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Suppressing vanadium crossover using sulfonated aromatic ion exchange membranes for high performance flow batteries†

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Liquid flow batteries have potential to achieve high energy efficiency as a large-scale energy storage system. However, the ion exchange membranes (IEMs) currently used in flow batteries do not have high ion selectivity and conductance at the same time, owing to the trade-off between ionic membrane resistance and ion selectivity. Here, we report a rationally designed sulfonated aromatic polymer membrane which can greatly mitigate the trade-off limitation and achieve high performance vanadium RFB. Small-angle X-ray scattering studies and density functional theory calculations indicated that the narrowly distributed aqueous ionic domain of just the right width (<7 Å) and the strong hydrogen bond interaction of vanadium species with a unique polymer side chain structure play a key role in improving the ion selectivity. Our systematic studies of the polymer structures, morphologies, and transport properties provide valuable insight that can aid in elucidating the structure–property relationship of IEMs and in establishing design criteria for the development of high-performance membranes.

Introduction

Membrane-based electrochemical devices have shown great potential for use in many next-generation energy conversion and storage systems, such as fuel cells,¹ redox flow batteries,^{2,3} and reverse electrodialysis,⁴ owing to their high energy efficiency and large-scale adaptability. For a broader application of these technologies, ion exchange membranes (IEMs) with high

ion conductivity and selectivity properties are critical for enhancing the electrochemical performance of electrolyte cells. Conventional polymeric IEMs, however, suffer from the trade-off between ion conductivity (membrane resistance) and selectivity of co/counter-ions and fuels, which greatly reduces the efficiency of energy conversion and storage systems.^{5,6}

Among energy storage systems, vanadium redox flow batteries (VRFBs) have been recognized as one of the most promising technologies for grid-scale energy storage, owing to excellent design flexibility and safety, benefited from their decoupled energy storage and power generation.^{7–11} By using vanadium ions as the active species in both catholyte and anolyte solutions, VRFBs eliminate the risk of detrimental cross-contamination effects, thus greatly improving their service life.^{12,13} As a key component in VRFBs, IEMs should have low vanadium permeability for the separation of the vanadium species in the catholyte and anolyte solutions while allowing selective transport of charge-carrier ions with high ionic conductivity.¹⁴ Unfortunately, most of the cation exchange membranes (CEMs) do not meet these criteria, owing to their intrinsic trade-off between proton conductance and the selectivity of protons over vanadium ions (H^+/V^{n+}), thus hampering the widespread implementation of VRFBs. For instance, although Nafion[®], a perfluorosulfonated polymer CEM, is commonly used in VRFBs because of its high proton conductivity, chemical stability, and commercial availability, the high vanadium permeability of the Nafion[®] membrane causes undesired coulombic efficiency (CE) drop and fast capacity decay.^{14–16} To minimize the crossover of vanadium ions, a thicker Nafion membrane (e.g., Nafion 117) has to be employed at the expense of higher membrane resistance, raising the VRFB stack cost. Currently, Nafion membranes account for 40% of the total cost of a VRFB cell stack.¹⁷ To overcome the limitations of Nafion membranes, extensive efforts have been made to improve ion selectivity by introducing ion selective surface coatings¹⁸ or inorganic fillers, such as SiO_2 ,¹⁹ TiO_2 ,²⁰ and ZrO_2 .^{21,22} Although the modified Nafion membranes show

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a suppressed vanadium permeability, the additives can cause adverse effect of higher cell resistance, which does not help to overcome the trade-off limitation.¹⁴ Alternatively, hydrocarbon-based anion exchange membranes (AEMs)²³ have been investigated for VRFBs because of their cation (e.g. vanadyl cation) exclusion effect (Donnan exclusion). However, in highly concentrated electrolytes of VRFBs (typically ≥ 3 M), the Donnan exclusion effect is weak and cannot compensate for the lower ion conductivity of typical AEMs compared to Nafion. As a consequence, the decrease in voltage efficiency (VE) and energy efficiency (EE) makes AEMs less appealing for VRFB applications at high current densities.²⁴ Recently, a polyamide thin-film composite membrane exhibited an EE of VRFB greater than 80% at 260 mA cm⁻² by optimizing the thickness of the polyamide selective layer.²⁵ However, the polyamide membrane still exhibits the trade-off limitation. Furthermore, the amide bonds in polyamide are known to be susceptible to hydrolysis which could result in stability issues under strong acidic conditions.²⁶ Therefore, for deployment of durable, high-performance VRFB systems, the design and fabrication of advanced IEMs, which can overcome the intrinsic trade-off limitations, *via* the optimization of various parameters at molecular levels (e.g. ionic group, ion exchange capacity, and aqueous ionic domain width) is highly critical.

In this paper, we report a novel class of sulfonated aromatic polymer CEMs and demonstrate their superior battery performance in achieving both high VE and high CE and overcoming the trade-off limitation barrier of IEMs. To establish the relationship between the molecular structures and the selective ion transport properties, we rationally designed a series of polymers composed of a biphenyl backbone with different side chains (Fig. 1a). Among the polymers investigated, the biphenyl polymer with the longest side chain containing an additional aromatic ring and a perfluorinated segment (**BP-ArF4** of Fig. 1a) exhibited good proton conductivity while also maintaining extraordinary high proton/vanadium ion selectivity. The unique feature of this ionic polymer includes a hydrophobic/hydrophilic separation on a small length scale typical of hydrocarbons with a high degree of order and the super-acidity characteristic typical of perfluorosulfonate ionomers. The unique combination of these characteristics affords **BP-ArF4** a remarkable battery performance (CE \sim 99%, EE up to 93.9%) exceeding that of all other IEMs in VRFB applications. Small-angle X-ray scattering (SAXS) and density functional theory (DFT) calculations provide a semi-quantitative understanding of the observed performance.

Results and discussion

Polymer synthesis and characterization

As shown in Fig. S1 (ESI[†]), three examples of cation exchange polymers (**BP-SA**, **BP-ArSA**, and **BP-ArF4**) were prepared from the biphenyl polymer precursor BPBr-100, which has a bromoalkyl group on the side chain. For **BP-SA**, the brominated side chain of the precursor polymer was replaced with $-\text{SO}_3\text{H}$,

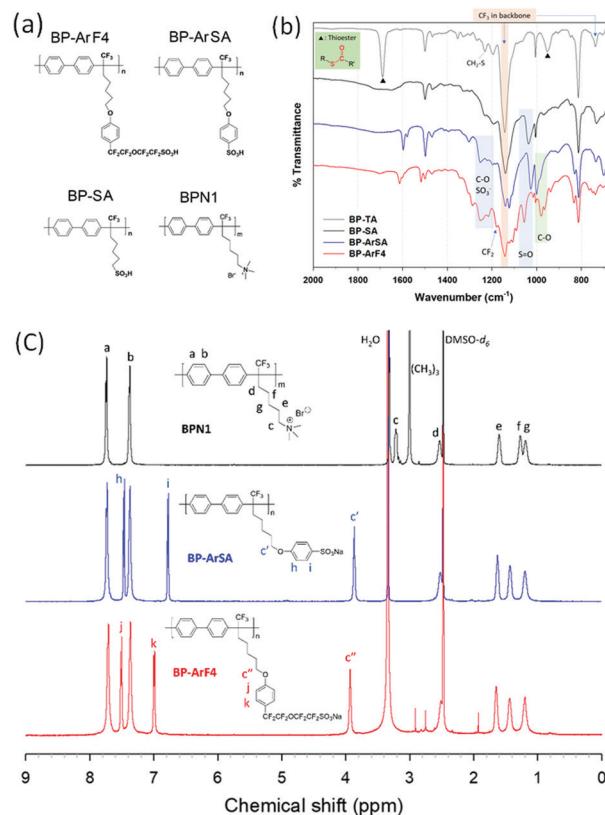


Fig. 1 Chemical structures and FT-IR spectra of the synthesized polymers. (a) Chemical structures of the polymers. (b) FT-IR spectra of the synthesized **BP-TA** (gray) and cation exchange polymers: **BP-SA** (black), **BP-ArSA** (blue), and **BP-ArF4** (red). (c) ¹H NMR spectra ($\text{DMSO}-d_6$) of the synthesized polymers: **BPN1** (black), **BP-ArSA** (Na salt form, blue), and **BP-ArF4** (red; the peaks at 1.96, 2.78, and 2.94 ppm are from residual DMAc solvent casting).

and it has the shortest side chain, with a flexible $-(\text{CH}_2)_5-$ spacer between the backbone and sulfonate group, among the three investigated CEMs. **BP-ArSA** has an additional aromatic ring in the sulfonate side chain, while **BP-ArF4** contains a perfluoroalkylsulfonate group in addition to an aromatic ring in the side chain. As all three sulfonated polymers share the same biphenyl backbone structure and were prepared from the precursor polymer BPBr-100, they should have no difference in molecular weight. The difference in properties of these polymers should be derived only from the side chain structures. Through the minor differences in the side chain structures, we studied how they could impact ion conductivity and vanadium ion permeability, which can be translated to battery efficiencies. We also prepared **BPN1**, an AEM counterpart of **BP-SA**, from BPBr-100 to study the effect of sulfonate *vs.* quaternary ammonium side chains on membrane properties and battery performance.

