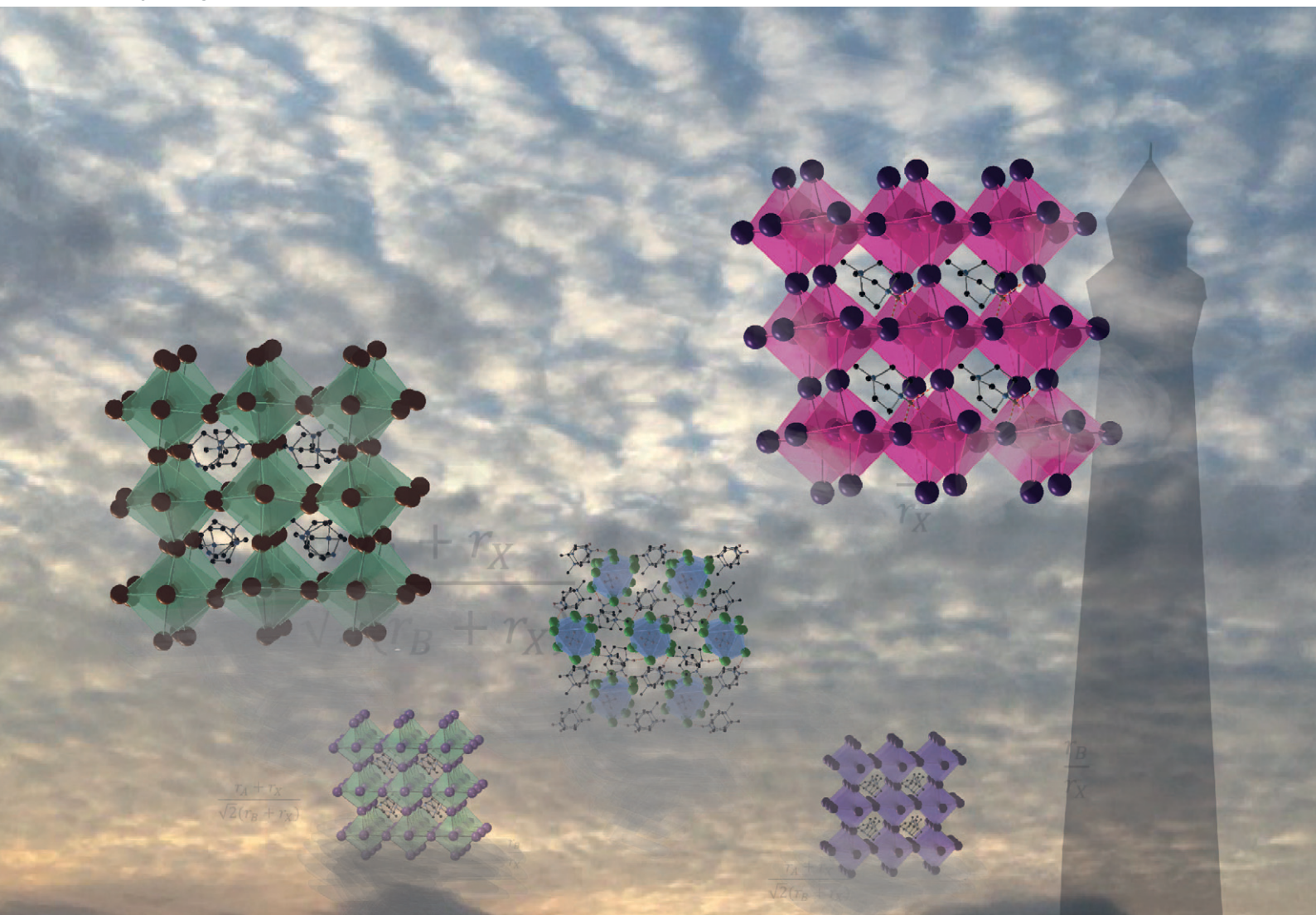


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Materials discovery and design limits in MDABCO perovskites†

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We report the structures of three new materials in the MDABCO-based perovskite family. Analysis of the Goldschmidt tolerance factor and octahedral factor enable us to propose compositional limits for pseudo-cubic perovskite phase formation and suggest directions for further materials discovery in this family of new ferroelectrics.

