



Cite this: *EES Batteries*, 2025, 1, 913

Current distribution simulation of parallel-connected modules using degraded lithium-ion battery cells

Jusuke Shimura,^a Kanta Onodera,^b Hikari Watanabe,^b Isao Shitanda^b and Masayuki Itagaki^b

This study introduces a method for determining current distribution during the charging of modules composed of parallel-connected lithium-ion battery cells exhibiting varying levels of degradation. The proposed method was validated by examining current distribution in two- and three-cell parallel modules containing both new and degraded cells, demonstrating that the calculated charging currents were highly consistent with experimental measurements, with discrepancies between 1.1% and 2.2%. Furthermore, an overdistribution phenomenon was observed, where degraded cells received excessive current toward the end of the charging process. Investigation attributed this phenomenon to a rapid alteration in the internal resistance balance during charging. The proposed methodology is extendable to configurations with more than three cells through recursive calculations, highlighting its applicability in designing large-scale energy storage systems and strategies for repurposing used batteries.

Received 27th May 2025,
 Accepted 2nd June 2025
 DOI: 10.1039/d5eb00103j

rsc.li/EESBatteries

Broader context

The global shift toward renewable energy and a low-carbon future depends on effective and safe energy storage solutions. Lithium-ion batteries are essential for powering electric vehicles and large-scale energy storage systems, yet their performance degrades over time, creating challenges in safely reusing aging battery modules. Our research focuses on understanding and predicting how charging current divides among battery cells with different levels of degradation—a critical issue because uneven charging can lead to premature cell failure, safety hazards, and compromised system reliability. By developing a novel simulation method that accurately reflects real-world charging behavior, our work advances the ability to repurpose used batteries, reducing waste and mitigating the environmental impact of battery production. This approach not only supports the transition to sustainable energy systems but also provides valuable insights for policy makers, industry leaders, and researchers looking for safer, more efficient energy storage designs. Ultimately, our findings contribute to a more resilient and sustainable energy infrastructure, addressing pressing global issues such as energy security, resource conservation, and climate change.

1. Introduction

In recent years, the use of lithium-ion batteries has broadened to encompass large-scale applications such as electric vehicles and energy storage systems (ESSs).^{1–5} Given that lithium-ion batteries rely on scarce metals like cobalt, the reutilization of battery modules has gained attention for optimizing resource use.^{6–10} Reusing battery modules in different applications than their original purpose is termed “repurposing”, while utilizing them within the same application category is known as “reusing”.^{11,12} For instance, when constructing an ESS using low-capacity battery modules through repurposing, multiple battery modules need to be combined with varying degrees of degradation. Each battery

module experiences distinct types and degrees of degradation influenced by its usage history. Consequently, directly connecting these modules in parallel without proper management leads to complex current distribution dynamics.^{4,5,7,9–11} This can result in certain degraded modules experiencing unforeseen rapid charging. Such rapid charging accelerates the early degradation of lithium-ion batteries and heightens the risk of thermal runaway and fires in degraded battery modules.^{4,9,13,14} To mitigate these issues and ensure the safety and durability of repurposed battery modules, it is essential to comprehensively understand these complex current distribution phenomena and develop appropriate methods for combining modules.

Previous studies on parallel-connected battery groups under unmanaged conditions have documented instantaneous current distribution behaviors.^{15–20} For instance, Zabara *et al.* developed a highly accurate method to predict current distributions and voltage responses in hybrid battery/supercapacitor systems by utilizing differential evolution optimization algo-

^aMurata Manufacturing Co., Ltd, 1-10-1 Higashikotari, Nagaokakyo-shi, Kyoto 617-8555, Japan. E-mail: jusuke.shimura@murata.com

^bDepartment of Pure and Applied Chemistry, Faculty of Science and Technology, Tokyo University of Science, 2641 Yamazaki, Noda-shi, Chiba 278-8510, Japan



ithms based on electrochemical impedance spectroscopy (EIS) data.¹⁶ However, their approach is limited in simulation accuracy for extrapolated EIS measurement regions, particularly in extremely high- or low-frequency domains.

