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Structural optimization and engineering of $\text{In}_x\text{Ga}_{1-x}\text{N}$ quantum dot intermediate band solar cells with intrinsic GaN interlayers

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It is essential to have an adequately thick active layer to achieve efficient performance in quantum dot intermediate band solar cells (QD-IBSC) utilizing $\text{In}_x\text{Ga}_{1-x}\text{N}$ with high indium concentrations. The thickness plays a crucial role in maximizing photon absorption and optimizing the overall effectiveness of the solar cell (SC). In this paper, we introduce QD-IBSC with Ga-face (0 0 0 1) applying 1 nm i-GaN interlayers, which will provide strain relaxation to the $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}/\text{GaN}$ QD layer for increasing photovoltaic performance. Normally, the coupling among QDs splits the quantized energy level and leads to the formation of minibands within the forbidden region of conventional SC. In particular, the QDs are sensitive to dot regimentation and thus affect the properties of QD-IBSC. The electronic band structure of these QDs is controlled by changing the size of the QD, interdot distances and regimentation. In this paper, optimization of the optical structure of the QD-IBSC is performed by investigating the calculation results of both the maximum number of absorbed photons and the carrier transport property through tunneling simultaneously as a function of the thickness of the i-GaN interlayers. For the calculation, the three-dimensional regimented array of $\text{In}_x\text{Ga}_{1-x}\text{N}$ QD is analyzed using an envelope function. This work demonstrates Ga-face n-i-p structure (n-GaN/i-GaN: $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$:i-GaN/p-GaN) utilizing the 20 periods of 3 nm thick $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$ QD layers and a GaN layer of 1 nm thickness can achieve a maximum conversion efficiency of 48%.

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Introduction

The quest for sustainable and renewable energy sources has positioned solar energy at the forefront of technological innovation and scientific research. Solar cells, which convert sunlight directly into electricity, play a crucial role in this energy transformation.¹ Over the past few decades, significant advancements have been made in the field of photovoltaic (PV) technology, driven by the need to improve efficiency,² reduce costs, and enhance the longevity of solar cells.³ The intermediate band solar cell (IBSC) offers^{4–6} a potential solution to counter the fundamental limitation associated with generating electric current through light absorption in semiconductors. This fundamental idea serves as the basis of Wolf's proposition⁷ to introduce energy levels within the forbidden

gap to reduce absorption losses. The inclusion of energy levels within the semiconductor material's bandgap facilitates the absorption of low-energy photons, which have energy below the bandgap energy of the host semiconductor.⁸ Detailed balanced calculations reveal that under the same conditions, the theoretical efficiency limit of sequential two-photon absorption (STPA) in conjunction with intermediate levels surpasses the efficiency limit of single-gap solar cells, commonly referred to as the Shockley and Queisser limit ($\sim 42\%$), achieving a remarkable efficiency limit of 63.2%.⁹ The IBSC necessitates the presence of three distinct and isolated "pseudo-Fermi" energy levels, each with specific carrier concentrations. Consequently, this requirement prohibits the utilization of quantum well, nanowire or quantum rod structures.¹⁰ The tunnelling of electrons towards the intermediate band (IB) levels is facilitated by their inherent capacity to adjust their crystal momentum. An effective approach to introduce additional isolated energy bands within the bandgap of the host material in single/multiple junction solar cells is by integrating quantum dots (QDs) into the intrinsic absorber layer. This incorporation forms an intermediate band (IB) structure, enhancing the overall functionality of the solar cell.^{11–15} The presence of the intermediate band (IB) facilitates a two-step absorption process for sub-bandgap photons with energy $E_L \leq E_{ph} \leq E_g$ and

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$E_H \leq E_{ph} \leq E_g$, enabling the transition of an electron from the valence band (VB) to the conduction band (CB). Initially, a photon is absorbed in the VB, promoting the electron to the IB. Subsequently, another electron jumps from the IB to the CB, completing the transition,¹⁶ thus delivering high voltage.¹⁷ The efficiency of converting solar energy is significantly influenced by the bandgap of the absorber material utilized in the active layer of the solar cell structure.^{5,15,18–22} IBSCs hold the potential to achieve efficiency levels comparable to those of triple-junction solar cells, which typically consist of two semiconductor interfaces.²³

Ab initio calculations^{5,24,25} are employed to select various IB materials. These materials possess fundamental properties such as strong sub-bandgap absorption, extended carrier lifetimes, and excellent carrier mobilities. Notably, the III-nitride family²⁶ exhibits these desirable characteristics. Among them, the direct bandgap $\text{In}_x\text{Ga}_{1-x}\text{N}$ alloy showcases the most promising properties for optoelectronic devices.²⁷ Its tunable bandgap, better drift velocity, high mobility, high absorption coefficient and high tolerance to radiation enable efficient absorption of a broad range of the solar spectrum in SC.^{28,29} $\text{In}_x\text{Ga}_{1-x}\text{N}$ exists in two different structures: zinc blende and wurtzite.²⁸ While the wurtzite structure is thermodynamically stable, it lacks an inversion plane perpendicular to the c -axis. This leads to spontaneous and piezoelectric polarization caused by an internal electric field.²⁹ On the other hand, zinc blende possesses high crystal symmetry, resulting in the absence of crystal polarization.^{30–32} In our investigation, we explore the utilization of wurtzite $\text{In}_x\text{Ga}_{1-x}\text{N}$ QDs embedded in GaN for IBSCs.

