



## Chiral optical scattering from helical and twisted silica nanoribbons†

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**Helical and twisted silica nanoribbons, deposited in an in-plane direction and with a random orientation, on a quartz substrate showed chiral optical scattering, and the helical nanoribbons had a g-factor of the order of 10<sup>-2</sup> below 250 nm. Their signs depend on the handedness of the nanohelices. The effect of the morphology and the orientation of the helices on the chiral optical scattering were investigated with simulations via the boundary element method.**

The investigation of the chirality of solid materials has been the focus of intensive studies. While these studies have been performed mainly on crystalline and/or periodic structures,<sup>1</sup> non-crystalline (non-ordered and non-periodic structures) materials also have the potential to show promising chiral properties.<sup>2</sup> An interesting example is that of amorphous (non-crystalline) chiral silica synthesized *via* the sol-gel condensation of silica alkoxide with chiral organic molecular assemblies as templates. Numerous helical (morphologically chiral) nano-materials have been synthesized.<sup>3</sup>

In general, the optical activity (OA) observed from solid materials can be classified into three contributions: (i) absorption- and emission-based OA,<sup>1f,4</sup> (ii) refraction-based OA<sup>5</sup> and (iii) elastic scattering or non-elastic Raman scattering-based OA.<sup>6</sup> Absorption- and emission-based OA are the difference in the absorption or emission of left-handed (LH) and right-handed (RH) circularly polarized (CP) light. Absorption-based OA (circular dichroism (CD)) has been widely studied for electronic-transition OA and vibrational OA. Emission-based

OA corresponds to circularly polarized luminescence (CPL). Refraction-based OA (circular birefringence) comes from the difference in the velocities of LH-CP light and RH-CP light that pass through the OA medium, which is determined by the different refractive indices of the material for the RH- and LH-CP light. In contrast to electron transitions such as light absorption and emission, light scattering from nanometric or submicrometric materials shows interesting optical properties such as fadeless coloring in the UV-vis region<sup>7</sup> based on the elastic light scattering. Scattering based OA comes from the scattering at the surfaces having different refractive indices from the surrounding media and having chiral structure. Due to the no-energy loss process, elastic scattering can lead to a number of promising applications. Meanwhile, the scattering-based OA observed from solid particles, which typically have high refractive indices, is often mixed with absorbance-based OA; therefore, the contributions of the two need to be separated. Indeed, in the transmission mode of UV-vis and CD spectrometers, the variation of the photon number through absorbance or scattering mechanisms is difficult to distinguish.

We have previously shown that silica nanohelices can be obtained *via* the sol-gel reaction of tetraethoxysilane (TEOS) using molecular assemblies of the chiral surfactant (C<sub>2</sub>H<sub>4</sub>-1,2-((CH<sub>3</sub>)<sub>2</sub>N<sup>+</sup>C<sub>16</sub>H<sub>33</sub>)<sub>2</sub> with a tartrate counterion) as the organic template<sup>8</sup> (Fig. S1, ESI†). With L- or D-tartrate as the counterion, RH- or LH-nanohelices are obtained, respectively. These silica nanohelices show strong vibrational circular dichroism (VCD) signals at the Si-O-Si asymmetric stretching vibrational band,<sup>3f</sup> but due to the transparency of silica in the UV-vis range, no electronic CD is expected. However, when dried on a substrate, these chiral silica nanoribbons show strong scattering in the UV range, which dominates the extinction and the absorption-based CD signals due to the high refractive index of silica. Therefore, when measuring the electronic CD signals it is very important to understand how the scattering affects the chiroptical signals with respect to the absorption-based signals. In this manuscript, we investigate and compare the optically