Because **BP-SA** has poor solubility in organic solvents, **BP-SA** membranes were prepared by the oxidation of **BP-TA** film (Fig. S1, ESI[†]). **BP-TA** was prepared *via* a nucleophilic substitution reaction of BPBr-100 and potassium thioacetate; whereafter, it was cast into a film and immersed in a hydrogen



peroxide solution for the oxidation of $-\text{SC}(=\text{O})\text{CH}_3$ of **BP-TA** to $-\text{SO}_3\text{H}$ of **BP-SA**.²⁷ Successful conversion to a sulfonic acid group in **BP-SA** was confirmed using FT-IR spectroscopy and titrated ion exchange capacity (IEC) (Fig. 1b), in which the thioester $\text{S}-(\text{C}=\text{O})-\text{C}$ stretching bands of **BP-TA** at 1690 and 952 cm^{-1} disappeared, and the $\text{S}=\text{O}$ stretching bands of $-\text{SO}_3\text{H}$ in **BP-SA** were clearly visible at 1200 and 1037 cm^{-1} . **BP-ArSA** was synthesized using a one-step nucleophilic substitution of **BP-Br** with sodium 4-hydroxybenzenesulfonate, as shown in Fig. S1 (ESI[†]). Because **BP-ArSA** (in $-\text{SO}_3\text{Na}$ form) is soluble in DMSO, the chemical structure of **BP-ArSA** was confirmed using ¹H NMR and FT-IR spectroscopies (Fig. 1c). In addition to $\text{S}=\text{O}$ stretching bands at 1220 and 1026 cm^{-1} , C–O stretching bands were observed at 1252 and 1000 cm^{-1} in the FT-IR spectrum. To synthesize **BP-ArF4**, we first synthesized **BP-Ar-I** via the nucleophilic substitution of **BPBr-100** with 4-indophenol and then subjected the aryl iodide in the polymer pendant chain to Ullmann coupling reaction with compound **1** (Fig. S1, ESI[†]). Structural characterization of **BP-ArF4** was confirmed using ¹H and ¹⁹F NMR (in $-\text{SO}_3\text{Na}$ form) and FT-IR (in $-\text{SO}_3\text{H}$ form) spectroscopies (Fig. S1 and S3, ESI[†]). The FT-IR spectrum showed the presence of $-\text{SO}_3\text{H}$ ($\text{S}=\text{O}$ stretching bands at 1216 and 1056 cm^{-1}), aryl ether bonds (C–O stretching bands at 1251 and 1090 cm^{-1}), and a perfluoroalkyl ether moiety (CF_2-O stretching at 980–960 cm^{-1}). **BPN1** was prepared by following the procedure mentioned in our previous report.²⁸

Ion transport properties

To characterize the ion transport properties of the membranes, we evaluated the IEC, vanadium ion permeability, proton conductivity, and area resistance of the prepared membranes (Table 1). Commercial Nafion 117 and Nafion 212 membranes, which are widely used in VRFBs, were used as reference samples. Low vanadium ion crossover is a critical property of IEMs to achieve high CE and low capacity loss for VRFB applications. Among all evaluated CEMs, **BP-SA** showed the highest vanadium permeability of $110.1 \times 10^{-7} \text{ cm}^2 \text{ min}^{-1}$ possibly due to the highest IEC and swelling ratio. In comparison, **BP-ArSA** exhibited a markedly lower vanadium permeability of $13.5 \times 10^{-7} \text{ cm}^2 \text{ min}^{-1}$, thus indicating that the incorporation of an aromatic group and an ether linkage in the side chain can greatly improve the vanadium ion rejection property of the membrane. **BP-ArF4** with an additional perfluoroalkyl pendant chain further suppressed the vanadium ion

permeability to $10.2 \times 10^{-7} \text{ cm}^2 \text{ min}^{-1}$, a value 4.0 times and 3.2 times lower than those for Nafion 212 and Nafion 117, respectively. Hydrated vanadium ion and proton transports in the sulfonated aromatic polymers have been found to be heavily affected by the dimension of the separated hydrophobic and hydrophilic domains in the microstructures.²⁹ In general, swelling ratio values are closely related to water uptake and, in Table 1, we use the swelling ratio to correlate the dimensional stabilities of membranes with ion selectivity. The swelling ratios for **BP-ArSA** (12.9%) and **BP-ArF4** (10.2%) were significantly lower than that of **BP-SA** (18.6%), suggesting a smaller aqueous domain within the polymer matrix in spite of the same backbone structure of all three biphenyl CEMs. We also tested **BPN1**, an AEM with the identical molecular structure of **BP-SA**, to investigate the structure–membrane property relationship of sulfonate *vs.* quaternary ammonium side chains in aromatic polymers. Although **BPN1** and **BP-SA** have comparable linear swelling ratios, **BPN1** exhibited a significantly lower vanadium permeability ($23.8 \times 10^{-7} \text{ cm}^2 \text{ min}^{-1}$). This is most likely because the highly concentrated positive quaternary ammonium functional groups of **BPN1** AEM impede the transport of the multi-valent vanadium cations as a result of the Donnan exclusion.^{30,31}

As the length of the side chain increases in the biphenyl polymer series, their IECs decrease due to lower ion exchange groups ($-\text{SO}_3\text{H}$) in unit mass (volume): **BP-SA** (2.29 meq. g^{-1}), **BP-ArSA** (2.01 meq. g^{-1}), and **BP-ArF4** (1.25 meq. g^{-1}). As expected, the proton conductivity of the CEMs follows the order of IEC: **BP-ArF4** < **BP-ArSA** < **BP-SA** (Table 1). The proton conductivities of **BP-ArSA** and **BP-ArF4** were 67.6 and 55.3 mS cm^{-1} , respectively, which are comparable to that of Nafion 117 (59.2 mS cm^{-1}) and Nafion 212 (73.5 mS cm^{-1}). **BP-SA** showed the highest proton conductivity (94.4 mS cm^{-1}) among all studied CEMs as shown in Table 1 due to the highest IEC.

We defined the ion selectivity (α) of the membranes as the ratio of proton conductivity and vanadium permeability, and the values are listed in Table 1. Although **BP-ArF4** and **BP-ArSA** have a lower IEC and lower proton conductivity than **BP-SA**, their ion selectivity values were almost seven times higher than that of **BP-SA**. This result suggests that the positive contributions from lower swelling (hydration number) and vanadium permeability due to the incorporation of an aromatic ring and additional perfluoroalkyl moiety in the flexible side chain of the polymers far outweigh the decreases in IEC and ion conductivity. In spite of

Table 1 IEC, VO^{2+} permeability, proton conductivity, ion selectivity, area resistance, and linear swelling ratio of the membranes

Samples	Thickness (μm)	IEC (meq. g^{-1})	VO^{2+} permeability ($\times 10^{-7} \text{ cm}^2 \text{ min}^{-1}$)	Ionic conductivity (mS cm^{-1})	α ($\times 10^4 \text{ min S cm}^{-3}$)	Area resistance ($\Omega \text{ cm}^2$)	Linear swelling ratio (%)
BP-ArF4	88 ± 1	1.25 ± 0.05	10.2 ± 0.8	55.3 ± 1.2^a	5.42	0.28 ± 0.02	10.2
BP-ArSA	90 ± 1	2.01 ± 0.06	13.5 ± 0.5	67.6 ± 0.9^a	5.08	0.26 ± 0.02	12.9
BP-SA	60 ± 2	2.29 ± 0.19	110.1 ± 2.5	94.4 ± 2.1^a	0.75	0.23 ± 0.01	18.6
BPN1	97 ± 2	2.60 ± 0.05	23.8 ± 3.4	14.5 ± 1.4^b	0.61	0.67 ± 0.07	17.4
Nafion 212	55 ± 1	0.90 ± 0.02	41.2 ± 2.0	73.5 ± 3.1^a	1.78	0.23 ± 0.05	14.3
Nafion 117	195 ± 1	0.89 ± 0.02	32.1 ± 1.7	59.2 ± 2.2^a	1.84	0.89 ± 0.09	15.1

^a Refers to proton conductivity. ^b Refers to anion conductivity.



lower proton conductivity, the ion selectivity of **BP-ArF4** is more than three times higher than those of Nafion 212 and Nafion 117. Areal specific resistance (ASR) of the membranes was measured using electrochemical impedance spectroscopy (Table 1). The ASR of **BPNI** ($0.67 \Omega \text{ cm}^2$) was measured for SO_4^{2-} anion transport of the AEM. Owing to the intrinsically low mobility of SO_4^{2-} anions ($8.27 \times 10^{-8} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1}$) in aqueous solution, which is approximately one-fourth the proton mobility,³² the ASR of **BPNI** was significantly higher than those of biphenyl CEMs with a similar thickness. Although the thickness of **BP-ArF4** and **BP-ArSA** membranes (approximately 90 μm) was higher than that of Nafion 212 (55 μm), they all showed comparable ASR values in the range of 0.23–0.28 $\Omega \text{ cm}^2$. These ASR values were significantly lower than that of Nafion 117 (0.89 $\Omega \text{ cm}^2$), the standard CEM in VRFB with a thickness of 195 μm to minimize vanadium ion crossover in the membrane.

