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Electron–phonon coupling and superconductivity in a 2D Tl–Pb compound on Si(111)

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Electron–phonon interaction in a single-layer Tl–Pb compound on Si(111) is investigated within the density-functional theory and linear-response approach in the mixed-basis pseudopotential representation. It is found that phonon-induced scattering of electrons at the Fermi level is primarily determined by surface electronic states responsible for bonding at the interface and by low-energy, predominantly shear-vertical vibrations of adatoms. The contribution of substrate-localized vibrations involved in the electron–phonon scattering turns out to be small. We have also estimated the superconducting transition temperature T_c by solving the linearized gap equation of the Eliashberg theory. An analysis of phonon-mediated transitions for a number of electronic states in the Tl–Pb surface bands showed that the strength of the coupling varies with the binding energy, increasing as it approaches the Fermi level, and significantly depends on the surface band to which the state belongs.

1 Introduction

Advances in nanotechnology have stimulated an active interest in two-dimensional 2D metallic films grown on semiconductor substrates due to their potentially advanced properties such as the discovered two-dimensional superconductivity.^{1–13} For example, two-dimensional superconductivity was found for the striped incommensurate (SIC) phase of Pb on Si(111) and for the quasi-rectangular Si(111) – $\sqrt{7} \times \sqrt{3}$ – In reconstruction.⁵ The scanning tunneling spectroscopy measurements (STS) demonstrated that one (two) atomic layers of Pb (In) were quite enough to retain superconductivity and showed that the structures become superconducting at $T_c = 1.83$ K and $T_c = 3.18$ K, respectively. The discovery of superconductivity was followed by a number of theoretical works which focused on the strength of the electron–phonon (e–ph) interaction and the critical temperature of superconductivity in Pb/Si(111) and In/Si(111) systems.^{9,14–17}

The experimental findings have also stimulated research activity on exploring other ultrathin superconductors, among them, a surface compound formed by metallic adsorbates, Tl and Pb, on Si(111) and Ge(111) surfaces.^{11–13,18–20} Both heavy metals are bulk superconductors with strong spin–orbit coupling. When alloying one monolayer (ML) of Tl with 1/3 ML of Pb a single atomic layer Tl–Pb compound with $\sqrt{3} \times \sqrt{3}$ periodicity is formed. The surface

metal phase exhibits both a noticeable Rashba-type spin splitting of surface electronic bands and 2D superconducting transport properties.^{12,19} The low-temperature conductivity measurements¹² showed that the Si(111) – $\sqrt{3} \times \sqrt{3}$ – (Tl – Pb) becomes superconducting at the critical temperature of 2.25 K.

Since the atomic arrangement and the electronic band structure of the compound have already been experimentally established,^{11,13} the available information can be used as a basis for further theoretical investigations. First of all, it seems useful to study the phonon-mediated scattering of electrons in the surface metallic bands of the Si(111)-supported Tl–Pb compound to obtain an accurate quantitative description and analysis of the e–ph interaction, which is still missing.

Here we present the results of a first-principles study focusing on the pairing strength of phonon-induced scattering processes in the Si(111) – $\sqrt{3} \times \sqrt{3}$ – (Tl – Pb) compound. We calculated both the e–ph coupling parameter and Eliashberg spectral function, averaged over electron momentum at the Fermi energy, E_F . Then, the superconducting transition temperature was estimated by solving the linearized gap equation. We also analyzed the strength of e–ph interaction in a number of fixed electronic states in the surface Tl–Pb bands.

2 Calculation details

The Eliashberg spectral function averaged over electron momentum at the Fermi level can be expressed as

$$\alpha^2 F(E_F; \omega) = \frac{1}{\hbar N(E_F)} \sum_{\mathbf{q}, \nu} \delta(\omega - \omega_{\mathbf{q}\nu}) \times \sum_{\mathbf{k}, i, f} \delta(\varepsilon_{\mathbf{k}i} - E_F) \left| \mathbf{g}_{\mathbf{k}+\mathbf{q}f, \mathbf{k}i}^{\mathbf{q}\nu} \right|^2 \delta(\varepsilon_{\mathbf{k}+\mathbf{q}f} - E_F), \quad (1)$$

