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Meta-stability through intermolecular interactions protecting the identity of atomic metal clusters: *ab initio* evidences in $(\text{Cu}_5\text{-Cu}_5)_n$ ($n < 3$) cases†

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Recent developments in new synthesis techniques have allowed the production of precise monodisperse metal clusters composed of a few atoms. These atomic metal clusters (AMCs) often feature a molecule-like electronic structure, which makes their physical and chemical properties particularly interesting in nanotechnology. Regarding potential applications, there is a major concern about the sintering of AMCs in nanoparticles due to the loss of their special properties. In this work, multireference *ab initio* theory is applied to demonstrate the formation of coupled AMC–AMC clusters in which the AMC partners maintain their ‘identity’ to a large extent in terms of their initial structures and atomic Mulliken charges, and their further oligomerization.

1 Introduction

Recent developments of highly selective experimental techniques enabling the synthesis of subnanometer metal clusters are pushing the understanding of these, more “molecular” than “metallic”, systems far beyond the present knowledge in materials science. In this way, when the atomic metal cluster (AMC) size is reduced to a small (less than 10) number of atoms, high stability and novel properties are achieved, that allow the AMC integration into materials. Additionally, interaction with the environment has the potential to boost the performance in applications particularly interesting in nanotechnology, including luminescence, sensing, bioimaging, theranostics, energy conversion, catalysis, and photocatalysis (see, *e.g.*, ref. 1 and 2 for recent reviews). From a more fundamental point of view, it has also been shown how modification of popular materials such as TiO_2 with

AMCs can convert them into “reporters” of fundamental surface polaron properties.^{3–5} From the microscopic point of view, the above behaviour is explained in terms of the d-band of the metal splitting into a subnanometric network of discrete molecule-like d orbitals, with fluxional inter-connections having the length of a chemical bond (1–2 Å). The spatial structures of these molecular orbitals make all the metal atoms cooperatively active and accessible and confer molecular characteristics to the complexes, that are responsible of their stability and properties.

Among the different AMCs, copper clusters have attracted much attention as catalysts⁶ since they have shown important catalytic properties *e.g.* for the oxidation of CO ,^{7,8} the selective hydrogenation of olefin and carbonyl groups,^{9,10} and in C–X (being X = C, N, S, P) bond forming reactions.¹¹ The oxidative dehydrogenation of cyclohexene on atomically precise subnanometer bimetallic Cu–Pd (tetramer) clusters is also worth mentioning.¹² Moreover, the work in ref. 13 showed an outstanding chemical and thermodynamical stability of atomic copper clusters in solution over the whole pH range. First-principles modelling, including methods beyond the state-of-the-art and an interplay with cutting-edge experiments, is helping to understand the special properties of AMCs at the most fundamental molecular level. Thus, the use of first-principles methods has disclosed the fundamental reasons why Cu_5 clusters experience a reversible oxidation,¹⁴ and are capable of increasing and extending into the visible region the solar absorption of TiO_2 ,¹⁵ also considering the decomposition and photo-activation of CO_2 as a prototypical (photo-)catalytic reaction.¹⁶

In spite of their potential applications, there is a major concern about the sintering of AMCs in metallic nanoparticles with the consequent loss of their special properties. In order to analyze the possible existence of metastable states in which Cu_5 preserves its identity, multireference Rayleigh Schrödinger (second-order) perturbation theory¹⁷ (RS2C) is applied here, allowing evidence of the formation and further oligomerization of coupled $\text{Cu}_5\text{-Cu}_5$ clusters at a high level of *ab initio* theory. It should be stressed that in our work preservation of identity at a

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molecular level encompasses a concept considerably broader than just aggregation by weak (dispersion-dominated) van der Waals (vdW) forces. It also includes the formation of covalent bonds between molecular sub-units, yet conserving their initial structures and, to a large extent, their atomic charge distributions.

2 Results and discussion

We optimized the Cu_5 cluster geometries in vacuum, their two main geometrical arrangements are shown in Fig. 1 (top panel): a planar trapezoidal two-dimensional (2D) structure with a spin quantum number equal to 1/2 and a trigonal bipyramidal tri-dimensional (3D) arrangement with spin equal to 3/2. In agreement with previous studies (see, e.g., ref. 11 and 18), the 2D structure is the most stable configuration by 0.6–0.7 eV (see Table 1). It can also be observed in Table 1 that the relative energies calculated at coupled-cluster and multireference perturbation levels of theory, using the largest active space, differ by less than 0.1 eV, thus indicating the accuracy of the latter.