VRFB performance

Fig. 2a–c illustrate VRFB single cell tests with various membrane separators. Among all membranes evaluated, **BP-ArF4** showed the best overall performance far exceeding Nafion 117, the most commonly used benchmark separator membrane. Because the transport of vanadium species may occur through diffusional processes even in the absence of current, coulombic losses are expected to dominate at low current density, whereas VE is expected to decrease with increasing charging/discharging current, owing to the charge transfer overpotential and transport resistance within the anolyte, catholyte, and membrane (Fig. 2a and b). As listed in Table 1, Nafion 212, **BP-SA**, **BP-ArSA**, and **BP-ArF4** have similar ranges of ASR (0.23–0.28 $\Omega \text{ cm}^2$), and thus they all exhibited higher VE than the thicker Nafion 117 (195 μm

thick, 0.89 $\Omega \text{ cm}^2$ ASR). It was found that, although **BP-SA** has a smaller ASR than **BPNI**, the VE of **BP-SA** is lower than **BPNI**. The unexpected low VE of **BP-SA** is presumably due to the voltage loss that resulted from the fast crossover of active species.³³ The effect of enhanced ion selectivity of **BP-ArF4** on VRFB performance was clearly visible in CE. Among all tested membranes, the CE of VRFBs with the **BP-ArF4** membrane approached 100% at a current density $>60 \text{ mA cm}^{-2}$. Even at a lower current density of 40 mA cm^{-2} , the **BP-ArF4** membrane still exhibited a very high CE of 98.6%, as compared with 95.0% exhibited by Nafion 117 and 85.9% by Nafion 212. Notably, the CE of **BP-ArF4** was even higher than that of **BPNI** (96.2%) at 40 mA cm^{-2} . The high CE of **BP-ArF4** can also be reflected from the charge–discharge curves (Fig. S4, ESI†). The discharge capacity of **BP-ArF4** is almost identical to the charge capacity, indicating that the loss of the discharge capacity has been minimized.

Since the CE and EE values of the **BP-ArF4**, **BP-ArSA**, **BPNI**, and Nafion 212 are similar at 100 mA cm^{-2} (Fig. 2a and c), we monitored the capacity retention of the IEMs to further evaluate their performance, particularly at a high current density. VRFB single cells loaded with each IEM were charged and discharged at 100 mA cm^{-2} for 200 cycles. As shown in Fig. 2d, **BP-ArF4** has the lowest capacity decay rate (0.08% per cycle) followed by **BP-ArSA** (0.16%), Nafion 117 (0.29%), **BPNI** (0.36%), Nafion 212 (0.44%), and **BP-SA** (0.49%). The capacity decay of the VRFB cell is typically a result of the charge imbalance due to the crossover of vanadium ions as well as water transfer.³⁴ Benefiting from remarkably lower vanadium permeability and swelling ratio, **BP-ArF4** and **BP-ArSA** exhibited a slow capacity decay rate and maintained high capacity retention after 200 cycles, 84% and 67%, respectively. In contrast,

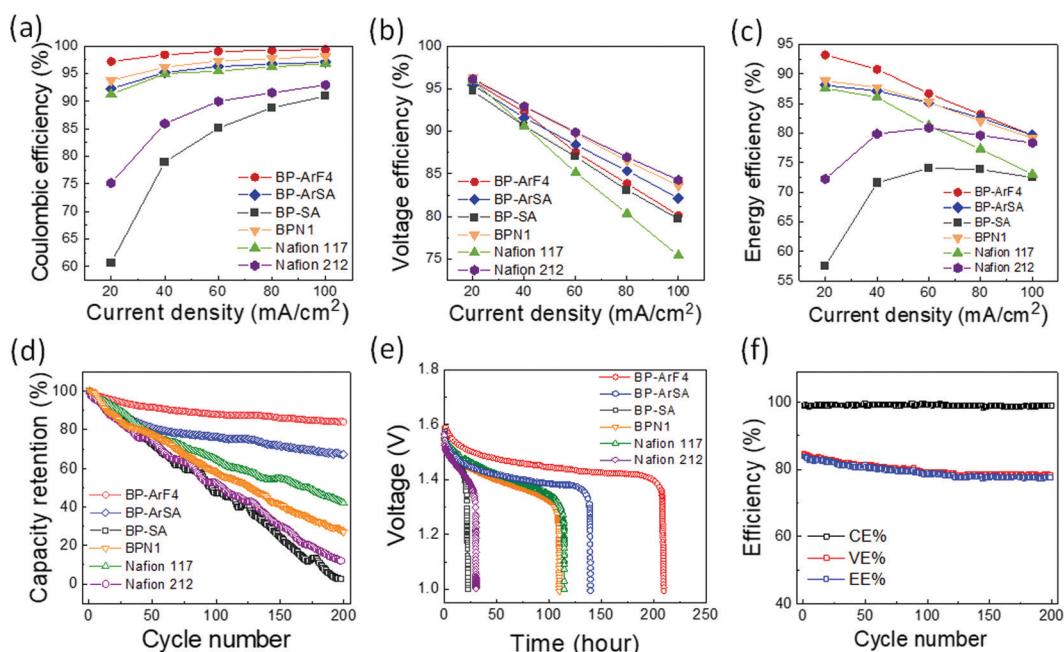


Fig. 2 VRFB single cell performance. (a) CE for PEMs at a current density from 20 to 100 mA cm^{-2} , (b) VE for PEMs at a current density from 20 to 100 mA cm^{-2} , (c) EE for PEMs at a current density from 20 to 100 mA cm^{-2} , (d) capacity retention for IEMs at 100 mA cm^{-2} , (e) self-discharge curves of PEMs, and (f) cycling stability of VRFB with the **BP-ArF4** membrane at 100 mA cm^{-2} .



BP-SA showed a faster capacity decay and lower capacity retention, presumably due to the more rapid vanadium and water crossover, which can deteriorate the charge imbalance between positive and negative half cells. Nafion 117 was able to achieve a higher capacity retention than Nafion 212 (40% vs. 10% after 200 charge–discharge cycles) by lowering vanadium ion crossover with increased thickness. Additionally, we evaluated the self-discharge rate of the IEMs which is closely related to the loss of energy capacity of VRFB.^{35,36} Fig. 2e shows the self-discharge curves of VRFB with IEMs starting from ~90% of the state of charge (SOC). Since the cells were held statically (zero current) during the self-discharge test, the difference of overpotential between each membrane is minimized. Therefore, the initial open circuit voltage (OCV) for all membranes approaches 1.6 V. However, because of the different crossover rates of active vanadium species through membrane separators, the OCV of VRFB cells decreased over time at varying speed. Toward the end of the test, OCV sharply decreased below 1.0 V. When OCV tests were compared with 1.0 V as a cut-off voltage, **BP-ArF4** exhibited the longest self-discharge time (209.5 h) among all tested IEMs: **BP-ArSA** (139.5 h), Nafion 117 (114.5 h), **BPN1** (109.9 h), Nafion 212 (30.5 h), and **BP-SA** (22.2 h). Interestingly, the 90 μ m-thick **BP-ArF4** membrane showed almost twice longer self-discharging time than the 195 μ m-thick Nafion 117, owing to its superior ability to mitigate vanadium crossover. Overall, the results of capacity retention and self-discharge tests agree well with the trend of vanadium permeability results provided in Table 1; the lower the vanadium permeability of the membrane, the higher the capacity retention and the longer the self-discharge time in a VRFB single cell.

