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# Proton transfer in hydrogen-bonded degenerate systems of water and ammonia in metal–organic frameworks

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Porous crystalline metal–organic frameworks (MOFs) or porous coordination polymers (PCPs) are emerging as a new class of proton conductors with numerous investigations. Some of the MOFs exhibit an excellent proton-conducting performance (higher than  $10^{-2}$  S cm<sup>-1</sup>) originating from the interesting hydrogen(H)-bonding networks with guest molecules, where the conducting medium plays a crucial role. In the overwhelming majority of MOFs, the conducting medium is H<sub>2</sub>O because of its degenerate conjugate acid–base system ( $\text{H}_3\text{O}^+ + \text{H}_2\text{O} \rightleftharpoons \text{H}_2\text{O} + \text{H}_3\text{O}^+$  or  $\text{OH}^- + \text{H}_2\text{O} \rightleftharpoons \text{H}_2\text{O} + \text{OH}^-$ ) and the efficient H-bonding ability through two proton donor and two acceptor sites with a tetrahedral geometry. Considering the systematic molecular similarity to water, ammonia ( $\text{NH}_3$ ;  $\text{NH}_4^+ + \text{NH}_3 \rightleftharpoons \text{NH}_3 + \text{NH}_4^+$ ) is promising as the next proton-conducting medium. In addition, there are few reports on NH<sub>3</sub>-mediated proton conductivity in MOFs. In this perspective, we provide overviews of the degenerate water (hydronium or hydroxide)- or ammonia (ammonium)-mediated proton conduction system, the design strategies for proton-conductive MOFs, and the conduction mechanisms.

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## 1. Introduction

Proton transport based on an acid–base nature is essential and critical in biological systems and electrochemical devices.<sup>1–4</sup>

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According to Brønsted–Lowry theory, an acid and base react with each other by proton transfer forming their conjugate acid–base pair. In particular, the conjugate acid–base pair in one species can provide a degenerate proton conduction chain (*i.e.*  $\text{H}_3\text{O}^+ + \text{H}_2\text{O} \rightleftharpoons \text{H}_2\text{O} + \text{H}_3\text{O}^+$ ) where  $\text{H}_3\text{O}^+$  and  $\text{H}_2\text{O}$  coexist through the mobile proton and the proton suffering from electron depletion is able to be shared by neighbouring electron rich atoms such as oxygen and nitrogen with symmetric hydrogen bonding.<sup>1</sup> Solid-state proton conductors (SSPCs) have



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hydroxide ion-conductive metal–organic frameworks, other ion-conduction in nano-structured materials, novel hybrid catalysts of metal nanoparticles and metal–organic frameworks, and flow reactors such as fuel cells and electrolyzers.



attracted much attention because of their application as a fuel cell (FC) component for alternative energy. FC technology converts chemical energy into electrical energy without the emission of CO<sub>2</sub>. In general, solid-state proton conductors show a higher conductivity at room temperature than other solid-state ionic conductors such as Li<sup>+</sup> or Na<sup>+</sup> conductors because hydrogen bonds have a covalent character and reduce the net charge of the proton, resulting in a reduction in the Coulomb potential of the proton pathway. By contrast, Li<sup>+</sup> or Na<sup>+</sup> in solids do not have a covalent character and their Coulomb potential is strong, resulting in a large energy barrier height for jump diffusion. For practical use, solid-state electrolytes are required for conductivities higher than 10<sup>-2</sup> S cm<sup>-1</sup>. To date, organic polymers or inorganic materials have been widely used and studied as proton conductors.<sup>5-9</sup> For example, CsHSO<sub>4</sub> working in a high-temperature range (119 < T < 145 °C) exhibits a high conductivity of 3.7 × 10<sup>-3</sup> S cm<sup>-1</sup> through phase transition. In particular, the organic polymer Nafion, which consists of a perfluorinated polyethylene backbone and a terminal sulfonic acid group, shows high performance (10<sup>-1</sup> to 10<sup>-2</sup> S cm<sup>-1</sup>) in the fully hydrated state at a relatively low temperature (T < 85 °C). However, it indicates efficiency degradation during the hydration and dehydration process, implying that the proton conductivity is critically affected by the incorporated proton-conducting medium.

