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Delocalisation enables efficient charge generation in organic photovoltaics, even with little to no energetic offset†

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Organic photovoltaics (OPVs) are promising candidates for solar-energy conversion, with device efficiencies continuing to increase. However, the precise mechanism of how charges separate in OPVs is not well understood because low dielectric constants produce a strong attraction between the charges, which they must overcome to separate. Separation has been thought to require energetic offsets at donor–acceptor interfaces, but recent materials have enabled efficient charge generation with small offsets, or with none at all in neat materials. Here, we extend delocalised kinetic Monte Carlo (dKMC) to develop a three-dimensional model of charge generation that includes disorder, delocalisation, and polaron formation in every step from photoexcitation to charge separation. Our simulations show that delocalisation dramatically increases charge-generation efficiency, partly by enabling excitons to dissociate in the bulk. Therefore, charge generation can be efficient even in devices with little to no energetic offset, including neat materials. Our findings demonstrate that the underlying quantum-mechanical effect that improves the charge-separation kinetics is faster and longer-distance hops between delocalised states, mediated by hybridised states of exciton and charge-transfer character.

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In organic photovoltaics (OPVs), understanding how charges overcome their large Coulomb attraction to separate efficiently has remained elusive.^{1–3} Due to the low dielectric constants in organic semiconductors ($\epsilon_r \approx 3$ –4), photoexcitation produces tightly bound excitons. To overcome the large exciton-binding energies and enable charges to separate, OPVs are made by blending donor and acceptor materials to form a heterojunction. At the donor–acceptor interface, the offset between the energy levels of the two materials produces a driving force to dissociate the exciton, resulting in one of the charges moving across the interface to form a slightly separated charge-transfer (CT) state. Nevertheless, charges in a CT state are still coulombically bound to each other with a strength more than an order of magnitude larger than the available thermal energy, an obstacle they must overcome to separate. The efficiency of the separation process is the internal quantum efficiency (IQE), the proportion of excitons that generate separated charges. The near-unity IQE in some OPVs has been attributed to delocalisation, with several groups observing efficient and fast separation of delocalised charges.^{4–9} The delocalisation enhancement has been attributed to a reduced electron–hole binding energy when the charges in a CT state delocalise and their separation increases. However, charge separation is a multi-step process,

and when disorder and entropy are considered, the free-energy barrier to separation disappears¹⁰ and actually increases when delocalisation is included,¹¹ indicating that delocalisation enhancements must come from non-equilibrium kinetic effects, rather than solely energetic ones.^{11,12} Therefore, a full kinetic model is required for studying the effects of delocalisation on charge separation. Significant progress has been made towards this goal, with many kinetic models including delocalisation and finding improved efficiencies.^{13–24} However, the computational difficulty of tracking the correlated motion of two quantum-mechanically delocalised charges limits these simulations to small systems or reduced dimensionality. Recently, we overcame this challenge to produce three-dimensional simulations of charge separation, finding that delocalisation enhancements to CT-separation efficiency are indeed a kinetic effect, with improved IQE even though delocalisation increases the binding energy.²⁵

Recent developments have further challenged conventional assumptions about the mechanism of charge generation. In particular, non-fullerene acceptors (NFAs) have produced efficient OPV devices^{26–28} without the large energetic offsets thought to be required for exciton dissociation.^{3,29,30} Explaining this observation is an outstanding theoretical challenge,³ with one hypothesis being that low offsets enable the formation of hybridised states with the character of both excitons and separated charges.^{31–34} Furthermore, experimental evidence suggests that delocalised and partially separated intermediate

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Fig. 1 Pathways of delocalised charge generation. (a) Charges in organic solar cells are usually assumed to separate via pathway A, interfacial charge generation: (A1) exciton diffuses to an interface where (A2) an energetic offset drives exciton dissociation into an interfacial CT state out of which (A3) charges separate. When excitons and charges become delocalised, they can separate more efficiently through pathway A, but also without an interfacial energetic offset via pathway B, bulk charge generation, where (B1) exciton dissociates and (B2) the charges separate within the single material. Delocalisation also enables pathway C, mixed charge generation: (C1) the exciton dissociates in the bulk, before (C2) the still-bound charges diffuse to the interface, where (C3) charge transfer occurs and (C4) the charges can separate in separate domains. (b) Classification of the types of site-pairs and the processes between them. (c) Classification of charge-generation pathways.

states form within NFA phases before reaching an interface,^{27,35–40} suggesting separation may not proceed through the typical pathway involving interfacial CT states. An even greater theoretical challenge is explaining the detection of free carriers in devices made of neat materials, where there is no interfacial energetic offset, including Y6.^{41–43}

