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Machine learning-driven investigation of the structure and dynamics of the BMIM-BF₄ room temperature ionic liquid†

Fabian Zills, ^a Moritz René Schäfer, ^b Samuel Tovey, ^a
Johannes Kästner ^b and Christian Holm ^{*a}

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Room-temperature ionic liquids are an exciting group of materials with the potential to revolutionize energy storage. Due to their chemical structure and means of interaction, they are challenging to study computationally. Classical descriptions of their inter- and intra-molecular interactions require time intensive parametrization of force-fields which is prone to assumptions. While *ab initio* molecular dynamics approaches can capture all necessary interactions, they are too slow to achieve the time and length scales required. In this work, we take a step towards addressing these challenges by applying state-of-the-art machine-learned potentials to the simulation of 1-butyl-3-methylimidazolium tetrafluoroborate. We demonstrate a learning-on-the-fly procedure to train machine-learned potentials from single-point density functional theory calculations before performing production molecular dynamics simulations. Obtained structural and dynamical properties are in good agreement with computational and experimental references. Furthermore, our results show that hybrid machine-learned potentials can contribute to an improved prediction accuracy by mitigating the inherent shortsightedness of the models. Given that room-temperature ionic liquids necessitate long simulations to address their slow dynamics, achieving an optimal balance between accuracy and computational cost becomes imperative. To facilitate further investigation of these materials, we have made our IPSuite-based training and simulation workflow publicly accessible, enabling easy replication or adaptation to similar systems.

Introduction

The application of machine learning in computational chemistry has started a revolution in material design and understanding. While the methods themselves have been developing gradually for more than a decade,^{1–3} it is only recently

^aInstitute for Computational Physics, University of Stuttgart, 70569 Stuttgart, Germany. E-mail: holm@icp.uni-stuttgart.de

^bInstitute for Theoretical Chemistry, University of Stuttgart, 70569 Stuttgart, Germany

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that the community has started to see breakthroughs in their applications to chemistry and materials science.⁶ This can be attributed to the development of advanced training strategies,⁷ improved accelerator hardware,⁸ and new model architectures.⁹ One family of materials that has been of great interest for years are room-temperature ionic liquids (RTILs). These molecular liquids find application in a diverse range of fields¹⁰ from battery technology,¹¹ super-capacitors,¹² carbon capture devices,¹³ biomass extraction,¹⁴ and many more.^{15–17} The potential to customize them for particular purposes has enabled their use in a wide range of applications. Their adaptability arises from the presence of cationic and anionic molecules, which can be modified to meet specific requirements. The large design space of RTILs make *in silico* studies an exciting endeavor. However, a significant obstacle is their complex and long-ranged interactions. Their treatment typically requires *ab initio* methods such as density functional theory (DFT), since classical approaches will struggle to capture all relevant effects. The highly viscous nature of RTILs results in slow dynamics, which are impossible to study using these levels of theory. However, with the development of machine-learned potentials (MLPs), these simulations have become tractable, as it is now possible to capture close to *ab initio* accuracy on near classical time and size-scales. RTILs possess a large configuration space, hence training of MLPs must be done with great care to not fall into unphysical configurations during deployment. Furthermore, DFT calculations need high accuracy to capture relevant interactions inside the materials which again incurs substantial computational cost. Moreover, careful attention must be paid to dispersion interactions.¹⁸

In this work, we demonstrate our approach for the construction of an MLP for the RTIL 1-butyl-3-methylimidazolium tetrafluoroborate BMIM⁺BF₄[−]. We train the model starting from a small number of configurations obtained from a classical trajectory and then perform a learning-on-the-fly (LotF) workflow to iteratively improve the MLP, thereby exploring a significant portion of configuration space. This approach allows us to overcome the use of extensive *ab initio* calculations, thus reducing the overall computation time. In order to assess the accuracy of the potential, we perform large-scale molecular dynamics (MD) simulations in the *NPT* and *NVT* ensembles and compare the resulting structures and dynamics to literature values. Our work demonstrates that, with state-of-the-art LotF strategies for MLPs approaches, it is feasible to study this complex family of materials to previously unseen accuracy. Comparable studies on RTILs by Shayestehpour and Zahn¹⁹ and Montes-Campos *et al.*²⁰ showed that MLPs can reproduce experimental self-diffusivity. With our MLPs we can achieve similar accuracy, while using significantly less training data than the DeepMD²¹ based approach.