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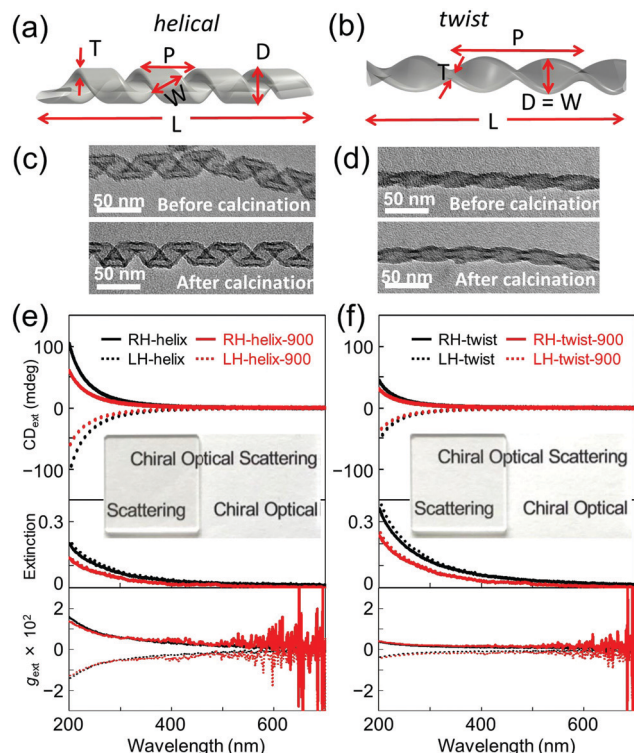
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**Fig. 1** 3D illustrations of RH- (a) helical and (b) twisted silica nanoribbons. TEM images of RH- (c) helical and (d) twisted silica nanoribbons.  $CD_{ext}$  (top), extinction (middle), and  $g$ -factor (bottom) spectra of drop-cast films ( $50 \mu\text{g cm}^{-2}$ ) of (e) helical and (f) twisted silica nanoribbons. Inset images show photos of the films of helical and twisted silica ribbons ( $50 \mu\text{g cm}^{-2}$ ) showing the good transparency of the films.

active absorbance and scattering of helical/twisted silica nanoribbons using a CD spectrometer with or without an integration sphere and compare with the results obtained *via* simulation.

In order to investigate the effect of the scattering and absorbance of individualized silica nanohelices, their suspension was subjected to ultrasonication to create a homogeneous suspension of short nanohelices in ethanol.<sup>8b</sup> The suspension was drop-casted onto a  $2 \times 2 \text{ cm}^2$  quartz substrate. These silica helices were then calcined at  $900 \text{ }^\circ\text{C}$  directly on the quartz plate for 2 hours. As we have previously reported,<sup>3f</sup> the silica nanohelices shrink after calcination and the dimensions measured from TEM images are compared on 200 points as shown in Table S1 (ESI<sup>†</sup>). In Fig. 1a and b, the schematic images show the various dimensions for the helical and twisted ribbons: the pitch ( $P$ ), width ( $W$ ), diameter ( $D$ ), length ( $L$ ), and thickness ( $T$ ) of the ribbons are shown.

The signals of absorbance and CD measured using the CD apparatus in transmission mode are based on the extinction, which includes both scattering and absorbance contributions, which we will call extinction and  $CD_{ext}$ , respectively, hereafter. When the silica nanohelices are dispersed in ethanol, the extinction increases in the UV range below 300 nm; meanwhile, no  $CD_{ext}$  is observed (Fig. S2, ESI<sup>†</sup>). When they are drop-casted onto the quartz substrates, the obtained transparent films showed strong extinction and  $CD_{ext}$  signals in the UV range.

In Fig. 1c and d, we show the TEM images of RH-helical and -twisted nanoribbons before and after calcination. In Fig. 1e and f, the extinction and  $CD_{ext}$  observed from helical and twisted silica nanoribbons are shown for both the RH- and LH-ribbons before and after calcination at  $900 \text{ }^\circ\text{C}$ . The extinction tails towards the wavelength up to 600 nm. Mirror-image  $CD_{ext}$  signals were observed for RH- (positive) and LH-nanohelices (negative). All the  $CD_{ext}$  signals of the films were obtained from the mean data of the  $CD_{ext}$  measured at two angles of  $0^\circ$  and  $90^\circ$  and the linear dichroism (LD) signals (less than  $5 \times 10^{-4}$ ) were measured in parallel (Fig. S3 and S4, ESI<sup>†</sup>). Both extinction and  $CD_{ext}$  signals decrease upon calcination. The  $CD_{ext}$  signals of the helical nanoribbons are higher than those of the twisted ribbon.