1. Introduction

Discovery and development of new ferroelectric materials is important for the realisation of new memory storage technology, such as FE-RAM in flexible devices, soft robotics and wearable electronics. Perovskites, such as BaTiO₃, have long been considered state-of-the-art in design of new FE materials owing to desirable properties and tunability of their composition.¹ Perovskites adopt the general formula ABX₃, where a larger A-site cation occupies the cavities within a pseudo-cubic corner-sharing network of BX₆ octahedra. Substitutions on any of the three sites has been shown to result in remarkable changes in FE properties.

The discovery of a new subset of hybrid organic–inorganic perovskites^{1e} based on the A-site MDABCO dication (MDABCO = *N*-methyl-*N'*-diazabicyclo[2.2.2]octonium) has led to renewed interest in hybrid inorganic–organic FE materials, owing to their properties that are comparable to BaTiO₃.² Variation in the B and X sites has given rise to four MDABCO-based halide perovskites to date: [MDABCO]RbI₃,^{2a} [MDABCO]NH₄I₃,^{2b} [MDABCO]KI₃ (ref. 2c) and [MDABCO]NH₄Br₃.^{2b} The ammonium iodide variant, in particular, has a large spontaneous polarization, high phase transition temperature and facile switching through eight possible polarisation directions. Factors thought to be important in driving spontaneous and switchable polarisation of MDABCO-based perovskites are the quasi-spherical nature of the A-site cation,³ orientation of the MDABCO dipole

moment along the pseudo-cubic $\langle 111 \rangle$ direction, strain coupling and dipolar interactions.⁴ Hydrogen bonding, whilst it does not drive FE behaviour, has been shown to be important in determining the magnitude of polarisation and coercive field.⁵

Formation of new perovskites requires the assembly of the BX₆ octahedra, which can empirically be predicted by the radius ratio or octahedral factor, $OF = r_B/r_X$, where r_B and r_X are the ionic radii of the B-site cation and X-site anion, respectively.⁶ Octahedra are expected to form in the range $0.41 \leq OF \leq 0.732$. In addition, design rules typically consider the Goldschmidt tolerance factor (TF) as a necessary criterion for their formation.⁷

$$TF = \frac{(r_A + r_X)}{\sqrt{2}(r_B + r_X)},$$

where in our case r_A is the effective radius of MDABCO. It has been found that values in the range $0.9 \leq TF \leq 1.0$ result in the formation of the pseudo-cubic ABX₃ structure in MDABCO-based perovskites.^{2b} It is therefore surprising that not more compositions of MDABCO-based perovskites have been reported; just within the alkali metal (and ammonium) halides, at least twelve compositions appear to satisfy this tolerance factor criterion (Table 1).

The discovery of new compositions is necessary to test how exactly each factor contributes to the ferroelectric performance, to refine our understanding of this important class of FE materials and suggest design rules for new materials. However, it is not yet clear where the compositional limits for MDABCO-based perovskite formation lie, knowledge of which would help to improve the success of future discovery efforts.

In this work, we report three new compositions in the [MDABCO]BX₃ family, namely [MDABCO]CsI₃, [MDABCO]RbBr₃ and [MDABCO]NH₄Cl₃, discovered in the course of a systematic investigation of the different compositions

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Table 1 Tolerance factors of selected [MDABCO]BX₃ compositions calculated (see ESI† section S3) following the method of Kieslich *et al.*^{7b} Polar phases are denoted with an asterisk. Previously reported compositions are shaded in light blue, those reported in this work are shaded in grey and as-yet unreported compositions are unshaded

A-site cation = [MDABCO] ²⁺	X-site anion		
	Cl [−]	Br [−]	I [−]
K ⁺	1.00	0.99	0.97 ^{*,a}
B-site [NH ₄] ⁺	0.98	0.96 ^{*,b}	0.95 ^{*,b}
cation Rb ⁺	0.96	0.95 [*]	0.93 ^{*,c}
Cs ⁺	0.92	0.91	0.90 [*]

^a Pseudo-cubic structure reported by An *et al.*^{2c} ^b Pseudo-cubic structures reported by Ye *et al.*^{2b} ^c Pseudo-cubic structure reported by Zhang *et al.*^{2a}

afforded by combinations of K⁺, [NH₄]⁺, Rb⁺ and Cs⁺ with Cl[−], Br[−] and I[−]. We are thus able to define upper limits to the compositional range of pseudo-cubic MDABCO-based perovskites with respect to TF and OF, and suggest directions for the exploration of further compositions in future.

