

## PAPER

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# Origin and regulation of triaxial magnetic anisotropy in the ferromagnetic semiconductor CrSBr monolayer†

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Magnetic anisotropy plays a vital role in stabilizing the long-range magnetic order of two-dimensional ferromagnetic systems. In this work, using the first-principles method, we systematically explored the triaxial magnetic anisotropic properties of a ferromagnetic semiconductor CrSBr monolayer, which is recently exfoliated from its bulk. Further analysis shows that the triaxial magnetic anisotropic properties originate from the coexistence of the magnetic dipole–dipole interaction (shape anisotropy) and the spin–orbit coupling interaction (magnetocrystalline anisotropy). Interestingly, the shape anisotropy, which has been neglected in most previous works, dominates over the magnetocrystalline anisotropy. Besides, the experimental Curie temperature of the CrSBr monolayer is well reproduced using Monte Carlo simulations. What is more, the easy magnetic axes and ferromagnetism in the CrSBr monolayer can be manipulated by strains and are relatively more susceptible to the uniaxial strain in the *x* direction. Our study not only explains the mechanism of triaxial magnetic anisotropy of the CrSBr monolayer, but also sheds light on how to tune the magnetic anisotropy and Curie temperature in ferromagnetic monolayers.

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## Introduction

Spintronic devices have attracted widespread attention because of their advantages of faster processing speed, ultra-low heat dissipation, denser storage density, lower power consumption, and non-volatility.<sup>1–5</sup> With the need for the miniaturization of spintronic devices, intrinsic two-dimensional (2D) ferromagnetic semiconductor (FMS) materials are the most promising candidates for nanoscale spintronics, which can fulfill the demand of independent control of charge and spin.<sup>6–8</sup> The Mermin–Wagner theorem shows that no 2D long-range isotropic ferromagnetism would exist with continuous spin symmetries at finite temperatures.<sup>9</sup> The discoveries of 2D long-range ferromagnetic (FM) order with thickness down to the atomic limit in van der Waals (vdWs) crystals CrI<sub>3</sub> and Cr<sub>2</sub>Ge<sub>2</sub>Te<sub>6</sub> have completely disrupted the Mermin–Wagner theory and opened new platforms for studying nanoscale spintronic devices.<sup>10,11</sup> Since then, more 2D FMS materials have been observed experimentally and predicted

theoretically.<sup>6–8,12–27</sup> Further analysis shows that magnetic anisotropy (MA) is the prerequisite and foundation to verify whether a 2D material exhibits a magnetically ordered phase above zero temperature,<sup>28–30</sup> and the 2D FM order can be stabilized by the magnon excitation gap caused by uniaxial magnetic anisotropy.<sup>31–33</sup> MA, which can be scaled by the magnetic anisotropy energy (MAE), is mainly determined by two factors; one is the magnetocrystalline anisotropy resulting from the spin–orbit coupling interaction (SOC-MAE) and the other is the shape anisotropy caused by the dipole–dipole interaction (shape-MAE).<sup>34</sup> Compared with the SOC-MAE, the shape-MAE is often relatively weak and of less concern. But for a 2D system with a weak SOC-MAE, the shape-MAE may have an important contribution. The larger the total MAE (sum of SOC-MAE and shape-MAE), the stronger the resistance of magnetic ordering against thermal fluctuations, which can improve the stability of magnetic states.<sup>35</sup> However, a detailed microscopic analysis of total MAE received little attention previously.

Recently, a promising 2D van der Waals semiconducting magnet, CrSBr, is of great interest owing to its exotic properties.<sup>12,25,36–50</sup> Bulk CrSBr is a layered A-type antiferromagnetic semiconductor with the Néel temperature  $T_N \approx 140$  K, and it exhibits triaxial magnetic anisotropy (intermediate magnetization *x* axis, easy magnetization *y* axis, and hard magnetization *z* axis) with a band gap of about 1.5 eV.<sup>25,44,49</sup>

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More importantly, CrSBr exhibits air stability and gate-tunable conductivity, which reinforces its potential application as a spintronic device.<sup>50</sup> In 2018, we predicted the possibility of a CrSBr monolayer stripping from its bulk, and it is a high-temperature ferromagnetic semiconductor with a  $T_C$  of 160 K.<sup>12</sup> Then, the  $T_C$  of the CrSBr monolayer was also predicted to be 290 K using the Ising model<sup>51</sup> and 124 K using the anisotropic Heisenberg model.<sup>16</sup> Yang *et al.* calculated the  $T_C$  of the CrSBr monolayer to be 175 K.<sup>36</sup> Very recently, CrSBr monolayers have been experimentally confirmed using the second harmonic generation technique, and the measured  $T_C$  is about 146 K.<sup>25</sup> Besides, considering the small value of MAE (below meV) and the outstanding deformation capacity of 2D materials, it is easily affected by external strains. Strain engineering has also been proved to be a powerful tool to tune the properties of 2D materials, which has been able to induce switching between indirect and direct band-gap semiconductors<sup>52,53</sup> and between antiferromagnetic (AFM) and FM states,<sup>54–56</sup> induce phase transition,<sup>57–59</sup> *etc.* Therefore, the effect of strain on MA is also necessary to be explored because of the importance of magnetic anisotropy in the context of 2D magnetism.