In order to quantify the contribution of the (chiral) scattering and absorbance from the silica nanohelices separately,  $CD_{abs}$  measurements of drop-casted silica helix films were performed in diffuse reflection CD (DRCD) mode with various setups (ESI<sup>†</sup>) for which the scattered light is collected using the integration sphere on the CD apparatus. The results of DRCD and absorbance (or extinction) of the RH- and LH-helical and -twisted silica nanoribbons are shown in Fig. S5, S13 and S14 (ESI<sup>†</sup>), respectively.<sup>9</sup> Very small  $CD_{abs}$  signals ( $\sim 2 \text{ mdeg}$ ) were observed at around 200–250 nm compared to  $\sim 100 \text{ mdeg}$  for  $CD_{ext}$  signals, which correspond to impurities (*e.g.*, OH or dissolved  $\text{O}_2$  molecules) and nonstoichiometric vacancies (*e.g.*, oxygen).<sup>10</sup> The amplitudes of the absorbance and  $CD_{abs}$  intensities in the UV range are much smaller ( $\sim 1/10$  and  $\sim 1/33$ , respectively, at  $\sim 200 \text{ nm}$ ) than that of the extinction and  $CD_{ext}$ , indicating that the scattering and the chiral optical scattering (COS) signals are the dominant origin of the extinction and  $CD_{ext}$ . Again, upon calcination at  $900 \text{ }^\circ\text{C}$ , both the absorbance and  $CD_{abs}$  decreased.

Hereafter, we focus on the scattering intensity and the COS. As seen from Table S1 (ESI<sup>†</sup>), both the helical and twisted nanoribbons shrink after calcination in all dimensions (the pitch, the diameter and the length). This is directly reflected in the decrease of the scattering intensity. In order to investigate how this shrinking affects the COS, we compared the  $g$ -factors, which correspond to the normalization of the  $CD_{ext}$  by the extinction. For both helical and twist ribbons, the  $g$ -factors before and after calcination are shown in Fig. 1e and f. No significant modification was observed both for the helical and twisted ribbons after calcination. For both morphologies, they showed a continuous decrease with increasing wavelength, showing a  $g$ -factor of  $\sim 0.015$  (at 200 nm) for the helical ribbons and  $\sim 0.0035$  (at 200 nm) for the twisted ribbons.

We then simulated the extinction and  $CD_{ext}$  values as well as the scattering cross-section and  $CD_{scat}$  values (Fig. 2 and Fig. S7, ESI<sup>†</sup>) of the individual helical and twisted silica ribbons before and after calcination using the measured values shown in Table S1 (ESI<sup>†</sup>), using the boundary element method (BEM), as described in the ESI<sup>†</sup><sup>11</sup> using the dielectric function of silica given by Palik<sup>12</sup> while ambient air is used as the medium. The simulations are performed by considering that the light beam is perpendicular to the helical/twisted ribbon (in-plane with the





Fig. 2 (a) Simulated extinction cross-section, (b)  $CD_{ext}$ , and (c)  $g$ -factors of helical and twisted silica nanoribbons.

substrate).  $CD_{ext}$  and extinction cross-section values are very close to the  $CD_{scat}$  and scattering cross-section values, respectively (Fig S7, ESI<sup>†</sup>), while the contribution of absorbance and  $CD_{abs}$  is negligible, in good agreement with the experimental results. Thus, in the following discussion,  $CD_{ext}$  is assimilated to  $CD_{scat}$ . Interestingly, the  $CD_{scat}$  and the  $g$ -factors for helical ribbons are higher than those for twisted ribbons, also in good agreement with the experimental observations. In Fig S8 (ESI<sup>†</sup>), we show the simulation of the two structures in which we compare how the vectors perpendicular to the surface are arranged along the ribbons. These results show that the vectors at the surface of a twisted ribbon rotate with the highest angle only at the center of the ribbon, whereas those of a helical ribbon rotate all together with the same highest angle.