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where $g_{\mathbf{k}+\mathbf{q},\mathbf{k}i}^{q\nu}$ is the e-ph matrix element, $\varepsilon_{\mathbf{k}i}$ and $\varepsilon_{\mathbf{k}+\mathbf{q}f}$ are energies of initial (i) and final (f) electronic states, and $N(E_F) = \sum_{\mathbf{k}i} \delta(\varepsilon_{\mathbf{k}i} - E_F)$ is the density of electronic states at the Fermi energy. The summation is carried out over (i) all combinations of electronic states ($\mathbf{k}i$) and ($\mathbf{k} + \mathbf{q}f$) and (ii) all phonon modes (\mathbf{q}, ν). Because of the slow convergence of Fermi-surface averages we used a dense mesh²¹ of k -points ($48 \times 48 \times 1$) corresponding to 217 special points in the irreducible part of the surface Brillouin zone (SBZ).

The averaged strength of electron-phonon interaction is related to the Eliashberg function by²²

$$\lambda(E_F) = \int_0^\infty \lambda(E_F; \omega) d\omega = 2 \int_0^\infty \frac{\alpha^2 F(E_F; \omega)}{\omega} d\omega. \quad (2)$$

All calculations were carried out within the density-functional formalism (DFT) and the generalized gradient approximation (GGA-PBE) for the exchange-correlation functional²³ using the mixed-basis pseudopotential approach.^{24,25} The scheme employs a combination of local

functions and plane waves for representing valence states.²⁴ For ground state calculations we used an implementation of the mixed-basis method by Meyer *et al.*²⁶ The norm-conserving pseudopotentials were constructed following the scheme of Vanderbilt.²⁷ For Tl, the semicore $5d$ states were treated explicitly as valence states for greater accuracy.²⁸ By using d -type local functions at each atomic site of Tl, the cutoff energy for plane waves is reduced to 20 Ry without loss of accuracy. Dynamical properties were calculated using the linear response theory²⁹ adapted to the mixed-basis pseudopotential approach.²⁵ In the self-consistent calculations the integrations over the SBZ were performed by sampling a uniform ($12 \times 12 \times 1$) k -point mesh in combination with a Gaussian broadening with a smearing parameter of 0.05 eV.

Due to the strong influence of spin-orbit coupling (SOC) on the two-dimensional electronic bands (spin splitting) of the $\text{Si}(111) - \sqrt{3} \times \sqrt{3} - (\text{Tl} - \text{Pb})$ compound,¹² spin-orbit interaction was taken into account. The inclusion of SOC improves the agreement of the calculated bulk phonon dispersion with experiment for both Tl and Pb.²⁸ Details of the spin-orbit