In this study, we have developed a simulation method that employs reference data obtained from direct-current charging at zero frequency to calculate long-term current distribution behavior across the full range from fully discharged to fully charged states. Additionally, we explore methods for simulating distributions involving three or more cells.

2. Theory

Instead of directly addressing the issue of the current distribution in an ESS composed of multiple battery modules, we employed a downscaling approach in which the fundamental aspects of the problem remain unchanged.

2.1 Current distribution ratio

In this study, we introduced the current distribution ratio i_j as a metric representing the proportion of the total current allocated to each cell j in a parallel-connected module comprising n cells.

$$\sum_{j=1}^n i_j = 1 \quad (1)$$

For example, consider two cells ($n = 2$) connected in parallel, as illustrated in Fig. 1. In this configuration, the total current I flowing through the module can be expressed using current distribution ratios i_1 and i_2 :

$$i_1 I + i_2 I = I \quad (2)$$

Furthermore, let us denote the open-circuit voltage (OCV) of each cell as $V_{OC,j}$, its internal resistance as R_j , and overvoltage as η_j . As all the cells in a parallel connection share an equal cell voltage V , they satisfy the following relationship:

$$V_{OC,1} + \eta_1 = V_{OC,2} + \eta_2 = V \quad (3)$$



Fig. 1 Current distribution in a two-parallel-module configuration. i_1 and i_2 represent the current distribution ratios, expressed as proportions.

The overvoltage of each cell can thus be expressed as $\eta_j = R_j i_j I$. Substituting this expression into the above equation and solving the resulting simultaneous equations yields explicit expressions for the current distribution ratios i_1, i_2 of each cell.

$$\begin{cases} i_1 = \frac{V_{OC,2} - V_{OC,1}}{(R_1 + R_2)I} + \frac{R_2}{R_1 + R_2}, \\ i_2 = \frac{V_{OC,1} - V_{OC,2}}{(R_1 + R_2)I} + \frac{R_1}{R_1 + R_2}. \end{cases} \quad (4)$$

The first term on the right-hand side of these equations represents the contribution of the OCV differences between the cells, whereas the second term accounts for the balance of their internal resistances.

2.2 Simulation of constant current charging in a two-cell parallel module

We outline the procedure for calculating the evolution of current distribution ratios $i_1(t)$ and $i_2(t)$ over time during constant-current (CC) charging of a parallel module consisting of two cells. The calculated current distribution ratios are discrete values obtained at specific time steps $t = 0, \Delta t, 2\Delta t, \dots$.

Before starting the calculations, two types of experimental reference data were prepared for each cell. The first dataset comprises the OCV $V_{OC,j}$ as a function of charge capacity Q_j , commonly referred to as the charging curve. The second dataset includes internal resistance R_j as a function of the charge capacity Q_j . Importantly, these internal resistance measurements account for all resistance components during charging, including concentration polarization with exceptionally large time constants, thereby reflecting real-world charging conditions. Internal resistance was determined by subtracting $V_{OC,j}$ from the cell voltage V_j measured during CC charging and then dividing the result by the applied current. Although both datasets consisted of discrete experimental points, continuous functions were necessary for subsequent analyses, necessitating appropriate interpolation of these discrete data.

The time evolution of the current distribution ratios was calculated using the following process: Initially, at $t = 0$, both cells were assumed to be fully discharged with initial charge capacities $Q_1(t) = Q_2(t) = 0$. Subsequently, based on their respective charge capacities, $Q_j(t)$, OCV $V_{OC,j}$ and internal resistances R_j were retrieved from the corresponding reference datasets (*). Utilizing the parameters defined in eqn (4), the current distribution ratios $i_1(t)$ and $i_2(t)$ were then calculated to determine the proportion of the charging current flowing into each cell. Assuming these currents remain constant over an interval Δt , the incremental increases in charge capacities $\Delta Q_1(t)$ and $\Delta Q_2(t)$ can be expressed as follows:

$$\begin{cases} \Delta Q_1(t) = i_1(t)I\Delta t, \\ \Delta Q_2(t) = i_2(t)I\Delta t. \end{cases} \quad (5)$$

By adding these increments to their respective existing charge capacities at each step, we obtain updated charge capacities $Q_1(t + \Delta t)$ and $Q_2(t + \Delta t)$ at time step $t + \Delta t$. From this point onward, starting again at step (*), the process is iteratively



repeated to obtain simulation results over consecutive time intervals.

