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Coupled instabilities of surface crease and bulk bending during fast free swelling of hydrogel

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Abstract

Most studies on hydrogel swelling instability have been focused on a constraint boundary condition. In this paper, we studied the mechanical instability of a piece of disc shape hydrogel during free swelling. The fast swelling of the gel induces two swelling mismatches; surface-inner layer mismatch and annulus-disc mismatch, which lead to surface crease pattern formation and saddle-like bulk bending, respectively. For the first time, stripe-like surface crease that are in right angle on the two surface of gel was observed. This stripe pattern is related to the mechanical coupling of the surface instability and the bulk bending, which is justified by investigating the swelling-induced surfaces pattern on thin hydrogel sheet fixed onto a saddle-shaped substrate *prior to* swelling. A theoretical mechanism based on an energy model was developed to show anisotropic stripe-like surface crease pattern on a saddle shaped surface. These results might be helpful to develop novel strategies for controlling crease patterns on soft and wet materials by changing its three-dimensional shape.

Introduction

Intriguing surface patterns and bulk deformations are often observed in dynamic, non-equilibrium processes of soft substances¹⁻⁵. For example, intricate morphological patterns found in the human body, such as creases of the brain, wrinkles on the skin, branches in the lungs and the morphology of

the gut, are formed during tissue growth⁶⁻⁹. Surface creasing of hydrogels induced by fast heterogeneous swelling is also a well-known phenomenon^{10, 11}. These phenomena are considered to be formed via the mechanical instability induced during tissue growth and hydrogel swelling^{12, 13}. Many researches, both theoretical and experimental, have been devoted to reveal the surface crease formation mechanism using hydrogels as a model substance¹⁴⁻¹⁷. The mechanical instability phenomenon has also been exploited to generate functional properties such as tunable wettability or adhesiveness, switchability of photonic properties, and cellular interaction ability¹⁸⁻²¹. Precise understanding of the mechanical instability of gels cannot only provide understanding on the morphology formation of biological tissues but also give direction to design and fabricate novel, functional soft materials.

Most studies on the hydrogel swelling instability have been focused on a constraint boundary condition^{14-17, 22-24}. That is, the gel layer is fixed to the rigid substrates that are flat or cylindrical. When a gel layer is constraint to a flat substrate, “polygonal” surface crease pattern is formed. The crease formation is explained by the swelling mismatch between the outer and inner layers of the gel. When the gel is immersed in water, the swelling starts from the surface layer of the gel, and this layer is able to expand freely. In contrast, the inner layer swelling is restricted to the substrate of the gel. This swelling mismatch induces a mechanical instability and leads to buckling. T. Tanaka, *et al.* firstly revealed this buckling mechanism and developed a theory that well describes the “polygonal” crease pattern under restricted swelling condition²⁵. Later, Suo *et al.* extensively studied the conditions for the occurrence of buckling²⁶.

When a gel is permitted to swell in an unrestricted condition, usually more rich and complicated phenomenon is observed. For example, a piece of sheet-shape hydrogel shows both surface buckling and bulk shape deformation, and the surface crease pattern evolves differently from the “polygonal” pattern observed for the gel restricted to a flat substrate^{14-17, 22-25}. This suggests the effect of mechanical coupling between the bulk deformation and the surface buckling. However,

understanding of the unrestricted swelling is still quite limited^{10,11}.

In this paper, we study the mechanical instability occurring during the free swelling of a piece of disc-shape hydrogel. The paper consists of three parts. In the first part, we show experimentally the evolution of surface crease pattern and bulk deformation during the swelling. A polyelectrolyte hydrogel, which has fast swelling kinetics was adopted to induce mechanical instability. Semi-rigid polyelectrolyte molecules carrying opposite charges were physically entrapped in the hydrogel network as stress sensor for analyzing the internal stress induced by the mechanical instability^{10,11,27}. The semi-rigid macromolecules can sense the internal stress field sensitively by orienting their direction along the internal tensile direction in hydrogels. Such orientation of the semi-rigid polyelectrolyte molecules is “memorized” by forming polyion complex with the oppositely charged network, even after swelling^{10,11}. So we could recall the instability pattern during heterogeneous swelling by analyzing the molecular alignment in the post-swollen sample from birefringence observation. Therefore this robust method should give us useful information which was previously unattainable. In the second part, we show that the unique crease pattern is the result of coupling of surface instability with the saddle-like bending of the gel. In the third part, we develop a theoretical mechanism to describe this mechanical coupling, based on the contraction energy initially proposed by T. Tanaka, *et al.*, assuming that the gel is not flat but saddle shaped with a mean curvature approaching zero (minimal surface).

Experimental section

Materials

The cationic monomer, *N*-[3-(*N,N*-dimethylamino)propyl]acrylamide methyl chloride quaternary (DMPAA-Q) (Kohjin Co. Ltd. Japan) and the photo-initiator, 2-oxoglutaric acid (OA) (Wako Pure Chemical Industries Ltd. Japan) were used as received without further purification. *N,N'*-methylenebis(acrylamide) (MBAA) (Wako Pure Chemical Industries Ltd. Japan) was

recrystallized from ethanol and used as a chemical cross-linker. Poly(2,2'-disulfonyl-4,4'-benzidine terephthalamide) (PBDT), a water soluble, anionic, semi-rigid polymer, was synthesized by an interfacial polycondensation reaction²⁸. The synthesized PBDT had an average molecular weight, M_w of about 200,000 g/mol, number average molecular weight, M_n of about 150,000 g/mol, and polydispersity, M_w/M_n of about 1.4. These values were investigated by GPC assay. The aqueous solution of PBDT exhibited a critical low liquid crystalline concentration, C_{LC}^* , of 2.8 wt%^{29,30}. For all experiments, water was deionized and purified with 0.22 μm and 5 μm membrane filters *prior to* use.

