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One-dimensional metal thiophosphate nanowires by cluster assembly<sup>†</sup>

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One-dimensional (1D) atomic wires with precise structures are not only excellent platforms for exploring novel 1D physics, but also promising building blocks to assemble functional materials and devices. However, stable atomic wires remain limited and are hard to search using global optimization algorithms. Inspired by the emerging layered ternary chalcogenides, here we offer a design strategy for rational assembly of metal thiophosphate (MPS<sub>4</sub>) nanowires based on the concept of a superatom. *ortho*-Thiophosphate [PS<sub>4</sub>] clusters are linked by proper main-group and transition metal atoms to form closed electronic shells, endowing the assembled nanowires with high dynamic and thermal

†Electronic supplementary information (ESI) available: Detailed structural parameters, stability, and electronic properties results of 1D, 2D and bulk MPS<sub>4</sub>. See DOI: https://doi.org/10.1039/d2nr03770j



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Dr Si Zhou is a professor at the School of Physics at Dalian University of Technology. She has focused on cluster science and low-dimensional materials using theoretical methods such as first-principles calculations and genetic algorithms. Her achievements include the prediction of many innovative lowdimensional structures for electronics, spintronics, optics, and energy conversion, some of which have been realized in

experiments. She has published over 90 peer-reviewed articles as the first- or corresponding-author in Chem. Rev., J. Am. Chem. Soc., Angew. Chem., Int. Ed., Nano Lett., ACS Nano, etc., with citations numbering over 6000 and an H-index of 39. stabilities. Diverse and exotic electronic band structures are hosted by these ternary  $MPS_4$  nanowires, such as the coexistence of a spin-orbit Dirac point protected by nonsymmorphic symmetry and a flat band near the Fermi level, with nanowires being bipolar magnetic semiconductors for electrical control of spin orientation. These 1D Lego blocks can be further built into higher-order architectures *via* vdW interaction or covalent bonding. This assembly approach generally produces stable atomic wires with designated compositions and structure symmetries to induce peculiar quantum states for future applications.

#### Introduction

With the boom of two-dimensional (2D) layered materials, searching for atomic-scale Lego blocks has aroused tremendous interest. Artificial nanostructures with peculiar physical properties and integrated devices with multiple functions can be conveniently constructed by assembly of these van der Waals (vdW) Lego units.<sup>1</sup> Stimulated by 2D transition metal dichalcogenides (TMDs) and trihalides, 1D atomic wires of binary transition metal compounds with various stoichiometries have been synthesized in experiments, such as the isolated chains of  $M_6X_6$  (M = Mo, W; X = S, Se, Te)<sup>2-5</sup> and  $Mo_5S_4$ ,<sup>6</sup> and the single-chain or the few-chain MTe<sub>3</sub> (M = Ti, Hf, Nb, V)<sup>7,8</sup> and NiY<sub>2</sub> (Y = Cl, Br)<sup>9</sup> stabilized in carbon nanotubes. The geometrical structures and fundamental properties of binary nanowires with different stoichiometries have been theoretically explored and compared with their 2D counterparts.<sup>10-13</sup> Intriguingly, most 1D transition metal chalcogenide nanowires exhibit metallic behavior, while a large number of TMD monolayers are semiconductors.14-16 Transition metal halide nanowires present diverse electronic and magnetic properties, somewhat similar to reported 2D halides (e.g. CrI<sub>3</sub>, FeCl<sub>2</sub>, and VI<sub>3</sub>) that comprise magnetic semiconductors and half metals.<sup>17-20</sup>

Recently, ternary metal phosphorus trichalcogenides in the form of MPX<sub>3</sub> (M = Mn, Fe, Co, Ni, Cu, Zn, Cd, *etc.*; X = S, Se)



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emerged as a new family of 2D materials.<sup>21</sup> They have a common layered structure with  $(P_2X_6)^{4-}$  bipyramids arranged in a triangular lattice that sandwich the metal layer. The MPX<sub>3</sub> monolayers have moderate band gaps of 1.5–3.5 eV falling in the range of visible light wavelengths, and are thereby attractive for optoelectronics, photodetectors, and photocatalysts.<sup>22</sup> Intrinsic long-range magnetic order exists in some 2D ternary compounds. For instance, antiferromagnetism is observed in MnPS<sub>3</sub>, FePS<sub>3</sub>, and NiPS<sub>3</sub> monolayers.<sup>23</sup> MnPS<sub>3</sub> exhibits the anisotropic behavior of magnetic moments, capable of coupling the valley degree of freedom to the antiferromagnetic order.<sup>24</sup> The CuInP<sub>2</sub>S<sub>6</sub> crystal and thin films have been demonstrated to be ferroelectric with an order to disorder transition temperature of 315 K. An out-of-plane electric polarization has been predicted for the CuInP<sub>2</sub>S<sub>6</sub> monolayer.<sup>25</sup>

