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# How covalence breaks adsorption-energy scaling relations and solvation restores them†

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It is known that breaking the scaling relations between the adsorption energies of \*O, \*OH, and \*OOH is paramount in catalyzing more efficiently the reduction of O<sub>2</sub> in fuel cells and its evolution in electrolyzers. Taking metalloporphyrins as a case study, we evaluate here the adsorption energies of those adsorbates on the metal centers Cr, Mn, Fe, Co, Ni and Cu, using H, F, OH, NH<sub>2</sub>, CH<sub>3</sub>, and BH<sub>2</sub> as ring ligands. We show that covalence systematically breaks scaling relations under vacuum by strengthening certain M–OOH bonds. However, covalence modifies adsorbate solvation in solution depending on the degree of covalence of the metal–adsorbate bonds. The two effects have similar magnitudes and opposite signs, such that scaling relations are restored in solution. Thus, solvation is a crucial ingredient that must be taken into account in studies aimed at breaking scaling relations in solution. Our findings suggest that the choice of metal and ligand determines the catalytic activity within the limits imposed by scaling relations, whereas the choice of an appropriate solvent can drive such activity beyond those limits.

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## Introduction

Since their discovery almost a decade ago,<sup>1</sup> adsorption-energy scaling relations have experienced rapid development<sup>2–4</sup> that has, in turn, revolutionized the “*in silico*” design of catalysts.<sup>4,5</sup> Among the numerous fields that benefit from their insight, oxygen electrocatalysis is a prominent example. For the oxygen evolution reaction (OER), scaling relations have provided a simple framework for selecting active catalysts<sup>6–9</sup> and revealed the existence of thermodynamic limitations to the efficiency of electrolyzers related to the relative stability of the adsorbed intermediates.<sup>6,10</sup>

If the OER proceeds through a mechanism in which water molecules are transformed into molecular oxygen as follows: H<sub>2</sub>O → \*OH → \*O → \*OOH → O<sub>2</sub>, the ideal energetic separation between \*OH and \*OOH (where \* denotes an adsorbed state) should be 2.46 eV. However, it is found to be ~3.2 eV, estimated from the energetics of: \*OH + H<sub>2</sub>O(l) → \*OOH + 2(H<sup>+</sup> + e<sup>−</sup>), regardless of the material types<sup>4,6,8–11</sup> and the geometry of their active sites.<sup>3</sup> Therefore, there is a substantial “scaling” overpotential  $\eta_{\text{OER}}^{\text{scaling}} \approx (3.20 - 2.46) \text{ eV}/2e^- \approx 0.37 \text{ V}$ . Note that such an overpotential is also present in the oxygen reduction reaction

(ORR) in proton-exchange membrane fuel cells, at the cathode of which molecular oxygen is transformed into water.<sup>12,13</sup> These stringent limitations make the breaking of scaling relations paramount in oxygen electrocatalysis, though only a few examples exist in which the breaking of the \*OH vs. \*OOH scaling is correlated with an experimental increase in catalytic activity.<sup>14,15</sup>

Given the versatility of MN<sub>4</sub> complexes<sup>16</sup> such as porphyrins and their high activities for the OER, the ORR and other reactions,<sup>17–20</sup> here we evaluate whether they can break scaling relations by changing the metal centers (Cr, Mn, Fe, Co, Ni, Cu) and ring ligands (H, F, OH, CH<sub>3</sub>, NH<sub>2</sub> and BH<sub>2</sub>). We show that Ni and Cu centers with various ligands break scaling relations under vacuum by virtue of their highly covalent bonds with \*OOH. However, such covalence entails poor solvation in aqueous solution, which restores scaling relations. Thus, scaling relations must be broken in solution, where substrate–solvent–adsorbate interactions are present. This is a simple yet important conclusion in computational electrocatalysis, as solvation is normally added as an external, constant correction, regardless of the nature of the active site.<sup>11,13,15,28,29</sup> In practice, our results suggest that a combination of high covalence and poor adsorbate–solvent interactions can be beneficial for oxygen electrocatalysis.