We also evaluated the cycling stability and chemical stability of **BP-ArF4** in oxidative/acidic V^{5+}/H_2SO_4 solution and compared with Nafion membranes. The high CE of **BP-ArF4** remained stable (nearly constant close to 100%) during the 200 charge–discharge cycles at 100 $mA\ cm^{-2}$, which indicates negligible crossover of vanadium ions through the membrane during the operation and good chemical stability in the strong oxidizing acidic environment (Fig. 2f). The observed decrease of VE and EE during the first 100 cycles is most likely due to the electrochemical degradation of carbon electrodes, as encountered in other works.^{37,38} While EE of **BP-ArF4** remained almost stable at 80% after 110 cycles and slightly decreased to 79% at 200 cycles, the EEs of VRFB cycling stability of the Nafion 212 and 117 membranes continuously decreased to 73% and 68%

after 200 cycles, respectively (Fig. S5, ESI†). When the chemical stability of the IEMs was evaluated in 0.1 M V^{5+} in 4 M H_2SO_4 , all our biphenyl CEMs showed significantly lower V^{4+} generation than other hydrocarbon PEMs such as BPSH60³⁹ (Fig. S6, ESI†). We believe that the enhanced chemical stability stems from the absence of chemically labile aryl ether bonds in the polymer backbone. As all biphenyl CEMs reported here have polymer backbones made only of carbon–carbon bonds, they should be chemically more resistant to strongly acidic oxidizing environments than aryl ether-containing polymer CEMs such as BPSH60. Among biphenyl CEMs, **BP-SA** which does not have any heteroatom other than CF_3^- and $-SO_3H$ moieties in the chemical structure exhibited the greatest chemical resistance against oxidation. Notably, the chemical stability of **BP-SA** is almost comparable to that of perfluorinated polymer Nafion, which is unprecedented for a hydrocarbon-based CEM. Overall, both the battery cycling test and off-cell chemical stability test clearly suggest that our biphenyl CEMs are quite stable in VRFBs during long-term operation.

SAXS and DFT studies: selective ion transport mechanism

On the basis of our recent work on selective ion transport,^{40,41} we suggest that the exceptionally good battery performance of **BP-ArF4** is due to its unique morphology created by the polymer structure of rigid biphenyl backbone and long tethered perfluoroalkylsulfonate side chain and optimum ion exchange capacity. When equilibrated with a 1.6 M $VOSO_4/4\ M\ H_2SO_4$ electrolyte, the hydration number (swelling) of the CEMs was low (Table 2) and a substantial amount of co-ions (sulfate/bisulfate anions) entered the membrane with a corresponding amount of counter-ions (mostly H_3O^+ and vanadyl species). Interestingly, there was a strong indication that VO^{2+} counter-ions were well hydrated and dissociated (they did not bind to the $-SO_3^-$ fixed ionic group), whereas excess VO^{2+} was strongly associated with SO_4^{2-} co-ions by forming neutral $VOSO_4$ species within the aqueous domains of the CEMs. Then, vanadium crossover mainly occurred through $VOSO_4$ diffusion, with a minor contribution from charged vanadium species, whereas the major contribution to the ionic current through the membrane was from protons, which were present as counter-ions and part of the excess H_2SO_4 entering the membrane as a consequence of the breakdown of Donnan exclusion at high acid concentrations (*i.e.*, 4 M H_2SO_4). We also demonstrated that the transport of vanadium-containing species was largely decreased when the extension of aqueous domains fell below

Table 2 Position of ionomer peak in q -space and calculated values for the average width of aqueous ionic domain d_{aq} of membranes in contact with different solutions. λ represents hydration number. Polymer density $\rho_{polymer}$ and water content w_{H_2O} , respectively, and electrolyte content $w_{electrolyte}$ were used to calculate d_{aq} using eqn (1)

Samples	Density $\rho_{polymer}$ (g cm^{-3})	H^+ form in water			In 4 M $H_2SO_4/1.6\ M\ VOSO_4$		
		q (\AA^{-1})	w_{H_2O} (%)	λ	d_{aq} (nm)	q (\AA^{-1})	$w_{electrolyte}$ (%)
Nafion 117	2.1	0.124	25	20.4	2.10	0.149	21
BP-ArF4	1.4	0.156	28	17.3	1.41	0.190	19
BP-ArSA	1.2	0.162	32	13.0	1.41	0.210	28
BP-SA	1.2	0.184	50	24.3	1.85	0.224	37



the hydrated sizes of these species (sieving-effect), which was also observed in the subnano-sieving PIM-1 membrane.⁴² This effect began to occur at a domain width of approx. 0.7 nm, which remained wide enough for rapid local H_3O^+ diffusion.

With their pronounced hydrophobic/hydrophilic separation, as indicated in Table 2, perfluorosulfonic acid membranes, Nafion 117 and Nafion 212, have much wider aqueous domains, despite the lower swelling in highly concentrated electrolytes (*i.e.*, 1.6 M VOSO_4 /4 M H_2SO_4), thus explaining their low CE values. In contrast, the flexible and long side chains of Nafion efficiently decouple hydrophobic aggregation within the polymeric domain from ionic ordering and water coalescence within the aqueous ionic domain, thus leading to a relatively smooth interface between the two domains and good connectivity of the aqueous ionic domain. Consequently, even with low IEC, Nafion membranes show less of a conductivity decrease than other IEMs as hydration decreases.⁴³ With respect to low hydration conditions, such as those in VRFBs, relatively high proton conductivity can still be achieved, thus leading to high VE for a given current density (Fig. 2b). Therefore, a key design criterion for obtaining both high CE and VE is the morphology of the IEMs, which should have narrow aqueous ionic domains that efficiently block the transport of vanadium species (*e.g.*, VOSO_4 , $\text{VO}_{\text{aq}}^{2+}$, $\text{VO}_{\text{aq}2}^+$, $\text{V}_{\text{aq}}^{3+}$, $\text{V}_{\text{aq}}^{2+}$) but are still wide enough and well-connected for high proton conductivity.

To investigate how the average width of the aqueous ionic domain d_{aq} and the degree of order/disorder affect ion selectivity and VRFB performance, we recorded SAXS patterns for CEMs immersed in pure water and in 1.6 M VOSO_4 /4 M H_2SO_4 (Fig. 3). From the structural correlation length d obtained from

the position of the ionomer peak in q -space, d_{aq} is estimated by using eqn (1).

$$d_{\text{aq}} = d \frac{V_{\text{aq}}}{(V_{\text{aq}} + V_{\text{poly}})}, \quad (1)$$

where V_{aq} and V_{poly} are the volume fractions of the aqueous ionic domain and the polymeric domain, respectively.

This estimation is based on the assumption that the structural correlation length d of the present ionomers scales in a linear fashion with the volume fraction of the aqueous ionic domain V_{aq} as observed for other CEMs with sulfonic-acid as fixed ionic groups.⁴⁴ This corresponds to the local anisotropic swelling, which had been claimed to be characteristic for the locally flat morphologies with the dominant swelling component parallel to the normal.⁴⁴

The relevant data are shown in Table 2. **BP-ArF4** has the unique molecular structure of a hydrocarbon backbone and flexible pendant side chains with a perfluorinated terminating part (Fig. 1a). Although the **BP-ArF4** membrane does not show the smallest structural correlation length d , its d_{aq} is the smallest as compared with other membranes, owing to its lower water volume fraction, essentially reflecting the low IEC. Notably, the ionomer peak of **BP-ArF4** is relatively narrow, and the second order peak is clearly visible (Fig. 3b and c), thus indicating a well-ordered morphology with a narrow distribution of the aqueous ionic domain width. This finding may be a reason for its superior blocking properties for vanadium species, thus leading to the highest CE over the entire current densities (20–100 mA cm⁻²). Despite low IEC, **BP-ArF4** maintains good ion conductivity because of the super-acidic perfluorosulfonate group which leads to its reasonably high VE.

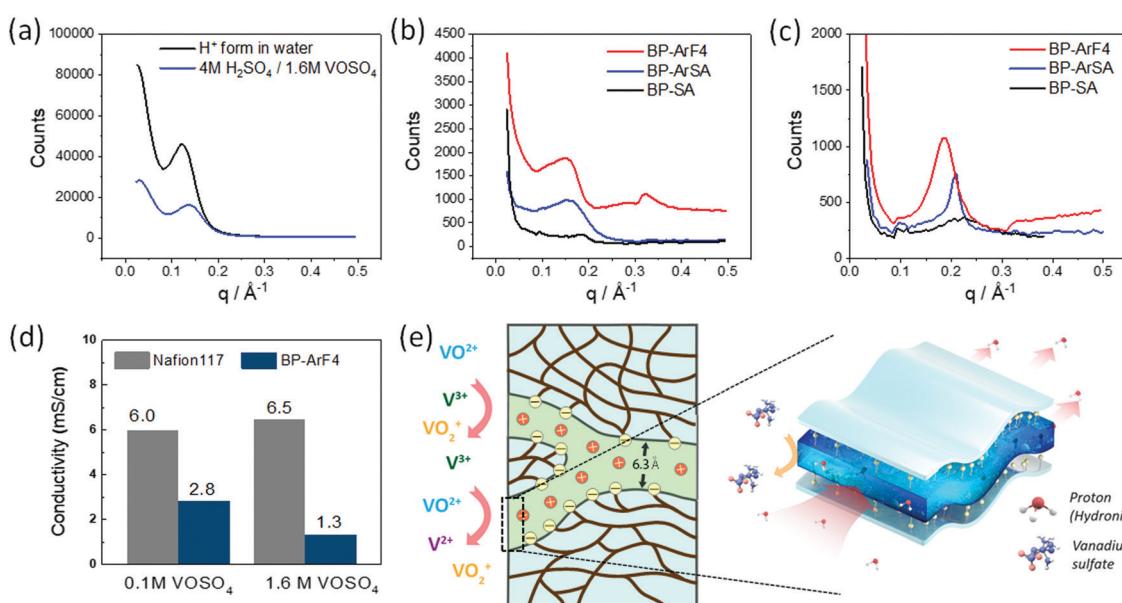


Fig. 3 SAXS patterns of: (a) Nafion 117 in water and 4 M H_2SO_4 /1.6 M VOSO_4 , (b) **BP-ArF4**, **BP-ArSA**, and **BP-SA** membranes in the acid-form immersed in water, and (c) equilibrated in 1.6 M VOSO_4 /4 M H_2SO_4 electrolyte. (d) Total room temperature conductivity of Nafion 117 and **BP-ArF4** membranes equilibrated in solutions of VOSO_4 with different molarities. (e) Illustration of the selective ion transport mechanism of **BP-ArF4** membrane. The narrow aqueous ionic channel (0.63 nm) and functionalities of **BP-ArF4** can efficiently block VOSO_4 transport, while keeping high proton conductivity.