Apparently, greater chemical diversity and structural complexity would induce richer physics in the 2D ternary compounds with regard to 2D binary chalcogenides and halides. It brings intriguing questions as to whether the atomic wires of ternary transition metal compounds can stably exist. How do their electronic structures depend on the elemental composition? How do their fundamental properties compare with those of their 2D counterparts? Computational screening the existing bulk materials with layered or chain-like structures has led to the discovery of many 2D and 1D materials.<sup>26-28</sup> The theoretical exfoliation energies can be used to evaluate the possibility for cleaving low-dimensional building blocks from their bulk crystals, that is, growth by the "top-down" approach. Then, the elemental substitution is useful to further extend the chemical compositions of monolayers or chains. However, such conventions only predict 2D and 1D materials with very limited structures, and omit a large number of possible structures that may be fabricated by the "bottom-up" approach on proper substrates or templates.

Here we develop a strategy for the rational design of 1D metal thiophosphate nanowires in the form of MPS<sub>4</sub> by cluster assembly. Based on the concept of a superatom, *ortho*-thiophosphate [PS<sub>4</sub>] units are linked by selective main-group metal atoms and transition metal atoms, such that the tetrahedral [PS<sub>4</sub>] cluster has a magic number of electrons to satisfy the electronic-shell closure. Following this assembly rule, a total of 26 MPS<sub>4</sub> nanowires are constructed. Their energetic, dynamic, and thermal stabilities are comprehensively examined by density functional theory (DFT) calculations to validate our assembly rule. The electronic and magnetic structures of these MPS<sub>4</sub> nanowires are investigated to illuminate their potential for device applications. The stable 1D MPS<sub>4</sub> building blocks are further exploited to assemble higher-order architectures.

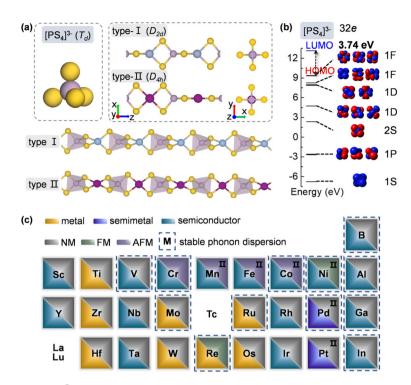
#### Computational methods

DFT calculations were carried out by the Vienna *ab initio* simulation package (VASP),<sup>29,30</sup> using the planewave basis set with an energy cutoff of 500 eV, the projector augmented wave (PAW) potentials,<sup>31,32</sup> and the generalized gradient approxi-

mation (GGA)<sup>33</sup> parametrized by Perdew, Burke and Ernzerhof (PBE) for the exchange-correlation functional.<sup>34</sup> A vacuum space of 15 Å was applied to the directions perpendicular to the axial direction of MPS4 nanowires. Uniform k-point meshes, with density 0.05  $\text{\AA}^{-1}$  and 0.0002  $\text{\AA}^{-1}$ , were used to sample the Brillouin zone of the nanowires for geometry optimization and band structure calculation, respectively.35 The cell parameters of MPS<sub>4</sub> nanowires along the axial direction were fully optimized and the ionic positions were relaxed with the convergence criteria for total energy and force of  $10^{-5}$ eV and 0.01 eV Å<sup>-1</sup>, respectively. The Heyd–Scuseria–Ernzerhof (HSE06) hybrid functional<sup>36</sup> was used to calculate the electronic band structures of simple metal thiophosphate nanowires assembled from group-IIIA atoms (B, Al, Ga, In) and [PS<sub>4</sub>] units, which predicts band gaps of about 1.2 eV larger than the values given by the PBE functional. For transition metal thiophosphate nanowires and monolayers, the DFT+Umethod<sup>37</sup> was adopted to compute their band structures to account for the strong correlation effect. For consistency, we used the Hubbard on-site Coulomb parameter U = 3 eV for all the transition metal MPS<sub>4</sub> nanowires. The obtained electronic band structures have features similar to those calculated by the PBE functional. Other U values were also tested, which generally affect the band gap, but do not influence the metallic systems. The detailed results obtained via different methods are compared in Table S1 and Fig. S1 of the ESI.<sup>†</sup> The phonon dispersion was calculated by the Phonopy code<sup>38</sup> interfaced with the density functional perturbation theory (DFPT) implemented in VASP. The thermal stability of the assembled MPS<sub>4</sub> nanowires was characterized by ab initio molecular dynamics (AIMD) simulations implemented in VASP. The molecular orbitals of a  $[PS_4]^{3-}$  cluster and natural population of the on-site charge were calculated by the Gaussian16 package,<sup>39</sup> using the PBE functional accompanied with LANL2DZ basis sets.

