

Cite this: *Mater. Horiz.*, 2026, 13, 2022Received 16th October 2025,  
Accepted 4th December 2025

DOI: 10.1039/d5mh01962a

rsc.li/materials-horizons

# Achieving strength and toughness limits of anisotropic microstructured alumina ceramics through interface engineering

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Advanced ceramic composites face a critical challenge: achieving the combined strength and toughness as in natural materials like nacre. Bioinspired anisotropic microstructured ceramics (AMCs) address this by mimicking nacre's hierarchical architecture. However, the critical role of the ceramic–matrix interface is often overlooked, due to a fundamental conflict: the weak interfaces needed for toughening through crack deflection are naturally difficult to achieve with conventional sintering processes that prioritize densification. Here, we bridge this gap by establishing universal energy- and strength-governed criteria for crack deflection in staggered microstructures, revealing two key mechanisms to unlock the full potential of AMCs. First, a low-stiffness matrix redistributes stress to mitigate stress concentrations, thereby enhancing failure strength. Simultaneously, a low-toughness interface facilitates crack deflection, leading to crack branching, micro-platelet bridging, and unstable crack growth. These mechanisms collectively amplify fracture toughness by enabling plastic-like deformation in brittle ceramics. In alumina AMCs, microplatelet thickness and interfacial toughness are identified as the primary factors reconciling experimental-theoretical discrepancies. By reducing microplatelet thickness to 300 nm and incorporating a compliant matrix, we predict a theoretical strength of 2.25 GPa. Critically, the matrix must strike a delicate balance: it must be weak enough to deflect cracks yet cohesive enough to operate near the crack-deflection threshold, thereby maximizing energy dissipation. Through systematic optimization of these parameters, we predict a 13.1- to 21.8-fold amplification in toughness for alumina AMCs. This performance surpasses most engineered ceramics and approaches the remarkable properties of nacre. By defining the precise interfacial properties required for optimal performance, our work provides clear screening criteria for mitigating the historical processing conflict, thereby establishing interface engineering as a cornerstone for

## New concepts

Nacre-like all-ceramic metamaterials can be programmed by two interface descriptors: the stiffness ratio and the toughness/strength ratio between matrix and platelet. Adjusting these descriptors switches the dominant crack path (deflection *versus* penetration) and, in turn, the macroscopic crack-growth resistance. A compact design map, built from unit-cell analysis and discrete-element simulations, yields simple rules that are independent of platelet aspect ratio and transferable across different brittle ceramics. In this picture, interfacial properties redistribute stress and activate extrinsic dissipation through crack branching, bridging, and interlayer sliding, leading to plastic-like deformation in otherwise brittle ceramics. The framework shows how modest improvements in initiation toughness at the unit-cell scale can accumulate into large, size-dependent toughness amplification as the crack spans many repeats, and it identifies practical levers for fabrication, including matrix selection and platelet thickness, for heat-resistant, architected nacre-like ceramics.

designing next-generation ceramic composites capable of withstanding extreme environments.

## 1. Introduction

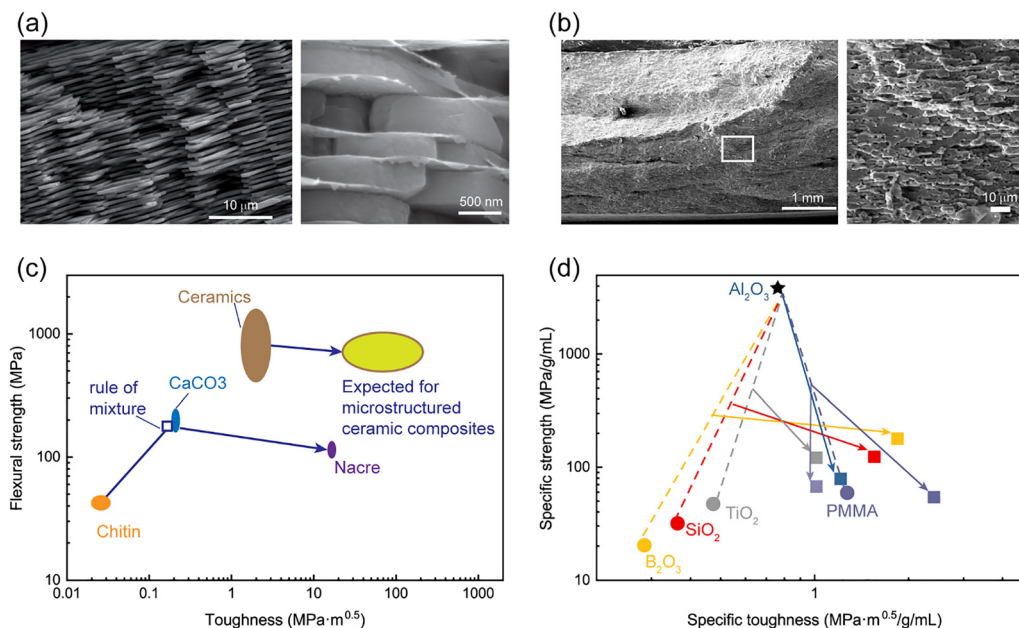
Nacre-like composites with a brick-and-mortar hierarchical microstructure have attracted significant attention in recent years for their ability to combine exceptional strength and fracture toughness. Nacre, a nanocomposite composed of ~95% brittle minerals and ~5% ductile proteins arranged in a brick-and-mortar structure (Fig. 1a), achieves a fracture toughness of ~10 MPa m<sup>0.5</sup> (≈40 times higher than pure aragonite), while maintaining a strength of ~140 MPa (*versus* ~200 MPa for pure aragonite).<sup>1–3</sup> This performance arises from the protein-based “mortar”, which redistributes stress, deflects

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**Fig. 1** Microstructure and property benchmarks for nacre and nacre-like alumina. Representative microstructures of (a) natural nacre<sup>14</sup> (electron micrograph; reproduced with permission from ref. 14; Copyright 2014, Springer Nature) and (b) nacre-like alumina (electron micrograph; this work). (c) Natural nacre demonstrates fracture toughness approximately 40 times higher than that of its mineral bricks, while its strength approaches the yield stress of the mineral bricks under uniform loading.<sup>3,7</sup> (d) The specific strength and toughness of nacre-like alumina are still limited by an insufficient understanding of the roles of nacre microstructure and interfacial properties.<sup>9,14–17</sup> Source data and digitized values used for panels (c) and (d) are provided in the SI in Table S1. Panel (a) reproduced with permission from ref. 14. The “specific” values denote normalization by density  $\rho$ : specific strength =  $\sigma/\rho$  and specific fracture toughness  $K_{Ic}/\rho$ ; densities are expressed in  $\text{g mL}^{-1}$  (where  $1 \text{ g mL}^{-1} = 1000 \text{ kg m}^{-3}$ ).

