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# H<sub>2</sub>-rich syngas production from gasification involving kinetic modeling: RSM-utility optimization and techno-economic analysis

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In this research article, H<sub>2</sub> rich syngas production is optimized using response surface methodology (RSM) and a utility concept involving chemical kinetic modeling considering eucalyptus wood sawdust (CH<sub>1.63</sub>O<sub>1.02</sub>) as gasification feedstock. By adding water gas shift reaction, the modified kinetic model is validated with lab scale experimental data (2.56 ≤ root mean square error ≤ 3.67). Four operating parameters (*i.e.*, particle size “*d<sub>p</sub>*”, temperature “*T*”, steam to biomass ratio “SBR”, and equivalence ratio “ER”) of air–steam gasifier at three levels are used to frame the test cases. Single objective functions like H<sub>2</sub> maximization and CO<sub>2</sub> minimization are considered whereas for multi-objective function a utility parameter (80% H<sub>2</sub>: 20% CO<sub>2</sub>) is considered. The regression coefficients ( $R_{H_2}^2 = 0.89$ ,  $R_{CO_2}^2 = 0.98$  and  $R_U^2 = 0.90$ ) obtained during the analysis of variance (ANOVA) confirm a close fitting of the quadratic model with the chemical kinetic model. ANOVA results indicate ER as the most influential parameter followed by *T*, SBR, and *d<sub>p</sub>*. RSM optimization gives H<sub>2|max</sub> = 51.75 vol%, CO<sub>2|min</sub> = 14.65 vol% and utility gives H<sub>2|opt.</sub> = 51.69 vol% (0.11%↓), CO<sub>2|opt.</sub> = 14.70 vol% (0.34%↑). The techno-economic analysis for a 200 m<sup>3</sup> per day syngas production plant (at industrial scale) assured a payback period of 4.8 (~5) years with a minimum profit margin of 142% when syngas selling price is set as 43 INR (0.52 USD) per kg.

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## 1. Introduction

Energy is one of the prime drivers for the development of mankind. Existing energy demand is primarily fulfilled by fossil fuels (coal, oil, and natural gas), accounting for approximately 80% of global commercial and residential energy demand.<sup>1</sup> However, dependency on fossil fuels has not only raised the global average temperature but has also disrupted weather cycles in most parts of the world. Burning of fossil fuels releases CO<sub>2</sub> gas and hence efforts must be made by deploying some sustainable technologies to lessen the effect of greenhouse gas emission. Hydrogen, a highly pure form of green alternative gaseous fuel, has the highest energy density among all hydrocarbon fuels. Thus, H<sub>2</sub> can be considered as an alternate fuel for replacing fossil fuel in a sustainable way to produce energy. Biomass derived hydrogen is a clean renewable source of energy that could preserve the environment and improve energy security.<sup>2</sup> Compared to other thermo-chemical processes, gasification is preferred for H<sub>2</sub> as almost all the gasification products (mainly CO, H<sub>2</sub>, CO<sub>2</sub> and CH<sub>4</sub>) are in gaseous form only. Gasification reactions are carried out in a controlled

environment [H<sub>2</sub>O(g), O<sub>2</sub>(g), & air(g)] and hence it is referred as steam-, oxy- and air-gasification. Steam is favoured over other gasifying agents as it enhances the combustible quality of syngas by improving H<sub>2</sub>(g) production and accelerating the steam gasification, methane reforming and water-gas shift reactions. In addition to it, in steam gasification process, there is a tendency of reducing tar content, which is one of the major challenges during gasification.<sup>3</sup> Apart from the technological and designing aspects of gasifier there are other factors that influence H<sub>2</sub> yield in biomass gasification such as feedstock type, quality and inherent moisture content, particle size and density, reaction temperature, bed height, heating rate, environment, flow of medium, steam flow rate, addition of catalyst, sorbent to biomass ratio, *etc.*

For computing the energy value/potential of a given biomass, researchers conducted experimental analysis in a lab scale setup. Alternatively, different methods on kinetic modeling are also available for predicting the same in a limited time/cost and that is why kinetic model technique is mostly adopted for gasification analysis. A chemical kinetic model is developed by Champion *et al.*<sup>4</sup> to understand the effect of equivalence ratio, temperature on syngas compositions. The plug flow distribution of the product gases, coming out from the bed, is approximated same as the output of ten continuous stirred tank reactors (CSTRs) in series. Results indicate that equivalence ratio (ER) from 0.25 to 0.35 and temperatures from 950 to 1050

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K are the major contributing parameters for H<sub>2</sub>-rich syngas production. Cao *et al.*<sup>5</sup> utilized “The Peng-Robinson/Boston–Mathias (PR-BM) equation of state” based Aspen Plus model for gasification of pine sawdust. The impact of variation in ER, SBR on gas compositions, tar yield and gas yield was observed. The analyses showed that SBR is an influential parameter for gasifier performance whereas CO and CH<sub>4</sub> gas composition diminishes with change in ER from 0.21 to 0.23. A Gibbs free energy minimization method based ASPEN Plus model was studied by Pala *et al.*,<sup>6</sup> Nikoo and Mahinpey<sup>7</sup> and Shahbaz *et al.*<sup>8</sup> The authors reported that H<sub>2</sub> shows linear trend with increase in temperature from 750 to 950 °C whereas it increases with change in SBR from 0.2 to 1 (Pala *et al.*<sup>6</sup>). Shahbaz obtained minimum CO<sub>2</sub> (5.42 vol%) and maximum H<sub>2</sub> (79.32 vol%) for SBR of 1.5, temperature of 700 °C, and sorbent to biomass ratio of 1.42 respectively.<sup>8</sup> Nikoo and Mahinpey<sup>7</sup> addressed both reaction kinetic modeling and hydrodynamic parameters for the gasification of pine sawdust. The article revealed the proportional relation between SBR & temperature with H<sub>2</sub> and CO gas composition, and ER with CO<sub>2</sub> concentration.

In the field of biomass gasification, applying statistical approaches to analyze the effect of process parameters is an interesting research area to the scientists working in this field. Different optimization techniques are used for optimizing hydrothermal gasification process such as Taguchi method, Response Surface Methodology (RSM), Univariate approach, Factorial method *etc.* RSM has the advantage of intra-parameters effect and requirement of fewer experiments over other optimization techniques.<sup>9</sup> On a CFD model for optimizing Portuguese biomass gasification, Silva and Rouboa<sup>10</sup> observed that for domestic natural gas application forest residue was found to be a preferred substrate followed by vine pruning waste for fuel cell. In a rice husk pyrolysis process Bakari *et al.*<sup>11</sup> used RSM technique for optimization. A quadratic model for gas yield and a cubic model for bio-oil yield were proposed in the article. ANOVA results of the RSM technique revealed the optimum bio-oil yield (36.72%) and gas yield (73.25%) conditions. Zaman *et al.*<sup>12</sup> considered parameters namely steam to biomass ratio and gasification temperature to conduct optimization study on steam-gasification process. Results showed that H<sub>2</sub> rich syngas production and cold gas efficiency goes up to 58% and 90% respectively. Recently, Singh and Tirkey<sup>13</sup> performed RSM based optimization of biomass air gasification. Typical parameters such as equivalence ratio, moisture content, and gasification temperature are varied to optimize hydrogen yield, HHV and CGE. For each optimizing function, RSM gives a mathematical model where the results identified gasification temperature as the most significant factor. To optimize a given objective function, RSM is preferred over other optimization techniques though in many engineering application, there are several factors that need to be optimized simultaneously for achieving the maximum utilization of the system. At that time, instead of targeting single optimizing function one has to consider multi-objective function. Hence, utility concept is important for analyzing multi-objective function. Rao *et al.*<sup>14</sup> employed graph theory & matrix approach (GTMA) and utility concept in micro-milling process for multi-response

optimization such as surface roughness, tool wear, cutter vibration. The mean utility value in ANOVA indicates that the parameter “depth of cut” has the maximum contribution for four different responses. In a similar work, the authors used RSM and utility technique to improve the machining characteristics.<sup>15</sup> By maximizing the utility value, it is concluded that nose radius (0.4 mm); cutting speed (170 m min<sup>-1</sup>); feed rate (0.1358 mm per rev) gives optimum process parameters.

After completing an extensive literature survey, the authors observed that most of the articles on gasifying problem consider different type of biomass using experimental technique or commercial software-based modeling and only a few employed optimization techniques with multi-objective function. In any gasification problem for a given biomass, usually it is targeted to obtain maximum H<sub>2</sub> production with least focus on environment like minimum release of CO<sub>2</sub> gas. Moreover, utilization of eucalyptus wood sawdust as a gasification feedstock material for H<sub>2</sub> rich syngas production was hardly investigated, especially from the point of view of production in large scale industrial level. In view of the above research gap, the current study is an attempt to throw light on finding a single solution for maximum utilization of eucalyptus wood sawdust (EWS) gasification process. For that, a chemical kinetic model developed by Wang and Kinoshita<sup>16</sup> has been modified by incorporating water gas shift reaction. Using this kinetic model different cases are designed and performed optimization using RSM technique with single objective functions like (i) maximizing H<sub>2</sub> production and (ii) minimizing CO<sub>2</sub> production. For multi-objective function, utility concept has been employed where both these objective functions are clubbed together into a single objective function and performed optimization for maximum utilization of the system. The present study considers four input parameters such as particle size, temperature, steam to biomass ratio, and equivalence ratio and two output parameters such as H<sub>2</sub> and CO<sub>2</sub> gas (vol%). In order to find out the feasibility of EWS biomass at industrial scale for H<sub>2</sub> gas production, a techno-economic study also has been performed. The following section elaborately discusses on the chemical kinetic model, RSM-utility optimization technique and techno-economic study of EWS biomass gasification.

