

## RESEARCH ARTICLE

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## Multi-step cation substitution facilitating the exploration of potential infrared nonlinear optical materials†

Ya-Xiang Han,<sup>a,b</sup> Chun-Li Hu,<sup>a</sup> Wen-Tong Chen<sup>c</sup> and Jiang-Gao Mao <sup>\*a</sup>

Crystal structure regulation and optical performance enhancement are huge challenges, especially for the laborious and inefficient trial-and-error method, in the research on infrared nonlinear optical (IR NLO) materials. In this work, multi-step cation substitutions were adopted to modulate the crystal structure for the effective design of well-performing IR NLO materials. Specifically, starting from the famous AgGaS<sub>2</sub> (AGS, *I4̄2d*) crystal, Ag<sub>2</sub>CdSiS<sub>4</sub> (*Pmn2<sub>1</sub>*) with diamond-like crystal structure, BaAg<sub>2</sub>SiS<sub>4</sub> (*I4̄2m*) with three-dimensional tunnel structure and LaAgSiS<sub>4</sub> (*Ama2*) with two-dimensional layer structure were designed and experimentally synthesized through multi-step cation substitutions. Structural analysis reveals the fundamental reason of their tetrahedral framework transformation: the size effect of cations and the reduction of component tetrahedra caused by cationic substitution change the assembly mode of the tetrahedral units. Additionally, three non-centrosymmetric Ag-based thiosilicates exhibit wide transmittance range (0.5–17 μm), higher laser-induced damage thresholds (2 times that of AGS) and significant phase-matchable second harmonic generation (SHG) enhancement from 0.6 to 3.2 times that of AGS. This work demonstrates that multi-step cation substitution is an effective way to extend non-centrosymmetric structures, which facilitate the exploration of potential infrared nonlinear optical materials.

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## Introduction

With the advancement of optical fields such as optical communication, optical imaging, laser guidance, and environmental monitoring,<sup>1–4</sup> there is a growing demand for infrared nonlinear optical (IR NLO) crystals with exceptional properties including large second harmonic generation (SHG) response, phase matching capabilities (suitable  $\Delta n$ ), high laser-induced damage threshold (LIDT), wide light transmission range, and good physical and chemical stability.<sup>5</sup> Prominent commercially available IR NLO materials include chalcopyrite-type

ionic crystals AgGaS<sub>2</sub> (AGS), AgGaSe<sub>2</sub> (AGSe), and ZnGeP<sub>2</sub> (ZGP), which are known for their large second harmonic generation (SHG) responses and broad IR transparency. However, their potential applications are significantly constrained by inherent limitations, including a low laser induced damage threshold (LIDT), poor phase matching ability and harmful two-photon absorption.<sup>6–8</sup>

Great efforts have been devoted to the exploration of new IR SHG materials.<sup>9–12</sup> A series of tetrahedron-based compounds, such as AgGa<sub>2</sub>PS<sub>6</sub> (1 × AGS), Hg<sub>3</sub>P<sub>2</sub>S<sub>8</sub> (4.2 × AGS) and Li<sub>4</sub>MgGe<sub>2</sub>S<sub>7</sub> (0.7 × AGS), were produced by combinations between different tetrahedral active groups.<sup>13–16</sup> Choosing [AsS<sub>3</sub>]<sup>3–</sup> and [SbS<sub>3</sub>]<sup>3–</sup> anions with stereochemical lone pair electrons or  $\pi$ -conjugated planar triangular [BS<sub>3</sub>]<sup>3–</sup> as infrared nonlinear optical genes led to the isolation of new IR SHG crystals such as LaBS<sub>3</sub> (1.2 × AGS) and BaHgSe<sub>2</sub> (1.5 × AGS).<sup>17–20</sup> Alkaline-earth or transition metal cations were introduced to adjust the band gaps as in BaGa<sub>4</sub>S<sub>7</sub> (0.9 × AGS) and Cd<sub>4</sub>SiS<sub>6</sub> (1.3 × AGS).<sup>21–26</sup> Searching for new IR NLO material systems, such as pnictides, oxyhalides and adducts, led to the discovery of new materials such as RuSi<sub>4</sub>P<sub>4</sub> (1.4 × AGS), Pb<sub>17</sub>O<sub>8</sub>Cl<sub>18</sub> (2 × AGS), Pb<sub>18</sub>O<sub>8</sub>Cl<sub>15</sub>I<sub>5</sub> (1 × AGS) and (CuBr)<sub>7</sub>(P<sub>4</sub>Se<sub>3</sub>)<sub>3</sub> (3.5 × AGS).<sup>27–31</sup>

