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# Meta-stability through intermolecular interactions protecting the identity of atomic metal clusters: *ab initio* evidences in $(\text{Cu}_5\text{--Cu}_5)_n$ ( $n < 3$ ) cases†

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Recent developments in new synthesis techniques have allowed the production of precise monodisperse metal clusters composed of a few atoms. These atomic metal clusters (AMCs) often feature a molecule-like electronic structure, which makes their physical and chemical properties particularly interesting in nanotechnology. Regarding potential applications, there is a major concern about the sintering of AMCs in nanoparticles due to the loss of their special properties. In this work, multireference *ab initio* theory is applied to demonstrate the formation of coupled AMC–AMC clusters in which the AMC partners maintain their ‘identity’ to a large extent in terms of their initial structures and atomic Mulliken charges, and their further oligomerization.

## 1 Introduction

Recent developments of highly selective experimental techniques enabling the synthesis of subnanometer metal clusters are pushing the understanding of these, more “molecular” than “metallic”, systems far beyond the present knowledge in materials science. In this way, when the atomic metal cluster (AMC) size is reduced to a small (less than 10) number of atoms, high stability and novel properties are achieved, that allow the AMC integration into materials. Additionally, interaction with the environment has the potential to boost the performance in applications particularly interesting in nanotechnology, including luminescence, sensing, bioimaging, theranostics, energy conversion, catalysis, and photocatalysis (see, *e.g.*, ref. 1 and 2 for recent reviews). From a more fundamental point of view, it has also been shown how modification of popular materials such as  $\text{TiO}_2$  with

AMCs can convert them into “reporters” of fundamental surface polaron properties.<sup>3–5</sup> From the microscopic point of view, the above behaviour is explained in terms of the d-band of the metal splitting into a subnanometric network of discrete molecule-like d orbitals, with fluxional inter-connections having the length of a chemical bond (1–2 Å). The spatial structures of these molecular orbitals make all the metal atoms cooperatively active and accessible and confer molecular characteristics to the complexes, that are responsible of their stability and properties.

Among the different AMCs, copper clusters have attracted much attention as catalysts<sup>6</sup> since they have shown important catalytic properties *e.g.* for the oxidation of  $\text{CO}$ ,<sup>7,8</sup> the selective hydrogenation of olefin and carbonyl groups,<sup>9,10</sup> and in C–X (being X = C, N, S, P) bond forming reactions.<sup>11</sup> The oxidative dehydrogenation of cyclohexene on atomically precise subnanometer bimetallic Cu–Pd (tetramer) clusters is also worth mentioning.<sup>12</sup> Moreover, the work in ref. 13 showed an outstanding chemical and thermodynamical stability of atomic copper clusters in solution over the whole pH range. First-principles modelling, including methods beyond the state-of-the-art and an interplay with cutting-edge experiments, is helping to understand the special properties of AMCs at the most fundamental molecular level. Thus, the use of first-principles methods has disclosed the fundamental reasons why  $\text{Cu}_5$  clusters experience a reversible oxidation,<sup>14</sup> and are capable of increasing and extending into the visible region the solar absorption of  $\text{TiO}_2$ ,<sup>15</sup> also considering the decomposition and photo-activation of  $\text{CO}_2$  as a prototypical (photo-)catalytic reaction.<sup>16</sup>

In spite of their potential applications, there is a major concern about the sintering of AMCs in metallic nanoparticles with the consequent loss of their special properties. In order to analyze the possible existence of metastable states in which  $\text{Cu}_5$  preserves its identity, multireference Rayleigh Schrödinger (second-order) perturbation theory<sup>17</sup> (RS2C) is applied here, allowing evidence of the formation and further oligomerization of coupled  $\text{Cu}_5\text{--Cu}_5$  clusters at a high level of *ab initio* theory. It should be stressed that in our work preservation of identity at a

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† Electronic supplementary information (ESI) available: Cartesian coordinates of optimized structures appearing in Fig. 1, complex 1 structure and charges, Cu–Cu distance Table. See DOI: <https://doi.org/10.1039/d2cp03537e>



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**Fig. 2** Top panels: scans of the interaction energy of two Cu<sub>5</sub> clusters as a function of the Z distance in vacuum. The geometries of the Cu<sub>5</sub> clusters have been kept fixed in the calculations. Top left panel: bipyramidal 3D structures. Top right panel: planar 2D structures. Bottom panel: interaction of two Cu<sub>5</sub>-Cu<sub>5</sub> coupled clusters as a function of the Z distance, with the Cu<sub>5</sub>-Cu<sub>5</sub> geometries fixed to those corresponding to the minimum in the top left panel. All calculations have been carried out with the cc-pVTZ-PP basis set.