#### **Results and discussion**

To design metal thiophosphate nanowires, we consider the *ortho*-thiophosphate  $[PS_4]$  units in a tetrahedral geometry linked by metal atoms to form a chain, as illustrated in Fig. 1a. The rule for assembling MPS<sub>4</sub> nanowires is to reach stable electronic configurations for both [PS<sub>4</sub>] clusters and M atoms after their bonding. For highly symmetric clusters, the jellium model suggests that the molecular orbitals generated by valence electrons resemble the shapes of atomic orbitals.<sup>40</sup> A cluster will have enhanced stability when its number of valence electrons coincides with a closed-shell structure (socalled "magic number"). For a tetrahedral cluster with  $T_d$  symmetry, the molecular orbitals split in energy and the magic numbers can be determined as 2, 8, 10, 16, 20, 26, 32, etc.<sup>41</sup> As a free [PS<sub>4</sub>] unit carries 29 valence electrons, it has to gain three electrons from the M linkers to reach a magic number and electronic-shell closure. Intuitively, group-IIIA atoms (B, Al, Ga, and In) with three valence electrons, as well as tran-



**Fig. 1** (a) Geometrical structure of a  $[PS_4]^{3-}$  cluster (top left panel) and the assembled 1D MPS<sub>4</sub> nanowire (top right panel and bottom two panels) from different views. The P, S, and M atoms are shown in purple, yellow, and blue (magenta) colors, respectively. (b) Energy diagrams and molecular orbitals of  $[PS_4]^{3-}$ . The energy is relative to the vacuum level. The HOMO–LUMO gap is given. (c) Electronic and magnetic properties of 1D MPS<sub>4</sub> nanowires, where M is either a transition metal element or a group-IIIA element. The dashed boxes indicate nanowires with a stable phonon dispersion. The systems with type-II structures are indicated by the symbol "II" in the upper right corner.

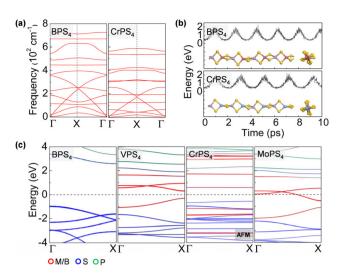
sition metal elements with open d shells and exhibiting variable oxidation states, may satisfy such criteria and form stable 1D nanowires with the  $[PS_4]$  unit.

Next, we constructed MPS<sub>4</sub> nanowires by linking [PS<sub>4</sub>] clusters with group-IIIA and transition metal atoms. To determine the ground-state geometry and magnetic order, we adopted different supercells  $(1 \times 1 \times 2 \text{ and } 1 \times 1 \times 4 \text{ unit cells})$  to arrange the adjacent [PS<sub>4</sub>] clusters in different orientations and tested different spin configurations for the magnetic atoms. As displayed in Fig. 1a, the two most stable structure phases are found for the assembled MPS<sub>4</sub> nanowires. In the type-I configuration, the adjacent [PS<sub>4</sub>] clusters are in the same orientation, such that each M atom stays in the center of S<sub>4</sub> tetrahedra as that of a P atom. The nanowire has  $D_{2d}$  symmetry and an M–S–P angle of about 90°. In the type-II configuration, the two adjacent [PS<sub>4</sub>] units rotate by 90° along the axial direction, such that each M atom stays in the center of the S<sub>4</sub> rectangle, resulting in  $D_{4h}$  symmetry for the nanowire.

Upon geometry optimization, all the considered 1D chains are stable. For both phases, the  $[PS_4]$  unit in the nanowire well maintains its tetrahedral structure. We examined the molecular orbitals of a free  $[PS_4]^{3-}$  ion, which mimics the  $[PS_4]$ building block in the MPS<sub>4</sub> nanowires. It exhibits highly symmetric superatomic orbitals, as displayed in Fig. 1b. The 32 valence electrons fill the electronic shell of  $1S^21P^62S^21D^{10}1F^61F^6||1F^0$  under the symmetry-adapted orbital model,<sup>41,42</sup> where the 1F orbital splits and the two lower energy levels are fully occupied, with a large gap of 3.74 eV between the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO). These results manifest the superatomic nature of the tetrahedral [PS<sub>4</sub>] cluster and indicate its high stability by gaining a proper number of electrons when assembled into MPS<sub>4</sub> nanowires.