Here, we show that delocalisation can enable efficient charge generation in OPVs with little or no energetic offset. To do so, we extend our delocalised kinetic Monte Carlo (dKMC) algorithm—which has already been used to show that delocalisation improves charge and exciton transport^{44,45} and the separation of charges from a CT state²⁵—to consider the full charge generation process, from excitons to separated charges. dKMC includes all of the essential ingredients: disorder, delocalisation, and polaron formation. We find that delocalisation produces large charge-generation improvements, especially in systems with little to no energetic offset, helping to explain the efficient low-offset and homojunction devices. The mechanism of the improved exciton dissociation is a kinetic, quantum effect: delocalised hops of greater speed and distance, mediated by hybridised states, allow separation to out-compete recombination. Overall, our findings support both of the hypotheses above, that delocalisation enables excitons to fully or partially separate in the bulk of one phase and that charge generation involves hybridisation of exciton and weakly bound states.

I. Methods

We begin by describing the dKMC model of charge generation. The details of the underlying quantum master equation, the approximations, and the full algorithm are in Secs. S1–S5 of the ESI.†

A. Model

We model an OPV heterojunction using a tight-binding model on a cubic lattice with lattice spacing a and N^d sites (molecules or parts of molecules), where N is the number of sites along each of d dimensions. The left $N^d/2$ sites represent the donor and the rest the acceptor (Fig. 2a). Every site is assigned a randomly oriented transition dipole moment μ_n with constant magnitude μ as well as HOMO and LUMO energies for a hole or an electron occupying that site, respectively.

Energetic disorder is modelled by drawing site energies from Gaussian distributions $\mathcal{N}(E_0, \sigma)$, centred on E_0 and with standard deviation σ measuring the disorder.⁴⁶ There are four distributions (Fig. 2): the donor HOMO energy centred at 0, the donor LUMO centred at E_g , the acceptor HOMO centred at $-E_{\text{offset}}^{\text{HOMO}}$, and the acceptor LUMO centred at $E_g - E_{\text{offset}}^{\text{LUMO}}$.

The energies drawn from these four distributions must be correlated to ensure that the exciton disorder is smaller than the electronic disorder. For uncorrelated LUMO and HOMO energies with disorders σ_{LUMO} and σ_{HOMO} and a constant exciton-binding energy E_b , the disorder in the exciton energy $E_{\text{xc}} =$



Fig. 2 dKMC model of charge separation. (a) A planar heterojunction is represented by a cubic lattice of donor (orange) and acceptor (blue) sites. Each site is coupled to its environment (motion lines) and is assigned a randomly oriented transition dipole moment μ and disordered HOMO and LUMO energies (different shades, see inset). There are nearest-neighbour electronic couplings J_e^c and J_h^c for electrons and holes and long-range exciton couplings J_{xc} . (b) Each eigenstate of the polaron-transformed system Hamiltonian describes the simultaneous wavefunction of the delocalised electron (blue) and hole (orange). The cartoon depicts the charges as separable, but they are correlated in reality. (c) Dynamics through the polaron states is propagated using dKMC, which tracks joint trajectories of both charges. After each hop, polaron states are re-calculated within the neighbourhood of the charges, outgoing rates (black arrows) are calculated to states within a cutoff distance (black circles), and the hopping destination is chosen probabilistically based on these outgoing rates.

$E_{\text{LUMO}}^{\text{LUMO}} - E_{\text{HOMO}}^{\text{HOMO}} - E_b$ would be $\sigma_{xc} = \sqrt{\sigma_e^2 + \sigma_h^2}$, which is larger than either electronic disorder. However, σ_{xc} should be less than σ_e and σ_h because local electrostatic variations shift HOMO and LUMO energies in the same direction (Fig. 2a). Therefore, we correlate the HOMO and LUMO energies to achieve a correlation $\rho = \text{Cov}(E_{\text{LUMO}}^{\text{LUMO}}, E_{\text{HOMO}}^{\text{HOMO}}) / (\sigma_{\text{HOMO}} \sigma_{\text{LUMO}})$, which gives $\sigma_{xc}^2 = \sigma_{\text{LUMO}}^2 + \sigma_{\text{HOMO}}^2 - 2\text{Cov}(E_{\text{LUMO}}^{\text{LUMO}}, E_{\text{HOMO}}^{\text{HOMO}})$. Assuming for simplicity that $\sigma = \sigma_{\text{LUMO}} = \sigma_{\text{HOMO}}$ leads to $\rho = 1 - \sigma_{xc}^2 / 2\sigma^2$, meaning that σ_{xc} can be chosen independently of σ . The correlated energies for the donor are drawn from the bivariate normal distribution

