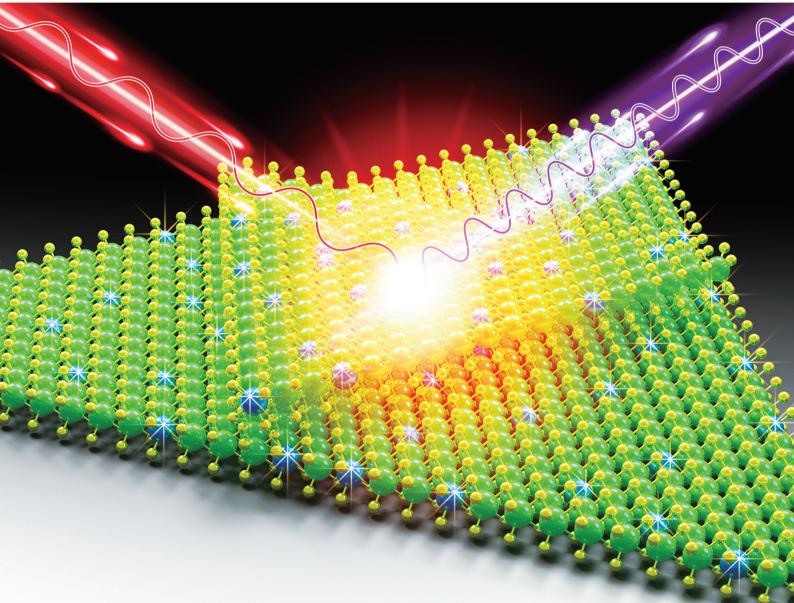
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Inversion symmetry broken in 2H phase vanadiumdoped molybdenum disulfide†

Hanjun Jiang,<sup>‡a</sup> Lu Zheng,<sup>‡a,b,c</sup> Jing Wang,<sup>d</sup> Manzhang Xu, <sup>b</sup>a,<sup>b,c</sup> Xuetao Gan, <sup>b</sup>\*<sup>d</sup> Xuewen Wang <sup>b</sup>\*<sup>a,b,c</sup> and Wei Huang<sup>a,b,c,e,f</sup>

Two-dimensional (2D) layered transition metal dichalcogenides (TMDs) have received much attention in nonlinear optical applications due to their unique crystal structures and second harmonic generation (SHG) efficiency. However, SHG signals in TMDs show a layer-dependent behavior, consistent with the presence (absence) of inversion symmetry in even-layer (odd-layer) of TMDs. Herein, we synthesized monolayer and bilayer 2H and 3R phase vanadium (V)-doped MoS<sub>2</sub> crystal. Raman spectroscopy, XPS, and STEM were used to identify the chemical composition and crystalline structure of as-grown nanoflakes. SHG measurement was used to research the symmetry of V-doped MoS<sub>2</sub> crystals with different stacking orders. Significantly, the SHG efficiency in bilayer 2H phase V-doped MoS<sub>2</sub> is equivalent to the 3R phase, indicating an inversion symmetry broken lattice structure caused by the *in situ* V substitute for Mo sites. This study will be conducive to promote the development of promising nonlinear optical devices based on 2D material.

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# Introduction

Two-dimensional (2D) transition metal dichalcogenides (TMDs), represented by MoS<sub>2</sub>, WS<sub>2</sub>, WSe<sub>2</sub>, MoTe<sub>2</sub>, have gained enhanced research interest in recent years. Many excellent physical properties were observed in atomically thin few layers or monolayer TMDs, such as high Young modulus,<sup>1–3</sup> excellent transistor mobility and on-off ratio,<sup>4</sup> as well as piezoelectricity,<sup>5,6</sup> superconductivity<sup>7,8</sup> and nonlinear Hall effect.<sup>9</sup> These make the TMDs an ideal candidate for next-

<sup>d</sup>Key Laboratory of Light Field Manipulation and Information Acquisition, Ministry of Industry and Information Technology, and Shaanxi Key Laboratory of Optical Information Technology, School of Physical Science and Technology, Northwestern Polytechnical University, 127 West Youyi Road, Xi'an, 710072, China

