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Assignment of the methanol OH-stretch overtone spectrum using the pattern recognition method†

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We present the measurement and analysis of the 2OH stretching band of methanol between 7165 cm⁻¹ and 7230 cm⁻¹ cooled down to 26 ± 12 K in a buffer gas cooling experiment. Measurements were performed with a cavity ring-down spectrometer having a detection limit $\alpha_{\min} = 2 \times 10^{-10}$ cm⁻¹. A total of 350 rovibrational transitions were assigned and 62 rovibrational transitions were tentatively assigned. This assignment was performed using the pattern recognition method developed by Rakvoský *et al.* [*Phys. Chem. Chem. Phys.*, 2021, **23**, 20193–20200]. In this work, we extended their method by using information on the relative intensities of the transitions to add one criterion to the validation of the assignments, allowing us to firmly assign 188 additional rovibrational transitions and to tentatively assign 14 more compared to the ir work.

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1 Introduction

Methanol is an interesting molecule for various fields of physics, *i.e.* astro-,¹ high-energy,^{2,3} and molecular physics.^{4,5} Due its relatively large dipole moment, this molecule can be observed in the microwave and millimeter ranges in a series of interstellar environments.⁶ Its spectral signature in the infrared range can also be used for remote sensing purposes.⁷ In particular it is one of the few molecules presenting several transitions which can be detected at cosmological distances on the order of a few gigalight-years. In addition, the observed transitions present a favorable sensitivity to any variation of the proton-to-electron mass ratio $\mu = \frac{m_p}{m_e}$. This feature makes methanol a molecule of choice to probe any variation of this ratio over cosmological time scales.^{3,8}

In terms of molecular and chemical physics, it is one of the smallest molecules presenting an internal rotation. It, therefore, has represented a reference system to study such phenomenon since the first part of the twentieth century.^{9–12} Notably,

Xu *et al.* compiled all the experimental data up to 2008 to retrieve the most precise spectroscopic parameters of the ground vibrational state.¹³ Because of the increase in states density, the study of vibrational excited states of this molecule has always represented a challenge. In the early 90's, the OH stretching fundamental band of methanol was recorded with sub-Doppler resolution using a molecular-beam optothermal spectrometer to achieve a low effective rotational temperature of 6 K.¹⁴ A total of 350 transitions were assigned in that work and fitted using ground state combination differences calculated by a program¹⁵ based on the internal axis method described by Herbst *et al.*⁵ A standard deviation of 0.0013 cm⁻¹ was obtained, being four times the experimental error (0.0003 cm⁻¹). Boyarkin *et al.*¹⁶ and Rueda *et al.*¹⁷ have then performed a series of spectroscopic studies combining the selective approach of double resonance and the cooling of a supersonic expansion. This infrared laser assisted photofragment spectroscopy (IRLAPS) method appeared to be very efficient and allowed for building a global modeling of the vibrations of methanol. This work was done at relatively low resolution (0.05 cm⁻¹) and only allowed for the assignment of a limited number of rovibrational transitions per vibrational band. They basically circumvented the complexity of the spectral signature through their experimental methodology. David S. Perry, a regular co-author of that series of works, also used a pulsed supersonic expansion combined with a continuous cavity ring-down spectroscopy to study the $\nu_1 + \nu_3$, *i.e.* OH + CH stretch combination band.¹⁸ On the order of 300 transitions were assigned from this work but the state-of-the-art effective Hamiltonians^{19,20} were unable to reproduce the line positions

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significantly affect the etalon's free spectral range (FSR). The interference pattern at the output of the etalon cavity consists in consecutive transmission peaks, each of them being separated by one FSR. The relative wavenumber grid is retrieved from the interference fringe pattern of the etalon. The reference cell consists of a vessel under vacuum with two viewports. Light has a single path inside the cell, efficiently interacting with water desorbing from the vessel walls. Absolute calibration was performed by fitting the relative wavenumber grid to 53 water transitions known with a precision better than 10^{-3} cm^{-1} .^{29,30} The root mean square value of the residuals of the linear fit was equal to $9 \times 10^{-4} \text{ cm}^{-1}$. This value is used as the frequency tolerance criterion when looking for patterns in the molecular spectrum, as detailed in Section 3.1. The wavenumber axis is then shifted down by the excitation frequency of the AOM.