$$\begin{bmatrix} E_n^{\text{HOMO}} \\ E_n^{\text{LUMO}} \end{bmatrix} \sim \mathcal{N}\left(\begin{bmatrix} 0 \\ E_g \end{bmatrix}, \begin{bmatrix} \sigma^2 & \rho\sigma^2 \\ \rho\sigma^2 & \sigma^2 \end{bmatrix}\right), \quad (1)$$

while those for the acceptor are drawn in the same way, but shifted by $[-E_{\text{offset}}^{\text{HOMO}}, -E_{\text{offset}}^{\text{LUMO}}]$. Throughout this work, we assume $\sigma = 150$ meV and $\sigma_{xc} = 30$ meV, corresponding to $\rho = 0.98$.

As exciton dissociation is a two-particle problem, the Hilbert space is spanned by site-pairs $|m, n\rangle$, which describe an electron on site m and a hole on site n . In this basis, the system is described by the Hamiltonian

$$H_S = \sum_{m,n} E_{mn} |m, n\rangle \langle m, n| + \sum_{m \neq m', n} J_{mm'}^e |m, n\rangle \langle m', n| \\ + \sum_{m, n \neq n'} J_{nn'}^h |m, n\rangle \langle m, n'| + \sum_{o \neq o'} J_{oo'}^{xc} |o, o\rangle \langle o', o'|, \quad (2)$$

where the energy of a site-pair with electron-hole separation r_{mn} is $E_{mn} = E_m^{\text{LUMO}} - E_n^{\text{HOMO}} + U(r_{mn})$, including the Coulomb potential of

$$U(r_{mn}) = \begin{cases} -\frac{e^2}{4\pi\epsilon_0\epsilon_r r_{mn}} & \text{if } r_{mn} \neq 0 \\ -E_b & \text{if } r_{mn} = 0 \end{cases}, \quad (3)$$

where e is the elementary charge, ϵ_0 the vacuum permittivity, and ϵ_r the dielectric constant (here, $\epsilon_r = 3.5$).

Eqn (2) shows that site-pair $|m, n\rangle$ is coupled to other site-pairs $|m', n'\rangle$ in three cases. First, if only the electron is moving ($n = n'$), the two site-pairs are coupled by the electron coupling $J_{mm'}^e$. Second, if only the hole is moving ($m = m'$), they are coupled by the hole coupling $J_{nn'}^h$. We assume constant, nearest-neighbour J^e and J^h , but this assumption could easily be relaxed to allow for disordered or non-nearest-neighbour couplings. Third, if both site-pairs represent excitons ($m = n = o$ and $m' = n' = o'$), they are coupled by the long-range dipole-dipole coupling $J_{oo'}^{xc} = \xi_{oo'} \mu^2 / 4\pi\epsilon_0 |\mathbf{r}_{oo'}|^3$, where the distance

vector between o and o' is $\mathbf{r}_{oo'}$ and the orientation factor is $\xi_{oo'} = \hat{\boldsymbol{\mu}}_o \cdot \hat{\boldsymbol{\mu}}_{o'} - 3(\hat{\mathbf{r}}_{oo'} \cdot \hat{\boldsymbol{\mu}}_o)(\hat{\mathbf{r}}_{oo'} \cdot \hat{\boldsymbol{\mu}}_{o'})$, with hats indicating unit vectors.

The environment is modelled as an independent bath of harmonic oscillators on each site,^{47,48}

$$H_B = \sum_{m,k} \omega_{mk} b_{mk}^\dagger b_{mk}, \quad (4)$$

where ω_{mk} is the frequency of the k th mode on site m , with creation and annihilation operators b_{mk}^\dagger and b_{mk} .

The interaction between the system and the environment is modelled as a linear coupling of each site to each of its bath

modes, with separate coupling strengths for electrons g_{mk}^e , holes, and excitons g_{mk}^{xc} ,

$$H_{SB} = \sum_{m,n \neq m,k} g_{mk}^e |m,n\rangle \langle m,n| (b_{mk}^\dagger + b_{mk}) + \sum_{m,n \neq m,k} g_{nk}^h |m,n\rangle \langle m,n| (b_{nk}^\dagger + b_{nk}) + \sum_{o,k} g_{ok}^{xc} |o,o\rangle \langle o,o| (b_{ok}^\dagger + b_{ok}). \quad (5)$$

