



Cite this: *React. Chem. Eng.*, 2019,  
4, 1331

## Mesoscale triphasic flow reactors for metal catalyzed gas–liquid reactions†

Dogancan Karan and Saif A. Khan  \*

In this study, we demonstrate a mesoscale triphasic (gas–liquid–liquid) reactor for fast, transition metal catalyzed gas–liquid reactions, which is capable of delivering kg per day productivity at the single channel level. More generally, our study addresses the limits of scale up of multiphase flow reactors beyond the micro- and milli-scale. We first conduct a rigorous hydrodynamic study that allows us to explore the channel dimension and reactor operating conditions within which a stable and regular flow regime can be maintained. We particularly focus on the presence of the organic phase as a thin film around the train of dispersed phase segments, since this plays a key role in process intensification and flow stability. A tube diameter of 3.2 mm is found to be the upper limit for the mesoscale channel, beyond which thin films cease to exist due to combination of gravitational drainage and dewetting. Next, we present experimental observations of a model reaction – the hydrogenation of 1-hexene in the presence of a rhodium nanoparticle catalyst (RhNP) to evaluate the reactor performance and highlight the key differences between micro/milli-scale and mesoscale operation. Finally, we develop and discuss a mathematical model that accurately captures the key experimental observations. Based on the insight we gain from our model, we demonstrate further scale up of the reactor to achieve the performance of  $>100\times$  equivalent milliscale flow reactors with a single mesoscale channel under ambient conditions.

Received 7th April 2019,  
Accepted 3rd June 2019

DOI: 10.1039/c9re00150f

[rsc.li/reaction-engineering](http://rsc.li/reaction-engineering)

### 1. Introduction

Drug substances and active pharmaceutical ingredients (APIs) differ significantly in molecular complexity when compared to commodity chemicals, and their manufacture generally requires a cascade of synthetic steps, in which transition metal catalyzed gas–liquid reactions such as hydrogenation, oxidation, and carbonylation play a common role.<sup>1</sup> In the pharmaceutical industry, these latter reactions are conventionally carried out in stirred batch tanks in which a gaseous reactant is pressurized on the top of the liquid phase, which contains solvent, substrates, and catalyst particles. However, the performance of such reactors is almost always limited by poor heat and mass transfer rate due to small interfacial areas and inefficient contacting of different fluid phases. Continuous flow microreactors offer remarkably accelerated heat and mass transport rate due to small characteristic dimensions which provides several orders of magnitude higher interfacial area compared to conventional macroscale gas–liquid contactors.<sup>2</sup> Furthermore, the small characteristic dimension results in surface tension-dominated flow, which enables regular and

stable multiphase flow regimes, in turn allowing fine control over reaction conditions and transport properties. In view of the advantages that small-scale systems offer, different microreactor platforms and configurations<sup>3–8</sup> have been developed to carry out various gas–liquid transformations<sup>6,9–12</sup> over the past decade.

However, despite the numerous advantages, operation in sub-millimeter channels severely constrains the productivity of such reactors, posing major challenges in their application for larger scale production.<sup>13</sup> Unlike conventional reactors, increasing the throughput of the microreactors is not as straightforward as increasing reactor dimension and/or volumetric flow rate of the reactants, especially for the case of multiphase reactions, since heat and mass transport performance and hydrodynamic behavior of the reactor are quite sensitive to characteristic dimension of the system as well as volume fraction of individual fluid phases.<sup>14</sup> High throughput production in microreactors can be realized by numbering-up (parallelization or scaling-out), in which multiple individual channels are operated simultaneously.<sup>15–21</sup> By doing so, the same hydrodynamic conditions in each elementary channel can be maintained while achieving higher production rates.

There are several engineering challenges which hinder exploitation of scaled-out microreactor networks. The key engineering challenge is to provide equal fluid distribution to

Department of Chemical and Biomolecular Engineering, National University of Singapore, 4 Engineering Drive 4, E5-02-28, 117576 Singapore. E-mail: [safikhhan@nus.edu.sg](mailto:safikhhan@nus.edu.sg)  
† Electronic supplementary information (ESI) available. See DOI: [10.1039/c9re00150f](https://doi.org/10.1039/c9re00150f)

different channels, in that good global reactor performance can only be realized by excellent consistency of reaction conditions among elementary reactor channels.<sup>22–24</sup> This problem has been well addressed in gas–liquid and liquid–liquid segmented flow configurations by using high-pressure drop zones across a fluid distributor which eliminate the variation in downstream pressure drop, and equal fluid distribution can be achieved.<sup>25–27</sup> However, minute differences in pressure drops can result in maldistribution or even gas–liquid channeling which severely affects the overall consistency of the reactor network. Such a crucial engineering challenge requires sophisticated monitoring and control systems, which further increases the complexity of the reactor network.<sup>22</sup> More importantly, hundreds or even thousands of parallel microchannels may be required to achieve commercial-scale production, which makes increasing the throughput solely by numbering-up quite impractical. Therefore, with all the existing challenges, we contend that scaling-up by increasing the characteristic channel dimension is still a viable route to enable large-scale applications of such reactors. Indeed, the best approach would be to find an intermediate mesoscale channel size which provides sufficiently high heat and mass transport rate along with higher production rate which allows to further increase the throughput by means of reasonable number of parallel reactor units to minimize the overall complexity of the reactor system.

Our research group has previously demonstrated a gas–liquid–liquid triphasic millireactor<sup>28,29</sup> for fast, metal-catalyzed reactions where catalyst was immobilized in a separate liquid phase for facile recovery and recycle. More recently, we have demonstrated design and operation of 8-fold parallelized triphasic millireactor network<sup>21</sup> with online catalyst recovery and recycle. The reactor setup employs resistance-based fluid distributors and capacitance-based hydraulic dampers to maintain consistency between elementary channels. In this study, we report the design and operation of a mesoscale reactor to push the limits of the triphasic millireactor setup for large-scale applications. A mesoscale channel retains the basic physics of operation of small-scale systems – accelerated transport rate, regular and consistent flow regime, yet provides significantly more throughput due to its unique intermediate size. It is worthwhile to note that increasing throughput *via* scaling-up is achieved at the expense of lower interfacial area and hence lower mass transport rate. Under comparable conditions, smaller channels provide better mass transport performance. This paper is organized three main parts. We first present a rigorous hydrodynamic study that allows us to explore the channel dimension and reactor operating conditions within which a stable and regular flow regime can be maintained. Next, we present experimental observations of a model reaction – the hydrogenation of 1-hexene in the presence of a rhodium nanoparticle catalyst (RhNP) to evaluate the reactor performance and highlight the key differences between micro/milli-scale and mesoscale operation. Finally, we develop and discuss a mathematical model that

accurately captures the key experimental observations. Based on the insight we gain from our model, we demonstrate further scale up of the reactor to achieve the performance of  $>100\times$  equivalent milliscale flow reactors with a single mesoscale channel under ambient conditions.