Synthesis of hydrogel

The positively charged gel was synthesized by radical polymerization of a cationic monomer, *N*-[3-(*N,N*-dimethyl amino)propyl] acrylamide methyl chloride quaternary (DMPAA-Q), and a chemical cross-linker, *N,N'*-methylenebis(acrylamide) (MBAA), in the presence of a small amount of semi-rigid polyanion, PBDT, as stress sensor. In order to synthesize the hydrogel film, the reaction cells were prepared by sandwiching a 1 cm wide silicone spacer (thickness: 1 mm) along the periphery between two parallel glass plates. The aqueous pre-gel solution contained 2.0 M DMAPAA-Q, 1.0 wt% PBDT, 2 mol% MBAA, and 0.15 mol% OA (the amount in mol% is related to DMAPAA-Q). After proper mixing, the pre-gel solution was injected into the reaction cells. UV irradiation from both sides of the reaction cell (UV light intensity is 3.9 mW/cm²) was performed for 6.0 h in an argon atmosphere at room temperature to form the gel. After polymerization, the as-prepared gel, of 60×60×1.0 mm³ in dimension, was carefully removed from the glass reaction cell and cut into disc shape (diameter (D):6 mm, thickness (T):1 mm) using a mechanical gel cutter (Dumb Bell Co. Ltd. Japan). The Young's modulus of the gel at as-prepared state is estimated by tensile-compressive tester (Tensilon RTC-1310A, Orientec Co.) as 0.24 MPa (see supporting information and Figure S1).

Swelling experiment

The as-prepared disc-shape gel was immersed in a large excess of water. Blue dye, Alcian blue (0.05 wt%), was added in the water to aid the visualization of the surface crease pattern. At different swelling times, the gel was taken out from the solution and photographed with a digital camera and then observed with an optical microscope. The Young's modulus of the gel at equilibrium state is estimated by tensile-compressive tester (Tensilon RTC-1310A, Orientec Co.) as 0.11 MPa (see supporting information and Figure S1).

Polarizing optical microscope (POM) observation

The birefringence of the gels in the equilibrium swelling state was observed with a polarizing optical microscope (POM) (Nikon, Eclipse, LV100POL) in parallel and crossed polarization modes at room temperature. Gel samples were placed on glass slides and observed from the top. All of the PBDT-containing PDMAA-Q gel samples exhibited a first-order white-gray birefringence color, so that a 530 nm sensitive tint plate was inserted between the polarizer and the analyzer to determine the orientation direction of the rigid PBDT molecules^{10,11,31}.

Results and Discussion

Swelling instability results

The as-prepared gel, with a diameter of 6 mm and a thickness of 1 mm, was smooth, flat, and transparent, as shown in Figure 1(a). When the sample was immersed in water, creasing at surface and annulus regions were immediately observed. Sharp boundaries between bumps of creases were clearly observed as blue lines. In concomitant to these surface and edge instabilities, the flat gel bended into saddle-like shape (Figure 1(b,c)). At the early stage of swelling (~100 s), polygonal-like surface creasing was observed [inset of Fig. 1(b)], in similar to the previous reports of the surface

crease pattern on gels constraint on flat rigid substrates^{14-17, 22-25}. As the swelling time increased (~200 s to ~400 s), the crease on the annulus region disappeared and the polygonal pattern on the central disc region changed to a stripe-like crease pattern [Fig. 1(c, d, e)]. The stripe creases on the two surfaces of the gel orthogonally aligned, so the blue boundary lines looked like “lattices” when being observed through the thickness of the gel [Fig. 1(d, e)]. It should be pointed out that this “lattice” like pattern was interpreted incorrectly as lattice crease pattern in the previous works^{10,11}. At a swelling time of around ~500 s, the surface crease patterns disappeared, and the gel surface became smooth, while the saddle-like shape still remained, with a decreased curvature [Fig. 1(f)]. After ~600 s swelling, the gel became completely smooth and flat without any deformation, as like the shape of the as-prepared sample but with an isotropic increase in volume (8 times of the initial volume) [Fig. 1(g)]. The stripe-like crease pattern observed in this study is unique and should be attributed to the free swelling of the gel, whereupon the saddle-like bending of the gel also occurred. The vertically crossed stripes on the two surfaces of the sample is the result of coupling of the surface crease pattern and the bulk saddle-like bending that has two bending axes crossing at right angles.

We further performed polarized optical microscopy (POM) observation on the post-swollen samples to analyze the internal stress built during swelling through the alignment of the semi-rigid molecules PBDT entrapped in the gel [Fig. 2(a)]. Specifically, the creasing instability induces the internal stress perpendicular to the crease border lines [Fig.2(a-i)] and the PBDT molecules align along the tensile direction of the internal stress [Fig.2(a-ii)]. The orientation of PBDT is fixed by polyion complex formation between the positively charged gel network and the negatively charged PBDT molecules as a result of dialysis of small ions from the gel during swelling in water^{10,11,27}. In order to investigate the correlation between the surface crease pattern and the internal stress, a piece of gel, of 7.0 mm (L)×4.0 mm (W)×2.0 mm (T) in geometry, was cut out from the central region of the disc-shaped sample, with the long axis of the gel piece parallel to one of the bending axes [Fig.2b(1-i)]. The gel piece was observed through the thickness under POM with inserting the 530 nm sensitive tint plate.