Although cells 1 and 2 are connected in parallel, it should be noted that in most cases both their charge capacities and their states of charge (SoCs) do not remain identical during charging. Unless the reference data for both cells are completely identical, discrepancies in OCV differences or internal resistance ratios prevent equal current distribution. As charging progresses, these differences accumulate over time, leading to conditions where $Q_1(t) \neq Q_2(t)$ for most cases when $t > 0$. Moreover, no constraint exists to enforce the alignment of the SoCs which are defined as the ratio of the current charge capacity to the full charge capacity.

2.3 Current distribution in modules with three or more cells

For modules with three or more parallel-connected cells, calculations can be performed by recursively grouping two cells into a single equivalent cell. For example, consider a module with three parallel-connected cells: cells 1, 2, and 3. First, cells 1 and 2 are conceptually grouped into a two-cell parallel module, and the current distribution is calculated under CC charging conditions. This calculation enables the derivation of composite reference data for this virtual two-cell module, specifically the composite OCV $V_{OC,1+2}$ and the composite internal resistance R_{1+2} . These values are defined as follows:

$$\begin{cases} Q_{1+2}(t) = Q_1(t) + Q_2(t), \\ R_{1+2}(t) = \frac{R_1(Q_1(t))R_2(Q_2(t))}{R_1(Q_1(t)) + R_2(Q_2(t))}, \\ V_{OC,1+2}(t) = \frac{V_{OC,1}(Q_1(t)) + R_1(Q_1(t))i_1(t)I + V_{OC,2}(Q_2(t)) + R_2(Q_2(t))i_1(t)I}{2} - R_{1+2}(t)I. \end{cases} \quad (6)$$

The composite charge capacity $Q_{1+2}(t)$ is the sum of the charge capacities of cells 1 and 2. The composite internal resistance $R_{1+2}(t)$ is calculated as the equivalent resistance of the two parallel resistors, based on the internal resistances of cells 1 and 2 at their respective charge capacities. Finally, the composite OCV $V_{OC,1+2}(t)$ was obtained by subtracting the overvoltage of the virtual two-cell module from the average cell voltage derived from the OCVs and the overvoltage of both cells. The reference data for this virtual two-cell module $Q_{1+2}(t)$, $R_{1+2}(t)$, $V_{OC,1+2}(t)$ consist of discrete values recorded at a specific time interval Δt . Similar to individual cell reference data, appropriate interpolation is necessary to ensure continuity for subsequent calculations. Fig. 2 provides a flowchart of the overall simulation procedure for clarity. An example figure to clarify how cells are grouped and current values are calculated is shown in Fig. 3.

3. Experimental

3.1 Battery cells

In this study, three cylindrical lithium-ion battery cells (US18650FTC1, Murata Manufacturing Co., Ltd) were employed. These cells utilized LiFePO_4 (LFP) as the positive

electrode active material, graphite as the negative electrode active material, and had a rated capacity of 1.05 Ah. Among the three cells, two were stored in isothermal chambers at 80 °C and 90 °C for 25 days. The unused cell is designated as “cell N”, while the cells stored at 80 °C and 90 °C are referred to as “cell D1” and “cell D2”, respectively.

3.2 Charging tests for parallel-connected modules

Charging experiments were conducted using a parallel two-cell module comprising cell N and cell D2. Each cell was individually connected to a potentiostat/galvanostat (Bio-Logic, SP-240), placed in an isothermal chamber maintained at 23 °C, and discharged at a constant current of 0.2C-rate (210 mA). Discharging was terminated when the voltage reached 2.0 V, herein referred to as the fully discharged state.

After both cells N and D2 were individually drained to their fully discharged states, they were connected in parallel to form a two-cell parallel module. To measure the charging current for each cell within the module, two clamp-type current probes (Yokogawa Electric Corp., Model 701917) were attached to each cell's negative-terminal wiring, and data were recorded using a Yokogawa DL950 ScopeCorder® data logger. The two-cell parallel module was then placed in an isothermal chamber maintained at 23 °C and charged at a constant 1C-rate (2.1 A) using a potentiostat/galvanostat.

