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Raising the benchmark potential of a simple alcohol-ketone intermolecular balance†

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2-Butanone offers two hydrogen bond docking variants to a solvating methanol which are cleanly separated by supersonic jet infrared absorption spectroscopy in the OH-stretching range, resolving earlier action spectroscopy indeterminacies for this elementary case of an intermolecular alcohol-ketone balance. The solvent preference for the shorter chain side is unambiguously derived from the spectra of homologous compounds. It is analysed in terms of competing steric and dispersion interactions and the resulting energy differences across a low interconversion barrier. Fortuitous cancellations are discussed and quantitative energy deficiencies of the employed DFT approaches are suggested. Some benchmarkable experimental observations: at low temperature, a single methanol molecule prefers the methyl-sided oxygen lone pair of 2-butanone over the ethyl-sided lone pair by 1–2 kJ mol⁻¹, the *trans* butane backbone is conserved in both low-lying isomers, the OH-stretching fundamentals differ by 47(2) cm⁻¹.

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1 Introduction

The hydrogen bond topology around C=O groups is diverse^{1,2} and highly relevant for the solvation of biomolecular model systems.³ Towards a reliable theoretical description of this solvation process, it is important to quantitatively model the first solvation step.⁴ It is essential to understand any potential error compensation between different intermolecular interactions⁵ which may break down when the system size is increased. Such competing intermolecular forces include London dispersion⁶ and it is attractive to study small systems with a controlled balance between hydrogen bonding and London dispersion.

Unsymmetrically substituted ketones offer the possibility to investigate whether a protic solvent molecule prefers one substitution side or the other (see Fig. 1), a situation which has been termed an intermolecular balance or scale.⁷ This preference may either result from a symmetry breaking of the lone electron pairs at the oxygen themselves, due to induction effects along the chemical bonds, or – more likely – from the different repulsive and attractive environment of the two non-equivalent docking half-spaces. Therefore, such unsymmetric ketones provide a unique opportunity to probe the interplay of intermolecular interactions on a very subtle level, if the two docking isomers can be spectroscopically distinguished, *e.g.* by vibrational

spectroscopy of the protic stretching mode of the solvent. This is only feasible at low temperatures and to avoid interference from the environment it should be attempted in vacuum, by studying isolated 1:1 complexes of one ketone molecule and one solvent molecule.⁸ The standard way to prepare such complexes is supersonic jet expansion,^{9,10} but this is a non-equilibrium method which may freeze competing conformations rather than equilibrating them in the course of collisional cooling across the isomerisation barrier. Therefore, such an experiment only reflects the docking preference near a conformational freezing temperature⁷ T_c , below which the barrier becomes unsurmountable on the time scale of the adiabatic jet expansion. Annealing processes like in weakly interacting matrix isolation are not possible.¹¹ Softer degrees of freedom like rotation, intermolecular vibration or translation may however be further cooled, simplifying the spectra. Excitation in stiff vibrations is depopulated inefficiently, but this is of minor concern if the initial temperature of the molecules is sufficiently low.

Therefore, one can idealise the outcome of a diluted supersonic co-expansion of a ketone with a protic solvent as the preparation of a single 1:1 complex for symmetric ketones and of two 1:1 complex isomers (see Fig. 1) for an unsymmetric ketone,^{8,12} the ratio of which depends on their energy difference and the barrier separating them. This isomerisation barrier is fairly transmissible for simple ketones. It involves a range of path options for the solvent over the top of the keto group or leaving the ketone plane, and none of these paths requires an intermediate breaking of the hydrogen bond.

Without a detailed simulation of the cooling process, it is difficult to predict the kinetic hindrance of the barrier, but

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Fig. 1 Schematic illustration of the two possible docking variants 5 and 5' of methanol (MeOH) to the oxygen lone pairs of an ethyl ketone (with Me for methyl and Et for ethyl on the other side) and relevant angles as well as alkyl torsion. For symmetric substitution the docking positions become spectroscopically indistinguishable.

based on several examples where such bistable complexes with low intermolecular barrier have been investigated in mild carrier gas expansions through room temperature slit nozzles, the conformational freezing temperature has been bracketed between about 20 K and 100 K for very low barriers,^{4,13} between 30 K and 150 K across barriers typical for ketone lone pair switching,¹² or more generously between 20 K and 200 K.⁷ This uncertainty does not allow to extract very quantitative information about the energy difference between the docking isomers, but decisions about the energy sequence can usually be made, even for fairly small differences on the order of 1 kJ mol⁻¹ or less. Gross errors in the size of the barrier can also be uncovered, if the spectral intensity information is reliable. Energy differences of more than 3 kJ mol⁻¹ can usually be safely ruled out if both isomers are clearly observed and if there is no reason for an untypically high interconversion barrier and thus conformational freezing temperature.