Despite great achievements, most previous explorations are based on the laborious and inefficient trial-and-error synthetic

<sup>a</sup>State Key Laboratory of Structural Chemistry, Fujian Institute of Research on the Structure of Matter, Chinese Academy of Sciences, Fuzhou, 350002, P. R. China.

E-mail: mjj@fjirsm.ac.cn

<sup>b</sup>University of Chinese Academy of Sciences, Beijing 100039, P. R. China

<sup>c</sup>Institute of Applied Chemistry, School of Chemistry and Chemical Engineering, Ji'an Key Laboratory of Photoelectric Crystal Materials and Device, Jiangxi Province Key Laboratory of Coordination Chemistry, Humic Acid Utilization Engineering Research Center of Jiangxi Province, Jinggangshan University, Ji'an, Jiangxi 343009, China

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methods.<sup>32</sup> Researchers are starting to find more efficient ways to design new IR NLO materials. One good way is based on computer-assisted structure and optical property prediction, which led to the discovery of  $\text{Zn}_3(\text{PS}_4)_2$  ( $52 \times \text{KH}_2\text{PO}_4$ ),  $\text{Zn}_2\text{BS}_3\text{Br}$  ( $2 \times \text{AGS}$ ), *etc.*<sup>33–35</sup> Another strategy is to screen potential nonlinear optical materials, such as  $\text{LiGaSe}_2$  ( $2 \times \text{AGS}$ ), from the database.<sup>36</sup> In addition, chemical substitutions were also considered an effective way to explore novel nonlinear optical crystals. For example,  $\text{BiFSeO}_3$  with strong SHG response of 13.5 times than that of  $\text{KH}_2(\text{PO})_4$  at 1064 nm was obtained using  $[\text{SeO}_3]^{2-}$  and  $\text{F}^-$  to simultaneously aliovalently substitute the  $[\text{IO}_3]^-$  and  $\text{O}^{2-}$  anions.<sup>37</sup> However, in previous reports, such works have only involved single-step substitution and similar crystal structures. Related systematic studies on structure and performance regulation are scarce, prompting us to utilize multi-step cation substitutions to extend more crystal structure types.<sup>38,39</sup>

To experimentally prove the effectiveness of multi-step cation substitution, the famous AGS was selected as the template due to its dominant diamond-like structure.<sup>40–44</sup> First,  $\text{Ag}_2\text{CdSiS}_4$  with a similar diamond-like structure was designed using one  $\text{Cd}^{2+}$  and one  $\text{Si}^{4+}$  to substitute two  $\text{Ga}^{3+}$  in AGS. Second, to preliminarily break the tetrahedral close-packed framework,  $\text{Ba}^{2+}$  with larger radius was adopted to substitute  $\text{Cd}^{2+}$  in  $\text{Ag}_2\text{CdSiS}_4$ , producing the three-dimensional tunnel structural  $\text{BaAg}_2\text{SiS}_4$ . Finally, by substituting one  $\text{Ba}^{2+}$  and one  $\text{Ag}^+$  with a  $\text{La}^{3+}$ ,  $\text{LaAgSiS}_4$  was created, forming two-dimensional  $[\text{AgSiS}_4]^{3-}$  layers with interlayer space filled by  $\text{La}^{3+}$  cations. Although  $\text{Ag}_2\text{CdSiS}_4$  and  $\text{BaAg}_2\text{SiS}_4$  were reported before, related studies on systematic structure regulation and IR NLO property are still absent.<sup>45,46</sup> Structure analysis revealed the fundamental reasons of the tetrahedral framework transformation: the size effect of cations and the reduction of the component tetrahedra caused by cationic substitution change the assembly mode of basic tetrahedral units. Furthermore,  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$  crystals exhibit wide transmittance range (0.5–17  $\mu\text{m}$ ), relatively high laser-induced damage thresholds (2 times that of AGS) and significant phase matchable SHG response enhancement (0.6, 1.4 and 3.2 times of AGS). Our work proves that multi-step cation substitution is an effective method to explore potential IR NLO crystals.