## 2. Problem statement

### 2.1 Material and methods

Eucalyptus wood sawdust (EWS) used in the present study are collected from a wood processing shop at Meerut, Uttar Pradesh (India). Then, the sample is dried in an air-oven at 35 °C for 24 h, and separated by the certified tested sieves into particles (size range 100 to 1000 μm). The sieved samples are kept in a closed plastic zip-bag to minimize the moisture absorption from the environment. Characterization process of a given biomass gives information of mass% of H<sub>2</sub>O, volatiles, fixed carbon, ash, carbon, hydrogen, nitrogen, sulfur, and oxygen present in a sample. Fixed carbon and oxygen content are determined using difference formulas. American Society for

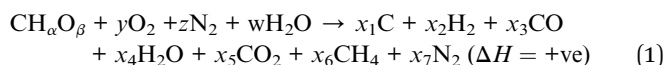


Testing Materials (ASTM) protocols<sup>17</sup> are adopted to perform characterization analysis (ASTM E871 for H<sub>2</sub>O, ASTM E872 for volatiles, ASTM D1102 for inert, ASTM E777 for carbon & hydrogen, ASTM E778 for nitrogen, and ASTM E775 for sulfur). The results obtained from the characterization process reveal that the biomass contains 7.76 mass% H<sub>2</sub>O, 75.38 mass% volatiles, 2.16 mass% ash, 40.12 mass% C, 5.462 mass% H, 0 mass% of S and N. Using difference formulas, the fixed carbon and oxygen content are computed as 14.70 mass% and 54.418 mass%, respectively. The EWS biomass can be expressed by empirical co-relation as CH<sub>1.63</sub>O<sub>1.02</sub> ( $\alpha = 1.63$  and  $\beta = 1.02$ ). The lower and higher heating value of EWS biomass (as-received) are computed as 13.58 and 14.78 MJ kg<sup>-1</sup>, respectively.

## 2.2 Kinetic model

It is a challenging task to develop a chemical kinetic model for biomass gasification due to large variation in feedstock material and changes in structural characteristics. Wang and Kinoshita<sup>16</sup> proposed a chemical kinetic model based on Langmuir–Hinshelwood mechanism where differential equations were formulated involving reaction rates for the syngas and char composition. Over other available models, this model is widely accepted and preferred because of its suitability for surface catalytic reactions.<sup>18</sup> The present kinetic model is an extended form of Wang and Kinoshita<sup>16</sup> where gas-shift reaction is additionally considered for computing the syngas composition close to the actual chemical reactions.

The air–steam biomass gasification occurs in a gasifier can be expressed in terms of general equation as:



where,  $\alpha = 1.63$  and  $\beta = 1.02$ , obtained from characterization of eucalyptus wood.

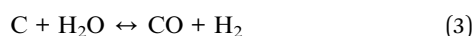
The operating range of temperature for reactions in the gasifier is from 900 K to 1200 K. The residue of eucalyptus wood reacts with the mixture of superheated steam and air that leads to conversion of biomass into syngas (H<sub>2</sub>, CO<sub>2</sub>, CO, and CH<sub>4</sub>) and biochar. At any given temperature the reaction is irreversible and always helps in production of hydrogen gas. Reactions occurred during the gasification process are given as follows:

Char gasification:

Boudouard reaction (R<sub>1</sub>):



Steam gasification (R<sub>2</sub>):

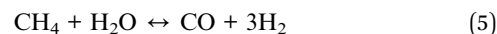


Hydrogen gasification (R<sub>3</sub>):



Homogeneous volatile reactions:

Methane–steam reforming (MSR) (R<sub>4</sub>):



Water-gas shift (WGS) (R<sub>5</sub>):



At  $t = 0$ , assuming  $x_2 = x_3 = 0$ ;  $x_7 = z$ , continuity equations are need to be satisfied and are expressed as:

Carbon balance:

$$x_1 + x_5 + x_6 = 1 \quad (7)$$

Hydrogen balance:

$$2x_4 + 4x_6 = \alpha + 2w \quad (8)$$

Oxygen balance:

$$x_4 + 2x_5 = 2y + \beta + w \quad (9)$$

Steam balance:

$$x_4 = \mu x_5 + w \quad (10)$$

where,  $\mu$  = ratio of steam to carbon dioxide. The current research work considers  $\mu = 1$  throughout the study.

Now, the rate equations, based on the Langmuir–Hinshelwood mechanism, can be given as:

For Boudouard reaction (R<sub>1</sub>):

$$-v_1 = \frac{k_1 K_5 C_T (p_5 - p_3^2 / k_{p1})}{1 + \sum K_i p_i} \quad (11)$$

where  $K_i$  is the adsorption constant for  $i$ th gas species,  $v_i$  is the net reaction rate for  $i$ th reaction and  $p_i$  is the partial pressure of  $i$ th gas species can be calculated as follows:

$$p_i = \frac{x_i}{P_X}, \quad \text{where } P_X = \frac{1}{p} \sum_{i=2}^7 x_i \quad (12)$$

Therefore,  $p_3 = \frac{x_3}{P_X}$  &  $p_5 = \frac{x_5}{P_X}$  and using

$C_T = \frac{72k_s}{\rho d_p} \left( \frac{x_1(t=0)}{x_1} \right)^{1/3}$   $x_1$  the Boudouard reaction (R<sub>1</sub>) eqn (11) can be rewritten as:

$$-v_1 = \frac{k_1 K_5 C_T (x_5 - x_3^2 / P_X k_{p1})}{P_X (1 + \sum K_i p_i)}$$

$$\Rightarrow -v_1 = \frac{k_1 K_5 C_T (x_5 - x_3 / P_X k_{p1})}{(P_X + \sum K_i p_i P_X)}$$

$$\Rightarrow -v_1 = \frac{k_1 K_5 C_T (x_5 - x_3 / P_X k_{p1})}{\left( \sum \frac{1}{p} x_i + \sum K_i x_i \right)}$$



$$\Rightarrow -v_1 = k_{a1} \frac{(x_5 - x_3/P_X k_{p1})}{\sum \left( K_i + \frac{1}{p} \right) x_i} \left( \frac{x_1}{\rho d_p} \right) \left( \frac{x_1(t=0)}{x_1} \right)^{1/3} \quad (13)$$

where  $k_{a1} = 72k_s k_1 K_5$  = the rate constant (apparent),  $k_{pi}$  = equilibrium constant for  $i$ th reaction. The magnitude of equilibrium rate constants, adsorption constants, and apparent rate constants are taken from available literature.<sup>19</sup>

As a similar way like Boudouard reaction ( $R_1$ ), steam gasification ( $R_2$ ) is given as:

$$-v_2 = k_{a2} \frac{(x_4 - x_3 x_2 / P_X k_{p2})}{\sum \left( K_i + \frac{1}{p} \right) x_i} \left( \frac{x_1}{\rho d_p} \right) \left( \frac{x_1(t=0)}{x_1} \right)^{1/3} \quad (14)$$

Hydrogen gasification ( $R_3$ ) can be expressed as:

$$-v_3 = k_{a3} \frac{(x_2^2 - x_6 P_X / k_{p3})}{P_X \sum \left( K_i + \frac{1}{p} \right) x_i} \left( \frac{x_1}{\rho d_p} \right) \left( \frac{x_1(t=0)}{x_1} \right)^{1/3} \quad (15)$$

Methane–steam reforming (MSR) ( $R_4$ ) can be expressed as:

$$-v_4 = k_{a4} \frac{(x_4 x_6 - x_3 x_2^3 / P_X^2 k_{p4})}{P_X \sum \left( K_i + \frac{1}{p} \right) x_i} \left( \frac{x_1}{\rho d_p} \right) \left( \frac{x_1(t=0)}{x_1} \right)^{1/3} \quad (16)$$

Water-gas shift (WGS) ( $R_5$ ) can be expressed as:

$$-v_5 = k_{a5} \frac{(x_3 x_4 - x_5 x_2 / k_{p5})}{P_X \sum \left( K_i + \frac{1}{p} \right) x_i} \left( \frac{x_1}{\rho d_p} \right) \left( \frac{x_1(t=0)}{x_1} \right)^{1/3} \quad (17)$$

Now, using reactions ( $R_1$ )–( $R_5$ ) as given in eqn (13)–(17), differential equations can be formulated for solving the gas composition and carbon content. These are expressed as follows:

$$\frac{dx_1}{dt} = v_1 + v_2 + v_3 \quad (18)$$

$$\frac{dx_2}{dt} = -v_2 + 2v_3 - 3v_4 - v_5 \quad (19)$$

$$\frac{dx_3}{dt} = -2v_1 - v_2 - v_4 + v_5 \quad (20)$$

$$\frac{dx_4}{dt} = v_2 + v_4 + v_5 \quad (21)$$

$$\frac{dx_5}{dt} = v_1 - v_5 \quad (22)$$

$$\frac{dx_6}{dt} = -v_3 + v_4 \quad (23)$$

Eqn (18)–(23) are numerically solved by applying explicit methodology where starting guesses are taken from eqn

(18)–(23). An in-house built FORTRAN code has been developed for solving the aforesaid equations to obtain the gas/carbon composition. Results obtain till the gasification reached a steady state condition where an error is kept fixed at 1% between two successive time steps.

### 2.3 Experimental set-up and procedure

The bubbling fluidized bed (BFB) gasifier setup at Process Engineering Research Laboratory of Indian Institute of Technology Roorkee<sup>20</sup> was used in this study whose schematic PFD is shown in Fig. 1.