The driving energy difference may be affected by different amounts of zero-point vibrational energy (ZPVE) in the isomers, but this effect is usually minimised for ketones, where the local hydrogen bond environment is almost the same on both sides. However, such a theory-favourable cancellation always needs to be checked. If it works, energy decomposition models^{14–16} can be directly interrogated to explain the energy imbalance in terms of London dispersion and other contributions, although one should always keep in mind that there is more than one way to decompose the observable total interaction energy into components. Error cancellation also helps in comparing observed (anharmonic) spectral shifts between isomers to the usual harmonic predictions, but again, one cannot expect perfect performance and must rely on trends across several systems. Deficiencies in the typically used DFT approaches^{8,12} can be further uncovered by single point energy calculations at higher levels of electronic structure theory.

Given all these caveats, it makes sense to investigate the simplest realistic model systems for ketone intermolecular balances in particular detail, to better understand the larger systems which start to be dominated by London dispersion interaction.¹⁷ The simplest unsymmetric ketone which comes

to mind is 2-butanone or methyl ethyl ketone (MEK). 2-Butanone is favourable because it is predominantly monocoformational, disregarding a slight symmetry breaking into a pair of rapidly interconverting enantiomeric conformations.^{18–20} Its 1:1 complex with the simplest alcohol methanol has been studied experimentally before,²¹ but possibly due to the action character of the employed IR-VUV double resonance technique, only a broad (109 cm⁻¹ FWHM) OH-stretching band was observed, likely spanning the two docking sides of interest. This was attributed by the authors to fluxionality of the observed species, which were theoretically characterised at DFT level without including dispersion corrections. As we had not observed such broad bands in related systems^{8,12} and found dispersion correction to be essential, we decided to reinvestigate this model system using linear FTIR spectroscopy in supersonic jets.²²

In this work, we show by comparison to homologous systems that the two docking sides of 2-butanone for methanol are separable and assignable by infrared spectroscopy. We investigate different theoretical approaches with respect to their quantitative deficiencies and error cancellations in describing the experimental findings. Thus, we endow this attractive model system²¹ with further theory benchmarking potential.

2 Materials and methods

2.1 Experimental methods

Gaseous mixtures of 2-butanone (Sigma-Aldrich, ≥99%) or 3-pentanone (Sigma-Aldrich, ≥99%) with methanol (Roth, >99.9%) were prepared in a large excess of helium (Linde, 99.996%) in a 67 L reservoir at typically 0.75 bar stagnation pressure and expanded over six magnetic valves through a pre-expansion chamber and a 600 mm × 0.2 mm slit nozzle into vacuum. Large (24 m³) buffer volumes and continuous pumping at 500 to 2500 m³ h⁻¹ kept the background pressure sufficiently low while the expansion was probed at a resolution of 2 cm⁻¹ using a Bruker 66v/S FTIR spectrometer, a 150 W tungsten lamp, CaF₂ optics and a liquid nitrogen cooled InSb detector. Detailed descriptions of the setup can be found elsewhere.²²

Spectra of the OH/CH stretching region were co-averaged over 125 to 550 pulses to obtain sufficient signal-to-noise ratios. Cluster size and composition estimates were obtained by concentration variation through temperature control of liquid samples in the gas flow. The abundance of homodimers and oligomers was minimised by methanol dilution to the extent which was achievable with the liquid saturator supply. Towards docking ratio estimates, experimental band integral ratios were determined using a modified automated statistical evaluation.^{23,24} Integration windows between 4 and 12 cm⁻¹ around the band maxima were statistically varied and synthetic noise appropriate for the instrument characteristics was added. Where band overlap with methanol dimer²⁵ was an issue, dimer-subtracted spectra were also explored. For raw data, see <https://doi.org/10.25625/2HXVYM>.