Motivated by these burgeoning developments, we focus on the recently observed 2D air-stable FMS CrSBr monolayer.<sup>25,43</sup> First, using the first-principles calculations, the triaxial magnetic MA of bulk CrSBr, which was confirmed experimentally, was well reproduced.<sup>36,45,49</sup> Interestingly, the CrSBr monolayer also exhibits triaxial MA, which originates from the coexistence of spin-orbit coupling and dipole-dipole interactions. The contribution of the dipole-dipole interaction to MA is much more important than that of the spin-orbit coupling interaction. Under strains, the intermediate magnetization, easy magnetization, and hard magnetization axes can be converted to each other, providing an ideal candidate material for triaxial magnetic switching. Besides, by using the four ordered spin state method, the value of  $T_C$  measured using the experiment was well reproduced and can be further increased by applying strains. Our findings not only provide a detailed understanding of 2D magnetism in the CrSBr monolayer, but also explore an effective strategy to control the MA and enhance the  $T_C$ .

## Method

Spin-polarized calculations are adopted within the framework of the density functional theory, especially implemented in the Vienna *ab initio* simulation package (VASP).<sup>60</sup> The projector augmented wave (PAW) pseudopotential method with an energy cutoff of 500 eV is used to describe the interaction between electrons and atomic nuclei.<sup>61</sup> The electronic exchange correlation function is expressed by the Perdew–Burke–Ernzerhof (PBE) functional under the generalized gradient approximation (GGA).<sup>62</sup> The convergence criterion is  $10^{-6}$  eV for total energies and  $0.01 \text{ eV } \text{\AA}^{-1}$  for force. A vacuum layer of about  $25 \text{ \AA}$  is added to prevent the interaction between layers.<sup>63</sup> The PBE +  $U$  approach was used to describe the strong

correlation effect for the 3d orbital of the Cr atom, in which the values of  $U$  and  $J$  are 4.03 eV and 0.96 eV, respectively.<sup>47</sup>

Total MAE is the sum of SOC-MAE and shape-MAE. The calculation of SOC-MAE is based on the second-order perturbation theory, and the Hamiltonian containing spin-orbit coupling interaction (SOC) can be written as:

$$H^{\text{SOC}} = \lambda^2 \left( \sum_{m \neq n} \frac{|\langle \uparrow, n | \hat{\mathbf{S}} \cdot \hat{\mathbf{L}} | \uparrow, m \rangle|^2}{E_n^{(0)} - E_m^{(0)}} \right) + \sum_{m \neq n} \frac{|\langle \uparrow, n | \hat{\mathbf{S}} \cdot \hat{\mathbf{L}} | \downarrow, m \rangle|^2}{E_n^{(0)} - E_m^{(0)}} \\ + \sum_{m \neq n} \frac{|\langle \downarrow, n | \hat{\mathbf{S}} \cdot \hat{\mathbf{L}} | \uparrow, m \rangle|^2}{E_n^{(0)} - E_m^{(0)}} + \sum_{m \neq n} \frac{|\langle \downarrow, n | \hat{\mathbf{S}} \cdot \hat{\mathbf{L}} | \downarrow, m \rangle|^2}{E_n^{(0)} - E_m^{(0)}}$$

where  $\lambda$  is the SOC constant,  $|\uparrow\rangle$  and  $|\downarrow\rangle$  denote the spin-up and spin-down states, respectively,  $|n\rangle$  and  $|m\rangle$  represent the eigenstates of the Hamiltonian operator respectively,  $E_n^{(0)}$  and  $E_m^{(0)}$  correspond to the eigenvalues of the eigenstates respectively, and  $\hat{\mathbf{S}}$  and  $\hat{\mathbf{L}}$  correspond to the spin momentum operator and orbital angular momentum operator, respectively. All the derivations are provided in the ESI.† The shape-MAE is caused by the dipole-dipole interaction and is expressed as:

$$E^{\text{dip-dip}} = \frac{1}{2} \frac{\mu_0}{4\pi} \sum_{q \neq q'} \frac{1}{r_{qq'}^3} \left[ M_q M_{q'} - \frac{3}{r_{qq'}^2} (M_q \cdot r_{qq'}) (M_{q'} \cdot r_{qq'}) \right]$$

where  $\mu_0$  is the permeability of vacuum,  $q$  is the atomic coordinate of the Cr atom,  $r$  is the distance between two magnetic atoms, and  $M$  represents the magnetic moment. According to the formula, shape-MAE is only related to the position and magnetic moment of magnetic atoms.

## Results and discussion

The optimized lattice constants of the CrSBr monolayer are  $a = 3.59 \text{ \AA}$  and  $b = 4.82 \text{ \AA}$ , which are in good agreement with previous studies.<sup>12,25</sup> The FM and four AFM states are considered for the CrSBr monolayer (Fig. S1†), and the results show that the FM state is the ground state, which is consistent with the experimental result.<sup>25</sup> Magnetism mainly stems from the Cr atoms with a magnetic moment of  $3\mu_B$  while the S/Br atoms hold a small opposite magnetic moment, which was shown in the spin density distribution (Fig. 1b).

