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# Reaction kinetics for ammonia synthesis using ruthenium and iron based catalysts under low temperature and pressure conditions†

T. Cholewa,<sup>ID</sup> \*<sup>ab</sup> B. Steinbach,<sup>a</sup> C. Heim,<sup>a</sup> F. Nestler,<sup>ID</sup> <sup>a</sup> T. Nanba,<sup>c</sup> R. Güttel,<sup>ID</sup> \*<sup>b</sup>  
and O. Salem‡<sup>a</sup>

Ammonia (NH<sub>3</sub>) production using green hydrogen and its emerging application as carbon-free energy carrier or fuel is predicted to play an important role for the global energy transition. Yet, the inherently fluctuating production of hydrogen from renewable energy and the corresponding new boundary conditions for NH<sub>3</sub> synthesis require efficient and intensified processes. A key strategy for the intensification of the NH<sub>3</sub> synthesis is the shift of the synthesis conditions to lower temperature and pressure compared to the conventional Haber–Bosch process. In this work, the reaction kinetics of ruthenium- and iron-based catalysts are determined experimentally at pressures between 10 to 80 bar and at temperatures from 350 to 450 °C. Using axially resolved temperature and concentration measurement, detailed experimental data were obtained in the kinetic regime and utilized to develop kinetic models for both catalysts. Therefore, an ideal plug-flow model for a fixed bed reactor, considering the axial temperature profile, is used to estimate the kinetic parameters. The developed kinetic models are based on the extension of the Temkin equation, which is adapted for both catalysts. Remaining deviation between simulated and experimental data is reduced to a root-mean-square error for the molar fraction of NH<sub>3</sub> of below 0.6%. The proposed extension of the Temkin equation allowed the reduction of this deviation by 20–30% compared to the conventional Temkin expression, which underlines the relevance of the novel kinetic expressions. Based on the validated kinetic models, concepts for process intensification and modularization of the NH<sub>3</sub> synthesis can be developed towards industrial realization.

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## Introduction

Deceleration of the temperature rise to the limit of 1.5 °C has become a global goal for researchers. This goal can only be attained by drastic reduction of CO<sub>2</sub> emissions across all sectors, emphasizing a substitution of fossil energy by renewable energy. Therefore, chemical energy carriers, fuels and chemical feedstocks need to be defossilized in the near future.<sup>1</sup> Ammonia (NH<sub>3</sub>), produced from renewable energy, is considered as a promising hydrogen (H<sub>2</sub>) carrier for the global point-to-point trade, shipping fuel, and for combined power generation. Considering the high global demand for low-carbon H<sub>2</sub>

projected to reach 500–650 Mt per annum by 2050, the demand for NH<sub>3</sub> as sustainable H<sub>2</sub> carrier and fuel is expected to grow three to four-fold compared to today's market.<sup>2</sup> Current NH<sub>3</sub> production *via* the Haber–Bosch (HB) process based mainly on natural gas (NG) as feedstock is currently the major pathway with an estimated global production capacity of 190 Mt in 2021, while causing *ca.* 2% of the annual global CO<sub>2</sub> emissions.<sup>3</sup> The shift from fossil feedstock-based NH<sub>3</sub> synthesis to a sustainable Power-to-Ammonia (PtA) process based on renewable energy therefore opens new horizons for NH<sub>3</sub> as gamechanger in the transition of the global energy system.

The conventional NH<sub>3</sub> synthesis is characterized by high reaction temperatures of 400 to 600 °C to obtain sufficient catalytic activity of commonly used Fe-based catalyst. Consequently, high pressures of 150 to 250 bar are required to achieve thermodynamic favorable conditions for the exothermic reaction given in eqn (1). However, the per pass conversion is limited under industrial synthesis conditions to 15 to 20% by thermodynamic equilibrium, making a product separation and recirculation of non-converted educts essential.<sup>4</sup>

<sup>a</sup>Fraunhofer Institute for Solar Energy Systems ISE, Heidenhofstr. 2, 79110 Freiburg, Germany<sup>b</sup>Institute of Chemical Engineering, Ulm University, Albert-Einstein-Allee 11, 89081 Ulm, Germany. E-mail: robert.guettel@uni-ulm.de<sup>c</sup>Renewable Energy Research Center, National Institute of Advanced Industrial Science and Technology, AIST, 2-2-9 Machiikedai, Koriyama, Fukushima 963-0298, Japan. E-mail: thomas.cholewa@ise.fraunhofer.de† Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d4se00254g>

‡ Current address: Air Company, 407 Johnson Avenue, Brooklyn, New York.



In the centennial history of industrial  $\text{NH}_3$  synthesis, the specific energy demand for the process was reduced to the range of 26–28  $\text{GJ t}^{-1}$  of  $\text{NH}_3$  approaching the thermodynamic limit of 22.5  $\text{GJ t}^{-1}$  for the NG-based production.<sup>5</sup> The reduction of energy consumption was mainly achieved by the scale-up of the production facilities to capacities exceeding 1000  $\text{t h}^{-1}$  using positive scale-effects.<sup>6</sup> However, the requirements for the sustainable PtA process differ significantly. On the one hand, the intermittency of  $\text{H}_2$  supply from renewable resources must be considered.<sup>7</sup> On the other hand, the scale for the production is expected to decrease according to the capacity of electrolyzers and the remote production sites based on local renewable energy production.<sup>8</sup> For small-scale PtA units based on the conventional HB process, scientific literature reported an energy demand of 33–46  $\text{GJ t}^{-1}$ , which is significantly higher compared to the conventional process.<sup>6</sup> Moreover, the relatively high pressure conditions of the conventional process do not match the upstream operating pressure of current commercial electrolyzers, typically operating below 100 bar.<sup>9</sup> Therefore, the PtA process can benefit significantly from a new process design, dedicated to small scale and dynamic operation at lower pressures and temperatures. A promising strategy to design processes for this application lies within process intensification, for example by shifting the thermodynamic equilibrium by the continuous removal of  $\text{NH}_3$  from the gas phase *via in situ* sorptive separation. Simulation-based evaluations of the sorption-enhanced approach pursued in our previous work indicates a significant energy saving potential up to 50% for the synthesis loop compared to conventional and other emerging technologies.<sup>7</sup> As the thermodynamic equilibrium of the sorptive  $\text{NH}_3$  removal is favored by low temperatures, sorption enhanced reactors should be operated at lowest temperature possible.<sup>10,11</sup> However, as low temperatures limit the  $\text{NH}_3$  synthesis reaction kinetically, catalysts with high activity at low temperature are necessary for this technology, which has been under investigation for many years.<sup>12,13</sup> So far, the implementation to an industrial scale was only achieved for two catalyst materials. Most commonly used are Fe-based catalysts, in form of different oxidation states, such as wüstite or magnetite, promoted by various compounds such as  $\text{K}_2\text{O}$ ,  $\text{BaO}$  or  $\text{Al}_2\text{O}_3$ . These catalysts benefit from being comparatively cheap, as no noble metals or rare elements are used, and show a high chemical and thermal stability under conventional synthesis conditions.<sup>14</sup> Drawbacks of Fe-based materials result from their high activation energies and the comparatively strong inhibition of the catalytic activity by  $\text{NH}_3$  formed along the reaction.<sup>15</sup> Accordingly, industrial processes using Fe-based catalysts need to be operated under relatively high temperatures and pressures, using a higher recycle ratio to achieve reasonable conversions and to limit the  $\text{NH}_3$  concentration in the reactor. In fact, the  $\text{NH}_3$  inhibition led to the development of a synthesis process based on a carbon-supported ruthenium (Ru) catalyst. Therefore, the catalyst was implemented in the rear section of a multistage reactor, allowing the efficient synthesis at increased  $\text{NH}_3$  concentrations in the commercialized Kellogg's process.<sup>16</sup> Ru-based catalysts benefit from a lower activation energy in comparison to Fe-based catalysts. Drawbacks are the

