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New model for aspartic acid species in aqueous calcium carbonate growth environments: challenges and perspectives†

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The lack of experimental data on the dynamics of aspartic acid species in water for its range of protonation states and the details of their atomic-level interaction with aqueous calcium carbonate species is a driver for accurate force field development. A classical model that is consistent with the few pieces of experimental data available and with first principles calculations has been developed. The complex dynamics of the aspartate anions relevant to biomineralization and calcium carbonate crystal growth has been explored in water, providing a quantitative description of solvation structure and free energies, including conformational free energy profiles and pairing free energies. The model has been used to probe the structure and dynamics of aqueous calcium aspartate homo- and hetero-chiral clusters, confirming their unlikelihood due to weak and water-mediated interactions. This supports the hypothesis that the formation of such clusters, observed while growing vaterite in the presence of acidic chiral amino acids, is favoured by the presence of the crystal surface.

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1 Introduction

The ability to model with high accuracy organic molecules of biological relevance in mineral growth environments has the potential to reveal the atomic-level intermolecular details that dominate mineral synthesis during biomineralization. While biomineralization is a complex phenomenon involving a variety of physico-chemical and mechanical processes, biomolecules are considered as the key players in growing, maintaining and repairing the hard tissues of living organisms. In particular, organisms belonging to all living kingdoms can synthesise minerals with specific sizes, compositions, textures and shapes; an ability that goes beyond our current knowledge in materials synthesis.^{1–4}

Calcium carbonate is arguably the most widespread and studied biomineral, and proteins, peptides and amino acids are the biomolecules that have received most attention in the context of calcium carbonate biomineralization.^{5–12} Numerous studies are available that demonstrate how these molecules affect the nucleation and growth of calcium carbonate, acting as

crystal structure modifiers, inhibitors, or forming organic-inorganic composites. Recently, non-racemic mixtures of chiral acidic amino acids, such as aspartic and glutamic acids, were found to induce the formation of chiral toroids of vaterite through the formation of homochiral clusters on the mineral surface.^{13,14}

While a certain level of knowledge exists on the macroscopic effects of proteins, peptides and amino acids on the nucleation and growth of calcium carbonate, the fundamental interactions that underpin the process are largely unexplored. The size and time scale of the dynamics of these molecules in aqueous environments has so far limited their theoretical investigation.⁴ Additionally, the majority of models available for biomolecular simulation^{15–17} have not been parameterised for this purpose, and therefore may not be directly transferable to investigations in mineral growth environments.

Recently, some of the present authors have started the development of accurate potential models that can bridge this gap. The dynamics of small organic molecules in aqueous environments and their interaction with both calcium carbonate aqueous species and calcite terraces and steps have been investigated with both polarisable and rigid-ion models.^{18,19} In particular, the simplest molecules with the most relevant functional groups for calcium carbonate biomineralization were considered, *i.e.* methylammonium, acetate, and the glycine zwitterion.

This work is focused on aspartic acid, its speciation in water and interaction with calcium carbonate aqueous species. While

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being a relatively simple and small additive, this molecule has two additional levels of complexity with respect to those that have been considered previously: (1) the presence of an additional carboxylate group, offering an additional binding site; (2) the flexibility to change conformation through the torsional angle defined by the four carbon atoms. A rigid-ion potential model presented in this paper has already been used to provide theoretical support to the formation of homochiral aspartic acid clusters as a result of the interaction between vaterite and aspartic acid solutions.¹⁴ However, the details of its development and its performance have yet to be examined in detail. Additionally, while numerous computational investigations on aspartic acid species exist, its complex conformational energy profile and speciation have never been thoroughly probed in aqueous environments relevant to biomineralization, while its interaction with calcium and carbonate ions in water have only been superficially discussed without considering the full complexity of this amino acid. Below we highlight the main works that have examined relevant systems to date.

Nada²⁰ modelled the interaction of aspartic acid with the various surface features of calcite. The CHARMM22²¹ force field was used for aspartic acid, in conjunction with an earlier calcite model from Raiteri *et al.*²² and TIP3P water.²³ This water model yields a self-diffusion coefficient that is twice the experimental value, meaning much faster dynamics occur than in real water, and a dielectric constant that is overestimated by more than 25%, meaning that charged species are over-stabilized with respect to complexes and the solvation structure is altered due to the discrepancy in the correlations in the orientations of water dipoles.²⁴ Additionally, the conformational arrangement of aspartic acid species was not fully explored and their dynamics and thermodynamics in water was not investigated.

Stepić *et al.*²⁵ performed umbrella sampling of aspartic acid species attachment to the surface of calcite. Here, a similar approach to model choice as in Nada²⁰ was adopted, combining the AMBER¹⁵ force field with the aforementioned calcite model from Raiteri *et al.*²² and TIP3P water.²³ Apart from being affected by the same inaccuracies as Nada,²⁰ due to the water potential model, again the flexibility of aspartic acid species to change conformation is not fully explored, as the attachment has been investigated only through the distance between the centre of mass of the molecule and the surface as a collective variable. Additionally, Stepić *et al.*'s results suggest preferential attachment to calcite *via* the amino group, rather than the carboxylate, which is counter-intuitive, while strongest binding for the monomer occurs on the terraces, rather than at steps or kinks. In contrast, Njegić-Džakula *et al.*⁹ and Wierzbicki *et al.*⁵ experimentally found attachment of polyaspartic acid and aspartic acid, respectively, to calcium sites on the calcite surface through chain carboxylate groups. Montanari *et al.*¹² showed that aspartic acid competes with carbonate ions to attach to the surface of calcite (hence suggesting preferential attachment to calcium sites). Additionally, Verch *et al.*²⁶ classified polyaspartic acid as an additive that binds to calcium in solution, though it is suggested that carboxylate groups are not solely responsible for the binding.

Innocenti Malini *et al.*²⁷ simulated the effect of a few different amino acids, including aspartic acid, on amorphous calcium carbonate. This model combines the ff12sc AMBER²⁸ force field with a more recent version of Raiteri *et al.*'s²⁹ model, using the SPC/Fw water model. This is an improvement with respect to earlier force fields, and provides a binding free energy of aspartic acid with calcium that is in much better agreement with the experimental values than a previous model by some of the present authors,³⁰ using the same calcium carbonate and water parameterisations. However, the dynamics of aspartic acid species in water, the energy profile of their interaction with water and dissolved ions was not examined. Additionally, also in this case it was shown that aspartic acid binds to calcium carbonate preferentially *via* the protonated amino group, which acts as a hydrogen bond donor. This is in contrast with the aforementioned pieces of experimental evidence, which do not exclude this kind of interaction, but suggest binding at biological pH occurs primarily through carboxylate groups.^{5,9,12,26} A similar model, though based on the ff14sp²⁸ parameterisation of AMBER, was used by Finney *et al.*³¹ to simulate the effect of several amino acids, including aspartic acid, on calcium carbonate speciation at different concentrations in aqueous solution.

