



Cite this: *Phys. Chem. Chem. Phys.*,
2022, 24, 18608

Geometry of tellurene adsorbed on the Si(111)- ($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface from first principles calculations†

Stefania Isceri,[†] Daniele Dragoni,[§] Davide Campi,^c Stefano Cecchi^{bc}
and Marco Bernasconi^{id}*^c

The 2D form of tellurium, named tellurene, is one of the latest discoveries in the family of 2D mono-elemental materials. In a trilayer configuration, free-standing tellurene was predicted theoretically to acquire two crystallographic forms, the α and β phases, corresponding to either a 1T-MoS₂-like geometry or a trilayer slab exposing the Te(10 $\bar{1}$ 0) surface of bulk Te with helical chains lying in-plane and further reconstructed due to the formation of interchain bonds. Either one or the other of the two phases was observed experimentally to prevail depending on the substrate they were grown onto. In the perspective to integrate tellurene on silicon, we here report an *ab initio* study of the adsorption of tellurene on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30° surface passivated by antimony. According to the literature, this substrate is chosen for the growth of several tellurides by molecular beam epitaxy. The calculations reveal that on this substrate the adsorption energy mostly compensates the energy difference between the α and β phases in the free-standing configuration which suggests that the prevalence of one phase over the other might in this case strongly depend on the kinetics effects and deposition conditions.

Received 15th April 2022,
Accepted 13th July 2022

DOI: 10.1039/d2cp01759h

rsc.li/pccp

1 Introduction

Mono-elemental 2D materials referred to as Xenes, where X is an element of the groups III, IV, V or VI, have attracted great interest in recent years because of their extraordinary mechanical, electrical, and optical properties, which are different from those of their counterparts in the bulk phase.¹

The two-dimensional form of tellurium, known as tellurene, is one of the latest found materials in this class.¹ In the bulk under normal conditions, tellurium crystallizes in a trigonal phase (space group *P*3₁21)² made of helical chains with short (2.835 Å) Te–Te intrachain bonds. Weak interchain interactions lead to a hexagonal arrangement of the chains aligned along the *c* axis (in the hexagonal setting of the trigonal phase with

a = 4.45 Å and *c* = 5.93 Å). Due to its quasi-one-dimensional character, Te is less prone to be exfoliated into 2D sheets, although examples of mechanical exfoliation have been reported in the literature.³ Most often 2D tellurium is grown in the form of flakes in solution⁴ or is deposited as ultrathin films on different substrates by several means. For instance, molecular beam epitaxy (MBE) on graphene supported by a 6H-SiC(0001) substrate leads to the formation of helical chains with their axis lying parallel to the substrate which corresponds to the formation of the Te(10 $\bar{1}$ 0) face of bulk tellurium.⁵ This is actually the truncation of the bulk with the lowest surface energy.⁶ No preferred orientation between the Te chains and the substrate is observed because of the van der Waals epitaxy.⁵ The band gap of the films increases by decreasing the thickness from 0.33 eV (bulk) to 0.92 eV (a single chain layer) as measured by scanning tunneling microscopy.⁵ A field-effect transistor made of flakes of tellurene grown in solution in the Te(10 $\bar{1}$ 0) geometry was actually reported in the literature with hole mobilities as high as about 700 cm² V^{−1} s^{−1} at 300 K.⁴

The growth of helical chains with their axis perpendicular to that of the substrate has been attained instead by Wang *et al.*⁷ on flexible mica sheets with a film thickness of 32 nm. This geometry corresponds to the exposure of the (0001) surface of bulk Te.

On the other hand, theoretical calculations based on density functional theory (DFT) have shown that a free-standing trilayer

^a Department of Physics, Politecnico di Milano, Piazza L. da Vinci 32, 20133, Milano, Italy

^b Paul-Drude-Institut für Festkörperelektronik, Leibniz-Institut im
Forschungsverbund Berlin e. V., Hausvogteiplatz 5-7, 10117, Berlin, Germany

^c Department of Materials Science, University of Milano-Bicocca, Via R. Cozzi 55,
20125, Milano, Italy. E-mail: marco.bernasconi@unimib.it

† Electronic supplementary information (ESI) available: Atomic positions of tellurene adsorbed on the silicon surface in Cartesian coordinates. See DOI: <https://doi.org/10.1039/d2cp01759h>

‡ Present address: Institute of Solid-State Electronics, TU Wien, Gusshausstrasse 25-25a, 1040 Vienna, Austria. E-mail: stefania.isceri@tuwien.ac.at

§ Present address: Leonardo S. p. A., Piazza Monte Grappa 4, 00195, Roma, Italy.



made of helical chains lying in-plane is unstable with respect to a reconstruction forming additional interchain bonds.⁸ This geometry is referred to as the β phase in ref. 8 and it is consistent with the structure of ultrathin films grown on highly oriented pyrolytic graphite (HOPG).^{8,9}

Moreover, a trilayer corresponding to the truncation of the helical chains growing perpendicular to the layer plane exposing the Te(0001) face was shown to be unstable with respect to the formation of a trilayer 1T-MoS₂-like geometry, called the α phase in ref. 8. The 1T-MoS₂-like structure was later found to be consistent with transmission electron microscopy (TEM) images of ultrathin films grown by physical vapor deposition (PVD) on silica.¹⁰

The morphology and crystal structure of tellurene seem thus dependent on the growth method, the choice of the substrate and the film thickness.