## Results and discussion

### Phase analysis

Single crystals of  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$  were obtained through high-temperature solid state reactions under vacuum (ESI, Fig. S1†). Due to the deviations in the exposure of the sample's crystal planes from the ideal ones, even though the experimental and theoretical powder X-ray diffraction patterns may not look very similar, their purities are still confirmed by the same characteristic peak positions (Fig. S2†). The molar ratios of  $\text{Ag}:\text{M}:\text{Si}:\text{S}$  obtained by energy-dispersive X-ray spectroscopy are 2.1:1:1:4, 1:2.1:1.1:3.9 and

1:1.1:1.1:4.1 for  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$ , respectively, which are in good agreement with those determined from crystal structure analyses (Fig. S3†).

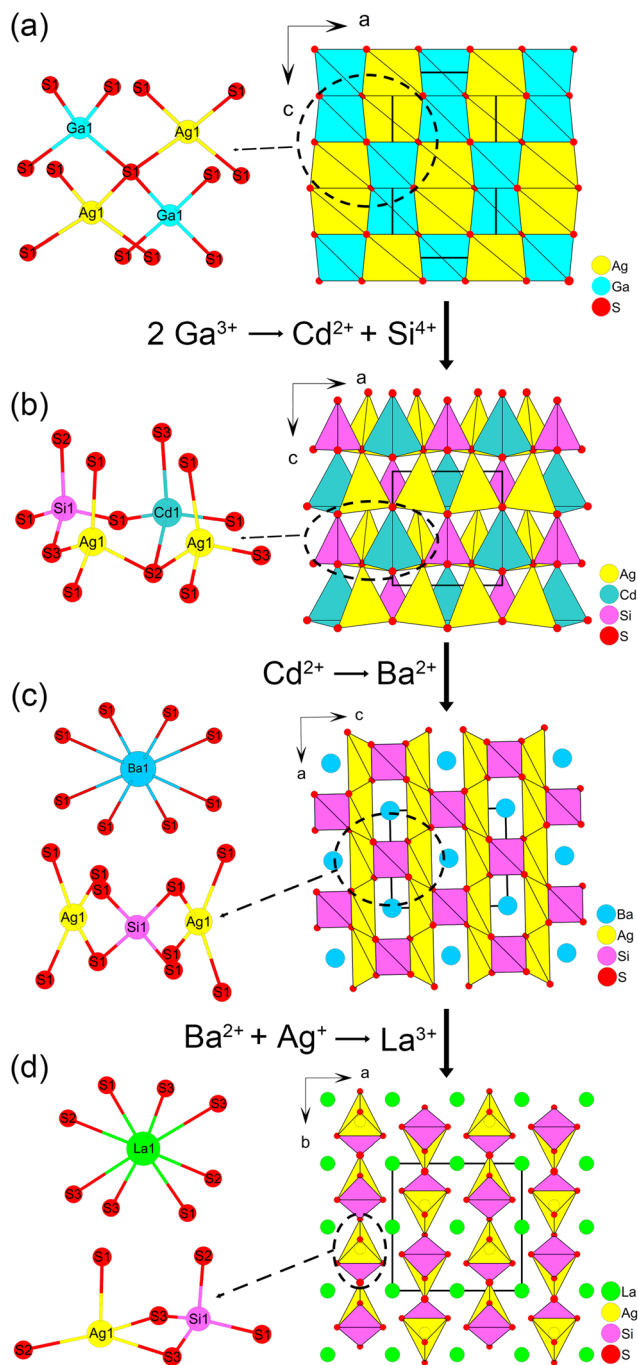
### Crystal structures

Similar to AGS,  $\text{Ag}_2\text{CdSiS}_4$  features a three-dimensional diamond-like crystal structure that is close-packed by the vertex-shared  $\text{AgS}_4$ ,  $\text{CdS}_4$  and  $\text{SiS}_4$  tetrahedra (Fig. 1a and b).  $\text{Ag}_2\text{CdSiS}_4$  crystallizes in the orthorhombic polar space group  $Pmn2_1$  (no. 31) (Table S1†). Its asymmetric unit consists of one Ag (4b), one Cd (2a), one Si (2a) and 3 S atoms occupying two 2a and one 4b sites (Table S2†). However, when two  $\text{Ga}^{3+}$  cations were replaced by one  $\text{Cd}^{2+}$  and one  $\text{Si}^{4+}$ , the  $\text{AgS}_4$ ,  $\text{CdS}_4$  and  $\text{SiS}_4$  tetrahedra in  $\text{Ag}_2\text{CdSiS}_4$  exhibits obvious distortion due to the mismatch of geometric sizes, which is manifested in the bond length elongation of the  $\text{Ag}(1)-\text{S}(1)\#2$  (2.973(5) Å),  $\text{Cd}(1)-\text{S}(2)\#6$  (2.929(8) Å) and  $\text{Si}(1)-\text{S}(3)\#7$  (2.456(8) Å) (Table S3†). This case indicates that substitution between different component tetrahedra only change their arrangements and distortions but the diamond-like tetrahedral framework is retained.