Recently, Koskamp *et al.*³² calibrated a model for the fully deprotonated aspartate species (pH = 10) through combining parameters from the ff99SB version of AMBER³³ (aspartic acid, originally developed in combination with TIP3P²³ water) and from Raiteri *et al.*²⁹ (calcium carbonate and SPC/Fw water²⁴) using combination rules. While the parameters between calcium and the carboxylate oxygen in aspartate were successfully calibrated to fit the numerical value of the experimental calcium aspartate association free energy at that pH, the model was not reparametrised to predict other properties that affect ion pairing, including the hydration free energy, conformational free energy profile, and pair distribution function.

As mentioned above, the force field developed in this paper is a first step towards being able to capture the complexity of aspartic acid species in environments relevant to crystal growth and biomineralization. In particular: (a) one of the most accurate models for liquid water at room temperature is used; (b) the model includes two different aspartic acid protonation states that are relevant to the biomineralization and crystal growth fields; (c) hydration free energies, water structure of the solvation shell, and conformational free energy profile of aspartic acid species are in agreement with first principles data; (d) ion pairing free energy values with calcium are in line with experiment. Despite lacking explicit inclusion of polarisability, the careful thermodynamic calibration means that it represents an improvement with respect to other existing models and a starting point for future applications to aqueous organic-biomineral interfaces.

2 Computational methods

Two aspartic acid anions were considered in this study; the negative zwitterion, namely Asp ZW⁻, which is the predominant

species at typical pH values for biomineralization, and the fully deprotonated anion, namely Asp^{2-} , which is the predominant species in highly alkaline environments, such as in recent experiments showing the growth of chiral toroids of vaterite in the presence of aspartic acid.¹⁴

All classical simulations were run using the LAMMPS³⁴ code, with a time step of 1 fs and trajectories recorded every 1 ps. Cubic boxes containing ~ 520 molecules (corresponding to a cell length of ~ 24.860 Å) were used to analyse the conformational energy profile and hydration of the aspartate anions, and cubic boxes containing ~ 4175 molecules (cell length ~ 49.969 Å) were used to explore the pairing free energy with calcium and the formation of clusters.

In all simulations the temperature (300 K) was controlled using a chain of five Nosé–Hoover thermostats with a relaxation time of 0.1 ps. For simulations in the isobaric–isothermal (NPT) ensemble, the pressure (1 atm) was maintained using a chain of five Nosé–Hoover barostats with a relaxation time of 1 ps. A MTK barostat³⁵ was additionally applied to reproduce the true volume probability distribution of the NPT ensemble.

All multiple-walker³⁶ well-tempered³⁷ metadynamics^{38,39} simulations were run using the Plumed⁴⁰ package. Gaussian functions with a width of 0.2 (radians or Å, depending on the collective variable being an angle or a distance, respectively) and 0.1 (dimensionless, coordination number) were deposited every 1 ps, with an initial height of $k_B T$. Collective variables in all simulations used a bias factor of 5 to progressively reduce the heights of the Gaussian functions until convergence was achieved.

The collective variables used in this study, as defined in the Plumed manual^{40,41} and with atoms labelled as in Fig. 1, are listed below and their use is summarised in Table 1:

- Distance between Ca and C1 ($d1$).
- Distance between Ca and C4 ($d2$).
- Distance between Ca and the centre of mass (COM) of aspartic acid species ($d3$).
- Distance between Ca in water and Ca in cluster ($d4$).
- Torsional angle of aspartic acid species (C1–C2–C3–C4).
- Coordination of Ca^{2+} by water molecules (with $d_0 = 2.3$ Å, $r_0 = 1.4$ Å, $n = 4$, $m = 10$).



Fig. 1 Ball and stick representation of L-Asp ZW^- . C atoms (cyan) are labelled to define the C1–C2–C3–C4 torsional angle. O, H and N atoms are coloured in red, white and blue, respectively. The same labelling is used for L-Asp²⁻, with the amino group deprotonated, and for the D-enantiomers.

Table 1 Collective variables used in this work, as defined in the text

	Asp	Ca + Asp	CaAsp + Asp	CaAsp ₂ + Ca
$d1$		✓		
$d2$		✓		
$d3$		✓	✓	
$d4$				✓
Torsional angle	✓	✓		
Water coordination	✓	✓		

- Coordination of L-Asp ZW^- by water molecules (with $d_0 = 3.1$ Å, $r_0 = 1.4$ Å, $n = 4$, $m = 10$).

Further details of the force field and the computational setup of the various types of simulations are reported in the following subsections and as ESI.†

2.1 Force field parameterisation

The potential model developed by Raiteri *et al.*²⁹ for calcium carbonate, combined with the SPC/Fw water model by Wu *et al.*,²⁴ was used. Although we have recently published an updated model for aqueous calcium carbonate simulation,⁴² the development of the organic parameters pre-dated this development. The force field for both aspartate anions was derived from GROMOS⁴³ with intermolecular parameters obtained from the Automated Topology Builder (ATB) and Repository.⁴⁴

Due to the scarcity of experimental information regarding the structure of water around aspartic acid species, the interactions with water were fitted to match the pair distribution function obtained from *ab initio* molecular dynamics and refined against *ab initio* solvation free energies. Here, Lennard-Jones (LJ and LJ-AB) and Buckingham potentials were used. Charges were also fitted against quantum mechanical data.

The aspartate–aspartate interaction parameters were adopted from the GROMOS force field as obtained from the ATB and Repository without change. The interactions of aspartate with carbonate were derived from the methylammonium–carbonate interactions with the GROMOS force field as obtained from the ATB and Repository without change and from intermolecular carboxylate–carboxylate interactions of aqueous aspartate. The interactions between calcium and aspartate were derived from fitting of Buckingham potentials to gas phase quantum mechanical potential energy surface data, at the $\omega\text{B97X-D3/ma-def2-QZVPP}$ level of theory, for a Ca^{2+} ion interacting with acetate (to derive the Ca–carboxylate repulsion) and methyl amine (for the Ca–N repulsion). A short-range repulsive Lennard-Jones potential for the interaction between calcium and the carboxylate carbon was added to prevent unphysical configurations from occurring in instances where the ion was above the plane of this functional group, as opposed to in the natural bidentate binding structure. More details regarding the parameterisation of the force field for methylammonium and acetate are available in Schuitemaker *et al.*¹⁸ Additional details and the full set of parameters are reported as ESI.†

2.2 Hydration structure

The water structure around the aspartate anions was explored using unbiased classical and *ab initio* molecular dynamics

simulations in an isochoric-isothermal (NVT) ensemble. Classical simulations were run for 10 ns, with the setup described above.