The exploitation of tellurene in electronic devices, such the field-effect transistors already mentioned⁴ or photodetector devices,¹¹ requires the development of large-area deposition of tellurene on a silicon substrate for eventual integration with standard microelectronic technologies. To this aim, a suitable passivation of the silicon surface is needed. Surface oxidation is a possible option which leads to an amorphous surface for the growth of 2D materials (see several examples in ref. 12). There are, however, numerous examples in the literature showing that the crystalline quality of epitaxial films of layered selenides can be improved by growing directly on the Si(111) surface with an adequate termination of the dangling bonds.^{13–15} Concerning tellurides, it has been shown that GeTe¹⁶ and layered Sb₂Te₃ and (GeTe)_n(Sb₂Te₃)_m¹⁷ can be grown in quasi single-crystalline films by MBE on the Si(111) surface passivated by Sb and reconstructed in a Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb geometry. In fact, this choice of the surface passivation mostly suppresses in-plane rotational domains, and for GeTe, it also reduces twinned domains, which are typical for chalcogenide thin films grown on Si(111).^{18,19} The reduction in the number of rotational domains is expected to reduce the overall number of defects leading to an improvement of the electrical mobility of the film which is beneficial for electronic and optoelectronic applications. The same Si(111) passivated substrate might thus be useful to grow ultrathin crystalline Te and tellurene films as well.

In this perspective, we here investigate the geometry of a trilayer of Te adsorbed on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface by DFT calculations. In particular, we compare the energetics of the formation of Te(10 $\bar{1}$ 0) termination, observed in ref. 5 on graphene, with the 1T-MoS₂-like structure proposed in ref. 8.

2 Computational details

The geometry and adsorption energy of tellurene on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface were studied within the DFT framework implemented in the Quantum Espresso suite of programs.^{20,21} The exchange and correlation functional by

Perdew, Burke and Ernzerhof (PBE)²² and norm-conserving pseudopotentials were employed. The Kohn–Sham (KS) orbitals were expanded on a plane wave basis set up to a kinetic energy cutoff of 24 Ry for geometry optimization at a fixed simulation cell. Optimization of the lattice parameters in a constant pressure relaxation algorithm was performed with a higher cutoff of 50 Ry for the convergence of the stress tensor. All energies reported hereafter refer to the calculation with 24 Ry. The semiempirical correction due to Grimme (D2)²³ was added to include van der Waals (vdW) interactions. The Brillouin zone (BZ) integration was performed on Monkhorst-Pack meshes.²⁴ The pseudopotential/PBE-D2 framework adopted here was also used and validated against different functionals for tellurene in ref. 8.

3 Results and discussion

In order to study the adsorption energy and geometry of tellurene on the Si surface, we first generated a slab model of silicon exposing the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface on one side and a H-passivated 1 $\times$ 1 surface on the other side. We then optimized the geometry of pure Te in the bulk and of a free-standing trilayer of Te in a slab geometry either in the 1T-MoS₂-like structure or exposing the Te(10 $\bar{1}$ 0) surface of the bulk.

Although previous DFT calculations⁸ predicted that, in a free-standing trilayer, tellurene is most stable in the 1T-MoS₂-like structure (α geometry of ref. 8), the interaction with the substrate might favor another configuration such as the Te(10 $\bar{1}$ 0) geometry seen experimentally in ref. 5. We therefore considered both possibilities for the geometry of tellurene adsorbed on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface.

The results of the individual steps summarized above are reported in the different subsections below.

3.1 The clean Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface

The theoretical lattice parameter and bulk modulus for bulk Si within our framework are 5.41 Å and 97 GPa which are close to the experimental values of 5.43 Å and 99 GPa.²⁵ We used the theoretical equilibrium lattice parameter for bulk Si to optimize the model of the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface in a slab with the bottom surface saturated by H in a 1 $\times$ 1 geometry. We applied 3D periodic boundary conditions with a vacuum 20 Å wide separating the periodic images along the direction perpendicular to the surface plane. The hexagonal surface unit cell has a lattice parameter of a_{hex} equal to $\sqrt{3}/2$ times the cubic lattice parameter of bulk Si which in our case yields $a_{\text{hex}} = \sqrt{3}/2 \times 5.407 \text{ Å} = 6.622 \text{ Å}$.