The reactor (R) (1.5 m tall  $\times$  0.102 m o.d.) made of stainless steel (SS-304), is electrically heated using ceramic band heaters (total height, 0.63 m) having kanthal-®A inner wire, which are controlled by a voltage barrier ( $V_B$ ) (set at 230 V). The “R” is covered with a highly insulated 2 to 3 cm thick layer of ceramic wool to prevent heat loss from the system to the surrounding. All the temperatures are dynamically sensed by the temperature thermocouples (TCs) (pt-100 and K-type (Nickel–Chromium)) and recorded in a temperature data logger at the control panel. These temperatures are regularly monitored and controlled using PID controllers (TC203 and TC344). The steam generator (Sg) having 15 L of water intake capacity, is designed for a maximum working pressure of 3 kg cm<sup>-2</sup>. The superheated steam (2 kg cm<sup>-2</sup> at 140  $\pm$  5 °C) followed by a preheating process, is used to fluidized the bed in the reactor (R). A bunch of Cu-tubes (length  $\times$  diameter = 40 mm  $\times$  6 mm) are arranged vertically, gas-welded and used as a flow-straightener. A ceramic porous disc of 50  $\mu$ m pore size is placed above the flow straightener. The EWS biomass is fed from the side-top section of the “R”, as shown in Fig. 1. The cyclone separator (C) is used to separate char and dust particles from the gasifier exhaust gas, collected in a char collection drum placed below the cyclone separator.

After that a gas cooler (Gc) (0.7 m tall  $\times$  0.20 m o.d.) is used to quench the gases/volatiles from “C”. The flow and temperature of cooling water inside “G<sub>C</sub>” are maintained by 0.25 HP centrifugal pump and water chiller unit, respectively. Then, the non-condensable/permanent gases (mainly CO, CH<sub>4</sub>, H<sub>2</sub> and CO<sub>2</sub>) coming out from “G<sub>C</sub>” are passed through an alkali-water tank (W) so that tars and reaming dust can be separated from the gases. The clean and cool gases from “W” is sent to the moisture trap (M), having silica beads so that moisture from the gases can be removed. Then, the gaseous mixture is passed through a gas flow meter (E-TFM-11), which is used to quantify the total volume (in L) and volumetric flow rate (in L h<sup>-1</sup>) of gas produced during a particular run. The sample gas is collected in a Tedlar bag for analyzing it using a gas chromatogram analyzer (NEWCHROM 6700). The remaining gases are burned using a gas burner after these come out from the inline flame arrestor (MODEL: 872).

**2.3.1 Procedure.** First, 2.5 kg of Fontainebleau silica sand, having particle size 350  $\mu$ m (“–450  $\mu$ m to +255  $\mu$ m”), is put into the gasifier though the feeder. The air/superheated steam, serving as the fluidizing gas, is introduced into the reactor (R) and its flow rate is set as per the desired steam to biomass ratio.



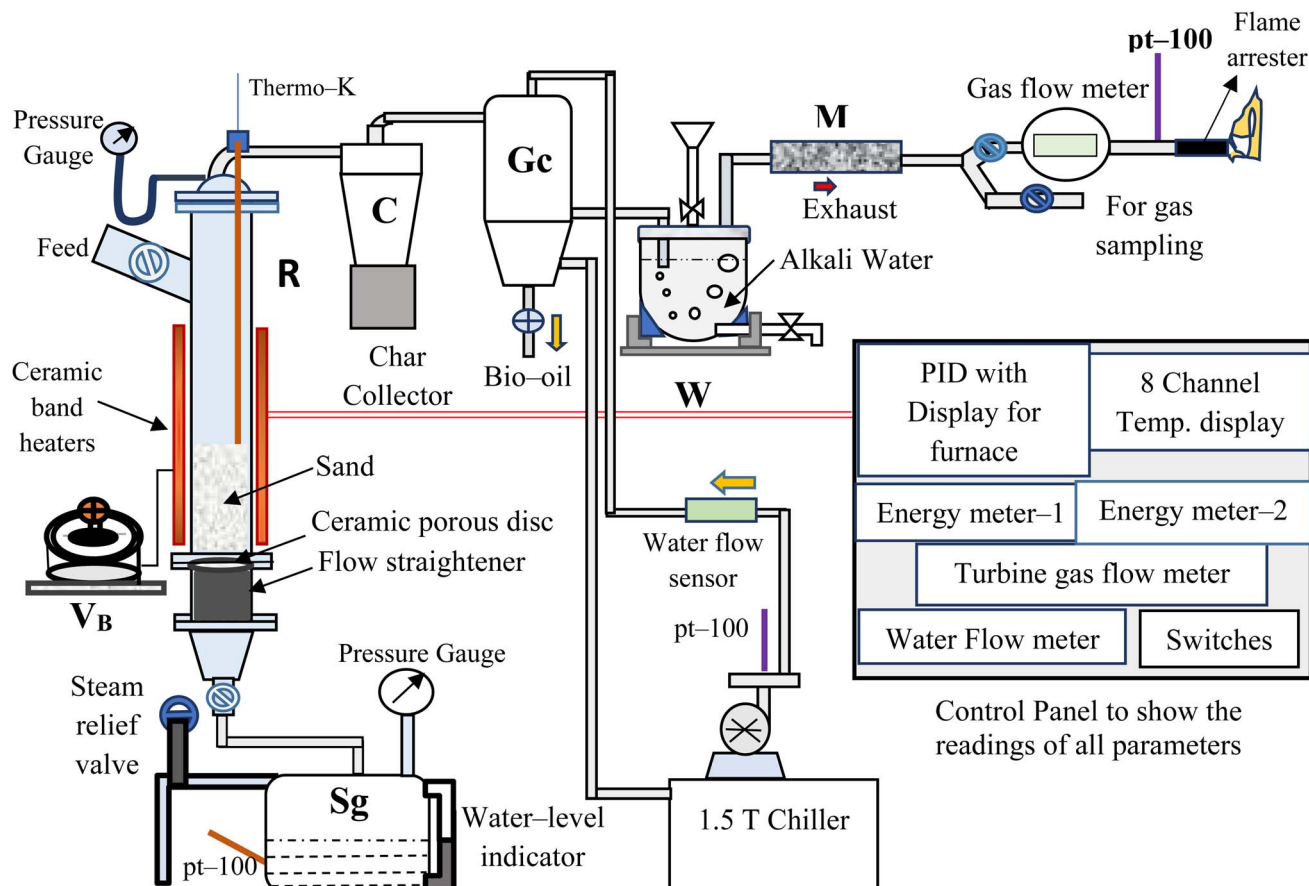


Fig. 1 Schematic diagram of experimental setup.

The reaction temperature is measured by a K-type thermocouple placed at the center of “R”, touches the sand. When the experiment reaches the desired condition, biomass is fed into “R” followed by collection of the gas sample in the Tedlar bag. The leftover gases are burnt at the exit of the flame arrester. During the whole process, air/steam is regularly injected at a specific flow rate to maintain the fluidization during the gasification process.

In order to construct different test cases, four input parameters at three levels are considered, as listed in Table 1.

Based on experiment matrix given by design of experiment, simulations are performed and volumetric compositions of  $H_2$  and  $CO_2$  gases have been computed, as reported in Table 2.

## 2.4 Response surface methodology

The central composite design (CCD) technique is employed to conduct the optimization analysis. A quadratic model, as

a function of independent input parameters, is opted for predicting maximum  $H_2$  (vol%) and minimum  $CO_2$  (vol%), expressed in eqn (24):<sup>21</sup>

$$Y = \beta_0 + \sum_{i=1}^k \beta_i X_i + \sum_{i=1}^k \beta_{ii} X_i^2 + \sum_{i=1}^k \sum_{j=i+1}^k \beta_{ij} X_i X_j + \varepsilon \quad (24)$$

where,  $k$  = no. of parameters;  $\beta_0$ ,  $\beta_i$ ,  $\beta_{ii}$  and  $\beta_{ij}$  = coefficients of regression for the intercept, linear, quadratic and interaction parameters, respectively and  $X_i = i$ th input parameter.  $\varepsilon$  = experimental error. The present analysis examines the effect of four input parameters, *viz.* equivalence ratio ( $0 \leq ER \leq 0.4$ ), particle diameter ( $100 \leq d_p \leq 1000$ ,  $\mu\text{m}$ ), reaction temperature ( $900 \leq T \leq 1200$  K) and steam to biomass ratio ( $0.5 \leq SBR \leq 2.5$ ), respectively on syngas compositions (vol%). Quantum XL software suggested 25 test cases taking  $n = 4$  and  $n_C = 1$  at  $\alpha = 1$  (face-centered CCD).