Ab initio simulations were run using the CP2K⁴⁵ program with the BLYP-D3 functional and a Gaussian planewave basis set. Core electrons and nuclei were described using GTH pseudopotentials⁴⁶ with valence basis sets of TZ2P quality. The electron density was described with an auxiliary basis set of planewaves with a cutoff of 400 Ry, while the self-consistent field calculation was performed using the orbital transformation algorithm.⁴⁷ Asp ZW[−] was placed in a cubic cell with length 13.774 Å containing 85 water molecules using an initial configuration derived from equilibration with classical molecular dynamics. Simulations were run for up to 50 ps in the NVT ensemble using a time step of 0.5 fs and the CSV thermostat. A temperature of 330 K was used to compensate for the known systematic over-structuring of liquid water with GGA functionals,⁴⁸ despite the inclusion of an empirical dispersion⁴⁹ correction. Asp^{2−} was treated with a similar procedure, except that the box length was 13.088 Å, containing 70 water molecules, and run for up to 32 ps.

2.3 Hydration free energies

Free energy perturbation⁵⁰ was run in the NPT ensemble by progressively switching off the van der Waals' and electrostatic interactions between the anions and water (20 equally spaced stages of 5 ns each per interaction, with 500 ps equilibration). To account for the partial screening of the 1–4 interactions leading to a non-zero internal energy, an additional gas-phase calculation was performed to remove the electrostatic interactions. The calculated hydration free energy values were then corrected for finite size effects.⁵¹

Due to scarce experimental reference values, quantum mechanical calculations were performed to estimate the free energy of hydration. Three different approaches were used to examine the sensitivity of the computed value. In the first approach, the molecules were optimised using Density Functional Theory (DFT) with the M06 meta-GGA hybrid exchange–correlation functional,⁵² in conjunction with a 6-31+G** Gaussian basis set, with or without the SM8 implicit solvation model⁵³ using QChem version 6.0.1.⁵⁴ The second set of quantum mechanical calculations using implicit solvent were performed using ORCA⁵⁵ with the SMD solvation model,⁵⁶ either alone or with a first solvation shell of 7 explicit waters. For these calculations, the ω B97X-D3 functional and ma-def2-QZVPP basis set were used as they have been shown to yield good thermochemistry against benchmark datasets. In order to extract the hydration free energy for the case where explicit water is included, the cluster method was used with a water hexamer as the reference water cluster.⁵⁷

2.4 Conformation of aspartate anions in water

In order to estimate the rotational barriers and preferred conformations of both enantiomers of Asp ZW[−] and Asp^{2−} in water, a scan of the C1–C2–C3–C4 torsional angle (Fig. 1) was conducted in the NVT ensemble using metadynamics as described above. The torsional angle was the only collective

variable and 24 individual walkers were run until convergence, resulting in a cumulative simulation time of 240 ns.

2.5 Ion pairing and cluster formation free energies

Metadynamics, with the setup described above, was used to simulate the free energy profile of ion pairs and cluster aggregation in water. Subsets of 1 to 3 of the following collective variables were used; the calcium–water coordination, the C–C–C–C torsional angle of the anions, the distance between each carboxylate group with calcium ions (d_1 , d_2) and the distance between COM of the aspartate anions and calcium (d_3). For the formation of Ca₂Asp₂ clusters, the distance Ca–Ca (d_4) was used as a collective variable. Details of the collective variables are reported in Table 1 and related discussion. Simulations were run for a total time of >1 μ s for the ion pairs and >0.5 μ s for the cluster, using 24 parallel walkers. All binding free energies reported in this paper include correction to the standard state.

To reduce the collective variable space and speed up sampling, an upper wall at 20 Å was applied to distance collective variables with a spring constant of 0.1 eV Å^{−2}. In cluster simulations, to keep the pre-formed cluster together, a second upper wall at 7.5 Å, again with a spring constant of 0.1 eV Å^{−2}, was applied to the calcium–COM distance(s) that was (were) not being biased.

3 Results and discussion

3.1 Hydration structure and free energy

Interatomic interactions between the aspartate anions and water were parametrised to reproduce pair distribution functions obtained from *ab initio* molecular dynamics, as well as the *ab initio* hydration free energy. Fig. 2 shows that the structure of water around aspartic acid functional groups is reproduced with very similar accuracy by the force field and *ab initio* methods. In particular, very good agreement is observed for the position of the first and the second peaks in all the plots.

Table 2 summarises the results of calculations of the hydration free energies for the aspartate species. Unfortunately, there are no experimental data to compare against, while the quantum mechanical results show some degree of variation depending on the treatment of solvation. Arguably QM2 is likely to be the most accurate value as it uses the highest level of theory, largest basis set and a shell of explicit water. A complication in comparing the force field hydration free energies to those computed quantum mechanically is that the aspartate zwitterion is unstable in the gas phase due to the proton on the amino group migrating to the carboxylate group. As a result, there is a large relaxation contribution in the quantum mechanical energy that cannot be accounted for by an unreactive force field where bonding is fixed. One solution to this is to focus on the free energy difference between the gas phase and solvated state at the optimised geometry for the aqueous state. Based on this approach, the hydration free energies for method QM1 (labelled as QM1* in the table) would be −356.2 and −945.0 kJ mol^{−1} for