The paper is structured as follows. We first introduce the machine learning and training methods used within our study. We then present the results of the production simulations and compare them to literature values. Finally, we highlight open areas for continued research into the material before summarizing our work in the conclusion. In particular, we demonstrate how the inclusion of physically inspired terms, namely D3 dispersion corrections, can be used in hybrid models. These corrections compensate for missing long-range interactions, which play a crucial role in obtaining accurate densities.



Methods

Reference quantum chemistry method

All quantum chemistry calculations were performed using the CP2K software package^{22–25} at the DFT level. The exchange–correlation energy was approximated using the B97-3C functional.^{26,27} The electronic wavefunctions were expanded in an atom-centered TZVP-GTH basis set²⁸ with GTH-PBE pseudopotentials.^{29–31} A cutoff of 800 Ry was used for the auxiliary plane wave basis. The parameters were adopted from Perl *et al.*¹⁸ and are tailored for the description of ionic liquids.

Dispersion correction

A good description of dispersion interactions is crucial, as they are known to play a significant role in imidazolium-based ionic liquids, due to hydrogen and alkyl chain interactions.¹⁸ During LotF, all DFT calculations were combined with the empirical D3 dispersion correction by Grimme *et al.*³² including Becke–Johnson damping.³³ Initially, the correction was applied within CP2K with a cutoff of 8 Å and many body C_9 terms. To investigate the effect of dispersion on MLP training and MD simulations, the dataset was recomputed without D3 correction. We utilize the performant Torch-DFTD³⁴ implementation of the D3 method to obtain a corrected and uncorrected version of the data. We added the D3 parameters for the B97-3C functional from Brandenburg *et al.*²⁶ to the Torch-DFTD package. Furthermore, we have extended the Atomic Simulation Environment (ASE) calculator provided by the package with an option to only rebuild the neighbor list when atomic displacements exceed a threshold value. This was set to 0.5 Å throughout this work and roughly doubled the inference speed of the Torch-DFTD ASE calculator.

Machine learning potential

In this work, we utilize the Apax³⁵ package for training Gaussian Moment Neural Networks (GMNNs).^{36,37} Similar to other MLPs, the nearsightedness of electronic matter³⁸ is exploited to divide the total energy of a structure, S , into atomic contributions.

$$E(S, \theta) = \sum_i^{N_{\text{atoms}}} E_i(\mathbf{G}_i, \theta) \quad (1)$$

Here, $\mathbf{G}_i$ are the descriptors of the local environments and θ denotes the set of all trainable parameters. The GMNN model, in particular, consists of two parts, the Gaussian moment descriptor and feed-forward neural networks. The former constructs a smooth neighborhood density from a basis of equidistant Gaussians. These are linearly combined by element-pair coefficients β to form contracted radial basis functions R and angular information is captured by an L -fold outer product of normalized, inter-atomic distance vectors $\hat{\mathbf{r}}_{ij}$.

$$\psi_{i,L,s} = \sum_{j \neq i} R_{Z_i, Z_j, s}(r_{ij}, \beta_{ij}) \hat{\mathbf{r}}_{ij}^{\otimes L} \quad (2)$$

The final Gaussian moment descriptor $\mathbf{G}_i$ is obtained from a set of full tensor contractions.



$$\begin{aligned}
 G_{i,s_1,s_2} &= (\Psi_{i,1,s_1})_a (\Psi_{i,1,s_2})_a \\
 &\vdots \\
 G_{i,s_1,s_2,s_3} &= (\Psi_{i,1,s_1})_a (\Psi_{i,3,s_2})_{a,b,c} (\Psi_{i,2,s_3})_{b,c}
 \end{aligned}
 \quad (3)$$

Atomic energies are predicted from neural networks. These are scaled and shifted by element-wise learnable parameters σ_{Z_i} and μ_{Z_i} .

$$E_i = \sigma_{Z_i} \cdot NN(S) + \mu_{Z_i} \quad (4)$$

Finally, the scaled and shifted atomic contributions are summed up as in eqn (1). Forces and virials are computed using automatic differentiation according to eqn (5) and (6).

$$\mathbf{F}_i = -\nabla_{\mathbf{r}_i} E(S, \boldsymbol{\theta}) \quad (5)$$

$$\boldsymbol{\sigma} = \frac{1}{V} \nabla_{\boldsymbol{\varepsilon}} E(S, \boldsymbol{\theta}) \Big|_{\boldsymbol{\varepsilon}=0} \quad (6)$$

Here, V denotes the cell volume and $\boldsymbol{\varepsilon}$ the symmetric strain deformation tensor. During training, the model parameters are updated using the Adam optimizer³⁹ to minimize a compound loss function comprised of energy, force and stress tensor errors.