Subsequently, charging experiments were performed on all three cell types (cell N, cell D1, and cell D2) by assembling a three-cell parallel module. Prior to connection, each cell was individually fully discharged. Three clamp-type current probes were installed to separately measure the charging current entering each cell. This three-cell parallel module was then placed in an isothermal chamber at 23 °C and charged at a constant 1C-rate (3.15 A) (Fig. 4).

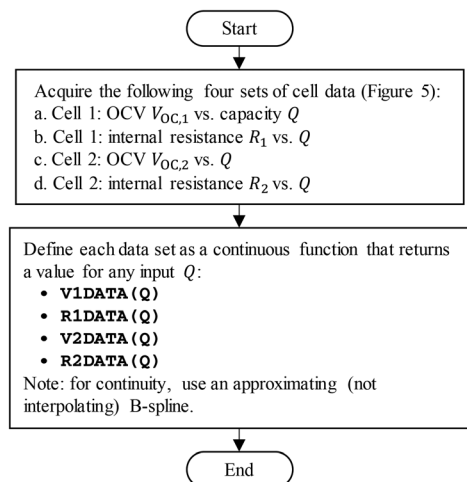
3.3 Preparation of reference data

For cell N, cell D1, and cell D2, two sets of reference data were prepared as outlined in the previous section: the OCV $V_{OC,j}$ as a function of charge capacity Q_j and the internal resistance R_j as a function of charge capacity.

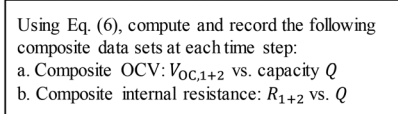
To obtain the OCV, each cell was first fully discharged and then subjected to CC charging at a 0.02C-rate (21 mA). During the CC charging process, the cell voltage was measured and recorded as $V_{OC,j}$. To determine the internal resistance R_j , the overvoltage at various charge capacities was initially calculated by subtracting the corresponding $V_{OC,j}$ from the measured cell voltage during CC charging at a 1C-rate (1.05 A). The internal resistance was then derived by dividing this overvoltage by the current at the 0.98C-rate (1.029 A).



(a) Preparation



* To generate composite data for the two-cell parallel module consisting of Cells 1 and 2, insert the following step. Once all discrete time-step data have been collected, convert them into continuous functions $V12DATA(Q)$ and $R12DATA(Q)$.



(b) Two-Cell Distribution Simulation



Fig. 2 Flowchart of preparation and simulation steps.

Both reference datasets comprise discrete values obtained experimentally for specific charge capacities. However, because continuous functions were necessary for the simulations, these discrete datasets were transformed into continuous functions by applying a non-rational, uniform, cubic B-spline implemented *via* a custom Excel VBA function.

3.4 Current distribution calculation for parallel-connected modules

Utilizing the reference data for cells N, D1, and D2, current distribution simulations during CC charging were conducted following the procedure outlined in the previous section. The simulations were performed for two configurations: a two-cell parallel module consisting of cells N and D2, and a three-cell parallel module consisting of cells N, D1, and D2.

A time step Δt of 15 s was employed in all simulations. During the simulations, both factors contributing to the current imbalance—the ODD (OCV difference dependent) term and the RBD (resistance balance dependent) term from eqn (4)—were calculated separately to evaluate their respective impacts on current distribution. All simulations were per-

formed using Microsoft Excel for Office 365 (MSO). The B-spline approximation was implemented with a custom VBA function. Correct operation was confirmed by visually comparing interpolated curves against raw data.

4. Results and discussion

4.1 Reference data

Fig. 5 presents the reference data for cells N, D1, and D2. Based on the OCV measurements conducted at a 0.02C-rate, the charge capacities were determined to be 1110, 1010, and 990 mA h for cells N, D1, and D2, respectively. Based on the measured values, the capacity loss for D1 and D2 were determined to be 10% and 12%, respectively.

