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# Helium nanodroplets as an efficient tool to investigate hydrogen attachment to alkali cations†

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We report a novel method to reversibly attach and detach hydrogen molecules to positively charged sodium clusters formed inside a helium nanodroplet host matrix. It is based on the controlled production of multiply charged helium droplets which, after picking up sodium atoms and exposure to H<sub>2</sub> vapor, lead to the formation of Na<sub>m</sub><sup>+</sup>(H<sub>2</sub>)<sub>n</sub> clusters, whose population was accurately measured using a time-of-flight mass spectrometer. The mass spectra reveal particularly favorable Na<sup>+</sup>(H<sub>2</sub>)<sub>n</sub> and Na<sub>2</sub><sup>+</sup>(H<sub>2</sub>)<sub>n</sub> clusters for specific “magic” numbers of attached hydrogen molecules. The energies and structures of these clusters have been investigated by means of quantum-mechanical calculations employing analytical interaction potentials based on *ab initio* electronic structure calculations. A good agreement is found between the experimental and the theoretical magic numbers.

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## 1. Introduction

In the ample search for suitable materials for hydrogen storage leading to more sustainable and green energy and fuels, the important role that nanoporous materials might play in the near future<sup>1,2</sup> and the relevance of metal decoration in improving the performance of such materials have been recognized.<sup>3–5</sup> Studies have proved that the adsorption of molecular hydrogen gas on graphite, graphene, carbon nanotubes, layers of fullerenes, and other polycyclic aromatic hydrocarbon (PAH) materials is significantly improved by doping the complex with alkali atoms.<sup>6</sup> Sodium is already well known for being a promising candidate for increasing the efficiency of hydrogen attachment in multiple storage systems and a good alternative to more scarce elements like lithium.<sup>7,8</sup>

Therefore the investigation and characterization of the hydrogen–sodium interaction are important to the H<sub>2</sub> energy community, driven by the need to develop fundamentally new ways to store hydrogen in low-weight environments with high

storage density.<sup>9</sup> The physisorption energy of H<sub>2</sub> in pristine carbon-based materials is only around 40–50 meV and ~30 meV in coronene,<sup>10</sup> so the goal of doped complexes would be to raise the adsorption energies sufficiently to allow for efficient storage at moderate pressures near ambient temperatures.<sup>11,12</sup> In line with this, the characterization of the isolated cation sites and their ability to attach H<sub>2</sub> molecules<sup>13</sup> are very important since it allows us to very accurately determine the structures and interactions intervening in the hydrogen storage on nanoporous materials.

Along with a high number of already established methods of investigating this process,<sup>14</sup> this work opens up a new approach using a well-tested technique in laboratory astrochemical investigations.<sup>15–18</sup> Superfluid helium droplets provide a powerful and flexible environment for investigations of hydrogen interactions with single molecules and dopants. With this different approach, complete knowledge of the most stable structures and configurations can be obtained. Laimer *et al.* reported in 2019 on the production and stability of highly charged droplets of superfluid helium.<sup>19</sup> The potential of these multiply charged helium droplets led to the construction of a new experiment, which enables a more intense and controlled investigation of processes including the nucleation of dopant cluster ions as well as their decoration with helium or molecular hydrogen<sup>20</sup> inside of these superfluid helium nanodroplets at a temperature of 0.37 K.<sup>21</sup> This experimental setup allows accurate and reproducible control of the number of the attached hydrogen molecules. The resulting charged sodium/hydrogen complexes are analyzed using time-of-flight mass spectrometry and shell closures for the

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attachment of hydrogen are determined *via* local maxima in the ion yield of these species.

In this work, we present experimental as well as theoretical data showing the relative ion abundance of up to 15 hydrogen molecules attached to either a monomer or sodium dimer cations. They are investigated in consideration of their ability to reversibly bind molecular hydrogen. The relative ion abundances of  $\text{Na}^+(\text{H}_2)_n$  and  $\text{Na}_2^+(\text{H}_2)_n$  from mass spectra obtained by sequential pickup of sodium and molecular hydrogen into multiply charged helium nanodroplets are compared with quantum mechanical calculations. The computational results provide detailed information about the binding energy and structure of a specific number of  $\text{H}_2$  molecules attached to a positively charged sodium atom or dimer. The structure of the paper is as follows: Section 2 outlines the methods employed, both experimental and theoretical; in Section 3 we analyze the experimental data and present the theoretical results; Section 4 is devoted to conclusions.