$$\begin{aligned}
 \mathcal{L}(\boldsymbol{\theta}) = \sum_{k=1}^{N_{\text{train}}} \left[\lambda_E \|E_k^{\text{ref}} - E(S_k, \boldsymbol{\theta})\|_2^2 + \lambda_F \sum_i \frac{1}{3N_{\text{atoms}}^{(k)}} \|\mathbf{F}_{i,k}^{\text{ref}} - \mathbf{F}_i(S_k, \boldsymbol{\theta})\|_2^2 \right. \\
 \left. + \lambda_S \|V_k \boldsymbol{\sigma}_k^{\text{ref}} - V_k \boldsymbol{\sigma}(S_k, \boldsymbol{\theta})\|_2^2 \right] \quad (7)
 \end{aligned}$$

For all training runs, a weighting of $\lambda_E = 1$, $\lambda_F = 4 \text{ \AA}$ and $\lambda_S = 0.2$ was used. Emphasizing the force contribution to the loss function has proven to be successful in many studies,^{5,37} as forces reveal more information about the local structure than the total energy of the system.⁴⁰ A limitation of short-range potentials is that longer range interactions, such as dispersion, cannot be fully captured. However, a correct reproduction of densities necessitates the inclusion of precisely these effects. While a part of the dispersion energy resulting from *e.g.* the D3 correction may be learned directly, it is also possible to build hybrid models^{34,41} for which the D3 correction is added on top of the model predictions as $E = E_{\text{MLP}} + E_{\text{D3}}$.

Throughout this work, we use 7 Gaussian functions for the radial grid and contract them down to 5 with $r_{\text{min}} = 0.7 \text{ \AA}$ and $r_{\text{max}} = 5.5 \text{ \AA}$. The latter was increased to $6.0 \text{ \AA}$ for the final model. Neural networks with 2 hidden layers consisting of 512 units, respectively, were used for all models. Learning rates for β , the neural network, scaling and shifting parameters were independently set to 0.01, 0.005, 0.001 and 0.05, respectively. The batch size was set to 4 and the number of training epochs to 500 during the iterative training procedure and set to 1 and 2000 for the final models.

Learning-on-the-fly

An initial dataset was sampled from a trajectory generated using GROMACS 2021⁴² with the OPLS-AA force field.^{43,44} A 5 ns simulation for 10 ion pairs at the



density of 1.210 g cm^{-3} at 500 K was conducted. Starting with this trajectory, the entire LotF workflow was built using the Python package IPSuite.^{45,46} Within IPSuite, interfaces to MLP, DFT, and MD codes, in conjunction with analysis methods, are available. Initially, 100 datapoints were randomly selected for both the training and validation datasets, and subsequently, a first set of models was trained. We introduce the following notation for the iteration and number of models in the ensemble: $\overline{\text{MLP}}_{\text{iteration}}^{\# \text{models}}$. Further, models for which the dispersion correction was learned implicitly are denoted by $\overline{\text{MLP}}(\text{D3})$ and hybrid models as $\overline{\text{MLP}} + \text{D3}$.

In order to obtain uncertainties for the predictions, an ensemble of two models was used throughout this work. During sampling simulations, the force uncertainty σ defined by eqn (8) was used as a stopping criterion with a threshold value of $0.5 \text{ eV \AA}^{-1}$.

$$\sigma = \max_{i \in N_{\text{at}}} \max_{\alpha \in \{x,y,z\}} \sqrt{\frac{1}{N_{\text{ens}}} \sum_m^{N_{\text{ens}}} \left(F_{i,m}^{(\alpha)} - \bar{F}_i^{(\alpha)} \right)^2} \quad (8)$$

From then on, each new iteration starts with a trajectory driven by the MLP. At iteration 4, the model was able to simulate for 25 ps in the NVT ensemble at 298.15 K without triggering the stopping criterion. The dynamics were modified to enhance the sampling and encounter more informative configurations in subsequent iterations. For this purpose, temperature and density were modified during the simulation according to eqn (9), where Q denotes the modified quantity.

$$Q(t) = Q_{\text{start}} + \frac{t}{t_{\text{end}}} (Q_{\text{end}} - Q_{\text{start}}) + Q_{\text{amp}} \sin\left(\frac{t}{t_{\text{per}}}\right) \quad (9)$$