cracks, and imparts damage tolerance to the brittle mineral phase.<sup>4–8</sup> To replicate these properties, researchers have developed synthetic analogues using polymer or metallic mortars, such as polymethylmethacrylate (PMMA) mortar between alumina bricks,<sup>9</sup> ethylene-vinyl acetate layers in glass bricks,<sup>10</sup> and copper interlayers in alumina.<sup>11,12</sup> However, these composites can degrade under extreme conditions, such as high temperature or oxidative environments, and often exhibit only moderate strength and fracture toughness. For instance, nacre-like composites with alumina bricks and polymer or metal mortar typically show strengths below 400 MPa and fracture toughness  $\leq 10 \text{ MPa m}^{0.5}$ . This is far lower than the 600 MPa strength and  $17.3 \text{ MPa m}^{0.5}$  fracture toughness achieved by all-ceramic counterparts.<sup>13,14</sup> Compared with polymer- and metal-based nacre-like composites, all-ceramic composites also offer greater resistance to environmental degradation, since oxide–oxide interfaces formed during sintering are far less sensitive to humidity and corrosion. Taken together, prior studies show that all-ceramic nacre-like composites can achieve high performance; however, delivering robust, environment-resistant operation with simultaneously high strength and high fracture toughness, particularly under severe thermal or oxidative conditions, remains unresolved. Here we adopt an interface-engineering design strategy in all-ceramic nacre-like composites: by tuning the ceramic–ceramic interface to control load transfer and crack-path selection, we aim to retain strength while increasing fracture toughness in a manner suitable for demanding environments.

Previous studies on all-ceramic nacre-like microstructures, or anisotropic microstructured ceramics (AMCs), in which ceramic microplatelets (“bricks”) are embedded in a ceramic matrix (“mortar”) (Fig. 1b), have reported high strength, elevated fracture toughness,<sup>14,15,18,19</sup> and good high-temperature performance.<sup>13,19</sup> These gains are commonly attributed to ceramic constituents and architecture-induced anisotropy, which promote microplatelet bridging and crack deflection.<sup>13</sup> Yet, the realized fracture toughness gains in AMCs remain below bioinspired benchmarks. For example, the toughness amplification factor (TAF), defined as the ratio of AMC fracture toughness to that of its primary ceramic ( $K_{Ic,AMC}/K_{Ic,brick}$ ), rarely exceeds 10 and often remains  $\sim 5$ , while natural nacre achieves up to 40 (Fig. 1c).<sup>3,6,13</sup> Although AMCs exhibit enhanced fracture toughness, their failure strength is significantly compromised due to the inherent strength–toughness trade-off. Fig. 1(d) shows that AMC failure strength may decline by up to 50% relative to alumina microplatelets, whereas natural nacre shows only a  $\sim 30\%$  decrease.<sup>9,14–17</sup> This gap motivates interface-focused design and modeling to guide experiments toward more balanced strength–fracture–toughness performance (Fig. 1c).

Resolving the strength–toughness trade-off in nacre-like composites requires optimizing both microstructural geometry and ceramic–ceramic interfacial properties. In all-ceramic architectures, however, this goal is particularly challenging. Fracture surface observations reveal that ceramic microplatelets with large aspect ratios often fail by tensile fracture rather



than interfacial sliding during crack propagation,<sup>5,8,11,12,20</sup> thereby suppressing extrinsic toughening mechanisms such as crack bridging and lowering the TAF.<sup>4,21,22</sup> This limitation can be addressed by balancing component properties. For instance, molecular mechanics simulations suggest that balancing matrix and brick stiffness, with a matrix-to-brick stiffness ratio of 0.3–0.6, can preserve structural rigidity while avoiding brittle failure.<sup>23</sup> Additionally, a systematic optimization strategy for staggered composites has been proposed, offering guidelines for platelet dimensions, material properties, volume content, interface strength, and platelet overlap.<sup>7,24–26</sup>

The primary constraint to implementing these theoretical designs is processing. Historically, introducing weak interfaces to promote crack deflection increases apparent toughness, but conventional densification and sintering make such interfaces difficult to reproduce. This conflict between “interfaces that toughen” and “processes that densify” was recognized early and remains a practical constraint for modern all-ceramic systems.<sup>27</sup> Consequently, many advances primarily apply to nacre-like composites with ductile polymer or metal matrices,<sup>28–30</sup> leaving all-ceramic AMCs comparatively underexplored. Predictive, fabrication-aware models for their mechanical behavior remain limited,<sup>23,31–33</sup> and high-temperature fabrication further complicates microstructure control through grain growth and diffusion, creating coupled constraints across material selection, processing, and architecture.<sup>11,13,18</sup> To bridge fabrication and modeling, we employ interface engineering, defined within a mechanics-guided design framework that focuses on tuning effective interfacial stiffness and toughness at the mesoscale rather than prescribing a specific experimentally realized interface chemistry. This design framework selects a ceramic matrix and processing conditions to achieve interfacial properties that guide crack propagation while maintaining overall strength. This approach focuses on a small set of controllable parameters: platelet thickness, matrix layer thickness, and interfacial toughness and stiffness.<sup>34,35</sup> A central question for all-ceramic AMCs is therefore: which matrix/interfacial combinations best reconcile deflection-driven toughening with strength retention under realistic sintering windows?

Here, we advance an interface-engineering design framework for AMCs viewed as mechanical metamaterials, in which the macroscopic fracture response is governed by the architected microstructure rather than by the homogeneous properties of the base ceramics. We posit that ceramic–ceramic interfaces, rather than platelet aspect ratio alone, govern crack-path selection and thus the attainable balance of strength and fracture toughness. First (Section 2), we formulate minimal both energy- and strength-based criteria for interface-guided crack deflection in staggered architectures and evaluate them with a simplified unit-cell model. Second (Section 3.1), we test these criteria using discrete-element simulations at the unit-cell level and identify a performance ridge near the deflection–penetration boundary that maximizes energy dissipation. Third (Sections 3.2 and 3.3), we track full-field crack evolution and rising *R*-curve behavior and then translate the design rules to alumina systems, identifying microplatelet thickness and interfacial toughness as actionable experimental levers. Fourth

(Section 3.4), we discuss processing-aware guidance for matrix selection and interface control. Finally (Section 4), we summarize the implications for programmable, nacre-like metamaterials, where interface tuning directly programs the crack path and the rising resistance curve and thereby enables damage-tolerant responses in all-ceramic architectures.

## 2. Theoretical considerations

This section introduces the minimal unit-cell framework and notation, and derives the interface-engineered criteria used to predict whether a crack deflects or penetrates. Interface engineering here means selecting the matrix properties so that the interfacial stiffness, strength, and toughness can steer cracks along platelet–matrix interfaces, where deflection, sliding, and bridging can occur. The overall architecture, unit cell, and representative failure modes are summarized in Fig. 2.