higher cost and lower availability of Ru, as well as the need for a thermal and chemical stable support materials.<sup>17</sup>

To design  $\text{NH}_3$  synthesis reactors the development of suitable kinetic models has been in the focus of research since the early work by Mittasch *et al.* in the beginning of the 20th century.<sup>18</sup> In their review, Nielsen *et al.*<sup>19</sup> give an overview of existing kinetic models and introduce a classification into two general approaches. While the first approach is based on the model developed by Temkin and Pyzhev,<sup>20</sup> the second class assumes a Langmuir-type adsorption according to the Langmuir–Hinshelwood approach. Yet, kinetic models available in the literature mainly focus reaction conditions typical for the conventional Haber–Bosch process, characterized by high pressures and temperatures. Consequently, this work focusses on a kinetic investigation under mild reaction conditions, needed to design small-scale PtA processes. Therefore, the commonly used Temkin–Pyzhev equation<sup>21–27</sup> is used as basis and systematically extended, in order to achieve sufficient agreement between prediction and experimental data. The model discrimination and parameterization are performed based on experiments with Ru- and Fe-based catalysts using axially resolved temperature and concentration measurements.

## Methodology

### Experimental

**Reactor setup.** Kinetic investigations were carried out in the reactor setup shown in Fig. 1. The reactor consists of a stainless-steel tube ( $d_{\text{in}} = 8$  mm) with seven axially distributed sampling positions, enabling the measurement of the axial gas phase composition along the catalyst bed. Gas sampling from the different positions was performed using an automated multi-port valve (Valco Vici), allowing to sequentially connect the

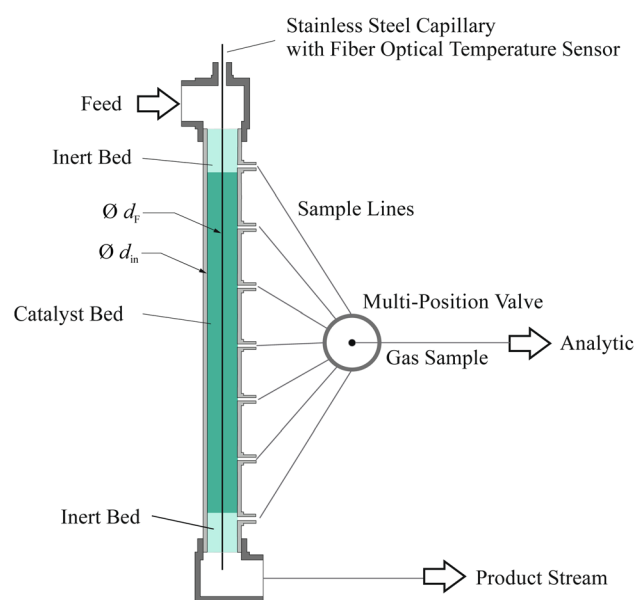


Fig. 1 Reactor concept used for the measurement of  $\text{NH}_3$  synthesis with different catalysts.



sampling positions to the downstream gas phase analytics. To achieve a continuous flow through the catalyst bed independently of the selected sampling position, the gas stream was split into the gas sample stream at the sampling position and a continuous product stream controlled by a mass flow controller (Cori-Flow, Bronkhorst). Pressure inside the reactor was adjusted using a membrane back-pressure regulator (Equilibar ZF) placed downstream of the sampling position. Further, the reactor was mounted in an electrically heated, cylindrical alumina shell with two temperature control zones, for the top and bottom of the reactor. Hot-spot formation inside the catalyst bed was reduced by dilution of the catalyst with silicon carbide (SiC) in a mass ratio of 1 g catalyst to 2.5 g of SiC. Furthermore, to identify temperature increases induced by  $\text{NH}_3$  synthesis reaction, the axial temperature profile along the catalyst bed was measured using a fiber optical temperature measurement (Luna OdiSi 6100) with a high resolution (temporal resolution: 5 Hz, spatial resolution: 2.6 mm). Measurement noise was reduced by calculation of the median of a sequence of 5 measurements, leading to a temporal resolution of one temperature profile per second. The glass fiber used as temperature sensor was contained inside a stainless-steel capillary with an external diameter of 0.8 mm and placed concentrically in the reactor tube. The system was calibrated by temperature measurements with two additional Pt-100 sensors placed at the beginning and end of the catalyst bed during a reference experiment under inert atmosphere. Based on these reference temperatures, a calibration polynomial was defined to determine the spatial temperature profile along the fiber as described elsewhere.<sup>28</sup>

**Catalyst materials.** The sample of a Ru/CeO<sub>2</sub> catalyst was provided by Fukushima Renewable Energy Institute (FREA-AIST), while the iron (Fe) based catalyst was supplied by Clariant AG. To avoid wall effects and internal mass transfer limitations, the catalysts were sieved and crushed into particle sizes ( $d_p$ ) between 250 to 500  $\mu\text{m}$ . For activation, 8.7 g Ru/CeO<sub>2</sub> catalyst were reduced for 5 h at 500 °C and ambient pressure under a flow of 2.55 mol per h H<sub>2</sub> and 0.85 mol per h N<sub>2</sub>, which corresponds to the stoichiometric H<sub>2</sub>/N<sub>2</sub> ratio of 3.9.4 g Fe catalyst were reduced under the same flow rates at 425 °C for 12 h at 80 bar. Different masses of catalysts were used, due to the difference in the bulk densities of the catalysts.