However, the fabrication of $\text{In}_x\text{Ga}_{1-x}\text{N}$ SC still faces significant challenges.²⁷ A few of them include: (1) the bandgap of $\text{In}_x\text{Ga}_{1-x}\text{N}$ varies indirectly with the indium composition, which can lead to poor crystallinity and high defect rate that significantly impact the emission process.³³ (2) The $\text{In}_x\text{Ga}_{1-x}\text{N}$ films often experience indium cluster segregation at the surface, caused by a solid phase miscibility gap resulting from a lattice mismatch and differences in enthalpy formation between GaN and InN.³⁴ (3) $E_{\text{polarization}}$ effects also affect the efficiency of optoelectronic devices, as discussed in the subsequent section.

Aouami *et al.* calculated the behaviour of different geometries for multiple quantum dot solar cells.³⁵ Pérez *et al.* considered a juxtaposition of two kinds of QDs and determined the energy levels.³⁶ Aissat *et al.* modelled $\text{In}_{0.25}\text{Ga}_{0.75}\text{N}/\text{GaN}$ QDSC with five layers of quantum dots at the temperature of 285 K and concluded that the efficiency of SC is highly dependent on temperature.³⁷ Chen *et al.* studied the single junction $\text{In}_x\text{Ga}_{1-x}\text{N}$ SC with three intermediate band gaps. Their research revealed that increasing the bandgap ($1 > x > 0$) results in a higher number of IBs within the absorber layer, leading to an efficiency of over 50%. While IBs can be obtained at low indium concentrations in $\text{In}_x\text{Ga}_{1-x}\text{N}$, higher concentrations often result in clustering, limiting the efficiency to around 12%.³⁸ Deng *et al.* conducted $\text{In}_x\text{Ga}_{1-x}\text{N}/\text{InN}$ IBSC computations with orthorhombic symmetry of QDs embedded in periodic arrays. Without considering polarization fields, they achieved a maximum efficiency of 60.3% for QD size 3.3 nm and interdot size 2 nm.³⁹

Zhang *et al.* ascertained an indium concentration of 45%, resulting in an efficiency of 61.67% for cubic QD size 3.3 nm and interdot size 2 nm.⁴⁰ Several studies have reported on simple PIN solar cells with polarization effects and potential solutions.^{41–44} However, to the best of our knowledge, no research group has reported a comprehensive study on quantum dot intermediate band solar cells (QD-IBSCs) that optimizes both the quantum dot layers and the active layer to reduce the lattice mismatch between $\text{In}_x\text{Ga}_{1-x}\text{N}/\text{GaN}$ layers.

In this study, we investigate and analyse the photovoltaic properties of n-i-p Ga-face (0 0 0 1) $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}/\text{GaN}$ QD-IBSC with three-dimensional $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}/\text{GaN}$ QDs embedded between n-type and p-type GaN emitters, with a 1 nm interlayer incorporated in the absorber layer. This interlayer aims to mitigate the strain relaxation caused by compressive forces at the interface between $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$ and GaN. By optimizing the size and distance of the quantum dots, we calculate the position and width of the intermediate band (IB). Additionally, we determine the energies of the quantum dots by solving the Schrödinger equation in the presence of $E_{\text{polarization}}$.

Device theory

The QD-IBSC structure comprises layers of GaN, an interlayer/ $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$:QD structure with pyramid-shaped QDs (PSQDs) embedded within the active $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$ layers. PSQDs have higher mobilities and longer lifetimes.⁴⁵ The incorporation of intrinsic GaN interlayers in this structure plays a crucial role in absorbing the compressive strain caused by the interface mismatch between GaN/ $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$. These interlayers need a thickness that allows the wave functions of carriers to flow through tunnelling from neighbouring vertically stacked QDs.⁴⁶ The $\text{In}_x\text{Ga}_{1-x}\text{N}$ layers need to be thick and numerous enough to absorb efficiently the incoming light beam, and thin enough to remain fully strained and without phase separation. The structure begins with a 300 nm p-doped GaN layer, followed by a 1 nm i-GaN interlayer. Multiple $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$ QDs are then stacked together in the active layer, and the QDs are capped with a 20 nm n-GaN layer, as depicted in Fig. 1(a).

The wurtzite structure of $\text{In}_x\text{Ga}_{1-x}\text{N}$ gives rise to a pronounced polarization effect due to the non-centric symmetry of charges. This $E_{\text{polarization}}$ polarization effect, along with potential barriers and band bending, significantly influences the behaviour of devices.⁴⁷ The characteristics of $\text{In}_x\text{Ga}_{1-x}\text{N}$ alloy exhibit a non-linear dependence on the alloy composition, resulting in complex properties.⁴⁸ The wurtzite structure encompasses two types of polarization. The first type, known as P_{sp} , is an inherent property of wurtzite semiconductors and arises from the absence of an inversion plane perpendicular to the c -axis.⁴⁹ This phenomenon contributes to variations in dislocation density and surface morphology.⁴⁶ Importantly, the P_{sp} values for InN and GaN are nearly equal.⁴⁹ The calculation of P_{sp} can be determined using the following relation:⁵⁰

$$P_{\text{sp}}(\text{In}_x\text{Ga}_{1-x}\text{N}) = xP_{\text{sp}}(\text{InN}) + (1 - x)P_{\text{sp}}(\text{GaN}) - b_{\text{InGa}}x(1 - x) \quad (1)$$