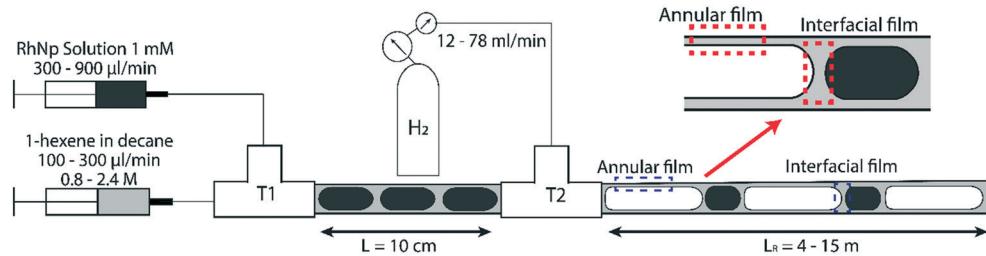
## 2. Materials and methods

### 2.1. Rhodium nanoparticle synthesis

Rhodium nanoparticles were synthesized by the ethanol-reduction method.<sup>30</sup> First, a 5 mM precursor solution was prepared with 66.8 mg of  $\text{RhCl}_3\cdot\text{xH}_2\text{O}$  (Alfa Aesar Rh 38.5–45.5%), 0.555 g of polyvinylpyrrolidone (PVP, Alfa Aesar, molecular weight: 40 000 g mol<sup>-1</sup>) as stabilizer, 30 mL of absolute ethanol (Fischer Scientific, 99.5%) as reducing agent, and 20 mL of ultrapure water (Milli-Q, 18.2 MΩ cm at 25 °C). The solution was refluxed at 115 °C for 1 hour, with a stirrer set at 575 RPM in the reflux flask. Thereafter, all solvent was evaporated in a rotary evaporator (Buchi R-210 Rotavapor) at 45 °C under vacuum to obtain a black residue at bottom of the volumetric flask. Finally, the black residue was dispersed into 50 mL ultrapure water to obtain a ‘5 mM’ rhodium nanoparticle stock solution, which was subsequently stored at 5 °C. Since PVP is a soluble polymer in polar solvents, rhodium nanoparticles can be suspended in water as a colloidally-stable solution. The stock solution was diluted 5× to 1 mM prior to hydrogenation experiments. The quality of nanoparticles was checked by TEM (JEOL 2010, accelerating voltage 200 kV). The average particle size was found to be 3.8 ± 0.8 nm (see ESI† Fig. S1 for the TEM picture of rhodium nanoparticles).

### 2.2. Triphasic flow visualization

For flow visualization, two 2 m long polytetrafluoroethylene (PTFE) reactor tubes of 3.2 mm and 4 mm ID respectively were chosen, since PTFE facilitates the wetting of reactor wall by the organic phase. Flow visualization was conducted under non-reactive conditions. Due to the large excess of gas supplied during the reaction, the volume change of gas bubbles is negligible, as will be discussed below; therefore, using non-reactive conditions is suitable for flow visualization.<sup>29</sup> A liquid–liquid segmented flow was formed at the first T junction (Swagelok, 3 mm ID) by introducing blue food dye solution from one arm and decane (ReagentPlus, Sigma-Aldrich, ≥99%) from the other arm *via* two syringe pumps (Harvard Apparatus PhD 2000, Programmable) at different volumetric flow rates. Blue food dye was used to distinguish the aqueous phase under the camera. Nitrogen gas was introduced from the second T-junction (Swagelok, 3 mm ID) at atmospheric pressure to form gas–liquid–liquid segmented flow at different volumetric flow rates. 20 cm long high-resistance polyether ether ketone (PEEK) tubes of 100 μm ID were used to fine tune the volumetric gas flow rate prior to feeding into the reactor channel. A schematic representation of the experimental setup is shown in Fig. 1. A microscope system, which was placed 30 cm away from the second T-junction was used



**Fig. 1** Schematic representation of the triphasic gas–liquid–liquid segmented flow experimental setup. The interfacial film is the thin organic segment separating the bubble and aqueous droplet caps, whereas the annular film is the organic lubricating film surrounding all gas bubbles.

to observe and record the flow pattern in the reactor channel; the system was composed of a 200-fps high-speed camera (Basler pia640-210gm) fitted to an optical microscope (Leica MZ16) and a light source at the bottom of the reactor channel. Bubble flow speeds, generation frequencies/periods and residence times were determined from high-speed videos recorded at different frame rates; statistics from at least 100 bubbles were used for each experimental condition. It is worthwhile to highlight that the different bubble residence times, lengths of the gas bubbles and hence the volumetric flow rate of the gas phase are adjusted by changing the gas pressure from the tank. Volumetric flow rate of gas phase used in our experiments ranged between  $12 \text{ mL min}^{-1}$  to  $146 \text{ mL min}^{-1}$ , while the total liquid flow rates used ranged between 0.4 to  $4.8 \text{ mL min}^{-1}$ . Since the volumetric flow rate of the gas phase is several orders of magnitude higher than that of liquid phase, changing the volumetric flow rate of the liquid phase (organic or aqueous) does not appreciably affect the bubble residence time. In addition, we estimated the change in the bubble length due to hydrogen consumption under different reactive flow conditions to be in the range of 5–15%, highlighting the fact that the volumetric flow rate of gas does not appreciably change as it flows through the reactor.

### 2.3. Hydrogenation in the mesoreactor

The experimental system described above was set up for 3.2 mm ID PTFE tube for various experimental conditions except that nitrogen gas was replaced with hydrogen gas and blue food dye solution was replaced with rhodium nanoparticle solution to provide the reactive conditions. Before the reaction was started, the reactor was primed with organic substrate mixture for 15 minutes with a flow rate of  $0.3\text{--}0.9 \text{ mL min}^{-1}$  to facilitate wetting and shorten the time to reach steady state. In order to prevent liquid back flowing to the gas line,  $12 \text{ mL min}^{-1}$  hydrogen gas was fed to the reactor along with organic phase during the start-up period. During the shut-down, ethanol and acetone were introduced to reactor channel to remove any residual catalyst and substrate mixture for another 15 minutes.  $100 \mu\text{L}$  reactor effluent was collected in vials and diluted with  $1200 \mu\text{L}$  diethyl ether (Fischer Scientific  $\geq 99\%$ ) and analyzed by gas chromatography (Shimadzu 2010 Plus). All GC measurements were conducted

off-line. Three samples were collected for each data point. All experiments were performed at atmospheric pressure and room temperature and were conducted in duplicate. Experimental runs were carried out on different days with freshly prepared rhodium nanoparticle catalyst (RhNP) solution to calculate the error bars.

### 2.4. Design and testing of hydraulic dampers for scaled-up synthesis

For the scaled-up synthesis, syringe pumps were replaced with peristaltic pumps, and hydraulic dampers were introduced into the fluid delivery lines before they joined the reactor. Hydraulic dampers were used to eliminate the pressure fluctuations introduced by peristaltic pumps to sustain the robust multiphase flow regime. Two different hydraulic dampers were designed for organic and aqueous fluid streams in accordance with desired flow rates. The design criteria were obtained from a recent study by Yap *et al.*<sup>21</sup> For the aqueous fluid stream, a 12 cm long #25 silicone tube (7.94 mm OD, Masterflex) was sandwiched between two 10 cm long 228  $\mu\text{m}$  ID polyether ether ketone (PEEK) tubes. For the organic fluid stream, a 12 cm #25 Viton tube (6.35 mm OD, Cole Parmer) was sandwiched between two 11 cm long 152  $\mu\text{m}$  ID polyether ether ketone (PEEK) tubes. The reliability of the dampers was tested by a liquid flowmeter (Sensirion, SLQ-QT500), with peristaltic pumps (Leadfluid BT-100S), and measuring the volume of different liquid samples. The deviation in the flow rate was found to be  $<2\%$  for both streams.