Analysis of the band structure shows that the CrSBr monolayer is a ferromagnetic semiconductor with an indirect bandgap of about 1.35 eV (Fig. 2a), which is in good agreement with the optical band gap measured in the experiment ( $1.25 \pm 0.07 \text{ eV}$ ).<sup>25</sup> Detailed analysis of the atomic-resolved band structure illustrates that the conduction band around the Fermi level is dominated by orbitals of Cr atoms, whereas the valence band is dominated by hybridized orbitals of Br and S atoms, which agree with the results of the density of states (DOS) as shown in Fig. S2.† Analysis of the orbital-resolved DOS shows that the conduction band minima and valence band maxima are mainly occupied by the  $d_{x^2-y^2}$  orbits of the Cr atom and  $p_y$  orbits of S and Br, respectively.

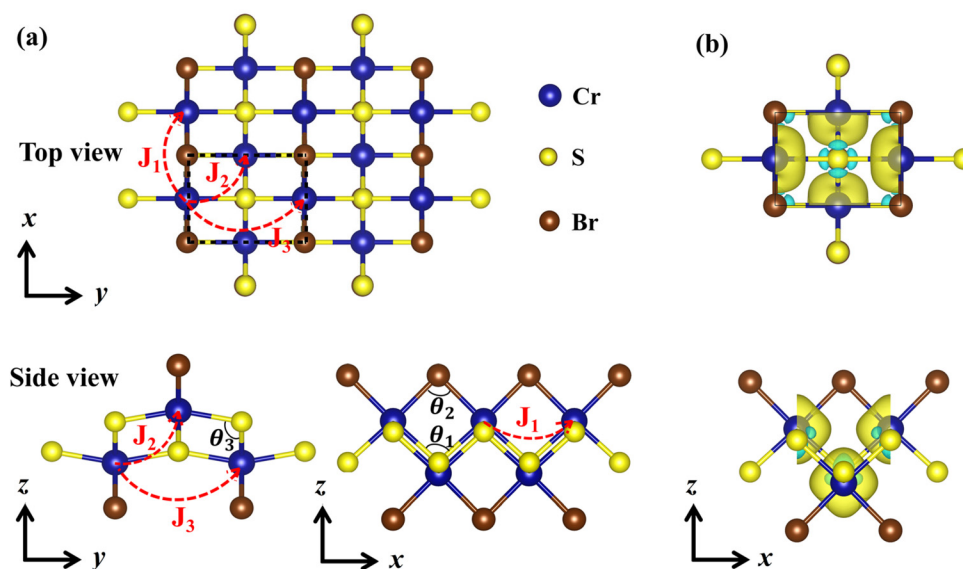


Fig. 1 (a) The top view and side view of the CrSBBr monolayer. (b) Spin density of the CrSBBr monolayer.

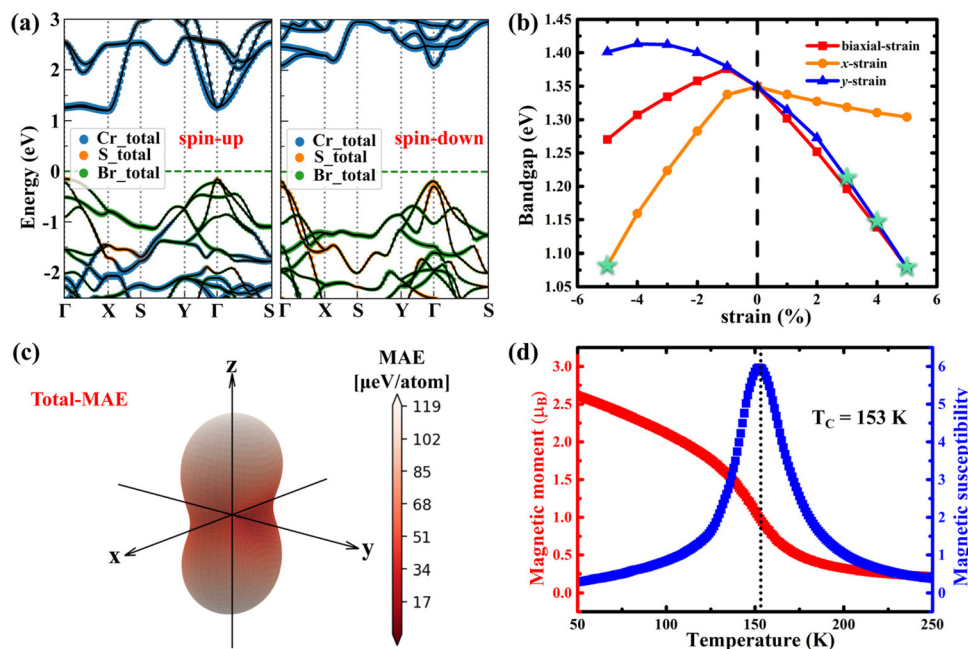


Fig. 2 (a) The band structure of the CrSBBr monolayer. (b) The band gaps of the CrSBBr monolayer under biaxial and uniaxial strains (−5%–5%). The star represents a direct band gap. (c) Angular dependence of the total-MAE of the CrSBBr monolayer with the direction of magnetization lying on the whole space. (d) The magnetic moment and magnetic susceptibility as functions of temperature for the CrSBBr monolayer.