<sup>e</sup>State Key Laboratory of Organic Electronics and Information Displays, Institute of Advanced Materials (IAM), Nanjing University of Posts & Telecommunications, 9 Wenyuan Road, Nanjing 210023, China

generation optoelectronic device.<sup>10,11</sup> Typically, 2D TMDs possess three crystalline structure, trigonal prismatic 3R, 2H phase and octahedral 1 T phase, respectively.<sup>12,13</sup> 3R polytype has AA stacking order of adjacent layers in same crystalline orientation with a slight in-plane shift. Based on the AA stacking order, 3R phase crystals exist with parallel in-plane nonlinear dipoles due to the absence of inverse symmetry.14-16 Thus, 3R TMDs possess effective second-order nonlinear susceptibility  $(\chi^{(2)})$  and phase-matched second harmonic generation (SHG) from monolayer to bulk crystal regardless of layer numbers. Distinguished from 3R polytype, 2H polytype TMDs have AB stacking order of adjacent layers in opposite crystalline orientation, leading to centrosymmetry (non-centrosymmetry) in even (odd) numbered layers.<sup>5,17,18</sup> As a result, 2H TMDs present a layer-dependent SHG due to the broken or recovery of inverse symmetry, which limits the application of 2D TMDs in the nonlinear optical devices since most 2D TMDs acquired by CVD synthesis or mechanical exfoliation from bulk crystal is 2H phase.

Currently, many strategies have been introduced to break the inverse symmetry of 2D TMDs and change the lattice structure,<sup>19–23</sup> such as tunning by electric field or defects,<sup>24,25</sup> strain regulation,<sup>9</sup> twisted TMDs *via* artificial stacking,<sup>26,27</sup> and controllable 3R phase crystal growth.<sup>14,15,28</sup> Yu *et al.* measured a strong SHG signal in bilayer 2H WSe<sub>2</sub> by applying an electrical gate field.<sup>24</sup> Further bond-charge model analysis indicated that accumulated sub-monolayer screening charge in the tungsten plane resulting in a nonuniform field distribution. The nonlinear Hall effect was observed in monolayer WSe<sub>2</sub> by



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<sup>&</sup>lt;sup>a</sup>Frontiers Science Center for Flexible Electronics (FSCFE) & Shaanxi Institute of Flexible Electronics (SIFE), Northwestern Polytechnical University, 127 West Youyi Road, Xi'an, 710072, China

<sup>&</sup>lt;sup>b</sup>Shaanxi Key Laboratory of Flexible Electronics (KLoFE), Northwestern Polytechnical University, 127 West Youyi Road, Xi'an, 710072, China

<sup>&</sup>lt;sup>c</sup>MIIT Key Laboratory of Flexible Electronics (KLoFE), Northwestern Polytechnical University, 127 West Youyi Road, Xi'an, 710072, China

<sup>&</sup>lt;sup>f</sup>Key Laboratory of Flexible Electronics (KLoFE) and Institute of Advanced Materials (IAM), Nanjing Tech University (Nanjing Tech), 30 South Puzhu Road, Nanjing 211800, China

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<sup>‡</sup>These authors contribute equal to this work.

### Paper

applying uniaxial strain to break  $C_{3v}$  symmetry.<sup>9</sup> Apart from applying external condition, precise regulation of growth factor during 2D materials preparation process is a direct way to achieve crystalline phase control. Chen *et al.* fabricated the 3R-stacked MoS<sub>2</sub> by homoepitaxial growth, and the flakes performed a vigorous SHG intensity by a factor of 6 compared with that of monolayer MoS<sub>2</sub>.<sup>15</sup> Although 3R MoTe<sub>2</sub>, WS<sub>2</sub> and WSe<sub>2</sub> have been synthesized by CVD or PVD route and exhibited considerable SHG in even layers, the large-area and highquality synthesis of a wide range of 2D TMDs remain big challenge up to now.<sup>13</sup>