## Methods

We have carried out spin unrestricted calculations of the porphyrins with and without the adsorbates and determined the most stable spin states, which can be found in the ESI, Section S4.† The spin states found are in agreement with those

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reported in previous studies. Fig. 1 contains typical geometric configurations of the metalloporphyrins and ligands in this study. While rings with H, F, OH and BH<sub>2</sub> ligands are flat, NH<sub>2</sub> and CH<sub>3</sub> introduce large distortions. In all cases, however, the four nitrogen atoms and the metal center are in a square planar arrangement. The DFT calculations of the adsorption energies were performed using the PAW method in VASP,<sup>21,22</sup> the RPBE exchange-correlation functional,<sup>23</sup> and a plane-wave cut-off of 400 eV. We used the computational hydrogen electrode<sup>24</sup> to describe proton–electron transfers and Rossmeisl *et al.*'s model for the ORR/OER on functionalized graphitic materials,<sup>26</sup> which has also been used before on porphyrins,<sup>11,19</sup> see full details in Sections S1 and S2.† The structures were optimized with the conjugate gradient method, allowing all atoms to relax in all directions until the maximum force on any atom was below 0.01 eV Å<sup>-1</sup>. Porphyrins, H<sub>2</sub>O and H<sub>2</sub> were calculated in boxes of 20 Å × 20 Å × 20 Å, with  $k_B T = 0.001$  eV, using the gamma point only and Gaussian smearing; all energies were extrapolated to 0 K. Section S1 in the ESI† contains the DFT adsorption energies ( $\Delta E$ ), zero-point energies (ZPE), entropy (TS) and solvation corrections ( $\Delta E^{\text{sol}}$ ) needed to calculate free energies under vacuum ( $\Delta G^{\text{vac}}$ ) and in solution ( $\Delta G^{\text{sol}}$ ). We assessed the solvation corrections with the Conductor-like Screening Model (COSMO)<sup>25</sup> to account for water–adsorbate–porphyrin interactions, following recent works.<sup>20</sup> See further details of the COSMO and ZPE calculations in Section S3 in the ESI,† where we also provide a comparison between implicit and first-shell

explicit solvation to demonstrate the suitability of the implicit method used here to capture solvation effects.