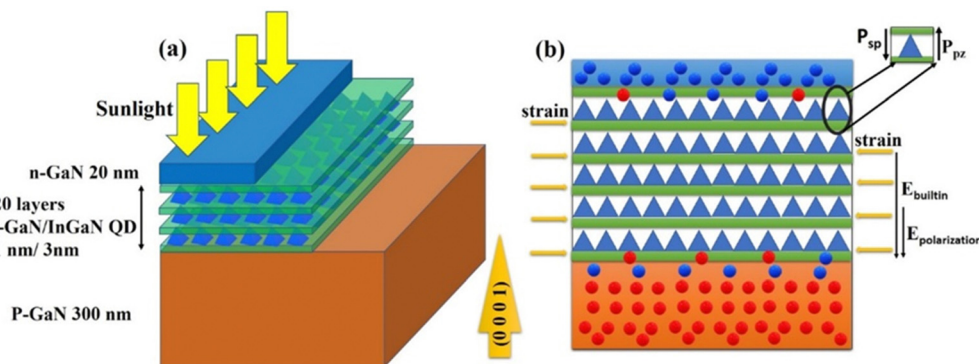


Fig. 1 (a) Epitaxial layer structure of IBSC based on $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$ QDs embedded in a GaN matrix with 1 nm GaN interlayers. (b) Schematic diagram of polarization-induced charges, and the electric fields at the $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}/\text{GaN}$ interfaces. The inset shows the directions of spontaneous polarization (P_{sp}) and piezoelectric polarization (P_{pz}) at the interface.

where b_{InGa} is the bowing parameter and is calculated by $b_{\text{InGa}} = 2P(\text{InN}) + 2P(\text{GaN}) - 4P(\text{In}_{0.5}\text{Ga}_{0.5}\text{N})$, when $x = 0.5$.

The presence of a second type of polarization, referred to as P_{pz} , can be observed in strained epitaxial layers. This polarization arises from the lattice-relaxation strain that occurs when two different materials are grown on the same substrate. In the case of wurtzite nitrides, the growth under biaxial strain induces piezoelectric polarization.⁵⁰ The magnitude of P_{pz} depends on the composition of the $\text{In}_x\text{Ga}_{1-x}\text{N}$ alloy and is related to its binary constituents, InN and GaN, through the following relation:⁵¹

$$P_{\text{pz}}(\text{In}_x\text{Ga}_{1-x}\text{N}) = xP_{\text{pz}}(\text{InN}) + (1 - x)P_{\text{pz}}(\text{GaN}) \quad (2)$$

In our specific case, the growth of InN QDs on a GaN layer with lattice mismatch induces strain effects due to the relaxation of the mismatched layers. A 1 nm interlayer of i-GaN is incorporated to mitigate this strain. The total polarization ($P_{\text{T}} = E_{\text{polarization}}$) is determined by the combined contributions of P_{pz} and P_{sp} . Since the layers are in compression, the two polarizations act in opposite directions (as shown in the inset in Fig. 1(b)), resulting in a reduced net polarization. The presence of a built-in electric field and lower polarization field facilitates the movement of more carriers across the interfaces from the n-type to the p-type layer. Fig. 1(b) displays the calculated P_{T} at the interfaces, along with the directions of the spontaneous polarization (P_{sp}) and piezoelectric polarization (P_{pz}) at the interface. The structures demonstrate the lattice orientations and the corresponding vectors of P_{sp} .⁵²

The following list of assumptions is used to carry out limiting efficiency calculations.

1. The solar cell absorbs blackbody radiation at a temperature of $T_{\text{s}} = 6000$ K and ambient $T_{\text{a}} = 300$ K and emits blackbody radiation at ambient $T_{\text{a}} = 300$ K.
2. Only radiative transitions occur between the bands.
3. All photons above the lowest energy gap are absorbed, and no high-energy photon is used in a low-energy process.
4. Carrier mobility is infinite; consequently, the quasi-Fermi energy levels are constant throughout the cell.
5. Only one electron-hole pair is created per photon.

6. A perfect mirror is located on the back of the cell so that radiation makes a double pass and can only escape through the front illumination area.

7. The net photon flux (number of incident photons minus the number of emitted photons) equals the number of charge carrier pairs collected at the contacts.⁹

In the case of intermediate band solar cells (IBSCs), the detailed balance assumptions mentioned above are applied with slight modifications as follows:

Firstly, it is assumed that photons with photon energy $E_{\text{ph}} < E_{\text{g}}$ are absorbed, even though they fall below the energy bandgap. This is possible because an additional bandgap within the forbidden region has been introduced, which is isolated and has zero density of states. Secondly, the original bandgap E_{g} ($E_{\text{g}} = E_1 + E_2$) is split into two separate energy levels, E_1 and E_2 . This splitting facilitates the absorption of photons with energy $E_{\text{ph}} < E_{\text{g}}$. Therefore, in addition to absorbing photons with $E_{\text{ph}} \geq E_{\text{g}}$ using the conventional mechanism, IBSCs can also absorb photons with $E_{\text{ph}} < E_{\text{g}}$ (assumption 3). As a result of absorbing photons with $E_{\text{ph}} < E_{\text{g}}$, the absorptivity of the cell increases. However, it should be noted that only one additional electron-hole pair contributes to the short-circuit current density, J_{sc} (assumption 5). Moreover, the intermediate band (IB) is partially filled, and the valence band offset is considered to be negligible. It is important to mention that the output voltage is not calculated based on the IB (assumption 7).⁴

Taking the aforementioned factors into account, the electronic state of quantum dots (QDs) is determined by utilization of the Schrödinger equation, employing the Kronig-Penney model. Our previous work⁵³ extensively discussed the theoretical framework behind this calculation. The position and width of the QDs are further optimized using the envelope function approximation. Simultaneously, the electronic properties are computed by solving Poisson's equation. To integrate these two calculations, we employ COMSOL Multiphysics, a software platform that combines the Schrödinger equation and electrostatics. This integration enables us to model the behavior of charge carriers in quantum-confined systems. Notably, the electric potential derived from the electrostatics is incorporated into the potential energy term of the Schrödinger equation within the COMSOL Multiphysics framework.