2.2 Theoretical methods

The dispersion-corrected B3LYP^{26–28} hybrid functional is primarily used for band assignment purposes and sometimes compared to a functional (X3LYP) used in the VUV study²¹ and claimed to be particularly suitable for intermolecular interactions. In the spirit of a benchmark experiment, the exploration of other functionals is invited to minimise some of the deficiencies which are identified in this work. For the GGA functional BP86,^{26,29} some results are given in the ESI† For manual structure searches, a def2-TZVP basis set³⁰ was employed and the D3 dispersion correction³¹ with Becke–Johnson damping^{32–35} was used with its three body term. CREST³⁶ structure screenings complemented the manual search. Re-optimisations were performed with the extended B3LYP-functional X3LYP³⁷ with D3 correction,³⁸ and for comparison to the VUV study²¹ also without dispersion correction. Electronic energy differences were recalculated at single-point DLPNO-CCSD(T) level^{39–41} for some DFT-optimised structures.

Most calculations were carried out using ORCA version 4.2.1,⁴² relaxed torsional scans of monomer and complex structures along with reaction path optimisations using Turbomole.^{43,44} Transition state structures were searched with the Turbomole tool Woelfling^{43,44} and re-optimised with ORCA.⁴² More information on the computational details can be found in Table S1 of the ESI† Due to the non-uniform cooling of different degrees of freedom during a supersonic jet expansion (10–20 K for rotation, 50–200 K for soft vibration, barrier-dependent for conformation) and the similarity of the interconverting species, partition functions were assumed to cancel between the different isomers and an effective Boltzmann conformational freezing temperature T_c was extracted from the predicted energy difference and the experimental population ratio. This serves to judge whether the predicted energy difference is realistic. Previous studies of ketone balances^{8,12} have suggested small net ZPVE corrections between the isomers, due to the strong similarity of the local hydrogen bond environment for the two oxygen lone electron pairs. Therefore, ZPVE correction was limited to the harmonic approximation and can even be neglected in several cases. A similar argument applies to IR OH-stretching downshift differences between isomers, where anharmonic effects are expected to cancel better than for the absolute shifts from the monomer to the complex, and much better than for absolute OH-stretching wavenumbers.

3 Results and discussion

3.1 Experimental assignment

To emphasise the benchmark experiment character of this study, the two docking isomers of the 1 : 1 complex of 2-butanone (methyl ethyl ketone, from now on MEK) with methanol (MeOH) shall be assigned purely experimentally. This is achieved by reference to the homologs 3-pentanone (ethyl ethyl ketone, from now on EEK) and acetone (methyl methyl ketone, from now on MMK), as shown in Fig. 2 in the IR spectral range where the hydrogen-bonded methanol OH-stretching fundamental is expected. At sufficient dilution, there is a single dominant peak for MMK (O_M) and EEK (O_E), as expected from the symmetry of the ketones and the



Fig. 2 Jet FTIR OH-stretching spectra of MEK, EEK and MMK⁴⁵ (scaled intensity) co-expanded with MeOH. Dashed lines connect analogous docking sites and lead to an unambiguous experimental assignment and preference for methyl side oxygen docking (O_M) over ethyl side docking (O_E) of MeOH to MEK. See Fig. S7 in the ESI† for more details.

dominance of a zig-zag or all-*trans* conformation of its alkyl backbone. For MEK, there are two peaks which are only slightly shifted from the symmetric MMK and EEK counterparts. O_M is significantly stronger than O_E , showing that MeOH prefers to dock on the methyl side, because the IR band strengths are unlikely to change much with alkyl substitution.⁸ The subtle spectral substitution shifts (dashed lines) can be rationalised in terms of the inductive effect of ethyl compared to methyl groups, which increases the hydrogen bond acceptor quality of the ketone and leads to a downshift of the coordinating OH vibration. In the following, this straightforward experimental assignment is further rationalised and analysed using quantum mechanical calculations, starting with DFT results.