Fig. S3† shows that the CrSBBr monolayer remains in ferromagnetic order under compression and tension strains (from −5% to 5%) and the strain has little effect on the lattice structures and magnetic moment. By applying external strain along different directions, the band-gap of the CrSBBr monolayer can be flexibly adjusted from about 1 eV to 1.4 eV (Fig. 2b). Interestingly, an increase in strain along the *x* and *y* directions is accompanied by a shift from an indirect to a direct band

gap (Fig. 2b). The detailed band structure of the CrSBBr monolayer under different strains is shown in Fig. S4–S6.† The reason may be that the applied strain causes a splitting of the band along the X– $\Gamma$  direction and changes the position of the conduction band bottom from the X to the  $\Gamma$  point.

The magnetocrystalline anisotropy energy (SOC-MAE) of CrSBBr bulk was first calculated using the second-order perturbation theory in three directions (the [100], [010], and [001]

**Table 1** The SOC-MAE, shape-MAE, and total-MAE ( $\mu\text{eV}/\text{Cr}$ ) of the CrSBr bulk and monolayer along the [100], [010], and [001] directions, respectively, which is referenced to the energy of the [010] direction

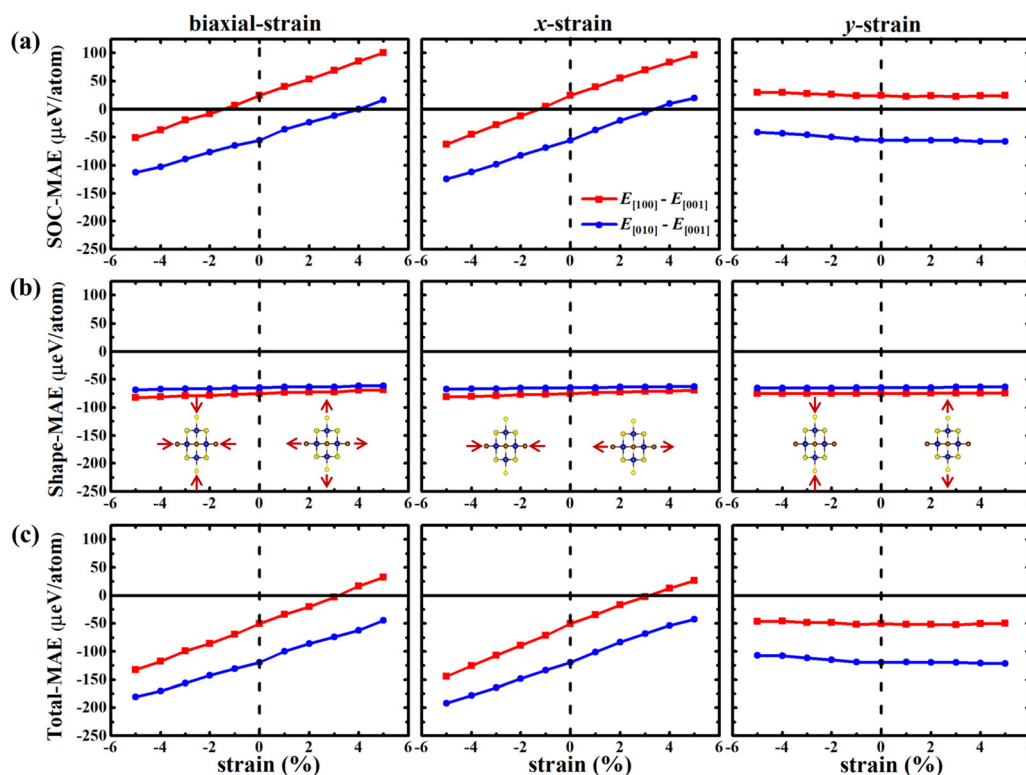
|           |           | $E_{[100]}$ | $E_{[010]}$ | $E_{[001]}$ | Energy order of magnetic axes                       |
|-----------|-----------|-------------|-------------|-------------|---|
| Bulk      | SOC-MAE   | 8           | -32         | 0           | $y < z < x$   |
|           | Shape-MAE | -59         | -40         | 0           | $x < y < z$   |
|           | Total-MAE | -51         | -72         | 0           | $y < x < z$<br>$y < x < z$ (exp. <sup>49,64</sup> ) |
| Monolayer | SOC-MAE   | 24          | -55         | 0           | $y < z < x$   |
|           | Shape-MAE | -75         | -64         | 0           | $x < y < z$   |
|           | Total-MAE | -51         | -119        | 0           | $y < x < z$   |

directions) as shown in Table 1. Obviously, the energy of the  $y$  axis (the [010] direction) is lower than that of the  $z$  axis (the [001] direction), and the  $x$  axis (the [100] direction) has the highest energy (the energy order is  $y < z < x$ ). This is not consistent with the results of the experiment ( $y < x < z$ ), which shows that bulk CrSBr exhibits the easy  $y$  axis, intermediate  $x$  axis, and hard  $z$  axis.<sup>38,40,49,64</sup> Although the calculated easy magnetic axis is the same as the experimental result (the [010] direction), the measured triaxial MAE by experiment is not well reproduced. Compared to the weak SOC-MAE, shape anisotropy induced by the magnetic dipole-dipole interaction may have an important contribution (shape-MAE).<sup>65</sup> The in-plane shape-MAE was also calculated (Table 1), in which  $r_{\text{max}} =$

3000 Å was used to ensure the numerical reliability. Interestingly, after considering the magnetic dipole-dipole interaction, the total-MAE (sum of SOC-MAE and shape-MAE) shows that  $y$ ,  $x$ , and  $z$  are indeed the easy, the intermediate, and the hard axis, respectively, reflecting its triaxial anisotropy. These results not only well reproduce the experimental triaxial MAE of bulk, but also demonstrate the important role of the magnetic dipole-dipole interaction (shape-MAE) in this material.