During some iterations we have extended the dataset with additional samples from geometry optimizations, rigid-molecule volume scans⁴⁷ and conformational sampling. To generate the conformers, we utilize RDKit.⁴⁸ Bulk structures are then created from these using PACKMOL⁴⁹ at reduced densities. MD as well as the other sampling methods generate a large number of candidate configurations. However, the structures at subsequent time steps are highly correlated and thus only a subset of these candidates should be recomputed with DFT. In order to select this subset we utilize recently developed batch data selection methods. Throughout this work we use the combination of last-layer gradients and MaxDist selection, as described by Zaverkin *et al.*⁵⁰ In cases where the pool is too large, we resort back to simple random selection. For this work, we have extended the Apex package with these methods. The parameters for the dynamics modifiers, the number of datapoints and data sources as well as the selection methods used are listed in Table 1 for each iteration. In total, a final training dataset of 1589 configurations was created. Until the final iteration, all models were trained on dispersion corrected DFT data. The final set of models were trained on just DFT, DFT+D3(8 Å) and DFT+D3(20 Å).

This setup makes very few assumptions about the material under investigation. Material dependent parameters are the selected ranges for temperatures and densities and the DFT parameters. This allows for straightforward transfer to similar systems.



Table 1 Details of the construction of the dataset. For each iteration the number of new data points as well as the sampling methods, temperature and density/pressure conditions. Whenever temperature/density are modified during the trajectory, the range of values is stated. For *NPT* simulations the pressure is reported. VS denotes rigid-body volume scans

It.	#	MD	T/K	Conditions
0	500	<i>NVT</i>	500	1.210 g cm ⁻³
1–4	4 × 50	<i>NVT</i> , GeoOpt	298.15	1.210 g cm ⁻³
5–7	3 × 50	<i>NVT</i> , GeoOpt	230–500	1.210 g cm ⁻³
8–10	3 × 50	<i>NVT</i>	298.15	0.992–1.499 g cm ⁻³
11	20	Conformers	—	0.900 g cm ⁻³
12	50	<i>NVT</i>	230–500	0.992–1.499 g cm ⁻³
13	100	<i>NPT</i> , VS	300	1.0 atm, 0.151–1.661 g cm ⁻³
14	50	<i>NPT</i>	300–500	1.0 atm
15	100	<i>NPT</i>	200–300	1.0 atm
16	105	<i>NPT</i> , GeoOpt	300	1.0 atm, —
17	164	<i>NVT</i> , <i>NPT</i> , GeoOpt	500, 298.15	1.210 g cm ⁻³ , 1.0 atm, 0.900 g cm ⁻³

Production simulations

In order to obtain initial structures, we generated conformations of the ions using RDKit⁴⁸ and PACKMOL⁴⁹ to place them in a cubic box at a reduced density of 0.9 g cm⁻³. After a geometry optimization using FIRE⁵¹ as implemented in ASE,⁵² the simulation box was adjusted to the experimental densities.⁵³ This was done for each temperature by continuously scaling the box size over the course of a 5 ps MD simulation.

Simulations for radial distribution functions (RDFs) and diffusion coefficients calculations were performed using $\overline{\text{MLP}}_{17}^2(\text{D3})$ in the *NVT* ensemble using the Nosé–Hoover chain thermostat.⁵⁴ Trajectories were simulated at temperatures $T \in \{283, 293, 313, 333, 353\}$ K for $n \in \{8, 16, 32\}$ pairs of BMIM⁺ and BF₄⁻ ions. The system was then equilibrated over 5 ps before a 20 ns production simulation using JaxMD⁵⁵ was conducted. The density simulations were performed for $n = 10$ ion pairs at the same temperatures. The initial structures were equilibrated in the *NVT* ensemble for 200 ps and production simulations in the *NPT* were performed for 1 ns using the Nosé–Hoover chain thermostat⁵⁴ with the Parrinello–Rahman barostat.^{56,57} While the JaxMD interface of Apax is significantly more performant than the ASE calculator, the utilization of Torch-DFTD for the hybrid $\overline{\text{MLP}}_{17}^2 + \text{D3}$ models necessitates the use of ASE. As such, all *NPT* simulations were performed with ASE. Confidence intervals for the simulated densities were obtained by applying the block averaging method.⁵⁸ Additionally, *ab initio* molecular dynamics (AIMDs) at temperatures of 283 K and 353 K were performed. The simulation box was prepared analogously to the *NVT* production simulations, using $\overline{\text{MLP}}_{17}^2(\text{D3})$. Both simulations span 10 ps with 16 ion pairs and were performed using a Langevin thermostat. All simulations used a time step of 0.5 fs.

Results and discussion

Model evaluation

The MLPs were continuously evaluated against the validation dataset during the LotF cycles. A final evaluation of $\overline{\text{MLP}}_{17}^2$ and $\overline{\text{MLP}}_{17}^2(\text{D3}(8 \text{ \AA}))$ is shown in Fig. 1.