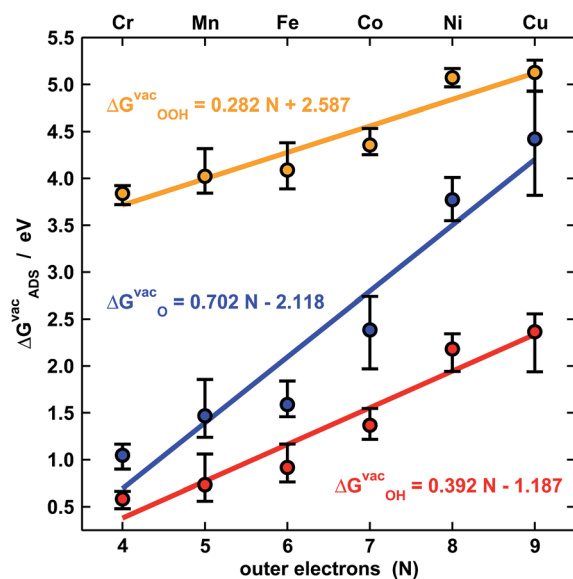
## Results and discussion

Fig. 2 shows the trends in adsorption energies for \*O, \*OH and \*OOH. The trends in average adsorption energies are a function of the number of outer electrons ( $N$ ) of the metal centers.<sup>7,9</sup> Since the oxidation state of those centers in porphyrins is +2,  $N$  is  $2e^-$  less than the number of valence electrons. The error bars in Fig. 2 show the influence of the ligands on the adsorption properties. According to the figure,  $N$  is the main parameter that modulates the trends, but the porphyrin's ligands can as well change the adsorption properties substantially. For instance, the effects of F, OH, CH<sub>3</sub>, NH<sub>2</sub> and BH<sub>2</sub> on the binding energies of \*OH are presented in Table S5.† In broad terms, F, OH, CH<sub>3</sub> and NH<sub>2</sub> stabilize the adsorption energies with respect to porphyrin rings with H ligands, while BH<sub>2</sub> destabilizes them, regardless of the metal center. Thus, ligand selection is a rational way of tuning the adsorption properties of porphyrins.

The approximate linearity of the relations between adsorption energies and  $N$  in Fig. 2 justifies the existence of linear scaling relations between the adsorption energies themselves shown in Fig. 3a.<sup>1–3,7,9</sup> Quantitatively speaking, combining the linear fits in Fig. 2 provides good estimates of the slopes and offsets in Fig. 3a. For instance, the ratio of the slopes for the adsorption energies of \*OH (0.38) and \*OOH (0.28) in Fig. 2 is equivalent to that observed at the bottom of Fig. 3a (0.79). In similar ways, one can obtain the rest of the slopes and offsets in Fig. 3a.



**Fig. 1** Ligands in the porphyrin rings under study. (a) H, (b) F, (c) OH, (d) NH<sub>2</sub>, (e) CH<sub>3</sub>, and (f) BH<sub>2</sub>. Rings with F, OH and BH<sub>2</sub> ligands generally exhibit the typical flat configuration of metalloporphyrins with H ligands, whereas NH<sub>2</sub> and CH<sub>3</sub> ligands introduce large distortions. In all cases, the MN<sub>4</sub> complex made of four nitrogen atoms and a transition metal atom (M) is in a square planar arrangement. Porphyrins with –H ligands and ORR/OER adsorbates are also shown: (g) \*O; (h) \*OH; (i) \*OOH.



**Fig. 2** Adsorption-energy trends of \*O (blue), \*OH (red) and \*OOH (orange) under vacuum for metal centers from Cr to Cu as a function of their number of outer electrons ( $N$ ). The points are the average adsorption energies and the error bars show the energetic effect of the ligands in Fig. 1.