Lattice-like birefringence pattern was observed [Fig. 2b(1-ii)] that can be related to the orientation of PBDT molecules that have positive optical property [Fig. 2b(1-iii)]. Here, the blue bars and orange bars in Figure 2b(1-iii) indicate the orientation of the PBDT in the two perpendicular directions and black lines indicate the crease border lines on the two surfaces of the sample. Given the high transparency of the gel, this lattice-like birefringence pattern is attributed to the overlapping of the two individual birefringence patterns on the two surfaces of the gel, as the surface stripe crease patterns are aligned in perpendicular with each other on the two surfaces of the gel. This is confirmed by the POM images of two half pieces of the sample sliced through the middle of the thickness [Fig. 2b(2-i,3-i)]. Both POM images of the two sliced pieces show the stripe-like birefringence patterns that are in perpendicular to each other [Fig. 2b(2-ii,3-ii)]. The PBDT molecules across the crease border lines are aligned perpendicular to the border lines; while PBDT molecules in between the crease border lines are aligned parallel to the border lines [Figure 2b(2-iii,3-iii)]. The latter indicates that the bending of the bulk gel exerts a tension on the ridge surface and a compression on the basin surface of the bending³². Since the stripe-like creases on the two surfaces of the gel are in perpendicular, the PBDT molecules on the two surfaces are also aligned perpendicularly, both for those across and in between the crease border lines. As a result, the whole sample exhibits the “lattice” like birefringence pattern due to the cancellation of birefringence between the border lines, as shown in Figure 2b(1-ii, 1-iii)³³.

We should notice that the small amount of PBDT molecules (about 0.1 wt% for swollen sample) only serve as stress probes and they do not affect the swelling ratio, the mechanical property (supporting information and Figure S2), and the crease pattern formation of PDMA-PAA-Q gel¹⁰.

Effect of coupling of two instabilities

The transient surface creasing and saddle-like bending only occurred when the polyelectrolyte gel was allowed to swell very fast in water. When the gel was allowed to swell slowly in a humid vapor,

no mechanical instability occurred¹⁰. Two mechanical instabilities occur during the fast free swelling of the polyelectrolyte gel. One is the saddle-like bending induced by the swelling mismatch between the annulus and inner region of the disc shape gel [Fig. 3(a)], because the annulus region swells faster by taking water from the top, bottom and sides [Fig. 3(a-i)], while the inner disc region swells slower only by taking water from the top and bottom surfaces [Fig. 3(a-ii)]. When the inner radius of the annulus is larger than the radius of the disc, the annulus region is compressed, thus the saddle-like bending occurs to minimize the radius mismatch. Such a kind of saddle-like bending was also reported by Y. Klein, *et al.*, and M. Pezulla, *et al.*^{34,35}. Especially, the investigation reported by M. Pezulla, *et al.* using a disc-shaped elastomer made from a swellable annulus and an unswellable disc, is closely related to our system³⁵. The other is surface buckling due to swelling mismatch between the surface layer and inner layer. The surface instability induced by this type of swelling mismatch, as clarified by previous works, generally forms polygonal surface creasing [Fig. 3(b)]. The unique stripe-like creasing of crossed orientation on the two surfaces observed in this work is the result of coupling of the surface instability with the saddle-like bending. When the bulk gel deforms into saddle-like shape, the ridge of the bending releases and the basin of bending receives additional stresses [Fig.3(c-i)], as shown by the orientation of PBDT molecules shown in Figure 2. In the center of saddle, on the same point, one direction is in compression and the other direction is in extension. As a result, each surface of the sample receives anisotropic stress by the saddle-like bending, which changes the isotropic polygonal surface creasing into anisotropic, stripe-like pattern [Fig.3(c-ii,iii)].

We notice that although the bulk bending can induce anisotropy of surface crease, it is not necessary to give continuous stripe-like patterns. The coupling of surface instability and bulk deformation was also studied by observing the surface crease patterns of hydrogel sheets fixed, *prior to* swelling, onto a flat substrate and a saddle-shaped substrate, respectively (see supporting information and Figure S3). Isotropic polygonal surface crease was observed for the hydrogel fixed on the flat substrate, the same as reported before [Fig.4(a)]¹⁵. In contrary, anisotropic,

straight-grained surface crease was found on the hydrogel fixed on the saddle substrate [Fig.4(b)]. The results confirm that the saddle-shaped bending induces anisotropic surface creases, but not necessarily continuous stripes. Next part, we introduce a theory to explain the formation of anisotropic stripe creasing pattern on hydrogel surface.