The $\overline{\text{MLP}}_{17}^2$ model is able to predict the DFT energies, forces and stress with mean absolute errors (MAEs) of 2.2 meV per atom, 48.0 meV $\text{\AA}^{-1}$ and 2.59 meV $\text{\AA}^{-3}$, respectively. Energy and stress prediction errors of the $\overline{\text{MLP}}_{17}^2(\text{D3}(8 \text{ \AA}))$ model have increased to 5.2 meV per atom and 2.99 meV $\text{\AA}^{-3}$. However, the quality of force predictions is essentially identical at an MAE of 48.0 meV $\text{\AA}^{-1}$. This is to be expected, as the tail of the dispersion interaction contributes a constant shift to energy and pressure.⁵⁹ Overall, the accuracy of force predictions by models of the 17th LotF iteration almost reach chemical accuracy (43 meV $\text{\AA}^{-1}$), and were thus chosen for the subsequent production simulations.

Another important aspect, crucial for the investigation of structural and dynamic properties of RTILs, is the inference time of the MLPs. An overview of different models on various system sizes is shown in Fig. 2. Whilst the hybrid MLP+D3 models are more accurate, they are not compatible with the JaxMD interface and thus running MD is 3.5 and 20 times slower using ASE. Compared to AIMD, simulations using $\overline{\text{MLP}}_{17}^2(\text{D3})$ are ≈ 3000 times faster on 16 ion pairs and can be scaled to larger system sizes. Although the linear scaling of MLPs allows for investigations of large-scale systems, the maximum system size on a single GPU is restricted by the VRAM capacity. Within the current Apax implementation of GMNN, this is limited to approximately 330 ion pairs on an RTX 4090 GPU.

Structure

The structure of the RTIL was analyzed by calculating the RDF for all atom pairs in the *NVT* simulations. The RDFs obtained from the MLP simulations as well as the deviation from the AIMD results are displayed in Fig. 3.

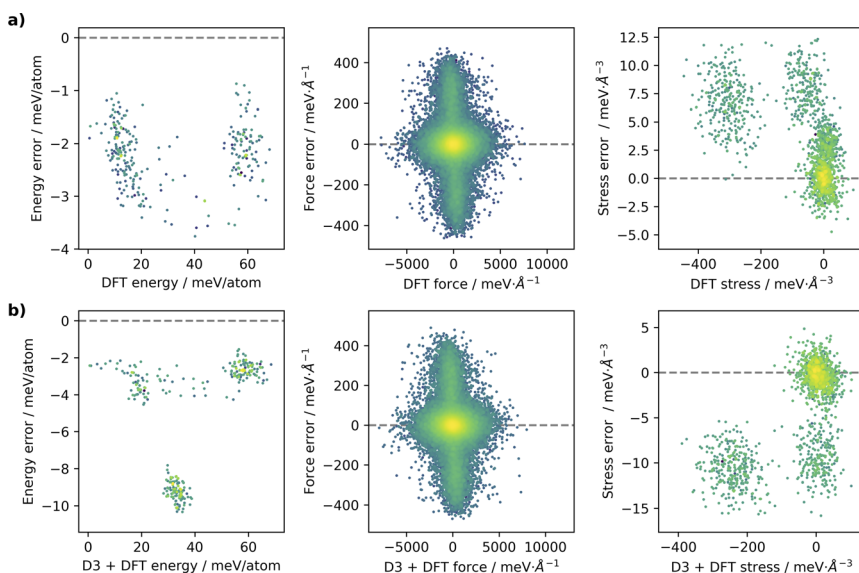


Fig. 1 Correlation plots for (a) $\overline{\text{MLP}}_{17}^2$ and (b) $\overline{\text{MLP}}_{17}^2(\text{D3}(8 \text{ \AA}))$ compared to the validation dataset without and with D3 corrections, respectively. The errors are computed as the difference between the MLP and DFT observables. A higher point density is indicated by a yellow hue.