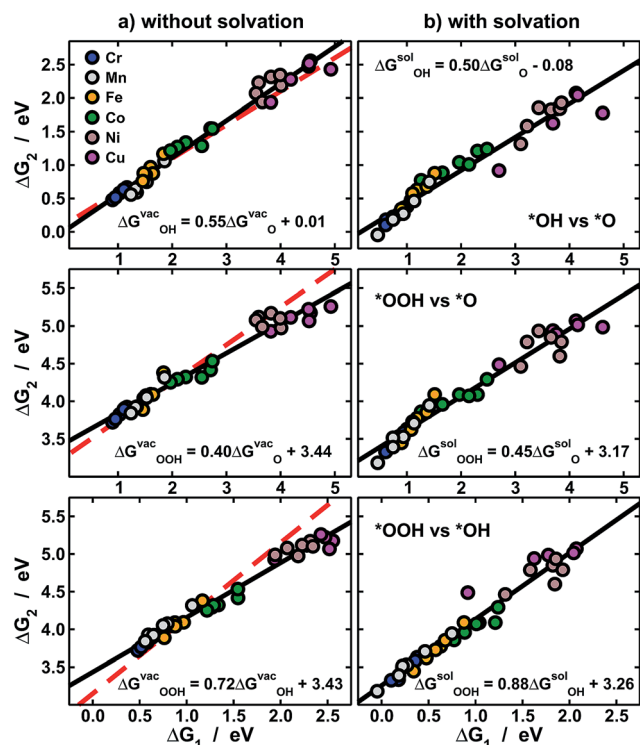


Fig. 3 Scaling relations between the adsorption energies of  $^*O$ ,  $^*OH$  and  $^*OOH$  (a) under vacuum, and (b) solvated. In each panel linear fits (black) and their equations are provided. Top:  $^*OH$  vs.  $^*O$ ; middle:  $^*OOH$  vs.  $^*O$ ; bottom:  $^*OOH$  vs.  $^*OH$ . The red dashed lines in (a) are from ref. 11 and show that while  $\Delta G_{O}^{vac}$  and  $\Delta G_{OH}^{vac}$  behave normally (top),  $\Delta G_{OOH}^{vac}$  (middle and bottom) causes large deviations in scaling relations. In (b) solvation restores the scaling relations broken under vacuum by making the slopes approach the ideal values of 0.5 and 1.

The expected slope of the adsorption-energy scaling relation of  $^*OH$  vs.  $^*O$  (Fig. 3a, top) is 0.5,<sup>1–3</sup> as oxygen in  $^*OH$  lacks  $1e^-$  to reach the octet and  $^*O$  lacks  $2e^-$ . The slope of 0.55 is, thus, in fair agreement with this prediction and our new data fit within previous trends,<sup>11,26</sup> represented by the dashed line. Analogously, the expected slope for  $^*OOH$  vs.  $^*O$  is 0.5, but the one observed here is 0.40 (Fig. 3a, middle). Furthermore, the expected slope for  $^*OOH$  vs.  $^*OH$  is 1,<sup>1–3</sup> as the oxygen in both  $^*OH$  and  $^*OOH$  lacks  $1e^-$  to reach the octet, but the observed slope is 0.72. These slopes of 0.40 and 0.72 cause deviations from the expected trends (red lines in Fig. 3a, middle and bottom) that can be as large as 0.65 eV for Ni and Cu centers. We note that smaller deviations were reported before on metal oxides from the unity slope,<sup>7,27</sup> but their origin and implications were not discussed. The even larger deviations in this study are systematic and stem from the sizably different slopes of the relations of  $\Delta G_{OOH}^{vac}$  and  $\Delta G_{OH}^{vac}$  with  $N$  in Fig. 2 (0.28 vs. 0.39). In Fig. 4 and 5 we show the reason for such different slopes.

In sum, Fig. 3a indicates that the adsorption energies under vacuum of  $^*O$  and  $^*OH$  behave normally, while those of  $^*OOH$  are anomalous. As described before, such deviations are important for OER/ORR electrocatalysis, as it is believed that the scaling between the adsorption energies of  $^*OOH$  and  $^*OH$  limits the performance of fuel cells and electrolyzers.<sup>3,6,7,9–11</sup> Let

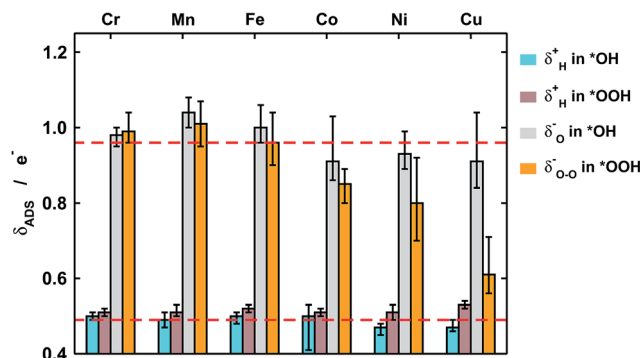


Fig. 4 Excess charge ( $\delta^-$ ) or lack of charge ( $\delta^+$ ) on H, O, and O–O in  $^*OH$  and  $^*OOH$ . While the charges of H in  $^*OH$  (light blue), H in  $^*OOH$  (brown), and O in  $^*OH$  (gray) are relatively constant for the different metal centers, that of O–O in  $^*OOH$  (orange) undergoes large changes as the metal ion goes from Cr to Cu. The red dashed lines correspond to the average values of O and H in  $^*OH$ . Error bars are provided to show the effect of the ring ligands.