In the process known as beam injection,³¹ a small flow of methanol was introduced ballistically inside the cold cell by passing it through a hole in its lid, using helium as a carrier gas. The rotational temperature was evaluated using a two-temperature analysis,^{21,28,32} utilising the twelve transitions that were unambiguously assigned by Svoboda *et al.*²¹ as a reference. The rotational temperature was estimated to be $26 \pm 12 \text{ K}$. The translational temperature of methanol was evaluated to $28 \pm 4 \text{ K}$ by assuming that the only contribution to the line broadening of these twelve methanol transitions is the Doppler effect.

A Labview program, originally developed for the FANTASIO setup^{33,34} manages the wavenumber scan of the DFB lasers and the simultaneous measurements of the light at the output of the etalon cavity and at the output of the reference cell, and the decay times of light leaking from the CRDS cavity. For the latter, once the intensity on the detector placed at the output of the cavity exceeds a threshold value, the AOM is turned off and the software records the light decay, it then performs the exponential decay fit to finally retrieve the absorption coefficient from the characteristic decay time. For a given spectral element, several decays are recorded and averaged. The cavity length is swept back-and-forth by moving the end mirror with a piezoelectric actuator to ensure that coupling between the laser and the cavity occurs periodically. After a proper calibration, the absorption coefficient with respect to the wavenumber is known. The absorption coefficient actually consists of the molecular fingerprint superimposed on a slowly varying baseline, *i.e.* the empty-cavity response. The contribution of the latter is evaluated using a weighted penalized least squares method, also known as the Whittaker algorithm.^{35–37} It is then subtracted, as suggested by Didriche *et al.*,³³ using the following relationship:

$$\alpha = \frac{L}{cl} \left(\frac{1}{\tau} - \frac{1}{\tau_0} \right) \quad (1)$$

with α the molecular absorption coefficient, τ_0 the empty-cavity ring-down time, τ the ring-down time in presence of the sample, L the total cavity length, l the length over which the sample spreads inside the cavity and c the velocity of light. We considered methanol to be confined to the cold cell when evaluating eqn (1), *i.e.* $l = 10 \text{ cm}$. The last step of the data

treatment before the analysis of the molecular signature was to approximate the spectrum as a sum of Gaussian functions, one per peak above the sensitivity threshold and to determine and tabulate the parameters of these Gaussian functions, that is their amplitude, position and width. At this point, the spectrum comes down to a list of three columns containing the parameters of all the peaks.

3 Results and discussion

The $2\nu_1$ band of methanol that was measured between 7160 cm^{-1} and 7235 cm^{-1} is shown in Fig. 2(a). About 80 ringdowns per spectral element were averaged to record this spectrum. A zoomed-in view on a 0.5 cm^{-1} wide spectral range is depicted in Fig. 2(b). The latter illustrates the complexity of the dense methanol molecular fingerprint and the high dynamic range of the measurement, with peaks covering 3 orders of magnitude in terms of intensity. More than 2500 transitions are spread over the spectral region of the measurement with up to 70 resolved transitions per cm^{-1} . Under these conditions and because of the failure of traditional molecular Hamiltonians to treat floppy molecular systems in the overtone range,^{18,38} alternatives to traditional assignment methods are required. The method developed by Rakvoský *et al.*²² consists in seeking for patterns in the peaks positions. This method is detailed in Section 3.1, along with its application to methanol.

The fit of an isolated transition is given in Fig. 2(c). The discrepancies plotted in the residuals panel are assigned to the presence of warmer methanol molecules within the cell. A more detailed analysis of the lineshape of molecular transitions in our buffer gas cooled environment can be found in ref. 28.

3.1. Pattern recognition method

In molecular spectroscopy, the ground state combination differences (GSCD) method is a commonly employed technique for the assignment of molecular spectra. This method relies on the fact that two transitions terminating in a same upper state are separated by the energy difference between the two lower states involved in these transitions. Rakvoský *et al.*²² extended the GSCD method by looking for all the allowed transitions that lead to a same upper state. These lower energy states form a group, called combination difference multiplet (CDM). Each upper rotational state possesses a unique CDM, determined by applying the selection rules for allowed transitions. Assignment of the rovibrational transitions then consists in the recognition of the CDM patterns in the molecular spectrum, as illustrated in Fig. 3. All the transitions belonging to a given CDM are spaced in the molecular spectral signature by the differences in energy of their lower energy states.