These characteristics of CE and VE lead to a better compromise than for other types of membranes. Therefore, the results of SAXS studies indicate that the unique molecular structure of **BP-ArF4** with narrow aqueous ionic domains can afford the combination of properly sized aqueous ionic transport pathways and the high degree of order. The morphological "sieving" effect can be characterized by a relatively distinct threshold with respect to the width of the aqueous ionic domain.⁴³ It is the very nature of this effect that only a narrow distribution of this width allows for a high blocking effect close to the percolation threshold. Otherwise, one has to further reduce the average width of the transport pathways so as to avoid transport through the fraction of wider parallel pathways. This would further reduce proton conductivity which is also the highest for a narrow domain width distribution because of the non-linear dependence of the water diffusion coefficient on the water volume fraction (domain width).⁴³ As shown in Fig. 3b and c, the morphology of the **BP-ArF4** membrane could provide both properly sized aqueous ionic domains and a high degree of order. The molecular structure of this ionomer represents a rare case of a hydrocarbon backbone with flexible pendant side chains with a perfluorosulfonate terminating group (see chemical structure of **BP-ArF4** in Fig. 1). This allows for the formation of a well-developed ordered hydrophobic/hydrophilic separation, while hydrocarbon structures with sulfonic groups tethered to the main chain *via* a short chain, such as **BP-SA**, are by far less ordered on the nano-meter scale as indicated by broad ionomer peaks of the SAXS patterns (Fig. 3b and c). It should also be mentioned that the super-acidity of the terminating group of **BP-ArF4** guarantees quasi complete dissociation at reduced water activity characteristics for VRFB electrolytes.

We further investigated the transport phenomena of vanadium species in two extreme cases, Nafion 117 (the largest d_{aq}) and **BP-ArF4** (the smallest d_{aq}), by estimating VOSO_4 transport rates. Because both membranes enabled complete exchange into VO^{2+} form in an excess of 0.1 M VOSO_4 with limited uptake of excess VOSO_4 (<10% of the fixed ion concentration), the total conductivity mainly represented the mobility of $\text{VO}_{\text{aq}}^{2+}$ in both structures (the volumetric density of ionic groups in both membranes was very close, *i.e.*, approximately 1.9 meq. mL^{-1}). As shown in Fig. 3d, the total conductivity of **BP-ArF4** (2.8 mS cm^{-1}) is lower than that of Nafion 117 (6 mS cm^{-1}) by approximately a factor of two. A more interesting observation was that the increase in the VOSO_4 concentration from 0.1 to 1.6 M left the total conductivity of Nafion 117 unchanged while the value of **BP-ArF4** largely decreased to 1.3 mS cm^{-1} . In the highly concentrated electrolytes, we observed a substantial amount of co-ion (SO_4^{2-}) uptake, mainly from neutral VOSO_4 and diminished water uptake (approximately 10%) as a response to the decreased water activity in the electrolyte solution. Thus, in more highly concentrated electrolytes with a further decrease in the membrane's hydration, the conductivity contribution of vanadium species (*e.g.*, VO^{2+}) can be further decreased in the **BP-ArF4** after its de-swelling. The lower swelling can decrease the width of the aqueous ionic domain to

an extent (*e.g.*, 0.63 nm in Table 2), which substantially impedes vanadium ions, whereas protons still can be transported through the channels. This result is consistent with the recent molecular dynamics simulation study which suggests that zeolite-based IEMs with pore size <0.7 nm are crucial for the selective hydronium ion transport over vanadium ions.⁴⁵

DFT calculation results provided additional insights into vanadium ion transport in terms of the chemical functionalities of polymer chains. A previous study has reported that the vanadium(IV) ion in sulfuric acid solution forms a $[\text{VO}(\text{SO}_4)(\text{H}_2\text{O})_4]\text{H}_2\text{O}$ complex.⁴⁶ Our further optimized vanadium ion structures indicated that the energetics of the vanadium ion was the lowest when its spin state was a doublet (Fig. S7, ESI†), and its structural parameters, such as the $\text{V}=\text{O}$ bond length and V-O bond length, were in good agreement with previously reported values.⁴⁷ Fig. S8–S11 (ESI†) illustrate the optimized structures of the vanadium ion complexes with different moieties of the sulfonated aromatic IEMs including Nafion and Table S1 (ESI†) lists the interaction energies (detailed calculation methods and optimized structures of IEMs can be found in the ESI†). The interaction energies between **BP-ArF4** and vanadium ion were in the range of 22.6–33.8 kcal mol^{-1} , which are significantly higher than those of other IEMs (14.2–21.4 kcal mol^{-1}). The higher interaction energy is due to the strong binding energy through $\pi \cdots \text{H}$ and $\pi \cdots \text{F}$ hydrogen bonding in **BP-ArF4** and vanadium ion complexes (Fig. S7, ESI†), which hinders the diffusion of vanadium ions through the polymer membrane. Among several complexes, comp3-**BP-ArF4**, the optimized structure of which is depicted in Fig. S8c (ESI†), showed a remarkably large binding energy (33.8 kcal mol^{-1}). In this complex, three hydrogen atoms of the vanadium ion interact with the fluorine atoms of **BP-ArF4**, which should contribute to the interaction to a large extent. In addition, the fourth hydrogen atom (H_D) interacts with the neighboring aromatic moiety. The formation of three $\pi \cdots \text{F}$ hydrogen bonding between vanadium ions and **BP-ArF4** is possible because of the uniquely designed side chain structure of **BP-ArF4** in which the flexible $-\text{CF}_2\text{CF}_2\text{OCF}_2\text{CF}_2\text{SO}_3\text{H}$ side chain is attached to the neighboring aromatic ring. In contrast, the interaction of Nafion with vanadium complexes occurs around its fluorine atoms, owing to the absence of an aromatic ring in the backbone or side chains (Fig. S11, ESI†). All complexes of Nafion showed that two hydrogen atoms of the vanadium complex interact with the $-\text{CF}_3$ group of Nafion. Thus, the computed binding energies indicated that the interaction between Nafion and the vanadium complex is weaker (13.7 and 21.0 kcal mol^{-1} for complexes with comp1 and comp2, respectively) than that of **BP-ArF4** (Table S1, ESI†). Although the fluorine atoms in the $-\text{CF}_3$ group typically have a sizeable negative charge, their hydrogen bonding ability with hydrogen donor molecules is rather weak.⁴⁸

As graphically illustrated in Fig. 3e, the extraordinary high ion selectivity property and VRFB performance of **BP-ArF4** are believed to be derived from the synergistic effects of its unique morphology and functionalities in the polymer chain which greatly hinder the vanadium ion transport, while keeping high



proton conductivity. We also investigated the differences of VOSO_4 transport in **BP-ArF4** and Nafion 117 by comparing the permeation activation energies. The activation energies of VOSO_4 transport for **BP-ArF4** and Nafion 117 membranes were calculated using Arrhenius plots obtained by measuring the VOSO_4 permeability at different temperatures. As shown in Table S2 (ESI†), **BP-ArF4** has almost two times higher activation energy ($9.14 \text{ kcal mol}^{-1}$, 0.40 eV) than Nafion 117 ($4.5 \text{ kcal mol}^{-1}$, 0.20 eV) and Nafion 212 ($5.4 \text{ kcal mol}^{-1}$, 0.23 eV), which agrees with the conclusion from our simulation data provided in Table S1 (ESI†) and the conductivity measurement from VOSO_4 equilibrated solutions shown in Fig. 3c.

