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The three-center two-positron bond†

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Computational studies have shown that one or more positrons can stabilize two repelling atomic anions through the formation of two-center positronic bonds. In the present work, we study the energetic stability of a system containing two positrons and three hydride anions, namely $2e^+[H_3^{3-}]$. To this aim, we performed a preliminary scan of the potential energy surface of the system with both electrons and positrons in a spin singlet state, with a multi-component MP2 method, that was further refined with variational and diffusion Monte Carlo calculations, and confirmed an equilibrium geometry with D_{3h} symmetry. The local stability of $2e^+[H_3^{3-}]$ is demonstrated by analyzing the vertical detachment and adiabatic energy dissociation channels. Bonding properties of the positronic compound, such as the equilibrium interatomic distances, force constants, dissociation energies, and bonding densities are compared with those of the purely electronic H_3^+ and Li_3^+ systems. Through this analysis, we find compelling similarities between the $2e^+[H_3^{3-}]$ compound and the trilithium cation. Our results strongly point out the formation of a non-electronic three-center two-positron bond, analogous to the well-known three-center two-electron counterparts, which is fundamentally distinct from the two-center two-positron bond [D. Bressanini, *J. Chem. Phys.*, 2021, 155, 054306], thus extending the concept of positron bonded molecules.

1 Introduction

The techniques to accumulate and manipulate positrons¹ and positronium (Ps) atoms² at very low energies have opened up new research areas in molecular sciences. For instance, a great variety of positronic molecules have been produced and detected.³ In these experiments, positron attachment to vibrationally excited molecules gives rise to positronic compounds. The existence of a different kind of positronic molecules was predicted by Charry *et al.*⁴ based on computational simulations. Two otherwise repelling hydride anions can be bound by a positron, and the analysis of the positronic orbital suggested the formation of a positron covalent bond. Subsequent

computational studies conducted by Moncada *et al.*⁵ pointed out that similar bonds should also exist in positronic dihalides.

The positronic dihydride system, denoted as $e^+[H_2^{2-}]$, has attracted considerable attention. Goli and Shahbazian⁶ addressed the nature of the interaction employing Multi-Component Quantum Theory of Atoms in Molecules (MC-QTAIM). The authors concluded that the accumulation of positron density between the two nuclei would underlie the bonding process, acting as “a positronic glue” that converts the repulsive H_2^{2-} system into a stable one. The energy stability of positron-bonded dihydrides was further confirmed by quantum Monte Carlo (QMC) calculations performed by Ito *et al.*,⁷ Bressanini⁸ and Charry *et al.*⁹ Bressanini also concluded that the bonding is not limited to one positron and in later works¹⁰ he showed that two singlet-coupled positrons can form a bond between two hydride anions, thus giving rise to the $2e^+[H_2^{2-}]$ molecule, or simply $(PsH)_2$. The equilibrium internuclear distance was reduced from 6.4 bohr to 6.0 bohr as the number of positrons was increased from 1 to 2. Unexpectedly, the bond length shortening was accompanied by a reduction in the bond energy (BE), from 23.5 mE_h to 10.4 mE_h .

These fascinating theoretical results raise questions on how complex positron-bonded compounds can become, or on how far the analogy between electronic and positronic bonds can be stretched. Along these lines, Bressanini¹¹ recently reported the local energy stability of $3e^+[H_2^{2-}]$, or more simply $e^+[PsH]_2$, a stable molecular system containing three positrons, which

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can be understood as resulting from the reaction $(\text{PsH})_2 + e^+$. The present study further explores positronic bonding mechanisms beyond the previously studied two-center to three-center systems. Bressanini has conjectured that a system analogous to H_3^+ with three protons, six electrons, and two positrons, could be stable.^{10,11}

Based on high-level QMC simulations, we demonstrate that this conjectured system, denoted as $2e^+[\text{H}_3^{3-}]$, is energetically stable. Our results, obtained for the singlet state in the D_{3h} symmetry, point out the existence of a three-center two-positron (3c2p) bond that stabilizes three repelling hydride anions. To gain further insight into the 3c2p bond, we compare it against the analogous three-center two-electron bond 3c2e, which is a well established bonding mechanism found in purely electronic molecules.^{12–15}

The H_3^+ molecule is probably the best known example of 3c2e bonds,¹⁶ in view of its astrochemical relevance.^{17–19} While the trihydrogen cation could be rated the closest analogue of $2e^+[\text{H}_3^{3-}]$ at first glance, previous studies have consistently shown that the properties of electronic and positronic bonds are closest when the systems have isoelectronic ion cores.^{4,5} We therefore consider Li_3^+ as an alternative purely electronic analogue of the di-positronic tri-hydride compound for comparison of the bonding properties. Our results confirm that $2e^+[\text{H}_3^{3-}]$ is stable against dissociation into chemically meaningful products. The presently reported results, which indicate the existence of a new kind of di-positronic stable system, may hopefully expand the landscape of the field.