Table 1 List of input varying parameters at three levels

| Parameters (units)                          | Low level (-1) | Mid-level (0) | High level (+1) |
|---|----------------|---------------|-----------------|
| Equivalence ratio (ER, unitless)            | 0              | 0.2           | 0.4             |
| Particle diameter ( $d_p$ , $\mu\text{m}$ ) | 100            | 550           | 1000            |
| Reaction temperature ( $T$ , K)             | 900            | 1050          | 1200            |
| Steam to biomass ratio (SBR, unitless)      | 0.5            | 1.5           | 2.5             |



Table 2 Experiment design matrix with model responses<sup>a</sup>

| Runs | Parameters |                         |         |     | Kinetic model         |                        |         | RSM-predicted         |                        |         |
|------|------------|-------------------------|---------|-----|-----------------------|------------------------|---------|-----------------------|------------------------|---------|
|      | ER         | $d_p$ ( $\mu\text{m}$ ) | $T$ (K) | SBR | H <sub>2</sub> (vol%) | CO <sub>2</sub> (vol%) | Utility | H <sub>2</sub> (vol%) | CO <sub>2</sub> (vol%) | Utility |
| 1    | 0.2        | 550                     | 1050    | 1.5 | 35.16                 | 28.84                  | 4.29    | 36.06                 | 28.66                  | 4.36    |
| 2    | 0          | 550                     | 1050    | 1.5 | 46.77                 | 17.69                  | 7.59    | 41.55                 | 20.25                  | 6.03    |
| 3    | 0.4        | 100                     | 900     | 0.5 | 27.08                 | 39.10                  | 1.51    | 29.62                 | 39.22                  | 2.06    |
| 4    | 0          | 100                     | 900     | 0.5 | 46.45                 | 19.21                  | 7.39    | 46.27                 | 18.73                  | 7.38    |
| 5    | 0.4        | 1000                    | 900     | 0.5 | 36.23                 | 41.26                  | 3.97    | 32.5                  | 42.32                  | 2.96    |
| 6    | 0          | 100                     | 900     | 2.5 | 32.87                 | 21.81                  | 4.16    | 30.83                 | 22.86                  | 3.61    |
| 7    | 0.4        | 100                     | 1200    | 0.5 | 38.44                 | 33.78                  | 4.82    | 38.29                 | 33.11                  | 4.78    |
| 8    | 0.4        | 100                     | 1200    | 2.5 | 39.58                 | 34.96                  | 5.01    | 35.81                 | 37.31                  | 3.85    |
| 9    | 0          | 1000                    | 1200    | 2.5 | 51.83                 | 15.95                  | 8.65    | 48.57                 | 16.24                  | 7.97    |
| 10   | 0.2        | 100                     | 1050    | 1.5 | 31.35                 | 30.29                  | 3.21    | 32.91                 | 28.85                  | 3.71    |
| 11   | 0          | 1000                    | 1200    | 0.5 | 52.19                 | 14.37                  | 8.88    | 54.92                 | 13.76                  | 9.4     |
| 12   | 0.4        | 1000                    | 1200    | 0.5 | 38.45                 | 33.79                  | 4.82    | 39.76                 | 33.14                  | 5.23    |
| 13   | 0.2        | 1000                    | 1050    | 1.5 | 39.54                 | 27.34                  | 5.41    | 37.68                 | 28.84                  | 4.89    |
| 14   | 0.4        | 100                     | 900     | 2.5 | 23.25                 | 42.57                  | 0.03    | 21.32                 | 42.76                  | 0.34    |
| 15   | 0.2        | 550                     | 1200    | 1.5 | 47.03                 | 24.01                  | 7.14    | 45.22                 | 24.39                  | 6.85    |
| 16   | 0.2        | 550                     | 1050    | 2.5 | 27.85                 | 32.24                  | 2.07    | 32.54                 | 29.49                  | 3.44    |
| 17   | 0.4        | 550                     | 1050    | 1.5 | 24.29                 | 42.38                  | 0.43    | 29.21                 | 39.89                  | 1.96    |
| 18   | 0.4        | 1000                    | 1200    | 2.5 | 39.57                 | 34.97                  | 5.01    | 40.55                 | 35.02                  | 5.17    |
| 19   | 0          | 100                     | 1200    | 2.5 | 37.39                 | 20.83                  | 5.36    | 41.92                 | 19.35                  | 6.51    |
| 20   | 0.2        | 550                     | 1050    | 0.5 | 44.86                 | 23.67                  | 6.75    | 39.87                 | 26.48                  | 5.35    |
| 21   | 0          | 100                     | 1200    | 0.5 | 52.10                 | 14.21                  | 8.89    | 51.53                 | 14.56                  | 8.82    |
| 22   | 0.4        | 1000                    | 900     | 2.5 | 27.62                 | 43.48                  | 1.51    | 27.46                 | 43.53                  | 1.44    |
| 23   | 0          | 1000                    | 900     | 2.5 | 37.94                 | 22.55                  | 5.36    | 38.89                 | 22.8                   | 5.53    |
| 24   | 0.2        | 550                     | 900     | 1.5 | 34.54                 | 31.04                  | 4.02    | 36.05                 | 30.73                  | 4.27    |
| 25   | 0          | 1000                    | 900     | 0.5 | 48.02                 | 22.93                  | 7.39    | 51.07                 | 20.99                  | 8.42    |

<sup>a</sup> Where, ER: equivalence ratio (mol mol<sup>-1</sup>),  $d_p$ : Particle size ( $\mu\text{m}$ ),  $T$ : gasification temperature (K), and SBR: steam to biomass ratio (mass/mass).

## 2.5 Utility concept

Any physical problem, it is important to get the maximum performance of the system and that is why optimization of multi-objective function is necessary to be analyzed. In that context, utility concept is important where different objective functions are clubbed together into a single objective function and depending upon their respective usage, maximum/minimum utilization of the system can be evaluated. The overall utility of the EWS gasification is computed as the total sum of all the performance utility characteristics *i.e.*, enriching H<sub>2</sub> concentration and diminishing CO<sub>2</sub> gas emission. “ $U$ ” = overall utility function [ $f(X_i)$ ], refers the effective quantity of  $i$ th performance characteristics, is given by as below:<sup>22</sup>

$$U\left(\sum_{i=1}^n X_i\right) = U(X_1, X_2, X_3, X_4, X_5, \dots, X_n) \\ = f[U_1(X_1), U_2(X_2), U_3(X_3), \dots, U_n(X_n)] \quad (25)$$

where  $U_i(X_i)$  = utility of  $i$ th performance characteristics.

The overall utility is calculated as the summation of individual utility and is given as:

$$U(X_1, X_2, X_3, X_4, X_5, \dots, X_n) = \sum_{i=1}^n U_i(X_i) \quad (26)$$

Based on the requirement of the system under consideration (like gasification in this study) priorities are given to the

performance characteristics and accordingly appropriate weights are assigned. Finally, the overall utility can be rewritten as:

$$U(X_1, X_2, X_3, X_4, X_5, \dots, X_n) = \sum_{i=1}^n W_i U_i(X_i) \quad (27)$$

where  $W_i$  is the allocated weight to the  $i$ th performance characteristics and total sum of all the weights of the performance characteristics, which is 1, as shown in eqn (28).

$$\sum_{i=1}^n W_i = 1 = W_{H_2} + W_{CO_2} \quad (28)$$

where  $W_{H_2}$ ,  $W_{CO_2}$  are respectively the weightage assigned to H<sub>2</sub> and CO<sub>2</sub> gas concentration.

For finding the utility value for a number of performances generally involves a preference scale and weightages are assigned. For this purpose, a logarithmic scale is considered and a preference number is calculated between 0 to 9 where 0 = the least acceptable quality and 9 = the finest quality. This can be expressed as:<sup>23</sup>

$$P_i = C \log \frac{X_i}{X'} \quad (29)$$

where  $C$  = constant,  $X_i$  =  $i$ th performance characteristics,  $X'$  = least acceptable value of  $i$ th performance characteristics.

For finding  $C$  value preference number is set as 9 and  $X_i = X^*$  where  $X^*$  = optimum value. This can be represented as:



$$C = \frac{9}{\log \frac{X^*}{X'}} \quad (30)$$

finally, the overall utility is computed by the following expression:

$$U = \sum_{i=1}^n W_i P_i \quad (31)$$

## 3. Results and discussion

### 3.1 Validation

Study on EWS gasification for optimum operating condition of the gasifier has been performed involving chemical kinetic modeling. The kinetic model includes various gasification reactions including gas shift reaction in the form of differential equations. The equations need to be solved in order to obtain the composition of syngas production. To obtain results, an in-house built FORTRAN code has been developed satisfying the initial conditions and utilizing explicit method. As the reactions are time dependent, so iterations are performed until steady state condition is arrived. It is important to perform validation work before proceed for different case studies. Validation has

been performed for different compositions of syngas production with different feed material and results generated by present code are compared with that of the available literature. In addition, experiments are performed in a lab scale setup using EWS biomass and the syngas compositions are compared with the results obtained by the present FORTRAN code using chemical kinetic model. All these validation parts are illustrated in Fig. 2 along with the RMSE value, calculated as:

$$\text{RMSE} = \sqrt{\frac{\sum_{i=1}^n (y_{\text{exp},i} - y_{\text{sim},i})^2}{n}}$$

It can be seen from the figure that the present kinetic model predicts syngas composition closer to the experimental one and the RMSE value lies well within the acceptable range. This validation encourages for conducting other case studies required for the analysis.

### 3.2 Maximizing H<sub>2</sub> production and minimizing CO<sub>2</sub> emission

In biomass gasification it is common to produce hydrogen rich syngas because of having higher heating value of hydrogen gas. In this study EWS biomass is used as a feedstock material and involving chemical kinetic modeling many experimental cases are planned for finding suitable condition for maximum H<sub>2</sub> production. But such process is a time taking, and inefficient.