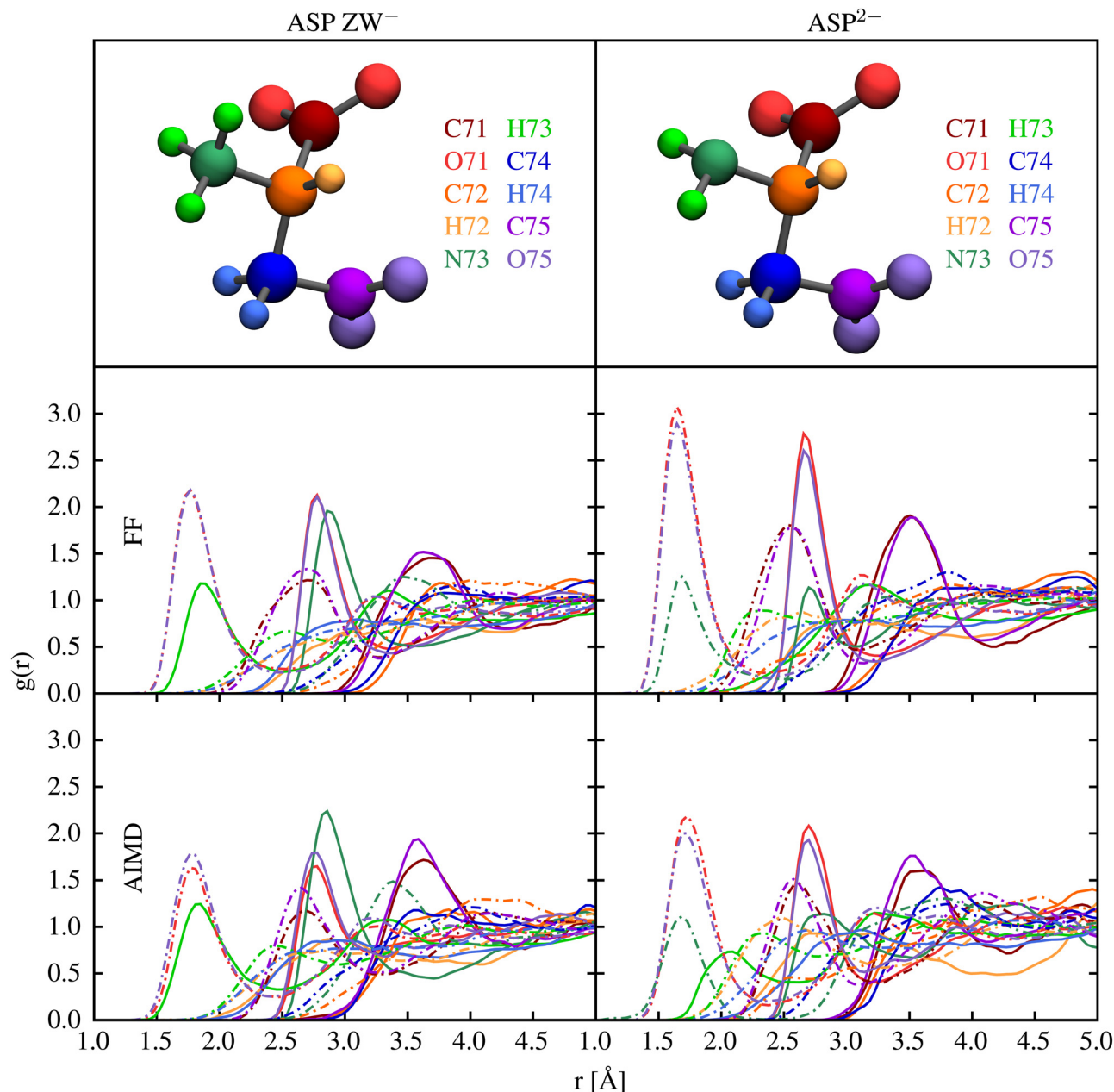


Fig. 2 Pair distribution functions, $g(r)$, between the atoms of the aspartic acid species and the hydrogen (dash-dotted lines) and oxygen (solid lines) of water calculated with our force field (FF) and *ab initio* molecular dynamics (AIMD). Plots are coloured according to the atoms represented in the top figures.

Table 2 Solvation free energies (ΔG [kJ mol⁻¹]) at 300 K obtained with the force field (FF) and with three DFT approaches (QM1 = SM8-M06/6-31+G**^{*}; QM1* = QM1 without gas phase relaxation; QM2 = SMD/ ω B97X-D3/ma-def2-QZVPP with 7 explicit water molecules; QM3 = SMD/ ω B97X-D3/ma-def2-QZVPP without explicit water)

	FF	QM1*	QM1	QM2	QM3
Asp ZW ⁻	-430.6	-356.2	-291.5	-294.9	-291.1
Asp ²⁻	-1018.1	-945.0	-879.1	-846.8	-839.4

the two species. This substantially reduces the discrepancy between the force field and quantum mechanical data.

Attempts to further reduce the difference between the force field and quantum-mechanical hydration free energies were unsuccessful, in that any improvement came at the expense of the reproduction of the pair distribution functions. Use of polarisable force fields in future work may be able to simultaneously describe the hydration thermodynamics and structure.

3.2 Conformational energy profiles of aqueous aspartate anions

Comitani *et al.*⁵⁸ provided an in-depth overview of the conformational profile of aspartic acid and its neutral zwitterion in the gas phase and in water, respectively, using classical

molecular dynamics and *ab initio* methods. The CHARMM36⁵⁹ parametrisation was used for aspartic acid species in conjunction with the TIP3P²³ water model. While we argued in Section 1 that such models suffer from a number of limitations in the context of biomineralization, this study provides a comparison of the main findings with results obtained with other classical force fields, DFT and second order Møller-Plesset perturbation theory (MP2), highlighting aspects on which there is a very good qualitative agreement between all methods. Therefore, this paper will be used as the main reference in this discussion.

Comitani *et al.*⁵⁸ identified the full set of torsional angles for the conformers of aspartic acid and of its neutral zwitterion. They highlighted that the majority of states are separated by rotational barriers that are fully accessible by unbiased molecular dynamics calculations, the exception being the C1–C2–C3–C4 torsional angle (named β in the original paper and labelled as C4–C3–C2–C1 with respect to Fig. 1) and the two C–C–O–H torsional angles (δ and ζ). For clarity of comparison with Comitani *et al.*,⁵⁸ in the remainder of this paper we will refer to the C1–C2–C3–C4 torsional angle as $-\beta$. Both species considered in this paper, *i.e.* the negative zwitterion Asp ZW[−] and Asp^{2−}, have both carboxylic acid groups deprotonated, meaning that only $-\beta$ is relevant to the conformational analysis.

The free energy profile along $-\beta$ for both species, in their D- and L-enantiomers, is shown in Fig. 3. As expected, Asp ZW[−] and Asp^{2−} have profiles that are nearly indistinguishable and the enantiomers have mirror-image profiles. Three minima are present at around 60, -60 and ± 160 degrees, as also found in Comitani *et al.*⁵⁸ (where the last minimum is shifted toward 170 degrees). In particular, L-enantiomers favour the conformation at $-\beta = +60^\circ$ and the second most stable conformation is

at $-\beta = +160^\circ$, whereas the D-enantiomers have their absolute free energy minimum at $-\beta = -60^\circ$ and the second lowest energy minimum at $-\beta = -160^\circ$. To confirm that our simulations are fully capturing the dynamics of the molecule, an additional scan of the L-Asp ZW[−] torsional angle was run for a total of 120 ns using the water coordination number as a second collective variable. The 1-dimensional free energy profiles of the $-\beta$ torsional angle, projected from the resulting 2-dimensional free energy surface, fully overlap with those obtained above.