In general, the majority of solid-state proton conductors contain water as the conducting medium<sup>10</sup> because there are several aspects to an efficient proton-conducting medium (Scheme 1). Specifically, (1) it obtains the degenerate conjugate acid–base system (H<sub>3</sub>O<sup>+</sup> + H<sub>2</sub>O ⇌ H<sub>2</sub>O + H<sub>3</sub>O<sup>+</sup>), and (2) it has two proton donor and two acceptor sites on the oxygen atom. Furthermore, these sites can form an H-bonding network with a tetrahedral geometry, which is advantageous for efficient proton hopping by local molecular rotational motion. In



Scheme 1 Schematic representation of proton transfer in water- and ammonia-conducting media with degenerate systems.

addition, (3) it has a small molecular size (kinetic diameter 2.65 Å), which is beneficial for dynamic molecular motion in diffusion and mobility. Moreover, the neutral liquid phase facilitates handling. Therefore, there are a large number of experimental and theoretical studies on proton conduction and diffusion mechanisms in water. For water, two types of proton diffusion mechanisms, the Grotthuss and vehicle mechanisms, are well established.<sup>11,12</sup> In the Grotthuss mechanism, a proton moves through the H-bonding networks between the hydronium ion and water, in which proton transfer and sequential molecular rotation occur simultaneously. On the other hand, in the vehicle mechanism, the protic species (H<sub>3</sub>O<sup>+</sup> or NH<sub>4</sub><sup>+</sup>) diffuses by itself as a proton-attached vehicle. These mechanisms can be identified from the activation energy because the required hydrogen bonding cleavage energy penalty is in the range of 2–3 kcal mol<sup>-1</sup> (0.09–0.13 eV).<sup>11</sup> Therefore, the Grotthuss ( $E_a < 0.4$  eV) and vehicle mechanisms ( $E_a > 0.4$  eV) generally have a difference in the activation energy.<sup>13</sup>

As an irreplaceable feedstock, ammonia has received considerable attention because of its various applications, such as in fertilizers<sup>14</sup> and pharmaceuticals,<sup>15</sup> and as a refrigerant<sup>16</sup> and fuel.<sup>17</sup> As a result, 150 million tons of ammonia are produced annually on the global scale<sup>18</sup> for use as a raw material in the manufacturing industry. In addition, liquid ammonia is used as a unique solvent because it closely approaches water in the ability to dissolve salt-like substances; it impressively dissolves alkali metals and alkali earth metals forming a conductive solution without appreciable reaction taking place.<sup>19</sup> In particular, ammonia is promising as a next proton-conducting medium because it has a molecular system most similar to that of water, specifically three proton donor sites and one acceptor site with a tetrahedral geometry, a degenerate conjugate acid–base system (NH<sub>4</sub><sup>+</sup> + NH<sub>3</sub> ⇌ NH<sub>3</sub> + NH<sub>4</sub><sup>+</sup>) and a small molecular size (kinetic diameter 2.60 Å). Nevertheless, liquid NH<sub>3</sub> shows a low proton conductivity (10<sup>-11</sup> Ω<sup>-1</sup>) without an acid source because of its low auto-ionization constant (2.2 × 10<sup>-28</sup> at 25 °C).<sup>20-23</sup> However, liquid NH<sub>3</sub> involving NH<sub>4</sub><sup>+</sup> reveals a molar conductivity of 142 S cm<sup>2</sup> mol<sup>-1</sup>, which is