Theoretical mechanism

Herein, let us consider the mechanism of creasing on the saddle-like hydrogel surface, based on the T. Tanaka's theory. In the beginning, we assume that the priority order of the energy due to compression is lowest with respect to suppression of an energy growth. Under this assumption, it is predicted that a thin gel in the form of a disc morphs into a saddle type minimal surface, because the stretching and bending energy are suppressed on a priority basis³⁵. After that, the energy due to compression will be minimized to an acceptable level. Therefore, in the following, we develop a theory by focusing on the energy due to compression of the mechanical potential energy suggested by Tanaka, and consider the influence of the compression with large deformation during swelling. Tanaka's theory is not intended to describe the dynamics in the swelling gel. However, it would be allowed to apply this theory for the crease pattern formation in the process of swelling, because the time scale of crease pattern formation is faster than that of the large deformation. That is, we refer the process of crease pattern formation in our system as a quasi-static transition. Furthermore, in order to fit it to our problem, we consider the energy due to compression from the geometry point of view. In ref. [25], the authors considered the restriction face as an x - y plane, and the energy due to compression, $U_{(\text{compression})}$, was described as follows:

$$U_{(\text{compression})} = \iiint P \left\{ 1 - \frac{1}{\sqrt{1 + (\vec{\nabla} w)^2}} \right\} d\vec{r} \cong \iiint \frac{P}{2} (\vec{\nabla} w)^2 d\vec{r}, \quad (1)$$

where, $w(x,y)$ and P represent the displacement of the top surface of the gel and the osmotic pressure, respectively. From the geometric viewpoint, it is possible to rewrite $U_{(\text{compression})}$ in eq. (1) as follows:

$$U_{(\text{compression})} = \iiint P\{1 - \cos \theta\} d\vec{r}, \quad (2)$$

where, θ is an angle between the standard layer (x - y plane) and the gel layer, *i.e.*, the angle between the normal directions of the two layers (See Fig. 5a-i). If we consider that the layer with the least deformity is the standard layer in Tanaka's system, a middle layer, Ω , of the gel will be regarded as the standard in our system with free swelling. That is, θ in eq. (2) represents the angle between the middle layer and the gel layer in our system (See Fig. 5a-ii). In order to evaluate $\cos\theta$, we set up the local coordinates of which the origin is some point on Ω . We choose this coordinate such that it consists of one outward normal direction and two principal curvature directions with respect to Ω (See Fig. 5b and Appendix 1). First, let us consider a point, R , on Ω . A position vector, $\vec{\varphi}(x, y)$, of R near the origin, O , can be described as $\vec{\varphi}(x, y) = (x, y, z(x, y))$ uniquely. Next, let us consider an inner point, Q , of the gel. According to ref. [25], we can treat the gel as a combination of thin layers, and then, Q is contained in some layer which is named the t -level with a parameter t as shown in Fig. 5a. Then, the position vector, $\vec{\phi}(x, y)$ of a point Q can be expressed by the following equation:

$$\vec{\phi}(x, y) = \begin{cases} \vec{\varphi}(x, y) + k(t, h)s(x, y)\vec{n}(x, y), & 0 \leq t \leq h, \\ \vec{\varphi}(x, y) + k(t, h)\bar{s}(x, y)\vec{n}(x, y), & -h \leq t < 0, \end{cases} \quad (3)$$

where, h , $\vec{n}(x, y)$, and $s(x, y)$ (or $\bar{s}(x, y)$) represent the half-thickness of the gel, an outward normal vector to Ω at R , and a displacement of the top (or bottom) surface with respect to the middle surface, respectively. Additionally, $k(t, h) = \sin(\pi t/2h)$ is constant with respect to x and y . It is then possible to obtain $\cos\theta$ at Q from an inner product of these normal vectors. As a result, the compression energy density, $U_{(\text{compression})}^Q$, in Q will be expressed by the following equation (See Appendix 2):

$$U_{(\text{compression})}^Q = 1 - \cos \theta = 1 - \frac{1}{A}. \quad (4)$$

If we supposed that the middle surface morphed into the minimal surface by the large deformation, A in eq. (4) can be calculated as follows:

$$A = \sqrt{\left(\frac{\kappa s_x}{1 - \kappa \kappa \Sigma}\right)^2 + \left(\frac{\kappa s_y}{1 + \kappa \kappa \Sigma}\right)^2} + 1, \quad (5)$$

where, $\kappa > 0$ is a positive curvature of middle surface. Here, at the point Q on the gel layer, the deformation of the gel will occur to suppress the total energy. Thus, the total energy converges to a minimal value (*i.e.*, A becomes bigger) with $s_x^2 + s_y^2 = \text{const.}$, then eq. (5) suggests that it is better for $s_y \rightarrow 0$ in the top surface because of $k \geq 0$ ($0 \leq t \leq h$). In contrast, $\bar{s}_x \rightarrow 0$ is better in the bottom surface because of $k < 0$ ($-h \leq t < 0$). The above discussion does not depend on a choice of the origin on Ω . Therefore, these results suggest that the top (or bottom) surface tends to tilt to the positive (or negative) curvature direction. The directions of the principal curvature are normal to each other, and same applies to the internal properties (such as creases, internal stress, and so on) of the top and bottom of the gel.