The slab consists of four Si layers, a topmost Sb layer and a hydrogen bottom layer with three atoms per surface unit cell in each layer. The top and side views of the slab are shown in Fig. 1. According to the literature,²⁶ the three Sb atoms per unit cell (one for each Si atom in the topmost surface layer) form a



Fig. 1 (Left panel) Top and (right panel) side views of the slab model of the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface with the bottom layer saturated by hydrogen atoms. In the top view the surface unit cell is shown with Si atoms in the first, second and fourth layers. The three Sb atoms in the surface unit cell (orange spheres) form a trimer with its centroid aligned with the Si atom in the fourth layer. Si, Sb and H atoms are shown by blue, orange and pink spheres, respectively.

Figure 1 illustrates the crystal structure of Te_2Te_3 . The structure is shown in three views: a top view (left), a side view (top right), and a perspective view (bottom). The top view shows a honeycomb-like lattice of Te atoms with Te1, Te2, and Te3 sites labeled. The side view shows the layered structure with Te1, Te2, and Te3 sites labeled. The perspective view shows the 3D arrangement of atoms. Coordinate axes (a, b, c) are shown for each view.

Figure 1 illustrates the crystal structure of Te_2Te_3 . The top part shows the molecular structure of Te_2Te_3 with Te1, Te2, and Te3 sites labeled. The bottom part shows the 3D crystal structure, which is a layered structure with Te_2Te_3 molecules arranged in a periodic fashion. The crystallographic axes a , b , and c are indicated.

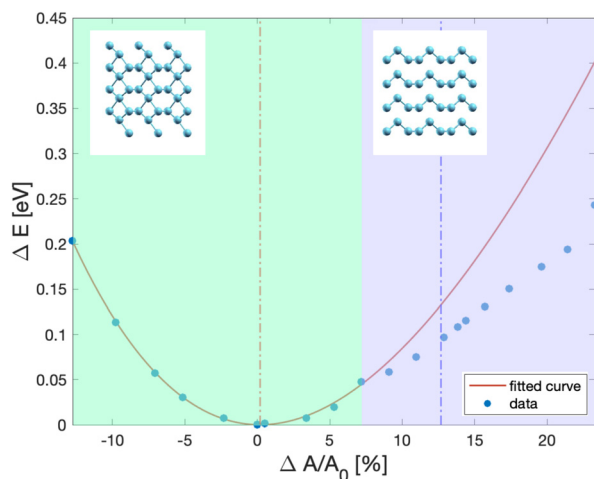


Fig. 4 Energy (dots) per unit cell (three atoms per cell) versus surface area of the Te(1010) trilayer slab from DFT calculations. The surface area is expressed in variation in % with respect to the area at the minimal energy ($4.142 \times 5.449 \text{ \AA}^2$, see text). The red line is a fitting of the data with a 2D version of the Birch–Murnaghan equation of state. In the green region the system is in the β geometry of ref. 8, while in the violet region the bulk-like helical chains are recovered. The insets show the crystal structure in the two regimes. The blue dashed line corresponds to the DFT equilibrium unit cell area of a Te(1010) double-trilayer from ref. 28.

using a hexagonal supercell made of a 5×5 hexagonal cell of tellurene adsorbed on a 3×3 hexagonal cell of the substrate.

The ideal lattice parameter of the adsorbed tellurene would correspond to $5 \times 4.121 \text{ \AA} = 20.61 \text{ \AA}$ which is close to the lattice parameter of the substrate supercell of $3 \times 6.622 \text{ \AA} = 19.87 \text{ \AA}$ (see Section 3.1) with a linear misfit of about 3.6%.

By using the six-layer slab for the silicon substrate (see Section 3.1 and Fig. 1), the commensurate supercell contains 237 atoms.

A better commensuration with a misfit of 0.2% could be obtained by using 8×8 cells of tellurene adsorbed on 5×5 cells of the substrate. This model would, however, contain 642 atoms which are more difficult to be tackled by DFT simulations within our framework. We therefore restricted ourselves to the smaller 237-atom slab. Tellurene was initially adsorbed at a large distance of 5 Å from the surface to allow for possible translation of the trilayer with respect to the substrate. Geometry optimization leads to an interplanar distance between Sb and Te planes of 3.41 Å.

The side and top views of the relaxed slab are shown in Fig. 5. The atomic positions in Cartesian coordinates and the cell edges are given in the ESI.† The calculations are performed by using a $5 \times 5 \times 1$ MP mesh.