Recently, atomic doping or alloy has been a common means in regulating electric and magnetic properties,<sup>7,29,30</sup> and phase controlled-synthesis of 2D material.<sup>31,32</sup> V-doped MoS<sub>2</sub> with different concentrations has been reported in tunning the electric conductance from n-type to p-type.<sup>29</sup> However, the nonlinear optical effect of 2D V-doped MoS<sub>2</sub> has not been investigated systematically before. Polarization angle-dependent SHG of monolayer  $\text{Re}_x \text{Mo}_{1-x} \text{S}_2$  (0 < x < 0.16) demonstrated that a slight lattice strain emerged in 2H MoS<sub>2</sub> due to Re substitute for Mo sites.<sup>33</sup> It provides a promising possibility to change the symmetry of pristine 2D material by atomic doping.

In this work, we synthesized V-doped  $MOS_2$  flakes *via* CVD growth using  $MOO_3$  and  $V_2O_5$  precursors. SHG measurement was employed to investigate the doping effect of bilayer flakes with different stacking orders for 2H phase AB stacking and 3R phase AA stacking. We find significant SHG efficiency in bilayer 2H phase V-doped  $MOS_2$  flakes compared with that of 3R phase, confirming a broken inverse symmetry regardless of crystalline orientation and layer numbers. We believe the significant result will promote the application of 2D materials in the nonlinear optoelectronic device. This work also provides a



**Xuewen Wang** 

Xuewen Wang is a professor and deputy Dean of the Institute of Flexible Electronics at Polytechnical Northwestern University, China. He received his Ph.D. in materials science from Nanyang Technological University, Singapore. His research interests are in the area of *flexible* electronics and advanced functional materials for flexible healthcare sensors. He explored new materials such as 2D materials, and new micro-

manufacturing technology for highly-integrated flexible smart sensors. His group is devoted to developing in situ and ex situ characterization techniques to reveal the sensing and failure mechanism for flexible materials and flexible sensors at the nanoscale. potentially valuable strategy for the design of 2D optical crystals with broken inversion symmetry.

# **Experimental section**

### CVD synthesis of V-doped MoS<sub>2</sub>

V-Doped MoS<sub>2</sub> crystals were synthesized by chemical vapor deposition (CVD) under standard atmospheric pressure. Fig. 1a illustrates the synthesis process of V-doped MoS<sub>2</sub> in this work. MoO<sub>3</sub> (Aladdin, 99.999%), V<sub>2</sub>O<sub>5</sub> (Aldrich, 99.99%) and S powder (Aladdin, 99.95%) were used as source materials for the synthesis of V-doped MoS<sub>2</sub> crystal. A powder mixture of 2 mg NaCl, 4 mg MoO<sub>3</sub> and 4 mg V<sub>2</sub>O<sub>5</sub> in an aluminium oxide boat was placed in the center of the quartz tube. Especially, the source MoO<sub>3</sub> and V<sub>2</sub>O<sub>5</sub> powder were mixed uniformly in the mortar in advance. 100 mg S powder was placed at the upstream side of the furnace. The grown substrate SiO<sub>2</sub>/Si was placed on downstream of the aluminium oxide boat with ~1 cm distance. The furnace was heated to the growing temperature 800 °C with a ramp rate of 35 °C min<sup>--1</sup> and the growth time was 5 minutes. After that, the furnace was decreased to room temperature naturally. Argon (Ar) with a flow rate of 80 sccm (standard cubic centimeters per minute) was used as the carrier gas.

### Characterization

Optical imaging was taken by ZEISS Primotech microscope. AFM topography and nanoindentation experiments were performed by Bruker Dimension Icon system. PL spectra and Raman mapping characterizations were carried out with the excitation laser of 532 nm using a WITEC alpha 300R Raman system. The system was first calibrated with the Raman peak of Si at 520 cm<sup>-1</sup> before the Raman measurement of V-doped  $MOS_2$  flakes. The PMMA-assisted wet-transfer method was employed to prepare the HADDF-STEM sample. STEM imaging was performed by FEI Themis system at 200 kV.