Methanol is an asymmetric top molecule containing six atoms with ground rotational constants $A = 4.254 \text{ cm}^{-1}$, $B = 0.824 \text{ cm}^{-1}$ and $C = 0.793 \text{ cm}^{-1}$.¹³ The near prolate character of this molecule can be illustrated by Ray's asymmetry parameter, $\kappa = (2B - A - C)/(A - C) = -0.982$, very close to $\kappa = -1$, the limiting case of a prolate symmetric top rotor. Methanol is the



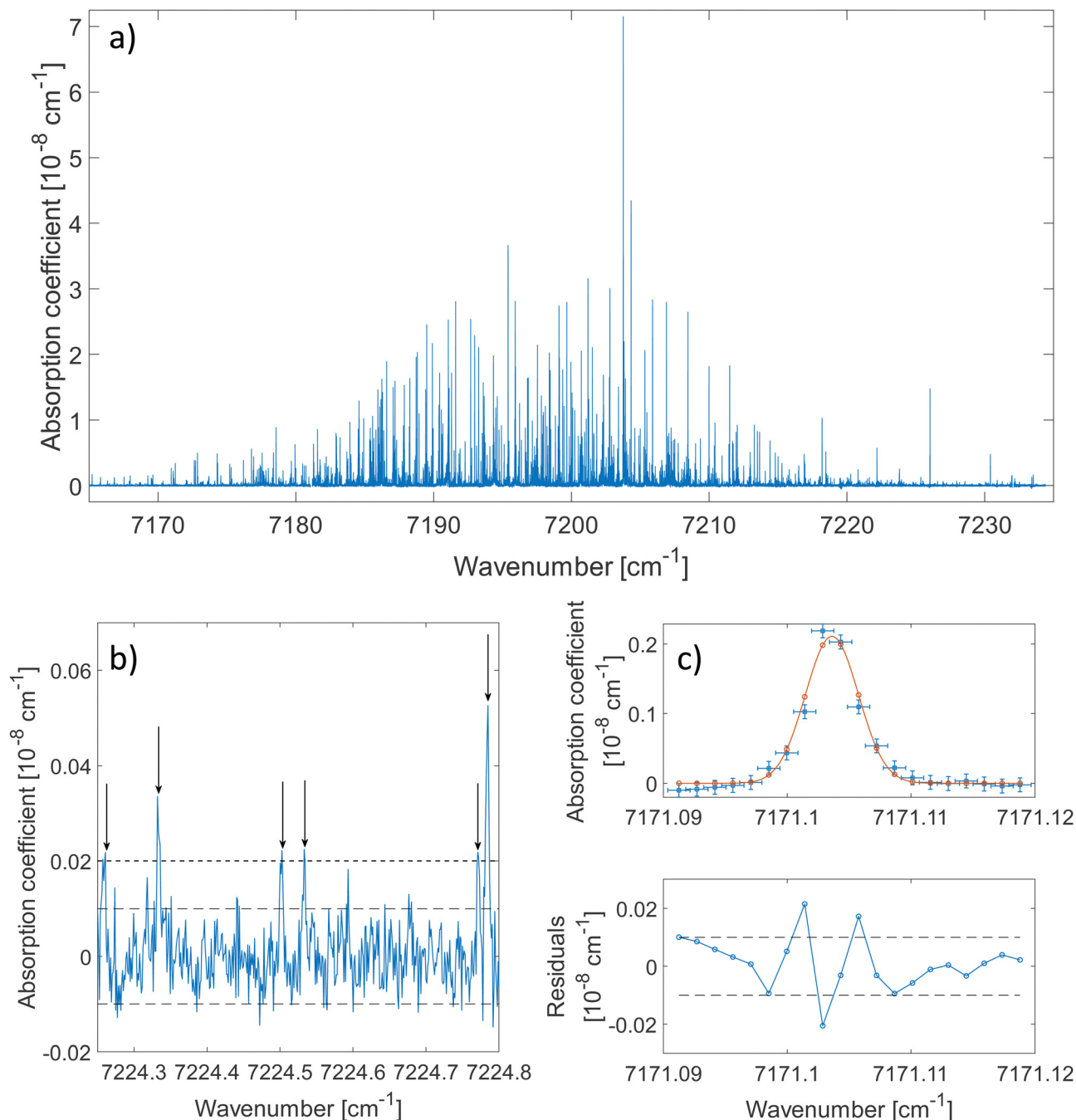


Fig. 2 (a) Spectral signature of the $2\nu_1$ band of buffer gas-cooled methanol. The rotational temperature was evaluated to 26 ± 12 K. (b) The zoom inset illustrates the density of peaks and the determination of the threshold intensity (dashed line) for the automated detection of peaks. Most of the baseline is contained between the two dotted horizontal lines at $\pm 10^{-10} \text{ cm}^{-1}$. The arrows represent the centre of the detected peaks. (c) Fit of an isolated transition (blue squares, upper frame) with a Gaussian function (red, dotted line, upper frame) and its residuals (blue, lower frame). The translational temperature associated with this line is 31 K. Vertical error bars are $\pm 10^{-10} \text{ cm}^{-1}$ and horizontal error bars are $\pm 9 \times 10^{-4} \text{ cm}^{-1}$. Two horizontal dashed lines at $\pm 10^{-10} \text{ cm}^{-1}$ are plotted.

smallest covalently bonded molecule exhibiting an internal rotation. The three equivalent minima of the molecule³⁹ and the relatively low barrier to internal rotation give rise to two tunnelling components noted A and E, where E is doubly degenerate. The spin statistical weights of these components are 4 and 2 respectively.⁴⁰ The CDMs were generated, for A and E