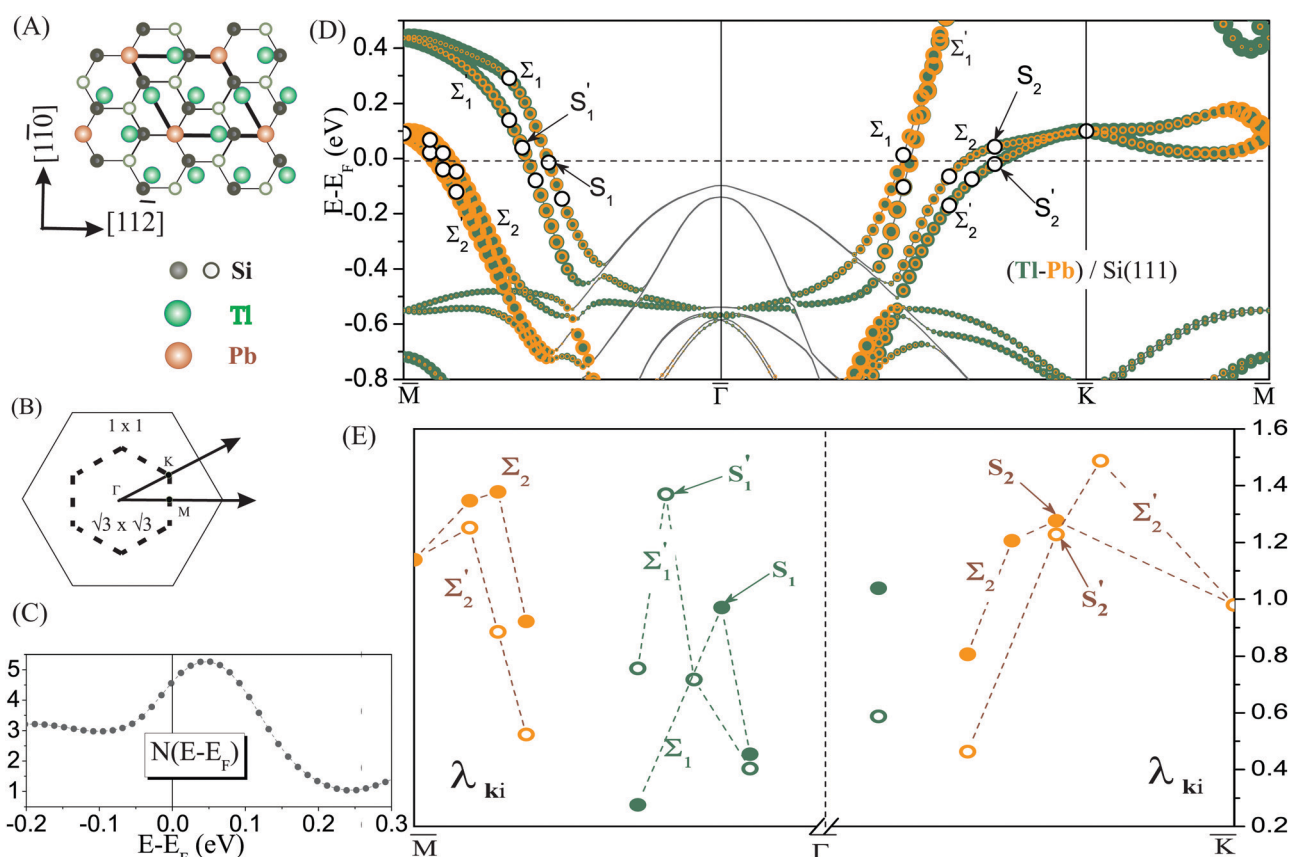


Fig. 1 (A) Top view of the $\sqrt{3} \times \sqrt{3}$ unit cell (bold lines) formed by 2D Tl-Pb compound on Si(111). Big circles correspond to Tl and Pb atoms. Si atoms are shown by full (in the first substrate layer, Si_1) and open (in the second layer, Si_2) small circles. The color assignments are as follows: green, Tl atoms; orange, Pb atoms; gray, Si atoms. (B) The surface Brillouin zones of the 1×1 and $\sqrt{3} \times \sqrt{3}$ structures. (C) Calculated density of electronic states around the Fermi level, in units of states/(eV unit cell). (D) Calculated band structure of the $\sqrt{3} \times \sqrt{3}$ phase formed by a single-layer Tl-Pb compound on Si(111). Circles (green and orange) show electronic bands formed mainly by Tl and Pb orbitals, respectively. The surface electronic states, for which the strength of the e-ph interaction, $\lambda_{\mathbf{k}i}$, is calculated, are marked by open circles. (E) Electron-phonon coupling parameter $\lambda_{\mathbf{k}i}$ as a function of electron momentum for the surface (Tl-Pb) electronic states marked by open circles in (D) in the $\overline{\Gamma M}$ and $\overline{\Gamma K}$ symmetry directions.



coupling implementation within the mixed-basis method can be found in ref. 28.

In our calculation we did not use the +U correction to resolve the band-gap problem. As it is known the DFT may underestimate the bulk band gap but the reduction is not important for analyzing the e-ph interaction in the system of interest. The main point is the position of E_F relative to the substrate valence band edge and the surface band dispersion around E_F .

3 Results and discussion

3.1 Structural parameters

We simulate the system by considering a single-layer-compound on top of periodically repeating six Si(111) layers (a three-bilayer film) separated by a vacuum gap of 12 Å. The imitation of the substrate by three Si bilayers provides practically convergent results on the structural parameters of the $\sqrt{3} \times \sqrt{3}$ phase and, most importantly, is sufficient to reproduce the band dispersion in good agreement with the data obtained for 12 bilayers of Si(111).¹¹ The bottom silicon dangling bonds are saturated with hydrogen atoms.