**Gas phase analytics.** The molar fraction of NH<sub>3</sub> in the product was measured using an online Fourier-transform infrared spectroscopy (FTIR) measurement device (MKS Multi-Gas 2030G). The FTIR was equipped with a gas cell with an optical pathway of 2 cm, leading to low dead volume of the analysis line, allowing for fast sampling of different operational conditions in the reactor. Gas phase measurements were carried out with a frequency of 1 Hz.

**Measurement procedure.** Temperature, pressure and feed gas composition were varied according to a full factorial experimental design in the range given in Table 1. The total catalyst amount  $m_{\text{cat,tot}}$  was homogeneously distributed along the total catalyst bed length  $L_{\text{bed,tot}}$  resulting in specific catalyst loadings in the order of 25 g m<sup>-3</sup>. The seven axially distributed sampling positions enabled the variation of the length of the

**Table 1** Experimental conditions applied for the respective catalyst defined by the total catalyst amount  $m_{\text{cat,tot}}$ , the estimated bulk density  $\rho_b$ , the catalyst bed length between inlet and sampling position  $L_{\text{bed}}(z)$ , the total inlet molar flow rate  $\dot{n}_{\text{tot,in}}$ , the catalyst particle diameter  $d_p$  and the ranges for temperature  $T$ , pressure  $p$  and feed gas composition H<sub>2</sub>/N<sub>2</sub>

Symbol	Unit	Ru/CeO <sub>2</sub>	Fe
$m_{\text{cat,tot}}$	g	8.7	9.4
$L_{\text{bed}}(z)$	m	0.06–0.35	0.05–0.36
$\dot{n}_{\text{tot,in}}$	mol h <sup>-1</sup>	2.7	2.8
$d_p$	$\mu\text{m}$	250–500	250–500
$T$	°C	350; 400; 450	350; 400; 450
$p$	bar (g)	10; 45; 80	10; 45; 80
H <sub>2</sub> /N <sub>2</sub>	mol mol <sup>-1</sup>	1.5; 2; 3	1.5; 2; 3
GHSV	h <sup>-1</sup>	12 000–38 000	12 000–38 000
$\rho_b$	kg m <sup>-3</sup>	2100	2500

catalyst bed between inlet and sampling position  $L_{\text{bed}}(z)$  at every 0.07 m while the molar flow rate at the reactor inlet,  $\dot{n}_{\text{tot,in}}$ , was kept constant over the whole experimental campaign. The variation of the catalyst bed length can also be expressed by the Gas Hourly Space Velocity (GHSV), defined by the standard volumetric flow rate of feed gases per volume of catalyst used. For each experiment, all process parameters were set to the desired value and held until steady-state was reached regarding the molar fraction of NH<sub>3</sub>. Steady-state was defined by a relative change in the measured molar fraction below 1% for a time span of at least 5 min. Once steady-state was reached, the sampling position was switched from bottom to top along the reactor axis, whereby the before mentioned criteria for steady-state was applied for each sampling position. All measured data (temperature profiles, FTIR measurements, sensor readings) were processed by a MATLAB script to a temporal resolution of 1 Hz. To improve data quality and to increase the signal-to-noise ratio, the mean values for one minute under steady-state conditions were calculated for each experimental point from data readings obtained with a frequency of 1 Hz. According to this procedure, 162 experimental points for each catalyst were measured.

**Validation of experimental conditions.** Ideal plug-flow behavior was validated by considering the guidelines provided by Dautzenberg.<sup>29</sup> Radial gradients and axial dispersion were avoided by using a high  $L_{\text{bed,tot}}/d_p$  ratio of around 700, which exceeds the recommended minimum 50. Bodenstein number (Bo) was evaluated to be 80 or higher for the most critical operating point concerning axial dispersion, meaning for the shortest catalyst bed at the first sampling position. Blind experiments with pure SiC were carried out to confirm absence of catalytic activity of the inert material or the reactor piping. The catalysts were activated and kept under steady-state conditions at 400 °C, 80 bar and a stoichiometric feed mixture, to confirm their stability for 12 h before the catalytic measurements. Deactivation of the catalyst was ruled out during the campaign duration of around 80 h for the Fe and 100 h for the Ru/CeO<sub>2</sub> catalyst, respectively. The absence of external and internal mass transfer limitations was proven by



checking the criteria by Carberry and Mears, respectively.<sup>30</sup> The calculations are provided in the ESI.†

## Modelling

**Reactor model.** A pseudo-homogeneous, one-dimensional, ideal plug-flow reactor model was implemented using MATLAB to represent the experimental conditions. The according material balance for the component  $i$  is given in eqn (2). For solving this differential equation, the inlet molar flow rates for each component are used as boundary condition.

$$\frac{d\dot{n}_i}{dz} = \frac{m_{\text{cat}}}{L_R} \nu_i r_{\text{NH}_3} \quad (2)$$

The available experimental data for the spatially resolved temperature profile was used for the model directly and the calculation of the energy balance could be omitted. As the measured pressure drop along the catalyst bed was less than 100 mbar for all experimental points, the impulse balance was neglected in the model.