The ground-state structure phases, electronic and magnetic properties, and dynamical stabilities of the assembled MPS<sub>4</sub> nanowires are summarized in Fig. 1c. Most of these 1D systems prefer the type-I structure with  $D_{2d}$  symmetry, while six MPS<sub>4</sub> nanowires (M = Mn, Fe, Co, Ni, Pd, and Pt) have the type-II structure with  $D_{4h}$  symmetry. In particular, there are 12 MPS<sub>4</sub> nanowires that have stable phonon dispersions (Fig. 2a and Fig. S2<sup>†</sup>), comprising either the group-IIIA elements (M = B, Al, Ga, and In) or selective transition metal elements (M = V,Cr, Co, Ni, Mo, Re, Ru, and Pd). We have also tested some other main group elements, such as those elements from group-IA (Na), group-IIA (Mg), group-IVA (Sn, Pb), and group-VA (Bi). Their assembled 1D MPS<sub>4</sub> structures are either broken down during optimization or have unstable phonon dispersions, which in turn corroborate our proposed assembly criteria. In the following content, we will focus on the 12 MPS<sub>4</sub> nanowires that are dynamically stable.

The thermal stability of  $MPS_4$  nanowires was assessed by an AIMD simulation. As depicted in Fig. 2b and Fig. S3,† single



**Fig. 2** (a) Phonon dispersions of BPS<sub>4</sub> and CrPS<sub>4</sub> nanowires. (b) Energy profile during AIMD simulation for BPS<sub>4</sub> and CrPS<sub>4</sub> nanowires at 300 K. The energy is referred to that of the equilibrium structure at 0 K. The insets are snapshot structures at 10 ps (left: side-view; right: top-view). The M, P, and S atoms are shown in blue (pink), purple, and yellow colors, respectively. (c) Electronic band structures of selective MPS<sub>4</sub> nanowires. The contributions from different atoms are shown by color. The Fermi level is shifted to zero (dashed lines).

chains of MPS<sub>4</sub> have outstanding thermal stability at 300 K. The structure does not show any noticeable distortion during a simulation time of 10 ps. Taking the BPS<sub>4</sub> and CrPS<sub>4</sub> nanowires as representatives, the variations of M–S and P–S bond lengths are within 0.14 Å and 0.19 Å for BPS<sub>4</sub> and 0.16 Å and 0.12 Å for CrPS<sub>4</sub>, respectively, signifying the structural robustness of these 1D ternary compound materials. We further characterized the energetic stability of 1D MPS<sub>4</sub> nanowires by their formation energy defined as,

$$E_{\text{form}} = E(\text{MPS}_4) - [E(H_3\text{PS}_4) - 3/2E(H_2)] - E(M)$$
 (1)

where  $E(MPS_4)$ ,  $E(H_3PS_4)$ , and  $E(H_2)$  are the total energies of MPS<sub>4</sub> nanowire per formula, a free H<sub>3</sub>PS<sub>4</sub> and H<sub>2</sub> molecule, respectively; E(M) is the energy of the M atom in its most stable bulk form. As presented in Tables 1 and 2, group-IIIA MPS<sub>4</sub> (M = B, Al, Ga, In) and 3d transition metal MPS<sub>4</sub> (M = V, Cr, Co Ni) nanowires have negative values of  $E_{form} = -1.44$  to -0.08 eV, while MoPS<sub>4</sub>, RuPS<sub>4</sub>, PdPS<sub>4</sub>, and RePS<sub>4</sub> nanowires have positive  $E_{form}$  values. A negative value of  $E_{form}$  indicates

**Table 1** Formation energy ( $E_{form}$ ) and band gap ( $E_g$ ) of 1D group-IIIA MPS<sub>4</sub> nanowires; inter-chain distance (*d*) and band gap ( $E_g$ ) of the assembled 3D MPS<sub>4</sub>

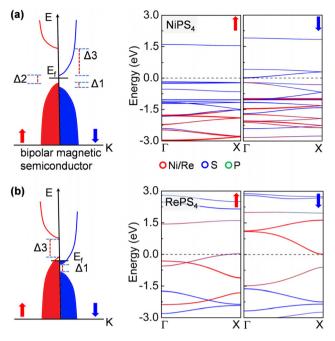
|                   | 1D                  |                                  | Bulk  |                                     |
|-------------------|---------------------|----------------------------------|-------|-------------------------------------|
|                   | $E_{\rm form}$ (eV) | $E_{\rm g}\left({\rm eV}\right)$ | d (Å) | $E_{\rm g} \left( {\rm eV} \right)$ |
| BPS <sub>4</sub>  | -0.93               | 3.57                             | 3.72  | 3.21                                |
| $AlPS_4$          | -2.42               | 4.14                             | 3.71  | 3.55                                |
| GaPS <sub>4</sub> | -1.34               | 4.01                             | 3.74  | 3.17                                |
| InPS <sub>4</sub> | -0.80               | 3.73                             | 3.82  | 3.12                                |