## 2. Methods

### 2.1. Experimental

The experimental setup utilized in this work has been explained in detail elsewhere,<sup>22</sup> but a brief description is given below. Helium nanodroplets (HNDs) are produced *via* supersonic expansion of ultrapure helium (Messer, purity 99.9999%) with a stagnation pressure of 20 bar through a 5  $\mu\text{m}$  pinhole nozzle into ultrahigh vacuum. The nozzle was cooled with a closed-cycle cryocooler (Sumitomo Heavy industries) and counter-heated with an ohmic resistor operated with a PID controller (Lakeshore Model331) to 8.8 K. Under the present conditions the pressure in the source chamber increases from 0.01 mPa to 53 mPa. According to Gomez *et al.*<sup>23</sup> and Laimer *et al.*<sup>19</sup> the resulting average droplet size is calculated to be  $5 \times 10^6$  He atoms under the present conditions. To prevent the destruction of HNDs by collisions with shock fronts, the resulting jet of He was then passed through a 0.5 mm skimmer (Beam Dynamics, Inc) located 10 mm after the nozzle. HNDs are ionized by a Nier-type electron impact ionization unit directly after the skimmer. The ion source was operated at an electron energy of 65 eV and an electron current of 350 mA. Under these conditions most HNDs are hit by multiple electrons that can directly ionize helium atoms; the positively charged  $\text{He}^+$  moves to the center of the droplet and, after several steps, ends forming  $\text{He}_2^+$ . This ion is subsequently solvated by neighboring He atoms leading to tight  $\text{He}_3^+$  structures.<sup>24</sup> The three atoms ionic core then forms the so-called Atkins snowball.<sup>25,26</sup> Mutual repulsion of these  $\text{He}_n^+$  charge centers into minimum energy configurations distributes them uniformly close to the surface of HNDs.<sup>27</sup> This results in a mean charge state of the selected HNDs of  $z = 15$ . Charged droplets, consisting of  $3 \times 10^5$  He atoms per charge were then mass-per-charge filtered by an electrostatic quadrupole bender. Subsequent guiding of the charged HNDs through sodium vapor leads to the pick-up of single atoms. Due to the heliophobic nature of sodium atoms, they stay unsubmerged on

the surface of the HNDs until a certain limit is reached.<sup>28</sup> The polarizability of captured sodium is much higher than that of He and therefore, ion-induced dipole interaction attracts dopants to the charge centers also sitting close to the surface of the droplet. Charge transfer from  $\text{He}_n^+$  to the first dopant leads to a  $\text{Na}^+$  charge center and the excess energy due to the difference in the ionization energies will be dissipated into the HNDs and leads to the evaporation of 1600 He atoms per eV. Further dopants will simply attach to an already existing ionic core and the binding energy will be transferred to the surrounding He, leading to the evaporation of additional He atoms from the surface of the HND. Subsequent collisions with room temperature  $\text{H}_2$  vapor first replaces He atoms surrounding the sodium ions with hydrogen molecules and upon consecutive collisions with  $\text{H}_2$  the droplet shrinks below the critical size for the given charge state and a hydrogen solvated sodium cation is ejected from the droplet. In the next section, we will compare binding energies for the cluster interactions in the cases of He and  $\text{H}_2$ , and the easy replacement of the first by the second species will then be easily understood. With increasing hydrogen pressure in this evaporation cell (see Fig. 1) the amount of  $\text{H}_2$  molecules solvating the sodium ions can be reduced appropriately to enhance the visibility of intensity anomalies and shell closures. This effect can be readily noticed in the ESI,<sup>†</sup> Fig. S1, where several pressures of hydrogen can be seen and its influence in the population of different sodium clusters. The hydrogen solvated sodium ions are analyzed using a time-of-flight mass spectrometer (Q-TOF Ultima Waters/Micromass).

Fig. 2 displays a section of mass spectrum obtained by the method described above. A larger range of masses ( $m/z$ ) that can be reached in the experiment can be found in the ESI,<sup>†</sup>

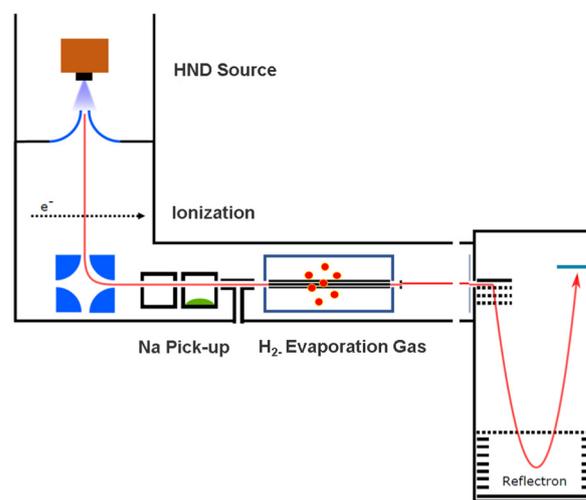


Fig. 1 The experimental setup used to decorate  $\text{Na}^+$  and  $\text{Na}_2^+$  sodium cations with  $\text{H}_2$  molecules embedded in helium nanodroplets (HNDs). The ionized and size-to-charge selected HNDs are first doped with sodium in the pick up chamber. Subsequent pick up of molecular hydrogen leads to a replacement of helium with  $\text{H}_2$  and to the solvation of the sodium ions with hydrogen. Furthermore, the helium matrix is then stripped from the embedded cluster ions by collisions with  $\text{H}_2$  gas at ambient temperature in the evaporation cell.



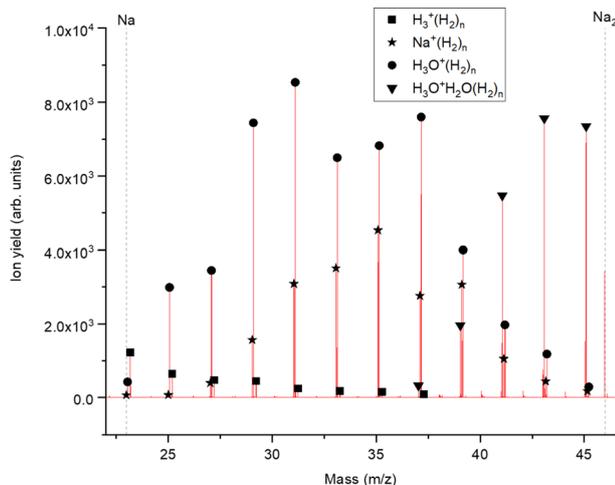
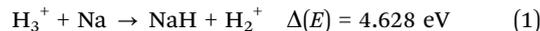


Fig. 2 Example of a mass spectrum showing the H<sub>2</sub> decoration of positively charged sodium monomers. A hydrogen pressure of 40 mPa leads to an environment where the pure hydrogen series as well as the hydrogen decoration of water clusters is visible. The exact mass of the impurities never overlaps with the slightly less heavy sodium series and is therefore not influencing its intensity distribution. On the left side of the spectrum the pure hydrogen series is still present (squares) and on the right half the water dimer (triangle) series is starting. The hydrogen decoration of the sodium cation is labeled with stars.