Crucial to OPVs is the formation of polarons, quasi-particles consisting of charges or excitons dressed by the induced distortion in the environment.^{49,50} Polarons are incorporated using the polaron transformation⁵¹

$$e^S = \exp \left(\sum_{m,n \neq m,k} \frac{g_{mk}^e}{\omega_{mk}} |m,n\rangle \langle m,n| (b_{mk}^\dagger - b_{mk}) + \sum_{m,n \neq m,k} \frac{g_{nk}^h}{\omega_{nk}} |m,n\rangle \langle m,n| (b_{nk}^\dagger - b_{nk}) + \sum_{o,k} \frac{g_{ok}^{xc}}{\omega_{ok}} |o,o\rangle \langle o,o| (b_{ok}^\dagger - b_{ok}) \right), \quad (6)$$

which displaces bath modes and transforms the entire Hamiltonian ($H = H_S + H_B + H_{SB}$) into the polaron-transformed version, $\tilde{H} = e^S H e^{-S} = \tilde{H}_S + \tilde{H}_B + \tilde{H}_{SB}$, given in Sec. S1 of the ESI.†

B. Polaron states

The polaron states are the eigenstates of the polaron-transformed system Hamiltonian \tilde{H}_S and represent the simultaneous state of the delocalised electron and hole in the polaron frame (Fig. 2b).

The polaron transformation leads to spatially smaller states, which are computationally more manageable. This occurs because the transformation decreases the electronic couplings, reducing eigenstate delocalisation.⁵² We quantify the delocalisation of a polaron state $|\nu\rangle$ using the inverse participation ratio (IPR)

$$\text{IPR}_\nu = \left(\sum_{m,n} |\langle m,n|\nu\rangle|^4 \right)^{-1}, \quad (7)$$

a measure of how many site-pairs $|m,n\rangle$ the polaron state is spread across. The extent of delocalisation is determined by the parameters in the model: electronic couplings and transition dipole moments increase IPRs, while disorder and system-bath coupling decrease them.

We classify the polaron states into categories based on their overlaps with the different types of site-pairs shown in Fig. 1b: exciton site-pairs, bound site-pairs (which are either CT site-pairs or weakly bound site-pairs), and separated site-pairs. Every polaron has an overlap with each of these types of site-pairs; for example, the exciton character of polaron $|\nu\rangle$ is $\sum_o |\langle o,o|\nu\rangle|^2$ and its separated-charge character is $\sum_{m,n} |\langle m,n|\nu\rangle|^2$, where the sum goes over site-pairs $|m,n\rangle$ in



Fig. 3 Delocalised polaron states. Energy \tilde{E} and electron–hole separation r_{eh} of polaron states of a representative \tilde{H}_S for (a) small couplings and dipole moments ($J = 1.5$ meV, $\mu = 1$ D) and (b) large ones ($J = 67.5$ meV, $\mu = 10$ D). States are classified based on which type of site-pair they overlap with the most and whether the electron and the hole in those site-pairs are predominantly in the bulk (same phase) or in separate phases. The two bands of separate-phase states correspond to whether the electron is in the donor and the hole in the acceptor or vice versa. For small couplings, the states are localised to about one site-pair centred on the lattice, with no hybridised states forming. When the couplings are larger, states become delocalised, are no longer centred on the lattice, and can be hybridised, with both exciton and non-exciton character. All results are in 2D for $E_{\text{offset}}^{\text{LUMO}} = E_{\text{offset}}^{\text{HOMO}} = 500$ meV, and the other simulation parameters are in Sec. S6 of the ESI.†

which the electron–hole separation exceeds $r_{\text{sep}} = 5$ nm. We classify the polaron states by which type of site-pair they overlap with the most. For example, exciton states have most of their population on exciton site-pairs. In addition, a state is hybridised if it has more than 25% of its population on both exciton and non-exciton site-pairs.

Fig. 3 shows the polaron states found by diagonalising a representative \tilde{H}_S . At small electron–hole separations, the Coulomb attraction is largest, reducing the energy of the states. For small couplings (Fig. 3a), each state is approximately a site-pair, meaning they are localised close to the lattice. However, for higher couplings (Fig. 3b), the states become delocalised and are no longer centred close to the lattice. Furthermore, a significant number of hybridised states only forms in the higher-couplings case. The IPRs of the states as a function of energy are included in Sec. S7 of the ESI.†

C. dKMC dynamics

dKMC propagates the dynamics through hops among the partially delocalised polaron states (Fig. 2c). The polaron transformation allows a perturbative treatment of the dynamics by moving most of the system–bath interaction into the polaron itself. As a result, the polaron interacts relatively weakly with its environment and this remaining coupling can often be treated perturbatively.⁵¹ Treating the perturbation to second order leads to the secular polaron-transformed Redfield master equation (sPTRE)⁵³ for transition rates between polaron states, as described in Sec. S2 of the ESI.† dKMC is a kinetic Monte Carlo procedure that tracks (and subsequently averages over) individual trajectories through the polaron states using sPTRE rates, in a similar way to how standard KMC uses Marcus or Miller–Abrahams rates to track classical trajectories across sites. The details are given in Secs. S3–S5 of the ESI.†