To induce structural transformation, the  $\text{Cd}^{2+}$  ions in  $\text{Ag}_2\text{CdSiS}_4$  were replaced by larger  $\text{Ba}^{2+}$  cations.  $\text{BaAg}_2\text{SiS}_4$  crystallize in the tetragonal space group  $I4_2m$  (Table S1†), and its asymmetric unit contains one Ba (2a), one Ag (4d), one Si (2b), and one S (8i) atom. As shown in Fig. 1b, the  $\text{Ba}^{2+}$  ion is eight-coordinated by surrounding atoms in a distorted bicapped trigonal prismatic geometry, with Ba–S bond lengths ranging from 3.236(12) to 3.301(13) Å. Both Ag and Si are tetrahedrally coordinated by S atoms with Ag–S distance of 2.5997(11) Å and Si–S distance of 2.1245(3) Å (Table S3†). The vertex-sharing interconnection of  $\text{AgS}_4$  and  $\text{SiS}_4$  tetrahedra result in a three-dimensional open anionic framework with 1D tunnels of 4-member rings, which are filled by charge-balance  $\text{Ba}^{2+}$  cations (Fig. 1c).

In order to further reduce the dimensionality of the tetrahedral anionic framework, the  $\text{La}^{3+}$  with higher valence was chosen to simultaneously substitute one  $\text{Ba}^{2+}$  and one  $\text{Ag}^+$  in  $\text{BaAg}_2\text{SiS}_4$ .  $\text{LaAgSiS}_4$  crystallizes in the orthorhombic polar space group  $Ama2$  (no. 40). The asymmetric unit of  $\text{LaAgSiS}_4$  contains one La (4a), one Ag (4b) and three S (4b and 8c) atoms. The  $\text{La}^{3+}$  cation is eight-coordinated by surrounding S atoms in a  $\text{LaS}_8$  bicapped trigonal prism geometry, with the La–S distances varying from 2.924(3) to 3.089(4) Å. Both Ag and Si are tetrahedrally coordinated by S atoms with Ag–S and Si–S distances in the range of 2.495(5)–2.727(4) and 2.117(5)–2.147(7) Å, respectively (Table S3†). When  $\text{Ba}^{2+}$  was substituted by  $\text{La}^{3+}$  with higher positive charge, one half of  $\text{Ag}^+$  in the anionic framework was eliminated. This led to a change in the connection mode between neighboring tetrahedral groups to sharing both the edge and corner, producing two-dimensional  $[\text{AgSiS}_4]^{3-}$  layers. These anionic  $[\text{AgSiS}_4]^{3-}$  layers are packed in an ABAB... pattern along the *a*-axis and separated by the  $\text{La}^{3+}$  cations (Fig. 1d).