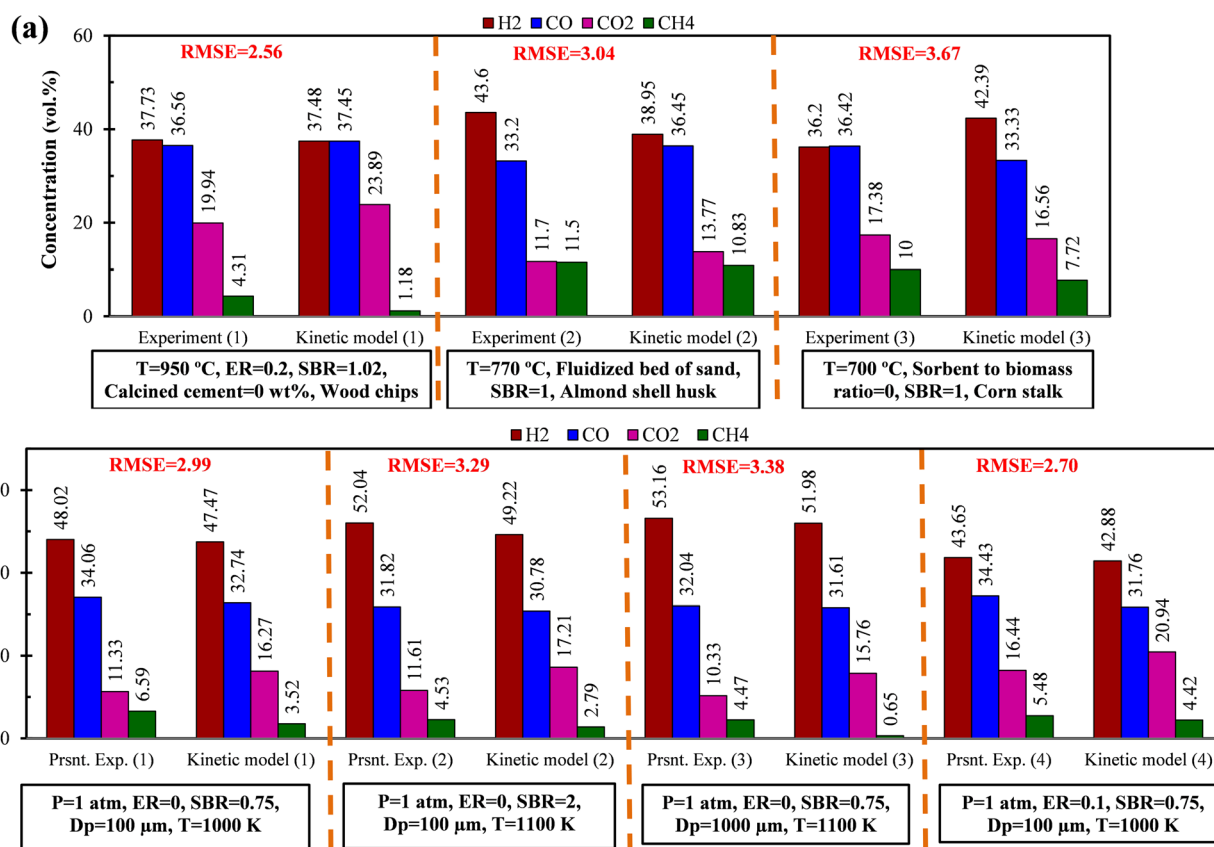


Fig. 2 Comparison of syngas composition between present kinetic model with (a) experiment-1,<sup>24</sup> experiment-2,<sup>25</sup> experiment-3 (ref. 26) (b) present experiments using EWS biomass.



Hence, optimization tool is important to minimize this effort. Here, response surface methodology (RSM) is employed as optimization tool with two different single objective functions *i.e.* (i) finding the best condition for maximum H<sub>2</sub> gas production (ii) minimizing CO<sub>2</sub> gas production. There are four input parameters such as equivalence ratio (ER), particle size ( $d_p$ ), gasification temperature ( $T$ ), steam to biomass ratio (SBR) and two output parameters *i.e.*, vol% of H<sub>2</sub> and CO<sub>2</sub> gas and using these parameters RSM optimization will be performed. For analyzing only 25 numbers of experimental cases/runs are required, given by design of experiments, as tabulated in Table 2.

Table 3 represents the analysis of variance (ANOVA) table for both the objective functions. For first objective function *i.e.* maximizing H<sub>2</sub> gas, one can see in Table 3 that lower  $p$ -values (<0.05) of input parameters (such as ER,  $d_p$ ,  $T$ , and SBR) indicate that all these parameters are significant for H<sub>2</sub> production but parameters like ER followed by  $T$  are the most influential one. However,  $p$ -values for square & two-way interaction parameters are found “(>0.05)” and thus insignificant for the objective function. A quadratic model is developed for H<sub>2</sub> gas which is a function of all input parameters is expressed in eqn (32). The ANOVA table also gives that the  $p$ -value for the quadratic model is 0.0049 (<0.05) which confirms the robustness of the developed model. For the second objective function *i.e.*, minimizing CO<sub>2</sub> gas production, Table 3 shows that except  $d_p$  all other parameters are significant. Because of the smallest  $p$ -value, ER is the most influential parameter followed by  $T$  and SBR. The quadratic model is given in eqn (33) and its lower  $p$ -value (<0.0001) certifies the authenticity of the model.

The centre composite design (CCD) technique recommends 25 number of experiments which includes 16 factorial, 8 axial,

and 1 center points experiments of input parameters (ER,  $d_p$ ,  $T$ , SBR). These suggested runs are numerically performed by adopting the developed FORTRAN code involving chemical kinetic modeling. The obtained value of H<sub>2</sub> and CO<sub>2</sub> gas compositions are used in the design matrix, suggested by design expert software (Design-Expert v22.0), to perform further investigations such as analysis of suggested model, optimization, and graphical interpretation. Finally, a mathematical model (2nd-order) is obtained for maximum volumetric composition of H<sub>2</sub> and CO<sub>2</sub> as shown in eqn (32) and (33), respectively, in the coded factors units.

$$\begin{aligned} \text{H}_2 \text{ (vol\%)} = & 36.06 - 6.17 \times \text{ER} + 2.38 \times d_p + 4.59 \times T - 3.66 \\ & \times \text{SBR} - 0.68 \times \text{ER}^2 - 0.76 \times d_p^2 + 4.57 \times T^2 + 0.14 \\ & \times \text{SBR}^2 - 0.48 \times \text{ER} \times d_p + 0.85 \times \text{ER} \times T + 1.78 \\ & \times \text{ER} \times \text{SBR} - 0.35 \times d_p \times T + 0.82 \times d_p \\ & \times \text{SBR} + 1.46 \times T \times \text{SBR} \end{aligned} \quad (32)$$

$$\begin{aligned} \text{CO}_2 \text{ (vol\%)} = & 28.66 + 9.82 \times \text{ER} - 6.0 \times 10^{-3} \times d_p - 3.17 \\ & \times T + 1.50 \times \text{SBR} + 1.41 \times \text{ER}^2 + 0.19 \times d_p^2 - 1.10 \\ & \times T^2 - 0.67 \times \text{SBR}^2 + 0.21 \times \text{ER} \times d_p - 0.49 \\ & \times \text{ER} \times T - 0.15 \times \text{ER} \times \text{SBR} - 0.76 \times d_p \\ & \times T - 0.58 \times d_p \times \text{SBR} + 0.17 \times T \times \text{SBR} \end{aligned} \quad (33)$$

Fig. 3(a)–(c) shows 3-D surface plots for H<sub>2</sub> production for a variation of any two operating parameters keeping other parameters fixed at their center points. The plots are useful to find out a small area, defined by the reduced ranges of operating parameters, in which the maxima of H<sub>2</sub> production lies. The importance of any input parameter on output parameter is determined by the slope of the curve, Fig. 3(a)–(c). It is observed that all the input parameters developed a steep slope for H<sub>2</sub> production representing the significant effect of all these

Table 3 ANOVA results for H<sub>2</sub> (vol%) and CO<sub>2</sub> (vol%)

| Response                | H <sub>2</sub> (vol%)   |            |               | CO <sub>2</sub> (vol%)   |            |               |
|-------------------------|---|------------|---------------|--|------------|---------------|
|                         | Coefficient   | $p$ -value | Remark        | Coefficient  | $p$ -value | Remark        |
| Model                   |   | 0.0049     | Significant   |  | <0.0001    | Significant   |
| Intercept ( $\beta_0$ ) | 36.06   |            |               | 28.66  |            |               |
| ER                      | -6.17   | 0.0002     | Significant   | 9.82   | <0.0001    | Significant   |
| $d_p$                   | 2.38  | 0.0496     | Significant   | -0.01  | 0.9910     | Insignificant |
| $T$                     | 4.59  | 0.0016     | Significant   | -3.17  | 0.0001     | Significant   |
| SBR                     | -3.66   | 0.0064     | Significant   | 1.50   | 0.0159     | Significant   |
| ER <sup>2</sup>         | -0.68   | 0.8157     | Insignificant | 1.41   | 0.3299     | Insignificant |
| $d_p^2$                 | -0.76   | 0.7933     | Insignificant | 0.19   | 0.8949     | Insignificant |
| $T^2$                   | 4.57  | 0.1381     | Insignificant | -1.10  | 0.4431     | Insignificant |
| SBR <sup>2</sup>        | 0.14  | 0.9610     | Insignificant | -0.67  | 0.6359     | Insignificant |
| ER $\times$ $d_p$       | -0.48   | 0.6818     | Insignificant | 0.21   | 0.7121     | Insignificant |
| ER $\times$ $T$         | 0.85  | 0.4686     | Insignificant | -0.49  | 0.3976     | Insignificant |
| ER $\times$ SBR         | 1.78  | 0.1459     | Insignificant | -0.15  | 0.7930     | Insignificant |
| $d_p \times T$          | -0.35   | 0.7622     | Insignificant | -0.76  | 0.1942     | Insignificant |
| $d_p \times$ SBR        | 0.82  | 0.4873     | Insignificant | -0.58  | 0.3167     | Insignificant |
| $T \times$ SBR          | 1.46  | 0.2271     | Insignificant | 0.17   | 0.7681     | Insignificant |
| LOF                     | 5.56  |            | Insignificant | 29.35  |            | Insignificant |
| Regression analysis     | $R^2 = 0.8863$ , adj. $R^2 = 0.7270$ , adeq precision = 9.58, std dev. = 4.53, mean = 38.42, CV% = 11.78, PRESS = 1317.19 |            |               | $R^2 = 0.9762$ , adj. $R^2 = 0.9430$ , adeq precision = 17.49, std dev. = 2.20, mean = 28.53, CV% = 7.71, PRESS = 283.66 |            |               |