**Kinetic equations.** In this work, different kinetic models from the literature are used and compared to identify the most suitable model in regard to the experimental data obtained. The commonly used Temkin approach (eqn (3)) assumes the dissociative adsorption of  $\text{N}_2$  as the rate determining step,<sup>20</sup> which was proven by the work of Ertl *et al.*<sup>31</sup> The adsorption of any other species involved in the reaction as considered negligible. Hence,  $\text{N}_2$  is assumed as the most abundant species on the catalyst surface. In contrast to a Langmuir based kinetic approach, a heterogenous surface was assumed by Temkin *et al.* leading to a change in the heat of adsorption depending on the degree of coverage. The coefficient  $\alpha$ , describing the reaction order was introduced by Temkin *et al.*<sup>20</sup> and fitted to 0.5 in their work, yet in various works values between 0.25 and 0.75 are reported.<sup>19</sup> The applied form of the Temkin equation based on the activities  $a_i$  of the reaction species is given in eqn (3).

$$r_{\text{NH}_3} = k_2 \left[ K_{\text{eq}}^2 a_{\text{N}_2} \left( \frac{a_{\text{H}_2}^3}{a_{\text{NH}_3}^2} \right)^\alpha - \left( \frac{a_{\text{NH}_3}^2}{a_{\text{H}_2}^3} \right)^{1-\alpha} \right] \quad (3)$$

Especially at lower temperatures, competitive adsorption becomes significant, which was shown by Ozaki, Taylor and Boudart<sup>32</sup> for NH species for example. Consequently, Rossetti *et al.*<sup>33</sup> proposed the kinetic approach shown in eqn (4), which was developed for Ru-based catalysts. The numerator of the equation is equal to the Temkin equation (eqn (3)), hence, still assuming the adsorption of  $\text{N}_2$  as rate-determining step. The denominator considers the adsorption of each gaseous species at the solid surface assuming the sorption step to be in equilibrium. The effect of the competitive adsorption of the different reactants is considered by a coefficient  $f_i$ .

$$r_{\text{NH}_3} = \frac{k_2 \left[ K_{\text{eq}}^2 a_{\text{N}_2} \left( \frac{a_{\text{H}_2}^3}{a_{\text{NH}_3}^2} \right)^\alpha - \left( \frac{a_{\text{NH}_3}^2}{a_{\text{H}_2}^3} \right)^{1-\alpha} \right]}{1 + K_1 a_{\text{N}_2}^{f_1} + K_2 a_{\text{H}_2}^{f_2} + K_3 a_{\text{NH}_3}^{f_3}} \quad (4)$$

The kinetic models in eqn (3) and (4) are taken from the literature,<sup>33,34</sup> while the reaction rate constant  $k_2$  and the equilibrium constants  $K_i$  were calculated according to the Arrhenius approach (eqn (5)) and the van't Hoff equation (eqn (6)).

$$k_2 = k_{2,0} \exp\left(-\frac{E_A}{RT}\right) \quad (5)$$

$$K_i = \exp\left(-\frac{\Delta H_{\text{ads},i}}{RT} + \frac{\Delta S_{\text{ads},i}}{R}\right) \quad (6)$$

The model was used to fit the pre-exponential factor  $k_{2,0}$ , the activation energy  $E_A$ , and the coefficient  $\alpha$ , as well as the parameters  $\Delta H_{\text{ads},i}$ ,  $\Delta S_{\text{ads},i}$ , and the coefficient  $f_i$ . All remaining parameters, *i.e.*, the activities  $a_i$  and the equilibrium constant  $K_{\text{eq}}$ , were calculated according to the following section.

**Thermodynamic calculations.** The equilibrium constant  $K_{\text{eq}}$  for  $\text{NH}_3$  synthesis is calculated according to eqn (7) from the Gibbs free energy,  $\Delta_R G^\circ$ , which depends on the measured axial temperature profile. Detailed calculations are given in the ESI.†

$$K_{\text{eq}}(z) = \exp\left(-\frac{\Delta_R G(T(z))}{R T(z)}\right) \quad (7)$$

The gas phase activities were calculated using the Soave–Redlich–Kwong (SRK) equation of state (EoS), as described in the ESI.† The consistency of the selected EoS with experimental data for the  $\text{NH}_3$  synthesis was checked and confirmed by Tripodi *et al.*<sup>35</sup>

**Method for the fitting of the model parameters.** The experimental data obtained in this work was used to parameterize the kinetic models according to the method described in Fig. 2. The temperature profile and the  $\text{NH}_3$  molar fraction at each sampling position were used as input for the model, while the inlet molar flow rate of each component was used as boundary

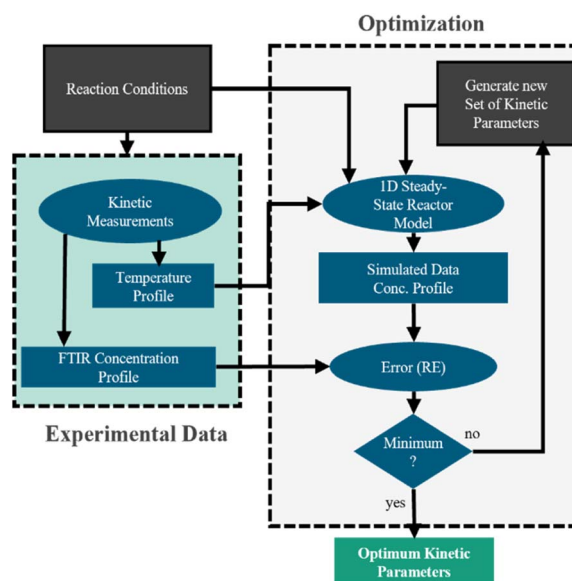


Fig. 2 Schematic illustration of the method applied for fitting of the kinetic parameters in this work.



conditions. The measured  $\text{NH}_3$  molar fraction was converted into a molar flow rate by calculating the extent of reaction for  $\text{NH}_3$  and the calculation of molar flow rates of  $\text{H}_2$  and  $\text{N}_2$  based on the stoichiometric  $\text{NH}_3$  synthesis reaction and the measured inlet flow rates, as given in the ESI.† The model is solved with a higher spatial resolution than that of the measured axial profiles. Hence, the temperature values between two axial measurement positions were interpolated linearly. Kinetic parameters were determined by minimizing the error function RE defined as the deviation between simulated and measured  $\text{NH}_3$  molar fraction at each sampling position (eqn (8)). Note that each experimental point is obtained for an individual inlet molar flow rate, operating temperature, and pressure as well as a specific catalyst mass, for which the outlet composition and the axial temperature profile was measured. The catalyst mass was varied by switching among the sampling positions distributed axially. To avoid falsification of the parameter estimation by data close to equilibrium, the deviation between data and equilibrium was used as weighing factor in eqn (8). Minimization of the error function was executed using the Nelder–Mead method implemented in MATLAB.<sup>36</sup> The quality of the model fit is discussed based on the root-mean-square error (RMSE), calculated based on the molar fraction of  $\text{NH}_3$  as given in eqn (9). Further, confidence intervals (CI) are calculated using a nonlinear model fit performed in MATLAB using the Jacobian matrix for a 95% confidence interval for the obtained parameters, as described elsewhere.<sup>37</sup> The complexity of the kinetic model was reduced from as in eqn (4) by stepwise removal of parameters, starting with those with the highest CI. The most appropriate kinetic model is chosen based on minimum RMSE after systematic elimination of parameters.