The solar cell and sun are considered blackbody systems. By applying the Roosbroeck–Shockley formula, the photon flux within the energy range of E_1 to E_2 can be determined using the following calculations,²⁰

$$N(E_1, E_2, T, \mu) = \frac{2\pi\zeta}{h^3 c^2} \int_{E_1}^{E_2} \frac{E^2 dE}{\exp\left(\frac{E-\mu}{k_B T}\right) - 1}, \quad (3)$$

where E_1 and E_2 are the maximum and minimum energies of the photons, T is the temperature in Kelvin, μ is the chemical potential energy of CB, VB and IB. h is Planck's constant, ζ the geometric factor, and k_B is the Boltzmann constant. Chemical potentials are further defined as,

$$\begin{aligned} \mu &= E_{FC} - E_{FV} = 3.39 \text{ eV}, \quad \mu_1 = E_{FIB} - E_{FV} = 1.89 \text{ eV}, \\ \mu_2 &= E_{FC} - E_{FIB} = 1.5 \text{ eV}, \end{aligned} \quad (4)$$

Under the condition of full-concentration sunlight, the photons absorbed and emitted by the QD-IBSC are expressed as²⁰

$$\begin{aligned} \frac{J_{sc}}{q} &= [S_f \zeta N(E_g, \infty, T_s, 0) - N(E_g, \infty, T_c, \mu)] + [N(E_2, E_1, T_s, 0) \\ &\quad - N(E_2, E_1, T_c, \mu_2)], \end{aligned} \quad (5)$$

Here μ_{ci} and μ_{cv} are the differences in quasi-Fermi levels from the CB to IB and CB to VB, respectively. $T_s = 6000 \text{ K}$ and $T_c = 300 \text{ K}$ are the surface temperature of Sun and SC, respectively, S_f is the concentration factor. The chemical potential of the sun is considered to be 0 eV when calculating the number of photons radiated by the sun as a blackbody and q is the charge of an electron.⁵⁴ E_g , E_2 and E_1 are the bandgap energies, from IB to CB, and from VB to IB, respectively. The terms in the first bracket explain conventional transitions of SC, whereas the second bracket involves the flux of additional IB transitions. The flux for IB to CB can be rewritten as

$$\begin{aligned} \frac{J}{q} &= [S_f \zeta N(E_g, \infty, T_s, 0) + (1 - S_f \zeta) N(E_g, \infty, T_c, 0) \\ &\quad - \mu_{CV} N(E_g, \infty, T_a, qV)] + [S_f \zeta N(E_2, E_g, T_s, 0) \\ &\quad + [(1 - S_f \zeta) N(E_2, E_g, T_a, 0) - N(E_2, E_g, T_a, \mu_2)] \end{aligned} \quad (6)$$

$$\begin{aligned} \frac{J}{q} &= [S_f \zeta N(E_g, \infty, T_s, 0) + (1 - S_f \zeta) N(E_g, \infty, T_c, 0) \\ &\quad - \mu_{CV} N(E_g, \infty, T_a, qV)] + [S_f \zeta N(E_1, E_g, T_s, 0) \\ &\quad + [(1 - S_f \zeta) N(E_1, E_2, T_a, 0) - N(E_1, E_2, T_a, \mu_1)], \end{aligned} \quad (7)$$

The output voltage can be calculated by $qV_{oc} = \mu = \mu_2 + \mu_1$.

The efficiency (η) can be calculated as:

$$\eta = \frac{P_o}{P_i} = \frac{FF V_{oc} J_{sc}}{P_i}, \quad (8)$$

The efficiency depends on the ratio of maximum output power to input light power density ($P_{in} = \zeta \sigma_s T_s^4$, where σ_s is Stefan's constant), where output power is further calculated by fill factor (FF), open circuit voltage (V_{oc}), and short circuit current (J_{sc}).

Results and discussion

QDs are incorporated within the intrinsic absorber layer, and their position, width, and interdot size have been extensively studied for a 50% indium concentration. The structure of the simulated SC is depicted in Fig. 1(a), where the IB region is positioned between p-GaN and n-GaN materials. To minimize polarization effects within the IBSC's active layer, a Ga-face n-i-p structure is employed. The p-layer has a thickness of 300 nm, while the n-layer is 20 nm thick, and both layers have a doping concentration of $5 \times 10^{18} \text{ cm}^{-3}$. A thin cap layer reduces surface recombination from the n-layer, allowing maximum photon absorption in the device's active layer.³⁷ The QDs are arranged in close proximity, both horizontally and vertically, enabling the penetration of wave functions from the QD region to the barrier region, effectively creating an intrinsic barrier within the forbidden region of the conventional bandgap.⁵ However, it is crucial to avoid inappropriate stacking of the QD layers, as this would result in QD localization within their designated region and prevent the formation of the intrinsic barrier. Therefore, careful placement and stacking of the QDs is necessary to establish the intrinsic barrier⁶ effectively. The QDs are selected with dimensions ranging from 1 to 5 nm, while the interdot distances vary from 1 to 3 nm.⁵³ These 20 layers of QDs are grown on top of p-GaN. The growth of $\text{In}_x\text{Ga}_{1-x}\text{N}$ on GaN with sapphire substrates introduces in-plane strain. To limit the elastic energy stored in the $\text{In}_x\text{Ga}_{1-x}\text{N}$ layers, referred to as the critical thickness,⁵⁵ an additional interlayer is introduced to alleviate the compressive strain on the $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$ quantum dots.⁴⁶ The presence of strained $\text{In}_x\text{Ga}_{1-x}\text{N}$ layers helps suppress phase separation.⁵⁶