components, using the selection rules given below,^{5,22} where the \pm indicates the sign in the following linear combination of basis vectors $|JKM\rangle \pm |J-KM\rangle$ for $K \neq 0$:

- For A component ($K \geq 0$):

$$\pm \leftrightarrow \mp, \quad \Delta J = 0, \quad |\Delta K| = 0, 1 \quad (2)$$



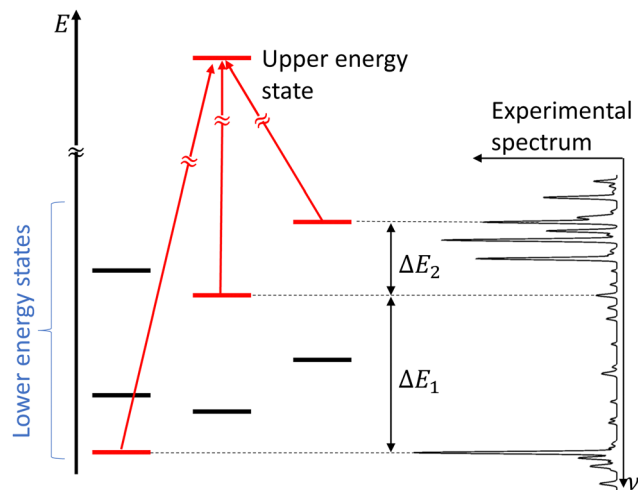


Fig. 3 Concept of combination difference multiplet and its application to the assignment of molecular spectra. Figure adapted from Rakvoský *et al.*²²

$$\pm \leftrightarrow \pm, \quad |\Delta J| = 1, \quad |\Delta K| = 0, 1. \quad (3)$$

- For E component:

$$\Delta J = 0, \quad |\Delta K| = 1 \quad (4)$$

$$|\Delta J| = 1, \quad |\Delta K| = 0, 1. \quad (5)$$

In these equations, J is the angular momentum number and K is the projection of J along the principal symmetry axis. As one can see from these selection rules, the $2\nu_1$ mixed band character (parallel and perpendicular) of methanol allows for

having up to nine transitions reaching the same upper level. This provides a significant decrease of fortuitous match in the pattern detection, as explained by Rakvoský *et al.*²²

The lower state energy levels used for the generation of the CDMs were extracted from the work done by Xu *et al.*¹³ Their spectral analysis included 19 000 far-infrared transitions and 5600 rotational transitions in the subTHz range for 119 parameters, allowing for producing a fit with an uncertainty of 150 kHz for the $\nu_t = 0$ torsional state. Although the output file of the fit was accessible from Appendix A of the publication, it was necessary to re-evaluate the energy levels to get a list of the rotational energy levels in the torsional states up to $J = 10$ with sufficient decimals.