**Table 2** Magnetic state, band gap ( $E_g$ ), magnetic moment (M), and exchange energy ( $E_m$ ), of 1D transition metal MPS<sub>4</sub> nanowires and the assembled MPS<sub>4</sub> monolayers. Formation energy ( $E_{form}$ ) is also given for 1D MPS<sub>4</sub>. For ferromagnets, band gaps for spin-up and spin-down channels are provided

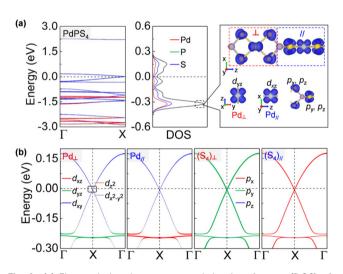
| 1D   | State                        | $E_{\rm g}\left({\rm eV}\right)$       | $M\left(\mu_{\mathrm{B}} ight)$ | $E_{\rm m}$ (meV)           | $E_{\rm form} \left( {\rm eV} \right)$ |
|--|------------------------------|--|---------------------------------|-----------------------------|--|
| VPS <sub>4</sub>   | NM                           | 0.60                                   | _                               | _                           | -1.21                                  |
| $CrPS_4$   | AFM                          | 1.15                                   | 2.78                            | -99                         | -1.44                                  |
| $CoPS_4$   | AFM                          | 0.81                                   | 1.53                            | -8                          | -0.16                                  |
| NiPS <sub>4</sub>  | FM                           | 1.73/0.22                              | 0.51                            | 26                          | -0.08                                  |
| MoPS <sub>4</sub>  | NM                           | Metal                                  | _                               | _                           | 0.13                                   |
| RuPS <sub>4</sub>  | NM                           | Metal                                  | _                               | _                           | 0.69                                   |
| $PdPS_4$   | NM                           | 0                                      | _                               | _                           | 0.06                                   |
| RePS <sub>4</sub>  | FM                           | 1.41/metal                             | 0.92                            | 44                          | 1.06                                   |
| 2D   | State                        | E (a)                                  | (7)                             | $\mathbf{M}(\mathbf{u})$    |  |
| 20   | State                        | $E_{\rm g} \left( {\rm e}^{2} \right)$ | <b>v</b> )                      | $M\left(\mu_{ m B} ight)$   | $E_{\rm m}$ (meV)                      |
| VPS <sub>4</sub>   | AFM                          | 0 .                                    | v)                              | M (μ <sub>B</sub> )<br>1.80 | $E_{\rm m}$ (mev)<br>-15               |
|  |                              | 0 .                                    |                                 | V/                          |  |
| VPS <sub>4</sub>   | AFM                          | 0.03                                   |                                 | 1.80                        | -15                                    |
| VPS <sub>4</sub><br>CrPS <sub>4</sub>  | AFM<br>FM                    | 0.03<br>0.66/<br>0.71                  | 1.69                            | 1.80                        | -15                                    |
| VPS <sub>4</sub><br>CrPS <sub>4</sub><br>CoPS <sub>4</sub>   | AFM<br>FM<br>NM              | 0.03<br>0.66/<br>0.71                  | 1.69<br>l                       | 1.80<br>2.91<br>—           | -15<br>6<br>                           |
| VPS <sub>4</sub><br>CrPS <sub>4</sub><br>CoPS <sub>4</sub><br>NiPS <sub>4</sub>                      | AFM<br>FM<br>NM<br>AFM       | 0.03<br>0.66/<br>0.71<br>Meta          | 1.69<br>l                       | 1.80<br>2.91<br>—           | -15<br>6<br>                           |
| VPS <sub>4</sub><br>CrPS <sub>4</sub><br>CoPS <sub>4</sub><br>NiPS <sub>4</sub><br>MoPS <sub>4</sub> | AFM<br>FM<br>NM<br>AFM<br>NM | 0.03<br>0.66/<br>0.71<br>Meta<br>Meta  | 1.69<br>l<br>l                  | 1.80<br>2.91<br>—           | -15<br>6<br>                           |

that the formation of an MPS<sub>4</sub> nanowire by metal ion substitution of  $H_3PS_4$  acid is exothermic. These proposed 1D MPS<sub>4</sub> nanowires may be synthesized by the assembly of  $[PS_4]^{3-}$  ions, and group-IIIA metal atoms or transition metal atoms in 1D templates with a hollow cavity. A variety of transition metal chalcogenide and halide chains have been grown by vapor transport in open-ended carbon nanotubes and boron nitride nanotubes in the experiment.<sup>3,43,44</sup>