The SOC-MAE and shape-MAE of the CrSBr monolayer were also calculated (Table 1), and the results show that this monolayer also possesses triaxial magnetic anisotropy. Moreover, the value of shape-MAE is larger than that of SOC-MAE. The presence of triaxial magnetic anisotropy in the CrSBr monolayer is different from the present in-plane and out-of-plane magnets,<sup>7,66</sup> reinforcing the interest in the CrSBr monolayer as a potential host for exotic magnetic states. In order to show more clearly this novel property, the angular dependences of SOC-MAE, shape-MAE, and total-MAE along the three planes (the  $xz$  plane,  $yz$  plane, and  $xy$  plane) and the whole space are presented in Fig. S7† and Fig. 2c. Clearly, the MAE strongly depends on the direction of magnetization in the whole space, which confirms again the strong magnetic anisotropy in this monolayer.

Fig. 3 shows the variation of SOC-MAE, shape-MAE, and total-MAE of the CrSBr monolayer under biaxial and uniaxial strains. The trend of energy change in Fig. 3a is almost the



**Fig. 3** Variation of the SOC-MAE (a), shape-MAE (b), and total-MAE (c) of the CrSBr monolayer under biaxial and uniaxial strains (−5%–5%). The energy is the reference along the [001] direction.



same under the biaxial strains and uniaxial strains along the  $x$  direction, while the relative energy is almost constant under strains along the  $y$  direction, suggesting the SOC-MAE is sensitive to the strains along the  $x$  direction. Fig. 3b shows that the effect of strains on the values of shape-MAE is negligible because of the small changes in the crystal structure and magnetic moment under different strains. Under different strains, Fig. 3c shows the variation of total MAE. Clearly, the variation trend of total-MAE in Fig. 3a and c is consistent, suggesting that the change in the total-MAE is mainly caused by the spin-orbit coupling under different strains, especially the uniaxial strain along the  $x$  direction. The corresponding SOC-MAE and total-MAEs through the whole space under different uniaxial strains are plotted in Fig. 4 and Fig. S8, S9.<sup>†</sup> These figures further confirm that the CrSBr monolayer has strong triaxial magnetic anisotropy and the MAE is most sensitive to uniaxial strain along the  $x$  direction.

To further elucidate the origin of the strain effect on the SOC-MAE, we first determine separate contributions of the Cr, S and Br atoms to SOC-MAE (Fig. S10<sup>†</sup>). The results show that the SOC-MAE is mainly contributed by the Cr\_d orbitals and Br\_p orbitals, which are the most sensitive to external strain. Taking a biaxial tensile strain of 5% as an example, Fig. S10a<sup>†</sup> shows that the contribution of Cr\_d orbitals to the MAE between the [100] and [001] direction is much more than that of the other orbitals. Fig. S10b<sup>†</sup> shows that the MAE between the directions [010] and [100] is mainly contributed by the Cr\_d orbitals and Br\_p orbitals. The values of SOC-MAE, of each d orbital of Cr\_d orbitals (including  $d_{xy}$ ,  $d_{yz}$ ,  $d_{z^2}$ ,  $d_{xz}$ , and  $d_{x^2-y^2}$ ) and the individual p orbitals of Br\_p (including  $p_y$ ,  $p_z$ , and  $p_x$ ) were also calculated. Fig. 5 and S11–S15<sup>†</sup> represent the amount of energy change in the [100], [010] and [001] directions for individual Cr\_d and Br\_p orbitals under biaxial,  $x$ -directional uniaxial and  $y$ -directional uniaxial strains,