Fig. S2. Important mass peaks are the bare sodium monomer ( $m/z = 23$ ) and dimer ( $m/z = 46$ ) cations, followed by mass peaks due to  $\text{Na}_{1,2}^+(\text{H}_2)_n$ . In the mass spectrum sodium cluster ions  $\text{Na}_m^+$  up to sizes of  $n = 13$  can be identified and the corresponding mass peaks are indicated in Fig. 2 by the dashed vertical lines (as well as in Fig. S2 in the ESI<sup>†</sup>). Under the present conditions, where sodium cluster ions are solvated by hydrogen molecules, the cluster size distribution of  $\text{Na}_m^+$  does not exhibit the well-known intensity anomalies often reported for cationic alkali clusters,<sup>29,30</sup> however, several  $\text{Na}_m^+(\text{H}_2)_n$  cluster size distributions exhibit clear intensity anomalies as a function of the number of hydrogen molecules  $n$ . The mass spectra for different pressures in the evaporation cell were measured to confirm the magic numbers of the  $\text{Na}^+(\text{H}_2)$  and  $\text{Na}_2^+(\text{H}_2)_n$  cluster size distributions shown in the results.

The setup is easily adjustable and in order to rule out pick up effects, experiments with H<sub>2</sub> predoping and helium as an evaporation gas were performed. This alternative sequence leads to the same cluster products and similar relative ion abundances as the previous pick up sequence. To probe the possible underlying mechanism in the alternative pick up sequence, we carried out high level *ab initio* calculations. When sodium is picked up first, as in the regular sequence, the main pathway would follow a charge transfer from the HND to sodium ( $\text{Na}^+$ ) with subsequent addition of molecular hydrogen, resulting in the mass spectrum shown in Fig. 2. On the other hand, with a reversed pickup sequence in which H<sub>2</sub> doping is achieved first, charge transfer leads to  $\text{H}_2^+$  and *via* pickup of additional hydrogen molecules to  $\text{H}_3^+$  as the first charge carrier (see ref. 20 for an explanation leading to this triatomic species),

this species can further encounter Na with two possible outcomes,



It can be seen that the theoretical electronic energy difference (obtained from reactants and products optimizations at the MP2/aug-cc-pVTZ level of theory) clearly favors the second pathway, thus suggesting an explanation of why both pick up sequences lead to the same results. Since  $\text{NaH}^+$  is not a chemical species but rather an aggregate and H in eqn (2) is more weakly attached to the  $\text{Na}^+$  cation than the corresponding diatomic, H<sub>2</sub>, it is preferentially removed from the cluster upon collision induced activation. This explains the low abundance of the  $\text{Na}_{1,2}^+(\text{H}_2)_n\text{H}$  peak series. It is also worth noting that for similar clusters of  $\text{Cs}^+(\text{H}_2)_n$  formed in HNDs, no  $\text{CsH}^+$  species were detected.<sup>31</sup> A mass spectrum corroborating this fact can be found in the ESI,<sup>†</sup> Fig. S3.

## 2.2. Theoretical methods

**2.2.1. Potential interaction.** In order to provide an adequate theoretical description of the experimental findings, we first need to produce a suitable interaction potential for clusters containing several hydrogen molecules and cationic sodium ( $\text{Na}^+$  or  $\text{Na}_2^+$ ) species.

We have taken for the total interaction potential a sum of two-body (2B) terms and thus we write for  $(\text{H}_2)_n\text{Na}_m^+$

$$V[(\text{H}_2)_n\text{Na}_m^+] = \sum_{i=1}^n V^{2\text{B}}[\text{H}_2^{(i)} - \text{Na}_m^+] + \sum_{i<j}^n V^{2\text{B}}[\text{H}_2^{(i)} - \text{H}_2^{(j)}] \quad (3)$$

where  $n$  runs from [1–14] and  $m = 1, 2$ , for  $\text{Na}^+$  or  $\text{Na}_2^+$ . In the case of the monocation,  $\text{Na}^+$ , we have also studied the influence of three-body (3B) interactions, by adding an extra term

$$V[(\text{H}_2)_n\text{Na}^+]^{3\text{B}} = \sum_{i<j}^n V^{3\text{B}}[\text{H}_2^{(i)} - \text{Na}^+ - \text{H}_2^{(j)}].$$

The different contributions are represented by suitable functional forms,<sup>31,32</sup> whose parameters are optimized on accurate quantum *ab initio* estimations<sup>33–35</sup> for both interaction energies and monomer properties. A full account of the procedure and parameters to describe the complete force field is given in the ESI.<sup>†</sup>

An important point to be emphasized is the different representation of the long range in  $\text{Na}^+(\text{H}_2)_n$  and  $\text{Na}_2^+(\text{H}_2)_n$  clusters stability which is controlled by the induction attraction. In particular, while  $\text{Na}^+$  is a charge point,<sup>36–38</sup>  $\text{Na}_2^+$  is a strongly polarizable and elongated ionic diatom<sup>39,40</sup> showing an equilibrium distance,  $R_e$ , of 3.71 Å and a strongly anisotropic charge distribution, as suggested by its high electric quadrupole moment (see the ESI<sup>†</sup>). Therefore, the radial dependence of the induction attraction for configurations involving  $\text{Na}_2^+$  aligned along the intermolecular distance (see configurations  $L$  and  $T_b$  in the Potential Energy Surfaces section of the ESI<sup>†</sup>) assumes the canonical  $R^{-4}$  dependence (such as that for  $\text{Na}^+$ )



only asymptotically ( $R \gg R_e$ ), while in the region of interest for cluster stability ( $R \sim R_e$ ) the  $R^{-6}$  dependence, typical of a dipole, is found to be more appropriate (see Fig. S4 in the ESI†).