Breaking the trade-off limitations in IEMs

Finally, to evaluate the battery performance with the ion transport properties of **BP-ArF4**, we compared its trade-off of ion selectivity and membrane resistivity with other high-performance CEMs and AEMs reported to date (Fig. 4). To make a fair comparison, the performance of IEMs that were enhanced with additional components or by thickness optimization (e.g., mixed matrix membranes, blended membranes, and nanocomposite membranes) are not included in the figure. As all data of **BP-ArF4** in this report were obtained from membranes in the form of a free-standing film directly related to the polymer's unique properties, they should be compared with the performance of membranes made of a single polymer. For example, low areal resistance ($3.9 \times 10^{-2} \Omega \text{ cm}^2$) and high ion conductivity (0.27 S cm^{-1}) values of a recently reported polyamide thin-film composite membrane were obtained by normalizing the resistance and conductance with the entire thickness of the composite membrane (support layer + polyamide selective layer) rather than using a thin selective polyamide layer.⁴⁹ Considering that the intrinsic resistivity and ion conductivity of the polyamide layer are $\sim 706 \Omega \text{ cm}^2$ and $1.4 \times 10^{-3} \text{ S cm}^{-1}$, respectively, a trade-off comparison between **BP-ArF4** and thin-film composite membranes does not provide insightful information about the properties of the materials.

As shown in Fig. 4a, **BP-ArF4** has the best combination of low membrane resistivity and low vanadium permeability outperforming all CEM and AEM materials reported so far. Generally, CEMs show low resistivity and high vanadium permeability, while AEMs

show high resistivity and low vanadium permeability. Notably, the performance of **BP-ArF4** overcomes the conventional trade-off limitation of ion selectivity and resistivity of IEMs. The high proton selectivity over vanadium ions by **BP-ArF4** demonstrates its great potential for application in VRFBs. Indeed, Fig. 4b shows a trade-off relationship between CE and VE, which is similar to the ion selectivity/conductivity trade-off. With a few exceptions, IEMs with high VE tend to show low CE due to high crossover of vanadium species and *vice versa*. However, **BP-ArF4** illustrates a remarkable combination of high CE with high VE, resulting in one of the highest EEs reported in the literature. It outperforms most of the CEMs and AEMs for VRFB systems reported to date and mitigates the trade-off limitation on battery performance due to the highly selective proton/vanadium ion transport.

Conclusions

In summary, we developed a novel class of sulfonated aromatic polymers that have a good combination of high proton conductivity and ion selectivity, and can greatly mitigate the trade-off limitations of conventional IEMs. The effects of the pendant group structure of the polymer on the IEM's ion selectivity and battery performance were investigated. The incorporation of an aromatic ring and a short perfluoroalkyl chain on the pendant group of **BP-ArF4** greatly improved the proton/vanadium ion selectivity, which is three times higher than that of Nafion®, the standard CEM in VRFB. With excellent vanadium ion blocking capacity and good proton conductivity, **BP-ArF4** achieved high CE and VE values in a VRFB single cell. SAXS and DFT calculation studies revealed that the narrowly distributed aqueous ionic domain width of **BP-ArF4** and the strong interaction between the side chain of the polymer and vanadium ion complexes through $\pi \cdots \text{H}$ or $\pi \cdots \text{F}$ hydrogen bonding synergistically improve proton/vanadium ion selectivity. This study suggests an effective path toward the design of high-performance IEMs that can overcome the trade-off limit of ion selectivity/conductivity in other energy conversion and storage systems. Enhanced evaluations on the IEM performance in VRFB (e.g. longer cyclic stability test, volumetric imbalance measurement) will further validate their practical-level cycling stability and efficiency. Additional optimization, such as nanocomposite membranes, using the unique material platform of **BP-ArF4** as a base material can lead to more advanced IEMs with further improvement in efficiencies of energy storage systems.

Experimental section

Reagents

The biphenyl precursor polymer BPBr-100 ($M_n = 60 \text{ kg mol}^{-1}$, $M_w/M_n = 2.0$) was synthesized using an acid-catalyzed polycondensation method as mentioned in our previous reports.^{28,50} Potassium thioacetate (Sigma-Aldrich, 98%), formic acid (VWR, 88%), hydrogen peroxide aqueous solution (ACROS, 35 wt%), sodium 4-hydroxybenzenesulfonate (TCI, > 98%), 4-iodophenol

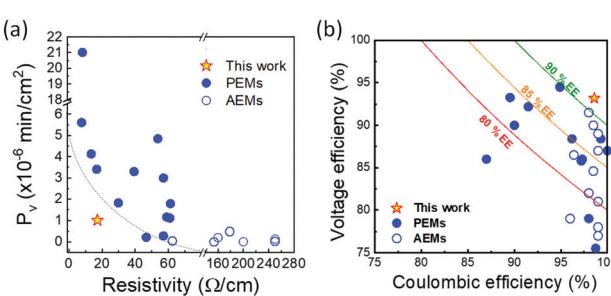


Fig. 4 (a) Trade-off between vanadium diffusivity and resistivity. (b) VRFB performance relationship among CE, VE, and EE at $40\text{--}60 \text{ mA cm}^{-2}$. Detailed information on the trade-off curves is available in Tables S3 and S4 (ESI†).



(Sigma-Aldrich, 99%), tetrafluoro-2-(tetrafluoro-2-iodoethoxy)ethanesulfonyl fluoride (Sigma-Aldrich, 97%), and copper powder (Sigma-Aldrich, 99%, 200 mesh) were used as received without further purification. Sodium hydroxide, potassium hydroxide and potassium carbonate (anhydrous) were purchased from Fisher Scientific. Ethanol, methanol, tetrahydrofuran (THF), dimethyl sulfoxide (DMSO) and *N,N*-dimethylacetamide (DMAc) were of reagent grade and used without further purification. Commercial Nafion® 117 and 212 membranes were purchased from Ion Power Inc. (DE, USA). Vanadyl sulfate (VOSO_4 , 99.9%) and magnesium sulfate (MgSO_4 , 99.5%) were purchased from Alfa Aesar (MA, USA). Sulfuric acid (H_2SO_4 , 98.0%) was purchased from Fisher Scientific (PA, USA).

Polymer synthesis and characterization

BP-SA

Synthesis of BP-TA. BPBr-100 (5.00 g, 13.0 mmol), potassium thioacetate (5.19 g, 45.4 mmol) and THF (150 mL) were added to a 250 mL round-bottom flask. After the precursor polymer was fully dissolved, the reaction flask was connected to a reflux condenser and was heated to 50 °C for 12 h. After cooling to room temperature, methanol (450 mL) was added to the solution to precipitate the polymer, which was then collected by vacuum filtration and dried. The crude polymer product was dissolved in THF (95 mL) and filtered through a cotton plug to remove insoluble solids. The filtrate was poured into methanol to precipitate BP-TA which was collected by filtration and dried under vacuum at 80 °C for 15 h (yield: 4.86 g). ^1H NMR (CDCl_3): δ (ppm) = 7.57 (d, 4H), 7.36 (d, 4H), 2.8 (t, 2H), 2.43 (m, 2H), 1.52 (m, 2H), 1.37 (m, 2H), 1.24 (m, 2H).

Fabrication of BP-SA membrane. Once BP-TA was converted to the sulfonic acid form in **BP-SA**, it exhibited poor solubility in all organic solvents. Thus, the oxidation of the thioacetate group of BP-TA to the $-\text{SO}_3\text{H}$ of **BP-SA** was conducted in a membrane form after casting BP-TA film from a 5 wt% THF solution onto a glass plate. After the membrane was dried, the oxidation was performed with a mixture of 6 M formic acid and hydrogen peroxide aqueous solution (35 wt%) in a glass container at 50 °C for 3 h. The membrane was then removed from the container and washed extensively with water.

BP-ArSA

Synthesis of BP-ArSA. BPBr-100 (3.00 g, 7.80 mmol), sodium 4-hydroxybenzenesulfonate (5.00 g, 25.5 mmol), and potassium hydroxide (1.80 g, 32.0 mmol) were added to a 250 mL round-bottom flask. Anhydrous DMSO (75 mL) and THF (15 mL) were added into the flask; then the reaction mixture was stirred at 40 °C for 24 h after which THF was removed under reduced pressure. The concentrated polymer in DMSO solution was stirred for an additional 12 h. After cooling to room temperature, the solution was poured into acetone (450 mL) to precipitate the polymer, which was washed with methanol to remove excess sodium 4-hydroxybenzenesulfonate. The polymer product was filtered and dried under vacuum at 50 °C for 12 h before fabricating into membrane (yield: 3.8 g). ^1H NMR (DMSO- d_6): δ (ppm) = 7.75 (d, 4H), 7.48 (d, 2H), 7.37 (d, 4H),

6.79 (d, 2H), 3.87 (t, 2H), 2.53 (m, 2H), 1.63 (m, 2H), 1.44 (m, 2H), 1.20 (m, 2H).

