power, and their results confirm the higher performance of ML models in groundwater.

Groundwater resource management on a catchment scale can be divided into two main classes, namely, surface water hydrology (precipitation, streamflow, flood, infiltration, soil moisture, and wetland/lake water level) and groundwater hydrology. Surface water hydrology is not well matched by porous media, but all relevant groundwater applications are in the area of porous media. Overall, modeling of fluid flow in porous media has numerous applications, from the micro-scale (cell membranes, filters, and rocks) to macro-scale (groundwater, hydrocarbon reservoirs, and geothermal) and beyond, and in the current review macro-scale application, which is more relevant to groundwater resources, has been reviewed and discussed. In natural science, soil and rocks are prominent examples of porous media. Fluid flow which goes through porous media (*i.e.*, ground/soil) is a fascinating subject and has a significant impact on other hydrologic cycles.³⁹⁹ DL algorithms employing CNNs have been used to analyze porosity, permeability, and tortuosity in porous media through fluid flow, yielding accurate results. In groundwater resource management, regression and classification-based methods can be applied, depending on the context and objective. Generally, a regression-based approach is used for time series prediction (*i.e.*, streamflow, rainfall, *etc.*), while classification-based methods are used for spatial modeling (*i.e.*, flood, groundwater, *etc.*).

The data inherent to porous media and subsurface systems exhibit distinctive attributes that differentiate them from commonplace datasets in other domains. In contrast to conventional data encountered in fields such as image recognition within computer science, the data associated with porous media adhere to physical laws. Consequently, the direct application of ML techniques to such data is often impractical,



necessitating reformulation and customization of these techniques to align with the inherent characteristics of the dataset. The burgeoning influx of data-sensing tools, coupled with the continuous evolution of advanced computational algorithms, underscores the imperative to develop ML and automated methods capable of addressing the complexities posed by such data.

Effectively unlocking the potential of big data in geosciences and making informed decisions mandates the development of advanced techniques adept at identifying intricate dependencies and patterns within the dataset. This involves overcoming inherent challenges that make traditional methods difficult or nearly impossible. As elucidated in this review, ML techniques emerge as a highly efficient alternative for discerning patterns within vast and multidimensional datasets. The adaptability of ML allows for the discovery and extraction of linear and nonlinear correlations among various physical parameters. Such capabilities of ML techniques have proven instrumental in unveiling the potential inherent in big data, thereby advancing our comprehension of complex phenomena within porous media, spanning scales from the minuscule to the expansive in GeoMedia.³⁹⁷

3.6.1. Infiltration. Entering the fluid (herein water) into and through any porous material (here from topsoil to soil media) is defined as infiltration, which is one of the most interesting topics in groundwater modeling, especially for sub-surface flow modeling. Deep infiltration is called percolation and leads to groundwater recharging. Infiltration/percolation is one of the most complicated processes on a catchment scale, as numerous phenomena are involved including catchment slope, soil, vegetation, and rainfall characteristics. Infiltration rate is measured using a double ring infiltrometer as the standard method. Double ring infiltrometers are made of two iron rings. Thus, a survey for infiltration rate measurement is difficult and time-consuming. Hence, an alternative and promising tool is highly recommended, which is the ML model's applications.

Panahi *et al.*⁴⁰⁰ applied an optimized DL of a CNN using gray wolf optimization (GWO), a genetic algorithm (GA), and independent component analysis (ICA) for the prediction of two important soil characteristics, cumulative infiltration and the infiltration rate. They considered time of measuring, sand, clay, and silt percent, bulk density and soil moisture percent from field survey as inputs. They showed that metaheuristic algorithms enhance the CNN model's prediction power and that they can accurately predict cumulative infiltration and infiltration rates. In addition, their findings revealed that time had the most effective impact on cumulative infiltration, while silt content was the most correlated variable with the infiltration rate. Rehman *et al.*⁴⁰¹ implemented ML-based intelligent modeling of sandy soils' hydraulic conductivity (k) considering a wide range of grain sizes. They considered and involved a comprehensive array of input parameters delineating geological characteristics, including but not limited to variations in grain sizes encompassing large, medium, and small dimensions (D), gradation parameters, and dry density (γ_d). This deliberate inclusion aims to address the inherent limitations of prevailing k -value predictive models, ensuring a more

robust coverage of output variability across diverse combinations of D -values within a sandy soil deposit. They applied the ANN, multi-expression programming (MEP), and genetic expression programming (GEP) on a large dataset. They revealed that the GEP model is the superior model. Lu and Mei⁴⁰² applied a DL approach for predicting excess pore water pressure of two-dimensional soil consolidation using PINN. The effectiveness of the developed approach was evaluated by comparison with the numerical solution of the partial differential equation (PDE) for two-dimensional consolidation. They depicted that the excess pore water pressure could be predicted efficiently using this developed approach. Pandhiani⁴⁰³ applied different ML models, including SVM, M5 Prime (M5P), Gaussian process (GP), RF, and multiple linear regression (MLR) for infiltration rate prediction and compared the result with those of some empirical models such as the Kostiaikove model using different error indicators. They revealed that time is the most influential parameter on the infiltration rate compared with sand, silt, density, initial moisture content, *etc.* In addition, they showed that the RF model outperforms other models.

3.6.2. Soil moisture. Top-surface and sub-surface soil moisture significantly impacts the infiltration rate, groundwater recharge, and rainfall-runoff process. According to the application process, soil moisture measurement at a different temporal and spatial scale is required. Soil moisture measurement is difficult, time-consuming, and costly which needs weighing the wet soil sampled from the field, drying it in an oven, and then weighing the dry soil (wet soil mass minus the dry soil mass divided by the dry soil mass is equal to the soil moisture or water content). Tensiometers are devices for measuring soil moisture, but they also need field surveys and collecting data, which makes it difficult. Recently, the application of the ML/DL model in this field of study has caught the attention of researchers, as it is easy to implement and leads to reasonable and accurate results.

Prakash *et al.*⁴⁰⁴ developed and compared the prediction accuracy of MLP, SVM, and RNN for predicting soil moisture 1, 2, and 7 days ahead. Their finding revealed that the MLP model outperforms other models by a mean square error (MSE) and coefficient of determination (R^2) of 0.14 and 0.975 for one day ahead, 0.353 and 0.939 for two days early, and 1.59 and 0.786 for seven days on, respectively. Singh and Gaurav⁴⁰⁵ compared the prediction accuracy of different ML/DP models for the prediction of surface soil moisture from multi-sensor satellite images. They developed an ANN, a generalized regression neural network (GRNN), a radial basis network (RBN), exact RBN (ERBN), Gaussian process regression (GPR), SVR, RF, boosting ensemble learning (boosting EL), RNN, binary decision tree (BDT), and an automated ML (AutoML) model. Finally, they stated that the ANN model outperforms other models. More papers and information about this subject can be found in Uthayakumar *et al.*⁴⁰⁶

3.6.3. Water movement in vadose and saturated zone area. A vadose zone/unsaturated area is defined as an area from topsoil to the water table or saturated area. Less attention has been paid to database-dependent accuracy, the uncertainty of



results, reproducibility, and delivery of ML models in vadose zone areas.^{407–409} Water movement in vadose/saturated zone areas is mainly used for groundwater flow and contaminant transport in unsaturated and saturated areas. Sahour *et al.*⁴¹⁰ evaluated different ML models of SVM, ANN, KNN, and Gaussian classifier model (GCM) for groundwater quality index (GQI) modeling. All models showed good prediction accuracy, but RF was considered superior. Feature selection analysis revealed that the distance to industrial areas is the main factor affecting groundwater quality. More papers and information about this subject can be found in Sajedi-Hosseini *et al.*,⁴¹¹ Zhu *et al.*,⁴¹² Kumar and Pati,⁴¹³ and Meray *et al.*⁴¹⁴

3.6.4. Groundwater potential area. Groundwater is defined as water that fills rock and pore spaces in a saturated zone/aquifer.^{415,416} Groundwater potential is the possibility of groundwater occurrence in a specific area.⁴¹⁷ The dynamics of groundwater within an aquifer are influenced by numerous geo-environmental factors including lithology, topography, geology, fault and fracture networks and their interconnections, drainage patterns, and land use/land cover.⁴¹⁸ Geological strata serve as both conduits and reservoirs for groundwater, with the storage and transmissivity of these formations dictating the viability of groundwater exploitation. Topographical features contribute to runoff generation, enhancing recharge and infiltration.⁴¹⁹

Globally, groundwater constitutes a primary drinking water source for approximately 2 billion individuals,⁴²⁰ while in the agricultural sector, around 278.8 million hectares of land are irrigated by groundwater.⁴²¹ With population and economic

growth, the future demand for groundwater is expected to rise.⁴²² However, recognizing that groundwater is a finite resource underscores the imperative of understanding its potential for sustainable utilization. One of the most effective methodologies for managing groundwater resources is the delineation of groundwater potential zones.⁴²³

Numerous methodologies exist for groundwater potential mapping, with traditional techniques such as drilling, geological, geophysical, and hydrogeological methods being widely employed.⁴²⁴ However, these methods are often time-consuming and financially burdensome, particularly for expansive areas. In recent years, the integration of geographic information systems (GIS) and remote sensing has been proven instrumental in groundwater potential mapping,⁴²⁵ owing to their capacity to efficiently handle extensive spatial datasets. A sample methodology is given in Fig. 18. This methodology has been used in other fields of study such as groundwater recharge area delineation, groundwater vulnerability assessment, and even flood modeling, landslide occurrences evaluation, and land subsidence spatial mapping.

Khosravi *et al.*⁴²⁶ optimized the ANFIS model with five metaheuristic models, including weed optimization (IWO), differential evolution (DE), firefly algorithm (FA), particle swarm optimization (PSO), and the bee's algorithm (BA) for delineating potential groundwater mapping through 2463 spring locations in Koohdasht–Nourabad plain, Iran. They revealed that based on the result of ANFIS–DE as a superior model, 39.33% of the study area has a high and very high groundwater potential north of the plain. In addition, they depicted that based on the finding



Fig. 18 Groundwater potential mapping approach using ML models, Khosravi *et al.*,⁴²⁶ adopted with permission from Copernicus Publications. The flowchart outlines a method involving data collection, analysis, model development, and validation. Initially, groundwater samples are divided into training (70%) and testing (30%) datasets. Key impacting parameters are identified through data correlation and multicollinearity analysis. ML models are then developed using metaheuristic optimization techniques such as invasive weed optimization, differential evolution, the firefly algorithm, PSO, and the bees algorithm. Model performance is evaluated using metrics such as MSE and RMSE, followed by statistical tests (Friedman and Wilcoxon signed-rank) to ensure accuracy. The final goal was to select the optimal model for mapping groundwater spring locations.



of the information gain ratio (IGR) technique, land use/land cover, lithology, rainfall, and TWI are among the most efficient factors in groundwater occurrence. Hakim *et al.*⁴²⁷ compared the prediction accuracy of the CNN and LSTM models to delineate a potential groundwater map in Anseong, South Korea. To meet the aim, a total of 295 well locations were separated using the median value of transmissivity data (T) and assigned “1” as high groundwater productivity data and “0” as the point with low groundwater productivity. Finally, they stated that both models under a receiver operating characteristics (ROC) curve (AUC) of more than 0.80 show good accuracy. Morgan *et al.*⁴²⁸ applied RF models to delineate potential groundwater zones in the desert fringes of the East Esna-Idfu area, Nile Valley, Egypt. They revealed that the soil type factor has the highest impact on groundwater occurrences. In addition, they showed that the RF model, with an accuracy of 97%, selectivity (recall) of 92%, and *F1*-score of 94%, has an excellent prediction power in delineating potential groundwater areas.

3.6.5. Groundwater vulnerability assessment. The DRASTIC model, developed by Aller *et al.*,⁴²⁹ is one of the most widely used and practical approaches in groundwater vulnerability assessment of inland areas for delineating areas with different pollution risks. At the same time, GALDIT is suitable for coastal vulnerability assessment. DRASTIC stands for depth to water (D), recharge (R), aquifer media (A), soil media (S), topography (T), impact of the vadose zone (I), and hydraulic conductivity (C). GALDIT stands for aquifer type or groundwater occurrence (G), aquifer hydraulic conductivity (A), levels of groundwater above the sea level (L), distance from the shoreline (D), the impact of the current status of seawater intrusion (I), and the aquifer thickness (T). The main drawback of empirical models such as DRASTIC and GALDIT is the expert opinion in determining the weights and rates of these models. Therefore, several ML models have been combined with a DRASTIC model to improve the prediction power of the model. In addition, the effectiveness of DRASTIC parameters can change from one study area to another DRASTIC model input parameter is not obtainable, while the ML model provides a flexible framework in which different input parameters can be tested and investigated.

Khosravi *et al.*⁴³¹ modified the DRASTIC model using four statistical/ML models, weights-of-evidence (WOE), Shannon entropy (SE), logistic model tree (LMT), and bootstrap aggregating (BA) to generate a groundwater vulnerability map for the Sari-Behshahr plain, Iran. In addition, they investigated the effectiveness of eight additional factors, including distance to fault, fault density, distance to a river, river density, land use, soil order, geological time scale, and altitude, to improve groundwater vulnerability assessment for the first time as displayed in Fig. 19. They stated that additional factors could enhance the result of groundwater vulnerability assessment. They demonstrated that all models have improved the modeling performance of the original DRASTIC model. Their results showed that considering the input variable for groundwater, vulnerability directly depends on the plain characteristics and the input variable in original models may lead to higher error and need to be removed from the modeling. In another study,

Khosravi *et al.*³⁹⁶ implemented metaheuristic (DE and BBO) and multi-attribute decision-making (MADM), stepwise weight assessment ratio analysis (SWARA), and statistical index (SI) methods to improve the GALDIT model at the Gharesoo-Gorgan Rood coastal aquifer in Iran. Metaheuristic models were used to improve weight, while MADM models were applied to enhance the rating of the GALDIT model. Based on the findings, all models improved the prediction power of GALDIT, while the GALDIT_{SI-DE} model outperformed all other models. Their finding showed that integrating intelligent ML-based models can improve the results of empirical models. Ijlil *et al.*⁴³⁰ developed five hybrid ML models of DRASTIC-RF, DRASTIC-SVM, DRASTIC-MLP, DRASTIC-RF-SVM, and DRASTIC-RF-MLP, for groundwater pollution assessment in the Saiss basin, in Morocco. DRASTIC-RF-MLP (AUC = 0.953) and DRASTIC-RF-SVM (AUC = 0.901) showed higher performance, followed by DRASTIC-RF (AUC = 0.852), DRASTIC-SVM (AUC = 0.802), and DRASTIC-MLP (AUC = 0.763).

4. Challenges and future outlook

This section presents the challenges and future outlook pertinent to the previous chapter. In the field of heat exchanger and storage, research has a rich history dating back to the application of thermal systems in various industries. The extensive volume of currently available data, accumulated over the years, provides a valuable resource for categorization and future predictions through the application of ML approaches. The rapid development of ML technology sparks optimism and enthusiasm for leveraging more sophisticated tools in research, aiming to predict target functions and optimize thermal systems. An exciting avenue for advancement lies in the development of image-processing systems complementing ML methods. Such systems can potentially create online optimization tools on a real scale, reducing reliance on time-consuming numerical modeling. However, a significant challenge arises from the limited availability of comprehensive data, particularly for complex thermal systems or those involving hazardous fluids, posing a potential threat to the reliability of ML outputs. To address this challenge, the deployment of accurate thermal and hydrodynamical sensors is imperative, along with meticulous avoidance of random errors in experiments. Additionally, conducting high-fidelity numerical simulations becomes crucial to prevent the incorporation of noisy and imprecise data into ML models. The careful consideration of feature selection further contributes to refining the accuracy of predictions.