We calculated the formation energy of the trilayer adsorbed on the substrate with respect to bulk Te as

$$E_{\text{form}} = \frac{1}{n}(E_{\text{tot}} - E_{\text{sub}} - n \cdot E_{\text{atom bulk}}) \quad (1)$$

where $n = 75$ is the number of Te atoms in the supercell, E_{tot} is the total energy of the relaxed supercell, E_{sub} is the total energy

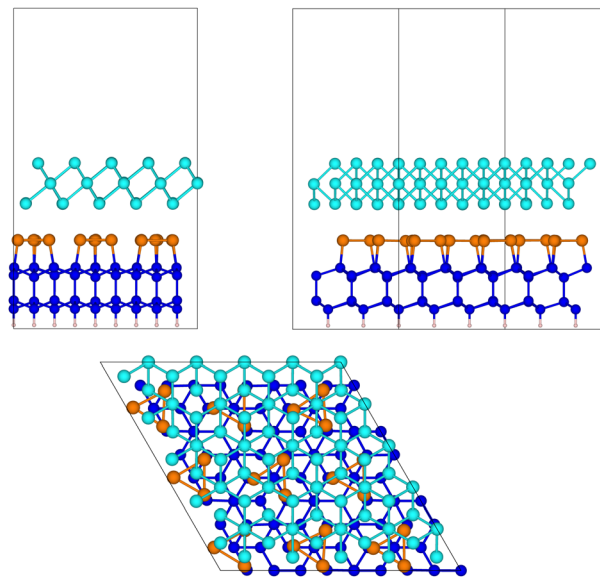


Fig. 5 The relaxed configuration of tellurene in a trilayer 1T-MoS₂-like geometry adsorbed on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface in a slab geometry. Side and top views are shown.

of the clean (no Te) substrate slab and $E_{\text{atom bulk}}$ is the energy per atom of bulk Te.

The resulting formation energy is 94 meV per atom which is positive because the energy gain due to the interaction of Te with the substrate is lower than the energy paid to form a trilayer from the bulk.

The adsorption energy of tellurene on the substrate with respect to the free-standing trilayer is estimated instead by

$$E_{\text{ads}} = \frac{1}{n}(E_{\text{tot}} - E_{\text{sub}} - n \cdot E_{\text{Te-fs}}) \quad (2)$$

where n is still the number of Te atoms and $E_{\text{Te-fs}}$ is the energy per atom of free-standing tellurene in the 1T-MoS₂-like trilayer geometry at its equilibrium lattice parameters (see Section 3.2).

The adsorption energy $E_{\text{ads}} = -59$ meV per atom is negative due to the attractive interaction with the substrate with an energy gain with respect to the free-standing tellurene. The value of E_{ads} is most probably an underestimation because of the strain experienced by the adsorbed tellurene due to the constraint of the supercell geometry which features a 3.6% misfit with respect to the equilibrium lattice parameter of the free-standing trilayer. We then estimated the energy cost of straining tellurene by optimizing the free-standing trilayer with the lattice parameters of the substrate (equivalent to $a = 3.974 \text{ \AA}$). The resulting strain energy with respect to the equilibrium lattice parameters of the free-standing trilayer is 29 meV per atom. By assuming that the same energy penalty is paid by tellurene adsorbed on the substrate, one would predict for tellurene adsorbed in an incommensurate manner on the substrate a formation energy of 65 meV per atom with respect to that of bulk Te (eqn (1)) and an adsorption energy of about -88 meV per atom with respect to that of the optimized free-standing trilayer.



This value of the adsorption energy is larger than the difference in energy between the Te(10 $\bar{1}0$) and the 1T-MoS₂-like geometries of the free-standing trilayer (68 meV per atom, see Section 3.2).

One might thus conceive that the interaction with the substrate might change the hierarchy in energy among the different configurations of the free-standing trilayer.

In the next subsection we will therefore discuss the optimization of the trilayer of Te adsorbed on the substrate in the Te(10 $\bar{1}0$) geometry.

3.3.2 The Te(10 $\bar{1}0$) geometry. For the reconstructed geometry of the Te(10 $\bar{1}0$) structure (β geometry mentioned in ref. 8, see inset in Fig. 4) a commensuration with the substrate is not easy. A possibility is to align the a lattice parameter of tellurene with the a lattice parameter of the hexagonal unit cell in the geometry shown in Fig. 6 which corresponds to 3×2 cells of tellurene matched with a $2a \times \sqrt{3}a$ rectangular supercell of the substrate. By considering the a and b equilibrium lattice parameters of tellurene in the Te(10 $\bar{1}0$) trilayer ($a = 4.142$ Å and $b = 5.449$ Å, see Section 3.2) the mismatch is as large as 5–6% along both the a and b directions.