## 3. Results and discussion

### 3.1. Mesoscale flow systems – defining the limits of scale-up

The first question we address in this study is that of scale-up; specifically, we ask – how much can the flow channel be enlarged beyond the ‘micro’ ( $\sim 0.01\text{--}0.1 \text{ mm}$ ) and ‘milli’ ( $\sim 1 \text{ mm}$ ) scale before the advantage of highly regular flow patterns is lost? In multiphase flows (gas–liquid, liquid–liquid, *etc.*) through micro and milli-scale channels, gravitational and inertial forces are negligible, whereas viscous and interfacial forces are dominant; this situation is reflected by the typically low ( $<0.01$ ) Capillary and Bond numbers in such channels.<sup>14</sup> This leads to extremely regular flow regimes, such as the segmented/Taylor flow regime, which has been

well studied and applied in flow chemistry over the past decade.<sup>6,9,10,31</sup>

However, as the characteristic dimension of the channel increases, the balance between these forces alters; specifically, gravitational forces start becoming comparable to interfacial forces. An estimate of a crossover dimension may be obtained by considering the Bond number (Bo), which is the ratio of hydrostatic pressure to Laplace pressure, as shown below:<sup>32</sup>

$$Bo = \frac{\Delta \rho g L}{\gamma/L} = \frac{\text{Hydrostatic Pressure}}{\text{Laplace pressure}} \quad (1)$$

Equating the Bond number to unity yields a length scale  $L$  of  $\sim 3$  mm for an air-water system. Therefore, for all subsequent studies highlighted in this paper, we use two channel diameters in this size range (3.2 mm and 4 mm respectively) to illustrate important phenomena at the crossover of scales at which gravitational (and inertial) effects cannot be ignored in a triphasic gas–liquid–liquid flow. Further, we define a baseline for robust and ‘regular’ flow as being comprised of a perfectly regular pattern of alternating gas bubbles and aqueous drops, all encapsulated by a thin film of the organic liquid, as schematically depicted in Fig. 1, and reported in previous work from our group.<sup>29,33</sup>

Experimental stereomicroscopic images of gas–liquid–liquid flow in the two different channel sizes at different bubble flow speeds are shown in Fig. 2 and 3, respectively. In both channels, well-defined aqueous drop/plugs surrounded by organic liquid and located between gas bubbles were observed at flow speeds of  $0.005\text{--}0.36\text{ m s}^{-1}$ . The first phenomenon of note is the state of the organic films, which will have crucial implications on reactor performance, as will be discussed later in the paper. In the 4 mm ID channel, dewetting and breakage of the organic film surrounding the gas bubbles was observed at *all* flow speeds (Fig. 2a–d; also see movie M1 in the ESI†) whereas the same phenomenon was observed at only *low* flow speeds ( $0.005\text{--}0.01\text{ m s}^{-1}$ ) in the 3.2 mm ID channel (Fig. 3a and b; also see movie M2 in the ESI†). Breakage and dewetting of the organic film at high flow speeds is an important indicator of the crossover from a surface tension-dominated flow regime to a gravity-dominated one in 4 mm channel. For a detailed discussion and explanation of the physics of film breakage, we refer the interested reader to section 2 of the ESI† and its associated references. The second phenomenon of note is the effect of flow velocity beyond the range illustrated in Fig. 2 and 3. As the velocity was increased further beyond this range, we observed increasing instances of droplet rupture/breakup and unstable flows, as shown in Fig. 4 (also see movie M3 in the ESI†). The third phenomenon of note is the flattened shape of the gas–organic and organic–aqueous interfaces (Fig. 3c). Similar observations have been previously reported in studies of gas–liquid–liquid segmented flow in circular<sup>34</sup> and square geometries.<sup>33</sup> This arises from the difference in translational speeds between aqueous drops and gas bubbles. Therefore, the interfacial organic film between the aqueous drops and gas bubbles rapidly drains out and redistributes as an annular

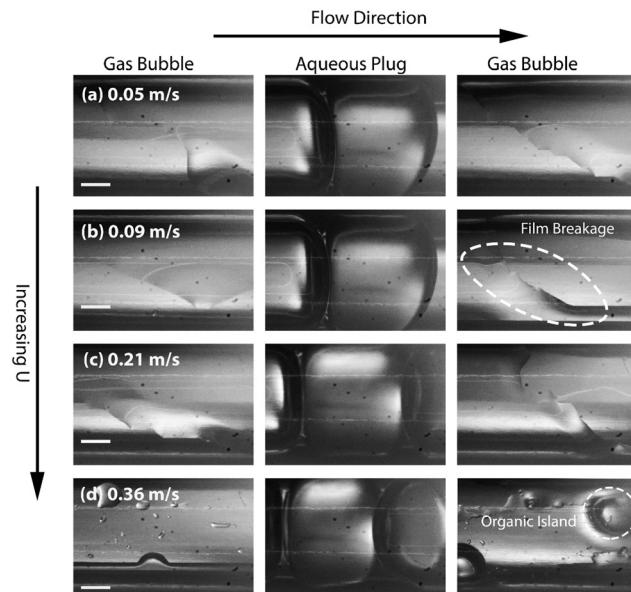
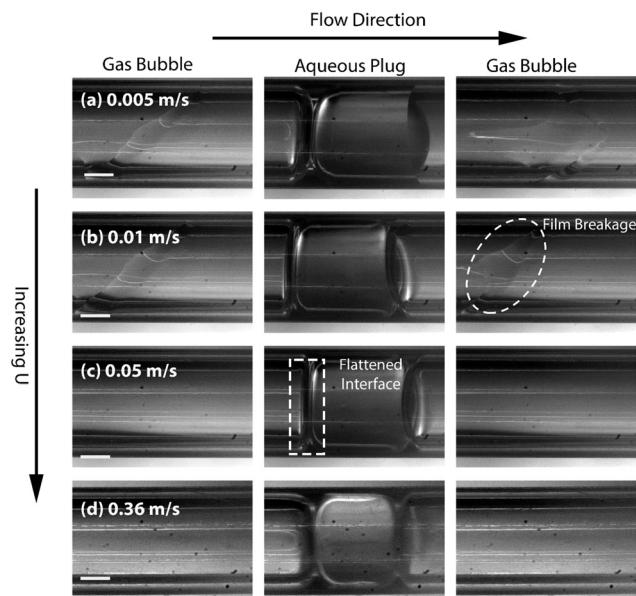


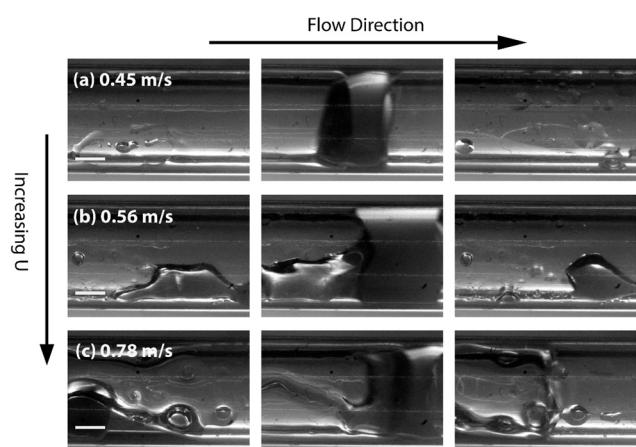
Fig. 2 (a)–(d) High-speed stereomicroscope images of gas–liquid–liquid segmented flow at different flow velocities in 2 m long 4 mm ID PTFE channel highlighting the breakage of the organic film around the gas bubbles.  $Bo_{L-L} = 0.9$ ,  $Bo_{G-L} = 4.8$ , where subscripts L–L and G–L represent organic–aqueous interface and organic–gas interface, respectively. The values of  $\gamma_{L-L} = 0.0512\text{ N m}^{-1}$ ,  $\gamma_{G-L} = 0.0239\text{ N m}^{-1}$ , and  $\Delta\rho = 730\text{ kg m}^{-3}$  were used to calculate the Bond numbers. An example of film breakage due to gravity is shown a dashed circle in Fig. 2b and an example of organic island deposited on the reactor wall is shown a dashed circle in Fig. 2d.  $Q_{\text{Org}} = 0.1\text{ mL min}^{-1}$ ,  $Q_{\text{Aq}} = 0.3\text{ mL min}^{-1}$ ,  $Q_{\text{Gas}} = 19\text{ mL min}^{-1}$ ,  $33\text{ mL min}^{-1}$ ,  $70\text{ mL min}^{-1}$ ,  $121\text{ mL min}^{-1}$  respectively. Channel walls cannot be seen in the picture due to magnification. All scale bars represent 1 mm.