One notable concern in ML applications for thermal systems with simple physics is the risk of underfitting. Reliance on heavy numerical simulations and expensive experiments currently hampers the ability to feed a sufficiently large volume of data to ML models, impacting the precision of their outputs. Furthermore, as thermal systems become increasingly integrated into daily life, it becomes crucial to balance ML optimization with customer-friendly necessities, such as appearance and space occupation, to avoid potential adverse effects on marketing. A noteworthy aspect of current ML versions is their lack of interpretability and discussion on the outputs,



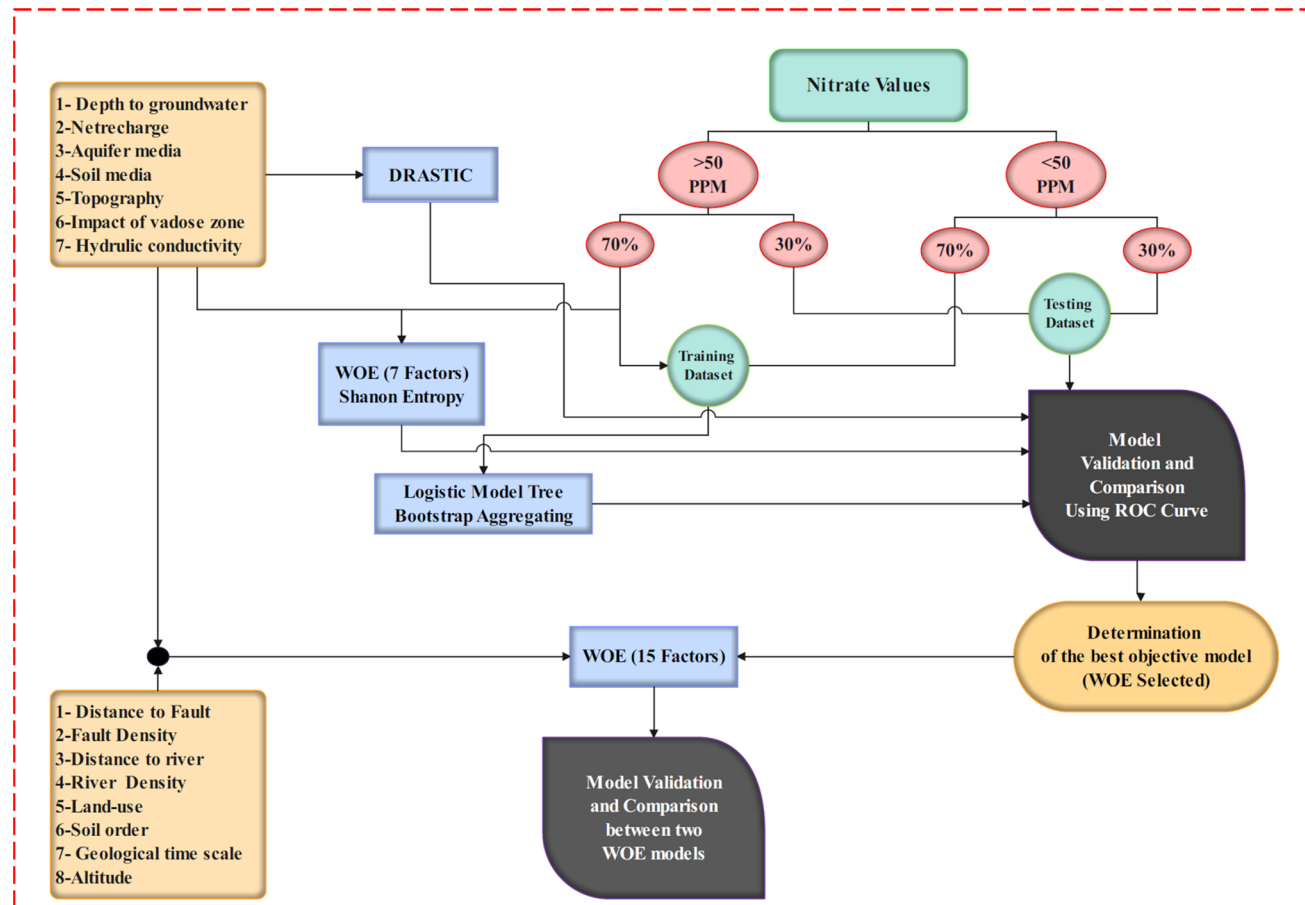


Fig. 19 Flowchart of the methodology for groundwater vulnerability assessment, Khosravi *et al.*,⁴³¹ adopted with permission from Elsevier. This flowchart outlines a systematic method to analyze nitrate levels in groundwater, focusing on data segmentation, model building, and verification. It starts by evaluating key factors such as groundwater depth, recharge rates, aquifer and soil media, and topography. The DRASTIC method is used to evaluate potential groundwater contamination. Data are divided into two categories based on the nitrate concentration: above and below 50 PPM, with each category split into 70% training and 30% testing datasets for modeling and validation. Model effectiveness is verified through the ROC curve for model performance evaluation and comparison.

potentially leading to incorrect interpretations. Despite these challenges, the outlook for ML in thermal science remains optimistic, with the potential for higher precision, reduced data feeding requirements, and improved identification and elimination of noisy input values. The realization of these advancements will largely depend on the continuous development of hardware capabilities.

When it comes to energy storage and combustion using porous media and ML, there are a few challenges and future outlooks to keep in mind. The first challenge is the availability and quality of data. ML algorithms require large amounts of data for training and validation, but obtaining comprehensive and high-quality data for some of the energy storage processes and combustion systems using porous media can be difficult. Limited data availability can affect the accuracy and generalizability of ML models. According to the literature, there is limited research on the integration of ML and geothermal energy storage, thermo-chemical energy storage, natural gas energy storage, and combustion using porous media. Thermo-chemical energy storage with porous media offers several

advantages, including high energy density, long-term storage capability, and reduced heat losses compared to some other storage technologies. However, there are also challenges associated with material selection, reaction kinetics, heat and mass transfer, and system design. Efficient utilization of porous media and optimal reaction conditions are crucial for achieving high storage capacity and fast heat transfer rates. Apart from lithium-ion batteries, experimental data for other batteries such as sodium-ion batteries and potassium-ion batteries are limited and it is hard to use ML to design and characterize battery materials.

Additionally, there are available hybrid energy storage options, such as electrical-gas hybrid energy storage and electrical-gravitational systems. This hybrid system combines electrical energy storage, such as batteries, with hydrogen gas storage using porous media. Excess electricity generates hydrogen through electrolysis and is stored in porous media, such as metal hydrides or adsorbents. When there is an electricity demand, the stored hydrogen can be utilized in a fuel cell to generate electricity. This hybrid storage system allows for the



storage of electrical energy in the form of hydrogen, providing longer-duration energy storage and enabling the use of hydrogen as an energy carrier. In another hybrid system, electrical energy storage is combined with gravitational potential energy storage using porous media. Excess electricity is used to lift heavy masses, such as concrete blocks or weights, against gravity, storing the energy as gravitational potential. When electricity demand is high, the potential energy is released, and the weight is lowered, driving a generator to produce electricity. Porous media can be used to support and control the movement of the weights, ensuring efficient energy storage and retrieval. An effective way to overcome this issue is through physics-informed ML (PIML). This approach combines principles from physics-based modeling with ML techniques to enhance the modeling, prediction, and understanding of complex physical systems. By incorporating domain knowledge, physical constraints, and governing equations into the ML framework, PIML recognizes that physical laws and governing equations provide valuable insights into the behavior of physical systems. This approach allows for more robust and interpretable models compared to purely data-driven ML models, as ML models can learn from limited data more effectively and make predictions that align with the underlying physical laws. Overall, PIML aims to leverage the strengths of both disciplines to provide more accurate and insightful predictions for complex physical systems.

Interpretability is also a challenge, especially with deep learning approaches that can be considered black boxes. It's crucial to understand the underlying physical phenomena within the porous media for gaining insights, optimizing system performance, and ensuring safe and reliable operation. Some challenges associated with thermal energy storage using porous media include heat transfer limitations, thermal degradation of the porous media, system efficiency, and economic viability. Overcoming these challenges requires advancements in materials science, system design, and optimization techniques. Another challenge is the complex and nonlinear dynamics of these systems. Modeling and understanding them accurately can be difficult due to the intricate interplay between fluid flow, heat transfer, chemical reactions, and porous media properties. Finally, ensuring the generalization and transferability of ML models across different scenarios and applications is a challenge that needs to be addressed. Energy storage and combustion systems using porous media can exhibit significant variations due to factors such as material properties, operating conditions, and system configurations.

Looking ahead, there are several exciting developments in the field of energy storage and combustion using porous media that are being facilitated by ML techniques. First, ML can greatly enhance the accuracy and optimization of these processes. Advanced algorithms such as deep learning and reinforcement learning can capture complex relationships and improve system performance. Secondly, by extracting valuable insights from large datasets, ML can help us better understand the intricate phenomena that occur within porous media. This understanding can then be used to improve materials, develop better system designs, and optimize operational strategies.

Thirdly, ML algorithms can enable real-time control and monitoring of energy storage and combustion systems, allowing for informed decisions and optimized performance. Fourthly, combining ML with experimental and computational methods can lead to more robust and reliable solutions. Finally, ML can also contribute to the development of safer and more sustainable energy storage and combustion systems by identifying potential risks and optimizing safety protocols. Overall, the future of energy storage and combustion using porous media aided by ML is bright. This technology can greatly improve system performance while advancing the adoption of sustainable energy technologies.

In the field of electrochemical devices, although ML has shown practical achievements, its application in porous media in electrochemical devices is still in its early stages, presenting several unexplored research prospects. There is ample opportunity for further advancements in the utilization of ML and DL to enhance the exploration of porous electrocatalysts for electrochemical devices. Additional efforts should be dedicated to advancing novel approaches that can enhance the efficiency and precision of ML in the identification of prospective porous electrocatalysts. Due to the intricate nature of the fuel cell system, current ML algorithms fall short of meeting the demands for both superior performance and cost-effectiveness. Consequently, there is a need for new ML methodologies to enhance the overall system performance. Supervised learning currently dominates the field of ML applications, requiring researchers to gather extensive sets of annotated data to train ML models. Whether obtained through resource-intensive high-throughput experiments or computationally demanding numerical simulations, the associated costs are significant. To tackle this challenge, new approaches need to be proposed. The integration of AI technologies is expected to enable the targeted design of porous media, provide guidance for experimental synthesis, validate predicted outcomes, and greatly advance the field of electrocatalysis.

Research into the manufacturing steps of LIBs, including electrolyte infiltration, formation, and electrochemical performance, continues to be a dynamic field where ML has demonstrated its potential. However, several challenges persist that necessitate further exploration and innovation. Notably, the robustness and adaptability of ML models for real-world applications need ongoing refinement and validation. These models must evolve to improve the accuracy of quantifying active material volume fractions, accommodate non-spherical particle morphologies, and address intricacies related to estimating the properties of actual electrodes, particularly in scenarios involving highly aligned platelets and high current densities. Bridging the gap between simulated and real microstructure data remains an important endeavor. To this end, the integration of additional data sources and the creation of accurate representations for reconstructed models are imperative. Furthermore, enhancing the computational efficiency of deep learning models for real-time battery management systems is paramount. As we look to the future, addressing these challenges will contribute to elevating the performance, longevity, and safety of LIBs across various applications.



Research in RFBs has made significant strides in optimizing various components, aided by the application of ML techniques. However, several challenges persist, and the path forward is marked by ongoing exploration and innovation. One critical challenge is the need for more realistic and manufacturable microstructures in electrode optimization. The assumptions made during microstructure generation, though helpful in discovering superior microstructures, may impact the practicality of their implementation. Future research should focus on bridging the gap between idealized designs and real-world manufacturability. Additionally, the generalizability of results in studies involving a limited number of simulations or small datasets needs to be addressed to ensure the applicability of findings to diverse scenarios. Furthermore, the characterization of electrode microstructure remains an essential aspect, and improvements in control and accuracy are vital for more precise estimations of specific surface area and porosity. In terms of future work, the optimization of manufacturing parameters, especially in designing porous materials for enhanced ion transport, remains a primary focus. ML offers the potential to revolutionize the design of porous materials to achieve specific transport characteristics. Moreover, the mechanical strength, heat transfer, and electron transfer properties of microstructures play pivotal roles in RFB performance. ML applications are well-suited to fine-tuning microstructure designs for improved strength, heat management, and electron transfer efficiency, thus advancing the overall capabilities of redox flow batteries.

ML techniques have been successfully applied to use existing literature data to optimize the properties of supercapacitor electrodes. Although there is still some scope for improvement in material performance by first creating accurate and valid physics-based models and then subsequently training neural networks on the performance metrics of those models to create fast surrogate-based models, these models should then be free of experimental error, noise, or inconsistency in experimental data reporting, allowing the microstructure of supercapacitor electrodes to be optimized. ML will likely be an invaluable tool for screening chemical compositions and structures for more durable cycle lifetimes and specific capacitance.

The oil and gas industry has always been at the forefront of technological advancements. With the advent of ML, the industry has been presented with new challenges that need to be addressed before ML can be fully integrated into the industry. One of the challenges of using ML in reservoir engineering is the lack of physical nature of ML algorithms. ML algorithms are data-driven and rely on finding patterns and correlations in data to make predictions. However, these algorithms do not inherently incorporate the underlying physical principles that govern the behavior of reservoirs. This can result in models that are not able to accurately capture the complex phenomena that occur in subsurface reservoirs. In contrast, traditional reservoir simulation models are based on physical equations that describe the flow of fluids through porous media. While these models can be computationally expensive and require a high level of expertise to develop and use, they can accurately capture the underlying physics of reservoir behavior. The lack of physical nature of ML

algorithms can result in models that are less accurate and less reliable than traditional simulation models. To address this challenge, it is suggested to work on developing hybrid approaches, such as PIML, that combine ML with traditional simulation methods. These approaches aim to leverage the strengths of both methods to develop more accurate and reliable models for reservoir engineering.

Data quality and quantity are other issues mentioned in previous research. ML algorithms rely on large amounts of high-quality data to make accurate predictions. Data quality refers to the accuracy and reliability of the data used to train machine learning models. In reservoir engineering, data are often collected from sensors and instruments that are deployed in the field. These sensors can be subject to various sources of error, such as measurement noise, calibration errors, and environmental interference. As a result, the data collected may not accurately reflect the true state of the reservoir. One way to improve data quality is by implementing rigorous data validation and cleaning processes to help identify and correct errors in the data. Furthermore, data is often collected at discrete points in time and space. This can result in sparse datasets that do not provide enough information to accurately capture the complex behavior of subsurface reservoirs. Using data augmentation techniques to produce synthetic data can increase data quantity. These techniques use existing data to generate new data that are similar but not identical to the original data. This can help enlarge the size of the dataset and enhance the accuracy of ML models.