The lattice constant is first fixed at the theoretical bulk Si lattice parameter $a = 5.402$ Å obtained by total-energy minimization. It is a bit smaller than the experimental value,³⁰ $a_{\text{exp}} = 5.43$ Å. A single-layer Tl-Pb compound is then deposited on the top of the substrate according to the $\sqrt{3} \times \sqrt{3}$ periodicity¹² (see Fig. 1(A)). The superstructure contains three Tl atoms and one Pb atom per unit cell: Tl atoms form a chained-trimer structure and are equivalent with respect to the underlying Si substrate, while 1/3 ML of Pb atoms occupy T_1 (on-top) sites where the Tl trimers are centered.¹² Essentially, the 2D Tl-Pb compound is confined to a single atomic layer, which is slightly buckled because Pb is 0.37 Å (0.34 Å in ref. 18) above the Tl atoms.

The bottom Si bilayer is held fixed to simulate the bulk environment. All other atoms are allowed to move both in-plane and along the stacking direction. The force criterion was chosen so as to ensure complete convergence of bond lengths with an accuracy of less than 0.01 Å. The H-Si distance was determined in the calculation of a Si(111) film saturated by H on both sides. The optimized structural parameters, namely, the bond length $d_{\text{Tl-Tl}}$ and the difference in the heights of atoms at the interface are given in Table 1. Also shown are available experimental data from ref. 18. The optimized Tl-Si₁ height spacing is a bit shorter than the interlayer distance for the Tl(0001) surface,³¹ $h_{\text{Tl-Tl}} = 2.74$ Å. We note that the structural parameters are hardly influenced by the spin-orbit coupling.

Table 1 Bond length, $d_{\text{Tl-Tl}}$, and the height differences, h , between atoms at the interface (in Å). The experimental data are taken from ref. 18

	$d_{\text{Tl-Tl}}$	$h_{\text{Tl-Si}_1}$	$h_{\text{Pb-Si}_1}$	$h_{\text{Pb-Tl}}$	
Si(111)	3.31	2.48	2.86	0.37	Present calc.
	3.34	2.50	2.85	0.34	Expt

3.2 Electron-phonon coupling

Superconducting properties can be associated with enhanced electron-phonon scattering whose strength is described by the e-ph coupling constant. Therefore, we estimated the momentum-averaged strength of the e-ph interaction at E_F . The calculated value $\lambda(E_F) = 1.06$ is close to the e-ph coupling strength obtained at the Fermi level of the Tl(0001) surface, $\lambda^{\text{surf}}(E_F) = 1.01$,³² and both values are larger than the bulk thallium parameter, $\lambda_{\text{theory}}^{\text{bulk}}(E_F) = 0.87$ ²⁸ and $\lambda_{\text{expt}}^{\text{bulk}}(E_F) = 0.795$.³³

In what follows, we will address two main factors that have a significant effect on phonon-mediated electronic transitions. One of the factors determining λ is the phase space, that is, the electronic states available for scattering processes. The calculated density of electronic states at the Fermi level, $N(E_F) = 2.3$ states/(eV unit cell spin), is close to the value at the Fermi energy of the Tl(0001) surface, $N^{\text{Tl(0001)}}(E_F) = 2.12$ states/(eV unit cell spin), the difference is $\sim 8\%$.

To clarify the role of Pb in the formation of the electronic structure of the compound and in the e-ph coupling, we considered the same structure, replacing Pb with Tl. The “hypothetical” (4/3) ML of Tl on Si(111) has a very similar band structure, but when Pb is replaced by Tl, the number of valence electrons in the unit cell decreases and, accordingly, the Fermi level drops. At the new position of E_F , the density of electronic states $N(E_F) = 1.14$ states/(eV unit cell spin) is more than 2 times less than for the Tl-Pb compound. The structure remains dynamically stable, but the e-ph coupling weakens by as much as a factor of 4 to $\lambda(E_F) = 0.28$. Therefore, the reduction of $N(E_F)$ is not the only relevant factor in this case. Fig. 2(B) shows spectral decompositions of the e-ph coupling parameter at the Fermi level, $\lambda(E_F; \omega)$, calculated for the Tl-Pb compound on Si(111) and for the “hypothetical” (4/3) ML of Tl on Si(111). It turns out that at the new position of the Fermi level, long-wavelength lattice vibrations (small-wave-vector phonons) hardly contribute to the scattering of electrons due to a lack of final electronic states. As a result, the spectral e-ph function is strongly suppressed in the low-frequency part up to ~ 3 meV, which drastically weakens the e-ph coupling due to the weighting factor $1/\omega$ in eqn (2). Thus, the role of Pb is twofold: (i) adding valence electrons, which increases the number of available electronic states for the pairing, and (ii) as a consequence of the new position of the Fermi level, activating low-frequency phonons for the pairing by greatly enhancing the probability of transitions mediated by these modes. Both effects lead to a fourfold increase in $\lambda(E_F)$ compared to the “hypothetical” (4/3) ML Tl on Si(111).