Numerical experimentation has been conducted to simulate the QD-IBSC device and analyze the behavior of stacked quantum dot layers. The calculation of the band structure employs a tight-binding model that superimposes wave functions for the individual quantum dots. The finite element method technique is utilized to solve the model to enhance computational efficiency. The simulation process involves several steps. Firstly, the eigenvalues of the quantum dots are determined by solving the Schrödinger equation.⁵³ Subsequently, the impact of embedding QDs in the intrinsic layer of a Ga-face n-i-p SC under the conditions mentioned above is simulated. The modeling incorporates the material properties specified in Table 1.

Table 1 Material parameters for $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$ ^{28,29}

Parameters	Values
Bandgap (E_g)	1.6875 (eV)
Lifetime (τ)	6.5 (ns)
Effective conduction band density of $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$	$1.6 \times 10^{18} \text{ (cm}^{-3}\text{)}$
Effective valence band density of $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$	$9 \times 10^{18} \text{ (cm}^{-3}\text{)}$
Effective electron mass of $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$	0.16 m_0
Effective hole mass of $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$	0.585 m_0
Electron affinity	5.29875 (eV)
Elastic constant (c_{13})	100 (GPa)
Elastic constant (c_{33})	299 (GPa)
Piezoelectric Const. (e_{31})	0.04 (C m ⁻²)
Piezoelectric Const. (e_{31})	0.88 (C m ⁻²)



Optical modes and the distribution of the electric field are also considered. The Fresnel model is applied to optimize the reflection and transmission of light. Boundaries are fine-tuned using Floquet's periodicity condition. Moreover, the influence of thin enough material strain is considered as per the equation described in Section 2 of the referenced article.

The three-dimensional doping profile of the proposed structure with excited state energy is shown in Fig. 2(a). The blue color shows the concentration of excess electrons, whereas the red indicates the excess holes. The green color indicates the intrinsic level with no doping. The inset shows the excited state energies of the QDs. Fig. 2(b) shows the energy band diagram for the proposed structure. E_c and E_v are the CB and VB energy levels, respectively. E_{IB} is the IB energy level created when QDs are placed within the intrinsic level of n-i-p IBSC. These bands have their Fermi levels. E_{fc} and E_{fv} are the quasi-Fermi levels for the CB and VB. The intermediate band has its Fermi level E_{fIB} which is separated from the quasi-Fermi levels of the CB and VB. This IB is half-filled with electrons by optimizing the distance between QDs and spacing between barrier regions.⁵³ E_g is the bandgap of GaN (3.39 eV) and E_{InN} is the bandgap for InN (0.7 eV). E_1 and E_2 are the energy gaps between E_v and E_{IB} , E_{IB} and E_c , respectively. L_{qd} is the distance between two adjacent QDs, and L_{br} is the width of the barrier. Upon illumination, photons are absorbed; if E_{ph} (energy from photons) $\leq E_g$, this energy photon is absorbed and creates an electron-hole pair. Additional electron-hole pairs are created other than the conventional ones, which results in higher efficiency.⁵³ Additionally, low-energy photons below E_g are absorbed, thus increasing the photocurrent.

Fig. 3(a)–(c) shows the 3×3 layer of QDs with their localized wave functions for the QD size of 3 nm and their interdot distance of 2 nm. Three eigenvalues are inside the conduction band at 1.3479, 1.8472, and 2.6289 eV. The first state is the pure quantum dot state. The wave function for this state is zero at the center of the quantum dot and vanishes at the boundary. The second and third states are weakly confined concerning the first state.⁵⁷ The band formation of IB strongly depends on the dot sizes⁵³ and interdot spacing between each QD. The wave

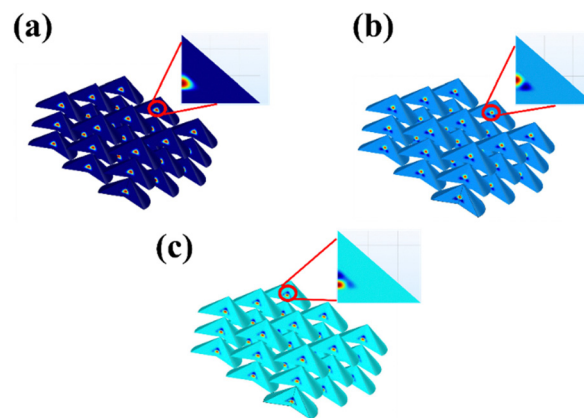


Fig. 3 WF of a system: (a) ground state $E_0 = 1.34$ eV, (b) first excited state $E_1 = 1.85$ eV and (c) second excited state $E_2 = 2.63$ eV.

functions of the QDs will overlap for certain QD sizes and interdot spacings such that energy level splitting occurs. Small confinement in barriers increases the tunneling probability of the wavefunctions.⁵³ Due to the quantum confinement effect, QD coupling occurs as soon as they are brought near each other. This results in new band formation within the available density of states (Fig. 4). The colors in Fig. 3 show the QD states for the excited states.