Transfer learning has the potential to address some of the challenges associated with using ML in reservoir engineering, such as data scarcity. By leveraging knowledge gained from other reservoirs, transfer learning can help improve the accuracy and reliability of ML models in reservoir engineering. Transfer learning is an ML technique that allows the knowledge gained from one task to be applied to another related task. This can help enhance the performance of ML models when there is limited data available for the new task. Transfer learning could be used to apply knowledge gained from one reservoir to another similar reservoir. In other words, if a machine learning model has been trained on data from one reservoir to predict production rates, transfer learning could be used to apply this knowledge to another reservoir with similar characteristics. This could help enhance the accuracy of the model and lower the amount of data needed to train the model on the new reservoir. In a nutshell, solving ML challenges in hydrocarbon reservoirs requires a combination of domain expertise and technical skills in areas such as data science and reservoir engineering. By leveraging advanced analytics tools, it is possible to gain valuable insight into reservoir behavior that can help improve production and efficiency and reduce costs over time.

For carbon capture and sequestration, there are still certain obstacles to be overcome, despite the recent successes, for the field to reach new levels. Prospects would be illustrated for investigation in using ML to create porous materials, adsorption techniques, and carbon capture optimization, as well as potential solutions to these problems. Despite the feasible extraction of meaningful experimental data from the literature's



papers, the calculating techniques would result in a significant amount of information being lost. It is recommended that they be standardized in order to disseminate the technique, basic information, and outcomes more effectively in detail. A different recommendation is to digitize lab notes in ML-code formats for future research and extensive data communication. This approach would be helpful and extend the rapid expansion of materials science data communities. Large-scale, high-quality experimental and computational data are necessary for developing ML models that function robustly and generally. Getting enough data in the field of materials science, particularly for computational and experimental purposes, requires a cost impact. To deal with the lack of data, new approaches have been developed, such as transfer learning, data wrapping, augmentation, and dimension transformation. Traditionally, finding, gathering, and interpreting literature takes a lot of effort and time. Natural language processing (NLP) has recently made it feasible to automatically gather data for creating a materials database so that it can be more effectively incorporated into ML workflows for material design and experimental mechanization. Therefore, autonomous literature extraction of porous media for carbon capture using NLP will be an exciting approach. The last issue is that gathering experimental data is expensive because training ML models with adequate prediction accuracy often necessitates a large volume of data. To overcome the issues outlined above, researchers have recently begun to merge physics-based principles with ML models. These methods embed physical limitations, cutting-edge physics-based normalization, symmetries, invariances, and equivariants into ML models, which could improve generalizing, speed up training, and improve transparency. Advancements in materials research and adsorption/absorption process optimization for carbon capture are expected to be fueled by the field's research developments.

In the field of groundwater resources, modeling natural resources and water-related issues using ML is very popular. Based on the literature review for all aspects of water science, several items and steps significantly impact the modeling performance of ML models. These are data quality, length, splitting ratio, hyperparameter tuning, optimum input variables, hybridization/ensemble, and model prediction power (model structure). Also, in each literature review, authors stated that their models are robust and have high accuracy; therefore, selection of an optimum model is challenging. Data quality has a significant impact on other models (numerical, physically based, *etc.*) and has a meaningful effect on ML models. Involving poor-quality data can bring about degradation in the findings and have further consequences when decisions are made on those results. The length of the dataset is another important and influential factor in modeling prediction power. The larger the data, the higher the probability of extracting trends, and finally, the higher the prediction power of models.

ML models are attracting the interest of researchers, and their implementation is on the rise. The issue with ML models is that they need to consider the physics underlying catchment modeling, which must still be addressed. In addition, the implementation of need-based physical models and the vast

quantity of data persist. In certain situations, their integration is highly recommended, such as the prediction of missing data and the prediction of unavailable data (*e.g.*, inadequate data capture) or the prediction of some input parameters such as effective rainfall *via* Identification of unit Hydrographs and Component flows from Rainfall, Evaporation and Streamflow data (IHACRES) model and feed to ML models.

It is worth mentioning that for further knowledge and reading, a list of available online databases in the six fields of the review is given in Table S1 of the ESI,[†] which can be used as an exercise to train ML models with the relevant data given in these databases. Also, all the reviewed literature in the manuscript is displayed as spreadsheets containing relevant information on each of the references in the ESI.[†]

5. Conclusion

The review paper provided an overview of the present status quo of the interface of ML and porous media in six different applications, namely, heat exchanger and storage, energy storage and combustion, electrochemical devices, hydrocarbon reservoirs, CCS, and groundwater resources. A comprehensive elaboration of different ML models employed in the study of porous media such as supervised learning, unsupervised learning, and deep learning methods was carried out. Additionally, particular models that have been deployed, such as decision trees, random forests, support vector machines, and neural networks, followed by evaluation metrics, were noted. The advances made in the application of ML to porous media were stressed and insights into the challenges and opportunities for future research were offered. In the realm of heat transfer research, ML holds promise for predicting target functions and optimizing thermal systems through the extensive available data. Challenges arise in image processing systems due to limited comprehensive data for complex thermal systems, urging the deployment of accurate sensors and high-fidelity numerical simulations to enhance ML reliability. In energy storage and combustion, ML faces challenges such as limited data availability for various storage processes and combustion systems. PIML models are proposed to address complexities in material selection and reaction kinetics. Electrochemistry applications of ML are in the early stages, with opportunities for enhancing the exploration of porous electrocatalysts, and challenges include the need for new ML methodologies to improve fuel cell system performance. ML in hydrocarbon reservoirs encounters challenges due to its lack of inherent physical principles, supporting hybrid approaches such as PIML. CCS faces obstacles related to data standardization, digitization, and the cost impact of obtaining high-quality experimental data. In the groundwater resources framework, there are challenges and crucial considerations, including data quality and dataset length. It is concluded that the application of ML in a spectrum of fields holds promise for optimizing systems and processes, but it also faces challenges. These challenges include the need for high-quality data, addressing the lack of physical nature in ML algorithms, and finding ways to overcome data scarcity. Despite these obstacles, there is an opportunity to improve



accuracy and efficiency through hybrid approaches that combine ML with physics-based principles. The outlook for ML in these domains is optimistic, with a focus on enhancing precision, reliability, and sustainability, as well as addressing ongoing issues related to data quality and the integration of physical principles, contingent on continuous hardware processing development. Ongoing research and innovation are essential to harness the full potential of machine learning in these fields.

Abbreviations

AAPE	Average absolute percentage error	ERT	Extremely randomized tree
AC	Activated carbon	FFNN	Feed-forward neural network
ADLSTM	Adaptive dropout long short-term memory	FIB-SEM	Focused ion beam scanning electron microscopy
AE	Activation energy	FOV	Field-of-view
AEM	Anion exchange membrane	GA	Genetic algorithm
AHM	Automatic history matching	GAN	Generative adversarial network
AI	Artificial intelligence	GBDT	Gradient boosting decision tree
ANN	Artificial neural network	GBR	Gradient boosting regression
APS	Average pore size	GBM	Gradient boosting machine
ARM	Association rule mining	GCMC	Grand canonical Monte Carlo
ASL	Airway surface liquid	GDL	Gas diffusion layer
BET	Brunauer, Emmett, and Teller	GPR	Gaussian process regression
BiLSTM	Bidirectional long short-term memory	GRNN	Generalized regression neural network
BLR	Bayesian linear regression	GRU	Gated recurrent unit
BP	Back-propagation	HER	Hydrogen evolution reaction
BPNNs	Back propagation neural networks	HDPCs	Heteroatom-doped porous carbons
BRR	Bayesian ridge regression	HOLE	Highly ordered laser-patterned electrode
BWDPCs	Biomass waste-derived porous carbons	HPC	High-performance computing
CBM	Coalbed methane	HVAC	Heating, ventilation, and air conditioning
CCL	Cathode catalyst layer	IGWO	Improved gray wolf optimizer
CCS	Carbon capture and sequestration	IOR	Improved oil recovery
CCST	Carbon capture or separation technology	IPCC	Intergovernmental panel on climate change
CCSTU	Carbon capture, storage, transport, and utilization	KELM	Kernel extreme learning machines
CCUS	Carbon capture, utilization, and storage	KNN	k-Nearest neighbors
CFD	Computational fluid dynamics	KNR	k-Nearest neighbor regression
CGP	Cumulative gas production	LASSO	Least absolute shrinkage and selection operator
CHP	Combined heat and power	LBM	Lattice Boltzmann method
CL	Catalyst layer	LGB	Light gradient boosting
CNN	Convolutional neural network	LIBs	Lithium-ion batteries
COBYLA	Constrained optimization by linear approximation	LIME	Local interpretable model-agnostic explanations
COFs	Covalent organic frameworks	LINMAP	Linear programming technique for multidimensional analysis of preference
COP	Coefficient of performance	LM	Levenberg–Marquardt
CT	Computed tomography	LR	Linear regression
Da	Damkohler number	LSSVM	Least-squares support vector machine
DCA	Decline curve analysis	LSTM	Long short-term memory
DCGAN	Deep convolutional generative adversarial network	M&V	Monitoring and verification
DFT	Density functional theory	MAE	Mean absolute error
DL	Deep learning	MAPE	Mean absolute prediction error
DNN	Deep neural network	MC	Monte Carlo
DNS	Direct numerical simulation	MDDFs	Minimum distance distribution functions
DT	Decision tree	MFO	Moth-flame optimizer
DTR	Decision tree regression	MICE	Multivariate imputation by chained equations
ECPEM	Evaluation criterion of the proton exchange membrane	ML	Machine learning
EES	Electrochemical energy storage	MLP	Multi-layer perceptron
EOR	Enhanced oil recovery	MLR	Multi linear regression
		MLP-NN	Multi-layer perceptron neural network
		MMMs	Mixed matrix membranes
		MMP	Minimum miscible pressure
		MOF	Metal–organic framework
		MPV	Micropore volume
		MSE	Mean squared error
		NDCs	Nitrogen-doped catalysts
		NLP	Natural language processing
		NNP	Neural network potential
		NPV	Net present value
		NSGA	Non-dominating sorting genetic algorithm
		ODE	Ordinary differential equation
		OER	Oxygen evolution reaction



OMs	Open metal sites
ORR	Oxygen reduction reaction
PBI	Polybenzimidazole
PCA	Principal component analysis
PCM	Phase change material
PDE	Partial differential equation
PEC	Performance evaluation criteria
PEI	Polyethyleneimine
PEM	Proton exchange membrane
PEMFC	Proton exchange membrane fuel cell
PEMWE	Proton exchange membrane water electrolyzer
PIML	Physics-informed machine learning
PINN	Physics-informed neural network
PLS	Partial least squares
PNM	Pore network modeling
POD	Proper orthogonal decomposition and trajectory
TPWL	piecewise linearization
PSA	Pressure swing adsorption
PSO	Particle swarm optimization
PSPM	Pore-scale porous media
PTL	Porous transport layer
RBF	Radial basis function
REPT	Reduced error pruning trees
RF	Random forest
RFR	Random forest regression
RMSE	Root mean squared error
RNN	Recurrent neural network
ROM	Reduced order models
RPCs	Regular porous carbons
RSM	Response surface methodology
RUL	Remaining useful life
SACs	Single-atom catalysts
SBU	Secondary building units
SCG	Scaled conjugate gradient
SCR	Selective catalytic reduction
SDGs	Sustainable development goals
SHAP	Shapley additive explanations
SML	Supervised machine learning
SmVAE	Supramolecular variational autoencoder
SoC	State-of-charge
SOFCs	Solid oxide fuel cells
SoH	State-of-health
SOM	Self-organizing map
SPC	Straw pyrolytic carbon
SRM	Surrogate reservoir model
SSA	Specific surface area
SVM	Support vector machine
SVR	Support vector regression
TCES	Thermochemical energy storage
TEPA	Tetraethylenepentamine
TES	Thermal energy storage
TOC	Total organic carbon
TOPSIS	Technique for order of preference by similarity to ideal solution
TSA	Temperature swing adsorption
VE	Voltage efficiency
VSA	Vacuum swing adsorption
XGBoost	Extreme gradient boosting

Author contributions

Writing – original draft: 1. Introduction: M.D.; 2. Background on machine learning and porous media: S. M. A & H. Y.; 3.1. Heat exchanger and storage: A. F.; 3.2. Energy storage and combustion: B. E.; 3.3. Electrochemical devices: M. G., J. S., & D. N.; 3.4. Hydrocarbon reservoirs: M. S. & H. M.; 3.5. Carbon capture and sequestration: H. M., M. A. A., & A. E.; 3.6. Groundwater: K. K. & S. R. Writing – review & editing: M. D., B. E., V. N. & M. M. Funding acquisition: M. D. & M. M. Conceptualization, methodology, supervision, & project administration: M. D.

Conflicts of interest

The authors declare there are no conflicts of interest.

Acknowledgements

The authors would like to acknowledge the UK Engineering and Physical Sciences Research Council (EPSRC) Project through the project number EP/W005204/1.

References

- Z. Niu, V. J. Pinfield, B. Wu, H. Wang, K. Jiao, D. Y. C. Leung and J. Xuan, *Energy Environ. Sci.*, 2021, **14**, 2549–2576.
- S. M. Moosavi, B. Á. Novotny, D. Ongari, E. Moubarak, M. Asgari, Ö. Kadioglu, C. Charalambous, A. Ortega-Guerrero, A. H. Farmahini, L. Sarkisov, S. Garcia, F. Noé and B. Smit, *Nat. Mater.*, 2022, **21**, 1419–1425.
- K. M. Jablonka, D. Ongari, S. M. Moosavi and B. Smit, *Chem. Rev.*, 2020, **120**, 8066–8129.
- N. Heinemann, J. Alcalde, J. M. Miocic, S. J. T. Hangx, J. Kallmeyer, C. Ostertag-Henning, A. Hassanpouryouzband, E. M. Thaysen, G. J. Strobel, C. Schmidt-Hattenberger, K. Edlmann, M. Wilkinson, M. Benthams, R. Stuart Haszeldine, R. Carbonell and A. Rudloff, *Energy Environ. Sci.*, 2021, **14**, 853–864.
- Y. Wang, Y. Pang, H. Xu, A. Martinez and K. S. Chen, *Energy Environ. Sci.*, 2022, **15**, 2288–2328.
- M. Bastos-Neto, C. Patzschke, M. Lange, J. Möllmer, A. Möller, S. Fichtner, C. Schrage, D. Lässig, J. Lincke, R. Staudt, H. Krautscheid and R. Gläser, *Energy Environ. Sci.*, 2012, **5**, 8294–8303.
- L. Bu, F. Ning, J. Zhou, C. Zhan, M. Sun, L. Li, Y. Zhu, Z. Hu, Q. Shao, X. Zhou, B. Huang and X. Huang, *Energy Environ. Sci.*, 2022, **15**, 3877–3890.
- P. P. Mukherjee, Q. Kang and C. Y. Wang, *Energy Environ. Sci.*, 2011, **4**, 346–369.
- S. Haussener, C. Xiang, J. M. Spurgeon, S. Ardo, N. S. Lewis and A. Z. Weber, *Energy Environ. Sci.*, 2012, **5**, 9922–9935.
- X. Lu, T. Li, A. Bertei, J. I. S. Cho, T. M. M. Heenan, M. F. Rabuni, K. Li, D. J. L. Brett and P. R. Shearing, *Energy Environ. Sci.*, 2018, **11**, 2390–2403.
- Q. Lyu, J. Tan, L. Li, Y. Ju, A. Busch, D. A. Wood, P. G. Ranjith, R. Middleton, B. Shu, C. Hu, Z. Wang and R. Hu, *Energy Environ. Sci.*, 2021, **14**, 4203–4227.