Another question is how the different surface bands are involved in the e-ph coupling. Fig. 1(D) shows the calculated band structure around E_F . The SBZ symmetry points are given in Fig. 1(B). The band structure has a metallic character with two spin-split metallic surface bands $\Sigma_1(\Sigma'_1)$ and $\Sigma_2(\Sigma'_2)$, which form the Fermi surface. The spin degeneracy is lifted in the entire SBZ, except for the high-symmetry points. On the one hand, the electronic bands participating in the e-ph interaction are formed by Tl and Pb states of p_x, p_y character (mainly $\Sigma_1 - \Sigma'_1$), which indicates an in-plane metallic Tl-Pb bonding.



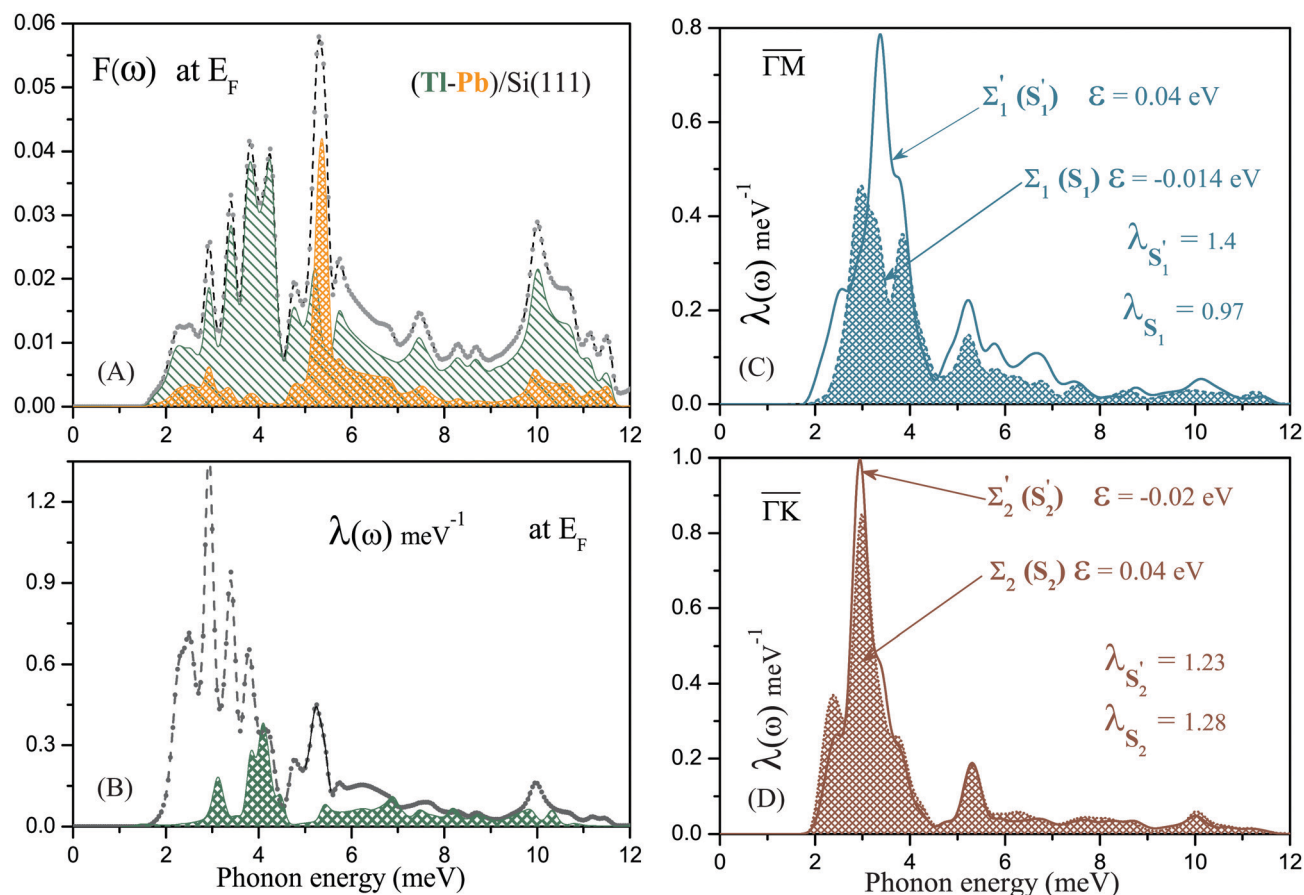


Fig. 2 (A) Calculated phonon density of states $F(\omega)$. The density is given up to 12 meV to show mainly surface localized Tl–Pb modes. Hatched areas show the contribution of Tl- and Pb-localized modes to $F(\omega)$ (green and brown, respectively). (B) Spectral decomposition of the e–ph coupling parameter at the Fermi level, $\lambda(E_F; \omega)$, calculated for the Tl–Pb compound on Si(111) and for the “hypothetical” structure of (4/3) ML of Tl (hatched area) on Si(111). (C and D) Spectral decomposition of $\lambda_{\mathbf{k}i}$ for surface electronic states S_1, S_1', S_2 , and S_2' . Hatched areas show $\lambda_{\mathbf{k}i}$ ’s for states $S_{1(2)}$.

Note that the electronic states localized on Pb atoms are exclusively of the character p_x, p_y within the band gap of the substrate. On the other hand, the bands (mainly $\Sigma_2 - \Sigma_2'$) show a coupling of Tl p_z orbitals to p_z and d_{xz}, d_{yz} orbitals of Si atoms from the topmost valence band. Moreover, these states dominate the density of states at the Fermi level, as they contribute $\sim 87\%$ to the total $N(E_F)$. A detailed description of the surface band structure can be found in ref. 11–13.