The CDMs were generated using the selection rules and looked for in the peak list from Section 2 in order to assign the transitions. Due to the density of peaks and to the experimental accuracy, this method leads to a relatively important set of fortuitous detections, as discussed in ref. 22. To circumvent this issue, they suggested to display the upper energies associated with the CDMs in a reduced energy plot with respect to J' , (where $'$ denotes the upper state) for a given tunneling component (A or E) and for a given K' value, the reduced energy being defined as:

$$E'_r = E' - \frac{1}{2}(B'' + C'')J'(J' + 1), \quad (6)$$

where B'' and C'' are the ground state rotational constants. The reduced energy plots of the A component of methanol resulting from our pattern recognition algorithm are presented in Fig. 4, where K' was limited to 2. The complete reduced energy plots for both A and E components are given in the ESL.[†]

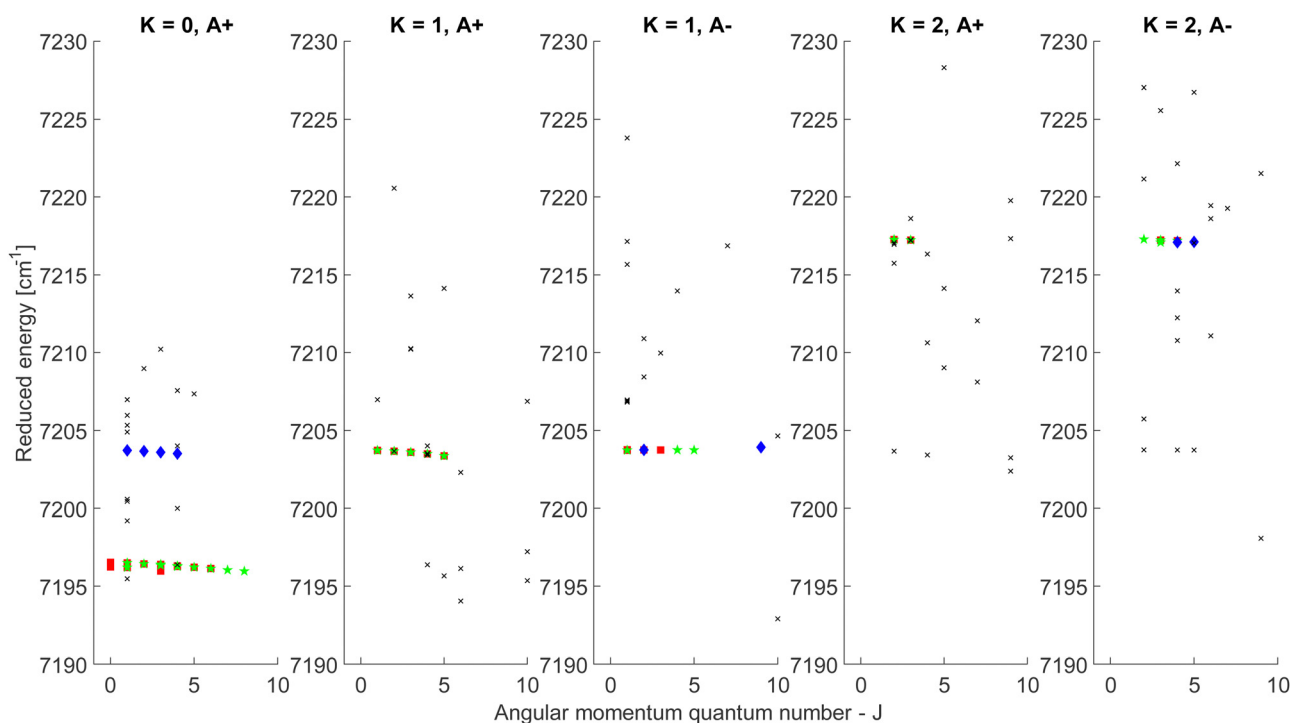


Fig. 4 Reduced energy plot of the A component of methanol. Black crosses are rejected CDMs, blue diamonds are tentative assignments and green stars are validated assignments. The red squares correspond to the CDMs previously detected by Rakvoský *et al.*²²