2. Experimental methods

Single crystals were synthesised at ambient temperature using protocols similar to previous reports and structures were determined at ambient temperature using single crystal X-ray diffraction either in-house or at beamline I19-2, Diamond Light Source. Full details of all synthesis and crystallography can be found in the ESI† sections S1 and S2.

3. Results and discussion

3.1 Pseudo-cubic perovskite [MDABCO]CsI₃

Crystallisation at room temperature of a reaction mixture containing MDABCO, Cs⁺ and I[−] resulted in the formation of crystals with rhombohedral symmetry that solved in the polar space group *R*3̄. Owing to the threefold symmetry, the asymmetric unit consists of one third of an MDABCO molecule, one third of a Cs⁺ cation and one I[−] anion. The crystal structure overall has three ABX₃ formula units per unit cell, which has the metric *a* = *b* = 9.8648(5) Å, *c* = 13.7921 Å, $\alpha = \beta = 90^\circ$, $\gamma = 120^\circ$ in the hexagonal setting. The cell volume, *V* = 1162.35(13) Å³; *i.e.*, the volume per formula unit *V'* = *V*/*Z'* = 387 Å³.

The structure consists of corner-sharing CsI₆ octahedra with MDABCO dications occupying the large intra-framework A-site cavities (Fig. 1), isostructural with the previous compounds [MDABCO]RbI₃ and [MDABCO]NH₄I₃. The N–N axes of the MDABCO molecules lie along the three-fold axes of the cell, parallel to the [111] direction with respect to the pseudo-cubic perovskite cell. Like the parent compounds, the MDABCO dication is involved in three weak hydrogen bonds

to nearby framework I[−] anions *via* the N–H group (N–I distance 3.76(3) Å). The similarities between these features and those of existing ferroelectric MDABCO-based perovskites suggest that [MDABCO]CsI₃ has the strong potential to exhibit ferroelectricity itself.

The distorted CsI₆ octahedra exhibit Cs–I distances within the range 3.682(3)–3.692(3) Å, which is slightly longer than the NH₄⁺ and Rb⁺ analogues. The bond valence sum (BVS)⁸ for Cs is 1.54, which suggests that I[−] anions can approach the B-site more closely than would normally be expected for Cs⁺; this may be related to the polarizability of Cs and I, and the OF, 0.76, of [MDABCO]CsI₃, which is larger than its previously reported analogues. We note also that although the structure refines well with full occupancy of all the atoms, we observe slightly improved fit statistics when the occupancy of the Cs⁺ cation is allowed to refine, converging to around 0.8.

This observation may be related to the above-average BVS and suggests that the structure contains randomly distributed substitutions of much lighter cations, such as H⁺, on the B-site and/or Cs⁺ vacancies co-existing with oxidation of the iodide sublattice, neither of which can easily be detected by X-ray diffraction.

The nearest neighbour I–Cs–I angles are within the range 78.89–102.89°, and the sum of deviations from the ideal octahedral angle,⁹ $\sigma = 81^\circ$, is within the range of existing MDABCO-based perovskites ($\sigma = 70$ – 92°). Although the CsI₆ octahedra are highly distorted, they do not exhibit any tilting in the conventional sense. Application of ISODISTORT¹⁰ confirms that the [MDABCO]CsI₃ structure can be assigned the Glazer notation *a*⁰*a*⁰*a*⁰.¹¹