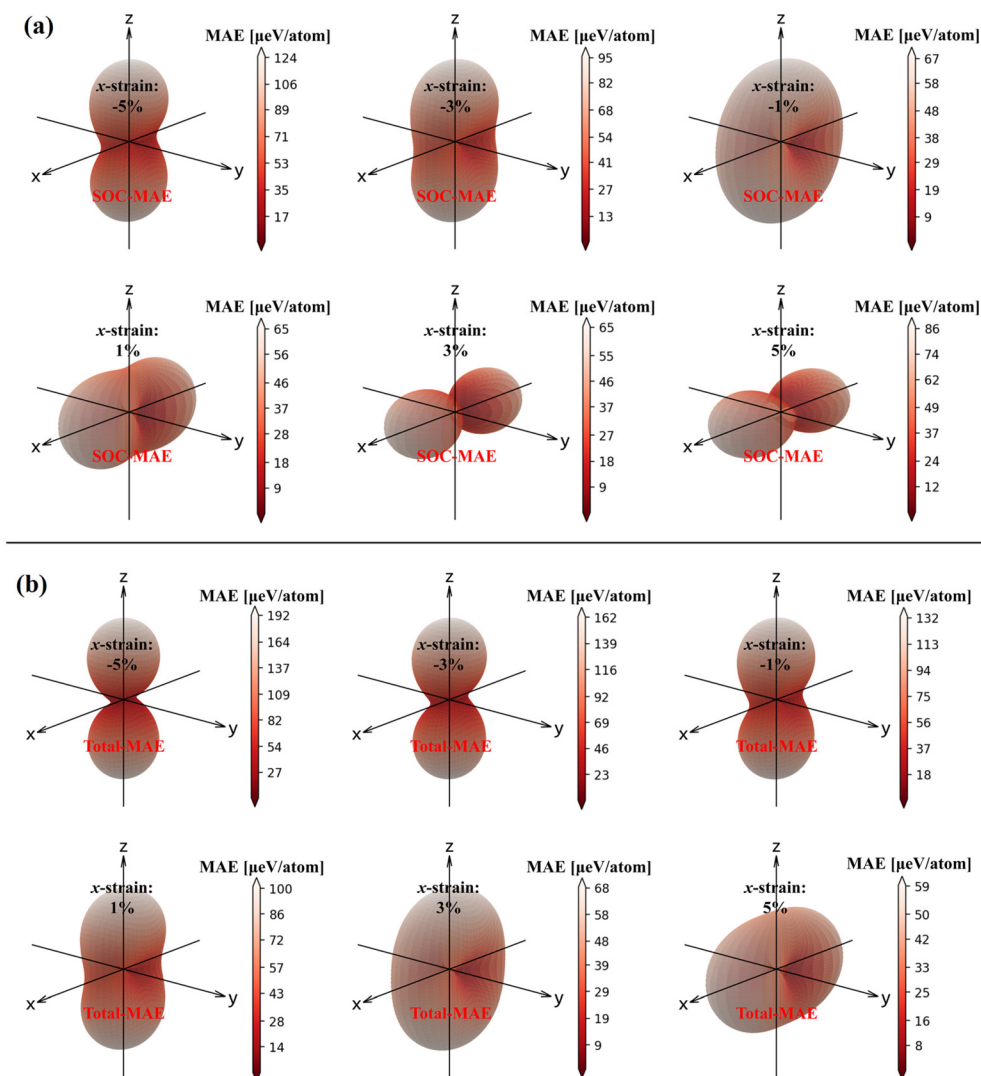
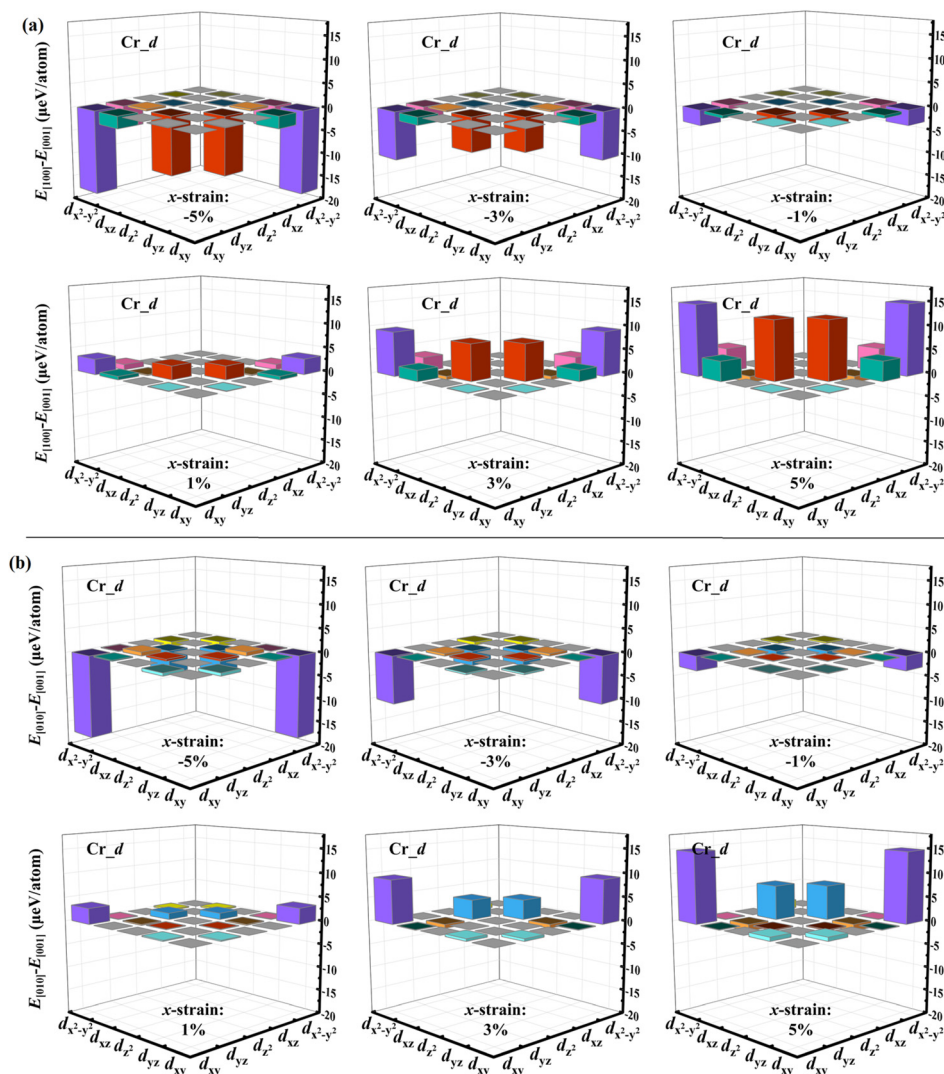


Fig. 4 The variation of SOC-MAE (a) and total-MAE (b) for the CrSBr monolayer in the whole space under uniaxial  $x$  strain (-5%–5%).