film around the gas bubbles. As the film is squeezed out, a lubrication pressure is built up which is high enough to invert the curvature of the droplet/bubble caps and flattens the gas–aqueous fluid interface as highlighted in Fig. 3c (also see ESI† Fig. S2). Nevertheless, the interfacial film does not drain out completely. The lubrication pressure prevents the film from draining further and it reaches a constant thickness,<sup>35,36</sup> which has important implications on reactor performance, as we will discuss below. We can reasonably hypothesize that the thickness of the *interfacial* film between the aqueous drop and gas bubble (see Fig. 1) does not depend strongly on the volumetric flow rate of the organic phase; instead, increasing the organic flow rate will result in thicker *annular* films surrounding the gas bubbles due to fluid redistribution.

Finally, in the light of the collective observations from Fig. 2–4 and the discussion above, we limited further investigations on reactive flows to the 3.2 mm ID tube and flow velocities in the range of  $0.05\text{--}0.365\text{ m s}^{-1}$  at which breakage of the organic film and droplet breakups are absent (see ESI† section 3 and movie M4). The presence of the organic films around the gas bubbles improves the multiphase flow stability by eliminating start-stop dynamics<sup>29,37</sup> and enhances the mass transport performance of the reactor, as we will discuss in detail below.



**Fig. 3** (a)–(d) High-speed stereomicroscope images of gas-liquid-liquid segmented flow at different flow velocities in 2 m long 3.2 mm ID PTFE channel highlighting situation of the organic film around the gas bubbles and the shape of the aqueous droplet/gas bubble meniscus.  $Bo_{L-L} = 0.5$ ,  $Bo_{G-L} = 3$ . An example of dewetting of the organic liquid is shown a dashed circle in Fig. 3b and an example of flattened gas-aqueous interface is shown a dashed rectangle in Fig. 3c.  $Q_{Org} = 0.1 \text{ mL min}^{-1}$ ,  $Q_{Aq} = 0.3 \text{ mL min}^{-1}$ ,  $Q_{Gas} = 1.2 \text{ mL min}^{-1}$ ,  $3 \text{ mL min}^{-1}$ ,  $12 \text{ mL min}^{-1}$ ,  $80 \text{ mL min}^{-1}$  respectively. All scale bars represent 1 mm.



**Fig. 4** (a)–(c) High-speed stereomicroscope images at higher flow velocities in 2 m long 3.2 mm ID PTFE channel, highlighting the extent of droplet breakup with increasing flow speed.  $Q_{Org} = 0.1 \text{ mL min}^{-1}$ ,  $Q_{Aq} = 0.3 \text{ mL min}^{-1}$ ,  $Q_{Gas} = 115 \text{ mL min}^{-1}$ ,  $120 \text{ mL min}^{-1}$  and  $146 \text{ mL min}^{-1}$  respectively. All scale bars represent 1 mm.

### 3.2. Rhodium nanoparticle catalyzed flow hydrogenation of 1-hexene

In this section, we use the rhodium nanoparticle (RhNP)-catalyzed hydrogenation of 1-hexene as a model reaction (see Fig. 5) to summarize key features of observed reactor behavior, which we then explain in the subsequent section. Collectively, the experimental observations reported in Fig. 6 and

subsequent explanations underscore the important differences in moving from micro- and milli-scale systems of past studies<sup>29</sup> to the larger ‘meso’ scale systems of this study.

Fig. 6a is a plot of substrate conversion *versus* bubble residence time and examines the effect of substrate (1-hexene) starting concentration for a fixed reactor length ( $L_R$ ) of 15 m. Residence time was calculated as reactor length  $L_R$  divided by flow speed  $U$  of the gas bubbles (as measured from recorded high-speed flow videos). We make two observations from this plot. Firstly, conversion monotonically increases with residence time as expected. Secondly, and more surprisingly, the curves at the two higher starting substrate concentrations (1.6 M and 2.4 M) show markedly different (zero-order) behavior as compared to the first order behavior at lower concentration (0.8 M). Also, nearly complete conversion is obtained within a residence time of  $\sim$  5 min for the 0.8 M case.

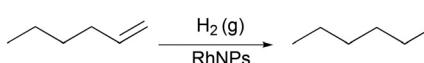
Fig. 6b is also a plot of substrate conversion *versus* bubble residence time and illustrates the effect of the reactor length, which was varied between 4.5 to 15 meters, under otherwise identical conditions. Once again, a transition from zero to first order behavior was observed with increasing reactor length. Equally interesting is the observation that the progressively *smaller* conversions were observed with decreasing reactor length, at the *same* residence times. Before we dive into the full explanation for this interesting behavior in the following section below, we note that longer reactors require higher flow speeds for the same residence time as shorter reactors, and flow speeds mediate mass transfer rates in the system. In our study, as already mentioned above, these flow speeds were adjusted by varying gas delivery rate into the system through a pressure regulator.

Finally, Fig. 6c summarizes the effect of total volumetric liquid flow rate ( $Q_T = Q_{Org} + Q_{Aq}$ ) on substrate conversion as a function of bubble residence time. Three different values of  $Q_T$  were studied, from  $0.4 \text{ mL min}^{-1}$  to  $1.2 \text{ mL min}^{-1}$ , while maintaining a constant organic to aqueous flow ratio of 1:3. Interestingly, at the same residence time, the observed conversion fell with increasing liquid flow rate  $Q_T$ , and no zero-order behavior was observed at all. For a further discussion of additional notable observations about bubble sizes in these experiments, we refer the reader to section 4 of the ESI.<sup>†</sup>

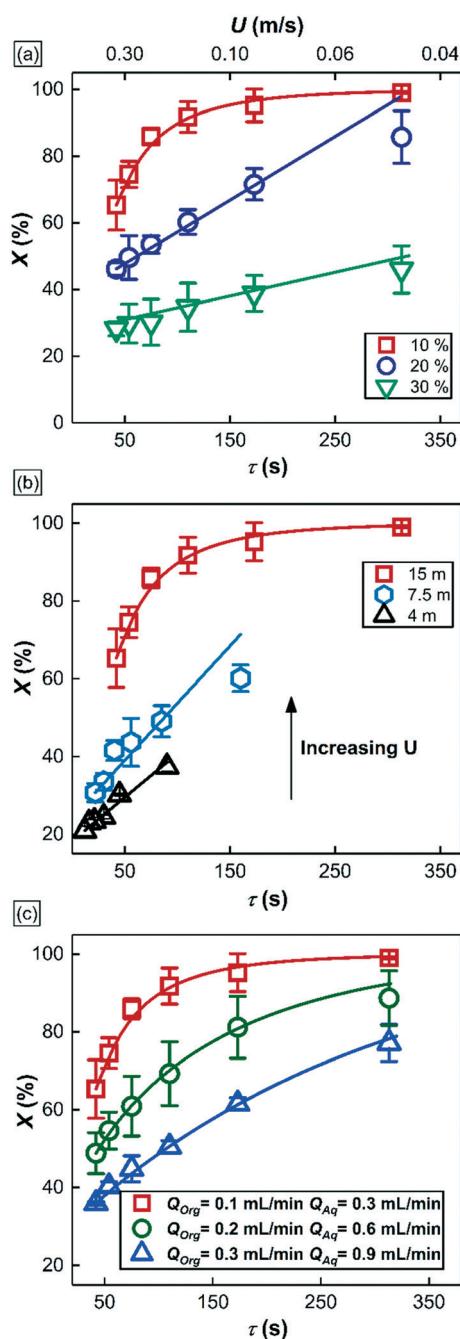
In the section 3.3, we develop a detailed description of reactor behavior in the form of a mathematical model that captures and unifies all the above disparate observations, ultimately enabling design of a scaled-up version of the reactor described in section 3.4.