- 12 F. M. Orr, *Energy Environ. Sci.*, 2009, **2**, 449–458.
- 13 S. L. Candelaria, R. Chen, Y. H. Jeong and G. Cao, *Energy Environ. Sci.*, 2012, **5**, 5619–5637.
- 14 R. S. Middleton, G. N. Keating, P. H. Stauffer, A. B. Jordan, H. S. Viswanathan, Q. J. Kang, J. W. Carey, M. L. Mulkey, E. J. Sullivan, S. P. Chu, R. Esposito and T. A. Meckel, *Energy Environ. Sci.*, 2012, **5**, 7328–7345.
- 15 Y. Yan, T. N. Borhani, S. G. Subraveti, K. N. Pai, V. Prasad, A. Rajendran, P. Nkulikiyinka, J. O. Asibor, Z. Zhang, D. Shao, L. Wang, W. Zhang, Y. Yan, W. Ampomah, J. You, M. Wang, E. J. Anthony, V. Manovic and P. T. Clough, *Energy Environ. Sci.*, 2021, **14**, 6122–6157.
- 16 W. Zhi, D. Feng, W.-P. Tsai, G. Sterle, A. Harpold, C. Shen and L. Li, *Environ. Sci. Technol.*, 2021, **55**, 2357–2368.
- 17 A. M. Norouzi, M. Babaei, W. S. Han, K. Y. Kim and V. Niasar, *Chem. Eng. J.*, 2021, **425**, 130031.
- 18 L. Hashemi, M. Blunt and H. Hajibeygi, *Sci. Rep.*, 2021, **11**, 8348.
- 19 S. Caré, R. Crane, P. S. Calabrò, A. Ghauch, E. Temgoua and C. Noubactep, *Clean*, 2013, **41**, 275–282.
- 20 Md. S. Hossain, L. I. Stephens, M. Hatami, M. Ghavidel, D. Chhin, J. I. G. Dawkins, L. Savignac, J. Mauzeroll and S. B. Schougaard, *ACS Appl. Energy Mater.*, 2020, **3**, 440–446.
- 21 J. Lin, Z. Liu, Y. Guo, S. Wang, Z. Tao, X. Xue, R. Li, S. Feng, L. Wang, J. Liu, H. Gao, G. Wang and Y. Su, *Nano Today*, 2023, **49**, 101802.
- 22 T. Yasuda, S. Ookawara, S. Yoshikawa and H. Matsumoto, *Chem. Eng. J.*, 2023, **453**, 139540.
- 23 D. A. Nield and A. Bejan, in *Convection in Porous Media*, Springer International Publishing, Cham, 2017, pp. 1–35.
- 24 N. Nishiyama and T. Yokoyama, *J. Geophys. Res.: Solid Earth*, 2017, **122**, 6955–6971.
- 25 J. M. McKinley, *Encyclopedia of Mathematical Geosciences: Encyclopedia of Earth Sciences Series*, ed. B. S. Daya Sagar, Q. Cheng, J. McKinley and F. Agterberg, 2022, pp. 1–3.
- 26 C. Wang, Y. Mehmani and K. Xu, *Proc. Natl. Acad. Sci. U. S. A.*, 2021, **118**, DOI: [10.1073/pnas.2024069118](https://doi.org/10.1073/pnas.2024069118).
- 27 S. Bakhshian, Z. Shi, M. Sahimi, T. T. Tsotsis and K. Jessen, *Sci. Rep.*, 2018, **8**, 8249.
- 28 S. Fagbemi, P. Tahmasebi and M. Piri, *Water Resour. Res.*, 2018, **54**, 6336–6356.
- 29 M. E. Rosti, S. Pramanik, L. Brandt and D. Mitra, *Soft Matter*, 2020, **16**, 939–944.
- 30 M. Kohr and G. P. R. Sekhar, *Eng. Anal. Bound. Elem.*, 2007, **31**, 604–613.
- 31 A. Lenci, F. Zeighami and V. Di Federico, *Transp. Porous Media*, 2022, **144**, 459–480.
- 32 K.-K. Phoon, T.-S. Tan and P.-C. Chong, *Geotech. Geol. Eng.*, 2007, **25**, 525–541.
- 33 Y. Da Wang, T. Chung, R. T. Armstrong and P. Mostaghimi, *Transp. Porous Media*, 2021, **138**, 49–75.
- 34 M. R. M. Talabis, R. McPherson, I. Miyamoto, J. L. Martin and D. Kaye, in *Information Security Analytics*, Elsevier, 2015, pp. 1–12.
- 35 H. Huo, Z. Rong, O. Kononova, W. Sun, T. Botari, T. He, V. Tshitoyan and G. Ceder, *npj Comput. Mater.*, 2019, **5**, 62.
- 36 K. M. Jablonka, D. Ongari, S. M. Moosavi and B. Smit, *Chem. Rev.*, 2020, **120**, 8066–8129.
- 37 J. Abdi, F. Hadavimoghaddam, M. Hadipoor and A. Hemmati-Sarapardeh, *Sci. Rep.*, 2021, **11**, 24468.
- 38 A. Banerjee, S. Pasupuleti, K. Mondal and M. M. Nezhad, *Int. J. Heat Mass Transfer*, 2021, **179**, 121650.
- 39 D. Thakur, A. Chandel and V. Shankar, *Water Pract. Technol.*, 2022, **17**, 2625–2638.
- 40 S. M. Alirahmi, S. F. Mousavi, P. Ahmadi and A. Arabkoohsar, *Energy*, 2021, **236**, 121412.
- 41 A. C. Cinar, *Arabian J. Sci. Eng.*, 2020, **45**, 10915–10938.
- 42 S. M. Alirahmi and A. Ebrahimi-Moghadam, *Appl. Energy*, 2022, **323**, 119545.
- 43 K. Kim, W. H. Lee, J. Na, Y. J. Hwang, H. S. Oh and U. Lee, *J. Mater. Chem. A*, 2020, **8**, 16943–16950.
- 44 R. Ding, Y. Ding, H. Zhang, R. Wang, Z. Xu, Y. Liu, W. Yin, J. Wang, J. Li and J. Liu, *J. Mater. Chem. A*, 2021, **9**, 6841–6850.
- 45 Ş. Neaţu, F. Neaţu, I. M. Chirica, I. Borbáth, E. Tálas, A. Tompos, S. Somacescu, P. Osiceanu, M. A. Folgado, A. M. Chaparro and M. Florea, *J. Mater. Chem. A*, 2021, **9**, 17065–17128.
- 46 S. Jha, M. Yen, Y. S. Salinas, E. Palmer, J. Villafuerte and H. Liang, *J. Mater. Chem. A*, 2023, **11**, 3904–3936.
- 47 N. Zobeiry and K. D. Humfeld, *Eng. Appl. Artif. Intell.*, 2021, **101**, 104232.
- 48 S. Keykhah, E. Assareh, R. Moltames, M. Izadi and H. M. Ali, *Phys. A*, 2020, **545**, 123804.
- 49 F. Selimefendigil, S. O. Coban and H. F. Öztöp, *Int. J. Therm. Sci.*, 2022, **172**, 107286.
- 50 N. A. Khan, M. Sulaiman and F. S. Alshammari, *Struct. Multidisc. Optim.*, 2022, **65**, 1–14.
- 51 Y. Ge, Z. Liu and W. Liu, *Int. J. Heat Mass Transfer*, 2016, **101**, 981–987.
- 52 Z. I. Butt, I. Ahmad, H. Ilyas, M. Shoaib and M. A. Z. Raja, *Int. J. Hydrogen Energy*, 2023, **48**, 16100–16131.
- 53 I. Ahmad, H. Zahid, F. Ahmad, M. A. Z. Raja and D. Baleanu, *Chin. J. Phys.*, 2019, **59**, 641–655.
- 54 Y. Su, T. Ng, Z. Li and J. H. Davidson, *Chem. Eng. J.*, 2020, **397**, 125257.
- 55 M. A. Z. Raja, M. Shoaib, Z. Khan, S. Zuhra, C. A. Saleel, K. S. Nisar, S. Islam and I. Khan, *Ain Shams Eng. J.*, 2022, **13**, 101573.
- 56 I. Ahmad, H. Ilyas, M. A. Z. Raja, Z. Khan and M. Shoaib, *Surf. Interfaces*, 2021, **26**, 101403.
- 57 U. Sajjad, I. Hussain, K. Hamid, S. A. Bhat, H. M. Ali and C. C. Wang, *J. Therm. Anal. Calorim.*, 2021, **145**, 1911–1923.
- 58 M. Singh, R. Ragoju, G. Shiva Kumar Reddy and C. Subramani, *Phys. Fluids*, 2023, **35**, 34103.
- 59 H. Pourrahmani, M. Moghimi, M. Siavashi and M. Shirbani, *Appl. Therm. Eng.*, 2019, **150**, 433–444.
- 60 R. Alizadeh, J. M. N. Abad, A. Ameri, M. R. Mohebbi, A. Mehdizadeh, D. Zhao and N. Karimi, *J. Taiwan Inst. Chem. Eng.*, 2021, **124**, 290–306.
- 61 M. Alhadri, J. Raza, U. Yashkun, L. A. Lund, C. Maatki, S. U. Khan and L. Kolsi, *J. Indian Chem. Soc.*, 2022, **99**, 100607.



- 62 J. Mohebbi Najm Abad, R. Alizadeh, A. Fattahi, M. H. Doranehgard, E. Alhajri and N. Karimi, *J. Mol. Liq.*, 2020, **313**, 113492.
- 63 M. M. Rajabi, M. R. Hajizadeh Javaran, A. oury Bah, G. Frey, F. Le Ber, F. Lehmann and M. Fahs, *Int. J. Heat Mass Transfer*, 2022, **183**, 122131.
- 64 R. A. Khan, H. Ullah, M. A. Z. Raja, M. A. R. Khan, S. Islam and M. Shoaib, *Int. Commun. Heat Mass Transfer*, 2021, **126**, 105436.
- 65 B. Yang, X. Zhu, B. Wei, M. Liu, Y. Li, Z. Lv and F. Wang, *Energies*, 2023, **16**, 1500.
- 66 M. Siavashi, H. R. Talesh Bahrami and E. Aminian, *Appl. Therm. Eng.*, 2018, **138**, 465–474.
- 67 J. H. Meng, Y. Liu, X. H. Zhu, Z. J. Yang, K. Zhang and G. Lu, *Energy Convers. Manage.*, 2022, **273**, 116404.
- 68 H. R. Abbasi, E. Sharifi Sedeh, H. Pourrahmani and M. H. Mohammadi, *Appl. Therm. Eng.*, 2020, **180**, 115835.
- 69 T. S. Athith, G. Trilok, P. H. Jadhav and N. Gnanasekaran, *Mater. Today: Proc.*, 2022, **51**, 1642–1648.
- 70 S. Chen, J. Mao, F. Chen, P. Hou and Y. Li, *Int. J. Heat Mass Transfer*, 2018, **117**, 617–626.
- 71 Z. J. Zheng, M. J. Li and Y. L. He, *Int. J. Heat Mass Transfer*, 2015, **87**, 376–379.
- 72 M. H. Mohammadi, H. R. Abbasi, A. Yavarinasab and H. Pourrahmani, *Appl. Therm. Eng.*, 2020, **170**, 115005.
- 73 G. Baiocco, V. Tagliaferri and N. Ucciardello, *Procedia CIRP*, 2017, **62**, 518–522.
- 74 T. Deshamukhya, D. Bhanja, S. Nath and S. A. Hazarika, *J. Mech. Sci. Technol.*, 2018, **32**, 4495–4502.
- 75 T. H. Wang, H. C. Wu, J. H. Meng and W. M. Yan, *Int. J. Heat Mass Transfer*, 2020, **149**, 119217.
- 76 Ö. Bayer, S. Baghaei Oskouei and S. Aradag, *Int. Commun. Heat Mass Transfer*, 2022, **134**, 105984.
- 77 R. Khosravi, M. Zamaemifard, S. Safarzadeh, M. Passandideh-Fard, A. R. Teymourash and A. Shahsavari, *Eng. Anal. Bound. Elem.*, 2023, **150**, 259–271.
- 78 H. K. Ghritlahre and R. K. Prasad, *Therm. Sci. Eng. Prog.*, 2018, **6**, 226–235.
- 79 S. Du, Y. L. He, W. W. Yang and Z. Bin Liu, *Int. J. Heat Mass Transfer*, 2018, **122**, 383–390.
- 80 Z. J. Zheng, Y. Xu and Y. L. He, *Sci. China: Technol. Sci.*, 2016, **59**, 1475–1485.
- 81 F. Hosseini and M. Siavashi, *Sol. Energy*, 2021, **230**, 208–221.
- 82 A. Grosjean, A. Soum-Glaude, P. Neveu and L. Thomas, *Sol. Energy Mater. Sol. Cells*, 2018, **182**, 166–177.
- 83 S. Du, T. Xia, Y. L. He, Z. Y. Li, D. Li and X. Q. Xie, *Appl. Energy*, 2020, **275**, 115343.
- 84 H. K. Ghritlahre and R. K. Prasad, *Energy Procedia*, 2017, **109**, 369–376.
- 85 A. Li, A. C. Y. Yuen, W. Wang, T. B. Y. Chen, C. S. Lai, W. Yang, W. Wu, Q. N. Chan, S. Kook and G. H. Yeoh, *Batteries*, 2022, **8**, 69.
- 86 J. Duan and F. Li, *J. Energy Storage*, 2021, **33**, 102160.
- 87 A. Tikadar and S. Kumar, *Int. J. Heat Mass Transfer*, 2022, **199**, 123438.
- 88 H. Ilyas, I. Ahmad, M. A. Z. Raja, M. B. Tahir and M. Shoaib, *Int. J. Hydrogen Energy*, 2021, **46**, 28298–28326.
- 89 Z. I. Butt, I. Ahmad, M. Shoaib, H. Ilyas and M. A. Z. Raja, *Int. Commun. Heat Mass Transfer*, 2023, **140**, 106516.
- 90 N. Bianco, M. Iasiello, G. M. Mauro and L. Pagano, *Appl. Therm. Eng.*, 2021, **182**, 116058.
- 91 T. Deshamukhya, D. Bhanja and S. Nath, *Neural Comput. Appl.*, 2021, **33**, 12605–12619.
- 92 S. Dathathri and C. Balaji, *Int. Commun. Heat Mass Transfer*, 2015, **60**, 32–36.
- 93 M. Shoaib, T. Rafia, M. A. Z. Raja, W. A. Khan and M. Waqas, *J. Braz. Soc. Mech. Sci. Eng.*, 2022, **44**, 1–21.
- 94 C. Yang, Y. Xu, X. Cai and Z. J. Zheng, *Int. J. Heat Mass Transfer*, 2022, **196**, 123309.
- 95 W. Cui, T. Si, X. Li, X. Li, L. Lu, T. Ma and Q. Wang, *Energy Reports*, 2022, **8**, 10203–10218.
- 96 K. Anand, A. Bhardwaj, S. Chaudhuri and V. K. Mishra, *Arabian J. Sci. Eng.*, 2022, **47**, 15175–15194.
- 97 N. Alqahtani, F. Alzubaidi, R. T. Armstrong, P. Swietojanski and P. Mostaghimi, *J. Pet. Sci. Eng.*, 2020, **184**, 106514.
- 98 A. Eghtesad, F. Tabassum and S. Hajimirza, *Int. J. Heat Mass Transfer*, 2023, **205**, 123890.
- 99 H. Wei, H. Bao and X. Ruan, *Int. J. Heat Mass Transfer*, 2020, **160**, 120176.
- 100 V. K. Mishra, S. C. Mishra and D. N. Basu, *Numer. Heat Transfer, Part A*, 2017, **71**, 677–692.
- 101 R. Singh, R. S. Bhoopal and S. Kumar, *Build. Environ.*, 2011, **46**, 2603–2608.
- 102 M. Laimon, T. Yusaf, T. Mai, S. Goh and W. Alrefae, *Int. J. Thermofluids*, 2022, **15**, 100161.
- 103 B. Ebrahimpour and M. Behshad Shafii, *Sol. Energy*, 2022, **247**, 453–467.
- 104 A. G. Olabi, C. Onumaegbu, T. Wilberforce, M. Ramadan, M. A. Abdelkareem and A. H. Al-Alami, *Energy*, 2021, **214**, 118987.
- 105 D. Ranjan Parida, N. Dani and S. Basu, *Sol. Energy*, 2021, **227**, 447–456.
- 106 Y. Liu, B. Guo, X. Zou, Y. Li and S. Shi, *Energy Storage Mater.*, 2020, **31**, 434–450.
- 107 A. Gopalan, B. J. Bucior, N. S. Bobbitt and R. Q. Snurr, *Mol. Phys.*, 2019, **117**, 3683–3694.
- 108 Z. Wen, P. Fang, Y. Yin, G. Królczyk, P. Gardoni and Z. Li, *J. Energy Storage*, 2022, **49**, 104072.
- 109 G. Yan, B. Teng, D. H. Elkamchouchi, T. Alkhalifah, F. Alturise, M. Amine Khadimallah and H. E. Ali, *Fuel*, 2023, **348**, 128253.
- 110 P. Roy, L. Rekhi, S. W. Koh, H. Li and T. S. Choksi, *J. Phys.: Energy*, 2023, **5**, 034005.
- 111 A. Rabbani, M. Babaei, R. Shams, Y. Da Wang and T. Chung, *Adv. Water Resour.*, 2020, **146**, 103787.
- 112 A. Chen, X. Zhang and Z. Zhou, *InfoMat*, 2020, **2**, 553–576.
- 113 L. Abualigah, R. A. Zitar, K. H. Almotairi, A. M. Hussein, M. A. Elaziz, M. R. Nikoo and A. H. Gandomi, *Energies*, 2022, **15**, 578.
- 114 G. Anderson, B. Schweitzer, R. Anderson and D. A. Gómez-Gualdrón, *J. Phys. Chem. C*, 2019, **123**, 120–130.
- 115 A. Ahmed and D. J. Siegel, *Patterns*, 2021, **2**, 100291.