us consider one exceptional site in Fig. 3a: Cu centers with  $CH_3$  ligands, which have an energetic difference of 2.55 eV between  $^*OOH$  and  $^*OH$ , implying that the predicted “scaling” overpotential is  $\eta_{OER/ORR}^{scaling} = 0.04$  V. Thus, those and several other Ni and Cu centers promise to catalyze almost reversibly the OER/ORR in view of their nearly ideal energetic differences between  $^*OH$  and  $^*OOH$ . However, the adsorption energies in Fig. 2 and 3a do not contain any solvation contributions, as those are traditionally added externally and are constant for all materials.<sup>11,13,15,28,29</sup>

To get a more accurate assessment of water solvation, we have used an implicit solvent model,<sup>25</sup> the results of which appear in Fig. 3b. Interestingly,  $^*O$  is substantially solvated on metalloporphyrins ( $-0.39$  eV on average), in contrast with metal surfaces where it has no solvation.<sup>15,28,29</sup> Moreover, for the scaling of  $^*OH$  vs.  $^*O$  the slope changes from 0.55 to 0.50, for  $^*OOH$  vs.  $^*O$  it changes from 0.40 to 0.45, and for  $^*OOH$  vs.  $^*OH$  it moves from 0.72 to 0.88. These changes, which make the slopes approach the values expected from electron-counting rules, are possible because the evaluated solvation contributions differ from one metal center to the next and also depend on the ring ligands, unlike traditional, constant-shift solvation corrections.<sup>11,28,29</sup>

Thus, solvation restores in aqueous solution the scalability lost under vacuum. It is important to emphasize that studies devoted to scaling relations<sup>1–3,6,10</sup> and their breaking<sup>14,30</sup> are usually carried out under vacuum and do not directly consider the effect of active-site-dependent solvation. In conclusion, non-scalability under vacuum is neither a necessary nor a sufficient condition to ensure high catalytic activity in solution, and actual breaking of scaling relations for electrocatalytic purposes can only be guaranteed if solvent–adsorbate–substrate interactions are properly accounted for.

It is then essential to understand why scaling relations are broken under vacuum but restored in solution. Recapping, Fig. 2 shows that adsorption energies become weaker as the metal center ranges from Cr to Cu, but the changes for those of