As identical quantum dots (QDs) are brought together, they form a QD array where their wave functions become highly extended, and their energy level becomes very small. Consequently, the energy bands formed by the QDs exhibit continuity rather than discrete levels,²⁷ as shown in Fig. 4. This can be explained using the QD Bloch state, *i.e.*, e^{ikz} , where the QD wavenumber ' k ' lies between $-\pi/L$ to π/L where L is the measure of one period ($L_{qd} + L_{br}$). Within this range, certain energy intervals between the intrinsic barriers (IBs) are unoccupied by the QD energies, resulting in energy gaps. These gaps represent regions with zero density of states, where carriers cannot thermally depopulate from the conduction band (CB) to the intrinsic barrier due to the delocalization of wave functions in the ground state energy.¹¹ Fig. 4 particularly estimates the variation in miniband formation for interdot spacing and size

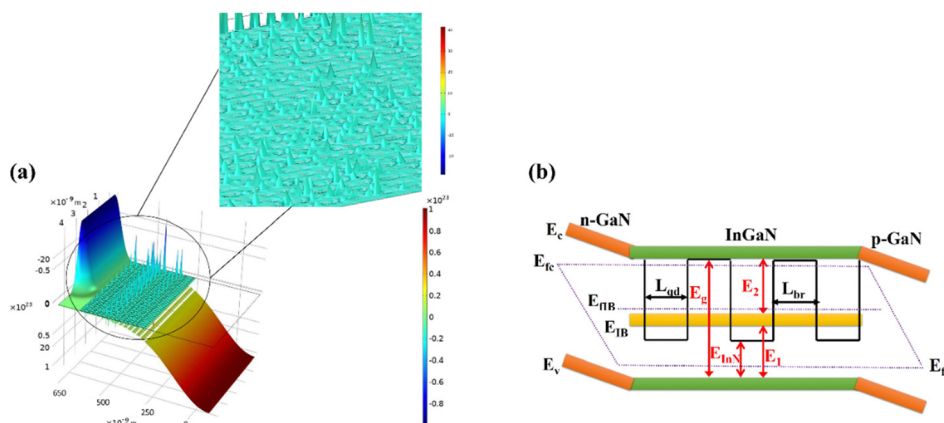


Fig. 2 (a) Three-dimensional doping profile of the proposed device structure; the inset shows the ground state energy of the QD wave function. (b) Band structure of QD-IBSC, showing transitions from VB to IB (E_1) and IB to CB (E_2), their Fermi levels (E_{fIB} , E_{fv} and E_{fc}) and energy gaps (E_g and E_{InN}).

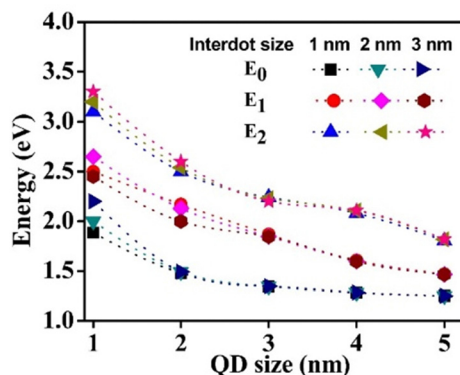


Fig. 4 Variation of the first optically strongest four states in the conduction band interdot spacing.

of the QD. The width of the E_0 miniband at $L_{qd} = 1$ nm is 403.6 eV; at $L_{qd} = 3$ nm it is 60.9 eV and it is lowered as the QD size decreases or the distance between vertically stacked QDs increases. For small QD sizes, the E_1 , E_2 and E_3 are so close that they overlap with the CB edge of the barrier material. Increasing the QD size decreases the gap between the ground states of the hole and electrons (IB-VB).

The inclusion of thin interlayers is crucial for absorbing excess indium and relieving compressive strain. These GaN interlayers need to strike a balance between being thick enough to be effective and thin enough to facilitate carrier transport through tunneling. The $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$ QD layers should be thick enough to capture the incident light beam while remaining fully strained. Fig. 5(a) exhibits increasing interlayer effects on the electrical parameters of QD-IBSC. Critical thickness plays a very vital role in strain layers. The barrier height at higher indium concentrations causes current transport through tunneling. The tunneling current diminishes even when the barrier thickness remains constant. The thickness of the GaN interlayer decreases the power conversion efficiency, as shown in Fig. 5(b).

Fig. 6(a) depicts the relationship between the J_{sc} and η as a function of the number of QD layers. It is observed that the increasing slope of J_{sc} reaches a maximum value of 34.2 mA cm^{-2} ,

while the efficiency peaks at 20 layers. Additionally, the V_{oc} also experiences an increase in the proposed structure. During illumination, a significant number of photons are absorbed in the top n-layer. Due to the higher mobility of electrons compared to holes, the electrons are transported from the n-layer to the p-layer. The energy band bending depends on the interfaces and the electric field induced within the materials, specifically, GaN and $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}$. The total induced polarization ($E_{\text{polarization}}$), as discussed in the device theory section, is reduced. Moreover, the built-in electric field ($E_{\text{built-in}}$) aligns in the same direction, facilitating the movement of carrier charges from the n-layer to the p-layer. This phenomenon contributes to the increased efficiency depicted in Fig. 6(b). Therefore, it can be concluded that the optimized configuration for maximum efficiency consists of up to 20 layers according to the proposed structure. It is worth noting that the literature suggests that increasing the number of QD layers introduces strain.^{5,38–40} However, the inclusion of i-GaN interlayers absorbs the strain generated at the interfaces, leading to an enhancement in both J_{sc} and η .