**Fig. 5** The contribution to MAE from the SOC interaction between different d orbital channels for Cr atoms under different uniaxial x strains along the [100] (a) and the [010] (b) directions. The energy is the reference along the [001] direction.

respectively. These figures reveal that the coupling between  $\text{Cr}_{d_{x^2-y^2}}$  and  $\text{Cr}_{d_{xy}}$  orbitals and that between  $\text{Cr}_{d_{z^2}}$  and  $\text{Cr}_{d_{yz}}$  orbitals are more sensitive to biaxial strain and uniaxial in the x-direction. According to the formula and Tables S3 and S4 given in the ESI,<sup>†</sup> the  $\text{Cr}_{d_{x^2-y^2}}$  and  $\text{Cr}_{d_{xy}}$  coupling through  $\hat{l}_x$  and  $\hat{l}_y$  in the same spin state and that in different spin states are both equal to 0, while the coupling of these two orbits *via*  $\hat{l}_z$  in the same spin state is not 0, which indicates that the coupling between  $\text{Cr}_{d_{x^2-y^2}}$  and  $\text{Cr}_{d_{xy}}$  will provide a higher spin orbit coupling energy in the z direction. Similarly, the coupling between  $\text{Cr}_{d_{z^2}}$  and  $\text{Cr}_{d_{yz}}$  orbitals gain a nonzero value only *via*  $\hat{l}_x$  for different spin states, suggesting that the coupling of  $\text{Cr}_{d_{z^2}}$  and  $\text{Cr}_{d_{yz}}$  orbitals will provide a low spin orbit coupling energy in the y and z directions. The coupling of other orbits can also be derived in the same way according to Tables S3 and S4.<sup>†</sup> Taking the example of x direction tensile strain, the enhancement of tensile strain weakens

the coupling strength of  $\text{Cr}_{d_{x^2-y^2}}$  and  $\text{Cr}_{d_{xy}}$  *via*  $\hat{l}_z$  in the same spin state, while at the same time,  $\text{Cr}_{d_{z^2}}$  and  $\text{Cr}_{d_{yz}}$  orbitals in the same spin state *via*  $\hat{l}_x$  coupling in different spin states and  $\text{Cr}_{d_{z^2}}$  and  $\text{Cr}_{d_{xz}}$  orbitals *via*  $\hat{l}_y$  in different states are both enhanced, eventually resulting in the lowest energy in the z direction. In addition, the SOC-MAE of individual p-orbitals of the Br atom is less sensitive to strain than that of the individual Cr\_d orbitals and the energy change is within 5  $\mu\text{eV}$ . The angular momentum coupling through the individual p-orbitals can also be obtained according to the formula and Table S3 in the ESI.<sup>†</sup> We also take the example of x-direction tensile strain. The strengthening of the tensile strain is accompanied by a weakening of the  $\hat{l}_z$  coupling between  $\text{Br}_{p_x}$  and  $\text{Br}_{p_y}$  in the same spin state, a weakening of the  $\hat{l}_x$  coupling between  $\text{Br}_{p_y}$  and  $\text{Br}_{p_z}$  in the same spin state, and a strengthening of the  $\hat{l}_y$  coupling between  $\text{Br}_{p_x}$  and  $\text{Br}_{p_z}$  in the same spin state.

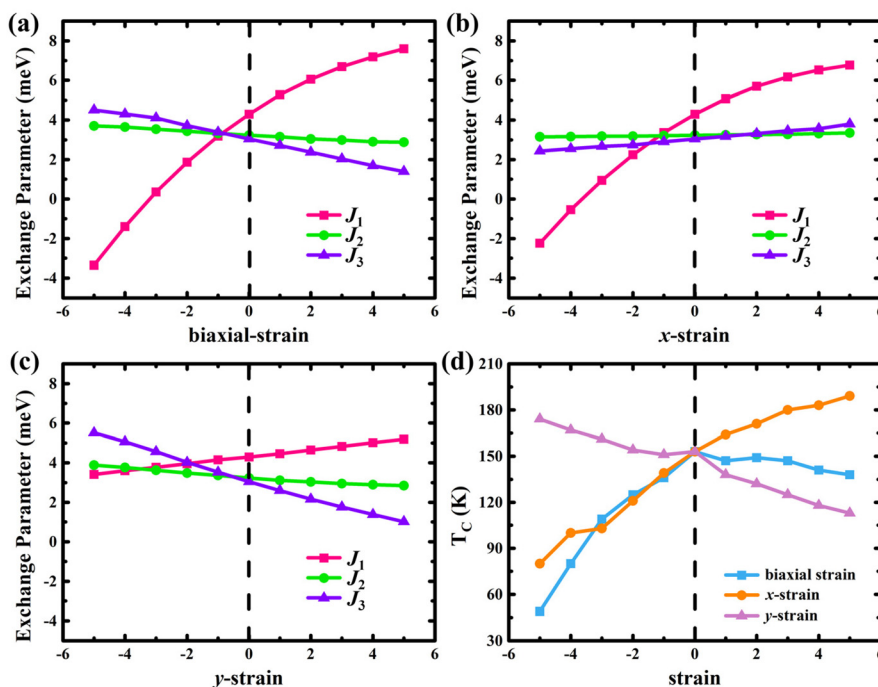


Fig. 6 Variation of exchange parameters with biaxial strain (a), uniaxial strain in the x-direction (b), and uniaxial in the y-direction (c), respectively. (d) The changes of  $T_C$  at different strains.