$$\text{RE} = \sum_{j=1}^N \left( \frac{(y_{m,j} - y_{s,j})}{y_{m,j}} \right)^2 \frac{(y_{\text{eq},j} - y_{m,j})}{y_{\text{eq},j}} \quad (8)$$

$$\text{RMSE} = \sqrt{\frac{\sum_{j=1}^N (y_{m,j} - y_{s,j})^2}{N}} \quad (9)$$

## Results and discussion

### Experimental results

In Fig. 3 selected experimental results for the Fe-based catalyst are shown to illustrate the axially resolved temperature profile

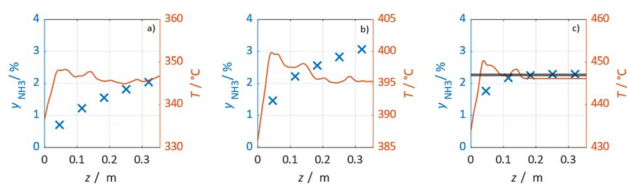


Fig. 3  $\text{NH}_3$  molar fraction measured at distinct sampling position (blue) and spatially resolved temperature profile (red) at temperature levels of 350 °C (a), 400 °C (b) and 450 °C (c). Reaction conditions:  $\text{H}_2/\text{N}_2 = 3.0$  and pressure of 80 bar using the Fe catalyst.

and the molar  $\text{NH}_3$  fraction measured at distinct axial positions. The full set of experimental results for both catalysts can be found in the ESI.† The plots indicate an increasing molar fraction of  $\text{NH}_3$  along the axial reactor coordinate. The equilibrium  $\text{NH}_3$  molar fraction (solid black line) calculated for the mean temperature in the reactor is included for the experiments carried out at maximum temperature (450 °C). Experiments at lower temperatures are clearly in the kinetic regime and rather unaffected by equilibrium constraints. The release of heat of reaction leads to hot-spot formation of up to 5 K close to the reactor inlet. Along the flow direction the temperature profile reaches constant values since the rate of formation and thus the heat release diminishes. In Fig. 4 the measured molar fraction and the specific molar flow rate of  $\text{NH}_3$  for both catalysts are displayed as function of the measured temperature. The temperature is represented by the average value of the measured temperature profile along the catalyst bed. The molar fraction and flow rate of  $\text{NH}_3$  are determined at the second sampling position (the first sampling position corresponds to the reactor inlet), in order to display data in the kinetic regime with minor effects of equilibrium constraints. The measured data with respect to temperature profiles and  $\text{NH}_3$  molar fraction along the reactor length are tabulated in the ESI.† For both catalysts the  $\text{NH}_3$  formation rate rises with rising temperature and pressure, as expected. At temperatures above 400 °C the increase of  $\text{NH}_3$  formation rate with temperature is less pronounced especially at lower pressures. This can be explained by more pronounced equilibrium constraints, as shown for the  $\text{NH}_3$  molar fraction (Fig. 4, right).

The Ru/CeO<sub>2</sub> catalyst shows a lower rate of formation under all applied reaction conditions in comparison to the Fe-based catalyst. The lower activity of the Ru/CeO<sub>2</sub> catalyst could be explained by the inhibition by  $\text{H}_2$  adsorption, as discussed in recent publications.<sup>38–40</sup> The potential inhibiting effect of  $\text{H}_2$  was investigated by variation of the  $\text{H}_2/\text{N}_2$  ratio in the gas mixture for both, Fe and Ru/CeO<sub>2</sub> catalyst, as depicted in Fig. 5. To compare the influence of  $\text{H}_2/\text{N}_2$  ratio on both catalysts, the relative  $\text{NH}_3$  formation rate  $\psi$  is calculated according to eqn (10). For the calculation of  $\psi$ , the specific molar flow rate of  $\text{NH}_3$

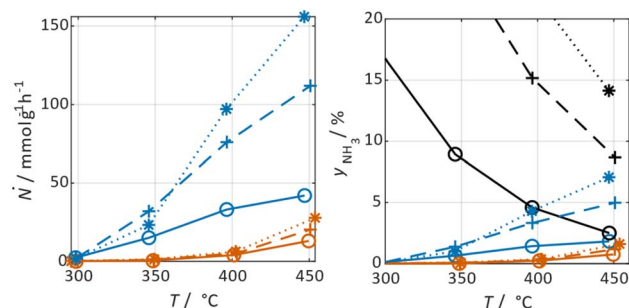


Fig. 4 Effect of temperature on the specific molar flow rate of  $\text{NH}_3$  per mass catalyst at reactor outlet  $\dot{N}_{\text{NH}_3, \text{out}}$  (left) and the measured molar fraction of  $\text{NH}_3$  (right) in comparison with the thermodynamic equilibrium (black) for the Fe (blue) and Ru/CeO<sub>2</sub> catalyst (orange) at pressures of 10 bar (o), 45 bar (+) and 80 bar (\*) at a  $\text{H}_2/\text{N}_2$  ratio of 3.0 using the minimum catalyst bed length  $L_{\text{bed}}(z)$ .



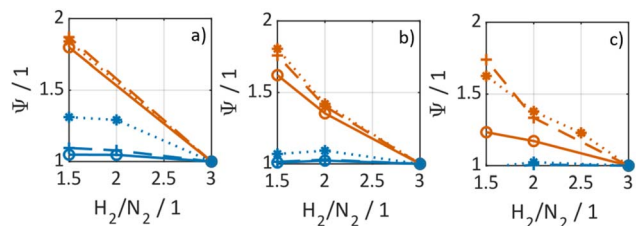


Fig. 5 Comparison of relative rate of  $\text{NH}_3$  formation  $\psi$  as function of  $\text{H}_2/\text{N}_2$  ratio for Fe (blue) and  $\text{Ru}/\text{CeO}_2$  (orange) catalyst at 350 °C (a), 400 °C (b) and 450 °C (c) and for pressures of 10 bar (o), 45 bar (+) and 80 bar (\*) using the minimum catalyst bed length  $L_{\text{bed}}(z)$  for both catalysts.