Fig. 7(a) and (b) provide insights into the J - V characteristics and efficiency of the QD-IBSC with respect to different parameters. It is observed that both the J - V characteristics and efficiency show an increasing trend as the QD size increases. The maximum efficiency achieved is 45% under the conditions of $L_{br} = 3$ nm, $L_{qd} = 3$ nm, and $x = 0.5$. For smaller QD sizes, the IB widens, leading to an increased carrier concentration and current. The V_{oc} remains constant for two values, then increases, and becomes constant again. The size of the quantum dot significantly influences the performance of the QD-IBSC. Larger QD sizes result in a lower position of the IB, allowing more space for accumulating bands and the creation of additional IBs. However, there is a limit to the number of IBs that can be formed. In this particular device, three bands are created within the forbidden region, leading to the generation of additional electron-hole pairs and enhancing the device's efficiency. In Fig. 7(c), it is demonstrated that the energy is maximum for the smallest QD size. The wave functions of the electrons are localized within the QDs, and the quantum confinement effect causes discrete energy levels rather than continuous energy levels. The sub gap decreases as the QD size

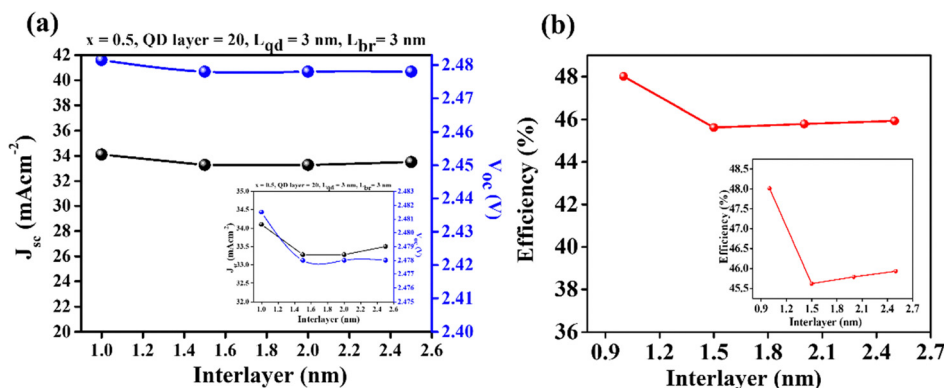


Fig. 5 (a) J - V characteristics and (b) efficiency of $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}/\text{GaN}$ QD-IBSC as a function of interlayers with QD layer = 20, $L_{qd} = 3$ nm, and $L_{br} = 3$ nm, respectively.

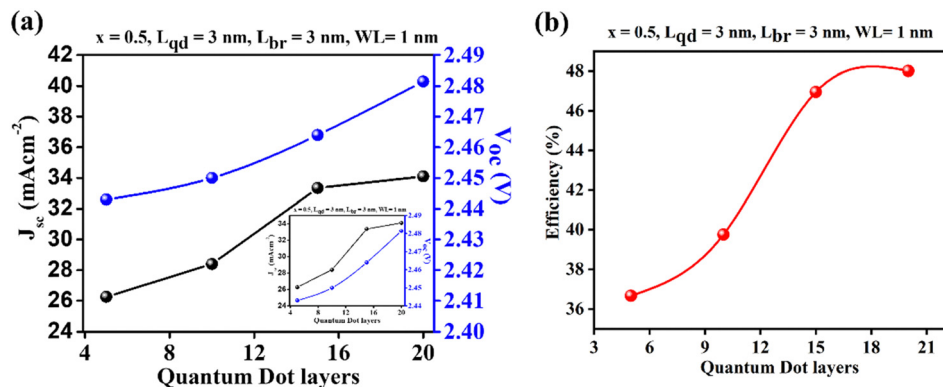


Fig. 6 (a) J - V characteristics and (b) efficiency of $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}/\text{GaN}$ QD-IBSC as a function of QD layers with $L_{qd} = 3$ nm, $L_{br} = 3$ nm, respectively.

increases due to this quantum confinement effect within the QDs.

Fig. 8(a) shows that an increase in the interdot size leads to a decrease in the J_{sc} . This reduction is attributed to the localization of QDs as the L_{br} increases. The weaker coupling of the wave functions results in individual QD behaviour, rather than a collective band behaviour. Additionally, the interdot size influences the width of the IB. Larger interdot sizes lead to higher sub-bandgap transition energies,⁵³ resulting in lower

overall efficiency. Fig. 8(b) illustrates the optimum efficiency of 49% obtained with specific parameters: L_{qd} of 3 nm, L_{br} of 1 nm, and x of 0.5. It shows a decrease in efficiency, which drops abruptly and significantly affects the performance of the QD-IBSC. This decrease is primarily attributed to recombination rates, especially radiative recombination, becoming dominant for small interdot distances. The reduction in bandgap at an indium composition of 0.5 contributes to this effect. On the other hand, Fig. 8(c) demonstrates the relationship between