However, the misfit decreases to 1.2 and 1.3% along the two directions if we consider the unreconstructed trilayer with the helical chains at the equilibrium lattice parameters of a bi-trilayer found in previous DFT calculations²⁸ ($a = 4.36$ Å and $b = 5.81$ Å, see Section 3.2). As a first attempt, we therefore considered the supercell geometry sketched in Fig. 6 with an initial configuration featuring helical Te chains as in the bulk (see Fig. 3).

The optimized geometry of tellurene adsorbed on the slab of the substrate is shown in Fig. 7. The Te chains are still present albeit slightly distorted, with the Te atoms two-fold coordinated. The average interplanar distance between the Sb and the innermost Te plane is 2.96 Å. The atomic positions in Cartesian coordinates and the cell edges of the slab are given in the ESI.†

We calculated the formation energy of the trilayer adsorbed on the surface with respect to bulk Te as given by eqn (1) ($n = 18$ for this geometry) which yields $E_{\text{form}} = 111$ meV per atom. This value is larger than the formation energy obtained for the 1T-MoS₂-like geometry reported in the previous section. This result confirms the higher stability of the latter configuration as it occurs for the free-standing trilayer. The adsorption energy of tellurene on the substrate with respect to that of the

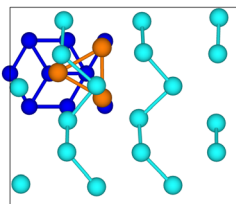


Fig. 6 Sketch of the commensuration of tellurene in the Te(10 $\bar{1}0$) geometry with the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface. The rectangular surface unit cell has edges $a = 13.244$ Å and $b = 11.470$ Å. For the silicon substrate only atoms within the surface unit cell in the first, second and fourth layers are shown.

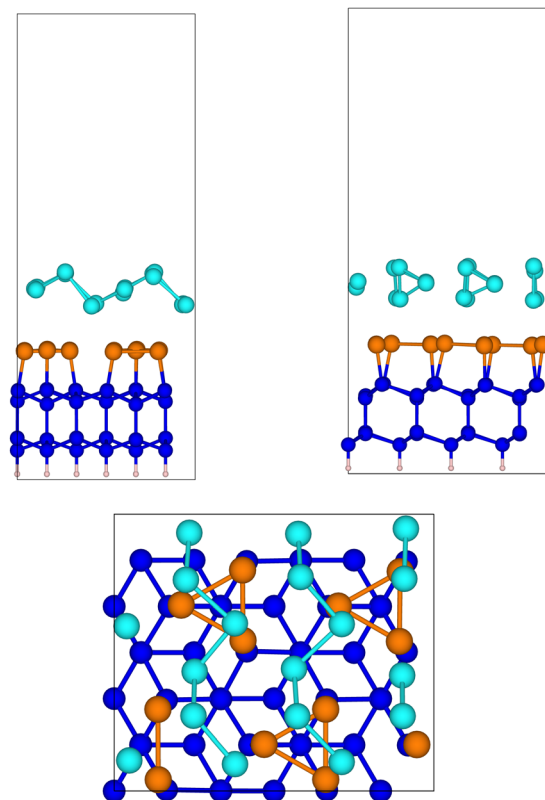


Fig. 7 Side and top views of the relaxed configuration of tellurene in the Te(10 $\bar{1}0$) geometry on Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface.

free-standing trilayer given by eqn (2) is instead $E_{\text{ads}} = -112$ meV per atom for the Te(10 $\bar{1}0$) geometry which suggests a stronger interaction between the trilayer and the substrate than for the 1T-MoS₂-like geometry (−59 meV per atom, see Section 3.3.1). We must also consider that tellurene adsorbed on the surface is highly strained with respect to the equilibrium lattice parameter of the Te(10 $\bar{1}0$) free-standing trilayer. We then calculated the strain energy from the energy difference between the trilayer at the equilibrium lattice parameter (β geometry of ref. 8) and at the lattice parameters commensurate with the substrate as given above. The resulting strain energy is 32 meV per atom. By assuming that the same energy penalty is paid by tellurene adsorbed on the substrate, one would predict for tellurene adsorbed in an incommensurate manner on the substrate a formation energy of $111 - 31$ meV per atom = 80 meV per atom which is higher by only 15 meV per atom than that of tellurene adsorbed in the 1T-MoS₂-like trilayer (65 meV per atom, see Section 3.3.1).