The expressions of the different terms in eqn (3) as well as a full account of the procedure and parameters to describe the complete force field is given in the ESI.†

**2.2.2. Cluster energies and structures.** Once a reliable potential interaction function has been formulated, our goal is to determine the structure and stability of the different clusters for increasing values of  $H_2$  monomers. The enhanced ion yield of the current experimental set-up together with the extraordinary accuracy reached in the mass spectra prompt us to take advantage of these data sets and to try the best theoretical framework to study these clusters. To this end we will make use of Path Integral Monte Carlo calculations (PIMC) in a pseudo-atom model for the  $H_2$  molecule and a Diffusion Monte Carlo (DMC) approach within a rigid rotor approximation for the mentioned hydrogen monomers. We will also check the importance of the 2B vs. 3B terms included in the interaction potential.

In the PIMC, hydrogen molecules will be treated as pseudoatoms.<sup>41,42</sup> In this method<sup>43</sup> the analogy in the partition function for a system composed of  $N$  classical ring polymers, each having  $M$  beads with the corresponding quantum system of the  $N$  particles is exploited to obtain the energy and structures of the clusters. We have used the thermodynamic estimator,<sup>44</sup> and classical minimization procedures such as Evolutionary Algorithm and a Basin-Hopping technique<sup>45,46</sup> to start sampling the initial configuration. Details of the method and parameters of interest are given in the ESI.†

The DMC method<sup>47,48</sup> computes the ground state of the cluster by means of a transformation of the time-dependent Schrödinger equation into a diffusion equation by changing the variable time,  $t$ , to imaginary time,  $\tau = it$ . The ground state of the system is then achieved as a lasting term in the (imaginary time) propagation of the diffusion equation. In this method, the wavefunction is represented by a set of replicas describing different configurations of the particles of the system and, at each time step  $\Delta\tau$ , the particles randomly move according to the kinetic energy term in the Hamiltonian and the replicas multiply or disappear with a probability depending on the value of the potential energy term.<sup>47,48</sup> We have used the implementation for rigid bodies due to Buch and collaborators<sup>49–51</sup> and a classical Monte Carlo (MC) method to obtain the initial configurations for the DMC calculations. The working parameters and details on the calculations can be found in the ESI.† We have used for all the calculations 1.007825 amu and 22.98977 amu for the masses of H and Na atoms, respectively.

Once we have briefly described the theoretical methods, we present in Fig. 3 the percentage of differences found in the cluster total energy when we use a pseudo-atom approach or we just take the 2B terms in the potential interaction for the case of  $Na^+(H_2)_n$ . A comparison is made with the rigid-rotor DMC approach including the 3B terms considered as the “exact” result. We can see that the error in total energy stabilizes very quickly and for  $n \geq 8$  it becomes practically constant. These differences correspond to the total energy but, actually, when

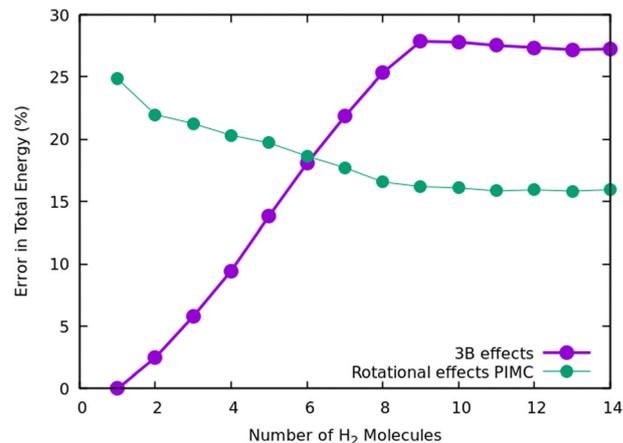


Fig. 3 Error in the estimation of cluster energies when a pseudoatom approximation is used, or when only 2B terms are employed for the interaction potential. In both cases it is assumed that the “exact” result is the one computed within the rigid rotor approximation and the additional use of a 3B term.

we consider energy differences known as evaporation energies, shown in Fig. 4, it can be appreciated that the main features regarding peaks, plateaus and slopes remain unchanged, and would lead to similar structures or magic numbers. In particular it can be observed that the 3B effects are more noticeable and that a pseudoatom approach, except for the smaller hydrogen clusters, brings no significant differences. This could be anticipated from Fig. 3 where the differences remain almost constant with a very small slope, for the pseudoatom approach.

Therefore our rather thorough analysis indicates that for larger clusters a simpler treatment (2B interactions only, or considering a system composed of pseudo atoms) can still yield accurate predictions, regarding structure and stabilities. For analysis of the results and comparison with the experiment in the next section, we will use DMC within the rigid rotor model and the 3B interaction potential for a sodium monomer, while a 2B interaction model will be used for the sodium dimer clusters.