SHG measurement of the 2D V-doped MoS<sub>2</sub> flakes was carried out in a home-built vertical microscope setup with the reflection geometry. A fiber-based pulsed laser with a central wavelength at 1550 nm, a repetition rate of 18.5 MHz, and a pulse width of 8.8 ps was used as the fundamental pump radiation, A microscope objective lens (50×) with a numerical aperture of 0.75 was employed to focus the pump laser into a spot size of about 2  $\mu$ m on the sample. The second harmonic signal scattered from the sample was collected by the same objective lens. In the signal collection path, a dichroic mirror was used to filter out the pump laser from the SHG signal, which was finally analyzed and detected by a spectrometer mounted with a cooled silicon charge-coupled device camera.

# Results and discussion

Monolayer or bilayer V-doped  $MoS_2$  flakes were synthesized by the salt-assisted CVD method, as shown in Fig. 1(a). Briefly,

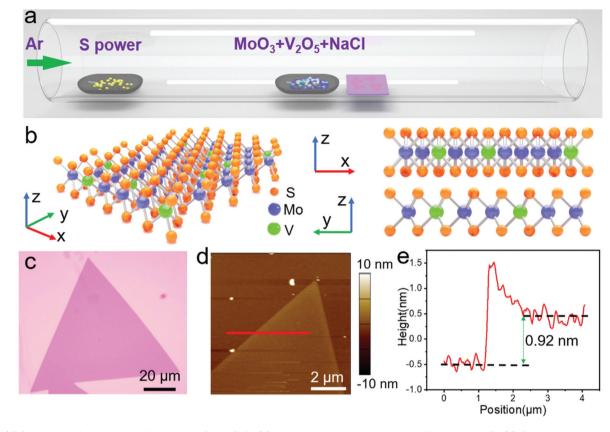
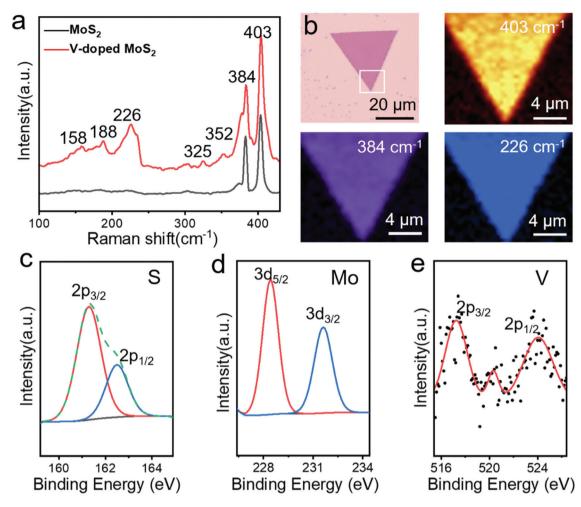


Fig. 1 (a) Schematic of synthesis of V-doped  $MoS_2$  by CVD. (b) Atom structure and side view of V-doped  $MoS_2$ . (c) Optical image of a V-doped  $MoS_2$  single crystal. (d and e) AFM topography and thickness measurement of V-doped  $MoS_2$ .

the mixed MoO<sub>3</sub> powder, V<sub>2</sub>O<sub>5</sub> powder and NaCl particles were placed in the center of the heating zone. The S powder was placed in the upstream. More detailed information can be found in the Experimental section. The atomic structure of monolayer V-doped MoS<sub>2</sub> crystal was schematically shown in Fig. 1(b). The left panel in Fig. 1(b) gives its three-dimensional atomic structure, which is similar as the structure of 1H phase MoS<sub>2</sub>. The difference is that in the center layer of the sandwich, partial Mo atoms were replaced by V atoms. The side view from x-z direction and y-z direction in the right panel gives a clear sight. The optical image of the growing V-doped  $MoS_2$  flake was shown in Fig. 1(c). A single triangle crystal was observed with lateral size of about 90 µm. AFM measurement was used to characterize the topography and thickness of the flakes. Its corresponding result was shown in Fig. 1(d). The step height of 0.92 nm between the SiO<sub>2</sub>/Si substrate and the sample measured by line scan indicates a monolayer flake.