Regarding the shapes of the charging curves, cells N, D1, and D2 exhibited nearly identical profiles except near full charge. The lithium-ion batteries in this study utilized Li_xFePO_4 as the cathode material. When x is between 0.032 and 0.962, LiFePO_4 and FePO_4 coexist as two distinct phases, resulting in a nearly constant open-circuit potential.²¹





Fig. 3 An example illustrating how cells are grouped and currents are calculated. First, the total current I is split between the composite cell (cells 1 + 2) and cell 3 in a two-cell distribution simulation. During that simulation, the current allocated to the composite cell (cells 1 + 2) is further split between cell 1 and cell 2 in a second two-cell distribution simulation.



Fig. 4 Schematic of the charging test for three-parallel-module configuration.

Therefore, the non-uniform behavior observed in the OCV in Fig. 5 is attributed primarily to variations in anode potential. Since this behavior remained largely consistent, high-temperature storage did not significantly affect anode capacity. The overall capacity loss may result from cathode degradation or other mechanisms such as loss of lithium inventory and electrode slippage; definitive attribution would require further half-cell or materials analyses.

Subsequently, internal resistance was examined and found to increase in the following order: cell N, cell D1, and cell D2.



Fig. 5 Reference data for cells N, D1, and D2. Open circle, open triangles, and crosses indicate the OCV of cells N, D1, and D2, respectively. Filled circles, filled triangles, and plus signs represent the internal resistance of cells N, D1, and D2, respectively.

Regarding the timing of internal resistance fluctuations during charging, all three cells displayed nearly identical patterns in the first half of charging, reaching a minimum at ~ 130 mA h and a maximum at ~ 230 mA h. Although the timing of the variations in the first half was almost identical across the cells, differences in behavior became apparent in the latter half. In all cases, internal resistance sharply increased just before full charging; however, the timing of this surge differed—with cell D2 exhibiting the increase first, followed by cell D1, and then cell N.

Considering that the anode capacity hardly declined, and that capacity loss is mainly caused by cathode degradation, the uniform behavior in the first half is primarily attributed to the anode, whereas the variations in the latter half are attributed to the cathode. In addition, the sudden surge in internal resistance in the latter half is interpreted as resulting from lithium extraction from the LFP cathode.

4.2 Current distribution

Fig. 6(a) displays the experimentally observed current distribution for cells N and D2 connected in parallel, while Fig. 6(b) shows the calculated current distribution based on the reference data for these cells. Fig. 6(c) illustrates the ODD and RBD term values for cell N derived from the calculations. We emphasize that the simulation relies exclusively on measured OCV and internal resistance curves (ODD and RBD term values) and does not attempt to model internal physical phenomena such as temperature gradients or spatially varying reaction rates.

Initially, the root-mean-square error (RMSE) between the measured currents in Fig. 6(a) and the calculated currents in Fig. 6(b) was calculated. The RMSE for the charging currents of cell N and cell D2 were 13.3 mA and 13.4 mA, respectively, which correspond to errors of 1.2% and 1.4% relative to the average measured current. These low RMSE values indicate





Fig. 6 (a) Observed current distribution for cells N and D2 connected in parallel. (b) Calculated current distribution using reference data from cells N and D2. In both panels, the solid line represents the charging current flowing into cell N, the dashed line represents the charging current flowing into cell D2, and the dash-dotted line represents the module voltage. (c) Calculated ODD (solid line) and RBD (dashed line) values for cell N obtained during the analysis.

that the calculated results closely match the experimental measurements.

Thereafter, the experimental data presented in Fig. 6(a) are analyzed. Despite charging the two-cell module at a constant current of 2.1 A, the current was unevenly distributed between cells N and D2, and the distribution ratio varied throughout the charging process. In detail, with respect to the charging current for cell N, the minimum and maximum values were observed at 5.5 min (point A) and 9.5 min (point B), and another set of minimum and maximum values at 19.5 min (point C) and 31.5 min (point D). Furthermore, up to 54 minutes (point E), a larger current flowed into cell N compared to cell D2. However, at point E, this pattern reversed, resulting in a greater current being delivered to cell D2 thereafter.