3.2 DFT results

The B3LYP-D3 optimised ketone MeOH complex structures can be characterised by the hydrogen bond angle α and the dihedral angle τ (see Fig. 1). The angle $0^\circ \leq \alpha \leq 180^\circ$ (see however ref. 46) between the hydrogen bonded H and the C=O group describes the deviation from the sp^2 -like preference of 120° . τ represents the inclination of the alcoholic proton relative to the ketone plane (out-of-plane twist) and encodes the docking preference for unsymmetric ketones with the limiting values of 0° and 180° . This preference is sensitive to local hydrogen bonding and repulsion of the OH group, but also to distant attractive methyl group interactions with the ketone substituents. The resulting complex geometry affects the OH-stretching wavenumber of the hydrogen bonded OH. For MMK and EEK complexes the two docking variants are either identical or enantiomeric and thus give rise to a single signal.

However, the ethyl groups in MEK and EEK induce further isomerism, which is not very competitive in the monomers but may gain importance in the complexes.^{47,48} Besides the preferred



synclinal (s) orientation close to the ketone plane, a pair of anticlinal (ac) orientations rotated by about $\pm 127^\circ$ out of the ketone plane and, induced by the neighbouring keto group, another pair of clinal (c^{49}) orientations rotated by about $\pm 90^\circ$ is predicted for MEK and EEK monomers, connected by low torsional barriers and uphill by more than 5 kJ mol^{-1} from the *syn* form (see Fig. S1–S3 and Table S2 in the ESI[†]). These predictions are in qualitative agreement with previous spectroscopic and computational evidence.^{18,19,50}

Turning to the complexes with methanol, two distinguishable and almost isoenergetic isomers with s and c conformation on the docking side of MeOH are predicted for EEK (see Fig. 3). The solvent thus brings the c arrangement almost down to s, whereas the ac conformation is not predicted to be favourable. A somewhat less pronounced energy lowering of c towards s is predicted when MeOH docks on the ethyl or E side of MEK, but methyl side docking (M) is more attractive than either sE or cE in this case (see Fig. 3) and separated by an out-of-plane barrier typical for ketones^{8,12} (for more details see ESI[†] Fig. S5 and S6). The common energy lowering of cE towards sE for MEK and EEK is likely connected to London dispersion interaction of the lateral ethyl group with the alcohol in combination with a relaxed steric repulsion between the alkyl and the OH groups. The ZPVE changes significantly between the two variants so that theory should not be fully trusted on their energy sequence. On the other hand, the shallow barrier predicted between the competing structures (see Fig. 3) should allow the less favourable structure to relax into the more favourable isomer. Because they are expected to differ spectroscopically (*vide infra*), experiment provides a way to decide between the close competition in a kind of secondary intermolecular balance, now more strongly affected by zero point motion.



Fig. 3 Most stable conformers for MEK (upper panel) and EEK (lower panel) solvated by MeOH and the relevant transition states for the interconversion, calculated at B3LYP-D3(BJ,ABC)/def2-TZVP level. The *syn*-ethyl- or sE-sided and clinal-ethyl- or cE-sided structure motifs are predicted for both ketones. For the methyl- or M-sided MEK complex only the most stable *syn*-conformation is shown (see also ESI[†] Fig. S4 and Table S4).

While X3LYP-D3 calculations are consistent with the B3LYP-D3 findings (see Table S4 in the ESI[†]), leaving away the D3 correction (as was done in ref. 21) strongly raises the cE energy for EEK and MEK, qualitatively confirming the role of dispersion in stabilising cE. Interestingly, the energy difference between sE and M, *i.e.* the primary intermolecular energy balance, is hardly affected by the D3 correction. This is a case of fortuitous error cancellation between hydrogen bond, repulsion and different dispersion interactions, when methanol coordinates methyl ethyl ketone. It is also a consequence of the rather small size of the investigated ketone balance.

When the distant, non-solvated ethyl group of the ketone is rotated, the energetics is similar to that of the monomers, *i.e.* the *syn* form is without serious competition. Therefore, this distant *syn* conformation is always implied in the following (as in Fig. 3).