We then investigated how modification of the pitch and length of the ribbons affects the scattering intensities, the  $CD_{ext}$  values and the  $g$ -factors. Fig. S9 (ESI<sup>†</sup>) shows the simulations of how the  $g$ -factor at a wavelength of 200 nm evolves with the length (at a fixed pitch and diameter) and pitch (at a fixed length and diameter), respectively, of a single helical or twisted ribbon. The corresponding extinction and  $CD_{ext}$  values are shown in Fig. S10 (ESI<sup>†</sup>). The incident light is perpendicular to the axis of the helix. We observe clearly that for pitches and lengths in the range of the helical and twisted ribbons observed for the present system ( $P$ , 25–150 nm;  $L$ , 200–500 nm), the  $g$ -factors of the COS signals do not vary much as both the cross-section and  $CD_{scat}$  decrease for the calcined helices with decreased dimension. As shown in Fig. S10 (ESI<sup>†</sup>), when the size of the ribbon decreases during the calcination, both  $CD_{ext}$  and extinction vary in the same direction ( $CD_{ext} \uparrow$  and extinction  $\uparrow$  for increasing  $L$ , whereas both  $CD_{ext} \downarrow$  and extinction  $\downarrow$  for increasing  $P$ ) compensating the variation in each other.

Globally, these simulated data are in very good agreement with the experimental data. A slight difference is likely due to the fact that the simulation is done on one helix whereas the measurements are done on the ensemble of helices with large size polydispersities (Fig. 3), leading to inter-helix scattering. Also, the variation in the refractive index of silica before and after calcination is not taken into account in the simulation. Indeed, the refractive index should depend on the density of the helices.

Finally, we compared the effect of the quantity of silica nanoribbons on the substrates. As shown in Fig. 3, various thicknesses of silica nanoribbon films were prepared on the  $2 \times 2 \text{ cm}^2$  quartz substrates and the extinction and  $CD_{ext}$  values were measured. While the intensity of the extinction increased



Fig. 3 Thickness dependence of the silica nanohelix films on (a) the scattering ( $Ext - Abs$ ) at 200 nm, (b) COS ( $|CD_{ext} - CD_{abs}|$ ), and (c)  $g$ -factor of the COS ( $|g_{ext-abs}|$ ). The original spectra are shown in Fig. S11 (ESI<sup>†</sup>). (d) SEM images of the surface (top) and cross-section (bottom) of helical silica nanoribbon films with different thicknesses. Scale bars, 1  $\mu\text{m}$ . (e) Proposed mechanisms of COS from nanohelix films. Yellow, red, and blue arrows are non-chiral scattered light from the quartz substrate, COS from in-plane helices, and opposite-handed COS from the out-of-plane helices respectively. (f) Simulated  $CD_{ext}$  of a helical nanoribbon oriented in-plane (red line) and out-of-plane (blue line) (Fig. S17, ESI<sup>†</sup>).

linearly with the quantity of silica nanoribbons (Fig. 3a),  $CD_{ext}$  intensity increased much more slowly beyond  $50 \mu\text{g cm}^{-2}$  of silica nanohelices (Fig. 3b), and the  $g$ -factor over this range decreased (Fig. 3c) with the concentration of helices. Scanning electron microscope (SEM) images confirmed that  $25 \mu\text{g cm}^{-2}$  of silica nanoribbons was enough to homogeneously cover the quartz surface of the substrate (Fig. 3d). In order to understand the decrease in the COS signal ( $g$ -factor) for the larger quantities of silica helices, we investigated the effect of the orientation (in-plane or out-of-plane of a helix on the COS signal by simulation. As shown in Fig. 3f and Fig. S17 (ESI<sup>†</sup>), the out-of-plane helix showed an opposite simulated  $CD_{ext}$  signal from that of the in-plane helix.<sup>13</sup> Although a similar coverage of the surfaces was observed for the top views of all the films, the cross-section SEM images of these films clearly showed the difference in their thicknesses. For the 25 and  $50 \mu\text{g cm}^{-2}$  films, the silica layer thicknesses (0.18  $\mu\text{m}$  and 0.35  $\mu\text{m}$ , respectively), are thinner than the average length of the silica nanohelices. On the other hand, in the case of the  $200 \mu\text{g cm}^{-2}$  film, the silica layer (3.2  $\mu\text{m}$ ) is thicker than the average length of the silica nanohelices. These results indicate that in the thinner layer ( $< 50 \mu\text{g cm}^{-2}$ ), only in-plane orientation is allowed, whilst in the thicker layers ( $> 100 \mu\text{g cm}^{-2}$ ), in-plane and out-of-plane orientations of silica nanohelices (Fig. 3e) can co-exist. Also, electromagnetic interaction between helices in the thicker layers of helices and the multiple scattering can perturb the polarization of the scattered light. These results can be compared with the drop-casted films of cut and non-cut nanoribbons (Fig. S12, ESI<sup>†</sup>). Non-cut silica nanoribbons show a smaller COS. In both cases, either for the highly concentrated



drop-cast film or the non-cut film, silica nanohelices are strongly aggregated in 3D directions with a high proportion of out-of-plane helices.