The electronic band structures of the assembled MPS<sub>4</sub> nanowires are given in Fig. 2c, 3, 4 and Fig. S4.† The group-IIIA MPS<sub>4</sub> (M = B, Al, Ga, and In) nanowires are semiconductors with large band gaps of 3.57-4.14 eV predicted by the HSE06 hybrid functional. Encouragingly, these 1D ternary compounds exhibit diverse electronic and magnetic properties, including those of semiconductors, metals, semimetals, and ferromagnetic and antiferromagnetic semiconductors, and thereby serve as a rich family of 1D candidates for electronics, spintronics, and optoelectronics. We calculated the magnetic anisotropy energy (MAE) given by the energy difference of the magnetization direction parallel and perpendicular to the axial direction. Most of the magnetic MPS<sub>4</sub> nanowires have the easy-axis perpendicular to the chain with MAE values of 0.02-0.75 meV per magnetic atom. Only the CoPS<sub>4</sub> nanowire has the spin orientation along the chain direction in an antiferromagnetic order. As shown by the electronic band structures in Fig. 2c and Fig. S4,† CrPS<sub>4</sub> and CoPS<sub>4</sub> nanowires are both antiferromagnetic semiconductors with band gaps of 1.15 and 0.81 eV and magnetic moments of 2.78 and  $1.53\mu_{\rm B}$  per metal atom, respectively. The VPS<sub>4</sub> nanowire is a non-magnetic semiconductor with band gap of 0.60 eV, while the single chains of MoPS<sub>4</sub> and RuPS<sub>4</sub> exhibit metallic behavior. It is worth mentioning that



**Fig. 3** Electronic band structures of (a)  $NiPS_4$  and (b)  $RePS_4$  nanowires. The contributions from different atoms or orbitals are shown by the colors. The Fermi level is shifted to zero (red dashed lines). The left panels are schematic plots of their band structures.



**Fig. 4** (a) Electronic band structures and density of states (DOS) of a PdPS<sub>4</sub> nanowire calculated without SOC. The right panel displays the partial charge density of the flat band at about -0.3 eV. (b) Band structure of a PdPS<sub>4</sub> nanowire calculated with SOC. The contributions from different atoms or orbitals are shown by the colors. The Fermi level is shifted to zero (dashed lines).

the  $\text{CoPS}_4$  nanowire can have a non-collinear magnetic order, with the preference of spin orientation alternately parallel and perpendicular to the wire, as shown in Fig. S5.<sup>†</sup> However, the energy of the non-collinear magnetic order is 1.6–4.8 meV per Co atom higher than that of the collinear antiferromagnetic ground state.

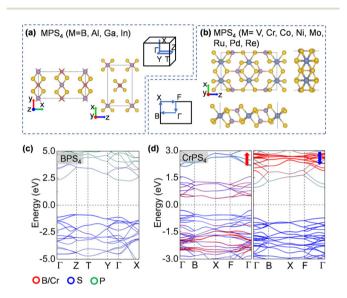
Remarkably, the NiPS<sub>4</sub> nanowire is a bipolar magnetic semiconductor, as is featured by its different conduction band minimum (CBM) and valence band maximum (VBM) in terms of electronic spins.<sup>45</sup> As shown in Fig. 3a, the VBM and CBM are contributed to by the majority and minority spin carriers, respectively, both from S atoms. There is a small gap of 0.20 eV, termed the spin-flip gap ( $\Delta_2$ ), between VBM and CBM. By applying a small positive (negative) gate voltage, the minority (majority) spin carriers are created, allowing for the electrical control of these carriers' spin orientations. The spin splitting near the Fermi level is mainly contributed to by S atoms. The RePS<sub>4</sub> chain exhibits similar features to that of NiPS<sub>4</sub>, but has no gap at the Fermi level. As displayed in Fig. 3b, the spin-up and spin-down channels are slightly doped. The electronic states near the Fermi level are dominated by Re atoms. When applying a small gate voltage, minority spin carriers are generated with a large spin-conserved gap  $(\Delta_3)$  of 1.46 eV, while a negative gate voltage is required to generate majority spin carriers with a large spin-conserved gap  $(\Delta_1)$  of 0.62 eV. Therefore, these nanowires can carry completely spin-polarized currents under a proper electric field, allowing for exciting applications, such as a bipolar field effect spin filter and field effect spin valve, as well as detection and separation of entangled electrons from superconductors for quantum information processing.46