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slightly lower than that of  $\text{H}_3\text{O}^+$  in water ( $350 \text{ S cm}^2 \text{ mol}^{-1}$ ).<sup>21</sup> The handling of  $\text{NH}_3$  is also advantageous because it is easy to liquify (at ambient temperature and *ca.* 8 atm or at 240 K and ambient pressure), and the infrastructures for  $\text{NH}_3$  technology, such as the production, storage, and transport systems, are well established. However, the corrosive gas phase of  $\text{NH}_3$  is a drawback as a conducting medium. Thus, the proton conductivity of  $\text{NH}_3$  was typically investigated below the boiling point (<240 K). Therefore, for the practical use of  $\text{NH}_3$  as a conducting medium, efficient and robust adsorbents are required as a template for encapsulation of  $\text{NH}_3$  species. Metal-organic frameworks (MOFs) or porous coordination polymers<sup>24–27</sup> constructed from metal ions and organic ligands have been of interest in a new class of solid-state proton conductors because of their high crystallinity, chemical tunability, considerable porosity, and versatile adsorption ability. Kanda *et al.* reported, for the first time, a proton-conductive Cu(II)-type MOF in 1979.<sup>28</sup> Since then, noticeable progress has been achieved in this field.<sup>13,29–31</sup> In most cases, proton conductive MOFs have been designed with intrinsic or extrinsic proton sources (Fig. 1). The intrinsic proton sources can be classified by their position. One such source is located in pores as counterions, such as  $\text{H}_3\text{O}^+$ ,  $\text{NH}_4^+$ ,  $\text{NH}_2(\text{Me})_2^+$ ,  $\text{H}_2\text{PO}_4^-$  and  $\text{OH}^-$  that are incorporated in the pore during the MOF synthesis to maintain the neutrality of the framework.<sup>32–35</sup> Another source is positioned in the organic strut of frameworks as dangling acid functional groups ( $-\text{SO}_3\text{H}$ ), ( $-\text{COOH}$ ), and ( $-\text{PO}_3\text{H}_2$ )), which are not coordinated to the metal center.<sup>36–39</sup> This can provide additional protons to the pore environment. The intrinsic sources form H-bonding networks with the framework and additional water molecules, resulting in improved proton conductivity. The extrinsic sources mean the artificial encapsulation of protic organic molecules (imidazole and histamine) or charge-neutral nonvolatile acids ( $\text{H}_2\text{SO}_4$  and  $\text{H}_3\text{PO}_4$ ) in the pores of MOFs through a simple inclusion method.<sup>40–43</sup> The pores are filled up by protic guest molecules with the formation of the H-bonding network. As a result, the low  $\text{pK}_a$  value of guest molecules can provide a potent high-proton donation ability at moderate temperatures.

In general, the ionic conductivity ( $\sigma$ ) of MOFs is estimated by the alternating current (AC) impedance measurement of a pelletized microcrystal powder or single crystal in a wide frequency range. The ionic conductivity can be expressed by eqn

(1), where  $z$ ,  $e$ ,  $n$ , and  $\mu$  mean the valence of the ion, elementary charge, charge carrier concentration, and carrier mobility, respectively. In addition, the proton conduction mechanisms are evaluated through the relationship of conductivity and temperature in eqn (2), where  $A$ ,  $k_B$ , and  $E_a$  are the pre-exponential factor, Boltzmann constant, and activation energy, respectively.

$$\sigma = zen\mu \quad (1)$$

$$\sigma T = A \exp(-E_a/k_B T) \quad (2)$$

Considering eqn (1), proton conductivity can be enhanced by the control of charge carrier concentration and mobility with an improved conduction pathway. Herein, we examine the selective examples of water (hydronium or hydroxide)- and ammonia (ammonium)-mediated degenerate H-bond systems in MOFs. In particular, their design, conduction properties, and diffusion mechanisms are discussed.

## 2. Water-based degenerate system for proton conduction in MOFs

### 2.1. Additional protons with water molecules

A water-based degenerate system consisting of  $\text{H}_3\text{O}^+$  and  $\text{H}_2\text{O}$  ( $\text{H}_3\text{O}^+-\text{H}_2\text{O}$  system), where these species are connected through H bonds, is important for showing high proton conductivity. Efficient proton transport using the  $\text{H}_3\text{O}^+-\text{H}_2\text{O}$  system can be described by a combination of a proton jump from  $\text{H}_3\text{O}^+$  to a neighboring  $\text{H}_2\text{O}$  and molecular rotations, and is named the Grotthuss mechanism.<sup>44</sup> Kreuer *et al.* reported a more detailed conduction mechanism using molecular dynamics (MD) simulations,<sup>44</sup> showing that the additional proton in the  $\text{H}_3\text{O}^+-\text{H}_2\text{O}$  system migrates through a recombination of two species of  $\text{H}_5\text{O}_2^+$  (Zundel ion) and  $\text{H}_9\text{O}_4^+$  (Eigen ion) through a proton jump within an H bond. The efficient transportation in  $\text{H}_3\text{O}^+-\text{H}_2\text{O}$  is also thought to be the origin of the abnormally high mobility of the proton ( $\text{H}^+$ :  $36.2 (\times 10^{-8} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1})$ ) in water solvent compared with other ions ( $\text{Li}^+$ : 4.0 and  $\text{Na}^+$ :  $5.2 (\times 10^{-8} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1})$ ).<sup>45</sup> Solid materials showing high proton conductivity at ambient temperature usually have the  $\text{H}_3\text{O}^+-\text{H}_2\text{O}$  system, as in the case of Nafion.<sup>46</sup> However, the structure of the inner H-bonding system in such amorphous organic materials could not be visualized. By contrast, MOFs were recently studied as a platform for visualization of the H-bonding system in a solid state because of its highly crystalline properties. We present an overview of the structure and proton conductivity of water and additional protons, *i.e.*, the  $\text{H}_3\text{O}^+-\text{H}_2\text{O}$  system, included in MOFs. An oxalate-bridged two-dimensional (2-D) MOF,  $(\text{NH}_4)_2(\text{H}_2\text{adp}) [\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  ( $\text{H}_2\text{adp}$  = adipic acid), showing the coexistence of a carboxylic acid group and a water molecule in the interlayer space, was reported in 2009.<sup>47</sup> As shown in Fig. 2, the carboxylic acid groups, water molecules, and ammonium ions formed 2-D H-bonding networks, where the dicarboxylic acid group of  $\text{H}_2\text{adp}$  is expected to give additional protons through partial dissociation. There are several short H bonds between  $\text{H}_2\text{adp}$  and ox ions ( $2.688(4) \text{ \AA}$ ,