On the Tl(0001) surface, an analysis of electronic states with a predominant contribution to the e–ph scattering also revealed that these states partially or completely are of p_z symmetry.³² Thus, the e–ph scattering is dominated by states that build interface bonds in the Si(111) – $\sqrt{3} \times \sqrt{3}$ – (Tl – Pb) compound or interlayer bonds of the Tl(0001) surface, respectively. In contrast, for the “hypothetical” (4/3) ML of Tl on Si(111), the Tl-induced electronic states prevailing in the e–ph coupling are of $p_x p_y$ and s types.

The participation of each electronic band in the e–ph scattering turns out to be proportional to its contribution to the density of states at E_F . The $\Sigma_2 - \Sigma_2'$ bands make the largest contribution to $\lambda(E_F)$, $\sim 83\%$, according to their density of states at E_F , 2.0 states/(eV unit cell). The share of bands $\Sigma_1 - \Sigma_1'$ is only $\sim 11\%$ and $\sim 6\%$ falls on the substrate.

3.2.1 Lattice dynamics and Eliashberg spectral function.

Another factor that affects the e–ph scattering is related to lattice vibrations. Calculated phonon density of states for the $\sqrt{3} \times \sqrt{3}$ – (Tl – Pb) compound on Si(111) is shown in Fig. 2(A). The phonon modes associated with vibrations of Tl and Pb atoms lie below 12 meV, while the vibrations of substrate atoms occupy the high-frequency region extending up to 75 meV. In the energy region up to 5.6 meV, most of the modes are predominantly shear-vertical (SV) with displacements of adatoms along the normal to the surface. The only exception is the lowest broad peak (around 2.4 meV) in $F(\omega)$, associated with both in-plane and out-of-plane shear surface vibrations.