At the microstructural level, bioinspired AMCs feature staggered ceramic microplatelets embedded in a ceramic matrix (Fig. 2a).<sup>25</sup> When subjected to tensile stress, this staggered microstructure can be represented by a schematic unit cell shown in Fig. 2(b), where the ceramic microplatelet primarily bears tensile stresses, while the ceramic matrix transfers the shear load.<sup>7,36</sup> The mechanical responses of this unit cell are analyzed using the widely applied load-transfer model for a brittle interface.<sup>33</sup> We focus on the intrinsic unit-cell response under a locally uniform stress field. This assumption holds when external loading varies over length scales much larger than the platelet repeat. Under this standard scale separation in hierarchical composites, unit-cell results capture materials trends without prescribing a specific crack-tip solution.<sup>37</sup> According to this model, when the aspect ratio  $\lambda$  of the microplatelet ( $\lambda = L/h$ , with  $L$  the microplatelet length and  $h$  its thickness) exceeds a critical value  $\lambda^*$ , the unit-cell tensile strength governed by matrix failure becomes independent of  $\lambda$  and is given by (as detailed in the SI, Fig. S1)<sup>33</sup>

$$\sigma_{\text{cm}} = \Phi \sqrt{\frac{E_{\text{p}} \Gamma_{\text{m}}}{h}}, \quad (1)$$

where  $\Gamma_{\text{m}}$  denotes the matrix critical energy-release rate (hereafter referred to as the interfacial toughness for brevity), and  $E_{\text{p}}$ ,  $h$ , and  $\Phi$  are the Young's modulus, thickness, and volume ratio of the ceramic microplatelets, respectively. For clarity,  $\sigma_{\text{cm}}$  refers to the unit-cell strength controlled by matrix failure,  $\sigma_{\text{cp}}$  denotes the unit-cell strength controlled by platelet failure, and  $\sigma_{\text{m}}$  and  $\sigma_{\text{p}}$  denote the constituent strengths of the matrix and the platelets, respectively. The critical length scale is

$$\lambda^* = 2 \sqrt{\frac{2(1 + \nu_{\text{m}})(1 - \Phi)E_{\text{p}}}{\Phi E_{\text{m}}}}, \quad (2)$$

where  $E_{\text{m}}$  is the Young's modulus of the matrix, and  $\nu_{\text{m}}$  is the Poisson's ratio of the matrix. Taking a rough estimate  $\nu_{\text{m}} = 0.22$ ,  $\Phi = 0.9$ , and  $E_{\text{m}}/E_{\text{p}} = 0.1$ , we find  $\lambda^* \approx 3.2$ . This critical aspect ratio is consistent with previous discrete element method (DEM) simulations<sup>32</sup> and is smaller than the aspect ratio of



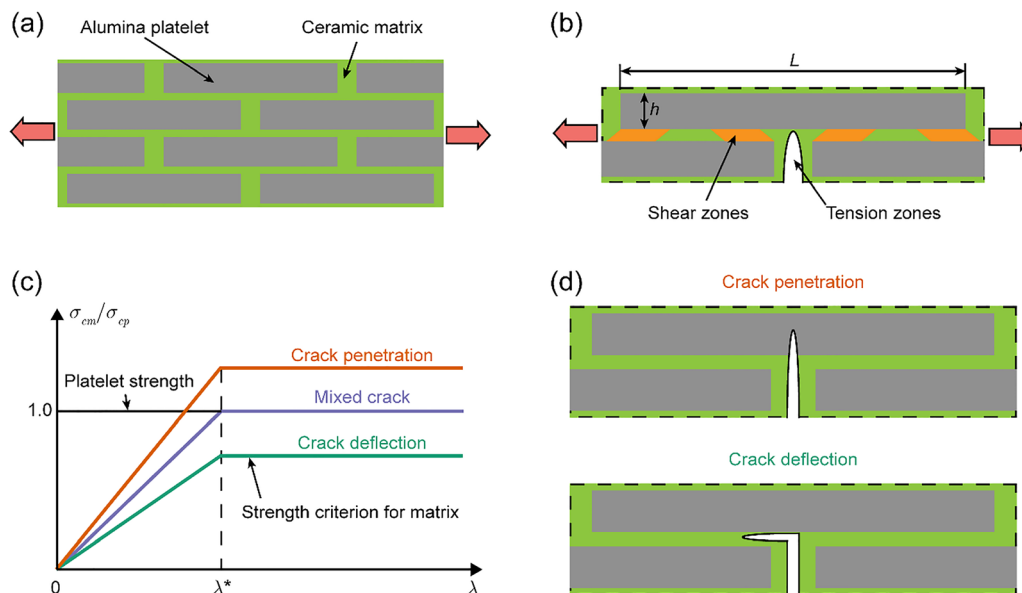


Fig. 2 Structural model of bioinspired AMCs. (a) Schematic representation of staggered ceramic microplatelets embedded in a ceramic matrix. (b) Simplified load-transfer unit cell: the ceramic microplatelet carries most of the axial load, while the ceramic matrix transfers load via interfacial shear zones between adjacent microplatelets. The parameters  $L$  (length) and  $h$  (thickness) define the aspect ratio  $\lambda = L/h$ . (c) Comparison of the matrix-controlled unit-cell strength ( $\sigma_{cm}$ , eqn (1)), and the platelet-controlled unit-cell strength ( $\sigma_{cp}$ , eqn (3)). The critical aspect ratio  $\lambda^*$  (eqn (2)) is indicated. (d) Schematic of crack-path modes (deflection vs. penetration) corresponding to the strength regimes in (c).

the microplatelets widely observed in AMCs.<sup>13</sup> Eqn (1) and (2) indicate that the tensile strength associated with matrix failure depends on the microplatelet thickness, Young's modulus, and the energy release rate of the matrix, rather than on the microplatelet aspect ratio. Moreover, most of the load is carried by localized shear zones with a characteristic length of  $h\lambda^*$  (Fig. 2b).

To ensure the structural integrity and optimize the strength and toughness of the bioinspired ceramics, the microplatelet must sustain high tensile stresses without fracturing, while the ceramic matrix dissipates energy through interfacial cracking and frictional resistance to interlayer sliding. For bioinspired AMCs, the tensile strength of microplatelets is not constant if the microplatelet thickness exceeds the critical value  $h^* \approx \Gamma_p E_p / \sigma_{th}^2$ , where  $\Gamma_p$  is the critical energy release rate of the microplatelet and  $\sigma_{th}$  is the theoretical strength of the microplatelet.<sup>25</sup> For alumina microplatelet with  $\Gamma_p = 20 \text{ J m}^{-2}$ ,  $E_p = 380 \text{ GPa}$ , and  $\sigma_{th} \approx 5 \text{ GPa}$ ,<sup>38</sup> we estimate  $h^* \approx 300 \text{ nm}$ . This critical thickness is comparable to the thickness of mineral microplatelets in natural nacre, which are several hundred nanometers.<sup>39</sup> When the microplatelet thickness exceeds this scale, the failure strength of unit cell becomes sensitive to structural size and stress distribution, as estimated by

$$\sigma_{cp} = \frac{\Phi}{2} \sqrt{\frac{E_p \Gamma_p}{h}} \left( \frac{E_p}{E_m} \right)^\eta \quad (3)$$

The first term of eqn (3) represents the fracture toughness component from the Griffith criterion,<sup>25</sup> whereas the second term describes the effect of elastic mismatch between the microplatelet and the matrix, where the exponent  $\eta$  depends on the stress distribution in the tension zone (typically  $0 \leq \eta < 1/2$ ). Physically, modulus mismatch modifies the shear-lag

transfer length and the near-tip stress profile.<sup>40</sup> In the limit of negligible mismatch ( $E_p/E_m \rightarrow 1$ ), the mismatch contribution vanishes ( $\eta \rightarrow 0$ ), while for strong mismatch the shear-lag-controlled field gives  $\eta$  approaching  $1/2$ .<sup>36</sup> Accordingly, we express the platelet-controlled strength with a mismatch factor  $(E_p/E_m)^\eta$ , and determine  $\eta$  by fitting the log-log slope of  $\sigma_{cp}/E_p$  versus  $E_m/E_p$  from DEM simulations at fixed geometry and volume fraction. For the present architecture the fitted slope is  $-0.125$ , giving  $\eta \approx 0.125$  (see the SI, Fig. S2).