- 116 P. Roy, L. Rekhi, S. W. Koh, H. Li and T. S. Choksi, *J. Phys.: Energy*, 2023, **5**, 034005.
- 117 D. Kaya, D. Koroglu, E. Aydin and B. Uralcan, *J. Power Sources*, 2023, **568**, 232987.
- 118 Y. Liu, B. Guo, X. Zou, Y. Li and S. Shi, *Energy Storage Mater.*, 2020, **31**, 434–450.
- 119 J. G. T. Tomacruz, K. E. S. Pilario, M. F. M. Remolona, A. A. B. Padama and J. D. Ocon, *Chem. Eng. Trans.*, 2022, **94**, 733–738.
- 120 T. Saboori, L. Zhao, M. Mesgarpour, S. Wongwises and O. Mahian, *J. Build. Eng.*, 2022, **54**, 104505.
- 121 A. Shodiev, M. Duquesnoy, O. Arcelus, M. Chouchane, J. Li and A. A. Franco, *J. Power Sources*, 2021, **511**, 230384.
- 122 M. Rahimi, M. H. Abbaspour-Fard and A. Rohani, *J. Power Sources*, 2022, **521**, 230968.
- 123 M. Witman, S. Ling, D. M. Grant, G. S. Walker, S. Agarwal, V. Stavila and M. D. Allendorf, *J. Phys. Chem. Lett.*, 2020, **11**, 40–47.
- 124 A. Shahsavari, A. Goodarzi, I. Baniasad Askari, M. Jamei, M. Karbasi and M. Afrand, *Eng. Anal. Bound. Elem.*, 2022, **140**, 432–446.
- 125 M. Pournali and J. A. Esfahani, *Energy*, 2022, **255**, 124553.
- 126 M. M. A. Khan, N. I. Ibrahim, I. M. Mahbubul, H. M. Ali, R. Saidur and F. A. Al-Sulaiman, *Sol. Energy*, 2018, **166**, 334–350.
- 127 L. Miró, J. Gasia and L. F. Cabeza, *Appl. Energy*, 2016, **179**, 284–301.
- 128 B. Liu, G. Lv, T. Liu, M. Liu, J. Bian, Q. Sun and L. Liao, *J. Mater. Chem. A*, 2024, **12**, 8663–8682.
- 129 K. Swaminathan Gopalan and V. Eswaran, *Int. J. Therm. Sci.*, 2016, **104**, 266–280.
- 130 F. Selimefendigil and H. F. Öztop, *J. Taiwan Inst. Chem. Eng.*, 2021, **124**, 381–390.
- 131 N. Tonekaboni, M. Feizbahr, N. Tonekaboni, G. J. Jiang and H. X. Chen, *Math. Probl. Eng.*, 2021, **2021**, 9984840.
- 132 D. Skrobek, J. Krzywanski, M. Sosnowski, A. Kulakowska, A. Zylka, K. Grabowska, K. Ciesielska and W. Nowak, *Adv. Eng. Softw.*, 2022, **173**, 103190.
- 133 Z. Shi, H. Liang, W. Yang, J. Liu, Z. Liu and Z. Qiao, *Chem. Eng. Sci.*, 2020, **214**, 115430.
- 134 A. Malley-Ernewein and S. Lorente, *Int. J. Heat Mass Transfer*, 2020, **158**, 119975.
- 135 X. Chen, Z. Dong, L. Zhu and X. Ling, *Renewable Energy*, 2023, **205**, 340–348.
- 136 T. Praditia, T. Walser, S. Oladshkin and W. Nowak, *Energies*, 2020, **13**, 3873.
- 137 S. Tasneem, H. S. Sultan, A. A. Ageeli, H. Togun, W. M. Alamier, N. Hasan and M. R. Safaei, *J. Taiwan Inst. Chem. Eng.*, 2023, 104926.
- 138 L. Mao, X. Zhao, H. Wang, H. Xu, L. Xie, C. Zhao and L. Chen, *Chem. Rec.*, 2020, **20**, 922–935.
- 139 A. Shodiev, M. Duquesnoy, O. Arcelus, M. Chouchane, J. Li and A. A. Franco, *J. Power Sources*, 2021, **511**, 230384.
- 140 H. Chun, J. Kim and S. Han, in *IFAC-PapersOnLine*, Elsevier B.V., 2019, vol. 52, pp. 129–134.
- 141 M. Shi, J. Yuan, L. Dong, D. Zhang, A. Li and J. Zhang, *Electrochim. Acta*, 2020, **353**, 136567.
- 142 F. Wang, X. Li, J. Tan, X. Hao and B. Xiong, *Int. J. Heat Mass Transfer*, 2022, **183**, 122085.
- 143 G. Cho, M. Wang, Y. Kim, J. Kwon and W. Su, *IEEE Access*, 2022, **10**, 88117–88126.
- 144 E. Galiounas, T. G. Tranter, R. E. Owen, J. B. Robinson, P. R. Shearing and D. J. L. Brett, *Energy AI*, 2022, **10**, 100188.
- 145 H. Xu, J. Zhu, D. P. Finegan, H. Zhao, X. Lu, W. Li, N. Hoffman, A. Bertei, P. Shearing and M. Z. Bazant, *Adv. Energy Mater.*, 2021, **11**, 2003908.
- 146 A. Aitio and D. A. Howey, *Joule*, 2021, **5**, 3204–3220.
- 147 M. Boujelbene, M. Goodarzi, M. A. Ali, I. M. T. A. Shigidi, R. A. Pashameah, R. Z. Homod, E. Alzahrani and M. R. Safaei, *J. Energy Storage*, 2023, **58**, 106331.
- 148 S. Ishikawa, X. Liu, T. H. Noh, M. So, K. Park, N. Kimura, G. Inoue and Y. Tsuge, *J. Power Sources Adv.*, 2022, **15**, 100094.
- 149 R. M. Weber, S. Korneev and I. Battiato, *Transp. Porous Media*, 2022, **145**, 527–548.
- 150 Z. Jiang, J. Li, Y. Yang, L. Mu, C. Wei, X. Yu, P. Pianetta, K. Zhao, P. Cloetens, F. Lin and Y. Liu, *Nat. Commun.*, 2020, **11**, 2310.
- 151 A. González, E. Goikolea, J. A. Barrena and R. Mysyk, *Renewable Sustainable Energy Rev.*, 2016, **58**, 1189–1206.
- 152 S. Nanda, S. Ghosh and T. Thomas, *J. Power Sources*, 2022, **546**, 231975.
- 153 J. Wang, X. Zhang, Z. Li, Y. Ma and L. Ma, *J. Power Sources*, 2020, **451**, 227794.
- 154 A. G. Saad, A. Emad-Eldeen, W. Z. Tawfik and A. G. El-Deen, *J. Energy Storage*, 2022, **55**, 105411.
- 155 S. Ghosh, G. R. Rao and T. Thomas, *Energy Storage Mater.*, 2021, **40**, 426–438.
- 156 X. Lu, P. Liu, K. Bisetty, Y. Cai, X. Duan, Y. Wen, Y. Zhu, L. Rao, Q. Xu and J. Xu, *J. Electroanal. Chem.*, 2022, **920**, 116634.
- 157 W. C. Tan, L. H. Saw, H. S. Thiam, J. Xuan, Z. Cai and M. C. Yew, *Renewable Sustainable Energy Rev.*, 2018, **96**, 181–197.
- 158 R. Ding, S. Zhang, Y. Chen, Z. Rui, K. Hua, Y. Wu, X. Li, X. Duan, X. Wang, J. Li and J. Liu, *Energy AI*, 2022, **9**, 100170.
- 159 G. Zhang, L. Wu, K. Jiao, P. Tian, B. Wang, Y. Wang and Z. Liu, *Energy Convers. Manage.*, 2020, **226**, 113513.
- 160 X. Liu, K. Park, M. So, S. Ishikawa, T. Terao, K. Shinohara, C. Komori, N. Kimura, G. Inoue and Y. Tsuge, *J. Power Sources Adv.*, 2022, **14**, 100084.
- 161 F. Zhang, P. Zhao, M. Niu and J. Maddy, *Int. J. Hydrogen Energy*, 2016, **41**, 14535–14552.
- 162 E. M. Thaysen, S. McMahon, G. J. Strobel, I. B. Butler, B. T. Ngwenya, N. Heinemann, M. Wilkinson, A. Hassanpouryouzband, C. I. McDermott and K. Edlmann, *Renewable Sustainable Energy Rev.*, 2021, **151**, 111481.
- 163 T. Hai, F. A. Alenizi, A. H. Mohammed, B. S. Chauhan, B. Al-Qargholi, A. S. M. Metwally and M. Ullah, *Int. Commun. Heat Mass Transfer*, 2023, **145**, 106848.
- 164 G. Anderson, B. Schweitzer, R. Anderson and D. A. Gómez-Gualdrón, *J. Phys. Chem. C*, 2019, **123**, 120–130.