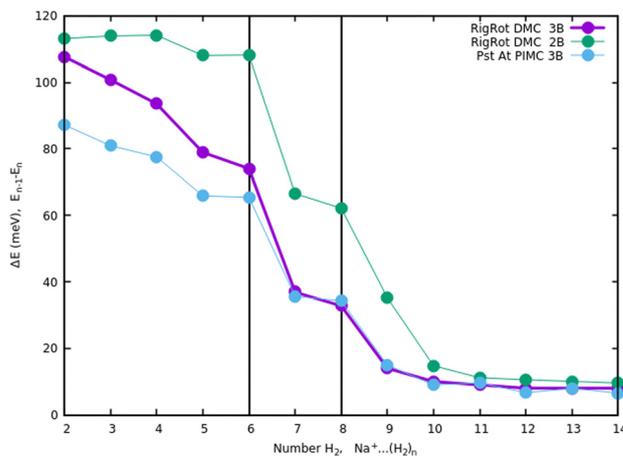


Fig. 4 Evaporation energies, for  $Na^+(H_2)_n$ , within several approaches, DMC with a rigid rotor model, 2B and 3B interaction potential and PIMC with a 3B potential.



At this point it is also useful to stress that dissociation energies computed in this work  $E_0 = -112.28$  meV for  $\text{Na}^+\text{H}_2$  and  $E_0 = -38.86$  meV for  $\text{Na}_2^+\text{H}_2$  dimers, are larger than those previously found for  $\text{Na}^+\text{He}$  ( $E_0 = 32.61$  meV in the harmonic approximation in ref. 52) and  $\text{Na}_2^+\text{He}$  ( $E_0 = -6.1$  meV,<sup>53,54</sup>  $E_0 = -7.0$  meV<sup>55</sup>), of about a factor of 3 and 6, respectively. These differences result in the easy replacement of He by  $\text{H}_2$  in the evaporation cell and are mostly due to the higher polarizability of  $\text{H}_2$  compared with He, even if the electrostatic contribution which is absent for adducts involving He plays a non-negligible role.

### 3. Data analysis and results

The experimental ion abundance  $I_n$  is plotted versus the number of the attached  $\text{H}_2$  molecules,  $n$ , in Fig. 5a and Fig. 6a for  $\text{Na}^+(\text{H}_2)_n$  and  $\text{Na}_2^+(\text{H}_2)_n$ , respectively. The data shown in these figures are extracted from the mass spectra shown in Fig. 2. The ion abundances feature local anomalies which suggest similar local effects in the evaporation energies  $\Delta E_n$ , for example at  $n = 6$  and 8 for  $\text{Na}^+(\text{H}_2)_n$ . Several procedures have been proposed in the literature in order to establish a quantitative

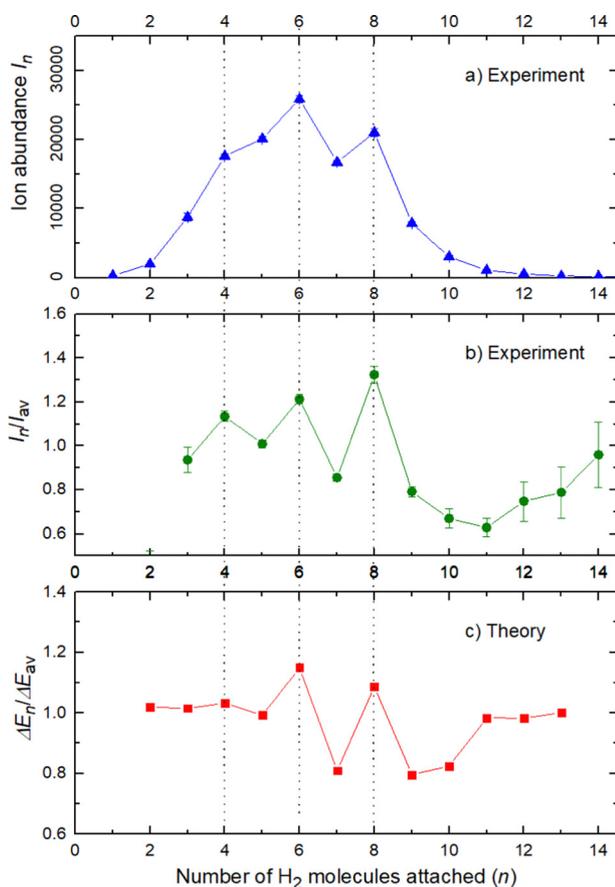


Fig. 5 Data for  $\text{Na}^+(\text{H}_2)_n$ . Panel a: experimental ion abundance versus size,  $n$ . Panel b: experimental ion abundance  $I_n$  divided by its local average,  $I_{av}$ . Panel c: evaporation energy  $\Delta E_n$  calculated with the rigid rotor model DMC, divided by its local average  $\Delta E_{av}$ . Note the similarity of the data in panels b and c.