determined for a certain  $\text{H}_2/\text{N}_2$  ratio  $j$  is divided by the value determined for a stoichiometric  $\text{H}_2/\text{N}_2$  mixture under equal reaction conditions.

$$\psi_j = \frac{\dot{N}_{\text{NH}_3, \text{out}}(\text{H}_2/\text{N}_2 = j)}{\dot{N}_{\text{NH}_3, \text{out}}(\text{H}_2/\text{N}_2 = 3)} \quad (10)$$

Fig. 5 indicates that the  $\text{Ru}/\text{CeO}_2$  catalyst was more sensitive towards the  $\text{H}_2/\text{N}_2$  ratio compared to the Fe catalyst. For instance, at 400 °C the reduction of the  $\text{H}_2/\text{N}_2$  ratio from 3.0 to 1.5 leads to an increase in  $\text{NH}_3$  formation rate by more than 80% for the  $\text{Ru}/\text{CeO}_2$  catalyst. Hereby, the sensitivity towards the  $\text{H}_2/\text{N}_2$  ratio is independent of temperature. In contrast, a sensitivity of the Fe-based catalysts towards the  $\text{N}_2/\text{H}_2$  ratio is only observed at the lowest temperature and highest pressure.

### Kinetic modeling

The kinetic model obtained in this work for the Fe catalyst was defined by the systematic simplification of eqn (4) towards the expression given in eqn (11). The highlighted parameters  $k_2$ ,  $K_3$  and  $f_3$  represent those determined by the parameter fitting according to the method illustrated in Fig. 2. Hence, the kinetic expression found in the present work (eqn (11)) extends the conventional Temkin (eqn (3)) by the adsorption constant  $K_3$ , which underlines the relevance of the observed inhibition by  $\text{NH}_3$ . Simultaneously, adsorption of  $\text{H}_2$  was found non-significant, which agrees with the observed low sensitivity towards  $\text{H}_2/\text{N}_2$  ratio for this catalyst. Table 2 lists the kinetic parameters estimated for eqn (11). The activation energy of 144  $\text{kJ mol}^{-1}$  is close to the range of 150 to 170  $\text{kJ mol}^{-1}$  reported by Liu for different Fe based catalysts.<sup>41</sup>

$$r_{\text{NH}_3} = \frac{k_2 \left( a_{\text{N}_2}^{0.5} K_{\text{eq}} \left( \frac{a_{\text{H}_2}^{1.5}}{a_{\text{NH}_3}} \right)^\alpha - \left( \frac{a_{\text{NH}_3}}{a_{\text{H}_2}^{1.5}} \right)^{1-\alpha} \right)}{1 + K_3 a_{\text{NH}_3} f_3} \quad (11)$$

The validity of the simplification of the model is shown by comparison of RMSE values for the different model complexities, given in Table 4. It becomes apparent, that the extended Temkin model (eqn (11)) provides the smallest RMSE, even though the number of parameters is still low. Hence, we

Table 2 Estimated kinetic model parameters for the extended Temkin eqn (11) with their respective confidence intervals for the Fe catalyst

Parameter	Unit	Value	CI (95%)
$k_{2,0}$	$\text{mol s}^{-1} \text{kg}^{-1}$	$3.35 \times 10^9$	$\pm 10.4$
$E_A$	$\text{J mol}^{-1}$	$1.44 \times 10^5$	$\pm 2.2$
$\Delta S_{3, \text{Ads}}$	$\text{J mol}^{-1} \text{K}^{-1}$	-24.4	$\pm 1.2$
$\Delta H_{3, \text{Ads}}$	$\text{J mol}^{-1}$	$-1.56 \times 10^4$	$\pm 4.4$
$f_3$	1	0.261	$\pm 11$
$\alpha$	1	0.5	—

propose this model as the optimal one. Extending the model from the conventional (eqn (3)) to the extended Temkin expression (eqn (11)) reduces the RMSE from 0.68% down to 0.43%, by introducing three additional parameters. Consideration of further parameters in the kinetic model does not lead to any improvement in RMSE.

The determined kinetic expression for the  $\text{Ru}/\text{CeO}_2$  catalyst is given in eqn (12), where the highlighted parameters  $k_2$ ,  $K_2$ ,  $f_2$ ,  $K_3$  and  $f_3$  are fitted to the experimental data and summarized in Table 3.

$$r_{\text{NH}_3} = \frac{k_2 \left( a_{\text{N}_2}^{0.5} K_{\text{eq}} \left( \frac{a_{\text{H}_2}^{1.5}}{a_{\text{NH}_3}} \right)^\alpha - \left( \frac{a_{\text{NH}_3}}{a_{\text{H}_2}^{1.5}} \right)^{1-\alpha} \right)}{1 + K_2 a_{\text{H}_2}^{1.5} f_2 + K_3 a_{\text{NH}_3} f_3} \quad (12)$$

This extended Temkin equation is characterized by consideration of  $\text{H}_2$  and  $\text{NH}_3$  adsorption, which is neglected in the conventional Temkin approach. Especially the relevance of  $\text{H}_2$  adsorption aligns with the observed experimental behavior and with the work of Rossetti *et al.*<sup>33</sup> However, the values for  $\Delta H_{\text{Ads}}$  and  $\Delta S_{\text{Ads}}$  of  $\text{NH}_3$  and  $\text{H}_2$  obtained in this work are significantly higher compared to,<sup>33</sup> resulting in a stronger inhibition of the  $\text{Ru}/\text{CeO}_2$  catalyst. The activation energy of 106  $\text{kJ mol}^{-1}$  agrees well with the value of 96  $\text{kJ mol}^{-1}$  for  $\text{Ru}/\text{C}$  catalysts reported by Rossetti *et al.*<sup>33</sup>

For the  $\text{Ru}/\text{CeO}_2$  catalyst the influence of model simplification is shown in Table 4 based on the RMSE. It can be seen that RMSE differs marginally between the fully complex (eqn (4)) and the extended Temkin model (eqn (12)), while the number of parameters is smaller for the latter. Hence, we propose eqn (12) as optimal kinetic model.