- 165 A. Gopalan, B. J. Bucior, N. S. Bobbitt and R. Q. Snurr, *Mol. Phys.*, 2019, **117**, 3683–3694.
- 166 B. J. Bucior, N. S. Bobbitt, T. Islamoglu, S. Goswami, A. Gopalan, T. Yildirim, O. K. Farha, N. Bagheri and R. Q. Snurr, *Mol. Syst. Des. Eng.*, 2019, **4**, 162–174.
- 167 M. Rahimi, M. H. Abbaspour-Fard and A. Rohani, *J. Cleaner Prod.*, 2021, **329**, 129714.
- 168 D. P. Dubal, O. Ayyad, V. Ruiz and P. Gómez-Romero, *Chem. Soc. Rev.*, 2015, **44**, 1777–1790.
- 169 F. Zhang, T. Zhang, X. Yang, L. Zhang, K. Leng, Y. Huang and Y. Chen, *Energy Environ. Sci.*, 2013, **6**, 1623–1632.
- 170 T. Gao and W. Lu, *iScience*, 2021, **24**, 101936.
- 171 N. Variji, M. Siavashi, M. Tahmasbi and M. Bidabadi, *J. Energy Storage*, 2022, **50**, 104690.
- 172 M. M. Heyhat, S. Mousavi and M. Siavashi, *J. Energy Storage*, 2020, **28**, 101235.
- 173 M. Boujelbene, M. Goodarzi, M. A. Ali, I. M. T. A. Shigidi, R. A. Pashameah, R. Z. Homod, E. Alzahrani and M. R. Safaei, *J. Energy Storage*, 2023, **58**, 106331.
- 174 M. Krishnamoorthi, R. Malayalamurthi, Z. He and S. Kandasamy, *Renewable Sustainable Energy Rev.*, 2019, **116**, 109404.
- 175 W. Jiang, X. Xing, X. Zhang and M. Mi, *Renewable Energy*, 2019, **130**, 1216–1225.
- 176 A. Banerjee and D. Paul, *Energy*, 2021, **221**, 119868.
- 177 L. Zhou, Y. Song, W. Ji and H. Wei, *Energy AI*, 2022, **7**, 100128.
- 178 H. Mai, T. C. Le, D. Chen, D. A. Winkler and R. A. Caruso, *Chem. Rev.*, 2022, **122**, 13478–13515.
- 179 A. Mistry, A. A. Franco, S. J. Cooper, S. A. Roberts and V. Viswanathan, *ACS Energy Lett.*, 2021, **6**, 1422–1431.
- 180 C. Song, S. Lee, B. Gu, I. Chang, G. Y. Cho, J. D. Baek and S. W. Cha, *Energies*, 2020, **13**, 1621.
- 181 P. Satjaritanun, M. O'Brien, D. Kulkarni, S. Shimpalee, C. Capuano, K. E. Ayers, N. Danilovic, D. Y. Parkinson and I. V. Zenyuk, *iScience*, 2020, **23**, 101783.
- 182 A. M. Nassef, A. Fathy, E. T. Sayed, M. A. Abdelkareem, H. Rezk, W. H. Tanveer and A. G. Olabi, *Renewable Energy*, 2019, **138**, 458–464.
- 183 B. Wang, B. Xie, J. Xuan and K. Jiao, *Energy Convers. Manage.*, 2020, **205**, 112460.
- 184 S. N. Steinmann, Q. Wang and Z. W. Seh, *Mater. Horiz.*, 2023, **10**, 393–406.
- 185 W. Xia, Z. Hou, J. Tang, J. Li, W. Chaikittisilp, Y. Kim, K. Muraoka, H. Zhang, J. He, B. Han and Y. Yamauchi, *Nano Energy*, 2022, **94**, 106868.
- 186 W. Zhou, L. Yang, X. Wang, W. Zhao, J. Yang, D. Zhai, L. Sun and W. Deng, *JACS Au*, 2021, **1**, 1497–1505.
- 187 E. O. Ebikade, Y. Wang, N. Samulewicz, B. Hasa and D. Vlachos, *React. Chem. Eng.*, 2020, **5**, 2134–2147.
- 188 A. Zheng, Y. Wang, F. Zhang, C. He, S. Zhu and N. Zhao, *iScience*, 2021, **24**, 103430.
- 189 M. Pourali, J. A. Esfahani, H. Jahangir, A. Farzaneh and K. C. Kim, *J. Energy Storage*, 2022, **55**, 105804.
- 190 Y. Chen, J. Feng, X. Wang, C. Zhang, D. Ke, H. Zhu, S. Wang, H. Suo and C. Liu, *Environ. Sci. Technol.*, 2023, **57**(46), 18080–18090.
- 191 R. Ding, Y. Chen, Z. Rui, K. Hua, Y. Wu, X. Li, X. Duan, J. Li, X. Wang and J. Liu, *J. Power Sources*, 2023, **556**, 232389.
- 192 M. E. Günay, N. A. Tapan and G. Akkoç, *Int. J. Hydrogen Energy*, 2022, **47**, 2134–2151.
- 193 M. E. Günay and N. A. Tapan, *Energy AI*, 2023, **13**, 100254.
- 194 Y. Zhang, Y. Tao, H. Ren, M. Wu, G. Li, Z. Wan and J. Shao, *J. Power Sources*, 2022, **543**, 231847.
- 195 G. Zhang, L. Wu, K. Jiao, P. Tian, B. Wang, Y. Wang and Z. Liu, *Energy Convers. Manage.*, 2020, **226**, 113513.
- 196 J. Wang, H. Jiang, G. Chen, H. Wang, L. Lu, J. Liu and L. Xing, *Energy AI*, 2023, **14**, 100261.
- 197 H. Pourrahmani and J. Van herle, *Energy*, 2022, **256**, 124712.
- 198 H. Pourrahmani and J. Van herle, *Appl. Therm. Eng.*, 2022, **203**, 117952.
- 199 H. W. Li, B. X. Qiao, J. N. Liu, Y. Yang, W. Fan and G. L. Lu, *Energy Convers. Manage.*, 2022, **271**, 116338.
- 200 T. Cawte and A. Bazylak, *Electrochem. Sci. Adv.*, 2023, **3**, e2100185.
- 201 X. Liu, K. Park, M. So, S. Ishikawa, T. Terao, K. Shinohara, C. Komori, N. Kimura, G. Inoue and Y. Tsuge, *J. Power Sources Adv.*, 2022, **14**, 100084.
- 202 Y. Lou, M. Hao and Y. Li, *J. Power Sources*, 2022, **543**, 231827.
- 203 N. Vaz, J. Choi, Y. Cha, J. kong, Y. Park and H. Ju, *J. Energy Chem.*, 2023, **81**, 28–41.
- 204 G. Xu, Z. Yu, L. Xia, C. Wang and S. Ji, *Energy Convers. Manage.*, 2022, **268**, 116026.
- 205 X. Liu, S. Zhou, Z. Yan, Z. Zhong, N. Shikazono and S. Hara, *Energy AI*, 2022, **7**, 100122.
- 206 A. Fathy, H. Rezk and H. S. Mohamed Ramadan, *Energy*, 2020, **207**, 118326.
- 207 A. Sciazko, Y. Komatsu, A. Nakamura, Z. Ouyang, T. Hara and N. Shikazono, *Chem. Eng. J.*, 2023, **460**, 141680.
- 208 M. H. Golbabaee, M. Saeidi Varnoosfaderani, A. Zare, H. Salari, F. Hemmati, H. Abdoli and B. Hamawandi, *Materials*, 2022, **15**, 7760.
- 209 Y. Wang, C. Wu, S. Zhao, Z. Guo, M. Han, T. Zhao, B. Zu, Q. Du, M. Ni and K. Jiao, *Sci. Bull.*, 2023, **68**, 516–527.
- 210 S. Wan, X. Liang, H. Jiang, J. Sun, N. Djilali and T. Zhao, *Appl. Energy*, 2021, **298**, 117177.
- 211 R. van Gorp, M. van der Heijden, M. Amin Sadeghi, J. Gostick and A. Forner-Cuenca, *Chem. Eng. J.*, 2023, **455**, 139947.
- 212 J. Bao, V. Murugesan, C. J. Kamp, Y. Shao, L. Yan and W. Wang, *Adv. Theory Simul.*, 2020, **3**, 1900167.
- 213 B. A. Simon, A. Gayon-Lombardo, C. A. Pino-Muñoz, C. E. Wood, K. M. Tenny, K. V. Greco, S. J. Cooper, A. Forner-Cuenca, F. R. Brushett, A. R. Kucernak and N. P. Brandon, *Appl. Energy*, 2022, **306**, 117678.
- 214 I. Arganda-Carreras, V. Kaynig, C. Rueden, K. W. Eliceiri, J. Schindelin, A. Cardona and H. Sebastian Seung, *Bioinformatics*, 2017, **33**, 2424–2426.
- 215 J. J. Patil, C. T. C. Wan, S. Gong, Y. M. Chiang, F. R. Brushett and J. C. Grossman, *ACS Nano*, 2023, **17**, 4999–5013.
- 216 T. Li, W. Lu, Z. Yuan, H. Zhang and X. Li, *J. Mater. Chem. A*, 2021, **9**, 14545–14552.



- 217 Y. Yang, N. Li, B. Wang, N. Li, K. Gao, Y. Liang, Y. Wei, L. Yang, W. L. Song and H. Chen, *Electrochem. Commun.*, 2022, **136**, 107224.
- 218 M. Duquesnoy, C. Liu, D. Z. Dominguez, V. Kumar, E. Ayerbe and A. A. Franco, *Energy Storage Mater.*, 2023, **56**, 50–61.
- 219 M. F. Niri, K. Liu, G. Apachitei, L. A. A. Román-Ramírez, M. Lain, D. Widanage and J. Marco, *Energy AI*, 2022, **7**, 100129.
- 220 J. Xu, A. C. Ngandjong, C. Liu, F. M. Zannotto, O. Arcelus, A. Demortière and A. A. Franco, *J. Power Sources*, 2023, **554**, 232294.
- 221 C. Sommer, C. Straehle, U. Kothe and F. A. Hamprecht, in *Proceedings – International Symposium on Biomedical Imaging*, 2011, pp. 230–233.
- 222 J. J. Bailey, A. Wade, A. M. Boyce, Y. S. Zhang, D. J. L. Brett and P. R. Shearing, *J. Power Sources*, 2023, **557**, 232503.
- 223 A. F. Frangi, J. A. Schnabel, C. Davatzikos, C. Alberola-López and G. Fichtinger, *Medical Image Computing and Computer Assisted Intervention – MICCAI 2018, 21st International Conference*, Springer International Publishing, Granada, Spain, 2018, vol. 11071.
- 224 V. Nagda, A. Kulachenko and S. B. Lindström, *Comput. Mater. Sci.*, 2023, **223**, 112139.
- 225 V. Kabra, B. Birn, I. Kamboj, V. Augustyn and P. P. Mukherjee, *J. Phys. Chem. C*, 2022, **126**, 14413–14429.
- 226 S. Ishikawa, X. Liu, T. H. Noh, M. So, K. Park, N. Kimura, G. Inoue and Y. Tsuge, *J. Power Sources Adv.*, 2022, **15**, 100094.
- 227 Y. Sun, S. M. Ayalamayajula, A. Deva, G. Lin and R. E. García, *Sci. Rep.*, 2022, **12**, 1–11.
- 228 J. Fu, D. Xiao, D. Li, H. R. Thomas and C. Li, *Comput. Methods Appl. Mech. Eng.*, 2022, **390**, 114532.
- 229 M. Faraji Niri, J. Mafeni Mase and J. Marco, *Energies*, 2022, **15**, 4489.
- 230 S. Kamrava and H. Mirzaee, *Phys. Rev. E*, 2022, **106**, 055301.
- 231 A. Shodiev, M. Duquesnoy, O. Arcelus, M. Chouchane, J. Li and A. A. Franco, *J. Power Sources*, 2021, **511**, 230384.
- 232 A. El Malki, M. Asch, O. Arcelus, A. Shodiev, J. Yu and A. A. Franco, *J. Power Sources Adv.*, 2023, **20**, 100114.
- 233 Z. Tong, J. Miao, S. Tong and Y. Lu, *J. Cleaner Prod.*, 2021, **317**, 128265.
- 234 B. Jiang, M. D. Berliner, K. Lai, P. A. Asinger, H. Zhao, P. K. Herring, M. Z. Bazant and R. D. Braatz, *Appl. Energy*, 2022, **307**, 118244.
- 235 V. Goel, K. H. Chen, N. P. Dasgupta and K. Thornton, *Energy Storage Mater.*, 2023, **57**, 44–58.
- 236 S. Mishra, R. Srivastava, A. Muhammad, A. Amit, E. Chiavazzo, M. Fasano and P. Asinari, *Sci. Rep.*, 2023, **13**, 6494.
- 237 M. Zhou, A. Gallegos, K. Liu, S. Dai and J. Wu, *Carbon*, 2020, **157**, 147–152.
- 238 A. G. Saad, A. Emad-Eldeen, W. Z. Tawfik and A. G. El-Deen, *J. Energy Storage*, 2022, **55**, 105411.
- 239 S. Ghosh, G. R. Rao and T. Thomas, *Energy Storage Mater.*, 2021, **40**, 426–438.
- 240 P. Liu, Y. Wen, L. Huang, X. Zhu, R. Wu, S. Ai, T. Xue and Y. Ge, *J. Electroanal. Chem.*, 2021, **899**, 115684.
- 241 S. Mathew, P. B. Karandikar and N. R. Kulkarni, *Chem. Eng. Technol.*, 2020, **43**, 1765–1773.
- 242 S. Jha, S. Bandyopadhyay, S. Mehta, M. Yen, T. Chagouri, E. Palmer and H. Liang, *Energy & Fuels*, 2021, **36**, 1052–1062.
- 243 M. Rahimi, M. H. Abbaspour-Fard and A. Rohani, *J. Power Sources*, 2022, **521**, 230968.
- 244 M. Seyyedattar, S. Zendejboudi and S. Butt, *Nat. Resour. Res.*, 2019, **29**, 2147–2189.
- 245 Z. Tariq, M. S. Aljawad, A. Hasan, M. Murtaza, E. Mohammed, A. El-Husseiny, S. A. Alarifi, M. Mahmoud and A. Abdulraheem, *J. Pet. Explor. Prod. Technol.*, 2021, **11**, 4339–4374.
- 246 X. Xie, H. Lu, H. Deng, H. Yang, B. Teng and H. A. Li, *J. Pet. Sci. Eng.*, 2019, **182**, 106243.
- 247 J. Ma, *Unconventional Oil and Gas Resources Handbook: Evaluation and Development*, 2016, pp. 127–150.
- 248 A. Fornel and A. Estublier, *Energy Procedia*, 2013, **37**, 4902–4909.
- 249 J. Hutahaean, V. Demyanov and M. Christie, *J. Pet. Sci. Eng.*, 2019, **175**, 444–464.
- 250 T. Ramstad, C. F. Berg and K. Thompson, *Transp. Porous Media*, 2019, **130**, 77–104.
- 251 Y. Da Wang, M. J. Blunt, R. T. Armstrong and P. Mostaghimi, *Earth-Sci. Rev.*, 2021, **215**, 103555.
- 252 M. Liu and T. Mukerji, *Leading Edge*, 2022, **41**, 591–598.
- 253 S. J. Jackson, Y. Niu, S. Manoorkar, P. Mostaghimi and R. T. Armstrong, *Phys. Rev. Appl.*, 2022, **17**, 054046.
- 254 Y. Niu, S. J. Jackson, N. Alqahtani, P. Mostaghimi and R. T. Armstrong, *Transp. Porous Media*, 2022, **144**, 825–847.
- 255 Y. Da Wang, R. T. Armstrong and P. Mostaghimi, *Water Resour. Res.*, 2020, **56**, e2019WR026052.
- 256 M. Liu and T. Mukerji, *Geophys. Res. Lett.*, 2022, **49**, e2022GL098342.
- 257 J. Fu, D. Xiao, D. Li, H. R. Thomas and C. Li, *Comput. Methods Appl. Mech. Eng.*, 2022, **390**, 114532.
- 258 Q. Zheng and D. Zhang, *Comput. Geosci.*, 2022, **26**, 677–696.
- 259 Y. Yang, F. Liu, J. Yao, S. Iglaue, M. Sajjadi, K. Zhang, H. Sun, L. Zhang, J. Zhong and V. Lisitsa, *J. Nat. Gas Sci. Eng.*, 2022, **99**, 104411.
- 260 H. L. Zhang, H. Yu, S. W. Meng, M. C. Huang, M. Micheal, J. Su, H. Liu and H. A. Wu, *J. Pet. Sci. Eng.*, 2022, **217**, 110937.
- 261 A. K. Ting, J. E. Santos and E. Gultinan, *Energies*, 2022, **15**, 8871.
- 262 O. Ishola and J. Vilcáez, *Fuel*, 2022, **321**, 124044.
- 263 H. Sun, L. ZHOU, D. Fan, L. Zhang, Y. Yang, K. Zhang and J. Yao, *Phys. Fluids*, 2023, **35**, 032014.
- 264 J. W. Tian, C. Qi, K. Peng, Y. Sun and Z. Mundher Yaseen, *J. Comput. Civ. Eng.*, 2022, **36**, 983.
- 265 X. Bu, H. Saleh, M. Han and A. AlSofi, presented in *SPE Reservoir Characterisation and Simulation Conference and Exhibition*, Society of Petroleum Engineers, 2023.
- 266 J. Lee and D. E. Lumley, *J. Pet. Sci. Eng.*, 2023, **220**, 111231.
- 267 T. Ore and D. Gao, *Comput. Geosci.*, 2023, **171**, 105266.