3.3.3 Electronic properties of tellurene adsorbed on the passivated silicon surface. We investigated the effect on the electronic gap of the interaction with the substrate for the α and β phases by comparing the electronic density of states (DOS) of the freestanding tellurene in the two phases with the DOS projected on the Te atoms for tellurene adsorbed on the silicon surface. To this aim, we used the Heyd–Scuseria–Ernzerhof hybrid functional (HSE06)²⁹ which is known to describe well the electronic band gap of bulk Te.³⁰ The same functional was



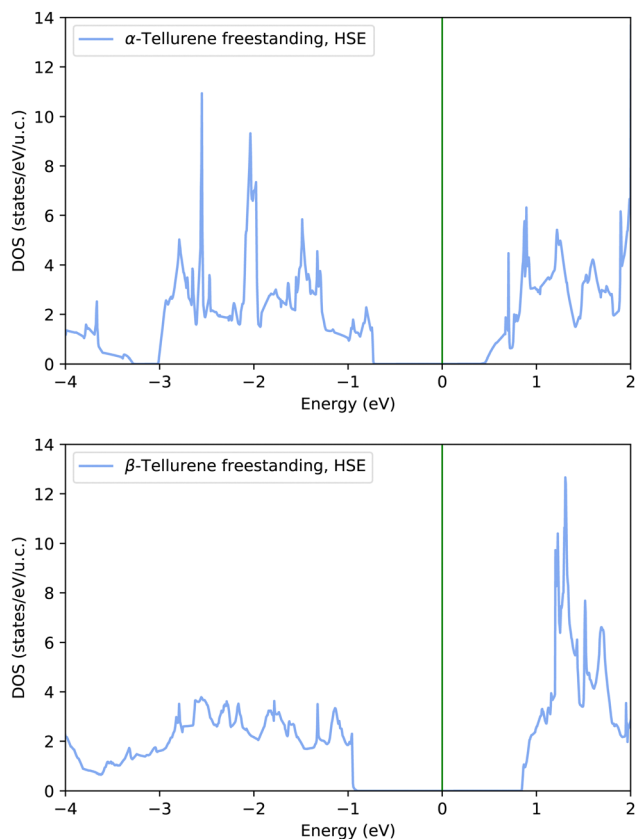


Fig. 8 Electronic density of states of the (top panel) 1T-MoS₂-like (α) and (bottom panel) Te(10 $\bar{1}$ 0) (β) phases of free-standing tellurene computed with the HSE06 functional and the tetrahedra method on 64×64 (α phase) or 64×48 (β phase) meshes.

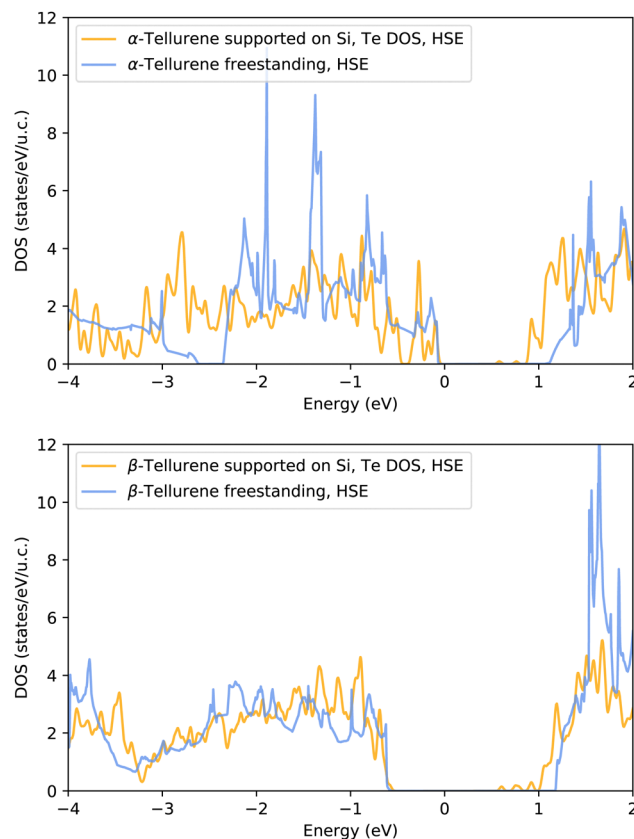


Fig. 9 Electronic density of states projected on the Te atoms of the (top panel) 1T-MoS₂-like (α) and (bottom panel) Te(10 $\bar{1}$ 0) (β) phases of tellurene adsorbed on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface. The DOS is computed with the HSE06 functional on a single special point with a smearing of the Kohn–Sham energy of 0.015 Ry. The DOS of the adsorbed tellurene is compared with that of the free-standing tellurene in Fig. 8. The DOS are aligned at the top of the valence band.

used for free-standing tellurene in ref. 8. The electronic DOS of the 1T-MoS₂-like (α) and Te(10 $\bar{1}$ 0) (β) phases of free-standing tellurene reported in Fig. 8 reproduces the band gap already found in ref. 8.

