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# Synthesis of radiolabelled aryl azides from diazonium salts: experimental and computational results permit the identification of the preferred mechanism†

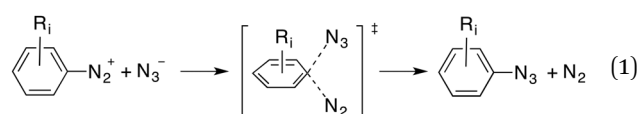
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**Experimental and computational studies on the formation of aryl azides from the corresponding diazonium salts support a stepwise mechanism via acyclic zwitterionic intermediates. The low energy barriers associated with both transition structures are compatible with very fast and efficient processes, thus making this method suitable for the chemical synthesis of radiolabelled aryl azides.**

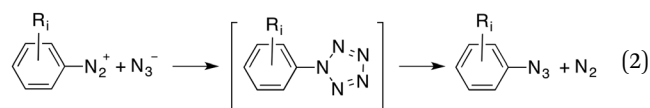
The relevance of organic azides, first synthesized by Griess in 1864,<sup>1</sup> ranges from the preparation of heterocycles, peptides<sup>2</sup> and pharmaceuticals,<sup>3</sup> to the synthesis of anilines and nitrenes.<sup>4</sup> The most prominent fields are currently Huisgen 1,3-dipolar azide-alkyne cycloadditions<sup>5</sup> and different variants of the Staudinger ligation.<sup>6</sup> Among organic azides, aryl azides have found industrial and biological application<sup>7</sup> in different fields due to their relatively high stability, and are important intermediates in organic chemistry.

Several approaches can be used for the preparation of aryl azides, including the reaction of diazonium salts with hydrazine,<sup>8</sup> *O*-benzylhydroxylamine hydrochloride<sup>9</sup> or azide ions.<sup>10</sup> Despite the latter reaction having been widely exploited for decades, its mechanism is still unclear and has been the subject of controversy.

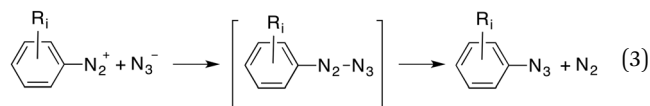
In principle, at least three possible mechanisms can be predicted for this reaction. The first one consists of an *Sn2Ar* process similar to that observed for solvolysis reactions of diazonium salts,<sup>11</sup> as indicated in eqn (1):



A second plausible mechanism involves a thermal (3+2) cycloaddition to form a 1*H*-pentazole cycloadduct<sup>12</sup> that, in turn, can yield the product *via* a second retro-(3+2) reaction:



Finally, an addition–elimination process *via* an acyclic intermediate can be also considered, according to eqn (3):



Previous studies<sup>13</sup> suggest that this latter mechanism is quite plausible. The process involves the attack of the azide on the diazonium ion with formation of aryl pentazenes and/or pentazoles, which subsequently lose nitrogen.<sup>13</sup> Whether the reaction occurs through a concerted (3+2) mechanism or takes place stepwise and the nature of the intermediate products are questions that remain unresolved. Studies performed using <sup>1</sup>H and <sup>15</sup>N-NMR spectroscopy suggest the formation of three isomeric aryl pentazenes.<sup>13</sup> One of them would lead to the formation of the aryl azide directly, while the other two would require the formation of intermediate ring structures to finally yield the aryl azide.

Nitrogen-13 (<sup>13</sup>N) is a positron emitter with a half-life of 9.97 minutes, and can be efficiently produced by proton irradiation of natural oxygen *via* the <sup>16</sup>O(p,α)<sup>13</sup>N nuclear reaction. When water is irradiated with 8–16 MeV protons, a mixture of [<sup>13</sup>N]NO<sub>3</sub><sup>−</sup>, [<sup>13</sup>N]NO<sub>2</sub><sup>−</sup>