Because of the increased sensitivity of CRDS, the molecular fingerprint we measured contains about 2.5 times more peaks than the molecular spectrum recorded by Rakvoský *et al.*²² Under such conditions, the reduced energy plots look like clouds of scattered data and the chance of false identification of progressions in J' in the reduced energy plots increases. Another criterion is therefore required to separate “the wheat from the chaff”. We suggest using information on the intensities of the transitions as a second feature for distinguishing between fortuitous and confirmed assignments. While the experimental intensities, *i.e.* the area under the peaks, can be easily evaluated using the results from the fitting of the spectrum, a model is needed to compute the theoretical ones. Evaluation of the theoretical intensities is detailed in Section 3.2.

3.2. Evaluation of the relative intensities

Information on the relative intensities of the transitions belonging to a given CDM can be used as a way to distinguish between the correct assignments and fortuitous ones. On one side, the integrated absorption coefficient can be evaluated experimentally by evaluating the area under the peaks, *i.e.* the transitions, in the experimental spectrum measured with the CRDS setup. On the other side, a theoretical integrated absorption coefficient $\tilde{\alpha}_{ij}$ can be estimated using the following expression:^{41,42}

$$\tilde{\alpha}_{ij} = C \times \tilde{\nu}_{ij} \times \exp\left(\frac{-E_i}{kT_{\text{rot}}}\right) \times S_{ij} \quad (7)$$

where C is a constant value, $\tilde{\nu}_{ij}$ is the wavenumber of the

transition, E_i is the energy of the lower energy state involved in the transition and expressed in cm^{-1} , k is the Boltzmann constant in wavenumber per Kelvin, T_{rot} is the rotational temperature and S_{ij} the line strength. The constant value C is common to all transitions within a CDM and since we are interested in relative intensities, there is no need to evaluate it. In eqn (7), a factor $\left(1 - \exp\left(\frac{-\tilde{\nu}_{ij}}{kT}\right)\right)$ relative to the population of the upper state was neglected since $kT \ll \tilde{\nu}_{ij}$. An analytical expression of S_{ij} is required to evaluate the theoretical integrated absorption coefficient. For a rigid symmetric top molecule, which is nearly the case of methanol, and if we are only interested in relative intensities, the line strength S_{ij} depends only on the J and K values of the lower energy state:^{41,42}

- $\Delta K = 0, \Delta J = +1$ (R branch)

$$S_{ij} \propto m \frac{(J+K+1)(J-K+1)}{J+1} (2 - \delta_{K,0}) \quad (8)$$

- $\Delta K = 0, \Delta J = 0$ (Q branch)

$$S_{ij} \propto m \frac{K^2(2J+1)}{(J+1)J} (2 - \delta_{K,0}) \quad (9)$$

- $\Delta K = 0, \Delta J = -1$ (P branch)