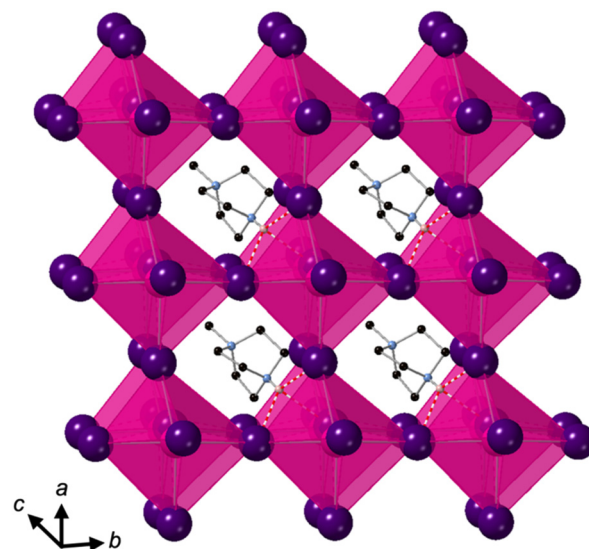


Fig. 1 Four adjacent pseudo-cubic motifs of [MDABCO]CsI₃, showing alignment of the MDABCO N–N axes along the unique axis (*c*). C, N, Cs and I are shown in black, blue, pink and purple, respectively. H atoms are omitted for clarity, apart from N–H atoms (pink) involved in hydrogen bonds, which are indicated by dashed red lines.



3.2 Pseudo-cubic perovskite [MDABCO]RbBr₃

[MDABCO]RbBr₃ forms at room temperature in the space group *Pna*2₁, which has spontaneous polarisation along the orthorhombic *c*-axis. There are four symmetry-related MDABCO dications per unit cell, which has the metric $a = 14.1838(10) \text{ \AA}$, $b = 9.9322(6) \text{ \AA}$, $c = 9.6159(6) \text{ \AA}$, $\alpha = \beta = \gamma = 90^\circ$. The cell volume, $V = 1354.65(15) \text{ \AA}^3$; i.e., $V' = 339 \text{ \AA}^3$.

The structure consists of a framework of distorted corner-sharing RbBr₆ octahedra with MDABCO dications occupying the perovskite A-site within the pseudo-cubic intraframework cavities (Fig. 2). In contrast to existing MDABCO-based perovskites, the N–N axis of the MDABCO dications are oriented along alternating pseudo-cubic $\langle 110 \rangle$ directions, which are tilted with respect to the crystallographic *c*-axis. If the overall polarisation was found to be switchable it would, therefore, constitute “ferrielectricity”. Each MDABCO dication has a single short N–H⋯Br hydrogen bond (N–Br distance 3.159(8) Å) stabilising its interactions with the RbBr₃ framework, rather than three weak hydrogen bonds as are found in other MDABCO-based perovskites.

The distorted RbBr₆ octahedra exhibit Rb–Br distances within the range 3.452(1)–3.654(1) Å. The BVS for Rb is 0.813, which indicates that the Rb⁺ cation is underbonded; it has the highest OF (*vide infra*) of the known pseudo-cubic perovskites. The average deviation from the mean Rb–Br distance is 18%, which is much larger than existing MDABCO-based perovskites (3–8%). However, nearest neighbour Br–Rb–Br angles are within the range 81.4–101.41°, such that the sum of deviations from the ideal octahedral angle, $\sigma = 68^\circ$, is slightly lower than existing

MDABCO-based perovskites. Application of ISODISTORT¹⁰ shows that the octahedral tilts of [MDABCO]RbBr₃ can be assigned the Glazer notation $a^-a^-c^0$.

3.3 Hexagonal-type perovskite [MDABCO]NH₄Cl₃

[MDABCO]NH₄Cl₃ forms at room temperature in the space group *P*2₁/*n*, which is centrosymmetric and, therefore, is not expected to exhibit FE properties at ambient temperature. The asymmetric unit consists of two MDABCO dications, six Cl[−] anions and two [NH₄]⁺ cations. One of the [NH₄]⁺ cations is disordered across an inversion centre with 50% occupancy on each of two sites. The other has an elongated anisotropic displacement ellipsoid, which is suggestive of similar disorder. These displacements coincide with the longest octahedral Cl–Cl axes, which suggests they occur in order to optimise ionic and/or hydrogen bonding interactions. The crystal structure overall has eight ABX₃ formula units per unit cell, which has the metric $a = 14.8238(4) \text{ \AA}$, $b = 10.1333(3) \text{ \AA}$, $c = 16.4441(4) \text{ \AA}$, $\alpha = 90^\circ$, $\beta = 90.577(2)^\circ$, $\gamma = 90^\circ$. The cell volume, $V = 2470.01(12) \text{ \AA}^3$; i.e., $V' = 309 \text{ \AA}^3$.