By comparing the failure strength of the matrix and microplatelet, we identify the critical condition that defines deformation modes in the unit cell. When the matrix-controlled unit-cell strength is lower than the platelet-controlled unit-cell strength ( $\sigma_{cm} < \sigma_{cp}$ ), the unit cell undergoes crack deflection (Fig. 2c). We derive the energy criterion of crack deflection for staggered microstructures as

$$\frac{\Gamma_m}{\Gamma_p} \leq \frac{1}{4} \left( \frac{E_p}{E_m} \right)^{2\eta} \quad (4)$$

If  $E_m/E_p = 1$ , eqn (4) simplifies to  $\Gamma_m/\Gamma_p \leq 0.25$ , corresponding to the criterion for interfacial crack deflection without elastic mismatch.<sup>41</sup> For a crack approaching a platelet/matrix interface, we assess deflection versus penetration using eqn (4).<sup>41</sup> Assuming constant matrix and microplatelet strengths at a given length scale, denoted as  $\sigma_m$  and  $\sigma_p$ , respectively, we estimate the energy release rate as  $\Gamma \sim \sigma^2/E$ . The strength criterion for crack deflection then becomes

$$\frac{\sigma_m}{\sigma_p} \leq \frac{1}{2} \left( \frac{E_m}{E_p} \right)^{\frac{1}{2}-\eta} \quad (5)$$



If  $E_m/E_p = 1$ , eqn (5) reduces to  $\sigma_m/\sigma_p \leq 0.5$ , closely matching the criterion for crack deflection at the interface obtained from FEM simulations.<sup>40</sup> Conversely, when the matrix-controlled unit-cell strength exceeds that of the microplatelet ( $\sigma_{cm} > \sigma_{cp}$ ), the microplatelet fails, leading to crack penetration within the unit cell (Fig. 2c). This strength-based criterion provides a simple design rule when detailed crack-tip fields are not evaluated.<sup>32,40</sup>

The above analysis indicates that the strength limit of bioinspired AMCs is governed by the failure strength of the microplatelet. The failure strength of AMCs is expressed by

$$\sigma_f = \begin{cases} \frac{\Phi\sigma_p}{2}, & h \leq h^* \\ \frac{\Phi}{2\sqrt{h}} \frac{E_p\Gamma_p}{h} \left(\frac{E_p}{E_m}\right)^\eta, & h > h^* \end{cases} \quad (6)$$

Eqn (6) suggests that the maximum strength of bioinspired AMCs reaches approximately 0.45 of the microplatelet strength when  $\Phi = 0.9$ , in good agreement with previous DEM simulations.<sup>32</sup> When the microplatelet thickness exceeds the critical length scale, this maximum strength becomes inversely proportional to the square root of the microplatelet thickness. Note that the strength model addresses intrinsic capacity under a mesoscale averaged field; the fracture-toughness response in the presence of macroscopic cracks is governed by the deflection/penetration criteria (eqn (4) and (5)) and the mode mixity at the interface.<sup>40</sup>

Fig. 2(c) also reveals an optimal ceramic matrix, corresponding to the condition in which both the matrix and the microplatelet fail simultaneously:

$$\frac{\Gamma_m}{\Gamma_p} = \frac{1}{4} \left(\frac{E_p}{E_m}\right)^{2\eta} \quad \text{or} \quad \frac{\sigma_m}{\sigma_p} = \frac{1}{2} \left(\frac{E_m}{E_p}\right)^{\frac{1}{2}-\eta} \quad (7)$$

The critical condition defined by eqn (7) typically represents the optimal balance of strength and toughness for bioinspired AMCs. Importantly, it depends solely on the mechanical properties of the matrix and is independent of microstructural dimensions. In practice, this optimum complements the deflection/penetration map (Fig. 2d) above and provides a simple screening rule for materials selection.

### 3. Results and discussion

#### 3.1. Optimization design based on unit cell

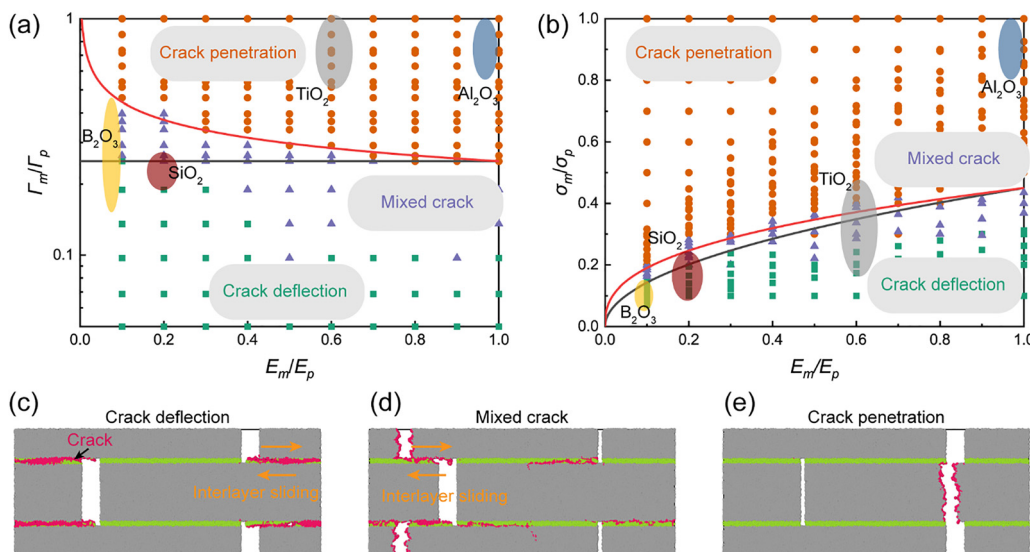
To validate the crack-deflection criteria, we systematically vary three key matrix properties: Young's modulus ( $E$ ), failure strength ( $\sigma$ ), and critical energy release rate ( $\Gamma$ ). DEM simulations are performed on a representative staggered microstructure unit cell, modeling both matrix and microplatelets as linearly elastic, brittle materials (Fig. 3; see the SI for details). Although the cohesive bonds are brittle, post-failure interfacial mechanics are governed by frictional contact interactions. These interactions naturally capture the nonlinear behavior, specifically the process of interfacial cracking followed by sliding and platelet pull-out, which is responsible for

toughening in AMCs. The material contrast between matrix and microplatelets is quantified using three dimensionless ratios: stiffness ( $E_m/E_p$ ), strength ( $\sigma_m/\sigma_p$ ), and energy release rate ( $\Gamma_m/\Gamma_p$ ). The energy release rate is defined as  $\Gamma = \sigma^2 l_0 / (2E)$ , where  $l_0$  is the characteristic length in the DEM. To isolate intrinsic interfacial effects from structural factors, we fix the microplatelet aspect ratio at  $\lambda = 10$ , a value exceeding the critical aspect ratio ( $\lambda^* \approx 3.2$ , eqn (2)), beyond which variations become negligible. By eliminating geometric variability, our simulations clearly reveal how matrix and microplatelet property contrasts govern crack deflection.