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† Electronic supplementary information (ESI) available: Experimental procedures for the synthesis of <sup>13</sup>N-labeled phenyl azide, and identification of the labelled species using radio-HPLC and GC-MS. Energies, zero-point vibrational energies, Gibbs energy corrections and Cartesian coordinates of all the stationary points discussed in this work. Movie including the CPMD simulations. Full ref. 18. See DOI: 10.1039/c5cc01913c



and  $[^{13}\text{N}]\text{NH}_4^+$  is obtained,  $[^{13}\text{N}]\text{NO}_3^-$  being the major species (*ca.* 85% of total radioactivity).  $[^{13}\text{N}]\text{NO}_3^-$  can be quantitatively reduced to  $[^{13}\text{N}]\text{NO}_2^-$  by passing  $[^{13}\text{N}]\text{NO}_3^-$  over cadmium, and in our hands this labeling agent has proved useful for the synthesis of  $[^{13}\text{N}]\text{nitrosamines}$ ,<sup>14</sup>  $[^{13}\text{N}]\text{nitrosothiols}$ <sup>15</sup> and  $[^{13}\text{N}]\text{azo derivatives}$ .<sup>16</sup>

In continuation of our work, and with the ultimate goal of synthesizing  $^{13}\text{N}$ -labeled polysubstituted triazoles, we decided to approach the preparation of  $^{13}\text{N}$ -labeled phenyl azides by adapting a recently reported methodology,<sup>17</sup> based on the reaction of an aromatic amine with  $\text{NaNO}_2$  and hydrazine hydrate (molar ratio 1:2:5) in the presence of acetic acid. According to the authors, one equivalent of sodium nitrite reacts with the aromatic amine to yield the corresponding diazonium salt; simultaneously, the reaction of another equivalent of nitrite with hydrazine hydrate generates *in situ* the azide ion, resulting in the formation of the aryl azide. When transitioning to radioactive conditions the reaction mechanism may have an impact on the radiochemical yield. If the reaction proceeds *via* the mechanism shown in eqn (1), the radiolabelling information contained in the azide anion should be completely transferred to the corresponding aryl azide; however, if the radiolabelled diazonium salt were reacted with non-radioactive azide ion, labeled aryl azide would never be obtained. Similar reasoning can be applied to mechanisms shown in eqn (2) and (3); hence the position of the label is paramount to prevent the formation of  $[^{13}\text{N}]\text{N}_2$  with the consequent decrease in the labeling efficiency. With the aim of optimizing radiochemical yields, we envisaged a unique opportunity to further explore the mechanism of this reaction.

The synthetic process for the preparation of  $^{13}\text{N}$ -labeled aryl azides was approached using two experimental settings (Scheme 1). In the first approach, denoted as A in Scheme 1, aniline was first reacted with sodium nitrite in the presence of hydrochloric acid, to yield the non-labeled diazonium salt (1). In a different vial, hydrazine hydrate was reacted with  $[^{13}\text{N}]\text{NO}_2^-$  in the presence of acetic acid, to yield the  $^{13}\text{N}$ -labeled azide ion (Scheme 1A). Both solutions were finally mixed in a capped vial to enable the formation of  $^{13}\text{N}$ -labeled phenyl azide. In the second approach, denoted as B in Scheme 1, aniline was first reacted with  $[^{13}\text{N}]\text{NO}_2^-$  in the presence of hydrochloric acid, to yield the  $^{13}\text{N}$ -labeled diazonium salt ( $[^{13}\text{N}]\text{1}$ ). In a different vial, hydrazine hydrate was reacted with sodium nitrite in the presence of acetic acid, to yield the non-labeled azide ion (Scheme 1B). Again, both solutions were

finally mixed in a capped vial to enable the formation of  $^{13}\text{N}$ -labeled phenyl azide.

After termination of the reaction, the amount of radioactivity was measured with a dose calibrator ( $A_1$ ), the vials were flushed with nitrogen to remove radioactive gases, the amount of radioactivity was measured again ( $A_2$ ), and the reaction mixture was analyzed by HPLC using a radiometric detector in series with a UV detector. Identification of the  $^{13}\text{N}$ -labeled azide was confirmed by co-elution with the reference standard (see ESI† for further details).