BP-ArF4

Synthesis of BP-Ar-I. BPBr-100 (10.0 g, 26.2 mmol), 4-iodophenol (17.75 g, 80.6 mmol), and potassium carbonate (11.15 g, 80.6 mmol) were added to a 500 mL round-bottom flask which was connected with a reflux condenser under a positive flow of nitrogen. Anhydrous DMAc (200 mL) was added to the flask and the reaction mixture was stirred at room temperature until all reagents were completely dissolved and then heated to 90 °C for 3 h. After cooling to room temperature, the solution was poured into methanol containing HCl (12 mL) to precipitate the polymer. The collected polymer was re-dissolved in THF (220 mL), filtered through a cotton plug, and precipitated by dropping into methanol. Precipitated polymer was filtered and dried in a vacuum oven at 50 °C overnight to afford BP-ArI (yield: 13.5 g). ^1H NMR (DMSO- d_6): δ (ppm) = 7.57 (d, 4H), 7.49 (d, 2H), 7.39 (d, 4H), 6.60 (d, 2H), 3.82 (t, 2H), 2.47 (m, 2H), 1.71 (m, 2H), 1.47 (m, 2H), 1.31 (m, 2H).

Synthesis of sodium tetrafluoro-2-(tetrafluoro-2-iodoethoxy)-ethanesulfonate (1). Tetrafluoro-2-(tetrafluoro-2-iodoethoxy)-ethanesulfonyl fluoride (5.00 g, 11.7 mmol) and NaOH solution (0.95 g in 6.5 mL H_2O ; 12.8 wt%) were added to a 25 mL round-bottom flask connected with a reflux condenser, and then the reaction mixture was heated to 95 °C for 16 h in an oil bath. After the reaction completed, water was removed under vacuum at 60 °C. Ethanol (20 mL) was added to the concentrated reaction mixture to precipitate sodium fluoride, which was removed by filtration through a cotton plug to give a clear solution. Removal of ethanol using a rotary evaporator gave compound **1** in sodium sulfonate form as an off-white powder which was dried in a vacuum oven at 50 °C overnight (yield: 5.20 g, 99.3%). ^{19}F NMR (D_2O): δ (ppm) = -68.38 (t, 2F), -83.17 (t, 2F), -86.31 (t, 2F), -118.46 (t, 2F).

Synthesis of BP-ArF4. **BP-Ar-I** (3.05 g, 5.75 mmol), Cu (3.65 g, 57.0 mmol), and DMAc (18 mL) were added to a 100 mL 2-neck round-bottom flask under a positive flow of nitrogen. After **BP-Ar-I** was dissolved, the reaction mixture was stirred at 95 °C for 1 h. DMAc (8.0 mL) solution containing compound **1** (5.13 g, 11.5 mmol) was then added dropwise slowly *via* a syringe at 95 °C. The reaction mixture was stirred at 95 °C for 2 h, then at 120 °C for 48 h and then at 160 °C for 24 h.⁵¹ The reaction mixture was cooled to room temperature and additional DMAc (20 mL) was added to dilute the polymer solution which was centrifuged at 9000 rpm for 30 min to separate copper powder. The centrifuged polymer solution was filtered through a short silica plug to remove any fine copper residue and poured into Petri-dishes evenly to cast polymer films. The **BP-ArF4** membranes (in $-\text{SO}_3\text{Na}$ form) were dried in a vacuum oven at 80 °C, washed with warm water, and finally dried under vacuum (yield: 4.07 g). ^1H NMR (DMSO- d_6): δ (ppm) = 7.71 (d, 4H), 7.52 (d, 2H), 7.37 (d, 4H), 7.01 (d, 2H), 3.94 (t, 2H), 2.52 (m, 2H), 1.66 (m, 2H), 1.45 (m, 2H), 1.21 (m, 2H). ^{19}F NMR (DMSO- d_6):



δ (ppm) -64.57 (s, 3F, $-\text{CF}_3$), -82.25 (t, 2F), -87.08 (t, 2F), -111.82 (t, 2F), -117.92 (t, 2F).

BP1

Synthesis of BP1. BP1 was prepared using a modified procedure mentioned in our previous report.⁵⁰ BPBr-100 (5.00 g, 13.0 mmol) was dissolved with DMAc (50 mL) in a 250 mL round-bottom flask. TMA in ethanol solution (33 wt%, 20 mL) was added to the flask and the reaction mixture was stirred at room temperature for 24 h. The polymer was precipitated by adding a mixture of hexane/THF solution (7:3 in v/v), which was collected by filtration and dried under vacuum at 40 °C overnight. ^1H NMR (DMSO- d_6): δ (ppm) = 7.56 (d, 4H), 7.39 (d, 4H), 3.22 (t, 2H), 3.01 (s, $-\text{CH}_3$, 9H) 2.54 (m, 2H), 1.61 (m, 2H), 1.28 (m, 2H), 1.20 (m, 2H).

Polymer molecular structure characterization. ^1H NMR spectra were obtained using a Varian Unity 500 MHz spectrometer, and chemical shifts were referenced to the NMR solvent peaks; CDCl_3 (at 7.26 ppm) and DMSO- d_6 (at 2.48 ppm). FT-IR spectra were obtained for the investigation of the functional groups of the synthesized polymer using a Thermo Nicolet Nexus 4700 FT-IR Spectrometer with ATR tool. The average molecular weight of the precursor polymer (BPBr-100) was determined using gel permeation chromatography (GPC, Viscotek T60A instrument), with THF as the eluent and a polystyrene standard curve.

Membrane fabrication and characterization

Membrane fabrication. Polymer solutions (ca. 5 wt%) of different polymer/solvent pairs [BP-TA/THF, **BP-ArSA**/DMSO and **BP-ArF4**/DMAc (both ionic polymers in $-\text{SO}_3\text{Na}$ form), and **BP1**/DMSO] were prepared to fabricate membranes with a thickness of 60–100 μm . The thickness of the membrane was controlled to optimize their VRFB performance. Each polymer solution was cast on a glass plate and dried in a vacuum oven at 80 °C for 24 h. The **BP-SA** membrane was obtained by the oxidation reaction of the BP-TA membrane as described in the synthetic procedure mentioned above. Fabricated membranes of **BP-SA**, **BP-ArSA**, and **BP-ArF4** were placed in a 1 M H_2SO_4 solution at 80 °C for 2 h and then washed with water several times over a period of 24 h. The **BP1** membrane with Br^- counter ion form was immersed in 1 M Na_2SO_4 solution for 24 hour and then washed three times with deionized water. The thicknesses of **BP-ArSA**, **BP-ArF4**, and **BP1** were in the range of 87–100 μm . The thickness of **BP-SA** (60 μm) was thinner than that of the other BP-based membranes due to the different fabrication method (required oxidation).

Ion exchange capacity, water uptake, and swelling ratio. Weight-based ion exchange capacity (IEC_w) of the polymer membranes was calculated from the following titration method. Membranes were equilibrated in 1 M NaCl solution at room temperature for 24 h, and then the solution was titrated with 0.01 M NaOH solution using phenolphthalein as the indicator. The IEC_w value was calculated from eqn (2):

$$\text{IEC}_w = \frac{0.01 \times V_{\text{NaOH}}}{W_{\text{dry}}}, \quad (2)$$

where V_{NaOH} is the volume of NaOH solution added in titration, and W_{dry} is the weight of membrane in a dry state.

Linear swelling (%) was obtained by measuring the x - y and diagonal length of dry and wet membrane samples. Water uptake ($W_{\text{H}_2\text{O}}$ in wt%) was measured by comparing the weights of wet vs. dry membranes at room temperature according to:

$$W_{\text{H}_2\text{O}} = \frac{W_{\text{wet}} - W_{\text{dry}}}{W_{\text{dry}}} \times 100\%, \quad (3)$$

Hydration number (λ), which is defined as molar ratio of water molecules per mole of ion exchange site, was obtained using the following calculation:

$$\lambda = \frac{W_{\text{H}_2\text{O}}}{M_{\text{H}_2\text{O}} \times \text{IEC}_w}, \quad (4)$$

where $M_{\text{H}_2\text{O}}$ is the molar mass of water.

Ion transport properties and VRFB performance

VO²⁺ permeability. The VO²⁺ permeability of membranes was determined using a diffusion test as described elsewhere.²³ The prepared membrane with an effective area of 1.76 cm^2 was placed between two diffusion half cells. 11 mL of 1 M VOSO₄ in 2 M H_2SO_4 solution was injected into one side of the diffusion cell (feed side). To balance the osmotic pressure across the membrane, the same amount of 1 M MgSO₄ in 2 M H_2SO_4 solution was injected into the other side of the cell (permeate side). The solution in both diffusion cells was continuously stirred with magnetic stirrers during the test to mitigate concentration polarization. The VO²⁺ concentration at the permeant side was monitored using UV-Vis spectroscopy (UV-1800, Shimadzu, Japan) at a regular interval. The VO²⁺ permeability through the membrane was calculated using the following formula:

$$V \frac{dC_B(t)}{dt} = A \frac{P}{L} (C_A - C_B(t)), \quad (5)$$

where V is the volume of solution in each reservoir, C_A is the feed side VO²⁺ ion concentration, C_B is the permeation side VO²⁺ ion concentration, t is the testing time, A is the effective membrane area, P is the VO²⁺ ion permeability, and L is the membrane thickness.