The calculated current variations closely matched the experimental results, except during the initial approximately 1.5 minutes period (Fig. 6(b)). Specifically, the extrema corre-

sponding to points A, B, C, and D—represented as A', B', C', and D' in the simulations—were observed, and the current-reversal phenomenon at point E (corresponding to E' in the simulation) was also reproduced. The discrepancy during the initial 1.5 minutes is attributed to the voltage difference between fully discharged cell N and cell D2; due to differences in internal resistance, the voltage of fully discharged cell D2 is higher than that of cell N. In the experiments using the real cells, when the cells are connected in parallel, a balancing current flows to adjust the voltage, but such an adjustment is not incorporated in the simulation. As a result, an instantaneous large current is estimated to have flowed into the lower-voltage cell N at the beginning of the simulation.

Fig. 6(c) portrays that the ODD term remains negative throughout the charging process, indicating that the OCV of cell N is consistently higher than that of cell D2. Since the OCV increases monotonically during charging, this suggests that the SoC of cell N was always higher than that of cell D2, meaning that cell N was being charged ahead of cell D2. Additionally, the RBD term stays above 0.5, indicating that the internal resistance of cell N remains consistently lower than that of cell D2. Although the internal resistance varied considerably near full charge (Fig. 5), the internal resistance of cell D2 remained higher than that of cell N.

Subsequently, the origins of the extrema were examined to determine whether they arose from differences in OCV or internal resistance. In the simulation near point A, the RBD term exhibits an upward convex profile, whereas the ODD term shows a downward convex profile. This indicates that the minimum charging current at point A is predominantly attributable to the OCV difference. Similarly, around point B, the RBD term displays a downward convex profile, and the ODD term presents an upward convex profile, suggesting that the maximum charging current at point B is also primarily due to the OCV difference. At point C, the simulation demonstrates that the charging current for cell N decreases monotonically from point B to point C, reaches a minimum at point C, and then increases monotonically up to point D. Furthermore, the simulation reveals that the overall variation from point B to point D is largely driven by the ODD term, with only the region near point C significantly influenced by the RBD term. Therefore, although the resistance balance partially affects the minimum at point C, the dominant factor across the range from points B–D is the OCV difference. Similarly, the maximum charging current for cell N observed at point D is primarily ascribed to the OCV difference between cell N and cell D2 at that time.

Because extrema at points A, B, C, and D were observed during the first half of the charging process, they were considered attributable to the anode. Graphite, utilized as the anode material, undergoes alterations in its staging structure during charging, leading to intricate variations in both the solid-state diffusion coefficient of lithium within the graphite particles and the anode potential.^{22,23} In this experiment, the charging of cell N consistently preceded that of cell D2, and the staging transitions occurred at different times.



Consequently, if discrepancies in the solid-state diffusion coefficient emerged from these timing mismatches, they manifested as peaks associated with the RBD term, while potential discrepancies appeared as peaks related to the ODD term.

4.3 Overdistribution phenomenon in degraded cell D2

As illustrated in Fig. 6(a), when the module comprising cells N and D2 was connected in parallel and subjected to CC charging, an overdistribution phenomenon was observed near the end of charging (after point E), where the current flowing into cell D2 exceeded that flowing into cell N. This section examines this phenomenon in detail.

The primary cause was the rapid changes in the internal resistance balance. Notably, Fig. 5 shows that each cell's internal resistance rises sharply near full charge during single-cell charging; we infer that the rapid resistance increase of cell N in the parallel module has the same origin. As depicted in Fig. 6(c), the RBD term experienced a sharp decline near point E'. Consequently, the excessive current overdistribution to cell D2 observed at the end of charging in actual cells was largely influenced by this shift in the internal resistance balance. However, as the RBD value consistently remained above 0.5 and the internal resistance of cell D2 did not fall below that of cell N, the variations in the internal resistance alone cannot completely account for this phenomenon.

Furthermore, the ODD term remains consistently negative, signifying that the SoC of cell N persistently surpasses that of cell D2, which is critical. Under these circumstances, an OCV difference develops between the two cells, resulting in a tendency to allocate more current to cell D2. Moreover, as charging nears its end, the internal resistance of cell N—which, owing to its higher SoC, reaches full charge sooner—surges sharply before that of cell D2, abruptly upsetting the resistance balance and causing an overdistribution phenomenon in which cell D2 receives more current than cell N.