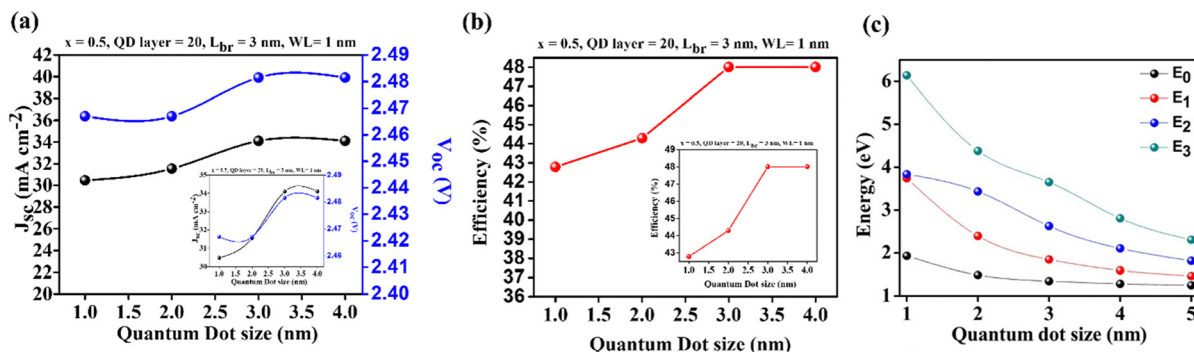


Fig. 7 (a) J - V characteristics, (b) efficiency and (c) excited state energies of $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}/\text{GaN}$ QD-IBSC as a function of QD size and IB formation in the CB for $x = 0.5$, QD layers = 20, $L_{br} = 3$ nm and $WL = 1$ nm.

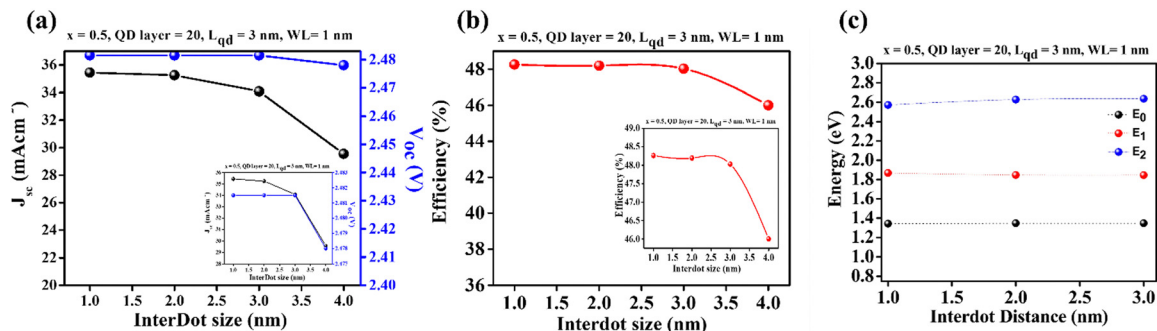


Fig. 8 (a) J - V characteristics, (b) efficiency and (c) E_0 , E_1 , E_2 of $\text{In}_{0.5}\text{Ga}_{0.5}\text{N}/\text{GaN}$ QD-IBSC as a function of distance between two QDs for $x = 0.5$, QD layers = 20, $L_{qd} = 3$ nm and $WL = 1$ nm.



Table 2 Photovoltaic parameters of QD-IBSC with different QD layers

Concentration	QD layer	QD size (nm)	Interdot (nm)	J_{sc} (mA cm ⁻²)	V_{oc} (V)	FF (%)	η (%)
0.5	5	3	3	20.27	2.44	74.39	36.669
	10			28.4	2.45	57.14	39.76
	15			33.35	2.464	60.79	46.95
	20			34.1	2.451	57.5	48.01

interdot distance and energy. When QDs are stacked at specific distances and sizes, wave function delocalization occurs, forming an IB. The interdot distance variation affects the bandwidth of the IBs, where larger interdot distances result in narrower bandwidths and discrete energy levels. A summary of this work is presented in Table 2.

Conclusion

In this paper, we proposed an optical structure that could increase photoelectric efficiency by applying and optimizing i-GaN layers in the active layer. The applied 1 nm thick i-GaN layer could compensate for the lattice mismatch caused by the In_{0.5}Ga_{0.5}N QD/GaN layer and absorb the excess strain to increase efficiency. We investigated the optical effect of the i-GaN interlayer by calculating the optical properties of Ga-face n-i-p QD-IBSCs in In_{0.5}Ga_{0.5}N/GaN arrays containing the i-GaN interlayer in the active layer under illumination. In our calculations, we applied 20 stacked high-concentration indium QD layers (In_{0.5}Ga_{0.5}N) that consist of 3 nm of QD size, 3 nm of an inter-dot size and 1 nm of a GaN layer ($E_g = 1.6875$ eV,) respectively. As a result, the photovoltaic efficiency of the device In_xGa_{1-x}N QD-IBSCs with an interlayer structure could potentially reach 48%. The optimal quantum dot structure size, interlayer thickness, and interdot spacing must be meticulously considered in the fabrication of QD-IBSCs using molecular beam epitaxy. This study is anticipated to provide solutions to the challenges encountered in the experimental fabrication of In_xGa_{1-x}N QD-IBSCs.

Author contributions

D. E. conceptualized the theoretical framework, simulated the device and wrote the manuscript. J. J. supervised and edited the manuscript. A. I. helped in simulation, and investigation of the device. A. A. K. revised the manuscript and helped in writing, and editing the visualizations.

Conflicts of interest

There are no conflicts to declare.

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