Fig. 1 Classification of proton sources in metal-organic frameworks: (a and b) intrinsic proton sources and (c) extrinsic proton sources.



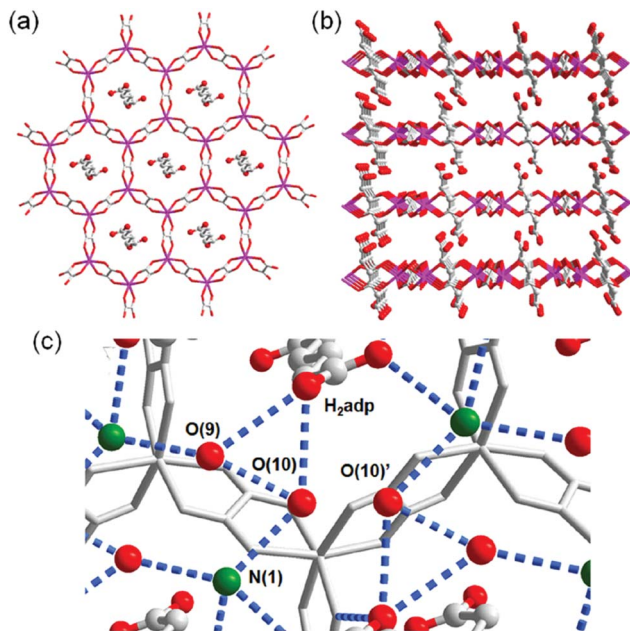


Fig. 2 (a) Honeycomb layer structure of  $(\text{NH}_4)_2(\text{H}_2\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$ . (b) Perspective view along the  $b$ -axis. Guest molecules are omitted. (c) H-bond arrangements of  $-\text{COOH}$ ,  $\text{H}_2\text{O}$ , and  $\text{NH}_4^+$  in the interlayer. H bonds are shown as blue dotted lines. The colors of red, green, gray, and blue correspond to O, N, C, and Zn atoms, respectively. Reproduced from ref. 47 with permission from American Chemical Society, Copyright 2009.

O(10), and O(9) atoms of water molecules ( $2.638(12) \text{ \AA}$ ), and N(1) atoms of ammonium ions and O(10) atoms of water molecules ( $2.789(7) \text{ \AA}$ ), implying that the additional protons should momentarily form the  $\text{H}_3\text{O}^+ - \text{H}_2\text{O}$  system in the pores and could migrate through the Grotthuss mechanism. This compound shows a high proton conductivity of  $0.8 \times 10^{-2} \text{ S cm}^{-1}$  ( $25^\circ \text{C}$ , 98% relative humidity (RH)), which is comparable to that of Nafion. From the results of the temperature dependence of proton conductivity, the activation energy was estimated to be 0.63 eV, whereas the conduction mechanism in this compound was expected to be the Grotthuss mechanism because of its closely packed guest molecules. The reason for the relatively high activation energy might be attributed to some direct diffusion process in the proton transfer in this compound, which is implied by the 50% occupancy of O(10) atoms with a remarkably short distance between O(10) and O(10') ( $2.189 \text{ \AA}$ ). The crystalline character of MOFs gave us the opportunity to discuss such a relationship between the structure of the H-bonding network and additional acid groups in the solid.