### 3.3. Understanding mesoscale multiphase reactor behavior

Understanding the various aspects of reactor behavior shown in Fig. 6 requires us to start with a *local* picture of molecular



**Fig. 5** Reaction scheme for the hydrogenation of 1-hexene over RhNP catalyst.



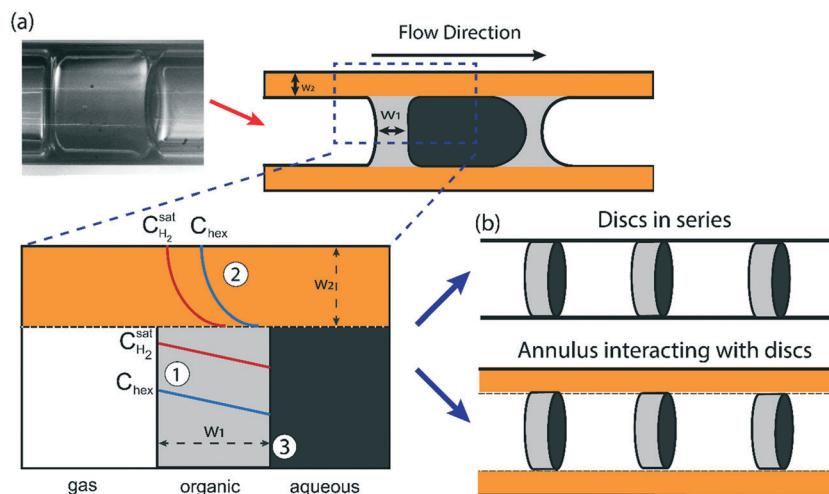
**Fig. 6** 1-Hexene conversion ( $X$ ) versus bubble residence time ( $\tau = L_R/U$ ) at various operational conditions. 1-Hexene conversion was calculated as  $X = (C_{\text{hex},0} - C_{\text{hex}})/C_{\text{hex},0}$  where,  $C_{\text{hex},0}$  is the initial 1-hexene concentration and  $C_{\text{hex}}$  is the concentration of 1-hexene in the reactor effluent at different bubble residence times, respectively. (a) The effect of starting 1-hexene concentration.  $C_{\text{hex},0} = 0.8 \text{ M}$  (10% v/v),  $1.6 \text{ M}$  (20% v/v), and  $2.4 \text{ M}$  (30% v/v).  $Q_{\text{Org}} = 0.1 \text{ mL min}^{-1}$ ,  $Q_{\text{Aq}} = 0.3 \text{ mL min}^{-1}$ ,  $L_R = 15 \text{ m}$ . (b) The effect of the reactor length.  $C_{\text{hex},0} = 0.8 \text{ M}$  (10% v/v),  $Q_{\text{Org}} = 0.1 \text{ mL min}^{-1}$ ,  $Q_{\text{Aq}} = 0.3 \text{ mL min}^{-1}$ . (c) The effect of total liquid flow rate  $Q_T$  at constant  $Q_{\text{Org}}:Q_{\text{Aq}}$  ratio of 1:3.  $C_{\text{hex},0} = 0.8 \text{ M}$  (10% v/v). Red:  $Q_{\text{Org}} = 0.1 \text{ mL min}^{-1}$ ,  $Q_{\text{Aq}} = 0.3 \text{ mL min}^{-1}$ , green:  $Q_{\text{Org}} = 0.2 \text{ mL min}^{-1}$ ,  $Q_{\text{Aq}} = 0.6 \text{ mL min}^{-1}$ , blue:  $Q_{\text{Org}} = 0.3 \text{ mL min}^{-1}$ ,  $Q_{\text{Aq}} = 0.9 \text{ mL min}^{-1}$  and  $L_R = 15 \text{ m}$ .  $Q_{\text{Gas}} = 12-80 \text{ mL min}^{-1}$ .  $C_{\text{RHNP}} = 1 \text{ mM}$  for all different experimental conditions. Solid lines represent model predictions (section 3.3).

transport and chemical reaction in the vicinity of any aqueous catalyst plug, as schematically depicted in Fig. 7a. The aqueous catalyst plug is surrounded by two distinct regions of organic liquid – a thick annular film around the reactor walls (region 2 in Fig. 7a) and a thinner ‘interfacial’ film (region 1 in Fig. 7a) immediately adjacent to the flattened aqueous–organic interface. The chemical reaction is assumed to take place nearly instantaneously at the aqueous–organic interface<sup>29</sup> and no reaction occurs inside the aqueous plug due to negligible solubility of 1-hexene in water. Therefore, the observed reaction rate is ultimately governed by how fast 1-hexene or hydrogen can be transported from the annular and interfacial film regions to this interface. It is also reasonable to assume that, given the long bubble lengths compared to the aqueous plug lengths (plug/bubble length ratio varies between 1/5 and 1/80), the annular film is always saturated with hydrogen and there is negligible hydrogen depletion within both the annular film and the bubbles. A detailed derivation of the model and description of the assumptions are presented in section 5 of the ESI;† we present the key elements of this model and highlight its explanatory power below.

Firstly, when the conversion is lower than the 60–65% range, such as in Fig. 6a (20% and 30% v/v 1-hexene) and Fig. 6b (7.5 m and 4 m of reactor length), the observed reaction rate is controlled entirely by the rate at which molecular hydrogen can be transported from the bubbles and across the *interfacial* film to the aqueous–organic interface, similar to the case of millifluidic reactors.<sup>29</sup> Since this transport is entirely a steady state diffusive process, an appropriate expression for this rate is given by eqn (2) below, where  $w_1$  is the interfacial film thickness. Most notably, this equation describes a *zero-order* process, as clearly seen in the experimental observations.

$$\frac{dC_{\text{hex}}}{d\tau} = -\frac{D_{\text{H}_2}}{w_1} \frac{\pi R^2}{\pi R^2 w_1} C_{\text{H}_2,\text{sat}} \quad (2)$$

Secondly, when the conversion is higher than the range mentioned above, such as in Fig. 6a and b and 5c (10% v/v 1-hexene), there is a considerable depletion of 1-hexene around the aqueous catalyst plug, and the observed rate is now controlled by the molecular transport of 1-hexene to the aqueous–organic interface. This transport occurs from the interfacial film *and* from the annular film, as captured by eqn (3) below, where  $w_2$  is the thickness of the annular film and  $n$  is the number of *interfacial* film regions in the reactor of length  $L_R$ . This simple model captures the fact that molecular transport of 1-hexene across the annular film region is an *unsteady* diffusive process, unlike the interfacial film (see ESI† for details). Crucially, this equation describes a *first-order* process, as clearly seen in the experimental observations of Fig. 6. Such transitions from zero order to first order kinetics have been observed in both millireactors<sup>29</sup> as well as conventional batch reactors.<sup>38,39</sup> Finally, the above dual-region



**Fig. 7** (a) Schematic illustration of mass transfer steps in the gas-liquid-liquid triphasic mesoreactor. (1): Mass transport across the interfacial film, (2): mass transport across the annular film, and (3): reaction between 1-hexene and dissolved hydrogen. Two different organic-occupied liquid regions – an annular film region (orange) and an interfacial film (grey), are highlighted. (b) Schematic illustration of two different reactor operation regimes, depending on the relative mass transport rates in the two highlighted liquid regions (refer to section 3.3 for a detailed discussion).