**Fig. 1** Vertex-shared  $\text{AgS}_4$ ,  $\text{GaS}_4$  tetrahedra; three-dimensional diamond-like  $\text{AgGa}_2\text{Si}_4$  crystal structures (a); vertex-shared  $\text{AgS}_4$ ,  $\text{CdS}_4$  and  $\text{SiS}_4$  tetrahedra; three-dimensional tetrahedra closed-packed  $\text{AgCdSi}_4$  crystal structures (b); coordination environment of  $\text{Ba}^{2+}$ ; vertex-shared  $\text{AgS}_4$  and  $\text{SiS}_4$  tetrahedra; three-dimensional tunnel structure of  $\text{BaAg}_2\text{Si}_4$  (c); coordination environment of  $\text{La}^{3+}$ ; edge-shared  $\text{AgS}_4$  and  $\text{SiS}_4$  tetrahedra; crystal structure of  $\text{LaAgSi}_4$  composed of  $[\text{AgSi}_4\text{Si}_4]^{3-}$  layers (d).

### Cation substitution-induced tetrahedral framework transformation

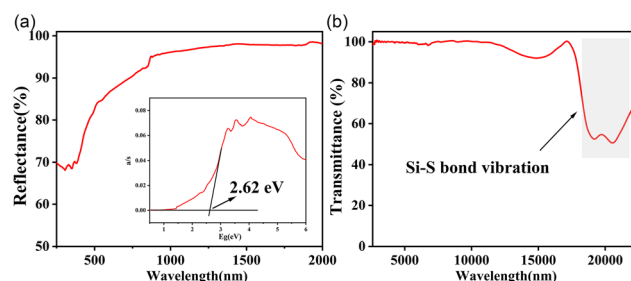
The crystal structure evolution of three compounds reveals that stepwise cationic substitution from a diamond-like struc-

ture is an effective way to extend new structures. To explore the underlying mechanisms, the minimal repeating unit of tetrahedral frameworks was analyzed. As shown in Fig. 1, from  $\text{Ag}_2\text{CdSi}_4$  to  $\text{BaAg}_2\text{Si}_4$  then to  $\text{LaAgSi}_4$ , accompanied with stepwise substitutions of higher valence cations, the component  $\text{CdS}_4$  and  $\text{AgS}_4$  tetrahedra in the minimal repeating unit of the tetrahedral frameworks are correspondingly reduced. This reduction of the component tetrahedra not only changes the connection mode of the tetrahedra but also the packing fashion to achieve the corresponding overall frameworks. On the other hand, the larger sizes of  $\text{Ba}^{2+}$  and  $\text{La}^{3+}$  cations also aid the formation of tunnels and layers in the tetrahedral frameworks, according to the theory of dimensional reduction.<sup>47</sup> Therefore, the size effect of cations and the reduction of component tetrahedra caused by cation substitutions are the fundamental reasons why the tetrahedral frameworks of three Ag-based quaternary thiosilicates transform from a three-dimensional close-packed structure to a tunneling structure and finally to a two-dimensional layer. In fact, the above analysis also coincides Mei *et al.*'s review on the tetrahedron-based infrared nonlinear materials that the tetrahedral arrangement pattern will evolve with the ratio of metal to tetrahedra.<sup>41</sup>

### Optical properties

As shown in the infrared spectrum, the powder samples of all the three compounds exhibit good light transmission in the 2.5–17  $\mu\text{m}$  band, which indicate that the asymmetric  $\text{Ag}_2\text{CdSi}_4$ ,  $\text{BaAg}_2\text{Si}_4$  and  $\text{LaAgSi}_4$  could be potential infrared nonlinear optical materials. The absorption band near 500  $\text{cm}^{-1}$  is attributed to the Si–S bond vibration, and the splitting vibration modes may be caused by the  $\text{SiS}_4$  tetrahedral distortion (Fig. 2b and S4†).