Table 3 Fitted kinetic model parameters for the extended Temkin eqn (12) with their respective confidence intervals for the  $\text{Ru}/\text{CeO}_2$  catalyst

Parameter	Unit	Value	CI (95%)
$k_{2,0}$	$\text{mol s}^{-1} \text{kg}$	$3.49 \times 10^8$	$\pm 15.7$
$E_A$	$\text{J mol}^{-1}$	$1.06 \times 10^5$	$\pm 2$
$\Delta S_{2, \text{Ads}}$	$\text{J K}^{-1} \text{mol}^{-1}$	-80.1	$\pm 0.16$
$\Delta H_{2, \text{Ads}}$	$\text{J mol}^{-1}$	$-8.71 \times 10^4$	$\pm 0.24$
$f_2$	1	0.116	$\pm 4.8$
$\Delta S_{3, \text{Ads}}$	$\text{J K}^{-1} \text{mol}^{-1}$	-143	$\pm 4.5$
$\Delta H_{3, \text{Ads}}$	$\text{J mol}^{-1}$	$-1.184 \times 10^4$	$\pm 2.9$
$f_3$	1	0.414	$\pm 2.6$
$\alpha$	1	0.25	—



**Table 4** Comparison of calculated RMSE for the Fe and Ru/CeO<sub>2</sub> catalyst, for the conventional Temkin equation as well as for the extended Temkin equation of this work

	Number of parameters	RMSE for Fe	RMSE for Ru/CeO <sub>2</sub>
Conventional Temkin eqn (3)	2	0.68%	0.72%
Extended Temkin eqn (11)	5	0.43%	0.81%
Extended Temkin eqn (12)	8	0.53%	0.54%
Full complexity Temkin eqn (4)	11	0.45%	0.52%

The parity plots shown in Fig. 6 compare the measured and simulated molar fractions of NH<sub>3</sub> in form of distance from equilibrium according to relative errors defined in eqn (13) and (14). For simulation the above recommended kinetic model is used for both the Fe and the Ru/CeO<sub>2</sub> catalyst. For the Fe catalyst, the relative error is within the  $\pm 10\%$  range, while it increases in proximity to the equilibrium as observed at small  $\Delta y_{\text{NH}_3}$ . However, the RMSE remains at a satisfactory value below 0.5% as shown in Table 4 for eqn (11).

For Ru/CeO<sub>2</sub> the deviation between experimental data and simulation is below  $\pm 10\%$  for a stoichiometric ratio of 3 and sufficient distance from equilibrium. Increasing deviations can be observed for reaction conditions approaching the equilibrium and for low H<sub>2</sub>/N<sub>2</sub> ratios, while the overall RMSE for the proposed eqn (12) is satisfactory with a value of 0.53% (see Table 4). The deviations in relative error at low H<sub>2</sub>/N<sub>2</sub> ratios indicate possible mechanism changes in the reaction at high H<sub>2</sub> molar fractions, which need further investigations. However, low H<sub>2</sub>/N<sub>2</sub> ratios are of less relevance for technical applications. Hence, the proposed kinetic expression is suitable for application in reactor design. Further parity plots for the other kinetic model complexities can be found in the ESI.†

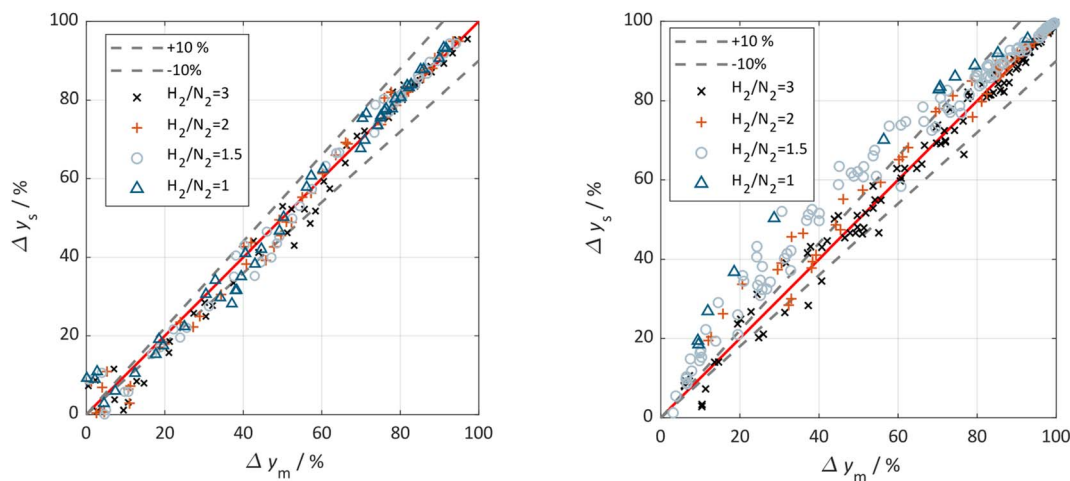
$$\Delta y_s = \frac{y_{\text{eq}} - y_s}{y_{\text{eq}}} \quad (13)$$

$$\Delta y_m = \frac{y_{\text{eq}} - y_m}{y_{\text{eq}}} \quad (14)$$

### Visualization of simulated and measured results

The simulated and measured molar fraction of NH<sub>3</sub> at distinct sampling positions along the flow direction are compared in Fig. 7 for the Ru/CeO<sub>2</sub> catalyst (columns (a) to (c) and rows (1) to (3)) and the Fe catalyst (columns (d) to (f) and rows (4) to (6)), respectively. The calculated reaction equilibrium is added, but only plotted in the visible range at 450 °C. Furthermore, the measured temperature profile is provided. Additional results are provided in the ESI.† For both catalysts, the NH<sub>3</sub> molar fraction is increasing in axial direction asymptotically towards the thermodynamic limit at a temperature of 450 °C. Comparing the influence of pressure and temperature for both catalysts, the lower rate of formation observed for the Ru/CeO<sub>2</sub> is visible, as it leads to lower gradients in the molar fraction and accordingly to lower heat release and less pronounced formation of a temperature hot spot. For both catalysts, the good agreement between the measured and modelled molar fractions is observed, especially in the kinetic regime.

However, more significant deviations between experimental and simulated results were observed towards the reactor outlet, where the approach towards the chemical equilibrium determines the molar fraction of NH<sub>3</sub>. Thus, the kinetic regime dominates for samples taken close to the reactor inlet, while equilibrium constraints become more pronounced towards the reactor outlet. Consequently, the parameter estimation relies largely on results where superimposed equilibrium effects can be neglected. This was achieved by the weighing of model deviations as introduced in eqn (8).