The structure consists of face-sharing chains of NH₄Cl₆ octahedra aligned along the *a*-axis and the chains are arranged in a hexagonal close-packed array (Fig. 3) similar to CsNiCl₃ and BaNiO₃,¹² and the analogous dabconium structure (dabconium = [C₆H₁₄N₂]²⁺).¹³ MDABCO dications lie between the chains with their N–N axes oriented along a variety of directions within the *bc*-plane. There are two short hydrogen bond lengths between MDABCO N–H functionalities and Cl[−] anions of the chains, which have N–Cl distances of 2.998 Å and 3.005 Å.

The distorted NH₄Cl₆ octahedra exhibit N–Cl distances in the range 3.154–4.25 Å; each [NH₄]⁺ cation has one long N–Cl interaction and five shorter N–Cl interactions, which are indicative of dipole-assisted hydrogen bonding. The effective BVSS¹⁴ of the two [NH₄]⁺ cations are 0.90 and 0.96, which indicates that the intermolecular interactions are satisfied in this arrangement with off-centred [NH₄]⁺ cations. Nearest neighbour Cl–N–Cl angles are within the range 74.2° to 107.3°. However, the sum of deviations from the ideal octahedral angle, σ , are 71° and 83°, which is well within the range of existing MDABCO-based perovskites.

3.4 Phase behaviour

Analysis of the three structures reported herein alongside the existing MDABCO-based perovskites reveals certain compositional limits in their phase behaviour, which can be quantified by TF and OF ranges (Fig. 4). All three new structures have TF values that fall within the previously proposed range for pseudo-cubic perovskite formation (see sections S3 and S4 in the ESI†).^{2b} However, in contrast to previous computational studies that assumed a pseudo-cubic perovskite for [MDABCO]NH₄Cl₃,¹⁵ we have found that it forms a hexagonal-type structure. Therefore, an upper TF limit can be defined between its TF, 0.98, and the highest TF

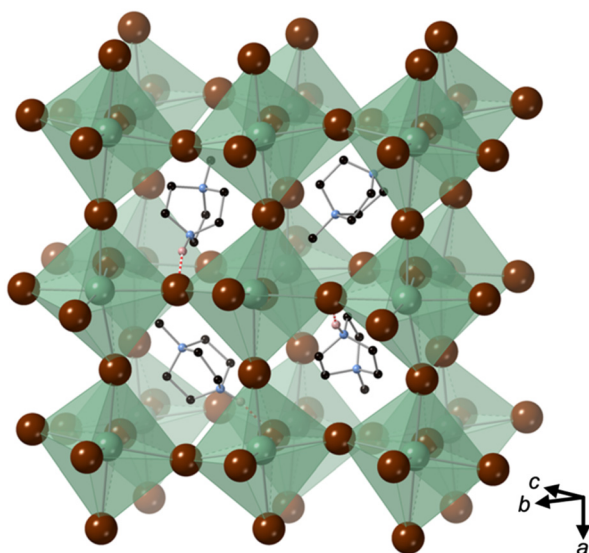


Fig. 2 Extended unit cell of [MDABCO]RbBr₃, showing the tilted orientations of four MDABCO dications within the pseudo-cubic framework of corner-sharing RbBr₆ octahedra. C, N, Rb and Br are shown in black, blue, green and brown, respectively. H atoms are omitted for clarity, apart from N–H atoms (pink) involved in hydrogen bonds, which are indicated by dashed red lines.