We investigated the chiral optical scattering from helical and twisted silica nanoribbons deposited on substrates parallel to the surface with random in-plane orientation. Using a CD spectrometer in both transmission and diffuse reflection mode, we demonstrated that the contribution of the absorbance and absorbance-based CD is present but negligible compared with the scattering and COS. Helical ribbons show larger COS and *g*-factors compared with twisted ribbons. For both morphologies, the variation of *g*-factor was negligible after calcination. All these results are in good agreement with the simulation performed on a single helix oriented perpendicular to the incoming light. The simulation of the COS on a helix oriented parallel to the incoming light shows the opposite signal from that of the helix oriented perpendicularly, which is probably the origin of the decrease in COS for the aggregated helices which contain the helices oriented out of plane. The *g*-factors observed for helical ribbons are of the order of  $10^{-2}$ , which is surprisingly high for materials made from silica alone. Thus, the strategy shown here represents an original and promising method to create fadeless circular polarizers while keeping good transparency in the visible range, with one of the most abundant inorganic atoms, Si, and O by simple coating of silica nanohelices on transparent films.

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## Conflicts of interest

There are no conflicts to declare.

## Notes and references

- (a) C. W. Bunn and E. R. Howells, *Nature*, 1954, **174**, 549–551; (b) T. Matsuura and H. Koshima, *J. Photochem. Photobiol., C*, 2005, **6**, 7–24; (c) O. Vogl, *J. Polym. Sci., Part A: Polym. Chem.*, 2011, **49**, 1299–1308; (d) K. Akagi, *Science*, 1998, **282**, 1683–1686; (e) C. Gautier and T. Burgi, *J. Am. Chem. Soc.*, 2008, **130**, 7077–7084; (f) W. Ma, L. Xu, A. F. de Moura, X. Wu, H. Kuang, C. Xu and N. A. Kotov, *Chem. Rev.*, 2017, **117**, 8041–8093; (g) M. V. Mukhina, V. G. Maslov, A. V. Baranov, A. V. Fedorov, A. O. Orlova, F. Purcell-Milton, J. Govan and Y. K. Gun'ko, *Nano Lett.*, 2015, **15**, 2844–2851; (h) A. ben-Moshe, D. Szwarcman and G. Markovich, *ACS Nano*, 2011, **5**, 9034–9043; (i) A. Ben-Moshe, S. G. Wolf, M. Bar Sadan, L. Houben, Z. Fan, A. O. Govorov and G. Markovich, *Nat. Commun.*, 2014, **5**, 4302; (j) H. E. Lee, H. Y. Ahn, J. Mun, Y. Y. Lee, M. Kim, N. H. Cho, K. Chang, W. S. Kim, J. Rho and K. T. Nam, *Nature*, 2018, **556**, 360–365.
- M. Simonyi, Z. Bikádi, F. Zsila and J. Deli, *Chirality*, 2003, **15**, 680–698.