**Fig. 6** Parity plot for the extended Temkin model (eqn (11)) applied to the Fe catalyst (left) and (eqn (12)) applied to the Ru/CeO<sub>2</sub> catalyst (right). All experimental points are included and classified by the used H<sub>2</sub>/N<sub>2</sub> ratio (3 (x), 2 (+), 1.5 (o), 1 (Δ)), 0% deviation line (red) and the  $\pm 10\%$  deviation lines (black) are given.





Fig. 7 Measured (markers), predicted (solid blue) and equilibrium (solid black) NH<sub>3</sub> molar fraction (primary axis) as well as temperature (orange, secondary axis) as function of the axial position  $z$  for the Ru/CeO<sub>2</sub> (top) and the Fe catalyst (bottom) at reaction pressure of 10 bar (row 1 and 4), 45 bar (row 2 and 5) and 80 bar (row 3 and 6) and temperatures of 350 °C (column (a and d)), 400 °C (column (b and e)) and 450 °C (column (c and f)) at a H<sub>2</sub>/N<sub>2</sub> ratio of 3.





## Conclusions

The kinetic models for a Fe and a Ru/CeO<sub>2</sub> catalyst were developed for reaction conditions in the range of 350 to 450 °C and 10 to 80 bar within this work. Therefore, kinetic experiments are performed to obtain spatially resolved profiles of NH<sub>3</sub> concentration and temperature. The temperature profile was measured with a spatial resolution of 2.6 mm, while the axially distributed sampling positions with spacings of 7 cm were used to measure the gas phase composition at constant inlet flow rates. The variation of the H<sub>2</sub>/N<sub>2</sub> feed gas ratio from 1 to 3 enabled the investigation of the influence of the H<sub>2</sub> partial pressure on the reaction kinetics. For the Ru/CeO<sub>2</sub> catalyst a significant inhibition of the catalyst by H<sub>2</sub> was observed, especially at low temperatures. In contrast, a significant influence of the H<sub>2</sub>/N<sub>2</sub> feed gas ratio on the reaction kinetics was absent for the Fe catalyst. Furthermore, a higher reaction rate is observed for the Fe compared to the Ru/CeO<sub>2</sub> catalyst. The measurement of the axial temperature profiles and concentration profiles provides a broad data basis and considers the observed, non-isothermal behavior for parameterization of the models.

The experimental data were used for discrimination and parameterization of kinetic models based on systematic extension of the frequently used Temkin approach. For the Fe catalyst adsorption of NH<sub>3</sub> is found to affect the kinetics significantly, while H<sub>2</sub> and NH<sub>3</sub> appear to be relevant for the Ru/CeO<sub>2</sub> catalyst. Accordingly, respective sorption terms are considered in the kinetic expressions of both catalysts. For both catalysts it is shown, that the selected kinetic models provide sufficient agreement between experiment and prediction under mild reaction conditions and that further model complexity is not inevitably necessary. Hence, the developed kinetic models provide a foundation for advanced reactor design under the PtA-specific process conditions such as lower pressures and milder temperatures. Future work will focus on the application of these models to investigate new reactor and process designs, as *e.g.* sorption-enhance NH<sub>3</sub> synthesis.<sup>7</sup>

## Abbreviations

### Latin symbols

$a_i$	Activity of component $i$ (1)
$A_R$	Cross sectional area of the reactor tube (m <sup>2</sup> )
CI	Relative confidence interval (%)
$d_F$	Outer diameter of fiber optical temperature sensor (mm)
$d_{in}$	Inner reactor diameter (mm)
$d_p$	Particle diameter (μm)
$E_A$	Activation energy (J mol <sup>-1</sup> )
$f_j$	Kinetic coefficient for adsorption equilibrium $j$ (1)
$\Delta_R G^\circ$	Standard Gibbs free energy of reaction (J mol <sup>-1</sup> )
$\Delta_{Ads} H_i$	Specific enthalpy of adsorption of component $i$ (J mol <sup>-1</sup> )
$\Delta H_f^\circ$	Enthalpy of formation under standard condition (kJ mol <sup>-1</sup> )

$K_{eq}$	Equilibrium constant of NH <sub>3</sub> synthesis (1)
$k_i$	Reaction rate constant (var.)
$K_i$	Adsorption constant of component (1)
$k_{i,0}$	Pre-exponential factor (var.)
$L_{bed,tot}$	Total length of catalyst bed (m)
$L_{bed}(z)$	Reactor length at sampling position (m)
$m_{cat}$	Catalyst mass (g)
$\dot{n}_{i,in}$	Molar flow of component $i$ at reactor inlet (mol h <sup>-1</sup> )
$\dot{n}_{tot,in}$	Total molar flow at reactor outlet (mol h <sup>-1</sup> )
$\dot{n}_{i,out}$	Molar flow of component $i$ at reactor outlet (mol h <sup>-1</sup> )
$\dot{N}_{NH_3,out}$	Specific molar flow rate of NH <sub>3</sub> per mass catalyst at reactor outlet (mmol g <sup>-1</sup> h <sup>-1</sup> )
$N$	Number of experimental points for each catalyst
$p$	Pressure (bar (gauge))
$r_{NH_3}$	Rate of formation of NH <sub>3</sub> (mol s <sup>-1</sup> kg <sub>cat</sub> <sup>-1</sup> )
$R$	Ideal gas constant (J mol <sup>-1</sup> K <sup>-1</sup> )
RE	Relative error function (1)
RMSE	Root-mean-square-error (1)
$\Delta_{Ads} S_i$	Specific entropy of adsorption of component $i$ (J K <sup>-1</sup> mol <sup>-1</sup> )
$T$	Temperature (°C)
$T(z)$	Measured temperature at reactor length $z$ (°C)
$y_{eq}$	Molar fraction of NH <sub>3</sub> in equilibrium (1)
$y_m$	Measured molar fraction of NH <sub>3</sub> in the gas phase (1)
$y_s$	Simulated molar fraction of NH <sub>3</sub> in the gas phase (1)
$z$	Axial coordinate in the reactor (m)

### Greek symbols

$\alpha$	Kinetic coefficient of Temkin equation (1)
$\nu_i$	Stoichiometric coefficient of component $i$ in ammonia synthesis (1)
$\varphi_i$	Fugacity coefficient of component $i$ (1)
$\psi_j$	Relative rate of formation at H <sub>2</sub> /N <sub>2</sub> ratio $j$ (1)
$\rho_b$	Estimated bulk density of catalyst

## Conflicts of interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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