Table 3 shows the relative free energies of the L-Asp minimum energy conformers. The results of Comitani *et al.*⁵⁸ for the zwitterion (L-ZW), calculated with their force field, hybrid DFT (B3LYP) and MP2, are compared with those obtained in this work for the negative zwitterion (L-ZW[−]). Here, Comitani *et al.* calculated the energy for all L-ZW minima resulting from the rotation around both β and δ torsional angles, combined. However, δ cannot be defined in ZW[−] because both carboxylic acid groups are deprotonated. Therefore, there are only three possible minima in L-ZW[−], resulting from the rotation around β , and their energy has been compared to the equivalent L-ZW conformer with δ in its most energetically favourable conformation. DFT, MP2 and our force field predict the same stability order for the three conformational minima, with $-\beta = 60^\circ$ and $-\beta = -60^\circ$ being the most and least stable ones, respectively. Results obtained with our force field are in reasonable quantitative agreement with MP2 calculations. The force field by Comitani *et al.*⁵⁸ predicts the conformation at $-\beta = 170^\circ$ as the most stable one and the conformation at $-\beta = 60^\circ$ as slightly more stable than that at $-\beta = -60^\circ$.

Activation barriers between the three minima are between 3 and 9 *kT*. A qualitative comparison with the force field results of Comitani *et al.*⁵⁸ is reported in Table 4 and shows that with both models the transitions between the conformation at $-\beta = 60^\circ$ and those at $-\beta = 160^\circ$ (L-ZW[−]) and 170° (L-ZW) are the ones with the lowest barrier, whereas the other transitions are more energetically expensive. The main question here is



Fig. 3 Free energy profiles for the torsional angle of the two enantiomers of Asp ZW[−] and Asp^{2−} in water.

Table 3 Relative free energies [kJ mol^{−1}] of the minimum energy L-Asp conformers as obtained by Comitani *et al.*⁵⁸ for the zwitterion (L-ZW) and in this work for the negative zwitterion (L-ZW[−])

$-\beta$	L-ZW ⁵⁸			L-ZW [−]
	FF	B3LYP	MP2	FF
+60	1.8	0.0	0.0	0.0
−60	2.0	8.6	10.8	11.4
+170/+160	0.0	0.9	3.9	6.2

Table 4 Free energy barriers [kJ mol^{−1}] for the rotation around the $-\beta$ torsional angle of L-Asp conformers as obtained by Comitani *et al.*⁵⁸'s force field for the zwitterion (L-ZW) and in this work for the negative zwitterion (L-ZW[−]). Only ranges of values are available for L-ZW

$-\beta$	L-ZW ⁵⁸	L-ZW [−]
+60 → +160 (L-ZW [−]) or +170 (L-ZW)	18.8–25.1	9.3
+60 → −60	37.6–44.0	21.0
+160 (L-ZW [−]) or +170 (L-ZW) → −60	37.6–44.0	21.3

whether classical dynamics simulations are able to access these barriers and to fully explore the conformational space of this molecule. Therefore, we ran 5 ns of unbiased molecular dynamics simulation with our force field model starting from the most stable conformation of L-Asp ZW⁻ at about $-\beta = 60^\circ$. Here, the conformation at $-\beta = 160^\circ$ was visited a few times whereas the conformation at $-\beta = -60^\circ$ was visited only once. This means that the β torsional angle should be used as a collective variable in free energy calculations to fully capture the dynamics and energy profile of processes involving aspartic acid species. Accelerating the conformational dynamics might be crucial when exploring the binding with other species and mineral surfaces, as the most stable conformation of the free solvated molecule might not necessarily correspond to the most favourable conformation of the same molecule when bound.

3.3 Ion pairing free energies

This section presents a detailed analysis of the ion pairing dynamics and free energy of Ca²⁺ L-Asp ZW⁻. The choices associated with using different sets of collective variables and the implications of such choices are discussed for this specific case. The same tests are repeated and commented on for Ca²⁺ L-Asp²⁻. The most convenient set of collective variables is then used to investigate the ion pairing free energy profile and dynamics between calcium and the D-aspartic acid species.

3.3.1 Choice of collective variables: Ca²⁺ L-Asp ZW⁻. The pairing free energy profile between Ca²⁺ and L-Asp ZW⁻ was computed through metadynamics using the $-\beta$ torsional angle and the distances between each of the carboxylate functional groups and calcium (d_1 and d_2) as collective variables. The pairing free energy is projected along d_1 and d_2 in Fig. 4 (with d_1 and d_2 defined in Fig. 5), and shows a preference for a solvent-shared (SSHIP) interaction, while the formation of contact ion pairs (CIP) is strongly disfavoured. The free energy surface is found to be asymmetric, meaning that the two carboxylate functional groups bind differently to Ca²⁺. In the same figure, the rotational free energy profile of the molecule around the $-\beta$ torsional angle is shown for a subset of local minima of the pairing free energy map, demonstrating that the relative stability of each minimum and the rotational barriers can vary significantly depending on L-Asp ZW⁻ being free or bound. This result alone shows that atomic-level investigations of cluster aggregation and adsorption events involving molecules with flexible conformations should always start with an accurate analysis of which collective variables can provide a dynamically and thermodynamically accurate description of the system.

In this specific case, the conformational free energy profile changes only for contact ion pairs, which are energetically disfavoured. To assess the effect of including $-\beta$ as a collective variable on the overall accuracy of the pairing free energy, the latter was also computed using only d_1 and d_2 as collective variables and the results compared with those discussed above. Fig. 5 shows the monodimensional free energy profiles projected along the d_1 and d_2 distances, obtained with and without using $-\beta$ as a collective variable. Here, minima are the