Fig. 3a illustrates the energy-governed phase diagram for crack-deflection behavior across ceramic matrices. Unlike conventional criteria, where crack deflection transitions to penetration at  $\Gamma_m/\Gamma_p = 0.25$  regardless of stiffness, this boundary broadens significantly for low-stiffness matrices ( $E_m/E_p < 1$ ) due to elastic mismatch between matrix and microplatelets. Eqn (4) with  $\eta = 0.125$  fits this widened boundary well, indicating that large elastic mismatch between microplatelet and matrix enhances the critical energy release rate of the matrix. Similarly, Fig. 3b presents the strength-governed phase diagram, where the transition boundary follows  $\sigma_m/\sigma_p \approx 0.45(E_m/E_p)^{0.375}$  (eqn (5)). For matched stiffness  $E_m/E_p = 1$ ,  $\sigma_m/\sigma_p \approx 0.45$  aligns with prior FEM results,<sup>40</sup> but incorporating elastic mismatch reduces the exponent from 0.5 to 0.375, further raising the critical strength ( $\sigma_m$ ) of the matrix. Consistent with these maps, the DEM snapshots in Fig. 3c–e show the corresponding crack paths in sequence: deflection (Fig. 3c), a mixed mode that combines interfacial deflection with kinked penetration (Fig. 3d), and penetration (Fig. 3e). The improvement in both critical release rate and failure strength for crack deflection reveals that optimal strength and toughness of AMCs are achieved with a low-stiffness matrix. At the optimal matrix condition defined by eqn (7), the mixed-crack mode in Fig. 3d lies on the boundary between deflection and penetration, representing the predicted balance of strength and toughness.

To validate this concept, we examine the load-displacement behavior of the unit cell using DEM simulations (Fig. 4). Fig. 4a presents representative stress-strain responses for three failure modes. In the crack penetration mode ( $\sigma_m/\sigma_p = 0.3$ ), the unit cell exhibits linear-elastic behavior with high strength but abrupt failure. In the crack deflection mode ( $\sigma_m/\sigma_p = 0.2$ ), nonlinear deformation occurs, featuring a brief plastic-like plateau and lower failure strength, attributed to interfacial crack propagation. By contrast, for the mixed-crack mode ( $\sigma_m/\sigma_p = 0.22$ ), the unit cell combines high failure strength comparable to that of crack penetration with nonlinear deformation, enabling simultaneous strength and toughness enhancement. The critical length of interfacial cracks in the crack-deflection mode depends on the microplatelet aspect ratio and saturates at  $\lambda = 17\lambda^*$ .<sup>33,42</sup> Once cracks spread throughout the interface, the stress in the unit cell rapidly decreases to a low level due to limited interlayer sliding resistance. In the mixed-crack mode, the crack initiates and propagates along the interface (Fig. 4b), producing the plastic plateau in Fig. 4a, and then deflects into the microplatelet, causing a sudden stress increase. However,





**Fig. 3** Deformation modes of bioinspired AMCs for different ceramic matrices. (a) Phase diagram based on the energy criterion and (b) phase diagram based on the strength criterion, both plotted against the ratio of Young's modulus ( $E_m/E_p$ ) between the ceramic matrix and microplatelets at an aspect ratio of  $\lambda = 10$ . Black lines are theoretical prediction from the load-transfer model, and red lines reflect modification due to elastic mismatch between the microplatelet and matrix. (c)–(e) Representative deformation modes obtained from DEM simulations: (c) crack deflection, (d) mixed crack, and (e) crack penetration. Markers: squares = deflection, triangles = mixed, circles = penetration. Labeled matrix points (e.g.,  $\text{SiO}_2$ ,  $\text{B}_2\text{O}_3$ ) are compiled from the literature; the underlying values and sources are provided in the Table 1.

microplatelet fracture in this mode reduces interlayer sliding distances compared to pure crack deflection, which in turn lowers energy dissipation efficiency. These results demonstrate that mixed-crack behavior achieves an optimal compromise, balancing strength retention with moderate toughening.

Building on the phase diagrams in Fig. 3, which define the regimes of crack deflection and penetration, we quantitatively map how these crack modes govern the failure strength and effective toughness of AMCs across a range of matrix properties (Fig. 4c and d). The contour plot for failure strength (Fig. 4c) reveals that low-stiffness matrices ( $E_m/E_p < 0.2$ ) maximize failure strength, a trend consistent with eqn (6), where strength scales inversely with  $(E_m/E_p)^{0.125}$ . This behavior stems from the inherent defect sensitivity of ceramics: low-stiffness matrices mitigate stress concentrations in tension zones, as evidenced by DEM-derived strain fields showing increasingly uniform stress distribution as matrix stiffness decreases (Fig. 4e). The effective toughness contour (Fig. 4d) peaks near the crack-deflection transition boundary (white dashed line, eqn (7)), where mixed-crack modes combine high strength with extended nonlinear deformation (Fig. 4b), enabling substantial energy dissipation. Notably, high-stiffness matrices within the crack-deflection regime yield suboptimal toughness despite extended interfacial crack propagation and sliding (eqn (S7)), as excessive stiffness restricts stress redistribution and limits strength.

By synergizing the complementary benefits of a low-stiffness matrix, which redistributes stress to mitigate concentration and improve failure strength, and a low-toughness matrix, which deflects cracks and dissipates energy through interfacial cracking, we demonstrate that bioinspired AMCs attain optimal

strength and toughness when the matrix combines low stiffness and controlled low toughness (Fig. 4a and b). DEM simulations identify the ideal matrix properties as  $E_m/E_p = 0.2$  and  $\sigma_m/\sigma_p = 0.22$  for  $\lambda = 10$ . Compared to bulk ceramics ( $E_m/E_p = \sigma_m/\sigma_p = 1$ ), this design yields a 15% strength improvement and a 2-fold toughness enhancement. Crucially, the small critical aspect ratio ( $\lambda^* \approx 3.2$ , eqn (2)) ensures that optimal performance is largely independent of the aspect ratio ( $\lambda$ ) of the microplatelet, simplifying scalable fabrication. The optimal matrix must satisfy the following condition:

$$\frac{1}{4} \leq \frac{\Gamma_m}{\Gamma_p} < \frac{1}{4} \left( \frac{E_p}{E_m} \right)^{2\eta} \quad \text{or} \quad 0.45 \left( \frac{E_m}{E_p} \right)^{\frac{1}{2}} \leq \frac{\sigma_m}{\sigma_p} < 0.45 \left( \frac{E_m}{E_p} \right)^{\frac{1}{2}-\eta}, \quad (8)$$

where  $\eta = 0.125$  for our 2D DEM simulations. This criterion balances stress homogenization and crack deflection, providing a universal guideline for designing high-performance AMCs.

With the optimal matrix condition identified from unit cell, we now examine how interface design controls crack propagation in finite domains, using DEM to resolve deflection, penetration, and mixed modes under tensile loading at fixed  $E_m/E_p = 0.2$  while varying  $\sigma_m/\sigma_p$ .