This paper is organized as follows: in Sec. 2 the methods and numerical procedures are summarized; the properties of the di-positronic system and the purely electronic analogues are presented and discussed in Sec. 3; concluding remarks and perspectives for future work are outlined in Sec. 4.

2 Methods

This study considers electrons and positrons as quantum particles and atomic nuclei as point charges within the Born–Oppenheimer approximation. Exploratory studies of the potential energy surface (PES) of the $2e^+[\text{H}_3^{3-}]$ system were performed at the MP2 level of theory. The MP2 expressions for systems composed of electrons and positrons can be found in ref. 20 and 21. Equilibrium energies and geometries were further refined with the variational Monte Carlo (VMC) and diffusion Monte Carlo (DMC) methods.

2.1 Quantum Monte Carlo methods

QMC methods are stochastic techniques employed to integrate the time-independent Schrödinger equation for a given trial wave function, the most common of which are VMC and DMC.^{22–24} The stochastic integration in VMC is carried out with the Metropolis–Hastings algorithm.^{25,26} The energy functional is evaluated over a trial wave function which is written as the product of a fermionic part, such as a Slater determinant, and a bosonic component, the Jastrow factor, used to describe explicit correlation between particles. The trial wave function

used in this study of electron–positron systems is written as the product

$$\Psi = \det[\mathbf{S}_{e\uparrow}] \det[\mathbf{S}_{e\downarrow}] \det[\mathbf{S}_{p\uparrow}] \det[\mathbf{S}_{p\downarrow}] e^J(\vec{r}, \vec{p}; \vec{R}), \quad (1)$$

where $\mathbf{S}_{e\uparrow}$ and $\mathbf{S}_{e\downarrow}$ are the electronic Slater matrices associated to the two spin populations, $\mathbf{S}_{p\uparrow}$ and $\mathbf{S}_{p\downarrow}$ are the corresponding matrices for the positrons, and e^J is the Jastrow factor. Several QMC studies have employed similar trial wave functions^{7,9,27–30} based on products of determinants constructed *via* atomic basis sets. This particular Jastrow factor was introduced in ref. 9 and it is now generalized for two-positron systems in the present work. The Jastrow factor is built as the sum

$$J(\vec{r}, \vec{p}, \vec{R}) = J_c^{\text{en}}(\vec{r}, \vec{R}) + J_c^{\text{pn}}(\vec{r}, \vec{p}, \vec{R}) + J_c^{\text{ee}}(\vec{r}) + J_c^{\text{pp}}(\vec{p}) + J_c^{\text{ep}}(\vec{r}, \vec{p}) + J_{3/4}(\vec{r}, \vec{p}, \vec{R}) \quad (2)$$

of five functions describing respectively the electron–nucleus ($J_c^{\text{en}}(\vec{r}, \vec{R})$), positron–nucleus ($J_c^{\text{pn}}(\vec{r}, \vec{p}, \vec{R})$), electron–electron ($J_c^{\text{ee}}(\vec{r})$), positron–positron ($J_c^{\text{pp}}(\vec{p})$) and electron–positron ($J_c^{\text{ep}}(\vec{r}, \vec{p})$) cusps, and a term that describes the dynamical correlation between the fermionic particles in the field of the nuclei ($J_{3/4}(\vec{r}, \vec{p}; \vec{R})$), which is an extension of the one defined in ref. 31. The functions used to describe the cusp conditions are of two types. For particle pairs with the same charge we employ slowly decaying functions³² together with a linear combination of Gaussian-type functions (GTFs),

$$J_c^{\text{ee}}(\vec{r}) = \sum_{i>j=1}^{N_e} \left(-\frac{\Gamma}{\beta_0^{\text{ee}}(1 + \beta_0^{\text{ee}}|\mathbf{r}_i - \mathbf{r}_j|)} + \sum_{g=1}^G \beta_g^{\text{ee}} e^{-\zeta_g^{\text{ee}}|\mathbf{r}_i - \mathbf{r}_j|^2} \right) \quad (3)$$

$$J_c^{\text{pp}}(\vec{p}) = \sum_{i>j=1}^{N_p} \left(-\frac{\Gamma}{\beta_0^{\text{pp}}(1 + \beta_0^{\text{pp}}|\mathbf{r}_i^p - \mathbf{r}_j^p|)} + \sum_{g=1}^G \beta_g^{\text{pp}} e^{-\zeta_g^{\text{pp}}|\mathbf{r}_i^p - \mathbf{r}_j^p|^2} \right) \quad (4)$$