More impressively, the PdPS<sub>4</sub> nanowire in the type-II configuration is a semimetal that is robust against spin-orbit coupling (SOC) protected by its nonsymmorphic symmetry.<sup>47</sup> As shown in Fig. 4a, the CBM and VBM touch each other nearly at the Fermi level. A gap is not opened by adopting denser k-points with 0.0001  $\text{\AA}^{-1}$ , larger SOC strength, or other *U* values (see Fig. S6<sup>†</sup>).<sup>48</sup> This type of Dirac point that is robust against SOC is termed a spin-orbit Dirac point (SDP) and is distinct in nature from the SOC-vulnerable Dirac point. It has been reported in some 2D materials, such as RhB4,49 MXenes<sup>50</sup> and HfGe<sub>0.92</sub>Te.<sup>51</sup> Even more excitingly, the PdPS<sub>4</sub> chain simultaneously harbors SDP and a nearly flat band near the Fermi level (at about -0.2 eV). A flat momentum-energy dispersion is the singularity in density of states, and the charge carriers in it have a zero group velocity and an infinite effective mass. It has been realized in Kagome lattice systems, graphene twisted bilayer and transition metal diachalcogenides,<sup>52-55</sup> and may lead to high-temperature superconductivity, fractional Chern insulators, Wigner crystal formations, and so on.<sup>56</sup> According to the density of states in Fig. 4a and b, the flat band of a PdPS<sub>4</sub> nanowire is localized on the Pd-S<sub>4</sub> planar unit, contributed to by the S p orbital and Pd d orbital perpendicular to the  $Pd-S_4$  plane. As the neighboring Pd-S<sub>4</sub> units are perpendicular to each other, their orbital hybridization is very weak, which may be the origin of the flat dispersion. Therefore, the PdPS<sub>4</sub> nanowire with its unique structure is a great 1D platform for exploring the coexistence of multiple exotic quantum states.

Next, we explore the possibility of assembling these 1D  $MPS_4$  building blocks into higher-order architectures. The interaction between two  $MPS_4$  nanowires is examined. Our

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results show that the group-IIIA MPS<sub>4</sub> (M = B, Al, Ga, In) nanowires favor vdW interactions between neighboring chains, while the transition metal MPS<sub>4</sub> nanowires are covalently bonded when approaching each other. As a result, group-IIIA MPS<sub>4</sub> (M = B, Al, Ga, In) nanowires form quasi-1D bulk structures as illustrated in Fig. 5a. The supercell consists of parallel MPS<sub>4</sub> chains arranged in a rectangular lattice. The chains in the center and at the corner of the supercell are shifted along the axial direction. The vertical distance between the center atoms of two neighboring nanowires is about 6.0 Å, and the separation between the outermost S atoms of two neighboring

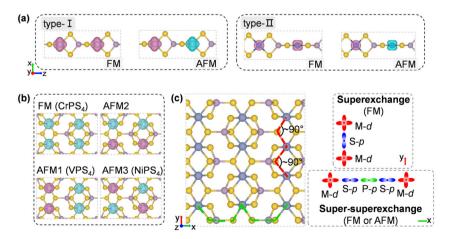


**Fig. 5** (a) and (b) Atomic structures of assembled bulk MPS<sub>4</sub> (M = B, Al, Ga, In) and an MPS<sub>4</sub> (M = V, Cr, Co, Ni, Mo, Ru, Pd, and Re) monolayer, respectively, displayed from different perspectives. The M, P, and S atoms are shown in blue (pink), purple, and yellow colors, respectively. The corresponding Brillouin zones are illustrated. (c) and (d) Electronic band structures of assembled bulk BPS<sub>4</sub> and monolayer CrPS<sub>4</sub>, respectively. The contributions from different atoms or orbitals are shown by color. The Fermi level is shifted to zero (dashed lines).

nanowires is more than 3.7 Å (see Table 1), manifesting the vdW interactions between them. Accordingly, needle-shaped crystallites of the above quasi-1D BPS4 and AlPS4 have been synthesized experimentally.57,58 Fig. 5c and Fig. S7† display the electronic band structures of three-dimensional (3D) MPS<sub>4</sub> by HSE06 calculations. The band gaps of bulk MPS<sub>4</sub> (M = B, Al, Ga, In) are reduced to 3.12-3.55 eV with regard to the single chains. The band along the inter-chain direction is dispersive owing to the moderate interaction between neighboring chains. The band dispersions along the inter-chain direction and axial direction are noticeably different, implying the anisotropic electronic transport behavior of these unique quasi-1D structures, which are desirable for certain device applications, such as anisotropic field effect transistors and photodetectors, thermoelectronics, piezoelectric and and ferroelectric devices.59,60