### 3.2. Tuning fracture propagation through interface design

Fig. 5a illustrates crack propagation under tensile loading (mode I crack) for matrices with  $E_m/E_p = 0.2$ , simulated in a  $6 \times 18$  unit-cell domain to capture full crack evolution. For a low-strength matrix ( $\sigma_m/\sigma_p = 0.2$ ), crack deflection dominates, initiating branching and microplatelet bridging *via* pullout



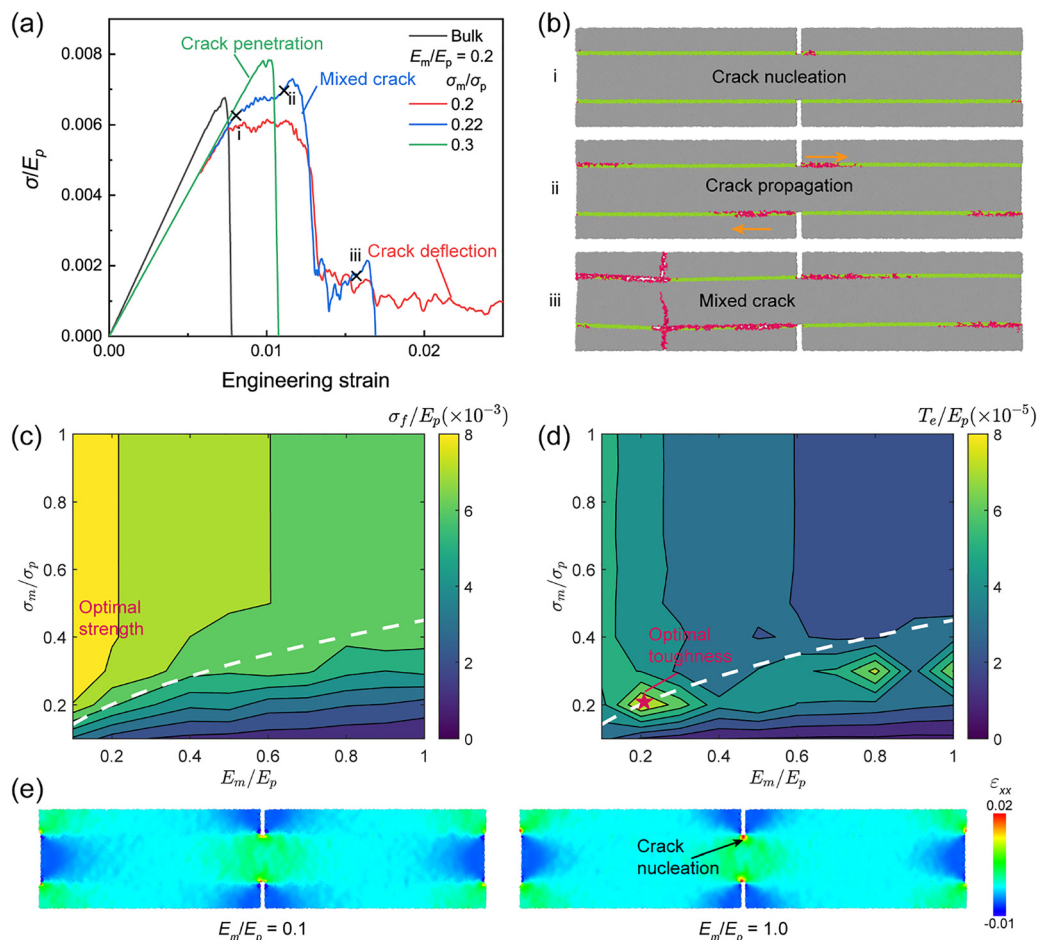


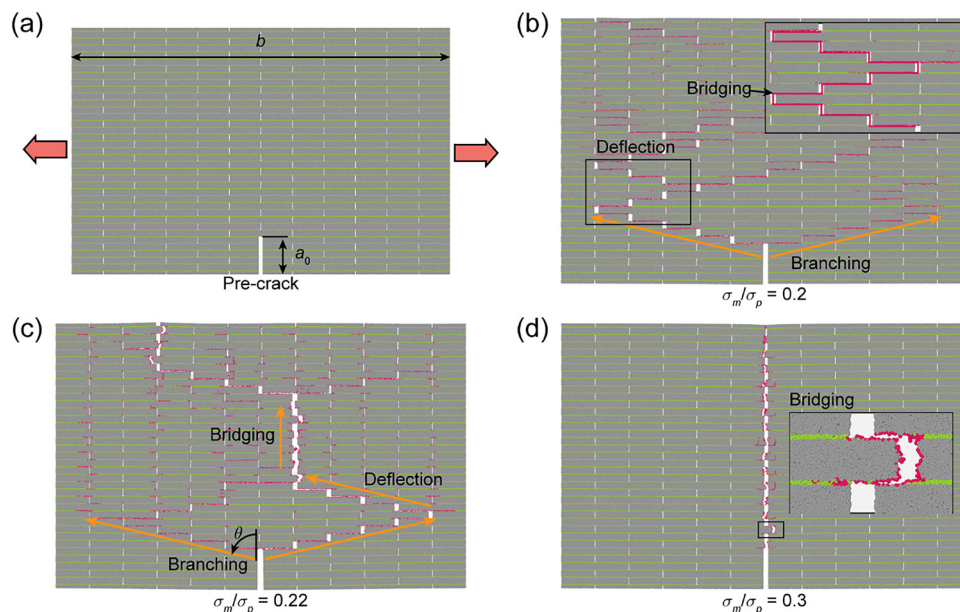
Fig. 4 Mechanical responses of bioinspired AMCs derived from DEM simulations. (a) Normalized tensile stress–strain curves of the unit cell under various ratios of matrix-to-microplatelet fracture strength ( $\sigma_m/\sigma_p$ ) at  $E_m/E_p = 0.2$ . The vertical axis is  $\sigma/E_p$  (stress normalized by the platelet Young's modulus  $E_p$ ). (b) Initial, propagating, and evolving stages of crack formation in the mixed-crack mode. (c) Normalized failure strength ( $\sigma_f/E_p$ ) and (d) effective toughness ( $T_e/E_p$ , defined as the area under the stress–strain curve) of the unit cell for different matrices at  $\lambda = 10$ . The white dashed lines mark the deflection–penetration boundary predicted by eqn (7) (the optimal matrix condition). (e) Strain colormap ( $\epsilon_{xx}$ ) under critical loading for various  $E_m/E_p$  ratios in the unit cell.

(Fig. 5b, Video S1), a hallmark of extrinsic toughening. For a transitional-strength matrix, ( $\sigma_m/\sigma_p = 0.22$ ), mixed-crack modes emerge (Fig. 5c, Video S2), combining bridging, deflection, and microplatelet fracture to enhance both strength and toughness. However, for a high-strength matrix ( $\sigma_m/\sigma_p = 0.3$ ), crack penetration prevails (Fig. 5d), though residual bridging in the low-stiffness matrix marginally improves toughness. Crack deflection angles  $\theta$  depend on the microplatelet aspect ratio  $\lambda$ , following  $\theta = \arctan \lambda/2$ , yielding  $\theta = 78.7^\circ$  for  $\lambda = 10$ , consistent with experimental observations.<sup>19,43</sup> These results confirm that staggered microstructures, coupled with tailored interfaces, activate synergistic toughening mechanisms, such as crack deflection, branching, bridging, and interlayer sliding, to overcome the brittleness of ceramics.