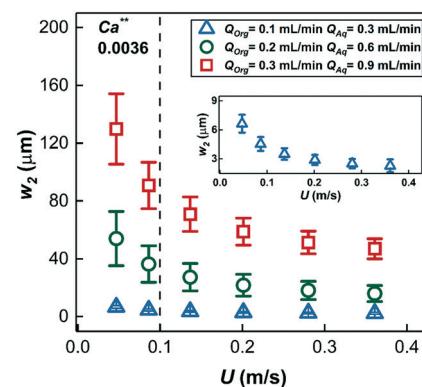
description of hexene-limited transport perfectly captures the experimental observations of Fig. 6c.

$$\frac{dC_{\text{hex}}}{d\tau} = -k_{\text{overall}} C_{\text{hex}} = - \left( \frac{1}{\frac{D_{\text{hex}}}{w_1} \frac{\pi R^2}{\pi R^2 w_1} + \frac{1}{2\sqrt{\frac{D_{\text{hex}} U}{\pi w_1}} \frac{2\pi R w_1 n}{2\pi R w_2 L_R}}} \right)^{-1} C_{\text{hex}} \quad (3)$$

The thickness of the two film regions,  $w_1$  and  $w_2$  were fitted to the experimental data (fitting was done in MATLAB *via* a non-linear least squares method) of Fig. 6a–c; the model curves show excellent fit to the measured data. It is important to note that the model curves overpredict the experimental data in Fig. 6a (20% substrate concentration) and Fig. 6b (7.5 m reactor length) at high conversions (above ~60%). This situation is a result of a transition in the dominant mass transport mechanism from hydrogen transport to 1-hexene transport. The fitted thickness of the interfacial film  $w_1$  varied within a narrow range of 35–45  $\mu\text{m}$  for different sets of experiments, an observation that highlights and supports the arguments on film drainage and stabilization discussed in section 3.1 above. On the other hand, the fitted thicknesses of the *annular* film under different conditions are shown in Fig. 8 and show an increasing trend with total liquid flow rate at the same bubble velocity, once again in complete agreement with the hydrodynamic arguments presented in section 3.1 about organic liquid drainage and redistribution. The fitted thicknesses of the annular and interfacial films allow us to estimate the annular and interfacial surface areas for mass transport (per unit cell consisting of a gas bubble and an aqueous drop with a sandwiched interfacial film) to be  $50 \text{ m}^2 \text{ m}^{-3}$  and  $20 \text{ m}^2 \text{ m}^{-3}$ , respectively. Finally, the annular films show an inverse trend with bubble

velocity (at fixed total liquid flow rate), in line with previous studies on Taylor flow in millichannels when the film deposition is purely inertia dominated<sup>40,41</sup> (for details see ESI† section 1).

Based on the fitted values of  $w_1$  and  $w_2$ , the *overall* mass transport coefficient of 1-hexene which accounts for both the mass transport across annular film and interfacial film in series,  $k_{\text{overall}}$  (the whole term in bracket in eqn (3)) as well as the mass transport coefficient of 1-hexene ( $k_{\text{L},\text{hex},\text{int}}$ ) and hydrogen ( $k_{\text{L},\text{H}_2,\text{int}}$ ) across the interfacial film (eqn (S5) in ESI†) were calculated at different operational conditions as depicted in Fig. 9a. Increasing  $Q_{\text{T}}$  at constant bubble flow speed decreased the overall 1-hexene mass transport coefficient,  $k_{\text{overall}}$ . Since the thickness of interfacial film was nearly constant, the reduction in the overall 1-hexene mass transport coefficient was mainly due to thickening of the annular film; a two-time increment in  $Q_{\text{T}}$  resulted in a halving



**Fig. 8** The thickness of the annular film around the gas bubbles estimated by fitting the mathematical model of eqn (3) at different volumetric liquid flow rates and bubble speeds. Insert shows a magnified view of the thickness of the annular film for  $Q_{\text{Org}} = 0.1 \text{ mL min}^{-1}$ ,  $Q_{\text{Aq}} = 0.3 \text{ mL min}^{-1}$ . (for  $\text{Ca}^{**}$  see ESI† section 1).

of the 1-hexene mass transport coefficient. In addition, increasing the bubble speed at constant volumetric liquid flow rate increased the overall 1-hexene mass transport coefficient due to thinner annular film and concomitantly higher mass transport rate.

From eqn (3), the individual mass transport coefficients of 1-hexene for annular and interfacial film regions were extracted and mass transport resistances were calculated for different  $Q_T$  and bubble speeds (Fig. 9b). The mass transport resistance is defined as the reciprocal of the mass transport coefficient. When  $Q_T = 0.4 \text{ mL min}^{-1}$ , the two organic regions (annular and interfacial film) had comparable 1-hexene mass transport resistances. On the other hand, when  $Q_T$  was increased beyond  $0.4 \text{ mL min}^{-1}$ , the annular film offers significantly more transport resistance for 1-hexene due to thickening. It is worthwhile to note that there is no hydrogen mass transport resistance within the *annular* film due to negligible hydrogen consumption there. Consequently, based on the relative 1-hexene transport resistances within different reactor regions, two different reactor behaviors can be identified. In the first case, when the mass transport resistance across the annu-

lar film is either comparable or lower than that of interfacial film, which was observed when  $Q_T < 0.4 \text{ mL min}^{-1}$ , and when the reaction rate is dictated by the molecular transport rate of hydrogen, the reactor can be thought of as a series of individual and *independent* reactive 'discs' traversing the channel (Fig. 7b, top). The performance of such a reactor is independent of the number of the discs (and hence the bubble length) since the reaction is confined within the interfacial film. In the second case, when the mass transport resistance of the annular film is greater than that of the interfacial film, which was observed when  $Q_T$  is beyond  $0.4 \text{ mL min}^{-1}$ , the reactor can be considered as an annulus of length  $L_R$  (Fig. 7b, bottom) along which there are 'sinks' depleting the substrate along the inside surface of the annulus. The performance of such a reactor is directly related to bubble length since it determines the number of sinks along the annulus. Interestingly, in passing we note that this reactor behavior is analogous to chemical vapor deposition (CVD) reactors.<sup>42</sup>

### 3.4. Further scale-up of the mesoscale reactor

Based on the insight we gained from our reactor model, we further scaled up our mesoscale reactor by increasing the volumetric flow rate of the substrate, catalyst and the reactor length. To achieve high-volume continuous flow conditions, syringe pumps were replaced by peristaltic pumps. Capacitance-based hydraulic dampers<sup>21</sup> were used to damp out the pressure fluctuations introduced by the peristaltic pumps, which can severely influence the multiphase flow stability (For the details of the experimental setup, see ESI† section 6 and movie M5). The reaction was conducted in a 45 m long 3.2 mm ID PTFE tube with  $0.8 \text{ M}$  (10% v/v)  $1.2 \text{ mL min}^{-1}$  organic substrate flow rate and  $1 \text{ mM}$   $3.6 \text{ mL min}^{-1}$  catalyst flow rate. Due to the large volumetric flow rate, molecular transport in the annular film was the dominant factor dictating the observed kinetics. A large  $Q_T$  led to short bubble lengths, thus providing a large number of interfacial film