$$S_{ij} \propto m \frac{(J+K)(J-K)}{J} (2 - \delta_{K,0}) \quad (10)$$

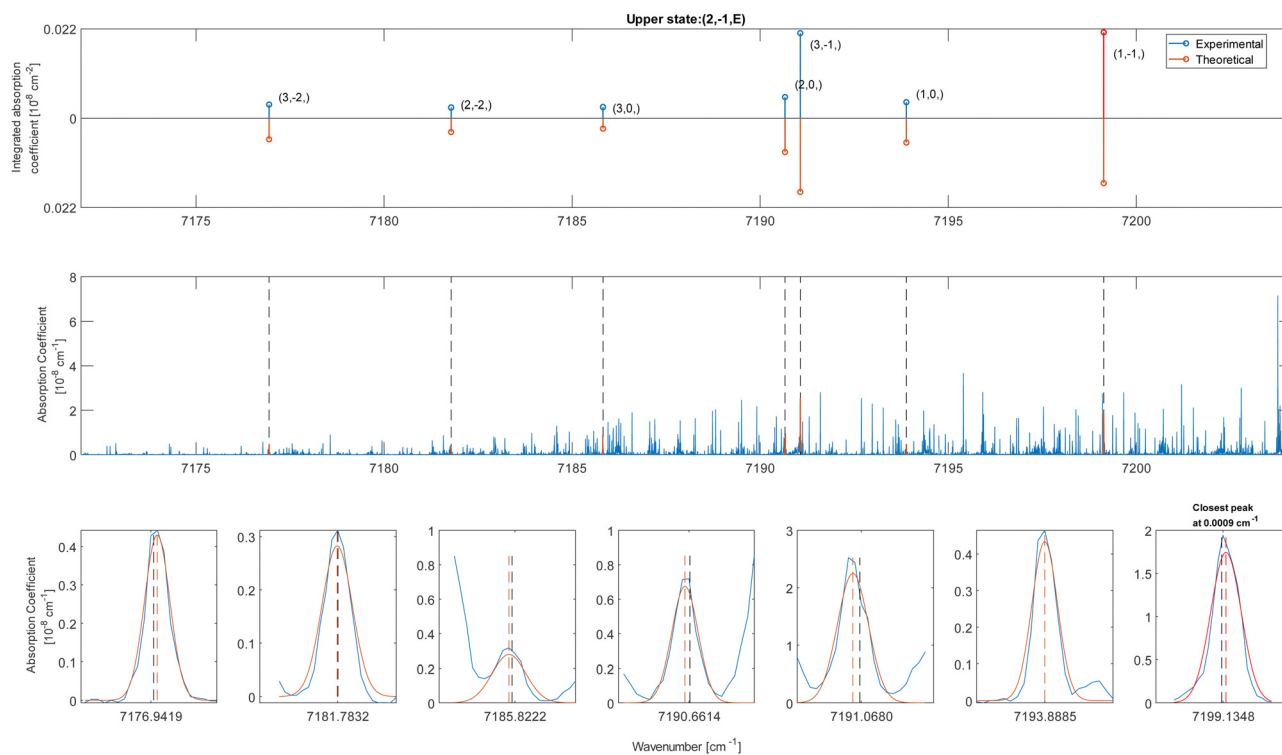


Fig. 5 Interface of the validation process of methanol CDMs. The upper panel compares the simulated and experimental absorption coefficients. The simulated data are normalized on the experimental ones to ease the comparison. The middle and lower panels respectively show the line positions on the spectrum and the peak fits.



- $\Delta K = \pm 1, \Delta J = +1$ (R branch)

$$S_{ij} \propto \frac{(J \pm K + 1)(J \pm K + 2)}{J + 1} \quad (11)$$

- $\Delta K = \pm 1, \Delta J = 0$ (Q branch)

$$S_{ij} \propto \frac{(J \pm K + 1)(J \mp K)(2J + 1)}{J(J + 1)} \quad (12)$$

- $\Delta K = \pm 1, \Delta J = -1$ (P branch)

$$S_{ij} \propto \frac{(J \mp K - 1)(J \mp K)}{J} \quad (13)$$

where m is a proportionality factor that weights the parallel transitions ($\Delta K = 0$) compared to the perpendicular ones ($\Delta K \neq 0$). These expressions can be employed in the computation of the integrated absorption coefficient α_{ij} given in eqn (7). Since the theoretical integrated absorption coefficient (evaluated with eqn (7)) depends only on the quantum numbers of the lower energy levels, it is thus possible to evaluate it for every transition belonging to a given CDM and to compare it to the observed integrated absorption coefficients in a relative manner. Fig. 5 shows the visual interface developed and used for the comparison between experimental and theoretical intensities. This interface pops up when clicking on any upper energy state displayed in the reduced energy plot of Fig. 4, allowing for line intensity inspection of the underlying CDM. In the upper frame of the interface presented in Fig. 5, both theoretical and experimental intensities are shown. The constant value C of eqn (7) used for the evaluation of the theoretical intensities, was computed using a least squares method to account for all the transitions of the CDM. The second frame shows how the transitions are spread over the molecular fingerprint and the last frame displays the Gaussian fits from which the experimental intensities are retrieved. Inspection of the individual peaks is required since a deviation between experimental and theoretical intensities in the upper frame can be due to partially overlapped peaks or issues in the automatic fitting procedure. Elements verified during the inspection include ensuring that the height, width, and position of the fit align overall with the experimental data and that the peak corresponds to an isolated transition. For instance, the transition at $7191.0680 \text{ cm}^{-1}$ in Fig. 5 seems to be composed of two lines. Furthermore, when a transition is missing in the sequence, the closest peak is displayed instead and the experimental intensity in the upper frame appears in red. Here again, visualizing the peak serves at ensuring the intensity in the upper frame is meaningful. This qualitative approach serves as a cross-check of the assignments made *via* the pattern recognition method. Indeed, for each upper energy state displayed in Fig. 4, a label is set depending on the belonging of the CDM to a progression in the J' value and on the match between theoretical and experimental intensities. If only one of the two features is met, then the CDM is labelled as tentative assignment, depicted by blue diamond in Fig. 4. If the two features are met, the CDM is labelled as validated assignment and a green star is displayed in the plot. Otherwise, the CDM is rejected. The red squares correspond to