According to the above considerations, we can predict the crease pattern on the gel which is in the process of swelling with $\lambda_+ + \lambda_- = 0$. Now, we consider that the middle layer in the process of deformation can be described as $(x, y, z(x, y))$ in the global coordinate system. In particular, we assume that the middle layer is Scherk's minimal surface, *i.e.*, $z(x, y)$ can be described as follows:

$$z(x, y) = \log\left(\frac{\cos y}{\cos x}\right), \quad |x| < \frac{\pi}{2}, |y| \leq \frac{\pi}{2}.$$

Then, we can easily obtain the principal curvature directions on the global coordinate system as follows (See Appendix 1):

$$\vec{\xi}_{\pm} = \frac{\tan x \tan y \cos^{-2} y}{(1 + \tan^2 x + \tan^2 y)} \begin{pmatrix} 1 \\ 0 \\ \tan x \end{pmatrix} - \left\{ \frac{\cos^{-2} x \cos^{-2} y}{(1 + \tan^2 x + \tan^2 y)} \mp \sqrt{\frac{\cos^{-2} x \cos^{-2} y}{(1 + \tan^2 x + \tan^2 y)}} \right\} \begin{pmatrix} 0 \\ -1 \\ \tan y \end{pmatrix}. \quad (6)$$

If we consider the continuous crease on the surface as some orbit of the differential equation, $\vec{c}'_{\pm}(\tau) = \vec{\xi}_{\pm}$ (τ is a parameter, and prime means the derivative with respect to τ), with an appropriate initial condition, we can check the orbits of the top and bottom that are normal to each other as

shown in Fig. 6. These above considerations suggest that the creases which are normal to each other can be observed, if the large deformation at the time of swelling has the mean curvature equal to zero.

The theoretical prediction corresponds reasonably well with the above experimental observation, which justified the proposed mechanism. Therefore, these results indicate that surface crease patterns are affected by large three-dimensional shape change induced by geometric swelling mismatch.

Conclusion

In this study, we have investigated the mechanical instabilities of a thin polyelectrolyte hydrogel disc in the process of fast free swelling in pure water. During the swelling process, the gel morphed into a saddle-like shape and then the polygonal surface creases changed to stripe creases due to two swelling mismatches, surface layer/inner layers, and inner disc/outer annulus region. The stripe creases were formed uni-directionally, and were perpendicular to each other at the two surfaces of the sample. From the detail observation of the internal stress analyzed by the orientation of semi-rigid polyanions, we found that both surface creasing and bulk deformation minimize the swelling mismatch. We further demonstrated the surface pattern change of thin hydrogel films fixed onto flat or saddle-shaped substrates and these results confirmed the mechanical coupling of the surface instability and bulk deformation. Under the assumption that the gel morphs into a saddle-like shape with mean curvature of zero, it was theoretically suggested that the gel layer tends to tilt in the one of the principal directions by the minimization of total energy in ref. [25]. The direction of tilt of the gel layer was separated by the middle surface, therefore, the creases on the top and bottom surface were normal each other.

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Figures

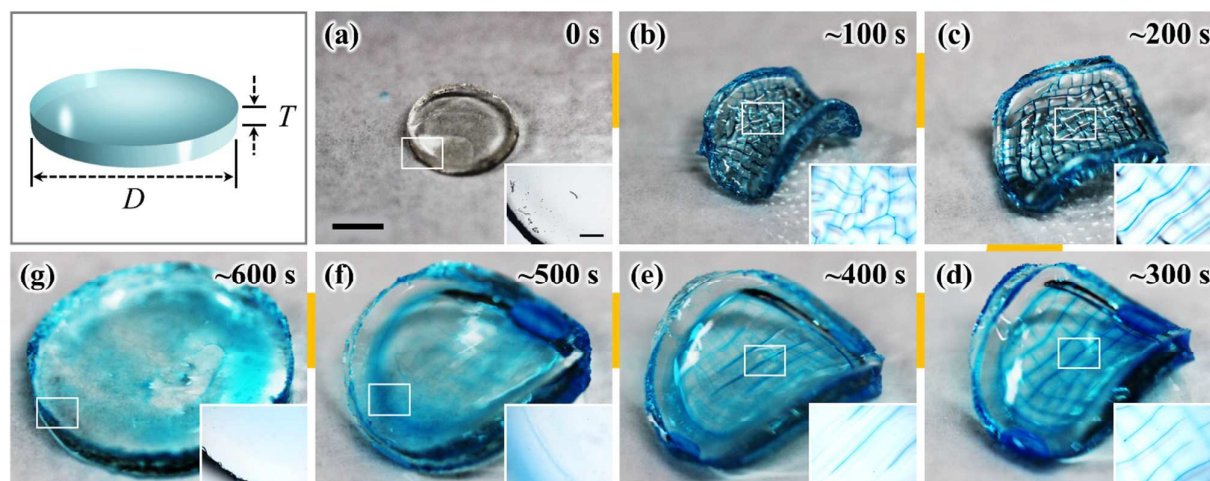


Figure 1| Evolution of surface crease pattern and bending of a disc shape polyelectrolyte hydrogel during free swelling in water. After the appearance of the isotropic polygonal surface crease, stripe-crossed surface pattern and saddle-like bending of the gel were observed. To observe clearly the shape and the boundary of surface pattern, the as-prepared hydrogel was swelled in water containing 0.05 wt% Alcian blue. Each inset in lower right corner reveals the clear surface pattern of the top surface observed with an optical microscope. All the images and insets are shown in the same scale as shown by the scale bars in 0 s (left: 3 mm, right: 500 μm). The dimension of the as-prepared gel was 6 mm (D) \times 1 mm (T). Even in the absence of Alcian blue, we observed exactly the same swelling behavior.