The DOS projected on the Te atoms 1T-MoS₂-like (α) and (bottom panel) Te(10 $\bar{1}$ 0) (β) phases of tellurene adsorbed on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface are shown in Fig. 9 and compared with the DOS of the corresponding free-standing phases. It turns out that the interaction with the surface leads to a substantial reduction of the band gap for both phases.

4 Conclusions

In summary, we reported on DFT calculations of the adsorption of a trilayer tellurene on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface. This surface has been chosen here as a suitable substrate for the growth of a high quality tellurene film directly on Si surfaces for integration with silicon technology. In fact, it has been shown in the literature that different telluride compounds, such as GeTe¹⁶ and layered Sb₂Te₃ and (GeTe)_n (Sb₂Te₃)_m¹⁷ can be grown on this substrate as quasi single-crystalline thin films with minimal rotational disorder of the crystalline domains which is expected to improve the electrical

properties of the film. Our DFT calculations reveal that the adsorption energy is substantially different for the two phases, α and β , of free-standing tellurene. Although in the free-standing geometry the α phase is 68 meV per atom lower in energy than the β phase, the adsorption energy partially compensates this energy difference. In spite of the many uncertainties due to the constraints of commensuration with the substrate, DFT calculations suggest that tellurene in the α phase, which consists of a trilayer 1T-MoS₂-like geometry, becomes only marginally (15 meV per atom) more stable than the β geometry when adsorbed on the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface. This result supports the experimental pieces of evidence that the formation of the α or β phases depends on the substrate the tellurene is grown on. On the Si(111)-($\sqrt{3} \times \sqrt{3}$)R30°-Sb surface, which is here suggested as a suitable substrate for the integration of tellurene on silicon in analogy with other tellurides, the energy difference of the two phases is particularly tiny and the prevalence of one trilayer phase with respect to the other might thus be strongly affected by the kinetics effects and deposition conditions. Obviously,



the Te(10 $\bar{1}0$) geometry will finally prevail by increasing the number of Te layers.

Author contributions

Conceptualization: M. B. and S. C.; investigation: S. I., D. D., M. B., and S. C.; validation and data curation: S. I., D. D., D. C., and M. B.; methodology and supervision: M. B.; writing—original draft: S. I. and M. B.; writing—review & editing: S. I., M. B., D. C., and S. C.

Conflicts of interest

There are no conflicts to declare.