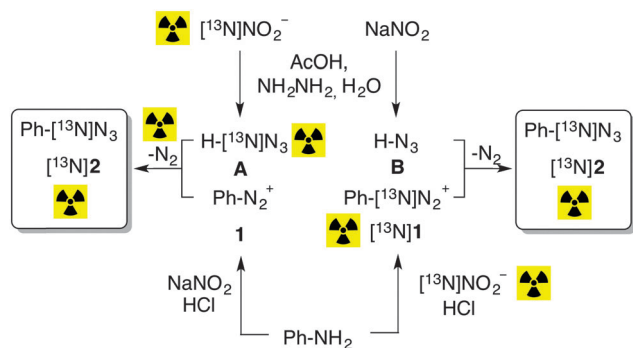
Both synthetic strategies led to the formation of  $^{13}\text{N}$ -labeled phenyl azide (2). However, the amount of radioactive gas generated during the reaction, determined as the difference between  $A_1$  and  $A_2$ , and referred to the total amount of  $^{13}\text{N}$ -labeled azide (the latter calculated as the product  $A_2 \times A_{\text{UC}}$ , where  $A_{\text{UC}}$  is the area under the peak for phenyl azide as measured in the radiometric detector and expressed as percentage with respect to all integrated peaks in the chromatogram) was  $100.3 \pm 1.7\%$  and  $4.0 \pm 1.1\%$  for strategies A and B, respectively. Analysis of the flushed gas by radio-GC-MS showed the presence of a single radioactive peak, which was identified as  $[^{13}\text{N}]\text{N}_2$ , while the amount of labeled azide obtained in 1B was twice the amount obtained in A. These results confirm that approximately half of the radioactivity is lost as  $[^{13}\text{N}]\text{N}_2$  when route A is followed, while the information of the radiolabel is almost quantitatively transferred to the azide under route B (Scheme 1).

The experimental data completely discard the reaction mechanism based on  $\text{S}_{\text{N}}2\text{Ar}$  (eqn (1)) and cleavage of the C–heteroatom bond, which would lead to a complete radioactivity loss (as  $[^{13}\text{N}]\text{N}_2$  when route B is followed). On the other hand, they strongly suggest that the formation of the intermediate ring (eqn (2)) is not taking place; in such a case,  $[^{13}\text{N}]\text{N}_2$  would be detected in a significant amount (*ca.* 100% with respect to the final amount of labelled aryl azide) when route B was used.

In view of these results, we performed DFT<sup>18</sup> calculations on the parent  $\text{PhN}_2^+(\text{1}) + \text{N}_3^- \rightarrow \text{PhN}_3(\text{2}) + \text{N}_2$  reaction in order to obtain evidence concerning the most plausible reaction mechanism and get a better understanding of the experimental data. A M06-2X<sup>19</sup> (PCM)<sup>20</sup>/def2-TZVPP<sup>21</sup> study of the reactants in aqueous solution revealed the presence of a local minimum associated with a weak complex formed denoted as RC in Fig. 1.

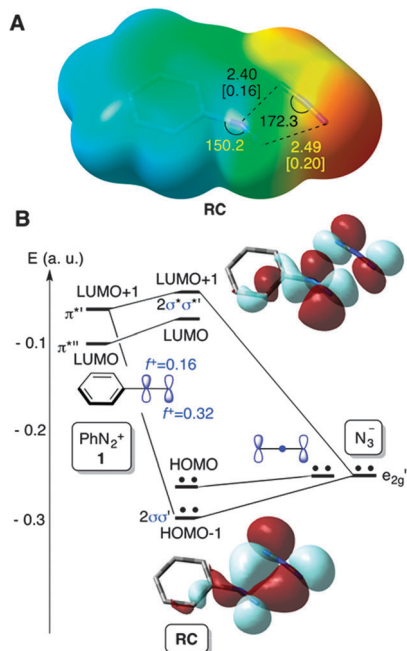
This stationary point on the potential energy surface (PES) consists of a charge transfer complex, in which both ionic reactants are in close contact, with a calculated charge transfer of 0.5 a.u. The new N–N bond distances are *ca.* 2.4–2.5 Å (Fig. 1A), the respective Wiberg bond indices<sup>22</sup> being *ca.* 0.2. This weak bonding pattern stems from a two-electron interaction between one of the  $e_{2g}''$  MOs of the azide anion and the in-plane  $\pi^*$  LUMO+1 of **1** (Fig. 1B). The occupied MOs  $\pi^{*//}$  of **1** and  $e_{1g}$  of  $\text{N}_3^-$  lead to a destabilizing four-electron interaction (not shown), thus resulting in a very weak bonding pattern between both the reactants at RC. Actually, this stationary point is not stabilized with respect to the separate reactants at 298 K (Fig. 2).