To get some insights on how 3D and 2D Cu_5 clusters interact as a function of their relative distances, we evaluated interaction energies keeping the intramolecular geometries fixed at the optimized values (see Fig. 2, top panels). Interestingly, for both structures, the interaction is repulsive in the triplet spin state but it becomes strongly attractive (by a few eV) in the singlet spin state. This outcome can be explained by considering that unpaired electrons occupying s-type orbitals on the two Cu_5 clusters feature repulsion/attraction to each other in parallel/anti-parallel spin configurations, producing repulsive/attractive inter-molecular interactions, as is the case for the interaction between two hydrogen atoms. It can also be observed that the attractive interaction is significantly enhanced when dynamical

Table 1 Relative energies of Cu_5 clusters at coupled-cluster singles and doubles (CCSD/Def2-TZVP) and multireference Rayleigh Schrödinger (second-order) perturbation theory¹⁷ (RS2C/cc-pVTZ-PP) levels with respect to the lowest-energy structure (in eV). The spin multiplicity ($2S + 1$) is also indicated. The active space in the preceding multi-configurational calculations is specified as well (see Appendix). Within parentheses, we indicate the nature of the stationary point: Min denotes minimum and TS denotes a transition state

Cu_5	$2S + 1$	CCSD	RS2C(5,5)	RS2C(7,7)
Planar (Min)	2	0	0	0
Planar (TS)	4	2.0	2.0	2.0
Bipyramidal (TS)	2	0.3	0.2	0.3
Bipyramidal (Min)	4	0.7	0.5	0.6

correlation is accounted for using the RS2C method (see the Appendix for the computational details). Interestingly, the interaction energies are hardly modified when the CASSCF space is enlarged from a minimal (2,2) space (2 electrons in 2 orbitals) to larger spaces (see Fig. 2, top panels).

Using the computational strategy described in the Appendix, the structures of coupled Cu_5 – Cu_5 clusters shown in the middle and bottom panels of Fig. 1 have been obtained. The corresponding interaction energies are indicated in Table 2 at both multiconfigurational (referred to as DF-CASSCF) and multireference Rayleigh Schrödinger (second-order), internally contracted, perturbation levels of theory (denoted RS2C). With the exception of the structure labeled as '4',¹⁹ note that the increase of the active space from that considering 10 electrons in 10 active orbitals [denoted as (10,10)] to that including 12 electrons in 12 active orbitals [referred to as (12,12)] modifies the energies up to 0.2 eV when dynamical correlation is not accounted for, while the consideration of the latter makes the interaction energies almost identical for both active spaces. It should be mentioned that the inclusion of the dynamical correlation with RS2C is crucial, accounting for ca. 70% of the attractive Cu_5 – Cu_5 interaction in cluster 1 (–5.2 eV, see Table 2). This value agrees well with that obtained using the natural orbital coupled-cluster approach DLPNO-CCSD(T)²⁰ (–4.9 eV from ref. 21). The good agreement with the interaction energy and structure of the lowest-energy isomer obtained with the DFT-D4 ansatz (–5.4 eV from ref. 21) is also worth-mentioning. A similar coupled Cu_5 – Cu_5 structure is also predicted to be more stable at the DFT-D4 level. Moreover (see Table S2 of the ESI†), the average values of the Cu–Cu bond lengths for the Cu_5 partners (2.5 Å) are in between those obtained through the DF-CASSCF and the RS2C optimizations (2.7 and 2.4 Å, respectively). It should also be considered that we are dealing with fluxional clusters bearing wide amplitude Cu–Cu motions (see below). For instance, an *ab initio* molecular dynamics simulation²¹ has shown that the values of Cu–Cu distances in circumpyrène-supported Cu_5 –(O_2)₄ at 473 K experience large fluctuations (within 0.5 Å).