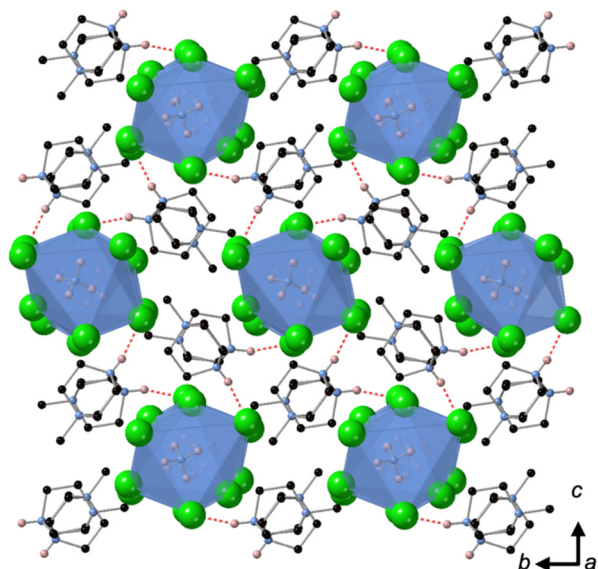


Fig. 3 Crystal structure of [MDABCO]NH₄Cl₃ containing a hexagonal array of chains of face-sharing NH₄Cl₆ octahedra aligned along the *a*-axis, showing the orientations of MDABCO dications between them. C, N and Cl are shown in black, blue and green, respectively. H atoms are omitted for clarity, apart from ammonium and MDABCO N–H atoms (pink) involved in hydrogen bonds, which are indicated by dashed red lines.

of known pseudo-cubic structures, 0.97, which is observed for [MDABCO]KI₃. This is somewhat reflected in the trends in the crystallographic volume per MDABCO dication, and a similar observation can be made regarding the lower limit of *V'*. Owing to the small size of the [NH₄]⁺ and Cl[−] ions, [MDABCO]NH₄Cl₃ has a lower *V'* (309 Å³) than the pseudo-cubic MDABCO halide perovskites (see section S5 in the ESI†). We can thus define a lower *V'* limit for pseudo-cubic perovskite formation between 309 Å³ and 339 Å³, which is the value of *V'* found for the smallest pseudo-cubic perovskite, [MDABCO]RbBr₃.

All the new structures reported herein have OF values above those of previously reported structures and, interestingly, all fall outside of the empirical range, 0.414–0.732, required for BX₆ octahedron formation.^{6a} However, both [MDABCO]RbBr₃ and [MDABCO]CsI₃ are found to form pseudo-cubic perovskites, owing to the high polarizability of the heavy ions involved. We can define an upper OF limit between the OF of [MDABCO]RbBr₃, 0.78, and that of the hexagonal-type structure [MDABCO]NH₄Cl₃, 0.81. Our initial analysis of crystals formed from the reaction of MDABCO with Cs⁺ and Br[−] appears to confirm this trend. The high OF value of 0.85 should prohibit pseudo-cubic perovskite formation even though [MDABCO]CsBr₃ falls within the TF range and, indeed, we observe a structure with similarities to other hexagonal-type halide perovskites,¹³ although we should note that refinement of this structure is ongoing.

Comparison of BVSS shows that structures close to the TF and OF limits deviate most from the ideal value of 1 for monovalent cations (see ESI section S6†), which may be