- 268 C. M. Saporetti, D. L. Fonseca, L. C. Oliveira, E. Pereira and L. Goliatt, *Int. J. Environ. Sci. Technol.*, 2023, **20**, 1585–1596.
- 269 H. Zhang, W. Wu and H. Wu, *Geoenergy Sci. Eng.*, 2023, **221**, 111271.
- 270 A. Bemani, A. Kazemi and M. Ahmadi, *J. Pet. Sci. Eng.*, 2023, **220**, 111162.
- 271 M. Rajabi, O. Hazbeh, S. Davoodi, D. A. Wood, P. S. Tehrani, H. Ghorbani, M. Mehrad, N. Mohamadian, V. S. Rukavishnikov and A. E. Radwan, *J. Pet. Explor. Prod. Technol.*, 2023, **13**, 19–42.
- 272 B. Shen, S. Yang, X. Gao, S. Li, K. Yang, J. Hu and H. Chen, *Eng. Appl. Artif. Intell.*, 2023, **118**, 105687.
- 273 C. Huang, L. Tian, J. Wu, M. Li, Z. Li, J. Li, J. Wang, L. Jiang and D. Yang, *Fuel*, 2023, **337**, 127194.
- 274 Q. Lv, R. Zheng, X. Guo, A. Larestani, F. Hadavimoghaddam, M. Riazi, A. Hemmati-Sarapardeh, K. Wang and J. Li, *Sep. Purif. Technol.*, 2023, **310**, 123086.
- 275 B. Liu, Z. Wang, Y. Jin, Z. Ge, C. Xu, H. Liu and H. Chen, *Energy and Fuels*, 2023, **37**, 935–944.
- 276 Y. Zhang, H. R. Zhong, Z. Y. Wu, H. Zhou and Q. Y. Ma, *J. Pet. Sci. Eng.*, 2020, **192**, 107234.
- 277 X. Zhao, X. Chen, Q. Huang, Z. Lan, X. Wang and G. Yao, *J. Pet. Sci. Eng.*, 2022, **214**, 110517.
- 278 L. Yang, S. Wang, X. Chen, W. Chen, O. M. Saad, X. Zhou, N. Pham, Z. Geng, S. Fomel and Y. Chen, *IEEE Trans. Neural Netw. Learn. Syst.*, 2023, **34**, 3429–3443.
- 279 M. Masroor, M. Emami Niri and M. H. Sharifinasab, *Geoenergy Sci. Eng.*, 2023, **222**, 211420.
- 280 M. Matinkia, R. Hashami, M. Mehrad, M. R. Hajsaeedi and A. Velayati, *Petroleum*, 2023, **9**, 108–123.
- 281 Z. Chao, Y. Dang, Y. Pan, F. Wang, M. Wang, J. Zhang and C. Yang, *Geomech. Energy Environ.*, 2023, **33**, 100435.
- 282 S. Pan, Z. Zheng, Z. Guo and H. Luo, *J. Pet. Sci. Eng.*, 2022, **208**, 109520.
- 283 J. Wang and J. Cao, *Arabian J. Sci. Eng.*, 2022, **47**, 11313–11327.
- 284 A. F. Ibrahim, S. Elkatatny, Y. Abdelraouf and M. Al Ramadan, *J. Energy Resour. Technol. Trans. ASME*, 2022, **144**, 083009.
- 285 Z. Zhao, X. P. Zhou and Q. H. Qian, *Sci. China: Technol. Sci.*, 2022, **65**, 458–469.
- 286 C. E. M. dos Anjos, T. F. de Matos, M. R. V. Avila, J. de, C. V. Fernandes, R. Surmas and A. G. Evsukoff, *Geoenergy Sci. Eng.*, 2023, **222**, 211335.
- 287 N. Alqahtani, F. Alzubaidi, R. T. Armstrong, P. Swietojanski and P. Mostaghimi, *J. Pet. Sci. Eng.*, 2020, **184**, 106514.
- 288 H. V. Thanh and Y. Sugai, *Upstream Oil and Gas Technology*, 2021, **6**, 100027.
- 289 M. Pal, P. Makauskas and S. Malik, *Processes*, 2023, **11**, 601.
- 290 Y. Wang, H. Li, J. Xu, S. Liu, Q. Tan and X. Wang, *Appl. Energy*, 2023, **337**, 120854.
- 291 Y. Wang, H. Li, J. Xu, S. Liu and X. Wang, *Energy*, 2022, **245**, 123284.
- 292 A. Santos, H. F. A. Scanavini, H. Pedrini, D. J. Schiozer, F. P. Munerato and C. E. A. G. Barreto, *J. Pet. Sci. Eng.*, 2022, **211**, 110071.
- 293 J. Siavashi, A. Najafi, M. Ebadi and M. Sharifi, *Fuel*, 2022, **211**, 110071.
- 294 O. S. Alolayan, A. O. Alomar and J. R. Williams, *Energies*, 2023, **16**, 860.
- 295 S. Jo, H. Jeong, B. Min, C. Park, Y. Kim, S. Kwon and A. Sun, *J. Pet. Sci. Eng.*, 2022, **208**, 109247.
- 296 X. Ma, K. Zhang, J. Zhang, Y. Wang, L. Zhang, P. Liu, Y. Yang and J. Wang, *J. Pet. Sci. Eng.*, 2022, **210**, 110109.
- 297 X. Ma, K. Zhang, H. Zhao, L. Zhang, J. Wang, H. Zhang, P. Liu, X. Yan and Y. Yang, *J. Pet. Sci. Eng.*, 2022, **214**, 110548.
- 298 C. Xiao, H. X. Lin, O. Leeuwenburgh and A. Heemink, *J. Pet. Sci. Eng.*, 2022, **208**, 109287.
- 299 A. Qubian, M. A. Zekraoui, S. Mohajeri, E. Mortezaazadeh, R. Eslahi, M. Bakhtiari, A. Al Dabbous, A. Al Sagheer, A. Alizadeh and M. Zeinali, in *Society of Petroleum Engineers – SPE Symposium: Leveraging Artificial Intelligence to Shape the Future of the Energy Industry, AIS 2023*, Society of Petroleum Engineers, 2023.
- 300 M. V. Behl and M. Tyagi, *SPE Reservoir Eval. Eng.*, 2023, 1–15.
- 301 H. Huang, B. Gong, Y. Liu and W. Sun, *Geoenergy Sci. Eng.*, 2023, **222**, 211418.
- 302 B. Saberali, N. Golsanami, K. Zhang, B. Gong and M. Ostadhassan, *Geoenergy Sci. Eng.*, 2023, **222**, 211415.
- 303 F. A. Shuaibi, M. M. Hadhrami, A. H. Sheheimi, B. Agarwal, Q. M. Riyami, M. Ruqaishi, N. Habsi, E. Mortezaazadeh and S. Mohajeri, in *Society of Petroleum Engineers - SPE Reservoir Characterisation and Simulation Conference and Exhibition 2023, RCSC 2023*, Society of Petroleum Engineers, 2023.
- 304 R. Manasipov, D. Nikolaev, D. Didenko, R. Abdalla and M. Stundner, in *Society of Petroleum Engineers - SPE Reservoir Characterisation and Simulation Conference and Exhibition 2023, RCSC 2023*, Society of Petroleum Engineers, 2023.
- 305 X. Kong, Y. Liu, L. Xue, G. Li and D. Zhu, *Energies*, 2023, **16**, 1027.
- 306 H. Chu, P. Dong and W. J. Lee, *Adv. Geo-Energy Res.*, 2023, **7**, 49–65.
- 307 A. F. Ibrahim, S. A. Alarifi and S. Elkatatny, *J. Pet. Explor. Prod. Technol.*, 2023, **13**, 1123–1134.
- 308 U. Osah and J. Howell, *Pet. Geosci.*, 2023, **19**, 071.
- 309 Z. A.-A. H. Al-Ali and R. Horne, presented in *Gas & Oil Technology Showcase and Conference, Society of Petroleum Engineers (SPE)*, Dubai, UAE, 2023.
- 310 Y. Liu, J. Zeng, J. Qiao, G. Yang, S. Liu and W. Cao, *Appl. Energy*, 2023, **333**, 120604.
- 311 H. Ullah, Z. U. Haq, S. R. Naqvi, M. N. A. Khan, M. Ahsan and J. Wang, *J. Anal. Appl. Pyrolysis*, 2023, **170**(105879).
- 312 S. Du, J. Wang, M. Wang, J. Yang, C. Zhang, Y. Zhao and H. Song, *Energy*, 2023, **263**, 126121.
- 313 H. Tang and L. J. Durlofsky, *Comput. Geosci.*, 2022, **26**, 1189–1206.
- 314 J. R. Bertini, S. F. Ferreira Batista, M. A. Funcia, L. O. Mendes da Silva, A. A. S. Santos and D. J. Schiozer, *J. Pet. Sci. Eng.*, 2022, **208**, 109208.



- 315 J. Zhou, H. Wang, C. Xiao and S. Zhang, *Energies*, 2023, **16**, 303.
- 316 Y. Nasir and L. J. Durlofsky, *SPE J.*, 2023, 1–14.
- 317 Y.-T. Chen, D.-X. Zhang, Q. Zhao and D.-X. Liu, *Pet. Sci.*, 2023, **20**, 1788–1805.
- 318 Y. Yao, Y. Qiu, Y. Cui, M. Wei and B. Bai, *Chem. Eng. J.*, 2023, **451**, 138022.
- 319 C. Fabbri, N. Reddicharla, W. Shi, A. Al Shalabi, S. Al Hashmi and S. Al Jaber, in *Society of Petroleum Engineers - SPE Reservoir Characterisation and Simulation Conference and Exhibition 2023, RCSC 2023*, Society of Petroleum Engineers, 2023.
- 320 M. Pirizadeh, N. Alemohammad, M. Manthouri and M. Pirizadeh, *Pet. Sci. Technol.*, 2023, **41**, 64–85.
- 321 P. S. Pavan, K. Arvind, B. Nikhil and P. Sivasankar, *Bioresour. Technol.*, 2022, **351**, 127023.
- 322 M. Mahdaviara, M. Sharifi and M. Ahmadi, *Fuel*, 2022, **325**, 124795.
- 323 R. K. Pachauri, M. R. Allen, V. R. Barros, J. Broome, W. Cramer, R. Christ, J. A. Church, L. Clarke, Q. Dahe and P. Dasgupta, *Climate Change 2014: Synthesis Report. Contribution of Working Groups I, II and III to the Fifth Assessment Report of the Intergovernmental Panel on Climate Change*, Ipcc, 2014.
- 324 *Climate Change 2022: Impacts, Adaptation and Vulnerability - Contribution of Working Group II to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change*, ed. H.-O. Pörtner, D. C. Roberts, E. S. Poloczanska, K. Mintenbeck, M. Tignor, A. Alegria, M. Craig, S. Langsdorf, S. Lösche, V. Möller and A. Okem, Cambridge University Press, Cambridge, UK, New York, NY, USA, 2022, p. 3.
- 325 G. Luderer, Z. Vrontisi, C. Bertram, O. Y. Edelenbosch, R. C. Pietzcker, J. Rogelj, H. S. De Boer, L. Drouet, J. Emmerling and O. Fricko, *Nat. Clim. Change*, 2018, **8**, 626–633.
- 326 R. Cavicchioli, W. J. Ripple, K. N. Timmis, F. Azam, L. R. Bakken, M. Baylis, M. J. Behrenfeld, A. Boetius, P. W. Boyd and A. T. Classen, *Nat. Rev. Microbiol.*, 2019, **17**, 569–586.
- 327 M. Bui, C. S. Adjiman, A. Bardow, E. J. Anthony, A. Boston, S. Brown, P. S. Fennell, S. Fuss, A. Galindo and L. A. Hackett, *Energy Environ. Sci.*, 2018, **11**, 1062–1176.
- 328 D. W. Keith, G. Holmes, D. S. Angelo and K. Heidel, *Joule*, 2018, **2**, 1573–1594.
- 329 H. Azarabadi and K. S. Lackner, *Environ. Sci. Technol.*, 2020, **54**, 5102–5111.
- 330 O. S. Bushuyev, P. De Luna, C. T. Dinh, L. Tao, G. Saur, J. van de Lagemaat, S. O. Kelley and E. H. Sargent, *Joule*, 2018, **2**, 825–832.
- 331 B. Smit, J. A. Reimer, C. M. Oldenburg and I. C. Bourg, *Introduction to Carbon Capture and Sequestration*, World Scientific, 2014, vol. 1.
- 332 J. C. Palmer, A. Llobet, S. H. Yeon, J. E. Fischer, Y. Shi, Y. Gogotsi and K. E. Gubbins, *Carbon*, 2010, **48**, 1116–1123.
- 333 P. Ugliengo, M. Sodupe, F. Musso, I. J. Bush, R. Orlando and R. Dovesi, *Adv. Mater.*, 2008, **20**, 4579–4583.
- 334 J. M. H. Thomas and A. Trewin, *J. Phys. Chem. C*, 2014, **118**, 19712–19722.
- 335 G. Férey, C. Mellot-Draznieks, C. Serre, F. Millange, J. Dutour, S. Surblé and I. Margiolaki, *Science*, 2005, **309**, 2040–2042.
- 336 S. Cai, L. Yu, E. Huo, Y. Ren, X. Liu and Y. Chen, *Langmuir*, 2024, **40**, 6869–6877.
- 337 M. M. Lozinska, E. Mangano, J. P. S. Mowat, A. M. Shepherd, R. F. Howe, S. P. Thompson, J. E. Parker, S. Brandani and P. A. Wright, *J. Am. Chem. Soc.*, 2012, **134**, 17628–17642.
- 338 S. Bandyopadhyay, A. G. Anil, A. James and A. Patra, *ACS Appl. Mater. Interfaces*, 2016, **8**, 27669–27678.
- 339 H. Mashhadimoslem, A. Ghaemi, A. Maleki and A. Elkamel, *J. Environ. Chem. Eng.*, 2023, **11**, 109300.
- 340 N. Von Der Assen, P. Voll, M. Peters and A. Bardow, *Chem. Soc. Rev.*, 2014, **43**, 7982–7994.
- 341 R. M. Cuéllar-Franca and A. Azapagic, *J. CO2 Util.*, 2015, **9**, 82–102.
- 342 S. Deutz and A. Bardow, *Nat. Energy*, 2021, **6**, 203–213.
- 343 R. Sathre and E. Masanet, *RSC Adv.*, 2013, **3**, 4964–4975.
- 344 M. Vafaeinia, M. S. Khosrowshahi, H. Mashhadimoslem, H. B. M. Emrooz and A. Ghaemi, *RSC Adv.*, 2022, **12**, 546–560.
- 345 M. S. Khosrowshahi, M. A. Abdol, H. Mashhadimoslem, E. Khakpour, H. B. M. Emrooz, S. Sadeghzadeh and A. Ghaemi, *Sci. Rep.*, 2022, **12**, 1–19.
- 346 H. Mashhadimoslem, M. Safarzadeh Khosrowshahi, M. Jafari, A. Ghaemi and A. Maleki, *ACS Omega*, 2022, **7**, 18409–18426.
- 347 M. S. Khosrowshahi, H. Mashhadimoslem, H. B. M. Emrooz, A. Ghaemi and M. S. Hosseini, *Diamond Relat. Mater.*, 2022, 109204.
- 348 L. Ward, A. Agrawal, A. Choudhary and C. Wolverton, *npj Comput. Mater.*, 2016, **2**, 1–7.
- 349 Y. Dong, C. Wu, C. Zhang, Y. Liu, J. Cheng and J. Lin, *npj Comput. Mater.*, 2019, **5**, 26.
- 350 A. O. Oliynyk, L. A. Adutwum, B. W. Rudyk, H. Pisavadia, S. Lotfi, V. Hlukhy, J. J. Harynyuk, A. Mar and J. Brgoch, *J. Am. Chem. Soc.*, 2017, **139**, 17870–17881.
- 351 H. Mashhadimoslem, M. Vafaeinia, M. Safarzadeh, A. Ghaemi, F. Fathalian and A. Maleki, *Ind. Eng. Chem. Res.*, 2021, **60**, 13950–13966.
- 352 P. Raccuglia, K. C. Elbert, P. D. F. Adler, C. Falk, M. B. Wenny, A. Mollo, M. Zeller, S. A. Friedler, J. Schrier and A. J. Norquist, *Nature*, 2016, **533**, 73–76.
- 353 D. T. Ahneman, J. G. Estrada, S. Lin, S. D. Dreher and A. G. Doyle, *Science*, 2018, **360**, 186–190.
- 354 M. Rahimi, S. M. Moosavi, B. Smit and T. A. Hatton, *Cell Rep. Phys. Sci.*, 2021, **2**, 100396.
- 355 H. Mashhadimoslem, V. Kermani, K. Zanganeh, A. Shafeen and A. Elkamel, *Can. J. Chem. Eng.*, 2023, 25060.
- 356 H. Pashaei, H. Mashhadimoslem and A. Ghaemi, *Sci. Rep.*, 2023, **13**, 4011.
- 357 D. M. D'Alessandro, B. Smit and J. R. Long, *Angew. Chem., Int. Ed.*, 2010, **49**, 6058–6082.