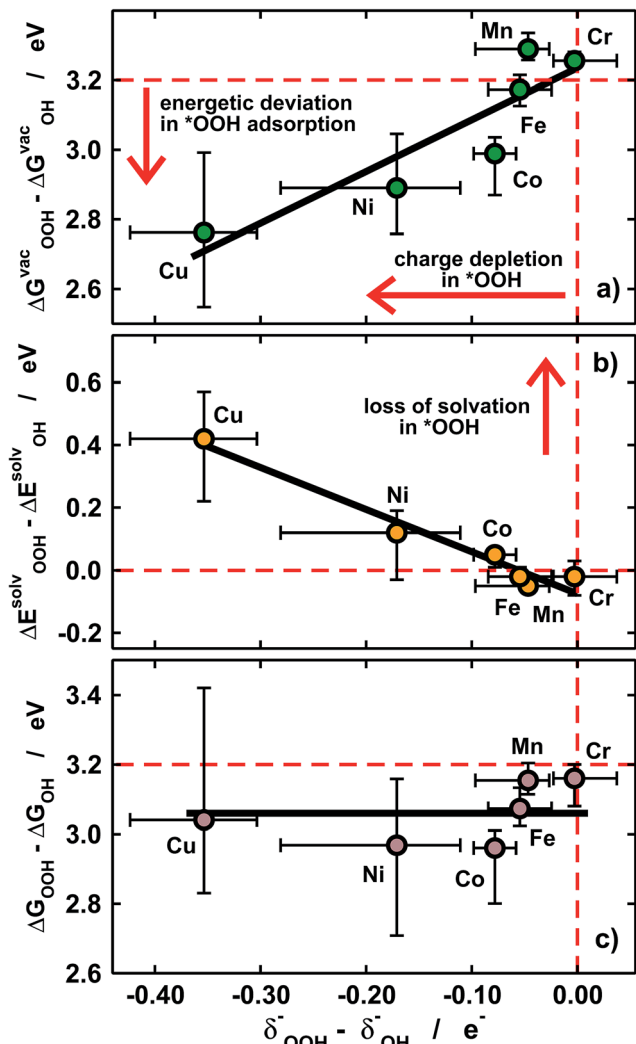


Fig. 5 Covalence effects on \*OH and \*OOH adsorption. (a) Differences in the adsorption energies of \*OOH and \*OH under vacuum vs. the differences in their electronic charges. (b) Differences in solvation energies vs. differences in electronic charges. In (a) and (b) the deviations from ideality grow in opposite directions when going from Cr to Cu, so that the differences in solvated adsorption energies in (c) are nearly constant ( $\sim 3.1$  eV). The dashed lines in (a–c) mark the ideal situation in which \*OOH and \*OH have identical charges and solvation energies and their energetic separation is 3.2 eV.

\*OOH are less pronounced than for \*OH. Fig. 3a shows that this results in sizable deviations from ideality for Ni and Cu centers under vacuum. However, Fig. 3b shows that water solvation restores the lost scalability. These observations intuitively suggest that a given aspect of Ni and Cu centers makes them bind \*OOH and \*OH differently compared to other centers, an effect which is compensated in solution by solvation losses. In the following we will argue that this such aspect is the covalence of the bonds created by Ni and Cu with the oxygen atom in \*OH and \*OOH.

First of all, in Fig. 4 we quantify covalence in terms of the average excess charge in \*OH ( $\delta_{\text{OH}}^-$ ) and \*OOH ( $\delta_{\text{OOH}}^-$ ), calculated with Bader's method.<sup>31</sup> The excess or lack of charge is

calculated with respect to the number of valence electrons: a lack of charge of  $0.5e^-$  for H ( $1s^1$ ) means that  $0.5e^-$  from its valence electron has been withdrawn. Analogously, an excess charge of  $1e^-$  for O ( $1s^2 2s^2 2p^4$ ) means that in addition to its 6 valence electrons, the interaction with H and the porphyrin ring grants it an additional electron. For all metal centers with \*OH and \*OOH the charge depletion in the H atoms is approximately constant ( $\sim 0.5e^-$ ). Similarly, the excess charge of the O atoms in \*OH is constant ( $\sim 1e^-$ ). Therefore, the charge in \*OH remains approximately constant regardless of the nature of the metal center and the ligands. However, significant changes are observed for the O–O moiety in \*OOH, where the excess charge decreases systematically from 1 to  $\sim 0.65e^-$  when the metal center varies between Cr and Cu. Thus, the covalence of the metal–oxygen bonds in \*OOH, measured as a depletion of charge in the adsorbate, changes substantially, is different compared with that of metal–oxygen bonds in \*OH, and is due to the O–O moiety.

Furthermore, we show in Fig. 5a that the degree of covalence and energetic deviation for the scaling relation between \*OH and \*OOH are directly related. This means that covalence is responsible for the breaking of scaling relations between adsorption energies for highly covalent metal–oxygen bonds, namely those in which there is little charge transfer between active sites and adsorbates. Since the exceptions arise only for late transition metals, namely Ni and Cu, the linearity of the relations is not affected and the deviations modify only the slope.

Given that \*OH and \*OOH are polar chemisorbates immersed in a polar solvent (water), intuitively large covalence should cause a loss of solvation. This is what we see in Fig. 5b, where covalence lowers the solvation energies in solution for Ni and Cu centers. The magnitude of the losses in Fig. 5b is commensurate with that of the adsorption-energy deviations under vacuum for all metal centers in Fig. 5a but their signs are opposite, so that the adsorption energies in solution behave normally (see Fig. 3b) and  $\Delta G_{\text{OOH}}^{\text{solv}} - \Delta G_{\text{OH}}^{\text{solv}} \approx 3.2$  eV for all metal centers and ligands, as shown in Fig. 5c.