From these reactants we characterized the saddle point  $\text{TS}_{\text{SN}2}$  (Fig. 2) with the computed activation energy of *ca.* 27 kcal mol<sup>−1</sup>. The geometric features of this transition structure are quite similar to those obtained for solvolysis reactions of aromatic diazonium salts.<sup>11</sup> In our case, however, there is an additional



**Scheme 1** The two alternative strategies A and B followed to synthesize  $^{13}\text{N}$ -labeled phenyl azide ( $[^{13}\text{N}]\text{2}$ ).

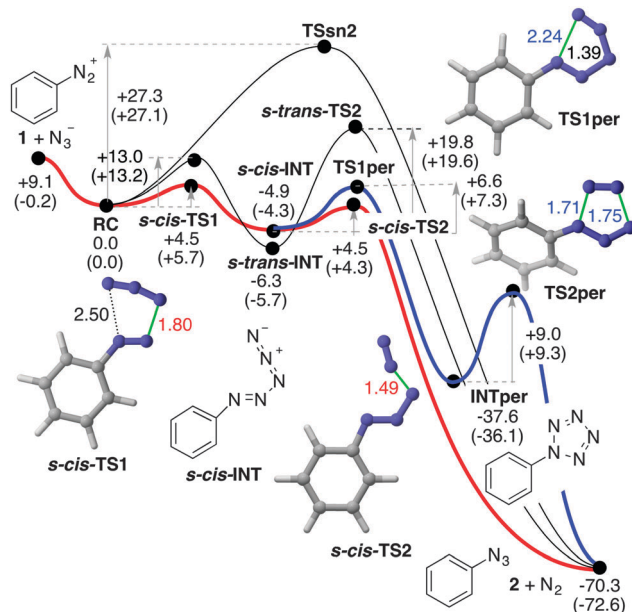




**Fig. 1** (A) Electrostatic potential and chief geometric features of complex **RC** associated with the interaction between azide anion and diazonium cation **1**. Bond distances and angles are given in Å and deg., respectively. Numbers in square brackets are the corresponding bond indices. (B) Selected Kohn–Sham molecular orbitals of **RC**. Descriptors  $f^*$  on the nitrogen atoms correspond to the local electrophilic Fukui indices.

interaction between the diazonium and azide moieties (Fig. 1). This remarkable barrier and our experimental results permit us to discard the  $S_N2Ar$  mechanism for this particular reaction.

The frontier MOs of the reactants at **RC** are also indicated in Fig. 1B and correspond to the in-plane MOs  $e_{2g}''$  and  $\pi^{*''}$ . These computational data are compatible with a high electrophilicity associated with the terminal nitrogen of the diazonium moiety of **1**, with a local electrophilic Fukui index<sup>23</sup>  $f^*$  of 0.32 a.u. (Fig. 1B). The interaction between the terminal nitrogen atoms of both reactants according to the mechanism reported in eqn (3) leads to saddle points **s-cis-TS1** and **s-trans-TS1** (Fig. 2). The former transition structure was calculated to be *ca.* 7 kcal mol<sup>-1</sup> less energetic than the latter (Fig. 2). The chief geometric features of **s-cis-TS1** closely resemble those expected for an asynchronous transition structure associated with a (3+2) cycloaddition.<sup>24</sup> However, all our attempts to connect **s-cis-TS1** directly with 2-phenyl-2H-pentazole **INTper** were unfruitful. Instead, this saddle point led to the zwitterionic intermediate **s-cis-INT**, from which we located a transition structure **TS1per**. This latter saddle point led to 2-phenyl-2H-pentazole **INTper** (Fig. 2), associated with the hypothetical (3+2) cycloaddition. From this local minimum we found the saddle point **TS2per** leading to phenyl azide **2**. Although this latter transition structure associated with a retro-(3+2) cycloaddition is compatible with the reaction scheme gathered in eqn (2), it is important to note that **INTper** does not stem from **RC** but from **s-cis-INT**, which constitutes the key intermediate of the less energetic reaction profiles. In addition, our calculations indicate that the formation of **INTper** occurs with an activation barrier



**Fig. 2** M06-2X(PCM)/def2-TZVPP reaction profiles associated with the reaction between diazonium cation **1** and azide anion to yield phenyl azide **2** and dinitrogen. Numbers close to reactants, intermediates and products indicate the relative energies in kcal mol<sup>-1</sup>. Numbers close to the arrows indicate the respective activation energies, in kcal mol<sup>-1</sup>. Numbers in parentheses indicate the respective Gibbs energies, computed at 298 K, in kcal mol<sup>-1</sup>. The lowest energy reaction paths are highlighted in red and blue.

that is *ca.* 2 kcal mol<sup>-1</sup> higher than that associated with the formation of phenyl azide **2**.