- 358 Z. Zhang, J. A. Schott, M. Liu, H. Chen, X. Lu, B. G. Sumpter, J. Fu and S. Dai, *Angew. Chem.*, 2019, **131**, 265–269.
- 359 S. Wang, Z. Zhang, S. Dai and D. Jiang, *ACS Mater. Lett.*, 2019, **1**, 558–563.
- 360 X. Yuan, M. Suvarna, S. Low, D. Dissanayake, K. B. Lee, J. Li, X. Wang and Y. S. Ok, *Environ. Sci. Technol.*, 2021, **55**, 11925–11936.
- 361 X. Ma, W. Xu, R. Su, L. Shao, Z. Zeng, L. Li and H. Wang, *Sep. Purif. Technol.*, 2023, **306**, 122521.
- 362 C. Xie, Y. Xie, C. Zhang, H. Dong and L. Zhang, *J. Environ. Chem. Eng.*, 2023, **11**, 109053.
- 363 A. Ahmed, S. Seth, J. Purewal, A. G. Wong-Foy, M. Veenstra, A. J. Matzger and D. J. Siegel, *Nat. Commun.*, 2019, **10**, 1568.
- 364 D. Alezi, Y. Belmabkhout, M. Suyetin, P. M. Bhatt, Ł. J. Weseliński, V. Solovyeva, K. Adil, I. Spanopoulos, P. N. Trikalitis and A.-H. Emwas, *J. Am. Chem. Soc.*, 2015, **137**, 13308–13318.
- 365 P. G. Boyd, A. Chidambaram, E. García-Díez, C. P. Ireland, T. D. Daff, R. Bounds, A. Gładysiak, P. Schouwink, S. M. Moosavi and M. M. Maroto-Valer, *Nature*, 2019, **576**, 253–256.
- 366 Z. Yao, B. Sánchez-Lengeling, N. S. Bobbitt, B. J. Bucior, S. G. H. Kumar, S. P. Collins, T. Burns, T. K. Woo, O. K. Farha and R. Q. Snurr, *Nat. Mach. Intell.*, 2021, **3**, 76–86.
- 367 Y. G. Chung, E. Haldoupis, B. J. Bucior, M. Haranczyk, S. Lee, H. Zhang, K. D. Vogiatzis, M. Milisavljevic, S. Ling and J. S. Camp, *J. Chem. Eng. Data*, 2019, **64**, 5985–5998.
- 368 Q. Li, S. Gupta, L. Tang, S. Quinn, V. Atakan and R. E. Riman, *Front. Energy Res.*, 2016, **3**, 53.
- 369 S. Babamohammadi, A. Shamiri, T. N. G. Borhani, M. S. Shafeeyan, M. K. Aroua and R. Yusoff, *J. Mol. Liq.*, 2018, **249**, 40–52.
- 370 J. Krzywanski, T. Czakiert, T. Shimizu, I. Majchrzak-Kuceba, Y. Shimazaki, A. Zylka, K. Grabowska and M. Sosnowski, *Energy & fuels*, 2018, **32**, 6355–6362.
- 371 Y. Yan, T. Mattisson, P. Moldenhauer, E. J. Anthony and P. T. Clough, *Chem. Eng. J.*, 2020, **387**, 124072.
- 372 Z. Zhang, X. Cao, C. Geng, Y. Sun, Y. He, Z. Qiao and C. Zhong, *J. Membr. Sci.*, 2022, **650**, 120399.
- 373 J. Guan, T. Huang, W. Liu, F. Feng, S. Japip, J. Li, X. Wang and S. Zhang, *Cell Rep. Phys. Sci.*, 2022, **3**, 100864.
- 374 W. Gao, S. Wang, W. Zheng, W. Sun and L. Zhao, *Sep. Purif. Technol.*, 2023, **313**, 123469.
- 375 P. Krokidas, S. Karozis, S. Moncho, G. Giannakopoulos, E. N. Brothers, M. E. Kainourgiakis, I. G. Economou and T. A. Steriotis, *J. Mater. Chem. A*, 2022, **10**, 13697–13703.
- 376 S. Yang, W. Zhu, L. Zhu, X. Ma, T. Yan, N. Gu, Y. Lan, Y. Huang, M. Yuan and M. Tong, *ACS Appl. Mater. Interfaces*, 2022, **14**, 56353–56362.
- 377 X. Cheng, Y. Liao, Z. Lei, J. Li, X. Fan and X. Xiao, *J. Membr. Sci.*, 2023, **672**, 121430.
- 378 Q. Zhu, Y. Gu, X. Liang, X. Wang and J. Ma, *ACS Catal.*, 2022, **12**, 12336–12348.
- 379 B. M. Kriesche, L. E. Kronenberg, F. R. S. Purtscher and T. S. Hofer, *Front. Chem.*, 2023, **11**, 210.
- 380 M. Feng, M. Cheng, X. Ji, L. Zhou, Y. Dang, K. Bi, Z. Dai and Y. Dai, *Sep. Purif. Technol.*, 2022, **302**, 122111.
- 381 A. Sturluson, A. Raza, G. D. McConachie, D. W. Siderius, X. Z. Fern and C. M. Simon, *Chem. Mater.*, 2021, **33**, 7203–7216.
- 382 A. Kondinski, A. Menon, D. Nurkowski, F. Farazi, S. Mosbach, J. Akroyd and M. Kraft, *J. Am. Chem. Soc.*, 2022, **144**, 11713–11728.
- 383 M. Raji, A. Dashti, M. S. Alivand and M. Asghari, *J. Environ. Manage.*, 2022, **307**, 114478.
- 384 S. Zhang, H. Dong, A. Lin, C. Zhang, H. Du, J. Mu, J. Han, J. Zhang and F. Wang, *ACS Sustain. Chem. Eng.*, 2022, **10**, 13185–13193.
- 385 B. Yan, D. R. Harp, B. Chen and R. J. Pawar, *Sci. Rep.*, 2022, **12**, 20667.
- 386 Q. Yuan, M. Longo, A. W. Thornton, N. B. McKeown, B. Comesana-Gandara, J. C. Jansen and K. E. Jelfs, *J. Membr. Sci.*, 2021, **627**, 119207.
- 387 A. J. Yamaguchi, T. Sato, T. Tobase, X. Wei, L. Huang, J. Zhang, J. Bian and T.-Y. Liu, *Fuel*, 2023, **334**, 126678.
- 388 J. C. Pashin and R. L. Dodge, *Carbon Dioxide Sequestration in Geological Media: State of the Science*, AAPG Studies in Geology, 2010, vol. 59, p. 59.
- 389 H. V. Thanh, Q. Yasin, W. J. Al-Mudhafar and K.-K. Lee, *Appl. Energy*, 2022, **314**, 118985.
- 390 F. Pappenberger, P. Matgen, K. J. Beven, J.-B. Henry, L. Pfister and P. Fraipont, *Adv. Water Resour.*, 2006, **29**, 1430–1449.
- 391 J. Teng, A. J. Jakeman, J. Vaze, B. F. W. Croke, D. Dutta and S. Kim, *Environ. Model. Softw.*, 2017, **90**, 201–216.
- 392 P. Hamel, D. Riveros-Iregui, D. Ballari, T. Browning, R. Céleri, D. Chandler, K. P. Chun, G. Destouni, S. Jacobs, S. Jasechko, M. Johnson, J. Krishnaswamy, M. Poca, P. V. Pompeu and H. Rocha, in *Ecohydrology*, John Wiley and Sons Ltd, 2018, vol. 11.
- 393 K. Khosravi, R. Barzegar, S. Miraki, J. Adamowski, P. Daggupati, M. R. Alizadeh, B. T. Pham and M. T. Alami, *Groundwater*, 2020, **58**, 723–734.
- 394 Z. Abdullelah Al-Sudani, S. Q. Salih, A. sharafati and Z. M. Yaseen, *J. Hydrol.*, 2019, **573**, 1–12.
- 395 D. T. Bui, K. Khosravi, J. Tiefenbacher, H. Nguyen and N. Kazakis, *Sci. Total Environ.*, 2020, **721**, 137612.
- 396 K. Khosravi, M. Bordbar, S. Paryani, P. M. Saco and N. Kazakis, *Sci. Total Environ.*, 2021, **767**, 145416.
- 397 P. Tahmasebi, S. Kamrava, T. Bai and M. Sahimi, *Adv. Water Resour.*, 2020, **142**, 103619.
- 398 K. Khosravi, A. Golkarian, P. M. Saco, M. J. Booji and A. M. Melesse, *Geocarto Int.*, 2022, **37**(27), 18520–18545.
- 399 W. Brutsaert, *Hydrology*, Cambridge University Press, 2005.
- 400 M. Panahi, K. Khosravi, S. Ahmad, S. Panahi, S. Heddami, A. M. Melesse, E. Omidvar and C. W. Lee, *J. Hydrol. Reg. Stud.*, 2021, **35**, 100825.
- 401 Z. U. Rehman, U. Khalid, N. Ijaz, H. Mujtaba, A. Haider, K. Farooq and Z. Ijaz, *Eng. Geol.*, 2022, **311**, 106899.
- 402 Y. Lu and G. Mei, *Mathematics*, 2022, **10**, 2949.
- 403 S. Muhammed Pandhiani, *Arabian J. Geosci.*, 2022, **15**, 1068.



- 404 S. Prakash and S. S. Sahu, *Int. J. Adv. Res. Sci. Eng. Technol.*, 2020, **11**(6), 426–435.
- 405 A. Singh and K. Gaurav, *Sci. Rep.*, 2023, **13**, 2251.
- 406 A. Uthayakumar, M. P. Mohan, E. H. Khoo, J. Jimeno, M. Y. Siyal and M. F. Karim, *Sensors*, 2022, **22**, 5810.
- 407 C. Hulbert, B. Rouet-Leduc, P. A. Johnson, C. X. Ren, J. Rivière, D. C. Bolton and C. Marone, *Nat. Geosci.*, 2019, **12**, 69–74.
- 408 C. Kadow, D. M. Hall and U. Ulbrich, *Nat. Geosci.*, 2020, **13**, 408–413.
- 409 C. Marone, *Nat. Geosci.*, 2018, **11**, 301–302.
- 410 S. Sahour, M. Khanbeyki, V. Gholami, H. Sahour, I. Kahvazade and H. Karimi, *Environ. Sci. Pollut. Res.*, 2023, **30**, 46004–46021.
- 411 F. Sajedi-Hosseini, A. Malekian, B. Choubin, O. Rahmati, S. Cipullo, F. Coulon and B. Pradhan, *Sci. Total Environ.*, 2018, **644**, 954–962.
- 412 M. Zhu, J. Wang, X. Yang, Y. Zhang, L. Zhang, H. Ren, B. Wu and L. Ye, *Eco-Environment & Health*, 2022, **1**, 107–116.
- 413 S. Kumar and J. Pati, *J. Water Health*, 2022, **20**, 829–848.
- 414 A. O. Meray, S. Sturla, M. R. Siddiquee, R. Serata, S. Uhlemann, H. Gonzalez-Raymat, M. Denham, H. Upadhyay, L. E. Lagos, C. Eddy-Dilek and H. M. Wainwright, *Environ. Sci. Technol.*, 2022, **56**, 5973–5983.
- 415 B. Berhanu, Y. Seleshi and A. M. Melesse, in *Nile River Basin: Ecohydrological Challenges, Climate Change and Hydropolitics*, Springer International Publishing, 2014, pp. 97–117.
- 416 C. R. Fitts, *Groundwater Science*, Elsevier, 2nd edn, 2012.
- 417 M. K. Jha, A. Chowdhury, V. M. Chowdary and S. Peiffer, *Water Resour. Manage.*, 2007, **21**, 427–467.
- 418 S. Mukherjee, *Hydrogeol J.*, 1996, **19**, 53–64.
- 419 H. P. Patra, S. K. Adhikari and S. Kunar, *Groundwater Geology and Geological Prospecting*, in *Groundwater Prospecting and Management*, Springer Hydrogeology, Springer, Singapore, 2016, pp. 47–51.
- 420 A. S. Richey, B. F. Thomas, M. H. Lo, J. T. Reager, J. S. Famiglietti, K. Voss, S. Swenson and M. Rodell, *Water Resour. Res.*, 2015, **51**, 5217–5238.
- 421 S. Siebert, V. Henrich, K. Frenken and J. Burke, *Update of the Digital Global Map of Irrigation Areas to Version 5*, 2013.
- 422 A. E. Ercin and A. Y. Hoekstra, *Environ. Int.*, 2014, **64**, 71–82.
- 423 A. Ozdemir, *J. Hyd.*, 2011, **405**, 123–136.
- 424 M. Israil, M. Al-hadithi and D. C. Singhal, *Hydrogeol J.*, 2006, **14**, 753–759.
- 425 O. A. Fashae, M. N. Tijani, A. O. Talabi, • Oluwatola and I. Adedeji, *Appl. Water Sci.*, 2013, **4**, 19–38.
- 426 K. Khosravi, M. Panahi and D. Tien Bui, *Hydrol. Earth Syst. Sci.*, 2018, **22**, 4771–4792.
- 427 W. L. Hakim, A. S. Nur, F. Rezaie, M. Panahi, C.-W. Lee and S. Lee, *J. Hydrol. Reg. Stud.*, 2022, **39**, 100990.
- 428 H. Morgan, A. Madani, H. M. Hussien and T. Nassar, *Geosci. Lett.*, 2023, **10**(9), DOI: [10.1186/s40562-023-00261-2](https://doi.org/10.1186/s40562-023-00261-2).
- 429 L. Aller, T. Bennett, J. H. Lehr, R. J. Petty and G. Hackett, *Robert S. Kerr Environmental Research Laboratory, Office of Research and Development*, US Environmental Protection Agency, 1987.
- 430 S. Ijlil, A. Essahlaoui, M. Mohajane, N. Essahlaoui, E. M. Mili and A. Van Rompaey, *Remote Sens.*, 2022, **14**, 2379.
- 431 K. Khosravi, M. Sartaj, F. T. C. Tsai, V. P. Singh, N. Kazakis, A. M. Melesse, I. Prakash, D. Tien Bui and B. T. Pham, *Sci. Total Environ.*, 2018, **642**, 1032–1049.