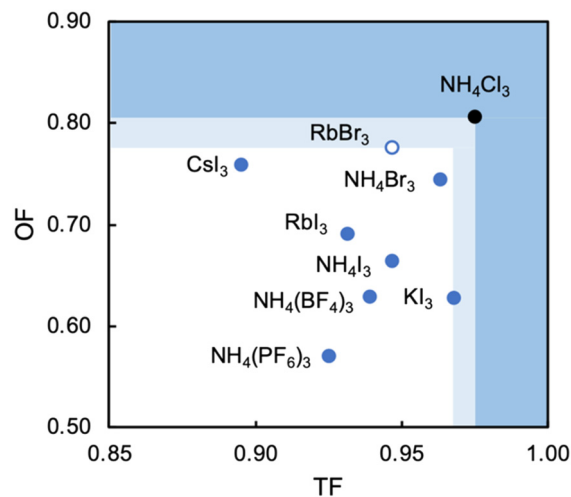


Fig. 4 Phase behaviour of MDABCO-based perovskites as a function of tolerance factor (TF) and octahedral factor (OF), showing B- and X-site compositions. Blue circles are pseudo-cubic perovskites with $\langle 111 \rangle$ MDABCO orientations. The open circle is the pseudo-cubic perovskite with $\langle 110 \rangle$ MDABCO orientations. The black circle is the hexagonal-type structure, which defines upper limits of ranges for pseudo-cubic perovskite formation, $0.97 < TF < 0.98$ and $0.78 < OF < 0.81$, shown in light blue. Darker blue shaded regions lie above these limits.

related to their borderline status and other properties. [MDABCO]KI₃ has exceptional mechanical properties,^{2c} whilst [MDABCO]RbBr₃ contains MDABCO dications in unusual $\langle 110 \rangle$ orientations.

4. Conclusions

In summary, we have described the new structures of three MDABCO-based materials in the ABX₃ perovskite family. The cesium iodide variant adopts a polar *R3* structure in common with its parent compounds and is expected to be ferroelectric. The low value of its TF, 0.90, extends the TF range of known MDABCO-based perovskites. The rubidium bromide variant contains MDABCO dications somewhat unusually oriented in $\langle 110 \rangle$ directions, tilted in alternating fashion such that the *Pna2*₁ structure is also polar. It has the highest OF, 0.78, of any known pseudo-cubic MDABCO-based perovskite. On the other hand, the ammonium chloride variant adopts a non-polar hexagonal-type structure, which allows us to define for the first time an upper TF limit of $0.97 < TF < 0.98$ and an upper OF limit of $0.78 < OF < 0.81$.

Whilst the TF for [MDABCO]CsI₃, 0.90, extends the range of TF in known MDABCO-based perovskites towards low TF values, the lower bounds for TF and OF remain undetermined. We expect that discovery of new MDABCO-based perovskites may be most successful using larger X-site anions to explore low TF and OF combinations, *i.e.*, towards the bottom left region of Fig. 4. For example, [MDABCO]NH₄(BF₄)₃ and [MDABCO]NH₄(PF₆)₃ have recently been shown to adopt pseudo-cubic perovskite structures¹⁶ and our TF and OF calculations suggest that all K, Rb and Cs



analogues with $[\text{BF}_4]^-$ and $[\text{PF}_6]^-$ on the X-site may also form, but to the best of our knowledge no other compositions have been reported.

The structures of the remaining halides shown in Table 1 currently remain undetermined, despite significant efforts in the lab. Our TF and OF analysis may explain why: Rb–Cl, Cs–Cl and Cs–Br have TF within the proposed perovskite formation range, and K–Cl and K–Br have OF within the expected range. However, none satisfy the criteria for both TF and OF together, which may explain why no chloride-based pseudo-cubic MDABCO perovskites have been reported to date. We may expect them to form alternative isomers, such as the hexagonal-type structure formed by $[\text{MDABCO}]\text{NH}_4\text{Cl}_3$ or different topologies altogether. Further work is required to synthesise them and determine their crystal structures.

Finally, we note that unusual $\langle 110 \rangle$ orientations of MDABCO in $[\text{MDABCO}]\text{RbBr}_3$ run counter to our previous observation that $\langle 111 \rangle$ orientations are required for spontaneous polarisation.⁴ This suggests that new and interesting properties may arise at the TF and OF boundaries. Preliminary results of differential scanning calorimetry in our lab indicate the existence of high-temperature phase transitions in all three structures reported herein, and further investigation into structural features that affect phase transitions and dielectric properties of the materials is ongoing.

Author contributions

Conceptualization: HHMY, PAA. Formal analysis: SDG, HJL, HHMY. Funding acquisition: HHMY, HJL. Investigation: SDG, HJL, LM, MRW, LKS. Methodology: SDG, HJL, LM. Project administration: HHMY, PAA. Supervision: MRW, LKS, PAA and HHMY. Writing – original draft: HHMY. Writing – review & editing: all authors.

Conflicts of interest

There are no conflicts to declare.

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