According to the UV-vis-NIR diffuse reflectance spectrum (Fig. 2a and S5†), the experimental band gap values of  $\text{Ag}_2\text{CdSi}_4$ ,  $\text{BaAg}_2\text{Si}_4$  and  $\text{LaAgSi}_4$  were measured to be 2.56, 2.32, and 2.62 eV, respectively, which are similar to that of AGS (2.72 eV) and match their yellow crystal colors. The unexpected smaller band gap value of  $\text{BaAg}_2\text{Si}_4$  agree with the reported one, which can be attributed to the outer 5d orbital of  $\text{Ba}^{2+}$ .<sup>46</sup> Combining the IR spectrum, the title compounds exhibit wide transmittance range from 0.5 to 17  $\mu\text{m}$ .



**Fig. 2** UV-vis-IR diffuse reflectance spectrum (a) and Fourier transform infrared spectrum (b) of  $\text{LaAgSi}_4$ .

Particle size-dependent SHG response measurements revealed that three asymmetric  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$  crystals exhibit phase-matchable SHG response intensity of 0.6, 1.4 and 3.2 times that of AGS under  $2.05\ \mu\text{m}$  laser irradiation (Fig. 3a and b). By comparing the SHG effect of new and reported thiosilicates, it can be found that  $\text{LaAgSiS}_4$  achieves the largest SHG effect among known thiosilicates (Fig. 3c).<sup>48–57</sup> Moreover, the SHG effect of title compounds are also comparable to similar thiogermanates and thiogstannates, such as  $\text{Li}_2\text{CdGeS}_4$  ( $1 \times \text{AGSe}$ ),  $\text{BaAg}_2\text{GeS}_4$  ( $1.7 \times \text{AGS}$ ),  $\text{BaAg}_2\text{SnS}_4$  ( $0.4 \times \text{AGS}$ ), and  $\text{BaCdSnS}_4$  ( $0.7 \times \text{AGS}$ ).<sup>58–65</sup>

Interestingly, from  $\text{Ag}_2\text{CdSiS}_4$  to  $\text{LaAgSiS}_4$ , their SHG responses increase with the reducing dimensionality of the tetrahedral frameworks. In order to understand the origin of the large SHG difference between polar structural  $\text{Ag}_2\text{CdSiS}_4$  and  $\text{LaAgSiS}_4$ , their local dipole moments of each fundamental group and unit cell were calculated based on the atomic coordinates. As listed in Table S4,<sup>†</sup> although the local dipole moments of  $\text{SiS}_4$  and  $\text{AgS}_4$  tetrahedral groups in both compounds are very close, the net dipole moments of per unit cell in  $\text{LaAgSiS}_4$  (54.060 D) are much larger than that of  $\text{Ag}_2\text{CdSiS}_4$  (18.028 D). This indicates that after the introduction of cations, the crystal structures achieve a more ordered arrangement of active groups in  $\text{LaAgSiS}_4$ , which is conducive to the superposition of strong microscopic SHG responses.

The LIDT tests were performed on the single crystals in the  $150\text{--}210\ \mu\text{m}$  particle size range with AGS as the reference. The results show that the LIDTs of  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$  are about twice of that of AGS (Table S5<sup>†</sup>), which may be attributed to the stronger Si–S covalent bonds compared

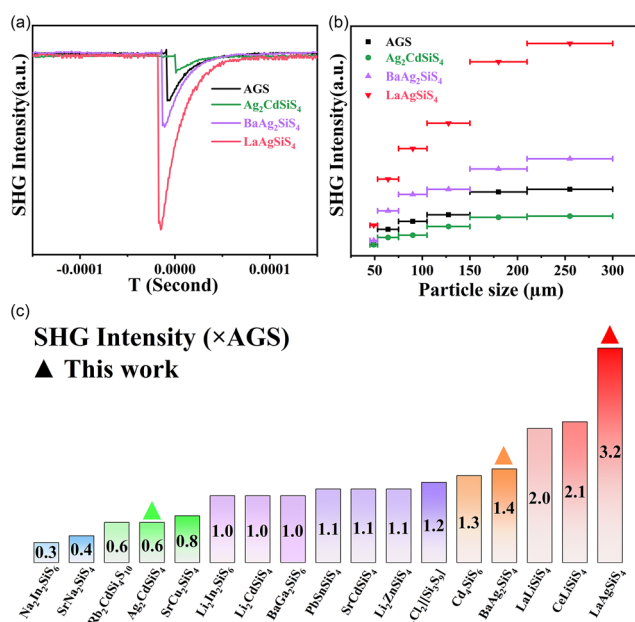
with Ga–S bonds and the introduction of strong Ba–S or La–S ionic bonds. In conclusion,  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$  achieve excellent IR NLO properties including large phase matchable SHG effect, wide IR transparent range and high LIDT.