$$J_c^{\text{pn}}(\vec{r}, \vec{p}, \vec{R}) = \sum_{i=1}^{N_p} \sum_{I=1}^{N_n} \left(-\frac{Z_I}{\beta_0^{\text{pn}}(1 + \beta_0^{\text{pn}}|\mathbf{r}_i^p - \mathbf{R}_I|)} + \sum_{g=1}^G \beta_g^{\text{pn}} e^{-\zeta_g^{\text{pn}}|\mathbf{r}_i^p - \mathbf{R}_I|^2} \right) \quad (5)$$

while for particles with opposite charges we employ faster decaying cusp functions,³³ along with the linear combination of GTFs,

$$J_c^{\text{en}}(\vec{r}, \vec{R}) = \sum_{i=1}^{N_e} \sum_{I=1}^{N_n} \left(\frac{Z_I}{\beta_0^{\text{en}}} e^{-\beta_0^{\text{en}}|\mathbf{r}_i^e - \mathbf{R}_I|} + \sum_{g=1}^G \beta_g^{\text{en}} e^{-\zeta_g^{\text{en}}|\mathbf{r}_i^e - \mathbf{R}_I|^2} \right) \quad (6)$$

$$J_c^{\text{ep}}(\vec{r}, \vec{p}) = \sum_{j=1}^{N_p} \sum_{i=1}^{N_e} \left(\frac{\Gamma}{\beta_0^{\text{ep}}} e^{-\beta_0^{\text{ep}}|\mathbf{r}_i^e - \mathbf{r}_j^p|} + \sum_{g=1}^G \beta_g^{\text{ep}} e^{-\zeta_g^{\text{ep}}|\mathbf{r}_i^e - \mathbf{r}_j^p|^2} \right) \quad (7)$$

Here β and ζ are sets of variational parameters, Z_I are the nuclear charges and Γ is a constant that is equal to 1/2 and 1/4 respectively for distinguishable and indistinguishable particles to correctly describe the cusp conditions. In this investigation, the number of GTFs used in the cusps expansions is $G = 5$. To reduce the variance in the wave function, the variational



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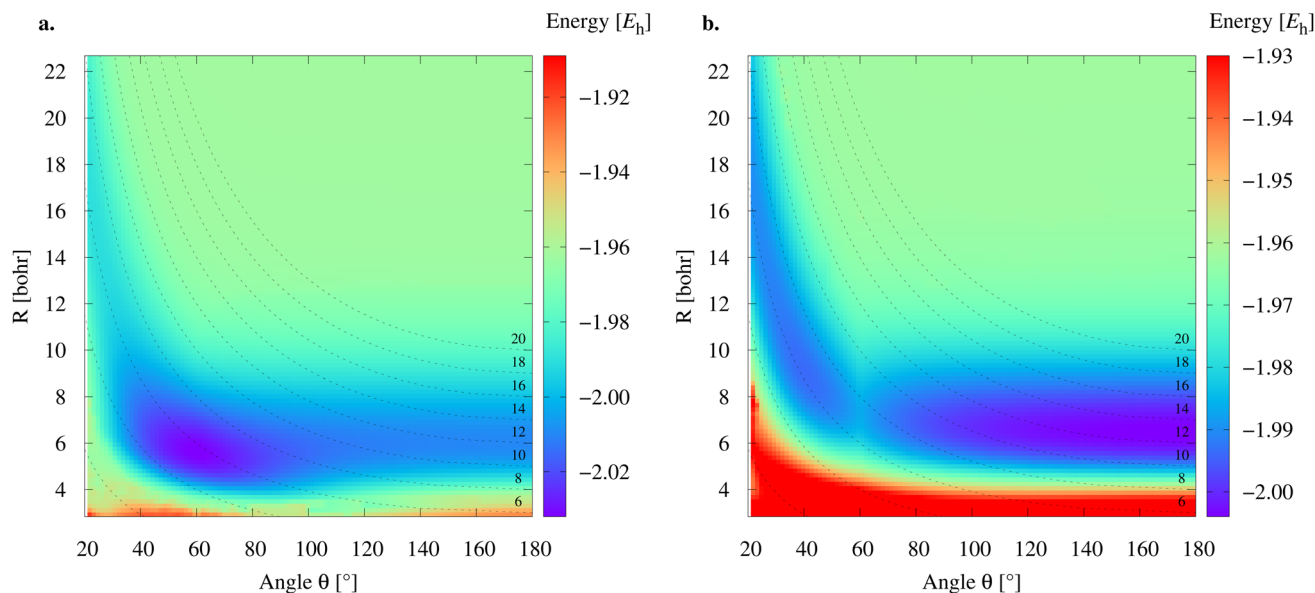