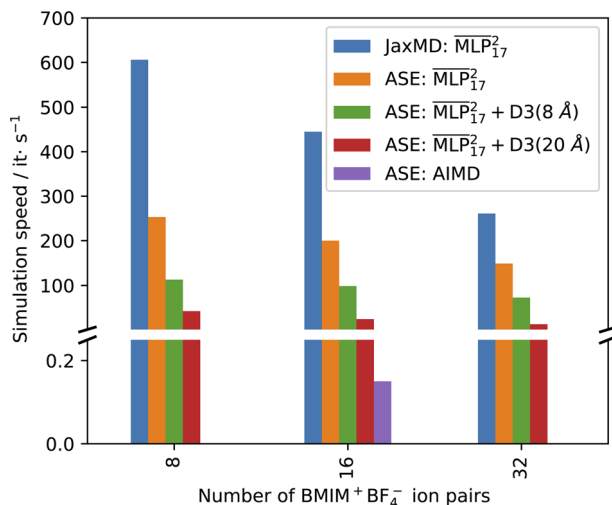


Fig. 2 Inference times of the original and hybrid $\overline{\text{MLP}}_{17}^2 + \text{D3}$ models for different system sizes on a single RTX 4090 GPU compared to AIMD simulations on 256 cores.

The RDFs are generally in good agreement with the reference AIMD simulations. This shows that inter- and intramolecular energies and forces are well predicted by the MLP. Differences between the RDFs of the MLP and AIMD can primarily be attributed to noise in the AIMD simulations caused by the short simulation times. The noticeable difference in the interatomic RDFs, especially the B-B RDF was further investigated by running 20×2.5 ps AIMD simulations at 353 K, starting at uniformly sampled configurations from the 20 ns MLP simulation. No significant energy jumps were observed in the AIMD trajectories, indicating that the MLP-obtained starting structures are also well equilibrated under the reference method. The energy over time of the trajectory is illustrated in Fig. S15.†

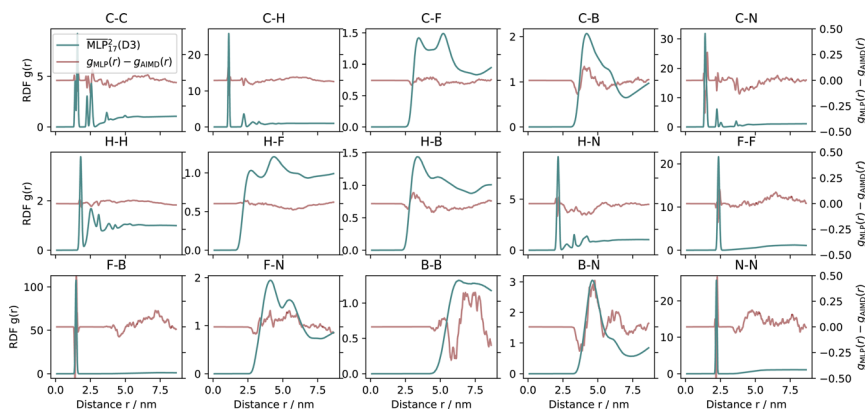


Fig. 3 Comparison of RDFs at 353 K for 16 ion pairs of $\text{BMIM}^+\text{BF}_4^-$ from 20 ns MLP MD and 10 ps AIMD simulations.



The combined RDF of the MLP and AIMD simulations is shown in Fig. 4. RDFs were computed using the MDSuite software⁶⁰ over the entire trajectories with 1000 bins each. The smoothing of the B–B RDF can be explained by the long correlation time in the movement of the *n*-butyl chains, which are not captured in the short AIMD simulations. Fig. 5 shows how the distribution of the dihedral angles φ of the *n*-butyl chain changes over time. Some angles are only visited after 1 ns of simulation time. Furthermore, emergence of an equilibrated angle distribution is not even fully reached after 20 ns of MLP simulation.

Dynamics

Diffusion coefficients were computed using the Einstein relation from the mean squared displacement of the H and B atoms in the NVT production simulations. The mean squared displacement was computed using a customized MDAnalysis^{62–65} toolkit integrated with IPSuite.⁴⁶

The results for the $\overline{\text{MLP}}_{17}^2(\text{D3})$ are finite-size corrected using $N \in \{8, 16, 32\}$ ion pairs.^{67,68} The diffusion coefficients for BF_4^- in Fig. 6 for the MLP and experiment are represented by the B atom, whilst the classical MD computes the self-diffusion from the center of mass of the ion. The diffusion coefficients for BMIM^+ are computed from the H atoms and center of mass of the entire cation, respectively.

The diffusion coefficients for BF_4^- shown in Fig. 6 at temperature above 313 K are in good agreement with the literature values. Below these temperatures, diffusion is underestimated by the MLP. The high viscosity of the RTIL at lower temperatures indicates that the MD simulations are not long enough to capture the long correlation times in the system.