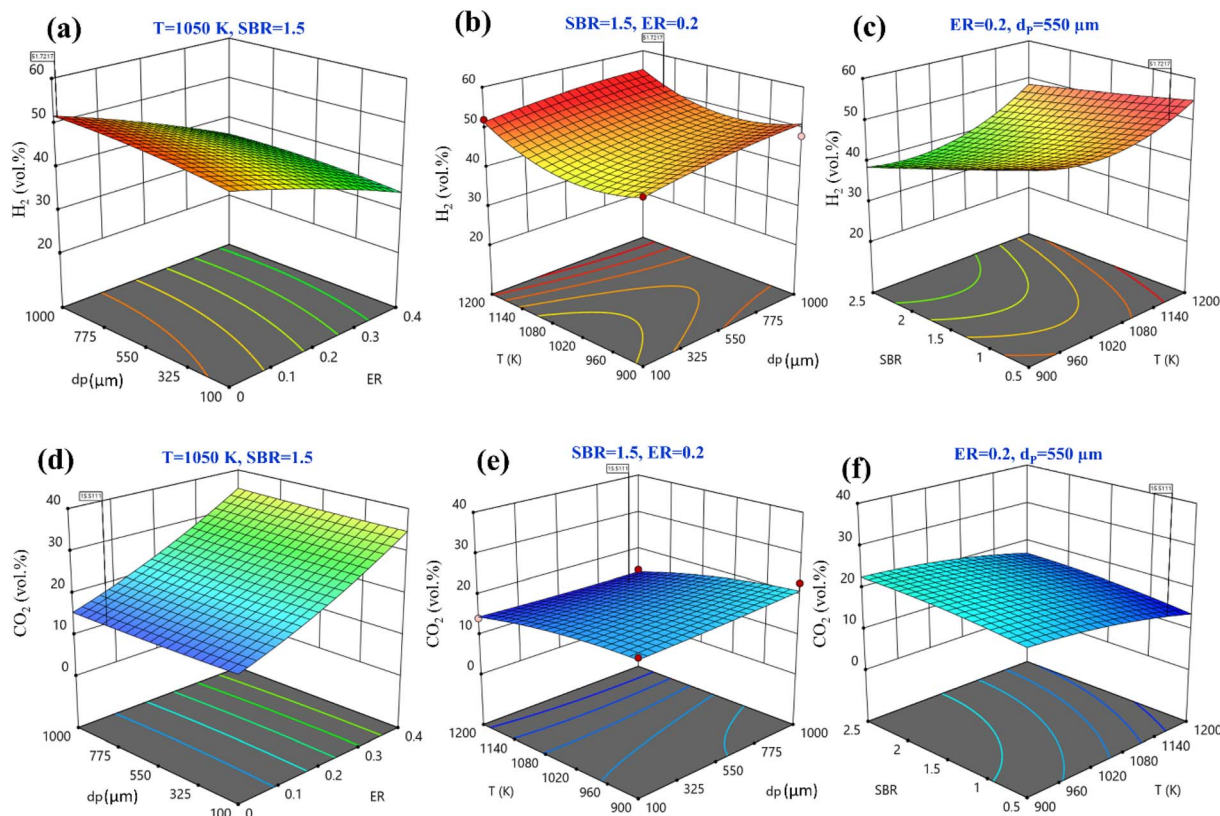
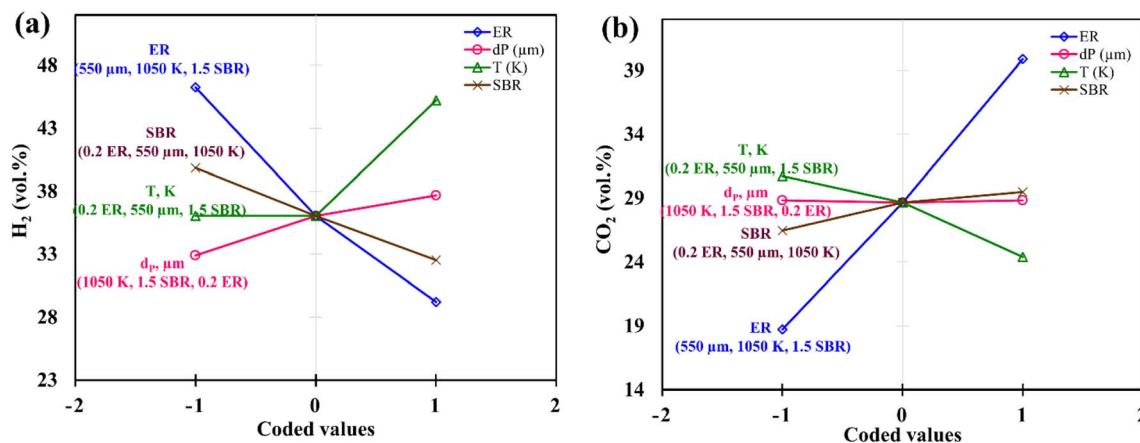


Fig. 3 Three-dimensional surface plots for (a–c)  $H_2$  maximization and (d–f)  $CO_2$  minimization.

parameters. Fig. 3(a) depicts the combined effects of ER and  $d_p$  on the  $H_2$  production. It shows that when ER is increased from 0 to 0.4 there is a rapid decrease in  $H_2$  production. When  $d_p$  increases from 100 to 1000  $\mu m$ ,  $H_2$  production rises slowly. The variation of  $H_2$  production with  $T$  and  $d_p$  is given in Fig. 3(b). It can be seen that maximum  $H_2$  production is found at 1200 K temperature and 1000  $\mu m$  particle diameter. The effect of SBR and  $T$  on the  $H_2$  production is shown in Fig. 3(c), it reveals that at SBR = 0.5 to 2.5 range  $H_2$  production diminishes. Therefore, the optimum setting for maximum  $H_2$  production, the quadratic model gives an accurate setting *i.e.*, ER = 0,  $d_p$  = 950  $\mu m$ ,  $T$  = 1170 K, and SBR = 0.5 predicted by central composite design at which maximum 51.72 vol%  $H_2$  production is achieved. Fig. 3(d)–(f) shows 3-D surface plots for  $CO_2$  minimization while varying two input parameters by taking other parameters fixed at their centre point values. By varying  $d_p$  from 100 to 1000  $\mu m$  there is hardly any change in  $CO_2$  concentration; however,  $CO_2$  concentration decreases when ER decreases from 0.4 to 0, as shown in Fig. 3(d). Fig. 3(e) represents the variation of  $CO_2$  with  $T$  and  $d_p$ . The  $CO_2$  emission reduces with rising  $T$  values whereas the reduction is comparatively less with dropping in  $d_p$  value. Fig. 3(f) shows that by augmenting gasification temperature and decreasing SBR diminishes  $CO_2$  gas production. By analyzing Fig. 3(d)–(f) for obtaining the second objective function *i.e.*,  $CO_2$  minimization, the model predicts the optimum setting as ER = 0,  $d_p$  = 794  $\mu m$ ,  $T$  = 1150 K, and SBR = 0.5 where the  $CO_2$  gas composition is predicted as 15.51 vol%.

Instead of analyzing three different 3-D surface plots, one can visualize the same by seeing a single figure like perturbation plot, as shown in Fig. 4. Such figure is important from the subject point of view as it describes the impact of each input parameter on the output parameter. The path traced by an individual parameter denotes its sensitivity or insensitivity on the output parameter like higher the slope more the sensitive parameter whereas less slope or flat line shows its insensitivity. The impact of varying parameters such as ER,  $d_p$ ,  $T$ , SBR on  $H_2$ -rich syngas production using EWS biomass is shown in Fig. 4(a). It is noticed that parameter 'ER' has attained the highest slope (from 0 to 0.4) and hence it is the most influential parameter. The plausible reason is that change in ER-value from 0.4 to 0 reduces the oxygen supply in the gasifier which in-turn suppresses the emission of  $CO_2$  gases resulting in the increase in  $H_2$  gas composition. Parameter 'T' has attained the second highest slope in the range 1050 to 1200 K. With rise in temperature the volumetric concentration of  $H_2$  rapidly increases because of the sudden jump of the equilibrium constant values of Boudouard ( $R_1$ ), steam gasification ( $R_2$ ), and methane-steam reforming ( $R_4$ ) reactions. Parameter 'SBR' gives the third highest slope where  $H_2$  production drops with supplying excessive steam that starts the reverse-water-gas shift (rev-WGS) reaction. The path traced by parameter ' $d_p$ ' approaches closely to a flat line and hence it is the least significant factor for  $H_2$ -rich syngas production. EWS biomass particle size stimulates the residence time but the present



Fig. 4 Perturbation plot for (a) H<sub>2</sub> maximization (b) CO<sub>2</sub> minimization.

analysis considers steady state condition to obtain the gas compositions and that is why parameter ' $d_p$ ' is comparatively less affective for maximum H<sub>2</sub> gas production. Fig. 4(b) depicts the effect of input parameters on CO<sub>2</sub> gas production. By observing this figure, one can easily identify parameter 'ER' as the most dominant factor in CO<sub>2</sub> gas reduction. The argument is already discussed above emphasizing that lower oxygen supply at small value of ER leads to partial oxidation of EWS biomass followed by minimum CO<sub>2</sub> generation. Secondly, referring to Boudouard reaction (R<sub>1</sub>), increase in temperature reduces CO<sub>2</sub> concentration as carbon reacts with CO<sub>2</sub> to produce CO gas and that is why parameter ' $T$ ' attains the second highest slope. It is also to be noticed that SBR-curve followed by  $d_p$ -curve has negligible slope and hence they are relatively less significant parameters compared to others.