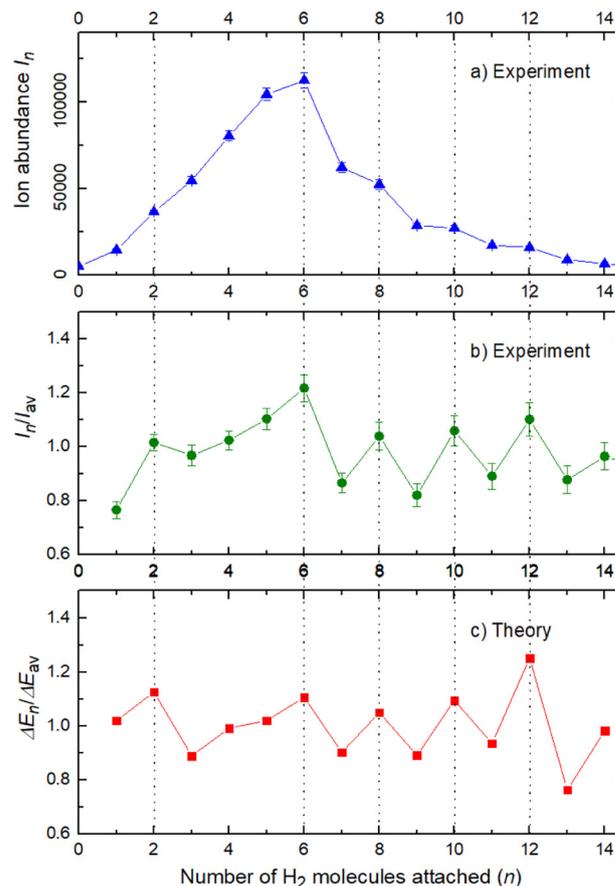


Fig. 6  $\text{Na}_2^+(\text{H}_2)_n$ . Panel a: experimental ion abundance versus size,  $n$ . Panel b: experimental ion abundance  $I_n$  divided by its local average,  $I_{av}$ . Panel c: evaporation energy  $\Delta E_n$  calculated with the rigid rotor model DMC, divided by its local average  $\Delta E_{av}$ . Note the similarity of the data in panels b and c.

relationship between anomalies in  $I_n$  and  $\Delta E_n$ ; their applicability depends on the experimental conditions. For the present data we adopt an approach that was first proposed by Leidlmair *et al.*,<sup>56</sup> and justified in more detail in ref. 57 and 58. It asserts that

$$\frac{I_n}{I_{av}} = \frac{\Delta E_n}{\Delta E_{av}} \quad (4)$$

where  $I_{av}$  and  $\Delta E_{av}$  are local averages of  $I_n$  and  $\Delta E_n$ , respectively. Eqn (4) is supposed to be valid, approximately, if two conditions are met: (i) The observed cluster ions are the unimolecular fragments of larger precursors, and (ii) the heat capacity of the observed cluster ions is close to zero, *i.e.* their vibrational modes are not excited at the relevant temperature. Condition (i) is clearly met because the hydrogen gas in the collision cell is at room temperature; the cluster ions that are extracted from the collision cell have ample time to cool by evaporation, reaching a temperature  $T \approx \Delta E_n / (G k_B)$  where  $G \approx 25$  is the Gspann parameter.<sup>59,60</sup> The most tightly bound cluster ions considered here have  $\Delta E_n \approx 0.1$  eV which corresponds to  $T \approx 50$  K. Condition (ii) is also likely to be met: Intramolecular vibrations of  $\text{H}_2$  are certainly not excited at or below 50 K, and the small mass of  $\text{H}_2$  results in



large intermolecular vibrational frequencies in the sodium-hydrogen complexes.

The left and right-hand sides of eqn (4) are plotted in Fig. 5b and c, respectively, for  $\text{Na}^+(\text{H}_2)_n$ . The local averages  $I_{\text{av}}$  and  $\Delta E_{\text{av}}$  were obtained by averaging over adjacent sizes with weights computed from a Gaussian with a standard deviation  $\sigma = 1$  (the results did not change significantly if  $\sigma = 2$  was chosen). The similarity of the data in Fig. 5b and c is excellent. Cluster ions with  $n = 6$  and 8 clearly form magic numbers, although the local maximum at  $n = 4$  in the experimental data is not completely supported by the theory. Likewise, experimental and theoretical data for  $\text{Na}_2^+(\text{H}_2)_n$  are plotted in Fig. 6b and c, respectively. Again, the two data sets are very similar; they feature local maxima at  $n = 2, 6, 8, 10,$  and 12.

These evaluations are also performed for different  $\text{H}_2$  pressures in order to exclude anomalies due to size distribution effects and the results for nearly all pressures are similar to the ones previously shown and in fact the survival of the higher ion yield at several pressures is also an indication of larger stability, or in other words, magic numbers.

The appearance of exceptionally stable structures or “magic numbers” with agreement between theory and experiment deserves some comments, specially concerning the differences and similarities between the sodium monomer and dimer and their interactions with the  $\text{H}_2$  molecules.

The simplest case corresponds to the sodium monomer, in which three clear islands of stability are apparent, for hydrogen sizes,  $n = 4, 6,$  and 8, as shown in the bottom of Fig. 5. In Fig. 7 we show the theoretical radial distribution,  $D(R)$ , for several compositions of these clusters. The distributions are normalized to the number of  $\text{H}_2$  contained within. It can be seen that up to  $n = 8$  the distributions vanish between 3–3.5 Å while for  $n = 9$ , there is a small recurrence between 4–4.6 Å that corresponds to the beginning of a new shell around the  $\text{Na}^+$  cation. These results are very similar to those found for  $\text{Li}^+\text{He}_n$ ,<sup>41</sup> where also a close resemblance can be found in the second energy differences for that system, and the one we show