Raman spectroscopy and X-ray photoelectron spectroscopy (XPS) characterization of the 2D V-doped MoS<sub>2</sub> sheets were collected and presented in Fig. 2. Raman spectra of pristine monolayer MoS<sub>2</sub> (black curve) and V-doped MoS<sub>2</sub> (red curve) flakes were displayed in Fig. 2(a). Typical Raman characteristic peaks were observed from the pristine MoS<sub>2</sub>. The  $E_{2g}^{1}$  mode at 384.5 cm<sup>-1</sup> refers to the in-plane vibration of Mo and S atoms. The A<sub>1g</sub> mode at 403 cm<sup>-1</sup> refers to the out-of-plane vibration of S atom. While with the doping of V atoms in MoS<sub>2</sub> lattice,

significant differences appear at the Raman spectra. Multiple peaks at 158 cm<sup>-1</sup>, 188 cm<sup>-1</sup>, 226 cm<sup>-1</sup>, 325 cm<sup>-1</sup>, 352 cm<sup>-1</sup> were observed in the V-doped MoS2, which was coincident with the previous report.<sup>29,30</sup> In particular, the peak at 226  $\text{cm}^{-1}$  is the characteristic peak of disordered MoS<sub>2</sub>, which could be caused by the V atoms induced broken of lattice symmetry. In order to find out the distribution of V dopant, Raman intensity mapping of V-doped MoS<sub>2</sub> flake was further carried out. As shown in Fig. 2(b), the upper left panel is an optical image of the sample, and the selected region is marked by a white frame. The homogeneous and uniform Raman intensity mapping of both  $E_{2g}^{1}$  mode at 384 cm<sup>-1</sup>,  $A_{1g}$  mode at 403 cm<sup>-1</sup> and characteristic mode of disordered MoS<sub>2</sub> at 226 cm<sup>-1</sup> reveal the V atoms are uniformly doped throughout the entire nanoflakes. XPS measurement further demonstrates the existence of S, Mo, and V elements. Fig. 2(c-e) give the narrow spectrum of S 2p, Mo 3d, and V 2p state, respectively. The spectra of S 2p core level binding energy have two strong peaks at 161.3 eV and 162.5 eV, corresponding to S 2p<sub>3/2</sub> and S  $2p_{1/2}$ . And the peaks of Mo 3d core level state at about 228.4 eV and 231.6 eV, corresponding to Mo 3d<sub>5/2</sub> and Mo 2p<sub>3/2</sub>, respectively. The bonding states of S and Mo elements in the V-doped MoS<sub>2</sub> alloy exhibit a slight energy shift compared with that of pristine MoS<sub>2</sub> in the previous report.<sup>34,35</sup> This can be explained by the effect of the nearby doped V atom. The red curve in Fig. 2(e) is the Gaussian fit of the signal of V 2p orbital split.



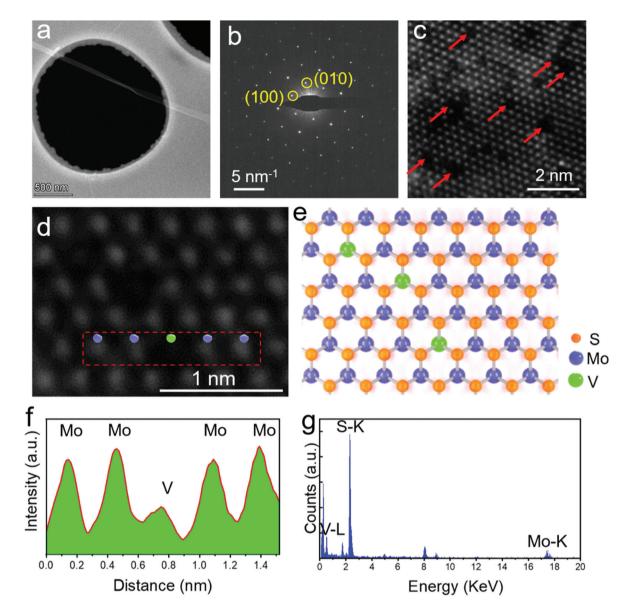
**Fig. 2** Raman and XPS measurement of V-doped MoS<sub>2</sub>. (a)Raman spectra of pristine MoS<sub>2</sub> and V-doped MoS<sub>2</sub>. (b) Optical image of V-doped MoS<sub>2</sub> and its corresponding Raman intensity mapping images at 403 cm<sup>-1</sup>, 384 cm<sup>-1</sup> and 226 cm<sup>-1</sup>. (c–e) XPS narrow spectra of the S 2p, Mo 3d, and V 2p orbitals, respectively.