Notes and references

- 1 C. Grazianetti, C. Martella and A. Molle, *Phys. Status Solidi RRL*, 2020, **14**, 1900439.
- 2 C. Adenis, V. Langer and O. Lindqvist, *Acta Crystallogr.*, 1989, **C45**, 941–942.
- 3 H. O. H. Churchill, G. J. Salamo, S.-Q. Yu, T. Hironaka, X. Hu, J. Stacy and I. Shih, *Nanoscale Res. Lett.*, 2017, **12**, 488.
- 4 Y. Wang, G. Qiu, R. Wang, S. Huang, Q. X. Wang, Y. Liu, Y. Du, W. A. G. III, M. J. Kim, X. Xu, P. D. Ye and W. Wu, *Nat. Electron.*, 2018, **1**, 228–236.
- 5 X. Huang, J. Guan, Z. Lin, B. Liu, S. Xing, W. Wang and J. Guo, *Nano Lett.*, 2017, **17**, 4619–4623.
- 6 R. Tran, Z. Xu, B. Radhakrishnan, D. Winston, W. Sun, K. A. Persson and S. P. Ong, *Sci. Data*, 2016, **3**, 1–13.
- 7 Q. Wang, M. Safdar, K. Xu, M. Mirza, Z. Wang and J. He, *ACS Nano*, 2014, **8**, 7497–7505.
- 8 Z. Zhu, X. Cai, S. Yi, J. Chen, Y. Dai, C. Niu, Z. Guo, M. Xie, F. Liu, J.-H. Cho, Y. Jia and Z. Zhang, *Phys. Rev. Lett.*, 2017, **119**, 106101.
- 9 J. Chen, Y. Dai, Y. Ma, X. Dai, W. Ho and M. Xie, *Nanoscale*, 2017, **9**, 15945–15948.
- 10 A. Apte, E. Bianco, A. Krishnamoorthy, S. Yazdi, R. Rao, N. Glavin, H. Kumazoe, V. Varshney, A. Roy, F. Shimojo, E. Ringe, R. K. Kalia, A. Nakano, C. S. Tiwary, P. Vashishta, V. Kochat and P. M. Ajayan, *2D Mater.*, 2018, **6**, 015013.
- 11 Z. Yan, H. Yang, Z. Yang, C. Ji, G. Zhang, Y. Tu, G. Du, S. Cai and S. Lin, *Small*, 2022, **18**, 2200016.
- 12 N. Youngblood and M. Li, *Nanophotonics*, 2017, **6**, 1205.
- 13 H. Li, L. Gao, H. Li, G. Wang, J. Wu, Z. Zhou and Z. Wanga, *Appl. Phys. Lett.*, 2013, **102**, 074106.
- 14 G. Zhang, H. Qin, J. Teng, J. Guo, Q. Guo, X. Dai, Z. Fang and K. Wu, *Appl. Phys. Lett.*, 2009, **95**, 053114.
- 15 N. Bansal, Y. S. Kim, E. Edrey, M. Brahlek, Y. Horibe, K. Iida, M. Tanimura, G.-H. Li, T. Feng and H. D. Li, *et al.*, *Thin Solid Films*, 2011, **520**, 224.
- 16 R. Wang, J. E. Boschker, D. D. S. Emilie Bruyer, S. Picozzi, K. Perumal, A. Giussani, H. Riechert and R. Calarco, *J. Phys. Chem. C*, 2014, **118**, 29724–29730.
- 17 J. E. Boschker, J. Momand, V. Bragaglia, R. Wang, K. Perumal, A. Giussani, B. J. Kooi, H. Riechert and R. Calarco, *Nano Lett.*, 2014, **14**, 3534.
- 18 L. H. X. Kou and K. L. Wang, *Phys. Status Solidi RRL*, 2013, **7**, 50.
- 19 N. V. Tarakina, S. Schreyeck, T. Borzenko, C. Schumacher, G. Karczewski, K. Brunner, C. Gould, H. Buhmann and L. W. Molenkamp, *Cryst. Growth Des.*, 2012, **12**, 1913.
- 20 P. Giannozzi, S. Baroni, N. Bonini, M. Calandra, R. Car, C. Cavazzoni, D. Ceresoli, G. L. Chiarotti, M. Cococcioni, I. Dabo, A. D. Corso, S. de Gironcoli, S. Fabris, G. Fratesi, R. Gebauer, U. Gerstmann, C. Gougoussis, A. Kokalj, M. Lazzeri, L. Martin-Samos, N. Marzari, F. Mauri, R. Mazzarello, S. Paolini, A. Pasquarello, L. Paulatto, C. Sbraccia, S. Scandolo, G. Sclauzero, A. P. Seitsonen, A. Smogunov, P. Umari and R. M. Wentzcovitch, *J. Phys.: Condens. Matter*, 2009, **21**, 395502.
- 21 P. Giannozzi, O. Andreussi, T. Brumme, O. Bunau, M. B. Nardelli, M. Calandra, R. Car, C. Cavazzoni, D. Ceresoli, M. Cococcioni, N. Colonna, I. Carnimeo, A. D. Corso, S. de Gironcoli, P. Delugas, R. A. D. S. Jr., A. Ferretti, A. Floris, G. Fratesi, G. Fugallo, R. Gebauer, U. Gerstmann, F. Giustino, T. Gorni, J. Jia, M. Kawamura, H.-Y. Ko, A. Kokalj, E. Küçükbenli, M. Lazzeri, M. Marsili, N. Marzari, F. Mauri, N. L. Nguyen, H.-V. Nguyen, A. O. de la Roza, L. Paulatto, S. Poncé, D. Rocca, R. Sabatini, B. Santra, M. Schlipf, A. P. Seitsonen, A. Smogunov, I. Timrov, T. Thonhauser, P. Umari, N. Vast, W. Xifan and S. Baroni, *J. Phys.: Condens. Matter*, 2017, **29**, 465901.
- 22 J. P. Perdew, K. Burke and M. Ernzerhof, *Phys. Rev. Lett.*, 1996, **77**, 3865–3868.
- 23 S. Grimme, *J. Comput. Chem.*, 2006, **27**, 1787–1799.
- 24 H. J. Monkhorst and J. D. Pack, *Phys. Rev. B: Solid State*, 1976, **13**, 5188–5192.
- 25 C. Kittel, in *Introduction to Solid State Physics*, Wiley; New York, 5th edn, 1976.
- 26 S. Bengió, M. Martin, J. Avila, M. C. Asensio and H. Ascolani, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2002, **65**, 205326.
- 27 R. Keller, W. B. Holzapfel and H. Schulz, *Phys. Rev. B: Solid State*, 1977, **16**, 4404–4412.
- 28 J. Qiao, Y. Pan, F. Yang, C. Wang, Y. Chai and W. Ji, *Sci. Bull.*, 2018, **63**, 159–168.
- 29 J. Heyd, G. E. Scuseria and Z. Ernzerhof, *J. Chem. Phys.*, 2003, **118**, 8207.
- 30 D. K. Sang, B. Wen, S. Gao, Y. Zeng, F. Meng, Z. Guo and H. Zhang, *Nanomaterials*, 2019, **9**, 1075.