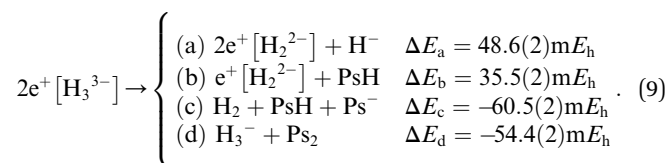
Fig. 2 Potential energy surfaces for the singlet (a) and triplet (b) positronic states of the $2e^+[H_3^{3-}]$ system. The energies were computed at the MP2 level using the aug-cc-pVTZ/PSX-TZ combination of electronic and positronic basis sets centered at the hydrogen nuclei. The dashed lines correspond to constant R_3 paths obtained for C_{2v} conformations.

Table 1 Equilibrium energies and distances computed with the VMC and DMC methods for the singlet and triplet states of the $2e^+[H_3^{3-}]$ system. The symmetry of the potential energy minima is also indicated

Positronic state	Symmetry	Method	Energy [E_h]	R_{eq} [bohr]
Singlet	D_{3h}	VMC	-2.1489(1)	6.15(1)
		DMC	-2.1652(2)	6.11(1)
Triplet	$D_{\infty h}$	VMC	-2.1266(1)	6.77(2)
		DMC	-2.1401(4)	6.62(1)

were further refined with the VMC and DMC methods for both the singlet and triplet states. The minima were located for geometries constrained to D_{3h} and $D_{\infty h}$ symmetries. The results shown in Table 1 corroborate the singlet D_{3h} state as the most stable one. Below, we focus the discussion on the lowest-energy $2e^+[H_3^{3-}]$ singlet state.

We explored the thermodynamic stability of $2e^+[H_3^{3-}]$ with respect to the dissociation channels given below,

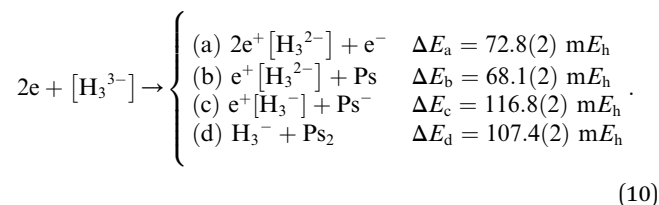


The dissociation energies of channels (9a–9d) were calculated employing the DMC results of Table 1 and the energy data reported in Table S1.† The negative ΔE of channels (9c and 9d) reveal that $2e^+[H_3^{3-}]$ is thermodynamically unstable with respect to these dissociation products. It is therefore clear that the lowest energy arrangement of a set of three protons, six electrons, and two positrons consists of a sum of dissociated species rather than

the bonded D_{3h} structure. Here we must add that the fixed-node errors of the DMC calculations are negligible in the computation of the binding energies, because the nodal surfaces of the purely electronic systems and of the electron–positron ones are described at the same level of theory, leading to a cancellation of errors when computing the energy differences. Moreover, the wave function optimization of the full set of variational parameters in the presence of the correlating Jastrow factor tends to reduce the fixed-node error also in the total energies.

A similar situation was found for positron bonded dihydrides. Previous studies pointed out that (I) $e^+[H_2^{2-}]$,^{7–9} (II) $2e^+[H_2^{2-}]$,¹⁰ and (III) $3e^+[H_2^{2-}]$ ¹¹ are thermodynamically unstable with respect to dissociation into (I') $H_2 + Ps^-$, (II') $H_2 + Ps_2$ and (III') $H_2 + Ps_2 + e^+$, respectively. The local range of stability for the systems I, II and III was explored by comparing the potential energy curves (PECs) for the (I, I'), (II, II') and (III, III') pairs. The PEC pairs were found to intersect at internuclear distances considerably shorter than the equilibrium distances of the corresponding positron bonded dihydrides. Those studies further confirmed the kinetic (or local) energy stability of the dihydrides I–III, since their energy barriers, calculated at the crossing points of the potential curves, were found to be sufficiently high to support a few vibrational states.