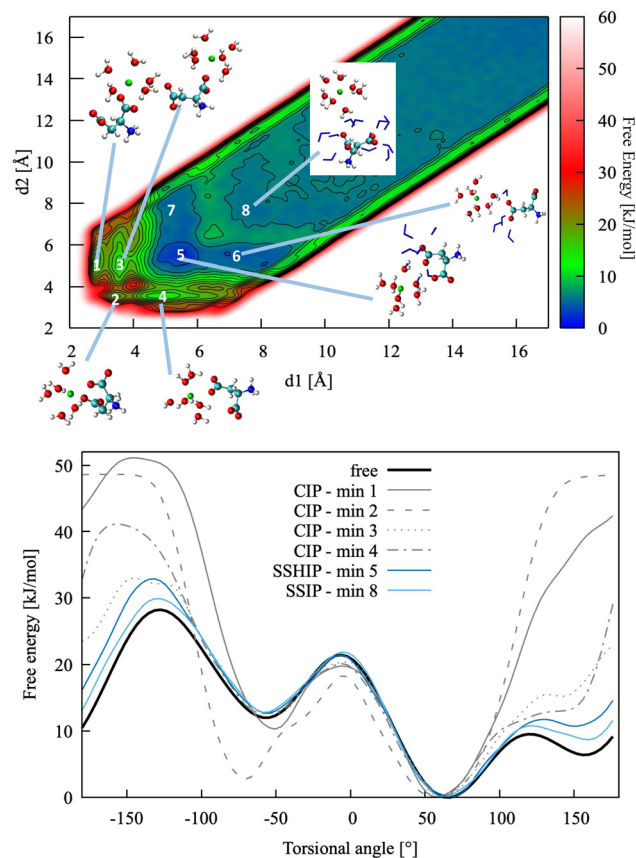


Fig. 4 Top: Pairing free energy of Ca²⁺ L-Asp ZW⁻ projected along two Ca-C distances, d_1 and d_2 (defined in Fig. 5). Minima correspond to contact ion pairs (CIP, 1 to 4), solvent-shared ion pairs (SSHIP, 5 to 7) and solvent-separated ion pairs (SSIP, 8). Examples of configurations for each minimum are provided, with Asp atoms coloured as in Fig. 1, Ca atoms coloured in green, water molecules belonging to the calcium solvation sphere coloured in white (H) and red (O), and water molecules belonging to the solvation sphere of the COO⁻ closest to calcium represented as blue sticks. Bottom: Rotational free energy around the $-\beta$ torsional angle of L-Asp ZW⁻, free and bound with Ca²⁺.

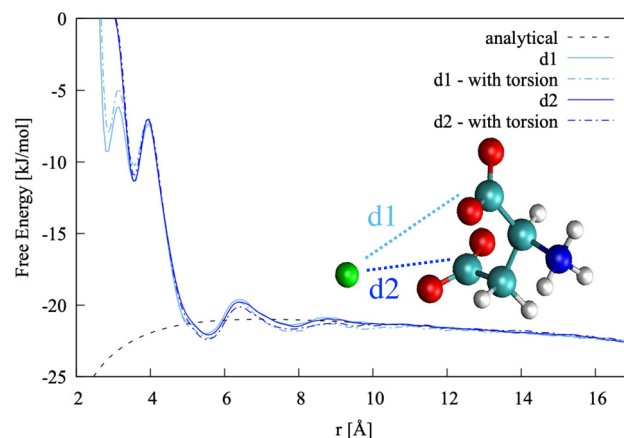


Fig. 5 Pairing free energy of Ca²⁺ L-Asp ZW⁻ projected along the two Ca-C distances and obtained with and without sampling along the $-\beta$ torsional angle collective variable.

result of mixed states: from left to right, the four minima in $d1$ correspond to state 1, states 2 + 3, states 4 + 5 + 7 and states 6 + 8 of Fig. 4, respectively; the three minima in $d2$ correspond to states 2 + 4, states 1 + 3 + 5 + 6, and states 7 + 8 of Fig. 4, respectively. The four plots overlap nearly exactly in the region above 4 Å due to the solvent-shared states being significantly more stable. Differences between the $d1$ and $d2$ profiles, and between the plots obtained with and without biasing $-\beta$ are observed in the contact ion pair region only.

The pairing free energy can be extracted from our data using the Fuoss^{60,61} equation and it can be used as a quantitative measure of the differences observed above. Results of the integration along the two reaction coordinates are very similar, with $\Delta G_{d1} = -4.27$ kJ mol⁻¹ and $\Delta G_{d1} = -4.42$ kJ mol⁻¹ when rotation around $-\beta$ is sampled. These values become -4.17 and -4.10 kJ mol⁻¹, respectively, when the $-\beta$ torsional angle is not considered as a collective variable, confirming the accuracy of the latter approach for this specific case.

An alternative to using the distance between calcium and each carboxylate group, resulting in having to bias two collective variables, is to use the distance between calcium and COM of the molecule, $d3$. Having to explore only one collective variable would significantly reduce the computational demand, something that becomes crucial when dealing with clusters and more complex systems, at the cost of losing information regarding the atomic contribution of each separate functional group and of the overall dynamics and geometry of the ion pair. This approach would also allow for a more direct comparison with experimental measures.

The pairing free energy between Ca²⁺ and L-Asp ZW⁻ was computed using $d3$ as a collective variable. Direct comparison of the resulting free energy profile with those obtained using $d1$ and $d2$ is reported as ESI† and shows very good agreement, with minima at a slightly higher distance (around 0.5 Å more than for $d1$ and $d2$) due to reference to the COM instead of to the carbon atoms in the COO⁻ groups. The pairing free energy value is $\Delta G_{d3} = -5.0$ kJ mol⁻¹.

In order to ensure that $d3$ can fully capture the dynamics and energetics of the ion pair, a simulation was run using the coordination of calcium with water as an additional collective variable. The resulting 1-D profile along $d3$ is reported as ESI†, showing the binding energy is slightly more negative (by 0.5 kJ mol⁻¹) when the water coordination number around calcium is considered.

The main conclusions of this analysis are listed below and apply to ion pairs and other water-mediated interactions, while noting that differences of 0.5 kJ mol⁻¹ are within the error of the method, but would need to be reassessed in systems dominated by direct-contact interactions:

- Calcium ions bind to L-Asp ZW⁻ weakly in water, and the most stable state is solvent-shared.
- The pairing free energy values obtained with and without biasing the $-\beta$ torsional angle are of comparable accuracy due to the solvent-shared nature of the ion pair.
- The pairing free energy value obtained *via* biasing the two individual distances between the carboxylate groups and

calcium differ by about 0.5 kJ mol⁻¹ from that obtained by using the distance between the COM of the anion and calcium as a sole collective variable, which is within the accuracy of the method.

- The pairing free energy values obtained with and without biasing the water coordination of calcium also differ by 0.5 kJ mol⁻¹.

3.3.2 Choice of collective variables: Ca²⁺ L-Asp²⁻. The free energy profile of this ion pair differs from that described above due to the amino group being deprotonated, resulting in a total charge of $-2|e|$. This affects both the structure of the ion pair and its free energy profile, as shown in Fig. 6 and 7. In particular, the most stable configurations (minima 1 and 2 in Fig. 6) correspond to a direct contact between nitrogen and calcium, and a solvent-shared state between calcium and the C1 carboxylate group. The remaining minimum geometries are comparable to those observed for the zwitterion, with contact interactions between calcium and the carboxylate groups being highly disfavoured.