Proton conductivity and area resistance. The in-plane ionic conductivity was measured via the electrochemical impedance spectroscopy (EIS) method using a Metrohm potentiostat/galvanostat (Metrohm, FL, USA). The frequency range adopted for the conductivity test was 10⁶ Hz to 10 Hz and the amplitude was 10 mV. Before the proton conductivity test, all membranes were immersed in deionized water for 24 hours. The proton conductivity was calculated from the resistance value obtained by extrapolating the low-frequency curve on the Nyquist plot based on the following equation:

$$\sigma = \frac{L}{R \cdot A}, \quad (6)$$

where L corresponds to the electrode separation, R is the membrane resistance and A is the membrane cross-sectional area. For the area resistance measurement, the conductivity cell



was setup using the method described in the literature.⁵² The resistance of the entire cell with (R_{tot}) and without the membrane (R_{blank}) was determined using EIS over a frequency range from 10⁶ Hz to 10 Hz with an amplitude of 10 mV. The area resistance of the membrane was calculated from the difference between the two values ($R_{\text{tot}} - R_{\text{blank}}$).

Activation energy measurement. The permeation activation energy of vanadium ions in Nafion and **BP-ArF4** was obtained from the Arrhenius plot (Fig. S12, ESI[†]). The vanadium permeability and temperature follow an Arrhenius like relation (eqn (6)). To measure the vanadium permeation activation energy, the VO^{2+} permeability test was performed at different temperatures for each membrane inside a temperature-control chamber. From all the experiments, it was found that $\log(D)$ is linearly correlated with $1/(RT)$. As suggested by eqn (6), activation energy (Table S2, ESI[†]) was obtained from the slope of the $\log(D)$ vs. $1/(RT)$ plot.⁵³

It is worth mentioning that a membrane has different swelling ratio at different temperatures. Hence, a change in membrane dimension was considered during calculating membrane permeability at each temperature. The activation energies of Nafion 117, Nafion 212, and **BP-ArF4** are listed in Table S2 (ESI[†]). The temperature dependence of the vanadium permeability of Nafion 117, Nafion 212, and **BP-ArF4** is displayed in Fig. S9 (ESI[†]).

$$D = D_0 \exp\left(-\frac{E}{RT}\right), \quad (7)$$

where D is the vanadium permeability/diffusivity ($\text{cm}^2 \text{ min}^{-1}$), D_0 is the pre-exponential factor ($\text{cm}^2 \text{ min}^{-1}$), E is the activation energy (kJ mol^{-1}), R is the universal gas constant ($8.314 \text{ J mol}^{-1} \text{ K}^{-1}$), and T is the absolute temperature (K).

VRFB single cell test. The configuration of the VRFB cell has been reported previously.⁵⁴ Two graphite felts (MTI, 30 × 30 × 4 mm) were used as electrodes without any post-treatment. The testing membrane was sandwiched between the two graphite felts with an active area of 9 cm². Two copper current collectors were coated with gold to prevent corrosion. The gold coated copper plates were separated from carbon felts by two TF6 SIGRACELL[®] bipolar plates (SGL Carbon, USA). The same volume of electrolytes (each 45 mL) containing 1.6 M vanadium ions and 4 M H_2SO_4 were adopted as the catholyte and anolyte solutions. The catholyte was prepared by oxidizing V(IV) to V(V) ions under galvanostatic conditions, and the anolyte was prepared by reducing V(V) to V(II). During the battery operation, the half-cell reaction on the positive electrode was $\text{V(IV)} \rightleftharpoons \text{V(V)} + \text{e}^-$, and the reaction on the negative electrode was $\text{V(II)} + \text{e}^- \rightleftharpoons \text{V(IV)}$.⁵⁵ The electrolytes were circulated using Masterflex L/S peristaltic pumps (Cole-palmer, USA) with the flow rate of 30 mL min⁻¹. The operation of the cell was controlled using a CT2001A-5V1.8A battery testing system (Landt, China) with the cut-off voltage of 1.65 V (charge process) and 0.8 V (discharge process), respectively. Coulombic efficiency (CE), voltage efficiency (VE) and energy efficiency (EE) of VRFB were calculated using the following equations:

$$\text{Coulombic efficiency (CE), \%} = \frac{t_{\text{Discharge}}}{t_{\text{Charge}}} \times 100\%, \quad (8)$$

$$\text{Voltage efficiency (VE), \%} = \frac{V_{\text{Discharge}}}{V_{\text{Charge}}} \times 100\%, \quad (9)$$

$$\text{Energy efficiency (EE), \%} = \frac{\text{CE} \times \text{VE}}{100}, \quad (10)$$

Oxidative stability. The oxidative stability of the membranes against V(V) species was tested according to a method widely reported in the literature.^{56–58} Prior to the test, the membranes were dried *in vacuo* for one day. Afterwards, 0.12 g (dry weight) of membrane sample was immersed in 10 mL of 0.1 M V(V)/4 M H_2SO_4 solution, which is prepared from the fully charged catholyte solution. The concentration of V(IV) species in the solution, which is generated due to the oxidation of the membranes, was monitored using a UV-Vis spectrophotometer (UV-1800, Shimadzu, Japan). The as-prepared 0.1 M V(V)/4 M H_2SO_4 solution was used as the blank reference for the measurements. The use of a diluted V(V) solution instead of highly concentrated battery testing solution is considered for the measuring range of UV-vis. The stability result can be found in Fig. S5 (ESI[†]).

Small angle X-ray scattering. Small angle X-ray scattering (SAXS) was carried out using a home-built camera using a rotating anode (Bruker FR591-Nonius) operating at 3 kW with a source of Cu-K α radiation ($\lambda = 1.5418 \text{ \AA}$). The X-ray optics consists of a set of two horizontal and vertical 16 cm long Ni-filtered total reflection mirrors (Kirkpatrick-Baez mirrors) positioned at 180 cm from the X-ray source. The size of the source ($0.2 \times 0.2 \text{ mm}^2$) and its distance from the X-ray optics (180 cm) provide a low divergence of the X-ray beam ($\sim 0.05 \text{ mrad}$), which is a key parameter (with the high-brightness) to optimize the SAXS and GISAXS applications.

The beam line is equipped with a set of 4 beam defining slits (close to mirror optics) and a set of 4 anti-scattering slits in front of the sample position (Xenocs motorized non-scattering slits). The distance between the two sets of slits is 180 cm, thus providing very low-background intensity even at low scattering angle. Scattering patterns were recorded using a two-dimensional $14 \times 14 \text{ cm}^2$ area (Bruker VANTEC-2000) mikroGap[®] detector. The mikroGap[®] technology gives a very fine Point Spread Function which allows the measurement of even weak scattering intensities close to strong diffraction peaks with pixel size resolution of either 70 μm , 140 μm or 280 μm . The flux on the sample is $\sim 3 \times 10^7 \text{ ph s}^{-1}$ with a beam size (FWHM) $\sim 600 \times 600 \mu\text{m}^2$. The sample-detector distance was placed at 1 m and 3.5 m to explore q values from about $q = 0.01$ up to 0.4 \AA^{-1} , where q is the momentum transfer $q = (4\pi \sin \theta)/\lambda$ and 2θ is the total scattering angle. The sample-detector distance was calibrated using silver behenate as the standard. The normalization of the scattering data was applied by first measuring the transmission with a semi-transparent beam stop, followed by the thickness of each sample, and finally using a Lupolen sample as the calibrating sample. After equilibration in pure water or in a 1.6 M VOSO_4 /4 M H_2SO_4 aqueous solution, two or three membrane samples with 4 mm diameter (total thickness around 300 μm) were placed in a brass cell



between 5 μm thick Mylar sheets serving as windows. The mass difference of the membranes in the dry proton and the soaked state was attributed to electrolyte uptake. For calculating the volume fraction of vanadium electrolyte in the membrane, its density was taken to be identical to that of the 1.6 M $\text{VOSO}_4/4\text{ M H}_2\text{SO}_4$ aqueous solution (1.4 g cm^{-3}).

Density functional theory (DFT) calculations. For density functional theory (DFT) calculations, we employed the ωB97XD functional⁵⁹ and 6-31G(d,p) basis sets for S, N, C, H, and O atoms.^{60,61} For vanadium, core electrons were represented using the LANL08 effective core potential (ECP) and for valence electrons of vanadium, we used LANL08 basis sets augmented by f function.^{62–64} Geometry optimizations and additional frequency calculations to confirm that the optimized structure is a minimum were conducted using the Gaussian 16 program.

Conflicts of interest

The authors declare no competing interests.

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