Along similar lines, we further explore the local stability of $2e^+[H_3^{3-}]$ around the D_{3h} minimum. We consider the four lowest-energy vertical detachment channels given by



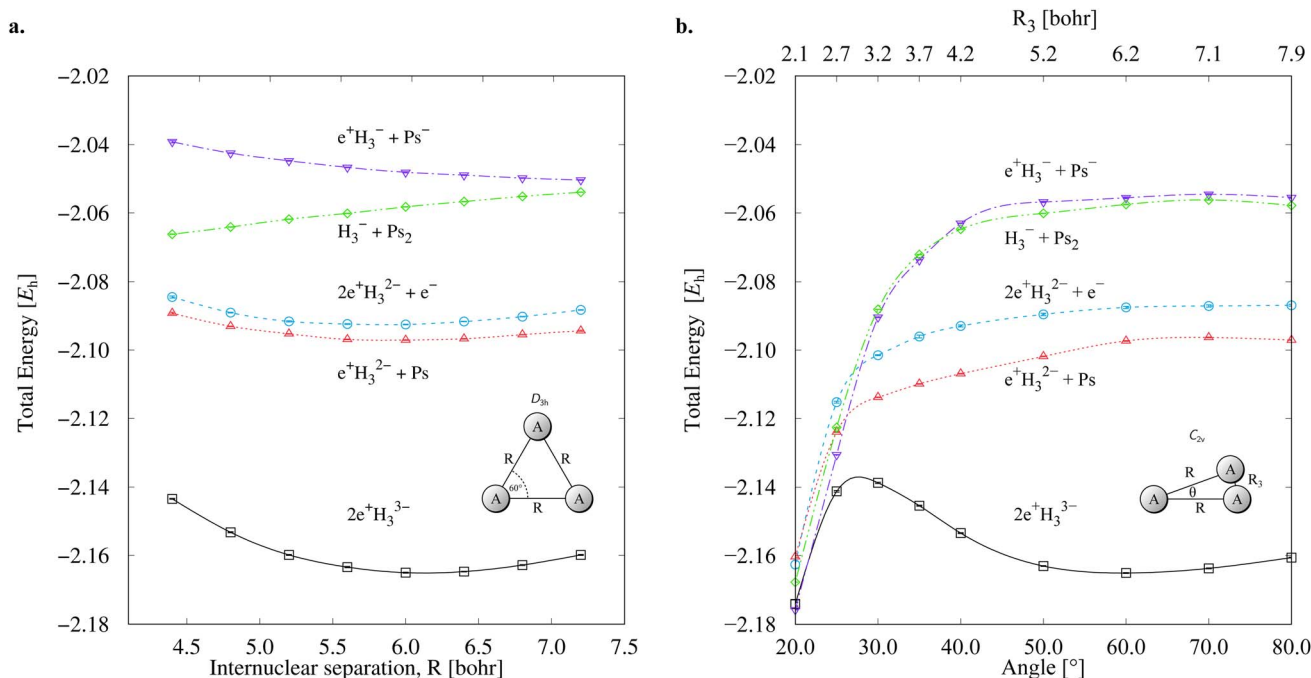


Fig. 3 Potential energy curves for the $2e^+[H_3^{3-}]$ system and the vertical detachment channels (10a–10d). The energies were computed with the DMC method as functions of the R coordinate in the D_{3h} symmetry (a) and of the θ coordinate in the C_{2v} symmetry (b) fixing $R = 6.1$ bohr. We employed the lowest energies obtained from variational calculations for Ps^- and Ps_2 ,^{45,46} and the exact value for Ps ($-0.25 E_h$).

Here, positive ΔE values confirm the stability of $2e^+[H_3^{3-}]$ against vertical detachments.

Fig. 3 presents PECs along the R coordinate constraining the system to preserve the D_{3h} symmetry, and along the θ coordinate imposing C_{2v} symmetry with $R = 6.1$ bohr. Fig. 3a reveals that the energy of $2e^+[H_3^{3-}]$ along the R coordinate is always lower than those computed for the (10a–10d) channels, and no curve crossings were found. In contrast, Fig. 3b reveals that the PEC of $2e^+[H_3^{3-}]$ intersects the (10c) potential around 20° and $R_3 = 2.1$ bohr. The stabilization of the (10c) channel as the R_3 distance decreases is consistent with the formation of a H_2 molecule ($R = 1.40$ bohr) in the adiabatic channel (9c). Although the (9c) channel energy lies below the $2e^+[H_3^{3-}]$ energy, the intersections are separated from the D_{3h} minimum by a rather high (≈ 20 m E_h) and broad ($\theta \approx 30^\circ$) energy barrier across the $2e^+[H_3^{3-}]$ potential. The PECs in Fig. 3a and b therefore corroborate the local (kinetic) energy stability of the $2e^+[H_3^{3-}]$ species.