Because of the importance of  $T_C$  for the application of 2D magnets, we estimated the  $T_C$  of the CrSBr monolayer using Monte Carlo simulations based on the Heisenberg model, and the Hamiltonian can be written as

$$H = -\frac{1}{2} \sum_{k=1,2,3} J_k \sum_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + A \sum_i (S_i^z)^2$$

where  $J_k$  ( $k = 1, 2, 3$ ) represents the magnetic exchange parameters of the nearest neighbor, the second-neighbor, and the third-neighbor between pairs of spins, respectively (Fig. 1).  $\mathbf{S}_i$  or  $\mathbf{S}_j$  stands for the spin vector, and  $S_i^z$  is the spin component along the z-axis.  $A$  represents the anisotropy parameter. By using four ordered spin states,  $J_k$  was calculated on the basis of density-functional calculations.<sup>67</sup> The values of  $J_1$ ,  $J_2$  and  $J_3$  for the CrSBr monolayer are 4.29, 3.23 and 3.04 meV respectively. The result shows that the  $T_C$  of the CrSBr monolayer is about 153 K (Fig. 2d), which is in excellent agreement with the experimental result (146 K).<sup>25</sup> The  $T_C$  is higher than that of other successfully prepared 2D ferromagnetic semiconductors, such as CrX<sub>3</sub> (X = Cl, Br, I) monolayers (27 K, 40 K, and 45 K)<sup>7</sup> and Cr<sub>2</sub>Ge<sub>2</sub>Te<sub>6</sub> bilayers (28 K).<sup>11</sup> The strain-dependent evolution of magnetic exchange parameters ( $J_1$ ,  $J_2$ , and  $J_3$ ) was also investigated and is shown in Fig. 6a–c. Due to the asymmetric structure of the CrSBr monolayer,  $J_1$ ,  $J_2$ , and  $J_3$  exhibit independent evolution depending on the crystallographic direction of the applied strain. The results show that  $J_2$  and  $J_3$  have a roughly similar trend in the whole strain while  $J_1$  was strongly influenced by the uniaxial strain in the x-direction. Moreover, the strain enables the adjustment of  $T_C$  in the range of 49 to

189 K (Fig. 6d), and the calculated magnetic moment and susceptibility as functions of temperature for the CrSBr monolayer under biaxial and uniaxial strains are also illustrated in Fig. S16S18.†

## Summary

In summary, we have investigated the origin of triaxial anisotropic magnetic properties of the air-stable 2D magnetic semiconductor CrSBr using first-principles calculations. The CrSBr monolayer exhibits triaxial anisotropy, which originates from the coexistence of the magnetic dipole–dipole interaction (shape anisotropy) and the spin–orbit coupling interaction (magnetocrystalline anisotropy), and we also unveil that the magnetic shape anisotropy, which has been neglected in most previous works, is of importance for works of weak magnetocrystalline anisotropy. Interestingly, the energy order of the three magnetic axes of the CrSBr monolayer can be tuned by applying strains, in which the SOC-MAE is more sensitive to strains than shape-MAE. Further analysis shows that the enhancement of biaxial and uniaxial x-direction tensile strain weakens the coupling strength of Cr- $d_{x^2-y^2}$  and Cr- $d_{xy}$  via  $\hat{l}_z$  in the same spin state while enhancing the coupling strength of Cr- $d_{z^2}$  and Cr- $d_{yz}$  via  $\hat{l}_x$  in different spin states and Cr- $d_{z^2}$  and Cr- $d_{xz}$  via  $\hat{l}_y$  in different spin states, eventually achieving triaxial switching in the process. Besides, the strains also can flexibly adjust the band gap and even change the original indirect band gap to a direct band gap. By using the four ordered spin states, the observed  $T_C$  (146 K) of the CrSBr monolayer is well

reproduced based on Monte Carlo simulations (152 K) and the  $T_C$  can be increased to 189 K under uniaxial strain in the  $x$  direction. Our work gives insights into understanding the MAE of 2D ferromagnetism and paves the way for strain control of switchable magnetic anisotropy and Curie temperature for exploring new spintronic applications.

## Author contributions

B. Wang: formal analysis, writing – original draft, and funding acquisition; Y. Wu: formal analysis, writing – original draft, and data curation; Y. Bai: supervision and writing – original draft; P. Shi: data curation; G. Zhang: visualization, methodology and funding acquisition; Y. Zhang: writing – review & editing and funding acquisition, C. Liu: writing – review & editing and project administration. All authors checked the manuscript.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

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