It is noteworthy that the model yields good results, despite lacking explicit long-range electrostatic interactions, crucial for classical force fields.⁶⁹ These findings are consistent with previous MLP studies of RTILs.^{19,20} However, the self-diffusion of the BMIM^+ cation is less accurately captured in MD simulations using the MLP. While we demonstrate that the implicitly learned dispersion interactions of our $\overline{\text{MLP}}_{17}^2(\text{D3})$ accurately describe the anion dynamics, a correct depiction of dispersion is particularly important for the cation, which exhibits the largest errors. It is possible that better agreement with experiment could be achieved if a hybrid model including an explicit dispersion term were used instead.

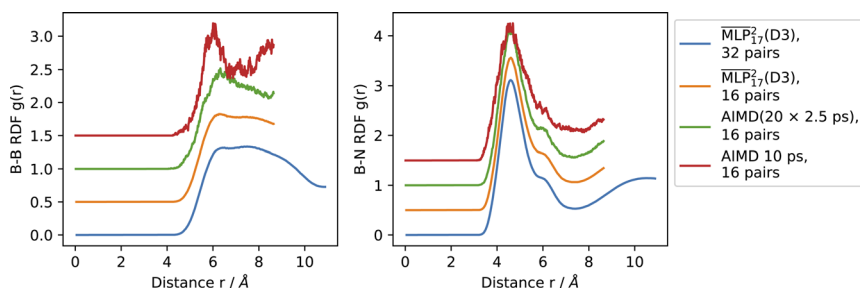


Fig. 4 RDF of B–B and B–N pairs. The B–B RDF shows significant structure, which is smoothed out over the 20 ns.





Fig. 5 Dihedral angle distribution of an *n*-butyl chain in a single BMIM⁺ cation plotted over different simulation time scales. Molecules are visualized using the ZnDraw⁶¹ package.

The results indicate that the MLP is capable of reproducing correct diffusion coefficients, drastically outperforming non-polarizable force fields. More work on learning inter-molecular interactions is required to remedy the remaining discrepancies. The errors for these observables obtained in this study are comparable to those of previous MLP-based works. However, our parameterization employed approximately 17 times fewer training configurations compared to Shayestehpour and Zahn,¹⁹ underscoring the advantages of the comprehensive LotF methodologies embedded within IPSuite, complemented by the efficiency of the Apax code.

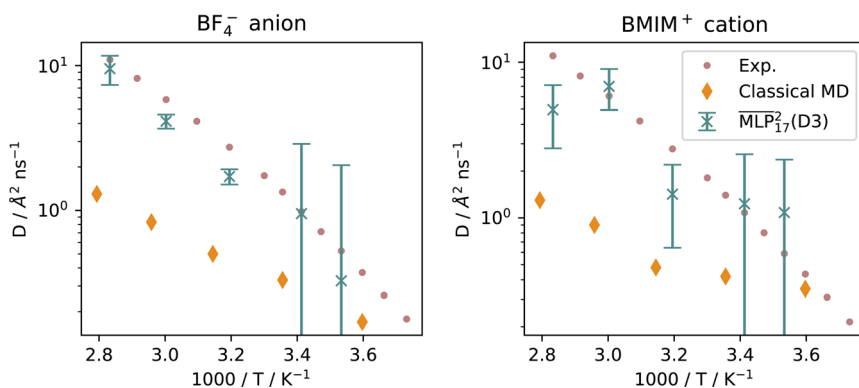


Fig. 6 Arrhenius plot of the diffusion coefficients at different temperatures. Experimental values are taken from Hayamizu *et al.*,⁵³ and results for classical MD are replicated from Bagno *et al.*⁶⁶



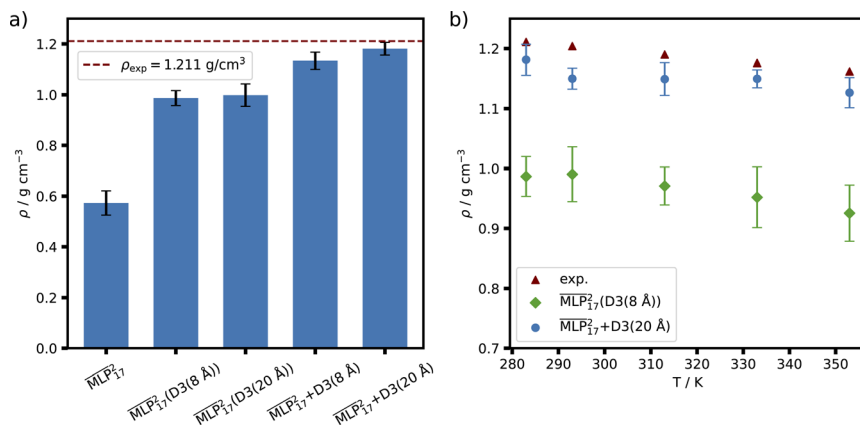


Fig. 7 Densities obtained from *NPT* simulations in comparison to experimental values taken from Hayamizu *et al.*⁵³ (a) Densities produced by models differing in the way the dispersion correction was learned or added for BMIM⁺BF₄[−] at 283 K. (b) Comparison of densities across temperatures for three of these models. Error bars indicate 95% confidence intervals.