### Theoretical calculations

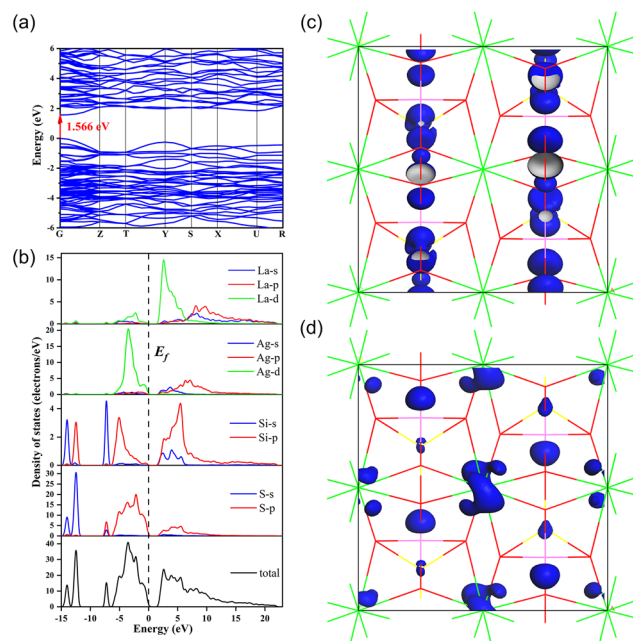
To further understand the relationship between the structures and properties of the title compounds, first-principles calculations based on DFT methods were performed.<sup>66,67</sup> The theoretical band gap values of  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$ , and  $\text{LaAgSiS}_4$  were calculated to be 1.13, 0.90, 1.57, respectively, which are much smaller compared to the experimental values due to the limitations of the GGA method (Fig. 4a and S6<sup>†</sup>).

The partial density of states (DOS) analysis revealed the band gap contributions of title compounds (Fig. 4b and S7<sup>†</sup>). For all the  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$  compounds, the Ag 4d and S 3p orbitals dominated the topmost valence bands (VB). The bottom of the conduction bands (CB), however, are not only contributed by the empty Ag-5s, 5p and unoccupied S-3p orbitals but also dominated by the outer 5d empty orbitals of the heavy cations. Overall, the band gaps of the three compounds are mainly determined by the  $\text{AgS}_4$  group, which explains why they exhibit similar direct band gap values.

The theoretical birefringence values ( $\Delta n$ ) of  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$  were calculated to be 0.070, 0.169 and 0.080, respectively (Fig. S8<sup>†</sup>). The suitable  $\Delta n$  of three asymmetric compounds coincide their phase-matching abilities. Given that all three crystal structural frameworks are composed of  $\text{AgS}_4$  and  $\text{SiS}_4$  tetrahedra, the apparent difference in  $\Delta n$  can be attributed to different tetrahedral arrangements.



**Fig. 3** Particle size-dependent SHG intensity curve for  $\text{Ag}_2\text{CdSiS}_4$ ,  $\text{BaAg}_2\text{SiS}_4$  and  $\text{LaAgSiS}_4$  (a and b); SHG intensity near  $2\ \mu\text{m}$  for the title and typical reported thiosilicates (c).



**Fig. 4** Calculated band structures (a) and partial density of states (b) and SHG density plots [VB (c) and CB (d)] for  $\text{LaAgSiS}_4$ .



Remarkably, the large theoretical birefringence value ( $\Delta n$ ) of  $\text{BaAg}_2\text{Si}_4$  breaks the bias that highly symmetric tetrahedral groups cannot generate large optical anisotropy. Proper crystal structure design is also essential to obtain large optical anisotropy.