In summary, the overdistribution to cell D2 is considered to occur when two conditions are met: first, during charging, cell N's SoC remains higher than that of cell D2 ($ODD < 0$), and second, under these conditions, cell N reaches the charging endpoint earlier with a rapid increase in internal resistance.

4.4 Current distribution in a three-cell module

Fig. 7(a) displays the measured current distribution from cells N, D1, and D2 connected in parallel, whereas Fig. 7(b) shows the calculated current distribution based on reference data. The RMSE for the charging currents of cells N, D1, and D2 were 24.8 mA, 16.8 mA, and 11.0 mA, corresponding to error rates of 2.2%, 1.6%, and 1.1% relative to their respective average measured charging currents. These results confirm that the simulation achieved highly accurate predictions even in a three-cell configuration. Furthermore, a concentration of charging current in cells D1 and D2 near the end of charging was observed experimentally and successfully replicated by the simulation.

Additionally, qualitative features, such as the number of extrema in the current profiles, were consistent between the experimental and simulation results. The success of accurately



Fig. 7 (a) Observed current distribution for cells N, D1, and D2 connected in parallel. (b) Calculated current distribution using reference data from cells N, D1, and D2. In both panels, the solid line represents the charging current flowing into cell N, the dashed line represents the charging current flowing into cell D1, the dotted line represents the charging current flowing into cell D2, and the dash-dotted line represents the module voltage.

simulating the current distribution behavior in this three-cell module validates the effectiveness of the recursive approach described in Section 2 for combining two or more cells into equivalent composite units for modeling purposes. By iteratively applying this recursive method, modules containing four or more cells can be simulated with comparable accuracy. Error accumulation arising from measurement equipment specifications and environmental conditions has not been considered in this recursive grouping approach and is beyond the scope of this study.

5. Conclusion

In this study, we developed a precise method for simulating the charging current distribution in modules composed of multiple parallel-connected lithium-ion battery cells with varying levels of degradation and validated its accuracy by comparing the calculated values with experimental measurements. The charging currents calculated using the proposed method closely matched the measured values, thereby demonstrating its effectiveness in predicting the performance of parallel-connected lithium-ion battery modules. Furthermore, this method can be recursively applied to configurations with three or more cells arranged in complex patterns, highlighting its potential for large-scale system deployment. We introduced a current distribution ratio, comprising ODD and RBD terms, as



- supercapacitor energy storage systems, *J. Energy Storage*, 2021, **43**, 103185.
- 17 M. P. Klein and J. W. Park, Current distribution measurements in parallel-connected lithium-ion cylindrical cells under non-uniform temperature conditions, *J. Electrochem. Soc.*, 2017, **164**, A1893.
- 18 Q. Qin, X. Li, Z. Wang, J. Wang, G. Yan, W. Peng and H. Guo, Experimental and simulation study of direct current resistance decomposition in large size cylindrical lithium-ion battery, *Electrochim. Acta*, 2023, **465**, 142947.
- 19 X. Liu, W. Ai, M. N. Marlow, Y. Patel and B. Wu, The effect of cell-to-cell variations and thermal gradients on the performance and degradation of lithium-ion battery packs, *Appl. Energy*, 2019, **248**, 489–499.
- 20 M. J. Brand, M. H. Hofmann, M. Steinhardt, S. F. Schuster and A. Jossen, Current distribution within parallel-connected battery cells, *J. Power Sources*, 2016, **334**, 202–212.
- 21 A. Yamada, H. Koizumi, N. Sonoyama and R. Kanno, Phase change in Li_xFePO_4 , *Electrochem. Solid-State Lett.*, 2005, **8**, A409–A413.
- 22 T. Zheng, J. N. Reimers and J. R. Dahn, Effect of turbostratic disorder in graphitic carbon hosts on the intercalation of lithium, *Phys. Rev. B:Condens. Matter Mater. Phys.*, 1995, **51**, 734.
- 23 Z. Ogumi and M. Inaba, Electrochemical lithium intercalation within carbonaceous materials: intercalation processes, surface film formation, and lithium diffusion, *Bull. Chem. Soc. Jpn.*, 1998, **71**, 521–534.