3.2 Comparison with analogous purely electronic systems

As in previous studies of positron bonded dihydrides⁴ and dihalides,⁵ we compare the properties of the $2e^+[H_3^{3-}]$ system with two 3c2e bonded systems, *i.e.*, H_3^+ and Li_3^+ . Specifically, the equilibrium distances and the force constants for the symmetric stretching (ν_1) and bending (ν_2) vibrational modes of the D_{3h} ground states, calculated with the DMC method, are shown in Table 2. The equilibrium distance of the positronic molecule ($R = 6.11$ bohr) is much closer to that of Li_3^+ ($R = 5.64$ bohr) than H_3^+ ($R = 1.63$ bohr). This result is consistent with our earlier studies, which pointed out that purely electronic

molecules with isoelectronic cores are the closest analogues to positron bonded systems. Although larger discrepancies are found for the vibrational frequencies of $2e^+[H_3^{3-}]$ and Li_3^+ (roughly a factor of 2), they are still much closer if compared to the frequencies of H_3^+ , having different orders of magnitude. The present calculations for three-center two-particle bonds therefore corroborate the previous findings for diatomic systems.

The longer equilibrium distances and lower vibrational frequencies also indicate a weaker 3c2p bond compared to the 3c2e analogues. In addition, we contrast the energy stability of $2e^+[H_3^{3-}]$ with those of the purely electronic Li_3^+ , and H_3^+ . To that aim, we consider the lowest energy chemically meaningful dissociation channels of Li_3^+ , and H_3^+

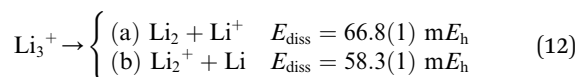
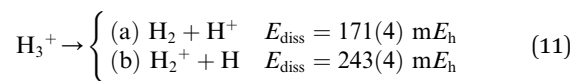


Table 2 Total energies (in E_h), equilibrium distance (in bohr) and force constants (in a.u.) for the symmetric stretching ν_1 mode and bending ν_2 mode of triatomic systems in D_{3h} symmetry calculated at DMC level

System	E	R	k_{ν_1}	k_{ν_2}
H_3^+	-1.346(4)	1.63(3)	0.57(5)	0.16(2)
Li_3^+	-22.3419(1)	5.645(7)	0.0254(3)	0.0110(4)
$2e^+[H_3^{3-}]$	-2.1652(2)	6.11(1)	0.0114(4)	0.0047(7)

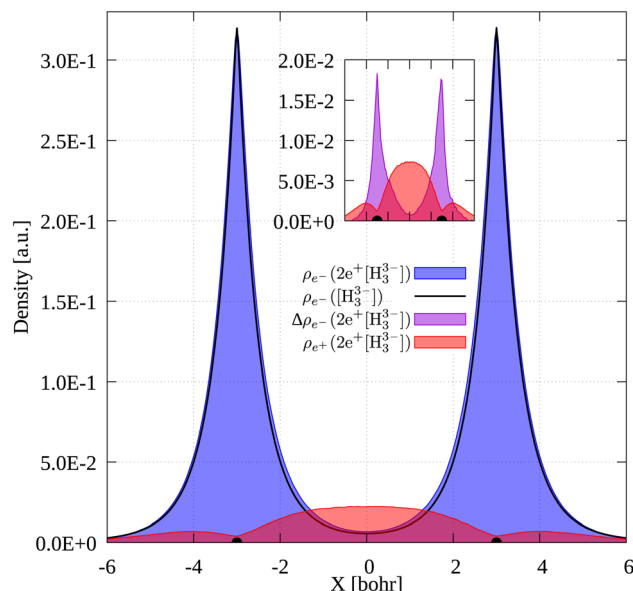
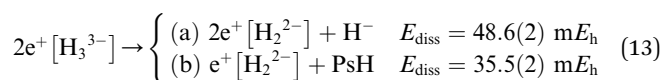


Fig. 4 1D cuts of the electronic density of $[H_3^{3-}]$ (black line) and the electronic (blue) and positronic (red) densities of $2e^+[H_3^{3-}]$. The inset panel displays the electronic density difference, $\Delta\rho_{e^-}$, between $2e^+[H_3^{3-}]$ and $[H_3^{3-}]$ (violet). The density of the unstable $[H_3^{3-}]$ system was constructed as the sum of the densities of three H^- anions at the equilibrium positions of $2e^+[H_3^{3-}]$. The densities were obtained as histograms of the number of particles inside voxels (width = 0.08 bohr) disposed along an internuclear axis.



The energies of channels (11) and (12) were calculated employing the DMC energy data reported in Table S1.† We observe that the lowest energy dissociation channel for H_3^+ ($E_{\text{diss}} = 171.84 \text{ m}E_h$) involves the formation of a neutral molecule and a proton. Contrastingly, for Li_3^+ ($E_{\text{diss}} = 58.27 \text{ m}E_h$) and $2e^+[H_3^{3-}]$ ($E_{\text{diss}} = 35.54 \text{ m}E_h$), involves the formation of

a neutral atom, and an ionic single particle bonded molecule. It is worth noticing that E_{diss} of Li_3^+ and $2e^+[H_3^{3-}]$ are of the same order and differ considerably from that of H_3^+ for all dissociation channels considered here.