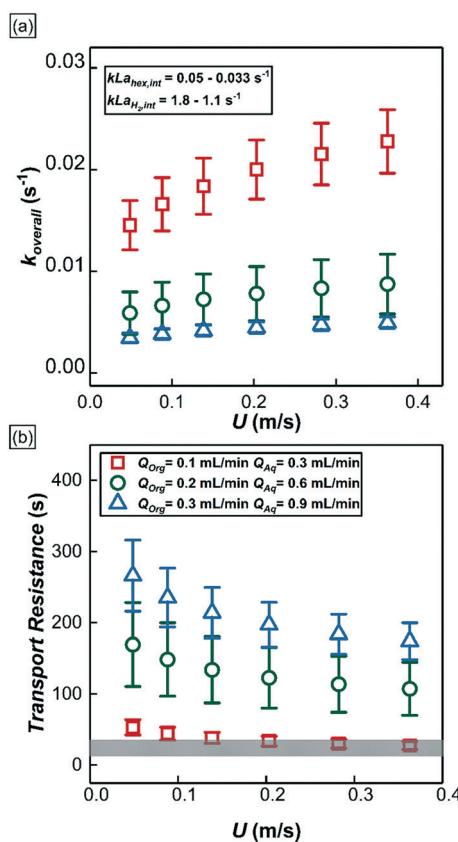


Fig. 9 (a) The overall mass transport of 1-hexene at different experimental conditions. Insert shows the mass transport coefficient of 1-hexene and hydrogen across the interfacial film calculated from eqn (S5†). (b) 1-Hexene mass transport resistances of two distinct reactor regions under different experimental conditions. Scatter plots represent the 1-hexene mass transport resistances in the annular film region whereas the shaded grey area represents the 1-hexene mass transport resistance in the interfacial film region.

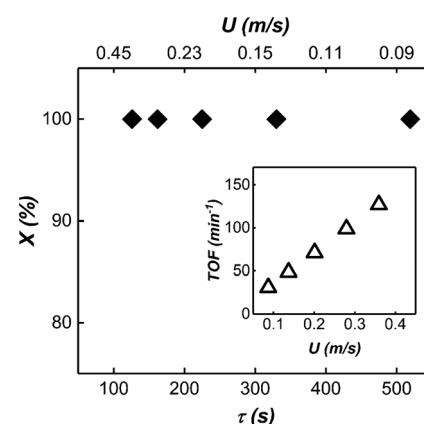


Fig. 10 1-Hexene conversion ( $X$ ) versus bubble residence time ( $\tau$ ) in scaled-up mesoreactor. Insert shows the turnover frequency of the reactor at different flow velocities. Turnover frequency is defined as number of moles of 1-hexene converted to product per number of moles of catalyst per unit time.

**Table 1** Comparison of performance of mesoreactor with different gas–liquid–liquid triphasic reactor setups

Reactor	Residence time (min)	Conversion (%)	Substrate flow rate	Throughput (g per day)	TOF (min <sup>-1</sup> )
50 mL round bottom flask <sup>29</sup>	60	100	5 mL 800 mM 1-hexene	8.25	21
1 mm ID single triphasic <sup>29</sup> milireactor channel	~1	82	10 $\mu$ L min <sup>-1</sup> 800 mM 1-hexene	0.8	634
1 mm ID 8-fold triphasic milireactor network <sup>21</sup>	~8	80	8 $\times$ 20 $\mu$ L min <sup>-1</sup> 100 mM nitrobenzene	2.26	80
Current work	~2	100	1.2 mL min <sup>-1</sup> 800 mM 1-hexene	120	130

regions for the reaction to take place. The large number of interfacial films along with longer residence time due to longer reactor length resulted in nearly complete conversion under all experimental conditions (see Fig. 10).

### 3.5. Performance comparison of mesoreactor with similar gas–liquid–liquid contactors

In this section, the performance between the triphasic mesoreactor of this work is compared to its single channel and 8-fold parallelized millireactor and small-scale round-bottom flask counterparts (see Table 1). All flow reactors in this comparison have the same gas–liquid–liquid flow configuration and the same catalyst is used in all cases. The mass throughput of our mesoreactor was 150 times higher than its single milireactor channel counterpart at comparable residence time and conversion<sup>29</sup> and ~50 times higher than its 8-fold parallelized millireactor counterpart at comparable conversion and shorter residence time.<sup>21</sup> In addition, when the same model reaction (hydrogenation of 1-hexene) was performed in a 50 mL round bottom flask under well stirred conditions (1200 RPM) with the same rhodium nanoparticle catalyst, significant improvement in reaction time and throughput was observed in our triphasic mesoreactor. A 120 g per day per channel throughput can be achieved with the operation conditions given in the previous section. The throughput of the single mesoscale channel can be further increased by more concentrated substrate and/or higher substrate flow rate with proper residence time. For example, if the reactor was operated with 1.2 mL min<sup>-1</sup> organic phase flow rate and 50% v/v substrate concentration with 5–10 minutes of residence time a single mesoscale channel would produce 665 g hydrogenated product per day. Indeed, by simple 4–8 fold parallelization,<sup>21</sup> 3–5 kg of product per day can be produced, and this would be a realistic pilot scale reactor for pharmaceutical production with all the advantages highlighted in the introduction section.

## Summary and conclusion

We demonstrated a mesoscale triphasic (gas–liquid–liquid) reactor for fast, transition metal catalyzed gas–liquid reactions, which is capable of delivering kg per day productivity at the single channel level. Despite the increase in channel dimension, the mesoreactor is still able to intensify the mass transport whilst the retaining similar basic physics of operation with small scale systems. We also develop a complete reactor model incorporating the effect of various operating con-

ditions for the model reaction – hydrogenation of 1-hexene in the presence of a colloidal rhodium nanoparticle catalyst. Moving from milliscale to mesoscale, we observe that annular film around gas bubbles acts as a *reservoir* for 1-hexene while in milliscale systems the reaction is confined to interfacial films with little or no role played by the annular films. Based on the insight we gain from the reactor model we further scaled up our system and achieved 150 times higher mass throughput compared to a single milliscale channel and ~50 times the throughput of an 8-fold scaled out millireactor network at comparable residence time. Moreover, the throughput of the mesoreactor can be further increased by a very reasonable scale out by parallelization (4–8 $\times$ ), and catalyst recovery and recycle can be easily achieved due to compartmentalization of catalyst in a separate liquid phase. The analysis and design principles presented in this work are general, and the working principle of the mesoreactor can be extended to other metal catalyzed gas–liquid transformations. Our ongoing works include exploitation of new flow structures to further intensify the mass transport rate, understanding of residence time distribution (RTD) of organic phase, and implementation of our mesoreactor on different catalyst types as well as chemical reactions of relevance in pharmaceutical manufacturing.