To further validate this finding, we performed DFT calculations with ORCA using the ω B97X-V level of theory and the triple- ζ basis set, both in the gas phase and with implicit solvent. As a starting configuration, we chose a snapshot extracted from the metadynamics trajectory where the Ca ion is close to the nitrogen and removed all the water molecules that did not belong to the calcium first hydration shell. We then performed a geometry optimisation of the structure first in vacuum and then with the implicit solvent. During the geometry optimisation, the aspartate undergoes a significant conformational rearrangement but the N-Ca distance remains around 2.4 Å. Although these calculations do not provide an indication of what the binding energy of the complex is, they do show that Ca is not immediately repelled by the amino group and suggest that Ca-N is not an unfavourable interaction.

This is also in agreement with the findings of Tang and Skibsted,⁶² though also in their case calculations were not run in explicit solvent and no conformational analysis was performed.

The main conclusions of the analysis of Ca²⁺ L-Asp²⁻ association are listed below. Apart from a few features, they are overall similar to those reported for the zwitterion and show that ion association can be simulated using one collective variable only, *i.e.* the distance between the COM of the anion and calcium, $d3$:

- The pairing free energy between calcium and L-Asp²⁻ is stronger than that between calcium and L-Asp ZW⁻ due to a higher charge and a contact interaction between the amino group and calcium.
- The interactions between calcium and the carboxylate groups are still weak and solvent shared, with contact interactions being highly disfavoured.
- The most stable conformation of L-Asp²⁻ is the same in all the main minimum energy ion pair configurations.
- The pairing free energy values obtained *via* biasing the two individual distances between the carboxylate groups and calcium are -10.9 ($d1$) and -10.5 ($d2$) kJ mol⁻¹, therefore the



Fig. 6 Top: Pairing free energy of Ca^{2+} L-Asp^{2-} projected along two Ca–C distances, $d1$ and $d2$ (defined in Fig. 5). Minima correspond to contact (N–Ca) plus solvent-shared (C–Ca) ion pairs (CSSHIP, 1 and 2), solvent-shared ion pairs (SSHIP, 3 to 6) and solvent separated ion pairs (SSIP, 7). Examples of configurations for each minimum are provided, with atoms coloured as in Fig. 4. Bottom: Rotational free energy profile around the $-\beta$ torsional angle of L-Asp^{2-} , free and bound with Ca^{2+} .

difference with the value obtained by using the distance between COM and calcium ($d3$, $-10.7 \text{ kJ mol}^{-1}$) as a sole collective variable is largely within the accuracy of the method.

3.3.3 Speciation, enantiomers, and comparison to experiments. Based on the analysis presented in the previous section, pairing free energies between calcium and the four species of aspartic acid examined in this paper were computed using $d3$ as the sole collective variable. The free energy values and profiles are reported in Table 5 and Fig. 8, respectively. The positions of the most stable minima confirm a preference for solvent-shared CO_2^- – Ca^{2+} interactions in all cases, and a NH_2 – Ca^{2+} contact interaction for Asp^{2-} species. As expected from its higher negative charge, the latter provides the strongest binding. Differences between the enantiomers are within the accuracy of the method.

Of the few experimental data available in the literature, Tang and Skibsted⁶² provide the latest and most complete dataset of association constants between aspartic acid and calcium at



Fig. 7 Pairing free energy of Ca^{2+} L-Asp^{2-} projected along two Ca–C distance and obtained with sampling along the $-\beta$ torsional angle collective variable.

Table 5 Binding free energies [kJ mol^{-1}] for ion pair and cluster formation at 300 K. The last column contains the collective variable (CV) along which the free energy has been sampled. The cut-off radius has been chosen as the distance corresponding to the maximum between the solvent-shared and the solvent-separated minima, i.e. 7.5 Å for $d3$ and 14.2 Å for $d4$

Asp ZW^-	ΔG	CV
$\text{L}^- + \text{Ca}^{2+}$	–5.0	$d3$
$\text{D}^- + \text{Ca}^{2+}$	–5.5	$d3$
$\text{CaL}^+ + \text{L}^-$	–2.3	$d3$
$\text{CaL}^+ + \text{D}^-$	–3.0	$d3$
$\text{CaL}_2 + \text{Ca}^{2+}$	–4.8	$d4$
$\text{CaLD} + \text{Ca}^{2+}$	–4.6	$d4$

Asp^{2-}	ΔG	
$\text{L}^{2-} + \text{Ca}^{2+}$	–10.7	$d3$
$\text{D}^{2-} + \text{Ca}^{2+}$	–11.6	$d3$
$\text{CaL} + \text{L}^{2-}$	–2.9	$d3$
$\text{CaL} + \text{D}^{2-}$	–3.0	$d3$
$\text{CaL}_2^{2-} + \text{Ca}^{2+}$	–11.3	$d4$
$\text{CaLD}^{2-} + \text{Ca}^{2+}$	–11.3	$d4$

various pH and at different concentrations. Here, the pairing free energy measured between pH = 6 and pH = 8 (where Asp ZW^- is the dominant species, $\text{pK}_{a1} = 1.88$ and $\text{pK}_{a2} = 3.65$ ⁶³) at 298 K ranges from -5.61 to $-6.43 \text{ kJ mol}^{-1}$, which is in very good agreement with our calculations for the Ca^{2+} – Asp ZW^- ion pair. The pairing free energy measured at pH = 10 (where Asp^{2-} is the dominant species, $\text{pK}_b = 9.60$ ⁶³) is $-9.78 \pm 0.05 \text{ kJ mol}^{-1}$, which is also in good agreement with our calculations for the Ca^{2+} – Asp^{2-} ion pair. The calculated values show a slight over-binding (pairing free energy of -10.7 and $-11.6 \text{ kJ mol}^{-1}$ for the L^- and D^- -enantiomers, respectively), but the difference between the calculated and the experimental values is close to the calculation error bar.