**Table 2** Interaction energies (in eV) of coupled Cu<sub>5</sub>-Cu<sub>5</sub> clusters at DF-CASSCF/cc-pVTZ-PP and RS2C/cc-pVTZ-PP energy levels (see Appendix for computational details). Within parentheses, we indicate the nature of the stationary point: Min denotes minimum and TS denoted a transition state

Cu <sub>5</sub> -Cu <sub>5</sub>	DF-CAS(10,10)/RS2C	DF-CAS(12,12)/RS2C
1 (Min)	-1.5/-5.2	-1.6/-5.2
2 (Min)	-1.5/-5.0	-1.7/-5.0
3 (Min)	-1.8/-2.3	-1.7/-2.3
4 (Min)	-1.4/-3.3	-2.3/-2.8
5 (TS)	-1.3/-4.7	-1.5/-4.7

ref. 18 for Cu<sub>10</sub>. The inclusion of dynamical correlation is clearly responsible for such behaviour. In fact, without considering it, the interaction energies are up to 0.7 eV more attractive upon the coupling of planar 2D structures than in the case of coupled 3D geometries.

We performed a Mulliken charge analysis of natural orbitals for both isolated Cu<sub>5</sub> and coupled Cu<sub>5</sub>-Cu<sub>5</sub> clusters using the geometries optimized at the DF-CASSCF level (see Table 3). Note that Mulliken charges are larger in the 3D Cu<sub>5</sub> structure than in the 2D Cu<sub>5</sub> structure. As a result, the electrostatic contribution to the Cu<sub>5</sub>-Cu<sub>5</sub> intermolecular interaction is favored when 3D Cu<sub>5</sub> clusters become coupled to each other. Most importantly, the values of Mulliken charges on all Cu atoms are (within numerical accuracy) the same for the two Cu<sub>5</sub>

**Table 3** Mulliken charges on the atoms of Cu<sub>5</sub> and coupled Cu<sub>5</sub>-Cu<sub>5</sub> clusters for the most stable structures optimized at the DF-CASSCF/cc-pVTZ-PP level of theory. No symmetry has been imposed in the calculations. CCSD/Def2-TZVPP results are reported within parentheses for the sake of comparison

Individual Cu <sub>5</sub> clusters				
Label	2D (Min)	3D (Min)		
1	-0.02	-0.07 (-0.06)		
2	-0.03	-0.07 (-0.06)		
3	0.01	0.10 (0.10)		
4	0.01	0.10 (0.10)		
5	0.03	-0.07 (-0.06)		
Coupled Cu <sub>5</sub> -Cu <sub>5</sub> clusters				
Label	1 (Min)	2 (Min)	3 (Min)	4 (Min)
1	-0.11	-0.14	0.15	-0.04
2	-0.11	0.10	-0.21	-0.06
3	-0.10	0.04	0.15	-0.01
4	0.16	-0.28	-0.05	0.01
5	0.16	0.28	-0.04	0.09
6	0.16	-0.27	-0.04	0.02
7	0.16	0.03	-0.05	0.01
8	-0.10	0.09	0.15	0.02
9	-0.11	0.29	0.15	0.01
10	-0.11	-0.14	-0.21	-0.06

clusters within Cu<sub>5</sub>-Cu<sub>5</sub> in clusters 1 and 3, leading to a symmetric structure of the complex with respect to the two



Cu<sub>5</sub> units. It is remarkable that, in spite of being strongly bound (interaction Cu<sub>5</sub>–Cu<sub>5</sub> energies of –5.2 eV using the RS2C method on geometries optimized at the DF-CASSCF level), the two Cu<sub>5</sub> clusters maintain their spatial arrangements in a symmetric way. Moreover, although the charge distributions in the coupled structures are not identical to those in isolated clusters, their modification is relatively modest on DF-CASSCF-based optimized structures. For the 3D structure of isolated Cu<sub>5</sub>, atomic Mulliken charges vary in between –0.07 and 0.10 a.u., while in the lowest-energy Cu<sub>5</sub>–Cu<sub>5</sub> structure found in this study, they range from –0.11 to 0.16 a.u. These modifications can be understood on the basis of polarization effects causing a higher electron localization on the peripheral, lower coordinated Cu atoms. The preservation of 3D and 2D Cu<sub>5</sub> structures in some of the coupled Cu<sub>5</sub>–Cu<sub>5</sub> clusters is also clear in Fig. 1, being more evident in the case of the 2D geometries (see also Fig. S1 in the ESI†). Altogether, these outcomes indicate the protection of the identity of the Cu<sub>5</sub> partners, yet in a way differing significantly from that characterizing weakly bound van der Waals aggregates. Thus, recently, it has been shown that, upon heating, the Cu<sub>5</sub> sub-units of coupled Cu<sub>5</sub>–Cu<sub>5</sub> structures experience a decoupling through fluxional rotational motion but none spatial separation,<sup>21</sup> in contrast to the case of vdW aggregates. Additionally, upon exposition to environmental O<sub>2</sub> molecules, a high oxygen gas pressure is necessary to achieve the individualization of Cu<sub>5</sub> sub-units.<sup>21</sup>