Two strong peaks located at about 517.2 eV  $(2p_{3/2})$  and 524.0 eV  $(2p_{1/2})$ , which is consistent with the original chemical state of V atom in a hexagonal structure, demonstrating the successful *in situ* replacement of Mo atom in MoS<sub>2</sub> lattice.<sup>36</sup> As shown in Fig. 2(e), the experimental result presented by black points is not so flat, indicating a low concentration doping of V atoms in the sample.

To assess the quality of the as-synthesized V-doped MoS<sub>2</sub> flakes precisely, high-angle annular dark-field scanning transmission electron microscopy (HAADF-STEM), selected area electron diffraction (SAED) and energy dispersive X-ray spectroscopy (EDS) were employed to explore the crystalline structure and chemical composition of the sample. Fig. 3(a) is a low magnification STEM image of a monolayer V-doped MoS<sub>2</sub> flake transferred on a copper screen. The edge of the nanofilm has been lapped over during the transfer process. The SAED pattern (Fig. 3(b)) taken from the flake exhibits regular hexagonally arranged diffraction spots, which can be fitted to the hexagonal lattice structure of MoS<sub>2</sub>. It means that no lattice mismatch generation with the doping of V atoms in MoS<sub>2</sub>.

high-resolution STEM imaging gives obvious evidence of *in situ* substitute between Mo and V atoms further. The aberration correction annular dark-field (ADF)-STEM imaging can provide the *Z*-contrast with atomic resolution, which is proportional to the quadratic square of the atomic number (*Z*). So, the Mo (Z = 42) site is bright and V (Z = 23) site is dark in the ADF-STEM imaging (Fig. 3(c)).

As a contrast, STEM imaging of pristine  $MoS_2$  flakes was also characterized and no dark filed was found in the  $MoS_2$ lattice (Fig. S1<sup>†</sup>). Red arrows marked the substitute of Mo sites by V atoms. The calculated doping concentration of V is ~8% by counting the number of Mo and V atoms in the image, which is the highest value of V-doping in  $MoS_2$  using  $V_2O_5$  as the precursor. An enlarged HAADF-STEM image (Fig. 3(d)) and its corresponding atomic structure (Fig. 3(e)) show a detailed atom distribution. The intensity line profile marked by the highlighted red frame in Fig. 3(d) is shown in Fig. 3(f). The four stronger intensity peaks are Mo sites and the weak peak in the center is V site. To identify the dark field is V substitute other than atomic defect, EDS spectroscopy (Fig. 3(g)) was



**Fig. 3** HADDF-STEM characterization of monolayer V-doped MoS<sub>2</sub>. (a) Low magnification image of transferred V-doped MoS<sub>2</sub> nanofilm on grid copper. (b) SAED pattern of H-phase V-doped MoS<sub>2</sub>. (c) HADDF-STEM image of V-doped MoS<sub>2</sub>. Partial V substitutes for Mo sites are marked by red arrow; (d and e) enlarged STEM image and its corresponding atomic distribution of Mo (blue), V (green) and S (yellow). (f) *Z*-Contrast intensity profile along the highlighted red dashed box in (d). (g) EDS spectra of V-doped MoS<sub>2</sub> flakes, confirming the coexistence of Mo, V and S elements.