From the spectral decomposition of $\lambda(E_F)$ shown in Fig. 2(B), it is obvious that the phonon-mediated scattering of electrons at the Fermi level is determined by vibrations of Tl and Pb adatoms. In the first place, these are low-energy, predominantly shear-vertical displacements. These modes form a multi-peak structure in $\lambda(E_F; \omega)$ between 2 and 4.5 meV, although some SV vibrations of Tl atoms are coupled to the longitudinal motion of Pb atoms (the highest peak, at about 3 meV). Contribution of shear-vertical Pb modes to $\lambda(E_F)$ shows a peak at ~ 5 –5.5 meV.



Since the position of Tl adatoms relative to the underlying Si surface layer is the same, the contributions to $\lambda(E_F)$ from vibrations of different Tl atoms are identical.

Thus, the vibrations dominating in the phonon-mediated scattering of electrons are concentrated up to ~ 6 meV. The adlayer-localized modes provide $\sim 93\%$ of $\lambda(E_F)$, while the substrate vibrations involved in the scattering of electrons contribute little. The reason is that these vibrations are predominantly high-frequency and, as a consequence, turn out to be much less important in the e-ph interaction because of the definition of λ as proportional to $1/\omega$.

3.2.2 Estimation of T_c . We estimated T_c by solving the linearized gap equation of the Eliashberg theory³⁴ on the imaginary axis. An explicit formula can be found in ref. 35. The linearized gap equation requires as input parameters $\alpha^2 F(\omega)$ and μ^* , the effective Coulomb repulsion. In bulk Pb it is assumed that μ^* is in the range 0.10–0.12, in Tl $\mu^* = 0.11$.^{36,37} We used a typical bulk value $\mu^* = 0.1$ and a reference frequency equal to the calculated logarithmic averaged phonon frequency $\omega_{\log} = 4.1$ meV, which is defined by $\omega_{\log} = \exp[2/\lambda \int_0^\infty d\omega \ln(\omega) \alpha^2 F(\omega)/\omega]$. The resulting transition temperature $T_c = 3.5$ K is higher than the value obtained from transport measurements,¹² $T_c = 2.25$ K.

However, transport measurements at a surface always show a lower value of T_c than that obtained by opening of the superconducting energy gap (STS), due to fluctuation effects inherent in low-dimensional superconductors³⁸ and which can only be detected by STS.⁷ So, for a (4/3)-monolayer of Pb on Si(111), a dense SIC phase, STS measurements⁵ give $T_c = 1.83$ K, while conductivity measurements⁷ showed the superconductivity transition at 1.1 K. The theoretical estimate¹⁶ gives the value T_c for the SIC phase of Pb on Si(111) which is closer to the STS data: $T_c = 1.84$ K with $\mu^* = 0.11$.

The calculated transition temperature for the Si(111) – $\sqrt{3} \times \sqrt{3}$ – (Tl – Pb) compound exceeds $T_c = \sim 2.4$ K for bulk thallium.²² However, the strength of e-ph interaction in the bulk³³ (~ 0.8) is also noticeably less than on the surface, both for Tl(0001) and Si(111) – $\sqrt{3} \times \sqrt{3}$ – (Tl – Pb) ($\lambda(E_F) = 1.06$). Therefore, it is not surprising that $T_c^{\text{bulk}} < T_c^{\text{surf}}$.

3.3 Band-resolved electron-phonon coupling

Besides the e-ph coupling parameter averaged over electron momentum at the Fermi level, we also analyzed phonon-mediated transitions for a number of electronic states in the Tl–Pb surface bands. The states are marked by open circles in Fig. 1(D).

To calculate the strength of the e-ph interaction for a fixed electron state with momentum \mathbf{k} and band index i , the state-dependent Eliashberg spectral function

$$\alpha^2 F_{ki}(\omega) = \sum_{\mathbf{q}, \nu, f} \delta(\varepsilon_{\mathbf{k}+\mathbf{q}f} - \varepsilon_{\mathbf{k}i}) \left| g_{\mathbf{k}+\mathbf{q}f, \mathbf{k}i}^{\mathbf{q}\nu} \right|^2 \delta(\omega - \omega_{\mathbf{q}\nu}) \quad (3)$$

is used in eqn (2). The sum is carried out over final electron states and all possible phonon modes (\mathbf{q} , ν). Since the e-ph matrix elements display quite significant variation throughout the SBZ, a dense mesh of \mathbf{q} -points is required for summation

over wave vectors. Therefore, we first calculated the e-ph matrices using a $12 \times 12 \times 1$ \mathbf{q} -point grid. Then, to improve convergence, denser meshes of \mathbf{q} -points were used up to $48 \times 48 \times 1$. Additional matrix elements were calculated using the Fourier interpolation scheme for changing of the self-consistent potential with respect to atomic displacements, as well as for dynamical matrices.