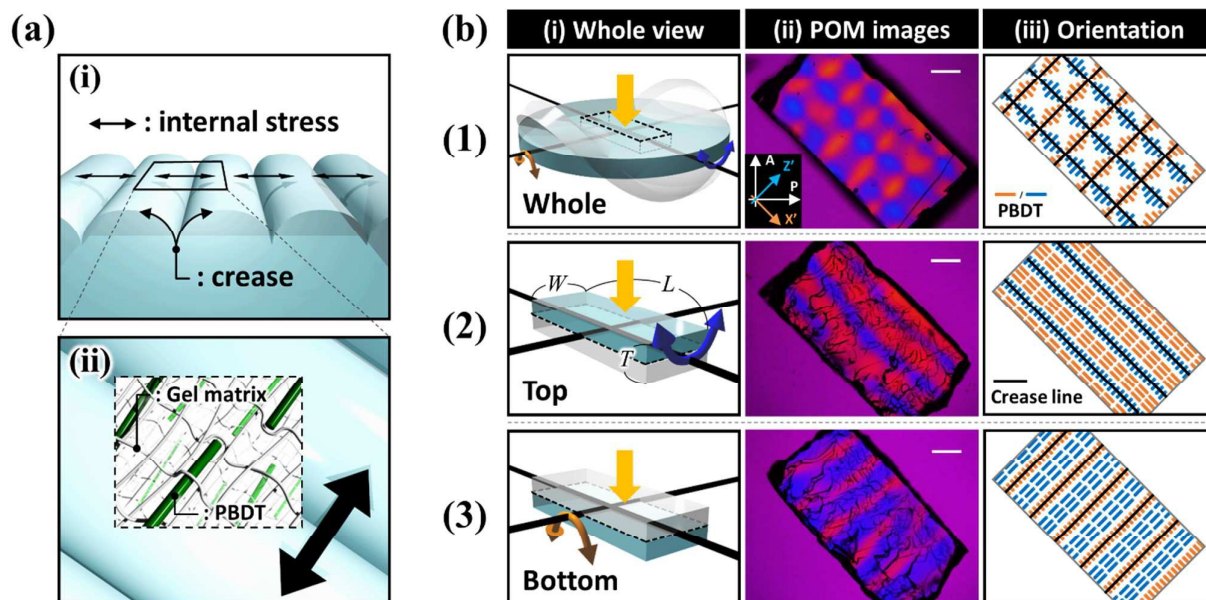


Figure 2| Polarized optical microscope (POM) observation of birefringence patterns due to the orientation of the rigid molecules (PBDT) induced by a fast-heterogeneous swelling of a PDMAPAA-Q hydrogel. (a) Schematic illustrations for the internal stress induced by creasing instability (i) and PBDT orientation inside gel matrix (ii). PBDT molecules were sensitively oriented along with the internal stress and fixed by polyion complexation even after swelling. (b) Birefringence pattern observation at equilibrium swollen state. The schematic illustration in (b-1-i) represents the equilibrium state of the gel, where the orange and blue arrows represent the bending direction of the saddle shape during swelling. The gel was cut from the disc-shape sample into specific dimensions about 7 mm (L) \times 4 mm (W) \times 2 mm (T) (b-1-i). To observe the birefringence pattern on the two surfaces of the gel separately, the sample of (b-1-i) is sliced into two sheets at the middle of the thickness direction to obtain the upper surface (b-2-i) and lower surface (b-3-i). The polarized optical microscope (POM) images of the (b-i) were observed from the thickness direction under crossed polarizers with 530 nm tint plate as shown in column (b-ii). Illustrations in column (b-iii) indicate the PBDT molecular orientation in the hydrogel and crease pattern during swelling. The POM observation confirms that the rectangular birefringence pattern of (b-1-i) sample is the result of the overlapping of the perpendicular aligned birefringence lines on two surfaces of the sample. All the POM images have the same scale bar (1 mm). Key: A, analyzer; P, polarizer; X' and Z', fast and slow axis of the tint plate, respectively.