To elucidate the toughening mechanisms, we analyze the fracture resistance ( $R$ -curves) of bioinspired AMCs with varying matrices ( $E_m/E_p = 0.2$ ) using DEM simulations (Fig. 6). Energy dissipation in staggered microstructures is quantified *via* the  $J$ -integral derived from stress–strain curves (Fig. 6a). Owing to the path independence of the  $J$ -integral, we compute it along

contours surrounding the crack tip, avoiding stress singularities.<sup>19</sup> Crack extension ( $\Delta a$ ) is measured through image analysis of crack length at incremental strain steps. Compared to bulk ceramics, AMCs with low-stiffness matrices exhibit higher failure strains ( $\sigma_m/\sigma_p = 0.3$ ), which further increase under crack deflection ( $\sigma_m/\sigma_p = 0.2, 0.22$ ). While initial fracture toughness improves for  $\sigma_m/\sigma_p = 0.3$  (Fig. 6b), limited crack extension reflects predominantly linear crack growth. Conversely, crack deflection amplifies  $\Delta a$  by up to 16-fold for  $\sigma_m/\sigma_p = 0.2$  and 6-fold for  $\sigma_m/\sigma_p = 0.22$ , driving significant energy dissipation and pronounced  $R$ -curve toughening (Fig. 6b). Remarkably, despite employing brittle matrices, AMCs achieve plastic-like deformation through interfacial crack propagation and interlayer sliding—mechanisms that mimic ductility in inherently brittle systems. These findings align with experimental observations: pre-cracked AMC samples exhibit plastic-like stress–strain responses due to local toughening mechanisms, while flexural tests retain brittle failure dominated by bulk material behavior.<sup>44</sup>





**Fig. 5** Crack propagation in bioinspired ceramics under different matrices with  $E_m/E_p = 0.2$ . (a) DEM simulation model of a staggered structure subjected to mode I loading with an initial pre-crack of length  $a_0$ , and  $b$  is the specimen width as labeled in the schematic. (b)–(d) Crack paths for  $\sigma_m/\sigma_p = 0.2$  (b), 0.22 (c), and 0.3 (d), with the crack region highlighted in red.  $\theta$  is the crack-deflection angle measured by averaging the initial three interface turns. All simulations share the same geometry and pre-crack  $a_0$  (aspect ratio  $\lambda = 10$ ). An inset in panel (d) illustrates microplatelet bridging in the crack-penetrate case.

These trends are quantified by evaluating the damage ratio, defined as the fraction of broken bonds relative to the total number of bonds, from DEM simulations. Fig. 6c demonstrates stark contrasts: bulk ceramics exhibit minimal damage ratio (0.06%), consistent with a straight crack path; crack penetration raises damage ratio to 0.19% *via* localized microplatelet bridging; and crack deflection amplifies damage to 2.1% due to widespread crack paths and the damage processing zone. In the crack deflection mode ( $\sigma_m/\sigma_p = 0.22$ ), we classify crack growth using an energy-consistent proxy based on the evolution of damage with applied strain rather than the force maximum: stable stage corresponds to a gradual, distributed increase in damage; unstable stage is identified by a sharp surge in damage within a small strain increment and the emergence of a spanning microcrack cluster (see Video S1). Using this criterion, about 10% of the total damage accrues in stable stage and  $\sim 90\%$  during unstable stage (Fig. 6c). Notably, exceeding the peak load does not by itself imply instability; stable extension can persist post-peak when the material's crack-growth resistance ( $R$ -curve) rises faster than the applied driving force. Within this framework, crack deflection achieves substantial energy dissipation through distributed interfacial damage and bridging prior to coalescence, consistent with toughening mechanisms reported for ceramics and layered composites.<sup>22,29,43</sup> Critically, matrix damage ratio constitutes  $\sim 70\%$  of total damage ratio in crack-deflection modes (Fig. 6d), underscoring the decisive role of interfacial properties in enhancing fracture toughness.

Adopting a hierarchical toughening perspective for nacre-like composites,<sup>22,39</sup> we estimate a size-dependent amplification by linking unit-cell work-of-fracture gains to the crack-

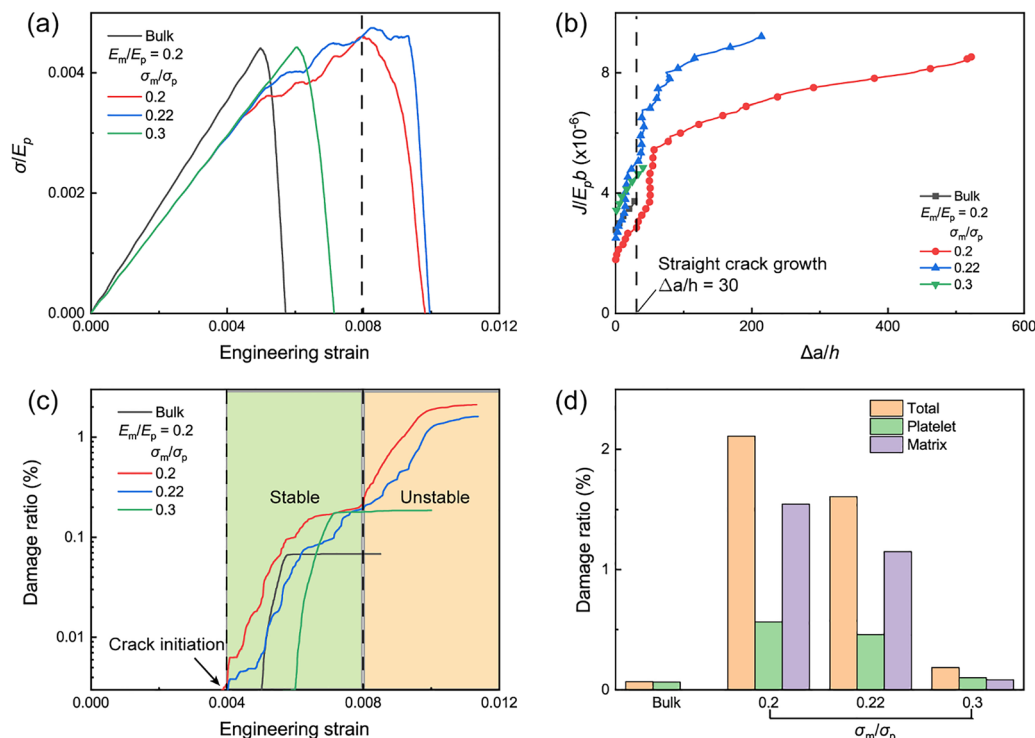
extension window quantified in Fig. 6. Following this view, local gains accumulate as the crack engages successive repeats along its deflected path. Our DEM indicates a  $\sim 2\times$  local (unit-cell) gain for  $\lambda = 10$ ; when deflection engages  $n$  repeats, the macroscopic amplification is roughly approximated by  $TAF \approx 1 + 2nf_s$ , where  $f_s$  is the fraction of stable extension contributing to the rising  $R$ -curve. From Fig. 6b, deflection enlarges  $\Delta a$  by  $\sim 6\times$  relative to a straight path and allocates  $\sim 10\%$  of damage to the stable stage, giving  $TAF \approx 1 + 2 \times 6 \times 0.10 \approx 2.2$  within our DEM window. As the process zone spans more repeats in larger AMCs (e.g.,  $n \sim 100$ ), the same linear accumulation gives  $TAF \approx 1 + 2 \times 100 \times 0.10 \approx 21$ , consistent with hierarchical models in which cooperative deformation across repeats raises toughness with structural extent and with extrinsic toughening frameworks that link rising  $R$ -curves to process-zone growth.<sup>45</sup>

This hierarchical toughening perspective demonstrates that macroscopic performance scales with the number of engaged unit cells, indicating that the theoretical performance limits of AMCs are not solely intrinsic to the constituent materials but are emergent properties of the architectural design and the interface-engineered crack path. To translate this principle into practical guidelines, we next apply our optimization framework to a representative class of high-performance ceramic systems.