## Nomenclature

<i>a</i>	Surface area to volume ratio
<i>Bo</i>	Bond number
<i>C</i> <sub>hex</sub>	Concentration of 1-hexene in decane
<i>C</i> <sub>H<sub>2</sub>,sat</sub>	Concentration of hydrogen in decane
<i>C</i> <sub>RhNP</sub>	Concentration of rhodium nanoparticle catalyst
<i>D</i>	Diffusivity
<i>g</i>	Gravitational acceleration
<i>k</i> <sub>overall</sub>	Overall mass transport coefficient of 1-hexene
<i>L</i>	Characteristic length
<i>L</i> <sub>B</sub>	Bubble length
<i>L</i> <sub>R</sub>	Reactor length
<i>n</i>	Number of the interfacial films per reactor length
<i>Q</i> <sub>Aq</sub>	Volumetric flow rate of aqueous phase
<i>Q</i> <sub>Gas</sub>	Volumetric flow rate of gas phase
<i>Q</i> <sub>Org</sub>	Volumetric flow rate of organic phase
<i>Q</i> <sub>T</sub>	Total liquid flow rate
TOF	Turnover frequency of catalyst
<i>U</i>	Flow speed
<i>w</i> <sub>1</sub>	Thickness of interfacial film
<i>w</i> <sub>2</sub>	Thickness of annular film

## Greek symbols

- $\gamma$  Interfacial tension
- $\rho$  Density
- $\tau$  Bubble residence time

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

The authors gratefully acknowledge funding from the GSK-EDB fund for Green and Sustainable manufacturing (GSM) and the Ministry of Education, Singapore.

## References

- 1 B. Gutmann, D. Cantillo and C. O. Kappe, *Angew. Chem., Int. Ed.*, 2015, **54**, 6688–6728.
- 2 J. Yue, G. Chen, Q. Yuan, L. Luo and Y. Gonthier, *Chem. Eng. Sci.*, 2007, **62**, 2096–2108.
- 3 M. Liu, X. Zhu, R. Chen, Q. Liao, H. Feng and L. Li, *Chem. Eng. J.*, 2016, **301**, 35–41.
- 4 M. Brzozowski, M. O'Brien, S. V. Ley and A. Polyzos, *Acc. Chem. Res.*, 2015, **48**, 349–362.
- 5 K. K. Yeong, A. Gavriilidis, R. Zapf and V. Hessel, *Catal. Today*, 2003, **81**, 641–651.
- 6 M. T. Rahman, T. Fukuyama, N. Kamata, M. Sato and I. Ryu, *Chem. Commun.*, 2006, 2236–2238.
- 7 C. P. Park and D.-P. Kim, *J. Am. Chem. Soc.*, 2010, **132**, 10102–10106.
- 8 Y. Önal, M. Lucas and P. Claus, *Chem. Eng. Technol.*, 2005, **28**, 972–978.
- 9 A.-K. Liedtke, F. Bornette, R. Philippe and C. De Bellefon, *Chem. Eng. J.*, 2013, **227**, 174–181.
- 10 L. Vanoye, J. Wang, M. Pablos, R. g. Philippe, C. d. Bellefon and A. Favre-Réguillon, *Org. Process Res. Dev.*, 2015, **20**, 90–94.
- 11 R. Chambers and R. H. Spink, *Chem. Commun.*, 1999, 883–884.
- 12 Y. Su, V. Hessel and T. Noël, *AICHE J.*, 2015, **61**, 2215–2227.
- 13 A. Woitalka, S. Kuhn and K. F. Jensen, *Chem. Eng. Sci.*, 2014, **116**, 1–8.
- 14 M. T. Kreutzer, F. Kapteijn, J. A. Moulijn and J. J. Heiszwolf, *Chem. Eng. Sci.*, 2005, **60**, 5895–5916.
- 15 R. D. Chambers, M. A. Fox, D. Holling, T. Nakano, T. Okazoe and G. Sandford, *Lab Chip*, 2005, **5**, 191–198.
- 16 Y. Wada, M. A. Schmidt and K. F. Jensen, *Ind. Eng. Chem. Res.*, 2006, **45**, 8036–8042.
- 17 A. M. Nightingale, J. H. Bannock, S. H. Krishnadasan, F. T. O'Mahony, S. A. Haque, J. Sloan, C. Drury and R. McIntyre, *J. Mater. Chem. A*, 2013, **1**, 4067–4076.
- 18 A. Nagaki, K. Hirose, O. Tonomura, S. Taniguchi, T. Taga, S. Hasebe, N. Ishizuka and J.-i. Yoshida, *Org. Process Res. Dev.*, 2016, **20**, 687–691.
- 19 Y. Su, K. Kuijpers, V. Hessel and T. Noël, *React. Chem. Eng.*, 2016, **1**, 73–81.
- 20 M. Al-Rawashdeh, J. Zalucky, C. Muller, T. Nijhuis, V. Hessel and J. Schouten, *Ind. Eng. Chem. Res.*, 2013, **52**, 11516–11526.
- 21 S. K. Yap, W. K. Wong, N. X. Y. Ng and S. A. Khan, *Chem. Eng. Sci.*, 2017, **169**, 117–127.
- 22 R. Schenk, V. Hessel, C. Hofmann, J. Kiss, H. Löwe and A. Ziogas, *Chem. Eng. J.*, 2004, **101**, 421–429.
- 23 S. G. Newman and K. F. Jensen, *Green Chem.*, 2013, **15**, 1456–1472.
- 24 M. Saber, J. Commenge and L. Falk, *Chem. Eng. Sci.*, 2010, **65**, 372–379.
- 25 M. Al-Rawashdeh, L. Fluitsma, T. Nijhuis, E. Rebrov, V. Hessel and J. Schouten, *Chem. Eng. J.*, 2012, **181**, 549–556.
- 26 M. m. Al-Rawashdeh, X. Nijhuis, E. V. Rebrov, V. Hessel and J. C. Schouten, *AICHE J.*, 2012, **58**, 3482–3493.
- 27 N. de Mas, A. Günther, T. Kraus, M. A. Schmidt and K. F. Jensen, *Ind. Eng. Chem. Res.*, 2005, **44**, 8997–9013.
- 28 S. K. Yap, Y. Yuan, L. Zheng, W. K. Wong, J. Zhang, N. Yan and S. A. Khan, *Green Chem.*, 2014, **16**, 4654–4658.
- 29 S. Yap, Y. Yuan, L. Zheng, W. Wong, N. Yan and S. Khan, *J. Flow Chem.*, 2014, **4**, 200–205.
- 30 X.-d. Mu, D. G. Evans and Y. Kou, *Catal. Lett.*, 2004, **97**, 151–154.
- 31 J. J. Bakker, M. M. Zieverink, R. W. Reintjens, F. Kapteijn, J. A. Moulijn and M. T. Kreutzer, *ChemCatChem*, 2011, **3**, 1155–1157.
- 32 P.-G. De Gennes, F. Brochard-Wyart and D. Quéré, *Capillarity and wetting phenomena: drops, bubbles, pearls, waves*, Springer Science & Business Media, 2013.
- 33 S. A. Khan and S. Duraiswamy, *Lab Chip*, 2009, **9**, 1840–1842.
- 34 K. J. Stebe, S. Y. Lin and C. Maldarelli, *Phys. Fluids A*, 1991, **3**, 3–20.
- 35 J. N. Connor and R. G. Horn, *Faraday Discuss.*, 2003, **123**, 193–206.
- 36 G. Barnocky and R. Davis, *Int. J. Multiphase Flow*, 1989, **15**, 627–638.
- 37 B. M. Jose and T. Cubaud, *RSC Adv.*, 2014, **4**, 14962–14970.
- 38 J. Campelo, A. Garcia, D. Luna and J. Marinas, *Appl. Catal.*, 1982, **3**, 315–325.
- 39 R. Madon, J. O'connell and M. Boudart, *AICHE J.*, 1978, **24**, 904–911.
- 40 P. Aussillous and D. Quéré, *Phys. Fluids*, 2000, **12**, 2367–2371.
- 41 Y. Han and N. Shikazono, *Int. J. Heat Fluid Flow*, 2010, **31**, 630–639.
- 42 M. L. Hitchman and K. F. Jensen, *Chemical vapor deposition: principles and applications*, Elsevier, 1993.