Intrinsic Reaction Coordinate<sup>25</sup> (IRC) scans from both **s-cis**- and **s-trans-TS1** led to the corresponding zwitterionic intermediates **s-cis**- and **s-trans-INT** (see ESI†). The relative stabilities of these polar intermediates were found to be the opposite ones with respect to the corresponding transition structures. Therefore, the preferred route to yield azidobenzene **2** and dinitrogen occurs *via* **s-cis-TS2** in which the cleavage of the  $\text{PhN}_2(-)\text{-N}_2(+)$  delocalized bond is produced (Fig. 2). This low barrier is associated with the formation of dinitrogen and azidobenzene **2**, two neutral stabilized species.

In order to confirm the preference for the mechanism outlined in eqn (3) we carried out Car–Parrinello<sup>26</sup> Molecular Dynamics (CPMD)<sup>27</sup> within the DFT framework, using the BLYP gradient-corrected functional<sup>28</sup> and ultrasoft Vanderbilt pseudopotentials.<sup>29</sup> These simulations were carried out at different temperatures with a 1 fs time step for the integration of the equations of motion. Our CPMD results for the entire  $\text{PhN}_2^+(1) + \text{N}_3^- \rightarrow \text{PhN}_3(2) + \text{N}_2$  reaction confirmed that the reactants at internuclear distances similar to those found in complex **RC** form **s-cis-INT** zwitterion in less than 100 fs at 100 K (Fig. 3). This intermediate is stable at this temperature within a time span of at least 1.2 ns. When the system was heated at *ca.* 300 K, the system reached **s-cis-TS2** in *ca.* 300 fs to yield the reaction products,<sup>30</sup> thus confirming the stepwise nature of the reaction *via* open intermediates of type **INT**. These results are in agreement with our experimental results and provide a rationale for the loss of radioactivity observed when radiolabelled azide anion was used following method A (Scheme 1).





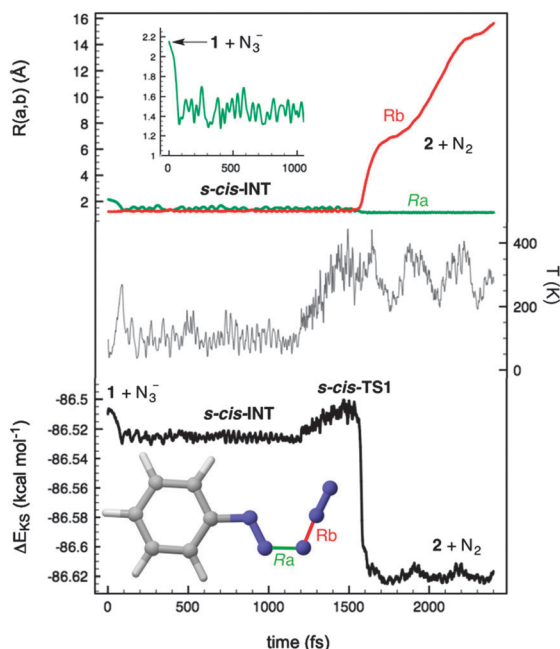


Fig. 3 Car-Parrinello Molecular Dynamics (CPMD) plots of the reaction between the diazonium cation **1** and the azide anion to yield phenyl azide **2** and dinitro.

Kinetic simulations carried out using reaction paths highlighted in red and blue in Fig. 2 indicate that ca. 99% of **2** stems from *s-cis-TS2*, whereas ca. 1% of the reaction product is formed *via INTper* (see the ESI† for additional details). These results are in good agreement with the release of [<sup>13</sup>N]N<sub>2</sub> obtained in our experimental studies following the synthetic strategy shown in Scheme 1, method A.

In conclusion, we have demonstrated using experimental and computational data that the formation of aryl azides from the corresponding diazonium salts occurs *via* a stepwise mechanism *via* acyclic zwitterionic intermediates. The use of the short-lived positron emitter nitrogen-13 for the elucidation of reaction mechanisms is unprecedented; hence, the work reported here can inspire future applications of this radio-nuclide beyond the preparation of radiolabelled compounds for imaging studies.

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- See movie SM1 in the ESI†.