- (a) Y. Ono, K. Nakashima, M. Sano, Y. Kanekiyo, K. Inoue, S. Shinkai, M. Sano and J. Hojo, *Chem. Commun.*, 1998, 1477–1478, DOI: 10.1039/a802829j; (b) S. Marx and D. Avnir, *Acc. Chem. Res.*, 2007, **40**, 768–776; (c) H. Qiu and S. Che, *Chem. Soc. Rev.*, 2011, **40**, 1259–1268; (d) K. J. C. van Bommel, A. Friggeri and S. Shinkai, *Angew. Chem., Int. Ed.*, 2003, **42**, 980–999; (e) J. A. Kelly, M. Giese, K. E. Shopsowitz, W. Y. Hamad and M. J. MacLachlan, *Acc. Chem. Res.*, 2014, **47**, 1088–1096; (f) Y. Okazaki, T. Buffeteau, E. Siurdyban, D. Talaga, N. Ryu, R. Yagi, E. Pouget, M. Takafuji, H. Ihara and R. Oda, *Nano Lett.*, 2016, **16**, 6411–6415.
- (a) X. Gao, B. Han, X. Yang and Z. Tang, *J. Am. Chem. Soc.*, 2019, **141**, 13700–13707; (b) H. Tanaka, Y. Inoue and T. Mori, *ChemPhotoChem*, 2018, **2**, 386–402; (c) J. Yan, W. Feng, J.-Y. Kim, J. Lu, P. Kumar, Z. Mu, X. Wu, X. Mao and N. A. Kotov, *Chem. Mater.*, 2019, **32**, 476–488.
- J. R. L. Moxon, A. R. Renshaw and I. J. Tebbutt, *J. Phys. D: Appl. Phys.*, 1991, **24**, 1187–1192.
- (a) C. Bustamante, I. Tinoco, Jr. and M. F. Maestre, *Proc. Natl. Acad. Sci. U. S. A.*, 1983, **80**, 3568–3572; (b) C. A. Ottaway and D. B. Wetlaufer, *Arch. Biochem. Biophys.*, 1970, **139**, 257–264; (c) J. A. Schellman, *Chem. Rev.*, 1975, **75**, 323–331; (d) T. Wu, G. Li, J. Kapitan, J. Kessler, Y. Xu and P. Bouř, *Angew. Chem., Int. Ed.*, 2020, **59**, 21895–21898; (e) G. Li, J. Kessler, J. Cheramy, T. Wu, M. R. Poopari, P. Bouř and Y. Xu, *Angew. Chem., Int. Ed.*, 2019, **58**, 16495–16498; (f) C. F. Bohren, *Chem. Phys. Lett.*, 1974, **29**, 458–462; (g) Z. A. Awan and D. Seetharamdoo, *Appl. Opt.*, 2020, **59**, 5670–5679; (h) J. Crassous, A. Amon and J. Crassous, *Phys. Rev. A: At., Mol., Opt. Phys.*, 2012, **85**, 023806.
- (a) T. Hu and J. Hong, *ACS Appl. Mater. Interfaces*, 2015, **7**, 23489–23495; (b) M. Iwata, M. Teshima, T. Seki, S. Yoshioka and Y. Takeoka, *Adv. Mater.*, 2017, **29**, 1605050; (c) Y. Takeoka, S. Yoshioka, A. Takano, S. Arai, K. Nueangnoraj, H. Nishihara, M. Teshima, Y. Ohtsuka and T. Seki, *Angew. Chem., Int. Ed.*, 2013, **52**, 7261–7265.
- (a) T. Delclos, C. Aimé, E. Pouget, A. Brizard, I. Huc, M.-H. Delville and R. Oda, *Nano Lett.*, 2008, **8**, 1929–1935; (b) Y. Okazaki, J. Cheng, D. Dedovets, G. Kemper, M.-H. Delville, M.-C. Durrieu, H. Ihara, M. Takafuji, E. Pouget and R. Oda, *ACS Nano*, 2014, **8**, 6863–6872; (c) K. Sugiyasu, S.-i. Tamaru, M. Takeuchi, D. Berthier, I. Huc, R. Oda and S. Shinkai, *Chem. Commun.*, 2002, 1212–1213, DOI: 10.1039/B202799M.
- (a) Z. Liu, J. Ai, P. Kumar, E. You, X. Zhou, X. Liu, Z. Tian, P. Bouř, Y. Duan, L. Han, N. A. Kotov, S. Ding and S. Che, *Angew. Chem., Int. Ed.*, 2020, **59**, 15226–15231; (b) M. Vybornyi, Y. Vyborna and R. Häner, *ChemistryOpen*, 2017, **6**, 488–491.
- D. L. Griscom, *J. Ceram. Soc. Jpn.*, 1991, **99**(10), 923–942.
- U. Hohenester and A. Trügler, *Comput. Phys. Commun.*, 2012, **183**, 370–381.
- E. D. Palik, *Handbook of Optical Constants of Solids*, 1985.
- A. Kuzyk, R. Schreiber, Z. Fan, G. Pardatscher, E.-M. Roller, A. Högele, F. C. Simmel, A. O. Govorov and T. Liedl, *Nature*, 2012, **483**, 311–314.