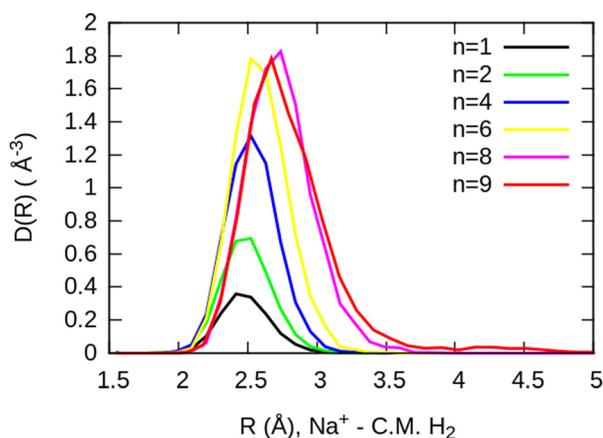


Fig. 7  $\text{Na}^+(\text{H}_2)_n$  radial distributions, normalized to the number of  $\text{H}_2$  molecules, for several cluster sizes. The closing shell at  $n = 8$ , can be noticed by the small bump that can be appreciated for  $n = 9$ .

at the bottom of Fig. 5. This result is a consequence of the interactions brought into play in both cases, with similar equilibrium distances and well depths between the cation and the other component of the cluster ( $\text{He}/\text{H}_2$ ) that, in turn, have a small interaction between them.

In the structure two angles are relevant, that we will call  $(\theta, \Phi)$ . The angles  $\theta$  in a given cluster are those formed between the vector defining the bond in a particular  $\text{H}_2$  molecule, and the vector from its center of mass to the cation. More interesting for the geometry are the  $\Phi$  angles, which are those formed between two vectors that are directed from the sodium atom, to the center of mass of two different  $\text{H}_2$  units. These angles can be better seen in the ESI,<sup>†</sup> where we have plotted the minimum energy structures obtained with classical MC simulations, in the case of  $\text{Na}^+(\text{H}_2)_6$  and  $\text{Na}_2^+(\text{H}_2)_{12}$  for the sodium monomer and dimer, respectively. They have also been included as insets, in some of the next figures.

In the case of the sodium monomer, the structure is nearly rigid, the  $\text{H}_2$  molecules orient with their bond perpendicularly to the vector joining each molecular center of mass to the cation, angle  $\theta = 90^\circ$ , with a narrow distribution around this value. On the other hand, how the different monomers are arranged surrounding the cation, is better defined by the angle  $\Phi$  and the distribution for the cluster  $\text{Na}^+(\text{H}_2)_6$  is shown in Fig. 8. As can be seen, this distribution,  $D(\Phi)$ , shows two predominant peaks with maxima at angles around 90 and 160 degrees and with little dispersion, certainly signaling a clear structure corresponding to an octahedron, that was also found previously in other clusters.<sup>41,61</sup> This structure is close to the classical one, which is included as an inset in the figure. Similar tight structures can be found for  $n = 4$  and 8, with geometries corresponding to a tetrahedron and square antiprism, respectively. Barbati *et al.*<sup>62</sup> reported structures obtained from *ab initio* calculations up to  $n = 7$  and the same structures were found for  $n = 2, 3, 4,$  and 6.

For the case of the sodium dimer clusters,  $\text{Na}_2^+(\text{H}_2)_n$ , we present in Fig. 9 the radial distributions of  $\text{H}_2$  molecules with respect to one of the sodium atoms composing the dimer ( $\text{Na}(1)$  in Fig. S3 in the ESI<sup>†</sup>). It can be seen that there are some  $\text{H}_2$

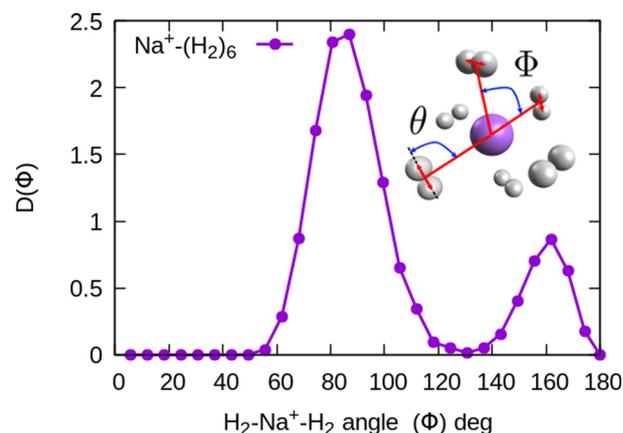


Fig. 8  $\text{Na}^+(\text{H}_2)_6$  angular distributions of  $\overline{\text{H}_2 - \text{Na}^+ - \text{H}_2}$ . The inset corresponds to the classical MC structure.



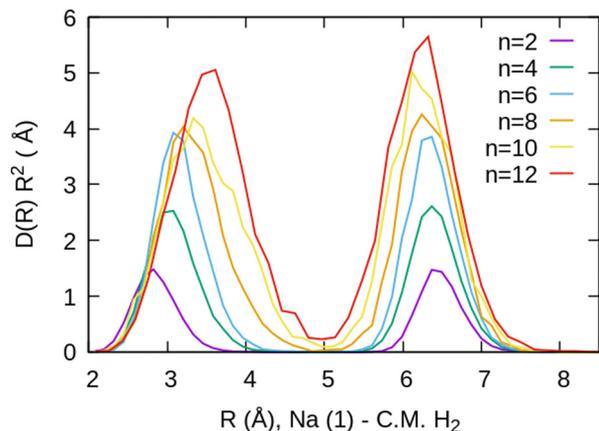


Fig. 9  $\text{Na}_2^+(\text{H}_2)_n$  radial distributions, normalized to the number of  $\text{H}_2$  molecules, for several cluster sizes, referred to the position of one of the sodium atoms  $\text{Na}(1)$  which is placed at the origin of the coordinates. The distributions are multiplied by the volume element  $R^2$  to show more clearly that there are similar numbers of monomers in the first and second peaks (around each atom of  $\text{Na}_2^+$ ). Note that the second sodium atom,  $\text{Na}(2)$ , is located at a distance of 3.71 Å.