### 3.3 Utility concept

In this study, utility concept is employed to combine two objective functions, *i.e.* (i) H<sub>2</sub> maximization and (ii) CO<sub>2</sub> minimization, into a single objective function by applying appropriately weightage to the respective objective functions depending upon the usage of the gasification process. Usually, gasification focusses on production of high heating value gases like H<sub>2</sub>-gas without affecting the surrounding environmental condition like low CO<sub>2</sub> production. Hence, more weightage is given to the first objective function and less weightage to the second objective function. The present analysis considers weightage as 80 : 20 ratio for framing the utility function as the maximization case.

Table 4 represents the ANOVA table for utility function. It can be seen from the table that except particle diameter of EWS biomass, all the three parameters have significant effect on utility function in the order like ER > T > SBR. The interaction between two parameters and square terms are found insignificant for the utility model. RSM generates a quadratic model for utility function involving all input parameters (*i.e.*,  $d_p$ , ER,  $T$ , SBR), as given in eqn (34).

Table 4 ANOVA results for utility<sup>a</sup>

| Source              | Coefficient   | <i>p</i> -value | Remark        |
|---------------------|---|-----------------|---------------|
| Model               |   | 0.0030          | Significant   |
| $\beta_0$           | 4.36  |                 |               |
| ER                  | -2.03   | <0.0001         | Significant   |
| $d_p$               | 0.59  | 0.0738          | Insignificant |
| $T$                 | 1.29  | 0.0014          | Significant   |
| SBR                 | -0.96   | 0.0089          | Significant   |
| ER <sup>2</sup>     | -0.36   | 0.6533          | Insignificant |
| $d_p^2$             | -0.06   | 0.9378          | Insignificant |
| $T^2$               | 1.21  | 0.1563          | Insignificant |
| SBR <sup>2</sup>    | 0.04  | 0.9633          | Insignificant |
| ER × $d_p$          | -0.03   | 0.9136          | Insignificant |
| ER × $T$            | 0.32  | 0.3290          | Insignificant |
| ER × SBR            | 0.34  | 0.2998          | Insignificant |
| $d_p$ × $T$         | -0.12   | 0.7200          | Insignificant |
| $d_p$ × SBR         | 0.22  | 0.5007          | Insignificant |
| $T$ × SBR           | 0.37  | 0.2712          | Insignificant |
| LOF                 | 6.30  |                 | Insignificant |
| Regression analysis | $R^2 = 0.8982$ , adj. $R^2 = 0.7555$ , adeq precision = 10.02, std dev. = 1.26, mean = 4.95, CV% = 25.38, PRESS = 98.32 |                 |               |

<sup>a</sup> For utility ( $U$ ) function, the model equation in coded factors units.

$$\begin{aligned}
 U = & 4.36 - 2.03 \times ER + 0.59 \times d_p + 1.29 \times T - 0.96 \\
 & \times SBR - 0.36 \times ER^2 - 0.063 \times d_p^2 + 1.21 \times T^2 + 0.037 \\
 & \times SBR^2 - 0.035 \times ER \times d_p + 0.32 \times ER \times T + 0.34 \\
 & \times ER \times SBR - 0.12 \times d_p \times T + 0.22 \times d_p \\
 & \times SBR + 0.37 \times T \times SBR
 \end{aligned} \quad (34)$$

Fig. 5 shows the three-dimensional surface plot for utility. Fig. 5(a) illustrates that increase in utility function is obtained at higher EWS particle size and lower ER value. Keeping the remaining parameters constant at their mid-values, both higher temperature and particle size maximizes the utility value, as shown in Fig. 5(b), whereas it is also maximum at small SBR and temperature value, as shown in Fig. 5(c). By analyzing Fig. 5(a)–(c) and satisfying the objective function *i.e.*, utility maximization, the RSM predicts the optimum setting as ER = 0,  $d_p$  = 840  $\mu$ m,  $T$  = 1150 K, and SBR = 0.5 where the H<sub>2</sub> and CO<sub>2</sub>



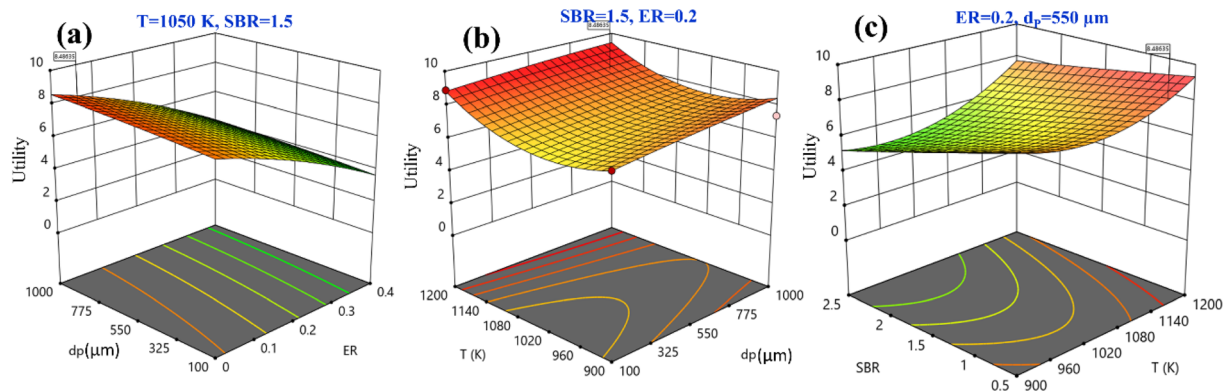


Fig. 5 Three-dimensional surface plots for utility maximization.

gas compositions are given as 51.54 vol% and 15.52 vol%, respectively.

Fig. 6 demonstrates the effect of each input parameters on utility function. It can be observed that for maximizing the utility function, parameter 'ER' has the highest contribution followed by parameter 'T', 'SBR', and 'd<sub>p</sub>'. The trend of each parameter for the utility function is similar to that of the first objective function *i.e.*, H<sub>2</sub> gas maximization and the reason is already discussed in the earlier section (Fig. 4(a)). This trend is quite obvious because while forming utility function more weightage (80%) is given to H<sub>2</sub> gas composition and less weightage (20%) to CO<sub>2</sub>. It is found that for single objective function H<sub>2</sub> maximization case gives 51.72 & 15.57 vol% of H<sub>2</sub> & CO<sub>2</sub> concentrations and CO<sub>2</sub> minimization case gives 51.45 & 15.51 vol% of H<sub>2</sub> & CO<sub>2</sub> gas compositions whereas utility gives 51.54 vol% and 15.52 vol% of H<sub>2</sub> and CO<sub>2</sub> gas compositions. After critically analyzed the scenario, the authors noticed that for the maximum utilization of gasification of EWS biowaste there is a reduction in H<sub>2</sub> gas production in the expense of more CO<sub>2</sub> emission. In order to validate the syngas compositions, at optimum condition given by utility concept, the results obtained by kinetic model are compared with the experimental one and quadratic model, as shown in Fig. 7. The figure shows

that syngas compositions obtained by different models are found close (std. deviation:  $\sigma \leq 2.245$  for H<sub>2</sub> and  $\sigma \leq 2.885$  for CO<sub>2</sub> gas compositions) to the experimental results which confirms the reliability or robustness of the models.

### 3.4 Techno-economic analysis

The present study focuses on maximum utilization of biomass gasification process for H<sub>2</sub> rich syngas production with minimum CO<sub>2</sub> emission through chemical kinetic modeling. On the other hand, global energy market demands continuous rise in green energy production (*e.g.*, H<sub>2</sub>) in order to limit the dependency on fossil fuel and preventing the greenhouse gases emission. In this regard, it is important to linkup the current analysis with the industrial level like finding the large-scale usage of EWS biomass and checking the feasibility of H<sub>2</sub> production in bulk amount. Apart from the technical part, cost analysis is an important tool for deciding the usage of EWS biomass in industrial plant. Such analysis is called techno-economic analysis where both technological and cost analysis/plant economics are simultaneously investigated.

For economic analysis of EWS biomass, an industrial level "down draft 20 kW h<sup>-1</sup> biomass pyrolysis gasifier" setup is considered. This analysis is conducted for a pilot plant, having a capacity of 500 m<sup>3</sup> per day of syngas production. Economic analysis involves computing the following items such as (i) fixed cost [FC] (ii) operating cost [OC] (iii) raw material cost [CRM] (iv) manufacturing cost [MC] (v) selling price [SP] (vi) total annual cost [TAC] (vii) annual cost of capital recovery [ACCR] (viii) payback period [PP]. Fixed cost primarily involves equipment/machinery cost and its related cost such as installation, delivery cost, instrumentation-control-piping-electrical arrangement cost, building cost, courtyard improvement cost, contingency and contractor fee *etc.*<sup>27</sup> The gasifier equipment (for 500 m<sup>3</sup> per day syngas production, waste processing capacity of 2000 kg per day) cost is taken from 'Sakthi Veera Green Energy Pvt. Ltd, Chennai [India]' manufacturing company. For computation of the plant operating cost, following data are collected from market survey and are shown in Table 5. Based on the optimum condition, obtained from the utility concept, manufacturing cost (INR per kg) and plant payback period (year) are estimated.