Tang and Skibsted⁶² also provide an estimation of the average binding at neutral or acidic pH (K_{zwitter}) and at alkaline pH (K_{base}) obtained through fitting their data collected at various pH values. The pairing free energy in this case is -5.68 and $-10.31 \text{ kJ mol}^{-1}$ for the zwitterion and the fully

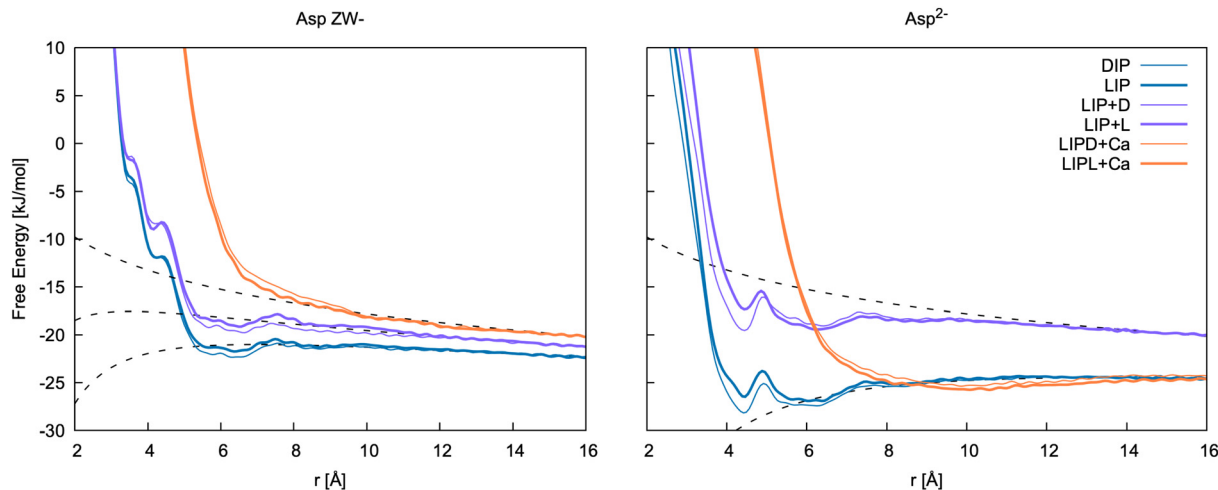


Fig. 8 Free energy profiles for the formation of ion pairs and clusters of Asp ZW⁻ and Asp²⁻ with Ca²⁺. DIP and LIP: ion pair between calcium and D-/L-aspartate; LIP + D and LIP + L: association between LIP and L-/D-aspartate; LIPD/L + Ca: association between LIP + D/L cluster and calcium. r is d_3 for LIP, DIP, LIP + L and LIP + D, and the distance between Ca²⁺ in the cluster and Ca²⁺ ions for LIPD + Ca and LIPL + Ca. The binding free energies determined from these 1D profiles are included in Table 5.

deprotonated aspartate, respectively. These values are, again, fully in line with our results.

A few other studies are available in the literature that provide experimental calcium aspartate binding free energies, most of which are in overall good agreement with our and Tang and Skibsted's⁶² values. Blaquiere and Berthong⁶⁴ provide similar values for the binding free energies of both species with calcium; -6.52 ± 0.95 kJ mol⁻¹ (Asp²⁻) and -6.78 ± 0.18 kJ mol⁻¹ (Asp ZW⁻). To obtain these values, we have assumed the same notation as in Covington *et al.*⁶⁵ was used in this paper. As only values for β_{MLH} are reported, we used the value of β_{HL} from Covington *et al.*⁶⁵ to estimate the Ca–Asp ZW⁻ binding free energy. Later, Maeda *et al.*⁶⁶ provided values of -11.42 and -6.97 kJ mol⁻¹ for the binding free energy of calcium with Asp²⁻ and Asp ZW⁻, respectively. Similar values, though slightly more binding for Asp ZW⁻, were measured by Covington *et al.*⁶⁵ using two different electrodes; -10.68 ± 1.21 and -11.89 ± 0.29 kJ mol⁻¹ for Ca–Asp²⁻, and -8.67 ± 1.72 and -9.88 ± 0.80 kJ mol⁻¹ for Ca–Asp ZW⁻.

3.4 Formation of Ca–Asp clusters in solution

The formation of homochiral clusters of aspartic acid species was identified as a main factor responsible for the formation of chiral toroids of vaterite by Jiang *et al.*^{13,14} While investigation of the structure and dynamics of such species at the calcium carbonate surface is beyond the scope of this paper, simulations were run to assess whether such clusters can form in solution, and whether there is any preference in forming homochiral aggregates in solution.

Free energies of formation are reported in Table 5 and free energy profiles in Fig. 8. These data show weak binding, of the same magnitude of the ion pairs, with CO₂²⁻–Ca²⁺ interactions mediated by water in a solvent-shared mode and with weak contact between NH₂–Ca²⁺ at high pH. There is no significant difference between homochiral and heterochiral interactions.

For comparison to the free energies determined in aqueous solution using the present force field, the relative energies of homo- vs. hetero-chiral clusters of aspartate with calcium were determined in the gas phase using quantum mechanical calculations at the ω B97X-D3/ma-def2-QZVPP level of theory, as used earlier for the hydration free energies. In this case, the homochiral cluster was found to be more stable by 93.1 kJ mol⁻¹ for Asp ZW⁻ and 26.3 kJ mol⁻¹ for Asp²⁻ based on the internal energy at the optimised structure. Inclusion of zero point energy and thermal corrections to room temperature increased the values by only 0.3 and 0.7 kJ mol⁻¹, respectively. While this confirms the expected preference for homochiral complexes in the gas phase, it is harder to validate the lack of clear preference in solution. Inclusion of a continuum solvent model (SMD) is found to greatly reduce the preference for homochiral clusters (*e.g.* for Asp ZW⁻ with Ca²⁺ the internal energy difference drops to 22.4 kJ mol⁻¹), though a stability difference remains. This is likely to be as much a reflection on the approximate nature of continuum solvation as it is suggestive of a discrepancy with the force field model.

4 Conclusions

This paper presents an in-depth analysis of the dynamics of aspartic acid species and of their association with calcium ions in water at pH values relevant to biomineralization.

A new classical model was developed that provides results consistent with first principles data, such as hydration structure and free energy, as well as conformational free energy differences. The model was then applied to the calculation of ion pairing free energy profiles, obtaining values that are in agreement with experiment. A weak and solvent-shared association was observed between aspartic acid species and calcium, resulting in a weak binding to form aqueous clusters,

and in no difference in the formation free energy of homochiral vs. heterochiral clusters.

The simulations presented in this paper show that modelling molecules with conformational freedom in the context of biomineralization comes with additional levels of complexity, due to the fact that different conformations can be more or less stable depending on whether the molecule is free or bound. In fact, if the rotational free energy barrier is high, an appropriate bias needs to be added to accelerate the dynamics.

In the specific case of aspartic acid species, we found that some of the activation barriers between different conformations are not accessible with unbiased molecular dynamics. Additionally, the most stable conformation of bound (contact interaction) and solvent-shared or free aspartic acid species are different. While this turned out to be irrelevant for ion pairs, due to their solvent-shared nature, whether or not to bias the torsional angle would need to be reassessed in systems dominated by direct-contact interactions (e.g. mineral surfaces).

Author contributions

RD planned the research and wrote the manuscript, with inputs from all authors. AS and RD ran and analysed most calculations. JDG ran and analysed most first principles calculations. KBK, PR, JDG and RD developed the force field model.

Conflicts of interest

There are no conflicts to declare.

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