### 3.3. Application to nacre-like alumina ceramics

To illustrate the proposed optimization framework, we consider alumina AMCs integrating various brittle matrices, including  $\text{TiO}_2$ ,  $\text{MgO}$ ,  $\text{SiO}_2$ ,  $\text{ZrO}_2$ , and  $\text{B}_2\text{O}_3$ , systems extensively characterized in prior experimental studies (Table 1).<sup>9,14–17</sup> For simplicity, the volume fraction of alumina microplatelets is fixed at





**Fig. 6** *R*-curve behavior of bioinspired ceramics under different matrices at  $E_m/E_p = 0.2$ . (a) Normalized stress–strain curves for the notched staggered structure: vertical axis is  $\sigma/E_p$  (stress normalized by the platelet Young's modulus  $E_p$ ). All simulations use an initial pre-crack of length  $a_0$ . (b) Normalized *J*–*R* response: vertical axis is  $J/(E_p b)$ , where *J* is the *J*-integral,  $E_p$  is the platelet Young's modulus, and *b* is the specimen width (as in Fig. 5a). The horizontal axis is crack extension  $\Delta a$ , defined as the increase in the main-crack length measured by image analysis. (c) Damage ratio versus strain: vertical axis is  $100\times$  (broken bonds/total bonds) expressed as a percentage. The green region denotes stable crack growth, while the orange region denotes unstable crack growth. (d) Damage breakdown versus strain using the same color code as in (c): orange = total damage, green = platelet damage, purple = matrix damage.

$\Phi = 0.9$ , consistent with experimental ranges (85–95%).<sup>13</sup> Given the prevalence of critical stress intensity factor ( $K_{Ic}$ ) measurements in ceramics research, we approximate the energy release rate as  $\Gamma = K_{Ic}^2/E$  for brittle ceramics under plane-stress condition. On this basis, the energy criterion can be recast as

$$\frac{K_{Ic}^m}{K_{Ic}^p} \leq 0.45 \left( \frac{E_m}{E_p} \right)^{\frac{1}{2}-\eta}, \quad (9)$$

where  $K_{Ic}^m$  and  $K_{Ic}^p$  are the critical stress intensity factors of the matrix and microplatelet, respectively. To bridge theory with experimental practice, where fracture toughness is typically measured under plane-strain conditions, we refine the Young's modulus ( $E' = E/(1 - \nu^2)$ ) in eqn (9) to account for Poisson's ratio differences between the microplatelets and matrix. While this introduces minor adjustments to the exponent  $\eta$ , the criterion retains validity under plane-strain constraints, ensuring fail-safe design irrespective of component geometry or loading conditions.

We first examine the strength limit of alumina AMCs. Eqn (6) indicates that the maximum strength of staggered microstructures depends on the intrinsic fracture strength of alumina microplatelets. For example, alumina- $B_2O_3$  AMCs exhibit flexural strengths of  $\sim 710$  MPa,<sup>15</sup> significantly below

the theoretical tensile strength of alumina microplatelets  $\sigma_{th} \approx 5$  GPa. This discrepancy arises because the experimental microplatelet thickness often exceeds  $1 \mu m$ ,<sup>13</sup> far surpassing the flaw-insensitive critical thickness  $h^* \approx 300$  nm, thereby introducing size-dependent weakening. Reducing microplatelet thickness below  $h^*$  could elevate the strength limit of alumina AMCs to  $\sim 2.25$  GPa. By comparison, the fracture toughness of monocrystalline alumina is highly anisotropic, with a critical energy release rate of approximately  $40 \text{ J m}^{-2}$  or higher when cleaving along the *c*-plane (0001), yet in the range of  $7\text{--}24 \text{ J m}^{-2}$  when cleaving along the *a*-plane (1 $\bar{2}$ 10) or *m*-plane (1 $\bar{1}$ 00).<sup>49,50</sup> Using  $\Gamma_p = 7\text{--}24 \text{ J m}^{-2}$  and  $h = 1.2 \mu m$ ,<sup>19</sup> eqn (6) predicts  $\sigma_f \approx 893\text{--}1654$  MPa for crack penetration. For alumina- $B_2O_3$  AMCs, the interface properties govern AMC failure strength. Using  $\Gamma_m = 2\text{--}4 \text{ J m}^{-2}$ ,<sup>19</sup> eqn (1) yields  $\sigma_f \approx 716\text{--}1013$  MPa, slightly exceeding experimental values. This overestimation may stem from microplatelet misorientation, a random staggered microstructure, and porosity in actual experiments.

To address the prevalent issue of microplatelet thickness exceeding the critical flaw-insensitive threshold ( $h^* \approx 300$  nm) in AMCs, we propose three strategies to enhance failure strength: (1) introduce a low-stiffness matrix to redistribute stress and mitigate tension-zone concentrations (Fig. 2b). For example, DEM simulations predict a 30% strength increase in







21.8 for alumina AMCs under current experimental protocols. Framed in the metamaterials context, these results show that tuning ceramic–ceramic interfaces directly programs the crack path and the rising *R*-curve, enabling programmable, damage-tolerant responses in all-ceramic, nacre-like architectures. The resulting design map provides actionable targets for materials selection and processing, helping bridge biological inspiration and scalable ceramic fabrication.

## Author contributions

Zezhou He: conceptualization, methodology, software, validation, investigation, writing – original draft, writing – review & editing. Rohit Pratyush Behera: experimental investigation, writing – original draft, writing – review & editing. Huajian Gao: conceptualization, writing – review & editing, supervision. Hortense Le Ferrand: conceptualization, writing – review & editing, supervision.

## Conflicts of interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Data availability

The data supporting this article have been included as part of the supplementary information (SI). The supplementary information file contains additional details on the shear-lag model, fracture-mechanics derivations, and discrete-element simulations (including model parameters); Fig. S1–S2, which illustrate the staggered platelet–matrix unit cell, interface mechanics, and modulus-mismatch scaling from DEM; Tables S1–S2, which compile the specific strength and toughness data used in Fig. 1 and provide a glossary of symbols and variables; and supplementary videos S1–S2, which show representative crack paths and process-zone evolution in the DEM simulations. See DOI: <https://doi.org/10.1039/d5mh01962a>.

## Acknowledgements

The authors acknowledge funding from the Ministry of Education of Singapore (award MOE-T2EP50122-0021). The computational work for this article was fully performed on resources of the National Supercomputing Centre, Singapore (<https://www.nsc.sg>).

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