The transition-metal-containing  $MPS_4$  (M = V, Cr, Co, Ni, Mo, Ru, Pd, and Re) nanowires favor covalent bonding between adjacent chains, leading to the formation of the monolayer structure shown in Fig. 5b. The tetrahedral [PS<sub>4</sub>] unit is slightly deformed, while each Cr atom is six-fold coordinated by S atoms and surrounded by four [PS<sub>4</sub>] units, resulting in an anisotropic rectangular lattice structure. Actually, such a layered structure of CrPS<sub>4</sub> has been synthesized in the experiment,<sup>61,62</sup> which again corroborates our proposed assembly rule for building stable nanostructures *via*  $[PS_4]$  clusters. As shown in Fig. 5d, the CrPS<sub>4</sub> monolayer is a ferromagnetic semiconductor with a magnetic moment of  $2.91\mu_{\rm B}$  per Cr atom, and band gap of 0.66 eV and 1.69 eV for the spin-up and spin-down channels, respectively, in good agreement with previous theoretical reports.<sup>63</sup> The VPS<sub>4</sub> and NiPS<sub>4</sub> monolayers are antiferromagnets, while the others are non-magnetic (see Table 2 and Fig. S8<sup>†</sup> for details). The magnetic moment prefers to align perpendicular to the layer for all these 2D magnets.

The robustness of the magnetism in cluster-assembled 1D and 2D MPS<sub>4</sub> structures is evaluated by the exchange energy  $E_{\rm m}$ , defined as the energy difference between the lowest-lying



**Fig. 6** (a) and (b) Spin density distributions of an MPS<sub>4</sub> nanowire and MPS<sub>4</sub> monolayer in FM and low-energy AFM states. The ground-state magnetic configuration is indicated for VPS<sub>4</sub>, CrPS<sub>4</sub>, and NiPS<sub>4</sub> monolayers, respectively. (c) Schematic illustration of superexchange and super-superexchange interactions for the MPS<sub>4</sub> monolayer.

antiferromagnetic state ( $E_{AFM}$ ) and ferromagnetic state ( $E_{FM}$ ) per MPS<sub>4</sub> formula *via*:

$$E_{\rm m} = E_{\rm AFM} - E_{\rm FM} \tag{2}$$

Spin-polarized charge density distributions for FM and lowenergy AFM configurations of 1D and 2D MPS<sub>4</sub> structures are presented in Fig. 6a and b. The 1D nanowires of CrPS<sub>4</sub>, CoPS<sub>4</sub>, NiPS<sub>4</sub> and RePS<sub>4</sub> have  $E_{\rm m}$  = -99 meV, -8 meV, 26 meV, and 44 meV per formula unit (f.u.), respectively (Table 2). Their magnetic orders can be understood by the super-superexchange interaction along the M-S-P-S-M long superexchange interaction through the Cr-S-Cr bonds with a bond angle of about 90°, as shown in Fig. 6c.64-67 VPS4 and NiPS4 monolayers are antiferromagnetic with  $E_{\rm m} = -15$  meV f.u.<sup>-1</sup> and -27 meV f.u.<sup>-1</sup>, respectively. The former shows competition between FM and AFM coupling along the two in-plane directions, while the latter favors AFM order along both in-plane directions. As a reference, an existing 2D magnetic material like the CrI<sub>3</sub> monolayer has  $E_{\rm m}$  = 28 meV f.u.<sup>-1</sup> and a measured Curie temperature of about 45 K;<sup>19</sup> the MnPS<sub>3</sub> monolayer has  $E_m =$ -13 meV f.u.<sup>-1</sup> and a measured Néel temperature of about 103 K.68 The present 1D MPS<sub>4</sub> nanowires have exchange energies competitive with the values of synthetic 2D magnetic materials, offering stable building blocks for integration of heterostructures and devices with desirable functions.

## Conclusions

In summary, based on the superatom concept, we exploited the tetrahedral  $[PS_4]$  cluster as a building block to construct assemblies of different dimensions by DFT calculations. Ternary MPS<sub>4</sub> nanowires with outstanding dynamic and thermal stabilities are obtained by linking  $[PS_4]$  units with group-IIIA (B, Al, Ga, and In) atoms or transition metal (V, Cr, Co, Ni, Mo, Ru, Pd, and Re) atoms. The assembled nanowires with unique structure symmetries exhibit diverse and peculiar electronic band structures, such as the coexistence of a SOC Dirac point and a nearly flat band, and being bipolar magnetic semiconductors. Moreover, these MPS<sub>4</sub> nanowires can be further assembled into quasi-1D bulk structures *via* vdW interactions as well as layered 2D structures by covalent bonding that are feasible in the experiment.

#### Conflicts of interest

There are no conflicts to declare.

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