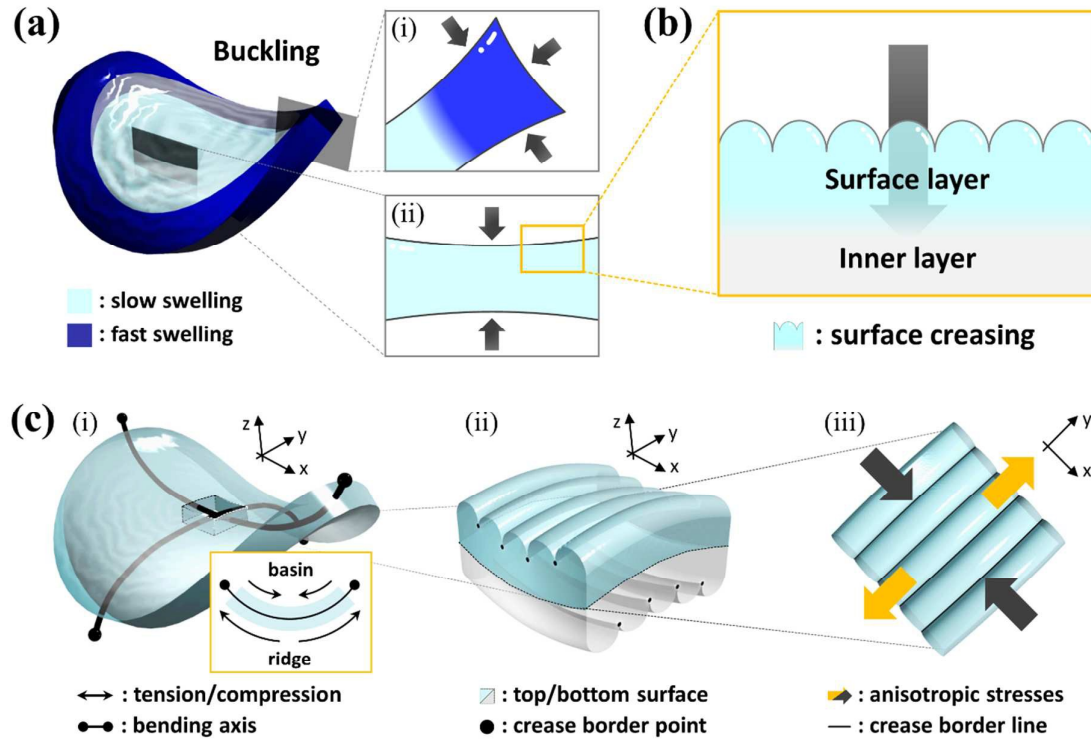


Figure 3| Schematic illustration of two kinds of swelling mismatch and their coupling to induce anisotropic surface creases during fast free swelling of a polyelectrolyte gel. (a) Swelling mismatch between the annulus (dark blue) and the inner disc (light blue) induced by the difference in swelling kinetics between the annulus and the inner disc. The annulus can absorb water from three directions (a-i), while the inner disc can only absorb water from two directions (a-ii) as shown by arrows in (a-i, ii). This swelling mismatch induces a saddle-like bending to minimize the swelling mismatch. (b) Swelling mismatch between the surface layer (light blue) and inner layer (gray) induced by the difference in swelling kinetics between the surface layer and the inner layer. Surface creasing instability is induced to minimize this swelling mismatch. (c) The two mechanical instabilities are coupled to induce anisotropic surface crease pattern. Bending of the sample exerts a tension to the ridge and a compression to the basin (c-i). The saddle-like bending induces anisotropic stresses, perpendicularly oriented, on the two surfaces of the sample (c-ii), which changes the isotropic polygonal crease patterns into the anisotropic stripe crease patterns aligned in right angles on the two surfaces (c-iii).

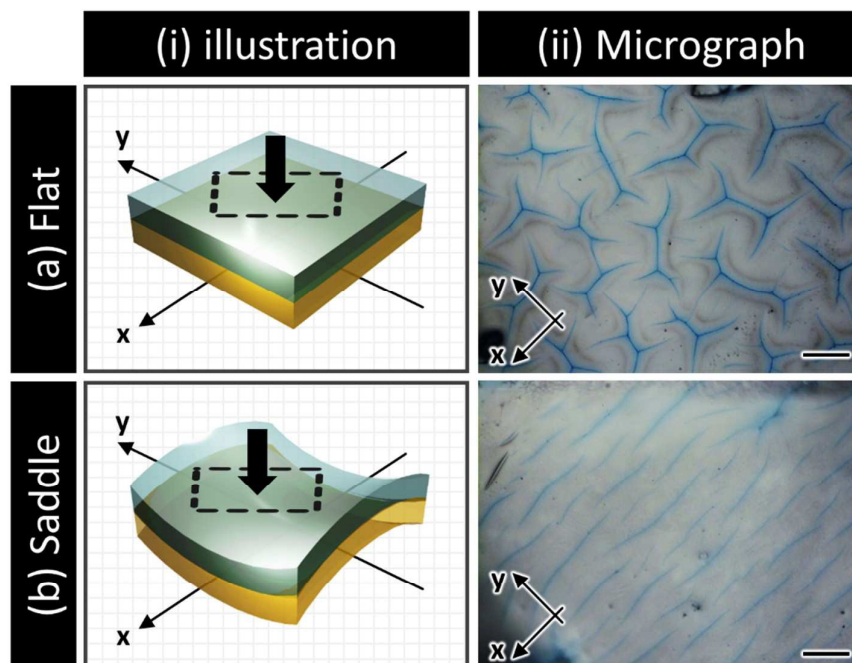


Figure 4| Experimental demonstration of the mechanical coupling of surface crease pattern with the saddle-like bending. Different surface crease patterns were formed for the hydrogel sheets fixed onto a flat substrate (a) and saddle-shaped substrate (b). Column (i) is a schematic illustration of the hydrogel-coated unswellable substrate, where the blue part represents the hydrogel sheet (thickness: 500 μm), while the yellow part indicates the polyurethane rubber which is the unswellable substrate. The micrographs presented in column (ii), observed with an optical microscope, show the surface morphology of the gel. In order to observe clearly the boundary of the surface pattern, the coated hydrogel sheets were swollen in water containing 0.05 wt % Alcian blue. After reaching the equilibrium state (~ 600 s), isotropic polygonal-like pattern and anisotropic straight-grained pattern were observed on the surface of (a-ii) and (b-ii), respectively. All the micrographs have the same scale bar (500 μm). After swelling, the thickness of gel reached to 1.15 mm. The curvature of saddle is 0.155 [1/mm].