applied to investigate the chemical composition of the sample. All the expected characteristic peaks of S–K at 2.31 keV, Mo–K at 17.48 keV and V–L at 0.51 keV certified their existence.<sup>37</sup>

Except for most monolayer V-doped MoS<sub>2</sub> nanoflakes, twisted bilayer nanoflakes with different angles were also observed in SiO<sub>2</sub>/Si substrate. Here, we measured the SHG response of monolayer, bilayer AA-stacking and AB-stacking pristine MoS<sub>2</sub> and V-doped MoS<sub>2</sub> flakes to verify the crystal character. Fig. 4(a) is a schematic diagram of SHG process of 2D crystal under a pump excitation ( $\lambda = 1550$  nm). We measured the SHG intensity of a monolayer flake under various excitation power (2 mW-10 mW). First, all the expected single peak has emerged at 775 nm, which is exactly at the doubled frequency of the fundamental 1550 nm excitation laser. Second, the function of SHG intensity and excitation power was presented by a double logarithmic plot (Fig. S2†). The slope of 1.9 affirmed the second-order nonlinear optical process. The side view of the atomic structure of bilayer 3R phase and 2H phase MoS<sub>2</sub> was shown in Fig. 4(b). The 3R phase has AA stacking of different layers being in the same orientation with a slight in-plane shift. The S atoms and Mo atoms of different layers do not align on top of each other preciously, ensuring the expected broken inversion symmetry. Comparing with 3R stacking, the 2H phase MoS<sub>2</sub> has AB stacking of bottom layer and top layer being in the opposite orientation with inversion symmetry.<sup>28,38</sup> Fig. 4(c) and (e) display

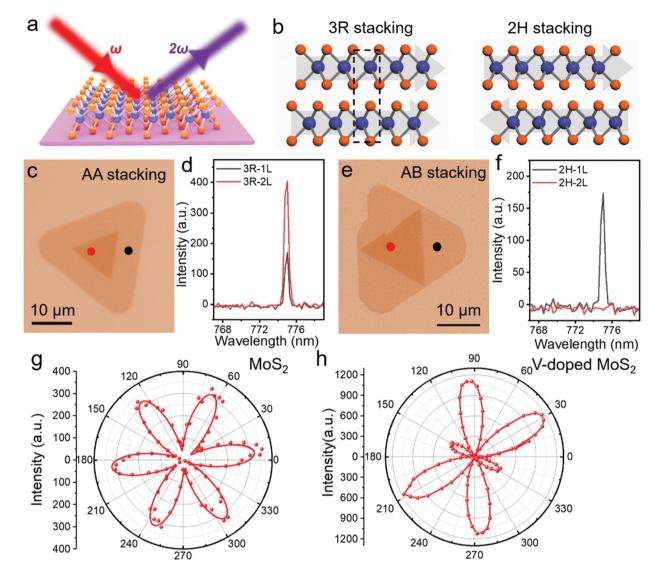
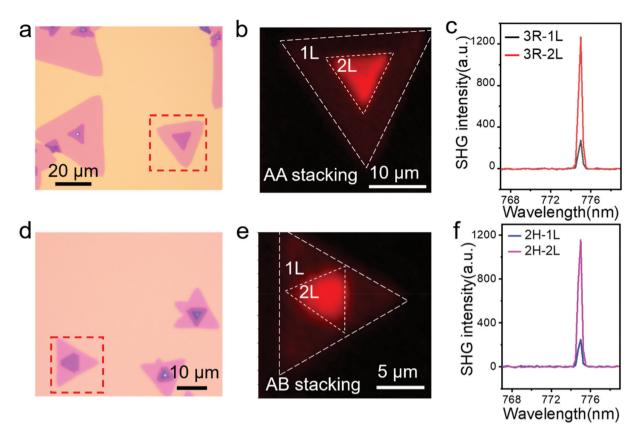