The predicted harmonic OH-stretching wavenumber of the isomers is strongly influenced by the hydrogen bond angle α . If it is close to 120° as in M and cE, the OH stretch has a low wavenumber, even lower for cE than for M. The sE conformation pushes the OH group further away ($\alpha > 130^\circ$, see Table S3 in the ESI[†]) and this leads to a predicted blueshift, which aids in the spectral assignment (see Fig. 2). The experimental quantification of isomers profits from robust IR absorption cross-section ratio predictions. As shown in Table S6 in the ESI[†], their functional dependence is moderate in the harmonic approximation, as in other ketone balances.^{8,12}

3.3 Comparison to experimental results

In Fig. 4 the OH-stretching region of MeOH expanded with MEK (top, blue) or EEK (bottom, red) is shown. The monomer signal (MeOH) with its rotational-tunneling substructure and

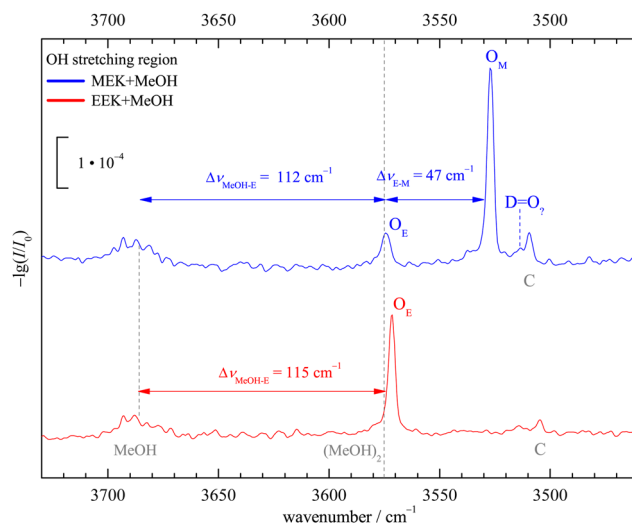


Fig. 4 Jet FTIR OH-stretching spectra of MeOH in co-expansion with MEK and EEK including the MeOH monomer region. C marks a non 1:1 stoichiometry and D=O₂ is the largest isolated signal which might perhaps be attributed to a third 1:1 isomer in the MEK case, beyond the dominant O_M (M docking) and the secondary signal O_E (sE docking, common to both ketones). For details, see the main text.



traces of the downshifted donor mode⁵¹ of the homodimer (MeOH)₂ at 3575 cm⁻¹ are marked with black vertical dashed lines. The main signals O_M (only MEK) and O_E (both ketones, for MEK overlapping with methanol dimer traces²⁵) are caused by the 1 : 1 complexes and have been assigned in Fig. 2. They fit the ketone balance trend of the sterically less hindered side exhibiting a lower OH-stretching wavenumber^{8,12} and the theoretical harmonic wavenumber splittings (51–52 cm⁻¹, see Tables S5 and S8 in the ESI[†]) match the experimental one (47 cm⁻¹) quite well due to cancelling anharmonicity contributions, if the sE conformation is assumed. Assignment to the theoretically competing cE conformation would instead invoke an inverted splitting of –(16–17) cm⁻¹ which can be safely ruled out for O_E relative to O_M. At best, cE could be responsible for the weak D=O₂ signal. All these conclusions can be drawn directly from experimental intensities, as the expected visibility of the conformers is similar (see Table S6 in the ESI[†]) and the methanol dimer contribution is minor (as evidenced in the EEK trace and Fig. S9 and S14 in the ESI[†]). By either subtracting an upper bound of the methanol dimer contribution or else not subtracting any methanol dimer signal contribution at all, one can bracket the possible influence of methanol dimer on the conformational signal ratio. A wider perspective of the experimental spectra is given in Fig. S8 (ESI[†]).

Together with the low interconversion barrier between cE and sE, this spectral sensitivity allows for a rigorous experimental constraint which is currently not easy to reproduce robustly by theory. In the complex of MeOH with MEK, the sE arrangement is definitely more stable than the cE arrangement. Because the two significantly differ in their harmonic ZPVE (cE generating more ZPVE when embedding the MeOH unit), this is not a benchmark for electronic structure theory only. It requires a reliable ZPVE prediction for the complexes to match experiment for the right reason. The M-sE balance itself is much less sensitive to such ZPVE issues and can thus be used to test electronic structure predictions more or less directly, as in previous cases.^{8,12} The C signals at lower wavenumber common to both ketone methanol expansions can be attributed to a trimeric or higher complex species, as shown by concentration and stagnation pressure variation for the EEK (see Fig. S15 and S16 in the ESI[†]) and MEK case (see Fig. S10–S13 in ESI[†]) and in analogous cases.⁵² For the small MEK signal D=O₂, a decision between a trimeric complex and a 1 : 1 isomer is less clear, but in the analogous EEK case, trimeric contributions in that region can also be identified (see Fig. S16 in the ESI[†]) and suggest that relaxation of cE is nearly quantitative in the presence of MeOH, if it forms at all in the supersonic jet expansion. Once more, this indicates a sensitive benchmarking potential for combined electronic structure and nuclear zero point motion theory. If cE is predicted below sE in the MeOH complex of MEK at some level of computation, this is in stark contrast to experiment. As shown in Table S4 in the ESI[†], all explored DFT-D3 calculations make this prediction at the bare electronic structure level, but the problem is resolved by adding harmonic ZPVE. Interestingly, it is also resolved by removing the D3 correction, so that the experiment is sensitive to