Initialisation. We begin a dKMC simulation by generating a disordered energetic landscape and randomly oriented dipoles on each site. Next, we choose the initial exciton state. This involves selecting an excitation location by randomly choosing a point whose distance from the interface is between 1 site and $d_{\text{xc}}^{\text{max}}$ (here 5 nm, motivated by typical domain sizes of 10 nm). Second, we diagonalise a subset of \tilde{H}_S that describes a neighbourhood of the selected excitation location that is large enough to contain the states the initial exciton is likely to hop to (Fig. 2c). The size of the neighbourhood is calibrated to ensure accuracy as described previously⁴⁵ and in Sec. S3 of the ESI.† Finally, the initial exciton state is chosen at random among exciton states centred within 1 nm of the excitation location, and in proportion to their oscillator strengths, which describe the probability that they would be excited by light.

Propagation. After initialisation, the dynamics is propagated through the polaron states using the dKMC procedure, as detailed in Sec. S5 of the ESI.† At each step, we calculate the outgoing hopping rates from the current polaron state. To do so, we only consider hops to states within a certain distance, allowing for different distances for charge and exciton hops. These cutoffs are calibrated as described previously⁴⁵ and in Sec. S3 of the ESI.†

At each step, the polaron state can also recombine due to its overlap with exciton site-pairs or CT site-pairs. The expressions for

these rates are given in Sec. S4 of the ESI,† and take the form of constant recombination rates modified by the square of amplitudes on site-pairs that can recombine, as in previous work.^{25,54,55}

As in KMC, one hopping destination (including recombination) is chosen probabilistically in proportion to the size of the corresponding rates. The current state and the elapsed time are updated, before diagonalising a new subset of \tilde{H}_S , centred on the new state.

Termination. The delocalised hopping is repeated until the charges either separate or recombine. The condition for separation is that the expectation value of the electron–hole separation, $|\langle \nu | \mathbf{r}_e | \nu \rangle - \langle \nu | \mathbf{r}_h | \nu \rangle|$, exceeds $r_{\text{sep}} = 5$ nm. For numerical purposes, we also impose a cutoff in the maximum number of hops, n_{hops} , to prevent infinite loops between, for example, two low-lying traps. This cutoff is chosen to be sufficiently large so that no more than 5% of trajectories exceed the cutoff, a tolerance that could be reduced by increasing n_{hops} .

The complete algorithm above is repeated for n_{traj} trajectories and on n_{iters} realisations of disorder. These numbers determine the uncertainty of the calculations and, in our calculations, are chosen so that the standard error of the mean in IQE calculations is never more than 2 percentage points (the values are listed in Sec. S6 of the ESI).† Finally, the IQE is calculated as the proportion of trajectories that separate.

D. Pathways of delocalised charge generation

As a framework for analysing our results, we describe the three pathways for charge generation, illustrated in Fig. 1. Charge generation is the full conversion of excitons into separated charges, and can be divided into two steps (Fig. 1b). Exciton dissociation, involves an exciton dissociating into a bound state, either a CT state or a weakly bound state. After that, charge separation is the separation of a bound state into separated charges.

Both steps—exciton dissociation and charge separation—can occur using the interface or entirely in the bulk of a single phase. The combinations of these possibilities lead to the three charge-generation pathways in Fig. 1a. Interfacial charge generation (pathway A) is the conventional pathway involving interfacial exciton dissociation and interfacial charge separation, *i.e.*, the exciton dissociates at the interface and the charges then separate in the different phases. In bulk charge generation (pathway B), both the exciton dissociation and the charge separation occur in the same phase. Finally, mixed charge generation (pathway C) involves bulk exciton dissociation followed by interfacial charge separation. A combination involving interfacial exciton dissociation and bulk charge separation is not possible because interfacial exciton dissociation yields charges on different sides of the interface, whose separation cannot occur in the bulk of one phase.