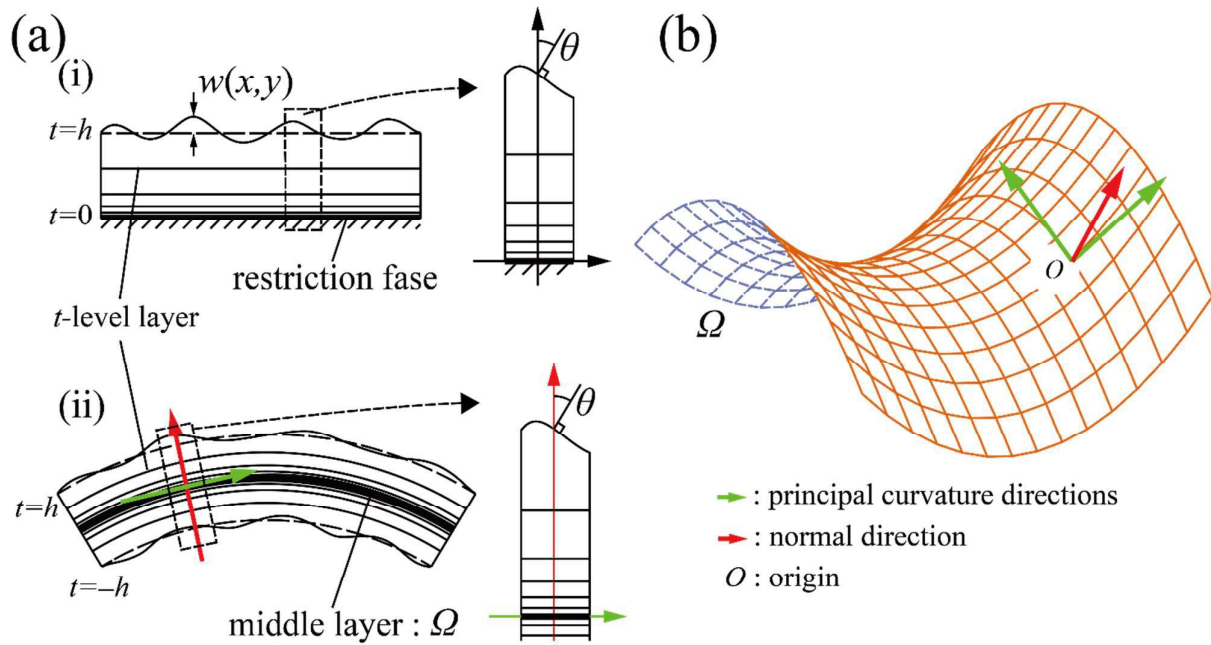


Figure 5| Schematic illustration of the model for describing the mechanical instability of gel sheet during free swelling. (a) The gel is treated as the combination of thin layers which are named t -level. In particular, the gel has the restriction face in the case of (i), and the gel passes through the process of the free swelling in the case of (ii). In both cases, θ means the angle between the layer with the least deformity and the t -level layer. (b) The local coordinates on the middle layer, Ω , of the free swelling gel. The green arrows correspond to the directions of the two principal curvatures, and the red arrow corresponds to the direction of the outward normal at the origin, O , on restriction phase.

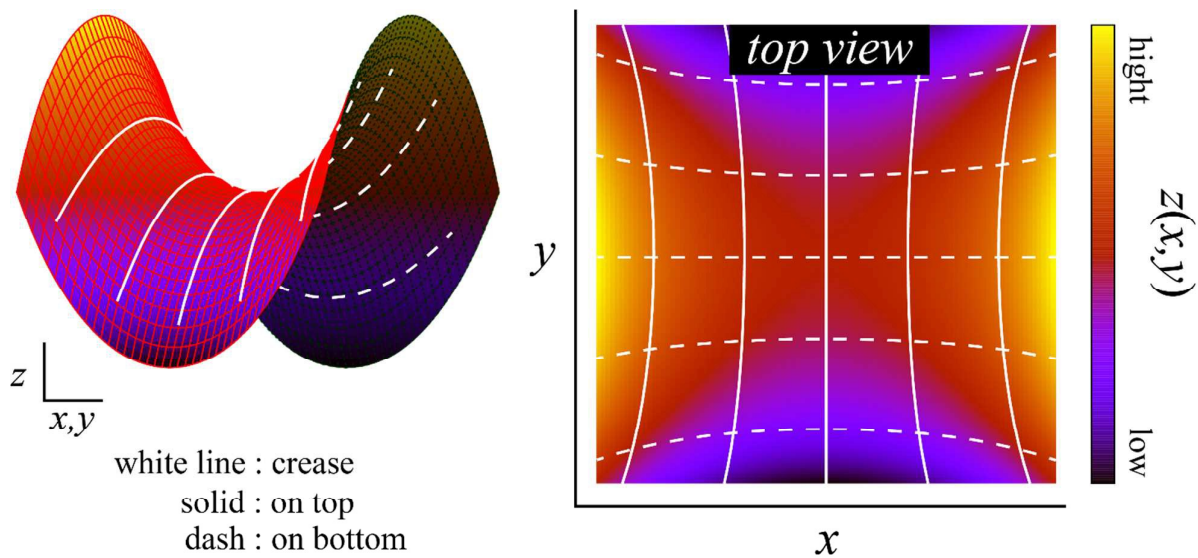


Figure 6| Creases on the Scherk's minimal surface. The colored surface is the Scherk's minimal surface, and the solid and dashed lines represent the creases of the top and bottom surfaces, respectively. These lines are the orbits obtained by the calculation of the differential equation from Eq. 6. On any intersection, these lines are at right angles to each other when viewed from the normal direction.