monomers around  $\text{Na}(1)$ , leading to one peak, and at longer distances, the rest of the monomers are more directly joined to the other atom,  $\text{Na}(2)$ , leading to the second peak. The plot indicates that there is a preference for  $\text{H}_2$  to evenly cover each Na atom. This feature has been checked by integration of the distributions of Fig. 9 up to the middle of the two peaks (around 5 Å), and it was found that the number of diatomic molecules around each Na is, in general terms, half the total number of them. This is the origin of the relatively large stability of the clusters with an even number of  $\text{H}_2$  molecules observed both in the calculations as well as in the measurements of Fig. 6.

The existence of a bond in  $\text{Na}_2^+$ , leading to a more anisotropic and weaker interaction with  $\text{H}_2$  as compared with  $\text{Na}^+$ , also makes the distribution more prone to forming caps around

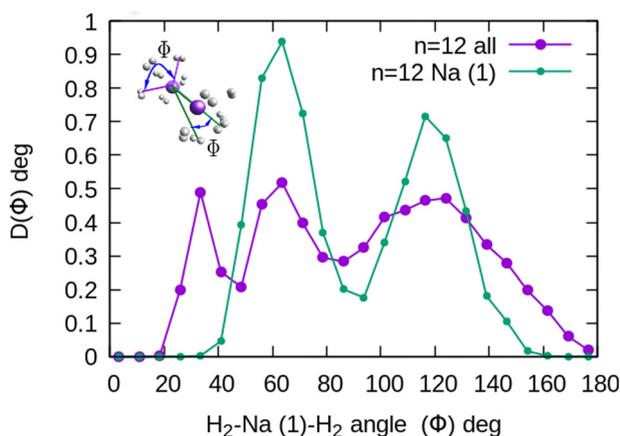


Fig. 10  $\text{Na}_2^+(\text{H}_2)_{12}$  angular distributions of  $\text{H}_2-\widehat{\text{Na}}^+-\text{H}_2$  angles, corresponding to one of the Na atoms in the dimer. The inset corresponds to the classical MC structure, indicating two possible  $\Phi$ 's angles.  $\text{Na}(1)$  is the sodium atom from which the angles are measured.

each alkaline atom, rather than a spherical distribution around a single sodium cation. This effect can be seen in Fig. 10 for  $n = 12$ , in which we plot (similarly as in Fig. 8) the distribution of angles  $\Phi$  formed between two vectors connecting one of the sodium atoms,  $\text{Na}(1)$ , and the center of mass of any two hydrogen molecules. The peak around  $\Phi = 30^\circ$  corresponds to  $\text{H}_2$  diatoms which are around the other Na atom,  $\text{Na}(2)$ . If we discard the  $\text{H}_2$  monomers surrounding that atom (equivalent to eliminating the peak on the right of Fig. 9), we get a bimodal distribution (green curve in Fig. 10 whose central angles correspond to six molecules forming the cap of an icosahedron (for comparison, see ref. 31 for the icosahedral structure found for  $\text{Cs}^+(\text{H}_2)_{12}$ ). This structure is close to the classical one, shown as an inset in Fig. 10.

## 4. Conclusions

In conclusion, this work shows an important mechanism for the future understanding of how molecular hydrogen binds to single sodium atoms. The good agreement between the experimental and theoretical data supports the idea of favored structures, where the attachment of 4, 6 and 8 hydrogen molecules is especially strong for the sodium monomer Fig. 5. The dimer complexes show agreement between theory and experiment regarding the special stability of complexes with 2, 6, 8, 10 and 12 molecules, since both Na atoms behave as quasi-independent attractors for  $\text{H}_2$  molecules, each of them showing the same number of stable molecule attachments. This symmetric hydrogen attachment to each side of the sodium dimer leads to two-step-plateaus (5,6–7,8–9,10–11,12) for ion yields, shown at the top of Fig. 6, that can also be observed in evaporation energies. Our calculations, concerning the energy difference of every possible pathway for the generation of the cluster complexes due to the experimental setup and its pick up sequence, conclusively explain the ion abundances observed. These calculations also indicate that protonation of single sodium atoms is very unlikely and that the binding energy of a hydrogen molecule is higher than the one of a single H atom, what explains the low abundance of sodium cluster ion complexes with an odd number of hydrogen atoms.

The theoretical calculations confirm and support these conclusions and explain the behavior of the monomer *versus* the sodium dimer. The present results are expected to be of relevance for organic materials containing alkali atoms, where electron transfer to the organic component leads to positively charged alkali ions that act as attractors for hydrogen molecules in novel hydrogen storage materials.<sup>6</sup>

## Data availability

The data that support the findings of this study are available from the corresponding authors upon reasonable request.

## Author contributions

S. Kollotzek, S. Tiefenthaler, and P. Scheier carried out the experiments. J. Campos-Martinez, M. Bartolomei, F. Pirani, M. I.



Hernández, T. Lázaro, E. Zunzunegui-Bru, T. González-Lezana, J. Bretón, and J. Hernández-Rojas worked on the theoretical results. O. Echt participated in the experiments and the comparison with the theoretical results.

## Conflicts of interest

We declare no conflicts of interest.

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