The strength of e-ph interaction for all states marked with open circles is shown in Fig. 1(E). All these states are located near the Fermi level: their energies are in the range $(-0.2) - (+0.3)$ eV. Nevertheless, there is a significant variation in λ_{ki} 's from 0.3 to 1.5. Spectral decompositions of λ_{ki} for four surface electronic states S_1 , S'_1 , S_2 , and S'_2 are shown in Fig. 2(C and D).

On the whole, for all considered states with the same electron momentum in a pair of neighboring subbands, the e-ph interaction is stronger for the electronic state, the energy of which is closer to the Fermi level. This is due to an increase in the density of electronic states as the Fermi level is approached (Fig. 1(C)). At energies very close to E_F or slightly higher, surface bands at the SBZ boundary come into play, sharply increasing the phase space for the scattering of electrons. For states in a pair of neighboring subbands with close binding energies, but different electron moments, the strength of e-ph interaction depends markedly on the surface band to which the states belong.

Both S_1 (band Σ_1) and S'_1 (band Σ'_1) are surface states of s , $p_{x,y}$ symmetry. The only difference between them is that in S'_1 the contribution of Tl p_z -type orbitals becomes noticeable. λ_{ki} 's differ in these two subbands, namely, $\lambda_{ki}^{\Sigma'_1}$ is substantially larger than $\lambda_{ki}^{\Sigma_1}$, as the spectral functions in Fig. 2(C) reveal. The calculated λ_{ki} 's show the same trend as the values roughly estimated experimentally for the Σ_1 (Σ'_1) bands from the slope of the temperature-dependent linewidth:¹² $\lambda_{\Sigma_1}^{\text{exp}} = 1.6 \pm 0.1$ and $\lambda_{\Sigma'_1}^{\text{exp}} = 0.7 \pm 0.1$.

As for the states S_2 and S'_2 , they do not differ in symmetry and both are characterized by the presence of a significant fraction of Tl p_z orbitals responsible for the coupling to the topmost valence band Si states. As a result, the corresponding λ_{ki} 's are equally large. At binding energies of about 60–200 meV, the calculated strength of the e-ph interaction in the Σ_2 (Σ'_2) bands varies from 0.46 to 0.8, and the averaged value of $\lambda_{ki} \approx 0.65$ is close to the value extracted for the same bands from the ARPES data,¹² $\lambda^{\text{exp}} = 0.6 \pm 0.05$. However, when approaching the Fermi level, the e-ph interaction in these two neighboring subbands with opposite spin orientations enhances drastically and $\lambda_{ki} \rightarrow 1.4$ –1.5 depending on electron momentum.

4 Conclusions

We have presented the results of an *ab initio* study of the electron-phonon coupling in the two-dimensional Tl–Pb compound on Si(111). The calculated $\lambda(E_F) = 1.06$ coincides with the e-ph coupling strength at the Fermi level of the Tl(0001) surface and both values are larger than the bulk thallium parameter.



It is found that bands $\Sigma_2(\Sigma'_2)$ make a decisive contribution ($\sim 83\%$) to $\lambda(E_F)$, proportional to their large density of states at E_F compared to the $\Sigma_1(\Sigma'_1)$ bands. The phonon-mediated scattering of electrons at the Fermi level is almost completely controlled by the vibrations of Tl and Pb atoms, predominantly by low-energy shear-vertical modes. Much less important are the high-frequency substrate-localized phonons participating in the scattering of electrons. The calculated superconducting transition temperature $T_c = 3.5$ K is higher than the value extracted from transport measurements.¹² An analysis of phonon-mediated transitions for a number of electronic states in the Tl-Pb surface bands showed that λ_{ki} varies with the binding energy, increasing as the Fermi level is approached, and at the same binding energy the strength of e-ph interaction depends on the surface band.

Conflicts of interest

There are no conflicts to declare.

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