In sum, Fig. 5 supports the following simple but important methodological conclusion: if scaling relations are to be broken to improve the efficiency of (electro)catalytic reactions in solution, solvation has to be taken into account in the calculations, which is not generally the case in the state of the art.

Before closing the discussion, it is important to evaluate the impact of solvation on catalytic-activity predictions. To do so, in Fig. 6 we present volcano-type activity plots for the OER and the ORR on the porphyrins under study. Fig. 6a contains free energies in solution including only a constant-shift solvation (CSS) correction of  $-0.30$  eV for \*OH and \*OOH on all centers.<sup>11,26</sup> On the other hand, Fig. 5b contains the metal- and ligand-dependent solvation (MLS) corrections in Fig. 3b and 5 added to the free energies of \*O, \*OH and \*OOH.

With the CSS and MLS approaches we find that the best catalysts for the ORR contain Co centers, and various ligands help in tuning the activity towards the top of the volcano. Note that F and  $\text{BH}_2$  enhance the ORR activity of Fe centers. For the OER, however, the predictions differ significantly. In the MLS



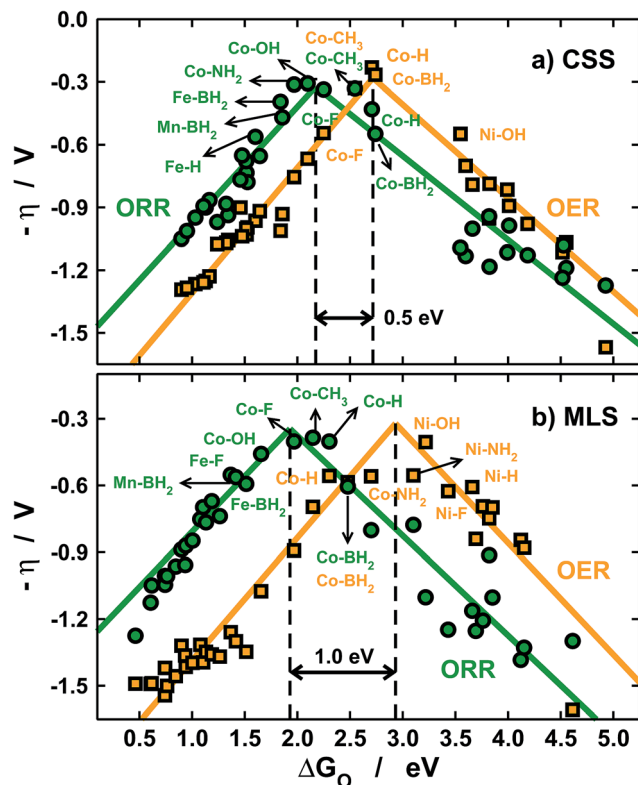


Fig. 6 Volcano-type activity plots for the ORR (green) and the OER (orange). The overpotential ( $\eta$ ) is plotted against the adsorption energies of  $^*O$ , see Section S2 in the ESI.† (a) Using a constant-shift solvation correction (CSS) from ref. 11 and 26 and (b) using the metal- and ligand-dependent solvation corrections (MLS) calculated in this study. The black dashed lines mark the top of the OER and ORR volcanoes and show that different solvation treatments lead to different activity predictions.

approach Ni centers with OH and  $NH_2$  ligands are predicted to be highly active, and Co centers with  $BH_2$  and  $NH_2$  also appear to be fairly active.

Conversely, the CSS approach predicts that only Co centers are active for the OER. The predictions are similar for the ORR and different for the OER because of the reaction mechanisms (see Section S2 in the ESI.†).