It is interesting to note that the energy difference between structures 1 and 2 in Fig. 1 is just 0.2 eV (see Table 2). Hence, the interconversion between them can be expected to be reversible. Although the potential energy landscape of Cu<sub>5</sub>–Cu<sub>5</sub> clusters has been carefully explored (see Appendix), many local minima with similar energies could co-exist with those found in this work. The existence of many meta-stable states bearing very close energies is a typical feature characterizing atomic metal clusters due to their fluxional nature and associated wide amplitude inter-atomic motions. The concept of structural fluxionality has recently been advocated to explain the catalytic activity of AMCs (see, *e.g.*, ref. 1, 16, 22 and 23). The occurrence of fluxional dynamics has also been suggested from recent spectroscopic observations.<sup>24</sup> Recent *ab initio* molecular dynamics simulations have also shown the fluxional rotational motion between the two Cu<sub>5</sub> units of the coupled Cu<sub>5</sub>–Cu<sub>5</sub> clusters upon heating.<sup>21</sup>

Finally, to get some insight into the interaction between two coupled Cu<sub>5</sub>–Cu<sub>5</sub> clusters, we evaluated the interaction energy as a function of their relative distance (see the bottom panel in Fig. 2). As expected from the closed-shell nature of the coupled clusters, the attractive interaction is extremely weak when the dynamical correlation is not accounted for. In contrast, the two coupled clusters become strongly bound (by *ca.* 2 eV) when the latter is included through the multireference RS2C perturbation method. Thus, the formation of covalent bonds between the clusters is clearly apparent in the minimum (see inset in the bottom panel of Fig. 2). The electrostatic contribution is expected to be responsible for the strong interaction between Cu<sub>5</sub> clusters, ultimately giving rise to their oligomerization.

It can be expected that more stable structures might exist, even implying the sintering in a Cu<sub>20</sub> structure in which the Cu<sub>5</sub> clusters have lost their identity. However, it should be stressed that the existence of many metastable states of fluxional, but strongly bound, oligomers might quench such structural rearrangements at experimentally relevant ranges of temperature. In this sense, it is worth pointing out that the individualization of Cu<sub>5</sub> clusters at certain conditions of oxygen pressure and temperature has been recently suggested, particularly in an O<sub>2</sub>-rich environment.<sup>21</sup>

### 3 Conclusions

In the quest for a fundamental level understanding of the outstanding stability experimentally probed for AMCs such as Cu<sub>5</sub>,<sup>13</sup> we have explored the possibility that AMCs couple to each other in such a way that their initial structures are preserved and, although their initial charge distributions experience modifications due to polarization effects, initial charge patterns can yet be recognized in the combined clusters. This concept of ‘identity’ thus goes beyond the classical concept of preservation of identity through the formation of vdW aggregates. In this work, we have found clear *ab initio* evidences on the favored coupled cluster formation and oligomerization of Cu<sub>5</sub> clusters in such a way that the Cu<sub>5</sub> units to a large extent keep their identity in terms of their structures. This outcome is reflected in the geometrical arrangements and in the Mulliken charge analyses of the resulting electronic structures. Additionally, the existence of metastable states of coupled Cu<sub>5</sub> clusters bearing very close energies has been found and can be interpreted as a consequence of the cluster fluxional nature. Our results could be valuable in the interpretation of experimental spectroscopic measurements of the (photo-)catalytic activities of atomic metal clusters, calling for high-resolution scanning electron microscopic probes on the formation of coupled clusters and their further oligomerization. From a theoretical perspective, additional work is necessary to analyze the concept of oligomerization of AMCs, including, *e.g.*, molecular dynamics simulations on surface-supported AMCs as a function of temperature and even stronger tests using different methods at high level *ab initio* theory, including some that allow an analysis of interaction energy contributions.

### Author contributions

Both co-authors have contributed equally to the manuscript in all the required steps (investigation, writing and editing). All authors have read and agreed to the published version of the manuscript.

### Conflicts of interest

There are no conflicts to declare.