the CDMs previously detected by Rakvoský *et al.*²² We've identified most of the patterns observed by Rakvoský *et al.*, yet our study reveals numerous additional patterns not previously documented. This gives confidence in our approach and makes it valuable for the automatic assignment of spectra based on pattern recognition methods. More specifically, 350 transitions were assigned based on the line intensity inspection of detected CDMs, including 162 from Rakvoský *et al.*²² Another 62 transitions which were assigned in²² were evaluated as tentative by our method. Lists with all the assigned transitions for both A and E components are given in the ESI.†

4 Conclusions

The spectral signature of methanol in the 2OH stretching region was recorded using a new apparatus combining a cw-CRDS and a buffer gas cooling cell. Even at low temperatures ($T_{\text{rot}} = 26 \text{ K}$), the assignment of such complicated spectrum appeared to be quite challenging.^{21,22} To tackle this difficulty, the technique suggested by Rakvoský²² was used, consisting in the detection of patterns in the position of the molecular transitions. Due to the large number of pattern detections, intensity information was included in the construction of the reference patterns. Reference intensities were evaluated using the analytical formula available for symmetric tops based on the nearly prolate character of this molecule. Using this extended approach, 162 transitions assigned by Rakvoský *et al.* were firmly confirmed and 48 others were tentatively confirmed. A further 188 transitions were firmly assigned and 14 more transitions were tentatively assigned. However, the challenge of digging into the complexity of methanol remains, with more than 2000 transitions observed but not yet assigned. We plan in the future to modify our set-up to improve significantly the accuracy in the determination of the line positions using a stabilized frequency comb to determine the wavenumber axis of the observed spectra. This will lead to a decrease of the erroneous detection of CDMs and thus an improvement of the efficiency of the assignment procedure. We also plan to simplify even further the molecular fingerprint by going lower in temperature with the fabrication of a new buffer gas cooling setup, going below 10 K. In these conditions, the pattern recognition method with the inclusion of the intensity information, which promises to be a relevant method for the assignment of complex spectral signatures often associated with the overtone range, could be fully automatized. This approach should prove to be particularly appropriate in the case of bands presenting a mixed character: parallel and perpendicular.

Author contributions

Alexis Libert: supervision, construction of the buffer gas cooling experiment, extension and implementation of the pattern recognition method, formal analysis, writing – original draft. Anthony Roucou: part of the collaboration on the buffer gas cooling cell and CW-CRDS preliminary testing, formal analysis,



extension of the pattern recognition method, writing – original draft. Brian Hays: recording of the final spectrum at the basis of the analysis. Robin Glorieux: work on the frequency calibration hardware and software development. Séverine Robert: part of the collaboration on the development of the buffer gas cooling cell and CW-CRDS. Baptiste Fabre: part of the collaboration on the development of the buffer gas cooling cell and CW-CRDS. Samir Kassi: improvement of the sensitivity of the CW-CRDS. Xavier Urbain: supervision of the experimental development. Clément Lauzin: supervision, extension of the pattern recognition method, funding acquisition, formal analysis, writing – original draft.

Conflicts of interest

There are no conflicts to declare.

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