For the ORR, the overpotential ( $\eta$ ) typically depends on elementary steps involving  $^*OH$  and  $^*OOH$  only, the solvation of which is accounted for by both the CSS and MLS methods. Conversely, for the OER the overpotential depends on steps involving  $^*O$ , the solvation of which is completely neglected in the CSS approach.

Besides, the tops of the OER volcanoes are located at 2.7 (CSS) and 2.9 eV (MLS) and those of the ORR are found at 2.2 (CSS) and 1.9 eV (MLS). Therefore, in the CSS approach the separation between the OER and ORR maxima is only  $\sim 0.5$  eV, while it is nearly 1 eV in the MLS approach (see the black dashed lines in Fig. 6). These considerable differences are also due to the omission of  $^*O$  solvation and lead to different predictions of bifunctional active metal centers, as the OER/ORR tops are considerably closer in the CSS approach. In any case, Co centers

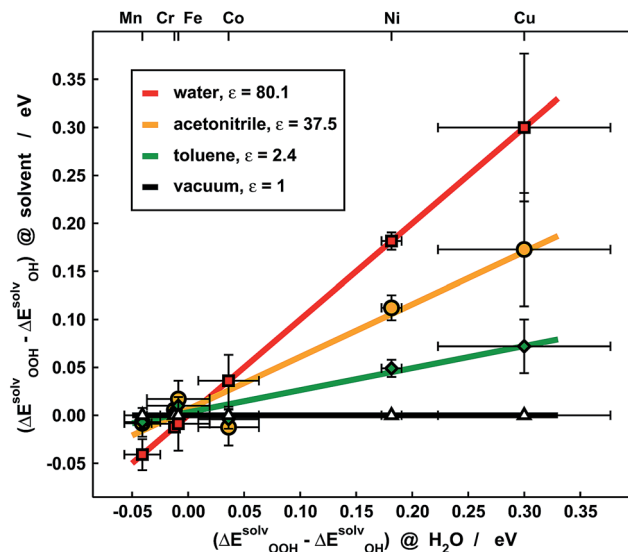


Fig. 7 Comparison between the loss of solvation of  $^*OOH$  with respect to  $^*OH$  in various solvents for porphyrins with  $-H$  and  $-F$  ligands. Data for water (red), acetonitrile (orange), toluene (green) and vacuum (black), where there is no solvation, are plotted as a function of those of water. Although the solvation losses are small for Cr, Mn, Fe and Co, they are substantial for Ni and Cu and depend on the solvent's dielectric constant. Solvents with small  $\epsilon$  such as toluene avoid the restoration of scaling relations broken under vacuum via high covalence.

with ligands such as  $CH_3$  and  $BH_2$  are predicted to have similarly low overpotentials for both reactions. Importantly, this observation also suggests that a significant decrease in adsorbate solvation could lead to OER/ORR bifunctionality.

## Conclusions

We have shown here that various metal centers and ring ligands can make metalloporphyrins break scaling relations, in particular those between the adsorption energies of  $^*OH$  and  $^*OOH$ , which are of importance for oxygen reduction and evolution. This shows that (1) flat sites made of a single metal species that binds  $^*OH$  and  $^*OOH$  similarly can indeed break scaling relations and (2) there is no need for the ligands to interact directly with the adsorbates in order to do so, which goes against commonly accepted ideas.<sup>10,11,26,32</sup> This stems from the fact that covalence is in this case the factor responsible for breaking scaling relations. However, the scaling broken under vacuum is restored in water by virtue of the loss of solvation caused by high covalence as well.

Methodologically speaking, this means that future studies aimed at breaking such relations in solution must take the solvent into account in the calculations. Although some examples exist, that is not a common practice in computational electrocatalysis.<sup>5,24</sup> For instance, the importance of the solvent's dielectric constant ( $\epsilon$ ) on the ORR activity of platinum has been recently pointed out by Fortunelli *et al.*<sup>33</sup> Moreover, other authors are making significant efforts to understand water solvation at pristine and stepped surfaces by including it





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