## Appendix

### Computational methods and additional details

Density fitting single-state multi-configurational self-consistent-field (DF-CASSCF) calculations have been carried out, as implemented in the last version of the MOLPRO code.<sup>25</sup> We used the polarized correlation-consistent triple- $\zeta$  cc-pVTZ-PP basis set for copper atoms,<sup>26</sup> including a small (10-valence-electron) relativistic pseudopotential. The DF-CASSCF approach is employed to account for the most important non-dynamical correlation effects. Then, the internally contracted multireference Rayleigh Schrödinger (second-order) perturbation theory RS2C method<sup>17</sup> has been applied to cover dynamical correlation effects. The RS2C method is basically a modified version of CASPT2 (complete active space with second-order perturbation theory) developed by Celani and Werner,<sup>17</sup> using CASSCF wave functions as a reference in the RS2C calculations. For complex 1 of the coupled Cu<sub>5</sub>–Cu<sub>5</sub> clusters, the CASSCF wave functions comprise up to 226 512 configuration state functions (CFSSs). The subsequent RS2C wave function consists of  $700 \times 10^6$  contracted CSFs. The RS2C method thus allows the use of reference wave functions with large active spaces and internally contracted configurations are used as a basis. For density fitting, the associated MP2FIT and JKFIT bases have been used in DF-CASSCF calculations. The diagonalization of the first-order reduced density matrix obtained from the wave function in DF-CASSCF calculations allowed us to obtain natural orbitals. An analysis of the Mulliken charges<sup>27</sup> was accomplished for both Cu<sub>5</sub> and Cu<sub>5</sub>–Cu<sub>5</sub> clusters. Additionally, for the sake of comparison, Coupled Cluster Singles and Doubles (CCSD) calculations have been carried out as implemented in the GAUSSIAN 09 code.<sup>28</sup>

Initial optimizations of the coupled Cu<sub>5</sub>–Cu<sub>5</sub> cluster geometries were performed at PBE and B3LYP levels,<sup>29,30</sup> using D4 Grimme's parameterization<sup>31</sup> to account for the dispersion correction. An excellent performance has been achieved with the predecessor PBE-D3(BJ) ansatz<sup>32</sup> in describing both supported and unsupported subnanometer silver<sup>3,33</sup> and copper<sup>16,34</sup> clusters. We used the atom-centered Def2-SVP<sup>35</sup> basis set for copper atoms. All dispersion-corrected DFT-based calculations have been performed with the ORCA suite of programs (version 5.0.1).<sup>36–38</sup>

We started our coupled Cu<sub>5</sub>–Cu<sub>5</sub> cluster calculations with a bipyramidal arrangement for the Cu<sub>5</sub> sub-unit. In this way, we placed together two trigonal bipyramidal arrangements with the center of mass of one of them located in the origin of the coordinate system and the corresponding main symmetry axis along the Z axis. The position of the second Cu<sub>5</sub> molecule with respect to the first one was modified in a range of distances and orientations. For this, we varied the distance between the two centers of mass along each of the axes, making it equal to 4.0, 5.0 and 6.0 Å for X, 6.0 and 7.0 Å for Y, and 7.0 and 8.0 Å for displacements along the Z-axis. Regarding the angles we considered three rotations for each of the geometries, *i.e.* the first one around the X-axis and with values of 0, 60, and 90 degrees; the second one around the Z axis, taking angles of 0, 45, and 90 degrees; and the last one around the X axis and with values of 0, 60, 120, 180, 240, 300, 360 degrees. The resulting geometries

were fully optimized at the dispersion-corrected DFT levels, and those corresponding to the lowest energies were selected for further optimizations through DF-CASSCF calculations. The active spaces in DF-CASSCF calculations [ $m$  electrons in  $m$  orbitals, referred as ( $m,m$ ) active space] varied until convergence was achieved in the follow-up RS2C calculations of coupled Cu<sub>5</sub>–Cu<sub>5</sub> cluster energies. In all cases we considered the singlet ground state of the clusters and no symmetry restrictions were imposed in the calculations. The results of the preliminary DFT calculations can be obtained from the authors upon request. Results on previous theoretical evaluations of copper cluster geometries are available in the literature, see for instance ref. 39 and 40, but as far as we are aware, the authors of these investigations applied DFT level and not multireference *ab initio* approaches, with the resulting geometries differing from those obtained in this work. All interaction energies ( $E_{\text{inter}}$ ) were calculated as follows:

$$E_{\text{inter}} = \{E_{\text{Cu}_5\text{--Cu}_5}\}_{\text{Min}} - \{E_{\text{Cu}_5\text{--Cu}_5}\}_{\text{Asymp}}$$

where  $\{E_{\text{Cu}_5\text{--Cu}_5}\}_{\text{Min}}$  is the energy at the minimum and  $\{E_{\text{Cu}_5\text{--Cu}_5}\}_{\text{Asymp}}$  is that at the asymptotic limit, correlating with the corresponding two Cu<sub>5</sub> + Cu<sub>5</sub> fragments in their energetically most favored structures. For the sake of size consistency, both calculations were carried out using the same active space within the DF-CASSCF and RS2C methodologies.

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