Fig. 4 (a) Schematic diagram of SHG process. (b) Side view of bilayer 3R and 2H phase  $MoS_2$  with different stacking order. (c and e) Optical images of  $MoS_2$  with 3R and 2H stacking. (d and f) Layer number-dependent SHG response 3R and 2H phase V-doped  $MoS_2$ . (g and h) Angular-dependent SHG intensity of monolayer  $MoS_2$  and V-doped  $MoS_2$ .

the optical microscopy images of pristine AA-stacking and ABstacking  $MoS_2$  flakes with different stacking orders. As shown in Fig. 4(d), an increased SHG intensity was observed in bilayer AA-stacking  $MoS_2$ . As a contrast, no SHG response was observed in bilayer AB-stacking  $MoS_2$  (Fig. 4(f)). Generally, the SHG disappeared in even layers of 2H phase  $MX_2$  ( $MoS_2$ ,  $WS_2$ ,  $WSe_2$ , *etc.*) due to the recovered inverse symmetry, which has been widely reported before.<sup>38,39</sup>

Polarization angle-dependent SHG was carried out to explore the crystalline structural characteristics. The monolayer  $MoS_2$  presents a typical six-fold symmetric pattern (Fig. 4(g)). However, the six-fold pattern of monolayer V-doped  $MoS_2$  was nonuniform shaped, with four folds enlarged compared with the two shrunken folds (Fig. 4(h)). Obviously, the situation changed with the doping of V atom in  $MoS_2$  lattice. We further measured the SHG response of bilayer V-doped  $MoS_2$  flakes with different stacking orders. Fig. 5(a) and (d) display the optical microscopy images of as-synthesized AAstacking and AB-stacking V-doped MoS<sub>2</sub> flakes. Their corresponding Raman spectra were given in Fig. S3.† Both AB-stacking and AA-stacking flakes grown on the uniform SiO<sub>2</sub>/Si substrate show consistent optical contrast, indicating they possess the same number of layers. AFM measurements were carried out to identify the thickness and layers, and the results of an AA-stacking flake demonstrate the center was bilayer (Fig. S4<sup>†</sup>). We characterized the SHG mapping (Fig. 5(b)) of a flake with bilayer AA-stacking in the center and monolayer in the edge, highlighted by red dashed box in Fig. 5(a). It is apparent that the center section presented stronger SHG response than the edge according to the image's contrast. The quantitative SHG intensities of 3R stack monolayer and bilayer are presented in Fig. 5(c). To our surprise, the bilayer AB-staking 2H phase



**Fig. 5** SHG mapping of bilayer 3R and 2H phase V-doped MoS<sub>2</sub>. (a and d) Optical images of V-doped MoS<sub>2</sub> with 3R and 2H stacking. (b and e) SHG intensity mapping of V-doped MoS<sub>2</sub> flakes from (a and d), marked by red dashed boxes. (c and f) Layer number-dependent SHG response 3R and 2H phase V-doped MoS<sub>2</sub>.

flakes also generate a strong SHG signal (Fig. 5(e)) and the intensity is almost same as that from 3R bilayer (Fig. 5(f)), demonstrating a breakage of inverse symmetry in 2H phase V-doped  $MoS_2$ . This was originally from the random distribution of V-substitute for Mo sites, which causes a slight lattice strain to break the symmetric structure.<sup>33</sup>

# Conclusions

In summary, we synthesized the V-doped  $MoS_2$  flakes using  $V_2O_5$  precursor *via* CVD method. The crystalline structure was determined by STEM characterization. SHG measurement was further used to investigate the inverse symmetry of 2H and 3R phase V-doped  $MoS_2$  with different stacking orders. The nearly consistent SHG response in bilayer 2H and 3R phase V-doped  $MoS_2$  indicated the broken inversion symmetry regardless of stacking order and layer numbers. The doping 2D crystal provides a profitable strategy to extend the range of atomically thin optical material with second-order nonlinearity.

# Conflicts of interest

There is no conflict to declare.

# Acknowledgements

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