Density

The ability of the MLP to reproduce experimental densities was investigated by computing the average density from MD simulations in an *NPT* ensemble at different temperatures. The experimental densities are taken from Hayamizu *et al.*⁵³ We compare various GMNN models that were trained on dispersion corrected DFT and hybrid models with different D3 cutoffs in order to determine the most suitable setup. Fig. 7(a) shows the densities computed by the various models at 283 K. It is known that semi-local DFT does not properly capture dispersion interactions.⁷⁰ Hence, the strong underestimation of the density by the $\overline{\text{MLP}}_{17}^2$ baseline is to be expected. Further, neither of the models trained on DFT+D3 at various dispersion cutoffs are able to capture the long range of the correction. We trained an additional model using an 8 Å radial cutoff. Unfortunately this model was not able to produce a stable simulation and increasing the cutoff further would incur a significant computational cost. The hybrid models come close to reproducing the experimental densities, with $\overline{\text{MLP}}_{17}^2 + \text{D3}(20 \text{ \AA})$ only slightly underestimating it.

The densities for the ionic liquid across various temperatures are displayed in Fig. 7(b). $\overline{\text{MLP}}_{17}^2(\text{D3}(8 \text{ \AA}))$ is also included as this was the model used to investigate the diffusion and structural properties. Across the range of temperatures $\overline{\text{MLP}}_{17}^2 + \text{D3}(20 \text{ \AA})$ achieves errors below 5% and is in good agreement with experiment. The remaining deviations may be explained by errors in the stress tensor predictions and a too small cutoff for the dispersion correction. However, increasing the latter becomes quickly expensive as the addition of the 20 Å cutoff D3 correction slows the simulation down by about a factor of 10, as shown in Fig. 2.

Summary and conclusion

We have presented an MLP for the RTIL BMIM⁺BF₄[−] using a transferable LotF approach. The MLP generated by this semi-automatic procedure was able to



reproduce structural properties compared to AIMD simulations and self-diffusion coefficients, as well as densities in good agreement with experimental values. We have shown that investigating structural and dynamic properties of the RTIL BMIM⁺BF₄[−] using AIMD is difficult due to the long correlation times in the system, and therefore, MLPs provide a pathway to study these systems with high accuracy. Finding a good compromise between accuracy and speed is still crucial with MLPs, as long-range dispersion interactions play a significant role in the RTIL BMIM⁺BF₄[−]. We have found that applying the dispersion correction terms *post hoc* to the MLP delivers the most accurate densities. However, developing efficient descriptions of long-range interactions remains one of the challenges for the application of MLPs. Nevertheless, the study of these RTILs is conducted at the performance and accuracy frontier of MLPs, demonstrating that, while recent research predominantly emphasizes accuracy enhancement, inference time is vital for performing simulations at significant system sizes and time scales.

Data availability

The workflow notebook as well as all input files for the various software packages needed to reproduce the work presented here can be found at <https://github.com/IPSPProjects/BMIM-BF4>.⁷¹ All data generated during the iterative training and production simulations are stored on an S3-object storage. It can be obtained by cloning the repository and executing `dvc pull` in the repository folder. Following the idea of Data as Code, models and simulation data can be loaded directly from the repository using the ZnTrack package.⁴⁵ Further, the data can also be accessed on DaRUS <https://doi.org/10.18419/darus-4086>.

Code availability

All software used throughout this work is publicly available. The Apax repository is available on Github at <https://github.com/apax-hub/apax>. IPSuite is available at <https://github.com/zincware/IPSuite> and can be installed from PyPi *via* `pip install ipsuite`.

Author contributions

F. Zills and M. Schäfer's contribution to the paper was conceptualization, methodology, investigation, software, validation, visualisation and writing – original draft. S. Tovey's contribution to the paper was conceptualization, methodology, supervision, writing – original draft. J. Kästner and C. Holm contributed in the fields of project administration, resources, supervision, funding acquisition and writing – review & editing.

Conflicts of interest

The authors have no conflicts of interest to declare.



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