II. Results and discussion

A. Delocalisation increases the IQE

To determine the effect of delocalisation on charge generation, we compare the IQE predicted by dKMC (which includes delocalisation) to that predicted by standard KMC (which does





Fig. 4 Delocalisation enhances charge generation. (a and b) IQE of charge generation predicted by KMC (blue) and dKMC (orange) as a function of electronic coupling J and transition dipole moment μ in (a) 2D and (b) 3D. As J and μ increase, and the charges and excitons become more delocalised, the IQE predicted by dKMC increases compared to KMC, showing that both charge and exciton delocalisation improve charge generation, increasing the IQE by up to $5\times$ in 2D, and $3\times$ in 3D. (c and d) For a slice of the 2D and 3D results, indicated by the red dashed line in (a and b), the IQE is split into additive contributions due to trajectories where charges separate across the interface (pathways A and C) and trajectories where they separate entirely in one phase (pathway B). In both 2D and 3D, delocalisation both helps charges separate across the interface and enables them to separate in the bulk, without the assistance of interfacial energetic offsets. We set $E_{\text{offset}}^{\text{LUMO}} = E_{\text{offset}}^{\text{HOMO}} = 500$ meV and the other simulation parameters are in Sec. S6 of the ESI.† The error bars are the standard errors of the mean (see text for details).

not include it). KMC results are calculated for localised charges hopping between sites using a Marcus-theory rate,⁵⁶ which is the localised limit of charge transport reproduced by dKMC in the correct regime (*e.g.*, weak inter-site coupling or strong system-bath coupling). Fig. 4a and b shows the two IQEs as a function of the electronic coupling J and the transition dipole moment μ ; these parameters independently increase the delocalisation of charges and excitons (other parameters being fixed), allowing the effect of charge and exciton delocalisation to be independently assessed. At small J and μ , the IQEs predicted by dKMC and KMC agree, as expected in the limit of localised states. As J and μ increase, the IQE predicted by dKMC increases compared to classical KMC, demonstrating that both charge and exciton delocalisation improve charge generation. Over our parameter ranges, we see up to a $5\times$ enhancement in 2D, and as much as $3\times$ in 3D, despite the more modest J and μ .

The surfaces in Fig. 4, as well as our other results, are not perfectly monotonic due to the stochastic nature of the simulations, which require averaging over n_{traj} trajectories on each of n_{iters} realisations of disorder. Error bars in figures provide the standard errors of the mean in each case, and could be reduced by increasing n_{traj} and n_{iters} . With the current choices of n_{traj} and n_{iters} , the standard errors of the mean in IQE calculations were less than 2 percentage points.

B. Delocalisation enables charge generation without energetic offsets

Delocalisation enhances the IQE both by enhancing charge generation involving the interface and by enabling charge generation in the bulk of a single phase. In Fig. 4c and d, we split the IQE into contributions due to interfacial charge separation—trajectories that separate across the interface, so that the electron and hole are on opposite sides (pathways A and C)—from those due to bulk charge separation—trajectories that separate completely in one phase, with the electron and hole on the same side of the interface (pathway B). As J increases and the charges become more delocalised, dKMC predicts an enhancement in the number of trajectories separating across the interface compared to KMC (up to $3\times$ in 2D and $2\times$ in 3D for our parameter choices), demonstrating that both charge and exciton delocalisation are beneficial at improving interfacial charge separation. However, Fig. 4c and d reveals that delocalisation also enables charges to separate in the bulk of one phase *via* pathway B, *i.e.*, without the assistance of an interfacial energetic offset. In both 2D and 3D, KMC predicts a negligible bulk-separation IQE, as expected for localised charges, which struggle to overcome the exciton binding energy without the interfacial energetic offset providing a driving force. However, as J increases and the states become delocalised, dKMC shows





Fig. 5 Delocalisation enables charge generation without energetic offsets. IQE of charge generation in a homojunction (no interfacial energetic offset) predicted by KMC (blue) and dKMC (orange) as a function of the electronic coupling J and transition dipole moment μ in (a) 2D (b) and 3D. Both charge and exciton delocalisation improve the efficiency, especially in 3D. Simulation parameters are in Sec. S6 of the ESI,[†] except that $E_{\text{offset}}^{\text{LUMO}} = E_{\text{offset}}^{\text{HOMO}} = 0$.

that excitons are able to separate efficiently within a single material, especially in 3D. Compared to KMC, there is an enhancement of up to $47\times$ in 2D and already $12\times$ in 3D for the smaller J and μ . Therefore a large proportion of delocalised charge generation occurs in the bulk without the assistance of an interfacial offset.