The effective NLO coefficients ( $d_{\text{eff}}$ ) of  $\text{Ag}_2\text{CdSi}_4$ ,  $\text{BaAg}_2\text{Si}_4$  and  $\text{LaAgSi}_4$  were calculated to be 7.05, 6.43 and 13.16 pm  $\text{V}^{-1}$  under the restriction of space group and Kleinman's symmetry, respectively, which agree with the experimental results that  $\text{LaAgSi}_4$  achieves a much larger SHG effect. It is worth mentioning that small deviations between experimental and theoretical values may be due to the fact that the experimental samples are powders but the theoretical samples are simulated grown single crystals. The SHG-weighted electron density (SHG density) plots intuitively display the distribution of the source of SHG effects in their crystal structure. As shown in Fig. 4c, d and S9,† in the valence band, the SHG effects originate from the Ag 4d electronic states and S 3p non-bonding states for all three compounds, while in the conduction band, the SHG process is contributed by the unoccupied Ag 5s, Si 3p, and S 3p electronic states for  $\text{Ag}_2\text{CdSi}_4$  and  $\text{BaAg}_2\text{Si}_4$  and by the unoccupied La 5d, Ag 5s, and Si 3p electronic states for  $\text{LaAgSi}_4$ . The different origins of the SHG effect also explain why they exhibit a large difference in the SHG performance. Furthermore, the contribution percentages of each structure building group were obtained by integrating the SHG density over VB and CB, which turns out to be 34.33%, 44.72% and 20.95% for  $\text{SiS}_4$ ,  $\text{AgS}_4$  and  $\text{CdS}_4$  groups in  $\text{Ag}_2\text{CdSi}_4$ ; 46.04%, 44.96% and 9.00% for  $\text{SiS}_4$ ,  $\text{AgS}_4$  and  $\text{Ba}^{2+}$  in  $\text{BaAg}_2\text{Si}_4$ ; 32.88%, 26.25% and 40.87% for  $\text{SiS}_4$ ,  $\text{AgS}_4$  and  $\text{LaS}_8$  groups in  $\text{LaAgSi}_4$ , respectively. For  $\text{Ag}_2\text{CdSi}_4$  and  $\text{BaAg}_2\text{Si}_4$ , the tetrahedral group dominates the SHG contribution, while for  $\text{LaAgSi}_4$ , the  $\text{LaS}_8$  group contributes more, which emphasizes the benefits of adopting multi-step cation substitution to introduce well-performing functional crystal material genes.

## Conclusions

In summary, three quaternary thiosilicates, namely,  $\text{Ag}_2\text{CdSi}_4$ ,  $\text{BaAg}_2\text{Si}_4$  and  $\text{LaAgSi}_4$ , were designed and synthesized successfully through multi-step cation substitutions from AGS. Interestingly, their tetrahedral frameworks transform from a three-dimensional close-packed structure to a tunneling structure and finally to a two-dimensional layered structure, which was essentially caused by the size effect of cations and the cation substitution-induced component tetrahedra reduction. In addition, as IR NLO materials,  $\text{Ag}_2\text{CdSi}_4$ ,  $\text{BaAg}_2\text{Si}_4$  and  $\text{LaAgSi}_4$  crystals exhibit wide transmittance range (0.5–17  $\mu\text{m}$ ), relatively high laser-induced damage thresholds (2 times that of AGS), phase-matching ability, and significant SHG response enhancement (0.6, 1.4 and 3.2 times of AGS, respectively), which results from the more ordered arrangement of active groups induced by cationic substitution. Theoretical calculations suggest that the large SHG effects of  $\text{LaAgSi}_4$  originated from not only  $\text{SiS}_4$  and  $\text{AgS}_4$  tetrahedral

groups but also from the active  $\text{LaS}_8$  cationic genes introduced through multi-step cation substitution. This work demonstrates the multi-step substitution-induced crystal structure transformation and nonlinear optical performance enhancement, indicating that multi-step cation substitution is an effective method to explore potential functional IR NLO crystal materials.

## Data availability

Supporting data for this article is presented in the ESI.† The raw data of this article can be obtained by contacting the corresponding author.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

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