3.3 Densities

To gain further insight into the 3c2p bond formation, we computed the positron (ρ_{e^-}) and electron (ρ_{e^-}) densities of $2e^+[H_3^{3-}]$. One-dimensional (1D) cuts of the electron densities obtained for the unbound $[H_3^{3-}]$ trianion and the bound $2e^+[H_3^{3-}]$ compound are shown in Fig. 4. The densities are remarkably similar, thus pointing out that the binding mechanism in $2e^+[H_3^{3-}]$ is not electronic, as previously observed for positronic covalent bonds.^{4,6} In contrast, the positron density prominently accumulates between the H nuclei, balancing the otherwise repulsive interaction between the anions and producing a slight increase of the electronic density in that region.

A comparison between the two-particle bonding densities in three-center systems is carried out in Fig. 5. In H_3^+ the bonding density presented in Fig. 5a is the total electron density, ρ_{e^-} . ρ_{e^-} in H_3^+ has maxima on top of the nuclei and accumulates around the centroid of the system, where ρ_{e^-} has a local minimum. For Li_3^+ the bonding density, $\Delta\rho_{e^-}$, displayed in Fig. 5b, was obtained as the ρ_{e^-} difference between the $[Li_3^+]$ and $[Li_3^{3+}]$ systems, both calculated at the same geometry. $\Delta\rho_{e^-}$ in Li_3^+ also displays maxima around the nuclei and accumulates around the centroid, but in this case, has a local maximum at that point. The symmetric accumulation of electronic density in the centroid of the system is a signature of 3c2e bonding. In turn, in $2e^+[H_3^{3-}]$ the bonding density is the total positron density, ρ_{e^+} , portrayed in Fig. 5c. ρ_{e^+} in $2e^+[H_3^{3-}]$ is depleted around the nuclei, as expected from the Coulomb interaction, gradually accumulates at the internuclear region and peaks at the centroid, clearly resembling $\Delta\rho_{e^-}$ of Li_3^+ in that region. Therefore, this accumulation around the centroid of $2e^+[H_3^{3-}]$ can be viewed as the formation of a 3c2p bond.

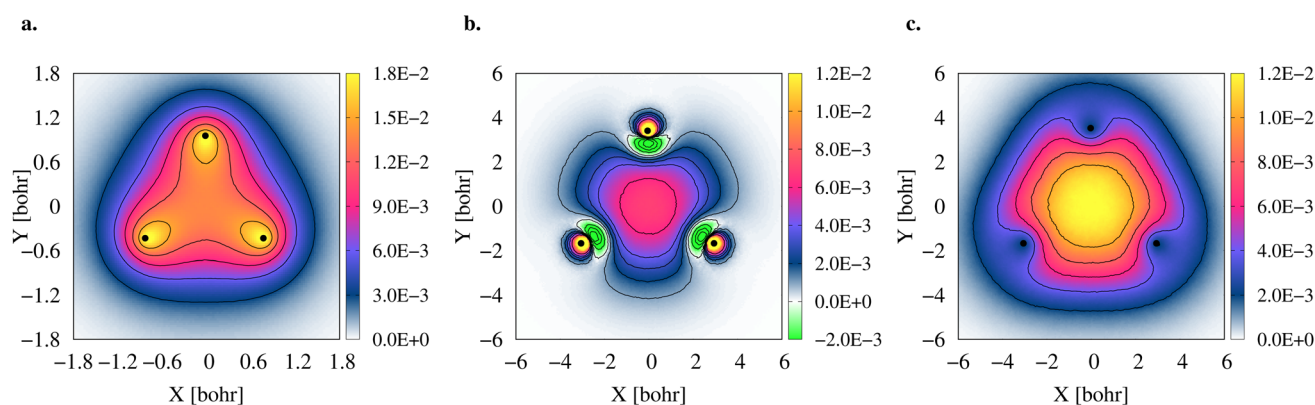


Fig. 5 Comparison of three-center two-particle bonding densities. Electronic density of H_3^+ (a), electronic bonding density of Li_3^+ (b), and positronic bonding density of $2e^+[H_3^{3-}]$ (c). The densities were obtained with the DMC method as histograms of the number of particles inside voxels (width = 0.08 bohr) disposed along the molecular plane. In all panels, the atomic nuclei are represented as black dots.



The densities (Fig. 5), vibrational properties (Table 2) and bond energies (eqn (9) and (12)) provide strong evidence that similar three-center two-particle bonding mechanisms are present in Li_3^+ and in $2\text{e}^+[\text{H}_3^{3-}]$.