Indeed, delocalisation enables efficient charge generation even in a single phase (a homojunction), without energetic offset to assist in separation. Fig. 5 shows the IQE for a homojunction, with KMC again unable to predict efficient separation at any J and μ . However, when the states are delocalised, at high J and μ , dKMC predicts considerable IQEs, with enhancements of $48\times$ in 2D, and already $11\times$ in 3D for modest J and μ . This demonstration that delocalisation can enable charge generation in a homojunction could explain observations of charge generation in neat Y6.^{35,41,43}

C. Energetic offsets are still beneficial for delocalised charge generation

Of course, interfacial energetic offsets are beneficial even with delocalisation because they can still drive interfacial charge separation. Fig. 6 shows heterojunction IQEs for varying LUMO offset, finding that for KMC to predict significant charge generation, a large offset is required. By contrast, dKMC



Fig. 6 Interfacial energetic offsets remain beneficial with delocalisation. IQE predicted by KMC (blue dots) and dKMC (orange dots) in 2D. Dashed lines are the contributions to the IQE from trajectories where charges separate across the interface (pathways A and C) and dotted lines are contributions from trajectories that separate in the bulk (pathway B). With KMC, large energetic offsets are required to see significant charge generation. By contrast, with dKMC, delocalisation enables charge generation in the bulk without interfacial energetic offsets. However, even though the interface is not required, it still improves interfacial charge generation by providing a driving force to dissociate excitons and by further separating states that have dissociated in the bulk but not fully separated. We set $J = 45$ meV, $\mu = 5$ D, $E_{\text{offset}}^{\text{HOMO}} = 500$ meV, and the other simulation parameters are in Sec. S6 of the ESI.[†] The error bars are the standard errors of the mean (see text for details).

predicts charge generation at all offsets, including small ones and even zero (as in the homojunctions above), a finding that could help explain efficient low-offset NFA devices.^{3,29,30}

However, Fig. 6 also shows that driving forces are still helpful for delocalised charge generation by improving separation across the interface. This improvement arises for two reasons.

First, as in conventional theories, an energetic offset helps dissociate excitons that would otherwise recombine in the bulk. Our results share another feature of classical theories based on Marcus theory, the inverted regime at very high offsets, where the transition is so far energetically downhill that the charge-transfer rates across the interface decrease.

The second benefit of the offset, which is not seen in conventional theories, is enabling mixed charge generation (pathway C in Fig. 1). Mixed charge generation occurs when an exciton dissociates in the bulk to a bound state without fully separating, and the bound state then uses an interface for the charges to separate completely. Our finding that delocalisation enables mixed charge generation supports the hypothesis of delocalised, partially separated intermediate states forming in single domains before they reach the interface.^{27,35–40}

D. Mechanism of delocalisation enhancements

Microscopically, the enhancements above arise because delocalisation enables longer and faster hops, which can bypass CT states and involve hybridised states instead. To see this, we note that delocalisation can improve overall charge generation by enhancing either the exciton-dissociation or the charge-separation steps in Fig. 1b. Previously, we described that delocalisation benefits charge separation by increasing the overlaps between states to





Fig. 7 The mechanism of delocalisation enhancement of exciton dissociation. Delocalisation enables charges to hop further and faster out of an exciton, allowing them to skip CT states and use hybridised states. (a) As delocalisation increases with electronic coupling J and transition dipole moment μ , charges hop further out of the exciton. Shown is the mean electron–hole separation in the first state following exciton dissociation. (b) Excitons dissociate faster with delocalised states, as shown by the rate of the exciton dissociation event. (c) Because of longer-range hopping, the fraction of separated trajectories that skip CT states increases with the couplings. (d) By skipping CT states, trajectories that are more delocalised can avoid large downhill hops, meaning they are less likely to become trapped in low-energy CT states. Shown is the average energy lost during the exciton dissociation event. (e) As couplings increase, and states become more delocalised, the character of the first bound state following exciton dissociation changes from CT state to weakly bound state. Shown are the mean populations of this state on CT and weakly bound site-pairs. (f) With stronger couplings, exciton dissociation is more likely to involve a hybridised state. Shown is the fraction of separated trajectories where exciton dissociation involves a state with more than 25% of both exciton and non-exciton character. All results are in 2D for $E_{\text{LUMO}}^{\text{offset}} = E_{\text{HOMO}}^{\text{offset}} = 500$ meV, and the other simulation parameters are in Sec. S6 of the ESI.†

kinetically assist charges in overcoming their Coulomb attraction.²⁵ And once separated, delocalised charges are more easily extracted because the longer and faster hops increase their mobilities.⁴⁴ Having extended dKMC to include excitons, we can now show that delocalisation benefits exciton dissociation in the same way, by accelerating long-distance hopping.