In contrast to the case of isolated Cu_5 clusters, for which the 2D structures are energetically favored, it can be observed in Table 2 that the most stable (by ca. 2 eV) arrangements of coupled Cu_5 – Cu_5 clusters correspond to coupled 3D structures. This structure (of D_{2d} symmetry) is similar to that reported in



Fig. 1 Optimized structures of individual Cu_5 clusters (at the CCSD/Def2-TZVP level above) and coupled Cu_5 – Cu_5 clusters (at the CAS(10,10)/cc-pVTZ-PP level below) in vacuum. Atom numbering included.





Fig. 2 Top panels: scans of the interaction energy of two Cu_5 clusters as a function of the Z distance in vacuum. The geometries of the Cu_5 clusters have been kept fixed in the calculations. Top left panel: bipyramidal 3D structures. Top right panel: planar 2D structures. Bottom panel: interaction of two Cu_5 – Cu_5 coupled clusters as a function of the Z distance, with the Cu_5 – Cu_5 geometries fixed to those corresponding to the minimum in the top left panel. All calculations have been carried out with the cc-pVTZ-PP basis set.

Table 2 Interaction energies (in eV) of coupled Cu_5 – Cu_5 clusters at DF-CASSCF/cc-pVTZ-PP and RS2C/cc-pVTZ-PP energy levels (see Appendix for computational details). Within parentheses, we indicate the nature of the stationary point: Min denotes minimum and TS denoted a transition state

Cu_5 – Cu_5	DF-CAS(10,10)/RS2C	DF-CAS(12,12)/RS2C
1 (Min)	–1.5/–5.2	–1.6/–5.2
2 (Min)	–1.5/–5.0	–1.7/–5.0
3 (Min)	–1.8/–2.3	–1.7/–2.3
4 (Min)	–1.4/–3.3	–2.3/–2.8
5 (TS)	–1.3/–4.7	–1.5/–4.7

ref. 18 for Cu_{10} . The inclusion of dynamical correlation is clearly responsible for such behaviour. In fact, without considering it, the interaction energies are up to 0.7 eV more attractive upon the coupling of planar 2D structures than in the case of coupled 3D geometries.

We performed a Mulliken charge analysis of natural orbitals for both isolated Cu_5 and coupled Cu_5 – Cu_5 clusters using the geometries optimized at the DF-CASSCF level (see Table 3). Note that Mulliken charges are larger in the 3D Cu_5 structure than in the 2D Cu_5 structure. As a result, the electrostatic contribution to the Cu_5 – Cu_5 intermolecular interaction is favored when 3D Cu_5 clusters become coupled to each other. Most importantly, the values of Mulliken charges on all Cu atoms are (within numerical accuracy) the same for the two Cu_5

Table 3 Mulliken charges on the atoms of Cu_5 and coupled Cu_5 – Cu_5 clusters for the most stable structures optimized at the DF-CASSCF/cc-pVTZ-PP level of theory. No symmetry has been imposed in the calculations. CCSD/Def2-TZVPP results are reported within parentheses for the sake of comparison

Individual Cu_5 clusters				
Label	2D (Min)	3D (Min)		
1	–0.02	–0.07	(–0.06)	
2	–0.03	–0.07	(–0.06)	
3	0.01	0.10	(0.10)	
4	0.01	0.10	(0.10)	
5	0.03	–0.07	(–0.06)	
Coupled Cu_5 – Cu_5 clusters				
Label	1 (Min)	2 (Min)	3 (Min)	4 (Min)
1	–0.11	–0.14	0.15	–0.04
2	–0.11	0.10	–0.21	–0.06
3	–0.10	0.04	0.15	–0.01
4	0.16	–0.28	–0.05	0.01
5	0.16	0.28	–0.04	0.09
6	0.16	–0.27	–0.04	0.02
7	0.16	0.03	–0.05	0.01
8	–0.10	0.09	0.15	0.02
9	–0.11	0.29	0.15	0.01
10	–0.11	–0.14	–0.21	–0.06

clusters within Cu_5 – Cu_5 in clusters 1 and 3, leading to a symmetric structure of the complex with respect to the two