Now that we have established the local stability of $2\text{e}^+[\text{H}_3^{3-}]$, its bonding properties and its similarities with Li_3^+ , it is worth exploring the chemistry of the latter to gain further insight into the chemical implications of the three-center two-positron bond.

Previous studies of the nature of the $3\text{c}2\text{e}$ bond in Li_3^+ based on topological analyses of the electronic density^{47,48} and an Interference Energy analysis⁴⁹ have concluded that Li_3^+ can be considered as the smallest metallic cluster, where the valence electrons in the centroid act as free metallic electrons. Additionally, to explain the relative stability and structure of Li_3^+ , the presence of σ -aromatic or σ -antiaromatic states is still widely discussed.^{47,49–51} Based on the reported similarities of the bonding densities of $2\text{e}^+[\text{H}_3^{3-}]$ and Li_3^+ , we speculate that the positrons in $2\text{e}^+[\text{H}_3^{3-}]$ could also be considered as ‘pseudo’-metallic in character and that the positronic delocalization in $2\text{e}^+[\text{H}_3^{3-}]$ could provide in the future evidence of a new type of positronic σ -aromaticity or σ -antiaromaticity. Exploring the extension of the metallic bond and aromaticity concepts to positronic molecules would require a more in-depth analysis of the bonding nature. For instance, by employing energy decomposition, quantum interference⁴⁹ or multicomponent atoms-in-molecules^{6,52,53} analyses. However, those studies are beyond the scope of the present work.

4 Conclusions

Theoretical studies have evidenced the formation of locally stable systems composed of two repelling atomic anions and one-to-three positrons. The anti-particles are mainly responsible for the conformers’ stabilization, thus expanding the definition of chemical bonding beyond the ordinary purely electronic systems.^{4,6–11} In this work, we have found that two positrons can form a locally stable bound state with three hydride anions in a D_{3h} configuration and singlet spin state. The results suggest the formation of a $3\text{c}2\text{p}$ bond, pointing out that the chemical bond concept reaches beyond the positron covalent bonds in two-center molecules, addressed in previous studies. The dissociation products $\text{H}_2 + \text{PsH} + \text{Ps}^-$ correspond to the lowest-energy configuration of the system comprising two positrons, six electrons and three hydrogen nuclei. Nevertheless, our vertical detachment and adiabatic energy dissociation analysis confirm the local stability of $2\text{e}^+[\text{H}_3^{3-}]$ around the D_{3h} equilibrium geometry. A comparative analysis reveals that the positronic molecule is similar to the trilithium cation with isoelectronic atomic cores, although it remarkably differs from the trihydrogen cation. Similarities were found for the equilibrium geometries, force constants for symmetric stretch and bending modes, and also dissociation energies trends. In addition, the electronic (Li_3^+) and positronic ($2\text{e}^+[\text{H}_3^{3-}]$) bonding densities are similar around the internuclear region and equally spread among all three atomic centers, suggesting strong similarities between the $3\text{c}2\text{p}$ and $3\text{c}2\text{e}$ bonds. The

positronic species has longer bond lengths, weaker force constants and lower bond energies than the trilithium cation, which can be viewed as the analogue purely electronic system. This trend does not seem to be general, as it was found for positronic hydrides but not for positronic dihalides.

The present results extend the findings of previous studies revealing that two positrons are capable of bonding three otherwise repelling atomic anions. Since positron bonded systems are fundamentally distinct from those formed by positron attachment to stable atoms and molecules, these results will hopefully stimulate further theoretical and experimental researches on novel physical and chemical processes involving those antiparticles.

Data availability

The datasets supporting this article have been uploaded as part of the ESI†

Author contributions

Conceptualization: J. C., F. M., L. P. G., A. R. Formal analysis: J. C., F. M., M. B. Investigation: J. C., F. M., L. P. G., A. R. Funding acquisition: M. T. N. V., A. T., A. R. Methodology: J. C., F. M., M. B., L. P. G., A. T., A. R. Project administration: A. T., A. R. Validation: M. T. N. V., A. T., A. R. Resources: J. C., F. M., M. B., A. T., A. R. Software: J. C., F. M., M. B., A. T., A. R. Supervision: M. T. N. V., A. T., A. R. Visualization: J. C., F. M. Writing – original draft: J. C., F. M., M. B., L. P. G., M. T. N. V., A. T., A. R. Writing – review & editing: J. C., F. M., M. B., L. P. G., M. T. N. V., A. T., A. R.

Conflicts of interest

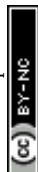
There are no conflicts to declare.

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