overestimated D3 corrections. Because the D3 correction affects the cE–sE energy difference by as much as 2 kJ mol⁻¹, the sensitivity is moderate.

In Fig. 5 the downshifts relative to the MeOH monomer fundamental from experiment are plotted against harmonic def2-TZVP DFT predictions. Consistent with the known systematic overestimation of hydrogen bond-induced harmonic downshifts by most DFT methods, all data points stay below the ideal diagonal line. The discrepancy depends on the employed functional. Note that inclusion of anharmonicity likely increases that discrepancy further,⁵³ suggesting that it is an intrinsic deficiency of the functionals. This intrinsic deficiency is not only hidden by the neglect of anharmonicity, but also by the neglect of London dispersion correction (*vide infra*).

Data from previously published MeOH complexes of MEK analogues are included in Fig. 5 at the B3LYP-D3 level. The M-sided isomers (empty symbols) for MEK, acetophenone,⁸ pinacolone,¹² and MMK⁴⁵ cluster together, as expected when the molecular variation is on the distant end. Solvation on the non-M side (filled symbols) leads to larger variation, but the difference between sE for MEK, EEK and acetophenone is still small. The main outlier is the bulky pinacolone (tBMK), but that was shown to be partly remedied by using a def2-QZVP basis set.¹² Besides that outlier, the slope of the isomer-connecting lines remains similar, underscoring the observation that isomer splittings are predicted more reliably than monomer-referenced downshifts by harmonic DFT.

The trend for X3LYP-D3 is very similar, but with a larger shift from the diagonal, in line with intermolecular deficits noted before.³⁸ Leaving away the dispersion correction brings the data points closer to the diagonal. Together with the insensitivity of the M-sE splitting to dispersion correction and the experimental elusiveness of the dispersion-favoured cE structure, this might encourage the empirical use of raw hybrid

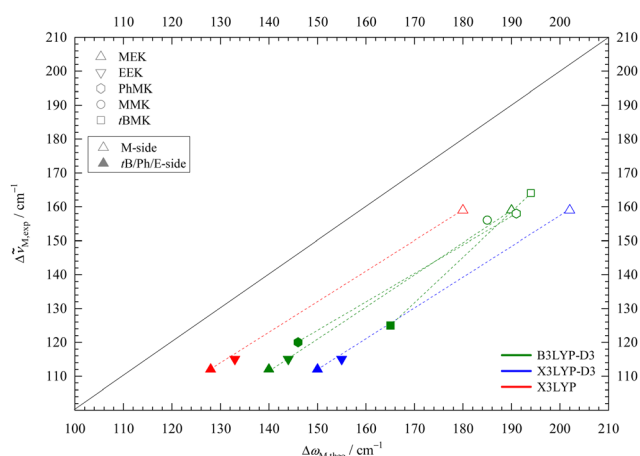


Fig. 5 Experimental (anharmonic) downshift $\Delta\tilde{\nu}_{M,\text{exp}}$ of MeOH in 1 : 1 complexes with EEK and MEK plotted against the harmonically calculated downshifts $\Delta\omega_{M,\text{theo}}$ for three different DFT/def2-TZVP variations. For comparison, published B3LYP-D3 values for acetophenone,⁸ pinacolone,¹² acetone⁴⁵ are included. Harmonic DFT overestimates wavenumber shifts uniformly, more so for X3LYP-D3 and less for bare X3LYP (even less for bare B3LYP, not shown).



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