To understand the delocalisation enhancement of exciton dissociation, we study the exciton–dissociation event, the last hop in each trajectory out of an exciton state and into a non-exciton one. To do so, we identify trajectories where charges have separated, find the hop where the state character changed from predominantly exciton to non-exciton, and then analyse the two states immediately before and after the hop. In the following analysis, we study both types of exciton–dissociation events—at the interface and in the bulk—together, as the mechanism by which delocalisation improves them is the same (see Sec. S8 of the ESI).†

Delocalised charges hop further out of an exciton during dissociation (Fig. 7a) and they do so faster (Fig. 7b). Fig. 7a shows that when charges are localised, or when classical KMC is used, the separation after leaving an exciton state is 1 lattice spacing, as expected for charges forming a tightly bound CT state. For dKMC, as the states become more delocalised with increasing couplings, the charges can hop further out of the exciton state, causing r_{eh} to exceed 1 lattice spacing. The ability to hop further provides the additional benefit of more possible hopping destinations, which can be important in disordered materials and when dissociating an exciton in systems with little or no energetic offset. The larger overlaps between delocalised states also increase the speed of individual hops, allowing for faster hopping out of the exciton state (Fig. 7b).

The longer hopping distance means that charges departing exciton states can often skip CT states, as shown by the proportion of separating trajectories that skip CT states in Fig. 7c. Because CT states tend to be tightly bound, skipping them means that a trajectory can avoid deeply downhill hops, which risk trapping it in a low-energy CT state. As shown in Fig. 7d, the average energy lost upon hopping out of an exciton is indeed less for more delocalised states.

The enhancements above are facilitated by strong couplings, which also change the character of the states involved. As the delocalised charges hop further, the first separated state has less CT character and more weakly bound character, as shown in Fig. 7e. Indeed, the strong couplings cause the formation of hybridised states, whose prevalence increases for more delocalised states (Fig. 7f). This result supports the hypothesis that hybridisation is involved in delocalised charge separation.^{31–34}

E. Outlook

Our results are the first three-dimensional simulations of charge generation that include disorder, delocalisation, and polaron formation. They are possible because dKMC reduces the computational cost of sPTRE by as much as 54 orders of magnitude (see Sec. S3 of the ESI).†

dKMC is a general method, and our concrete parameter choices could easily be altered. For example, we assumed isotropic couplings J^c and J^h for concreteness, but they could be made anisotropic to simulate, say, stronger couplings along polymer chains. Similarly, site energies could be arranged to simulate morphologies other than the bilayer.



However, three-dimensional dKMC remains limited by its computational complexity to moderate couplings and transition dipole moments (see Fig. 4 and 5). Future work may extend these calculations using further simplifications to dKMC, such as jKMC.⁵⁷

Furthermore, dKMC is limited by approximations in the underlying sPTRE, which could be relaxed if necessary, albeit at increased computational expense. For example, sPTRE is accurate in the regimes studied here,^{53,58} but can become inaccurate for systems weakly coupled to slow baths.⁵⁸ To treat such systems, the full polaron transformation could be replaced with a variational version.^{59,60} The secular approximation ignores coherences, which is ordinarily valid because sunlight does not induce coherences^{61–68} and even if they were induced otherwise, they would not survive on charge-transport timescales. However, if required, coherences could be tracked at additional computational expense by not making the secular approximation and tracking the entire density matrix. Finally, sPTRE uses a local system-bath coupling, as is relevant for disordered molecular systems,⁴⁸ but to treat organic crystals, non-local system-bath couplings may need to be included to describe the fluctuations of electronic couplings.^{69–71}

We expect that using dKMC in multiscale simulations could enable a full device model that incorporates delocalisation. This would involve parameterising dKMC using atomistic simulations, such as molecular mechanics followed by electronic-structure calculations. The results of dKMC could then parameterise drift-diffusion models for computing device properties. We also expect that dKMC can be extended to model other fundamental processes in organic devices, such as singlet fission, which is theoretically similar to charge generation.

III. Conclusion

Extending dKMC to the full charge-separation process, from excitons to separated charges, explains observations of efficient charge separation in disordered OPVs, especially those with little to no energetic offset. dKMC reveals that delocalisation produces large IQEs compared to those predicted by classical KMC. Delocalisation does so by enabling separated charges to be generated in the bulk and by enabling charges to hop faster and further out of an exciton during dissociation, mediated by hybridised states. Together with past dKMC studies, our results show that delocalisation accelerates all the fundamental processes in organic electronics—charge transport,⁴⁴ exciton diffusion,⁴⁵ charge separation,²⁵ and exciton dissociation (this work)—in essentially the same way, by allowing polaron states to hop further and faster. We anticipate that this new mechanistic understanding of charge generation in OPVs will explain the performance of efficient low-offset heterojunctions and neat devices and help design more efficient future ones.

Data availability

All data needed to evaluate the conclusions in the paper are present in the paper.

Author contributions

D. B. developed the theory, carried out the calculations, analyzed the data, and wrote the manuscript. Both authors conceived the project idea and edited the manuscript.

Conflicts of interest

There are no conflicts of interest to declare.

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