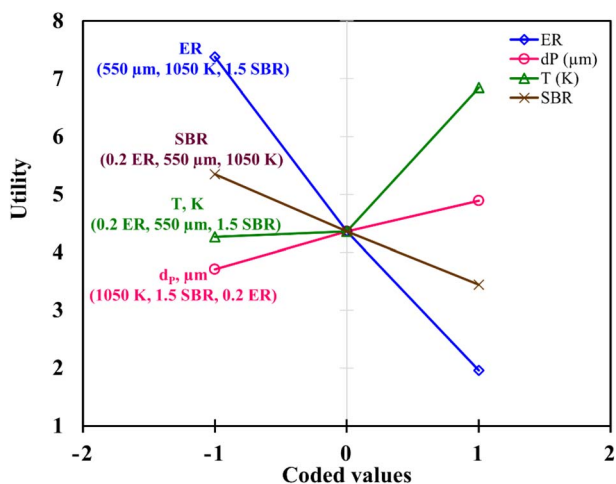


Fig. 6 Perturbation plot for utility maximization.



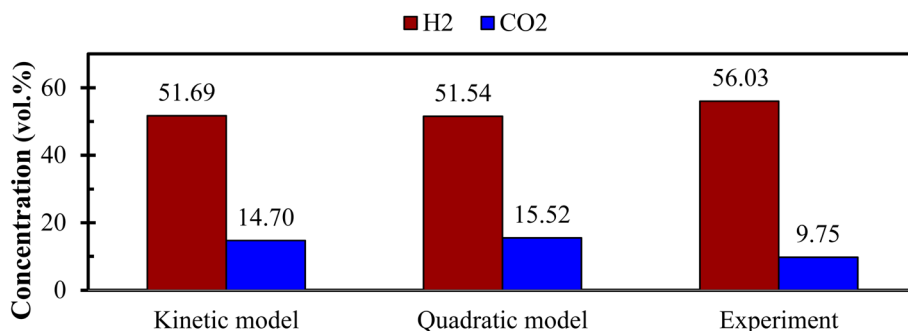


Fig. 7 Comparison of H<sub>2</sub> and CO<sub>2</sub> gas compositions between different models and experiment at optimum condition (ER = 0,  $d_p = 840 \mu\text{m}$ ,  $T = 1150 \text{ K}$ , SBR = 0.50).

The crucial part of techno-economic study is to obtain the plant payback period *i.e.*, in how many years the invested capital will be recovered. The entire computation is elaborately discussed in seven consecutive steps as given below:

Step I: fixed cost [ $F_C$ ]:

Fixed cost comprises of equipment cost [ $E$ ]; direct cost [ $D_C$ ] *i.e.*, insulation [8.5% of  $E$ ], purchased equipment delivery [ $E \times 10\%$ ], installation [ $E \times 40\%$ ], instrumentation and control [ $E \times 18\%$ ], piping [ $E \times 60\%$ ], electrical systems [ $E \times 12.5\%$ ], buildings [ $E \times 15\%$ ], yard improvements [ $E \times 15\%$ ], service facilities [ $E \times 55\%$ ], land [ $E \times 6\%$ ]; repair & maintenance cost [ $E \times 4\%$ ]; indirect cost [ $I_C$ ] *i.e.*, engineering and supervision [ $(D_C + E) \times 8\%$ ], construction expenses [ $(D_C + E) \times 10\%$ ]; contractor's fee [ $(D_C + I_C) \times 6\%$ ], and contingency [ $(D_C + I_C) \times 8\%$ ].

Therefore,  $F_C = E + D_C + I_C + \text{Contr. fee} + \text{conti.} = 10\,736\,832$  INR.

Step II: annual cost of capital recovery [ACCR]:

ACCR is computed using the mathematical expression given as:

$$\text{ACCR} = \text{FC} \times \left\{ \frac{i(1+i)^n}{(1+i)^n - 1} \right\}$$

where,  $i$  = interest rate,  $n$  = plant service life.

Table 5 Data used for techno-economic feasibility of the EWS gasification process

| Title                       | Specifications                                  |
|-----------------------------|---|
| Production capacity         | 500 m <sup>3</sup> per day of syngas production |
| Service life                | 20 years  |
| Electricity consumption     | 20 kW h <sup>-1</sup>                           |
| Equipment operating time    | 20 h per day                                    |
| Equipment cost              | 24 lakhs  |
| No of shift/day             | 3   |
| Working days                | 300 days per year                               |
| Cost of raw material        | 2 INR per kg                                    |
| Wage of one labour          | 500 INR/8 h                                     |
| Cost of electricity         | 5.5 INR per unit                                |
| Labours per shift           | 5 nos   |
| No. of trucks               | 2   |
| Cost per truck              | 80 000 INR per month                            |
| Syngas yield                | 693 g syngas per kg biomass                     |
| Inflation/depreciation rate | 7% annually                                     |

So, ACCR = 1715332.07 INR per year (taking  $i = 15\%$  and  $n = 20$  years).

Step III: operating cost [OC]:

The operating cost consists of cost of raw material, labor, transportation, and electricity. As per data provided in Table 5, the operating cost of envisaged gasification plant is calculated as:

OC = cost of (raw material + labor + transportation cost + electricity) = (1 200 000 + 2 250 000 + 1 578 080 + 660 000) = 5 688 080 INR per year.

Step IV: manufacturing cost [MC]:

For syngas production,

$$\text{MC} = \frac{\text{total annual cost (TAC)}}{\text{annual production rate (APR)}}$$

where, TAC = (ACCR + OC) and APR = (waste processing capacity  $\times$  syngas yield  $\times$  working days).

Here,  $\text{MC} = \frac{7403412.07}{415\,800} = 17.81$  INR per kg syngas.

Step V: depreciation cost ( $D$ ) using diminishing value method:

Salvage value (SV) after  $n$  years =  $\text{FC} \times (1 - \text{annual depreciation})^n$ . Here,  $D = 411092.43$  INR per year where (where  $D = \frac{\text{FC} - \text{SV}}{n}$ )

Step VI: profit and cash flow:

Net profit = GPAD – income tax on GPAD, where, GPAD = gross profit before depreciation = [(SP of syngas – MC)  $\times$  APR] – TAC. The SP of syngas is set in such a way that GPAD will be a positive value. Considering SP = 43 INR per kg, income tax = 30%, the net profit = 1863038.41 INR per year. Future cash flow (FCF) = net profit +  $D = 2\,274\,130$  INR per year. Present value of future cash flow (PVFCF) for  $a$ th year =  $\frac{\text{future value of cash inflow in } a\text{th year}}{(1+i)^a}$ .

Step VII: payback period:

In order to analyze the economic feasibility for setting up a biomass gasification plant, for H<sub>2</sub>-rich syngas production using eucalyptus wood sawdust, it is important to find out the payback period of the plant so that required profit margin can be targeted in the succeeding years. In the present analysis for a 20 years lifespan gasification plant considering all the major



Table 6 Computation of payback period<sup>a</sup>

| Title     | Year      |           |           |           |            |
|-----------|-----------|-----------|-----------|-----------|------------|
|           | 1st       | 2nd       | 3rd       | 4th       | 5th        |
| MC        | 17.81     | 18.76     | 19.79     | 20.88     | 22.06      |
| SP        | 43        | 46.01     | 49.23     | 52.68     | 56.36      |
| FCF       | 2 274 131 | 2 871 506 | 3 510 696 | 4 194 631 | 4 926 440  |
| Margin%   | 142       | 145       | 149       | 152       | 156        |
| PVFCF     | 1 977 505 | 2 171 271 | 2 308 340 | 2 398 294 | 2 449 312  |
| CCF (INR) | 1 977 505 | 4 148 776 | 6 457 116 | 8 855 409 | 11 304 721 |

<sup>a</sup> Abbreviations: MC: manufacturing cost; SP: selling price; FCF: future cash flow; PVFCF: present value of future cash flow; CCF: cumulative cash flow.

economic factors, the payback period is estimated as 4.8 (~5) years, shown in Table 6.

## 4. Conclusions

In this study, RSM-utility concept based optimization has been implemented in a gasification process considering eucalyptus wood biomass where a chemical kinetic model is used to compute the syngas composition. The modified kinetic model, involving water gas shift reaction, is validated with lab scale experiments, available literature and the RMSE value lies well within the acceptable range ( $2.56 \leq \text{RMSE} \leq 3.67$ ). In order to find out the optimal setting for maximum H<sub>2</sub> gas production and reducing CO<sub>2</sub> gas emission in air–steam gasification process, this research work is necessary. Results showed that the maximum H<sub>2</sub> is obtained at ER = 0,  $d_p = 950 \mu\text{m}$ ,  $T = 1170 \text{ K}$ , and SBR = 0.5 with 51.75 vol% production whereas minimum CO<sub>2</sub> is obtained at ER = 0,  $d_p = 794 \mu\text{m}$ ,  $T = 1150 \text{ K}$ , and SBR = 0.5 with 14.65 vol% production. Using utility concept (80% H<sub>2</sub>:20% CO<sub>2</sub>), the optimum H<sub>2</sub> is computed as 51.69 vol% (0.11% ↓) with a penalty of higher CO<sub>2</sub> production found as 14.70 vol% (0.34% ↑). ANOVA reveals that ER is the most influential parameter followed by  $T$ , SBR and  $d_p$ . For predicting H<sub>2</sub> and CO<sub>2</sub> gas composition, RSM proposes two quadratic models comprises of four input parameters. In order to understand the feasibility of using EWS biomass at an industrial scale (500 m<sup>3</sup> per day of syngas production capacity) for H<sub>2</sub> rich syngas production, a detailed technoeconomic study has been reported. The analysis indicates that for a 20 years life span gasification plant, the payback period is 4.8 (~5) years where fixing the selling price of H<sub>2</sub> rich syngas at 43 INR per kg a minimum 142% profit margin can be availed. The complete study gives a clear direction that if H<sub>2</sub> can be produced at optimum condition using EWS biomass, it could be an attractive option as energy source in the market.

## Conflicts of interest

There are no conflicts to declare.

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