Appendix

Computational methods and additional details

Density fitting single-state multi-configurational self-consistent-field (DF-CASSCF) calculations have been carried out, as implemented in the last version of the MOLPRO code.²⁵ We used the polarized correlation-consistent triple- ζ cc-pVTZ-PP basis set for copper atoms,²⁶ including a small (10-valence-electron) relativistic pseudopotential. The DF-CASSCF approach is employed to account for the most important non-dynamical correlation effects. Then, the internally contracted multireference Rayleigh Schrödinger (second-order) perturbation theory RS2C method¹⁷ has been applied to cover dynamical correlation effects. The RS2C method is basically a modified version of CASPT2 (complete active space with second-order perturbation theory) developed by Celani and Werner,¹⁷ using CASSCF wave functions as a reference in the RS2C calculations. For complex 1 of the coupled Cu₅-Cu₅ clusters, the CASSCF wave functions comprise up to 226 512 configuration state functions (CFSS). The subsequent RS2C wave function consists of 700×10^6 contracted CSFs. The RS2C method thus allows the use of reference wave functions with large active spaces and internally contracted configurations are used as a basis. For density fitting, the associated MP2FIT and JKFIT bases have been used in DF-CASSCF calculations. The diagonalization of the first-order reduced density matrix obtained from the wave function in DF-CASSCF calculations allowed us to obtain natural orbitals. An analysis of the Mulliken charges²⁷ was accomplished for both Cu₅ and Cu₅-Cu₅ clusters. Additionally, for the sake of comparison, Coupled Cluster Singles and Doubles (CCSD) calculations have been carried out as implemented in the GAUSSIAN 09 code.²⁸

Initial optimizations of the coupled Cu₅-Cu₅ cluster geometries were performed at PBE and B3LYP levels,^{29,30} using D4 Grimme's parameterization³¹ to account for the dispersion correction. An excellent performance has been achieved with the predecessor PBE-D3(BJ) ansatz³² in describing both supported and unsupported subnanometer silver^{3,33} and copper^{16,34} clusters. We used the atom-centered Def2-SVP³⁵ basis set for copper atoms. All dispersion-corrected DFT-based calculations have been performed with the ORCA suite of programs (version 5.0.1).³⁶⁻³⁸

We started our coupled Cu₅-Cu₅ cluster calculations with a bipyramidal arrangement for the Cu₅ sub-unit. In this way, we placed together two trigonal bipyramidal arrangements with the center of mass of one of them located in the origin of the coordinate system and the corresponding main symmetry axis along the Z axis. The position of the second Cu₅ molecule with respect to the first one was modified in a range of distances and orientations. For this, we varied the distance between the two centers of mass along each of the axes, making it equal to 4.0, 5.0 and 6.0 Å for X, 6.0 and 7.0 Å for Y, and 7.0 and 8.0 Å for displacements along the Z-axis. Regarding the angles we considered three rotations for each of the geometries, *i.e.* the first one around the X-axis and with values of 0, 60, and 90 degrees; the second one around the Z axis, taking angles of 0, 45, and 90 degrees; and the last one around the X axis and with values of 0, 60, 120, 180, 240, 300, 360 degrees. The resulting geometries

were fully optimized at the dispersion-corrected DFT levels, and those corresponding to the lowest energies were selected for further optimizations through DF-CASSCF calculations. The active spaces in DF-CASSCF calculations [m electrons in m orbitals, referred as (m,m) active space] varied until convergence was achieved in the follow-up RS2C calculations of coupled Cu₅-Cu₅ cluster energies. In all cases we considered the singlet ground state of the clusters and no symmetry restrictions were imposed in the calculations. The results of the preliminary DFT calculations can be obtained from the authors upon request. Results on previous theoretical evaluations of copper cluster geometries are available in the literature, see for instance ref. 39 and 40, but as far as we are aware, the authors of these investigations applied DFT level and not multireference *ab initio* approaches, with the resulting geometries differing from those obtained in this work. All interaction energies (E_{inter}) were calculated as follows:

$$E_{\text{inter}} = \{E_{\text{Cu}_5\text{-Cu}_5}\}_{\text{Min}} - \{E_{\text{Cu}_5\text{-Cu}_5}\}_{\text{Asymp}}$$

where $\{E_{\text{Cu}_5\text{-Cu}_5}\}_{\text{Min}}$ is the energy at the minimum and $\{E_{\text{Cu}_5\text{-Cu}_5}\}_{\text{Asymp}}$ is that at the asymptotic limit, correlating with the corresponding two Cu₅ + Cu₅ fragments in their energetically most favored structures. For the sake of size consistency, both calculations were carried out using the same active space within the DF-CASSCF and RS2C methodologies.

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