This compound also shows two different hydrated states of dihydrate (10–90%) and anhydrate (0%) in addition to the trihydrate state described above.<sup>48</sup> The crystal structures of the other states were determined using single-crystal X-ray diffraction (SCXRD) analysis (Fig. 3). The dihydrate and anhydrate states showed different space groups of  $P2_1/c$  (trihydrate:  $P\bar{1}$ ) because of a change in the orientation of  $\text{H}_2\text{adp}$  molecules by tilting in the opposite direction, whereas the fundamental structure was the same as that of the trihydrate (Fig. 4). There is no structural difference between the dihydrate and anhydrate

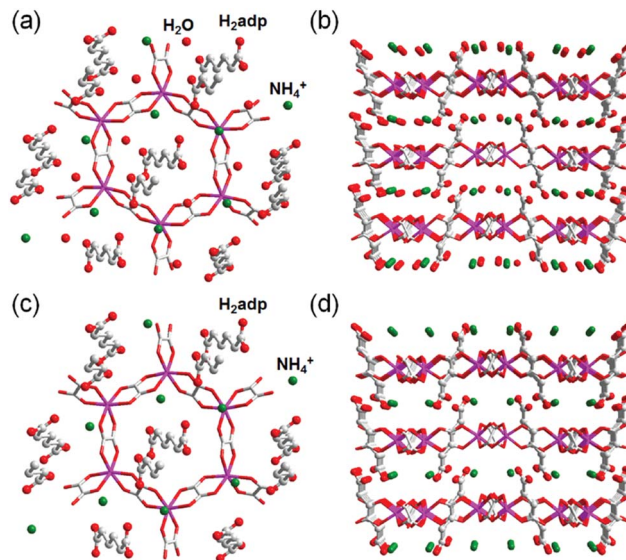


Fig. 3 Crystal structures of dihydrate and anhydrate phases. Honeycomb layer structure of (a) dihydrate and (c) anhydrate. The layered structure of (b) dihydrate and (d) anhydrate. Red, gray, green, and blue colors correspond to O, C, N, and Zn atoms, respectively. Reproduced from ref. 48 with permission from American Chemical Society, Copyright 2014.

states except for the absence of water molecules. The H-bonding networks of these phases are shown in Fig. 4. The 2-D H-bonding network between ammonium ions, water molecules, and the carboxylic acid group in the trihydrate was changed into a localized H bond in the anhydrate state because of dehydration. In the dihydrate, there also exists a 2-D H-bonding network. However, the averaged distances of the H bonds in the dihydrate became longer than those in the trihydrate. Additionally, the number of H bonds also decreased. These different states showed different conductivities. The anhydrate exhibited an insulating character ( $\sim 10^{-12} \text{ S cm}^{-1}$ ,  $25^\circ \text{C}$ ). The conductivity gradually increases with increasing RH ( $\leq 95\%$ ) to show a moderately high proton conductivity of around  $\sim 10^{-4} \text{ S cm}^{-1}$  in the dihydrate state. Finally, the trihydrate showed a superprotonic conductivity of around  $10^{-2} \text{ S cm}^{-1}$  at 98% RH. The proton conductivity in this system was consecutively controlled over the range from  $10^{-12}$  to  $10^{-2} \text{ S cm}^{-1}$  because of the change in the H-bonding networks in the pores.<sup>48</sup>

Another example of an oxalate-bridged MOF including a carboxylic acid group and water molecules,  $\{\text{NR}_3(\text{CH}_2\text{COOH})\} - [\text{M}_a\text{M}_b(\text{ox})_3] \cdot n\text{H}_2\text{O}$  ( $\text{R} = \text{Et}$  (ethyl) or  $\text{Bu}$  ( $n$ -butyl),  $\text{M}_a\text{M}_b = \text{MnCr}$ ,  $\text{FeCr}$ , or  $\text{FeFe}$ , abbreviated as  $\text{R-M}_a\text{M}_b$ ) was reported by Ōkawa *et al.* in 2012 (Fig. 5).<sup>49</sup> On the cationic components, the carboxylic acid group was located in the interlayer space to give additional protons. Adsorption measurements revealed that the water molecules ( $n = 0.5\text{--}4$ , depending on the hydrophilicity of the cationic component) were also present in the pores of the MOF (Fig. 5), but the positions of the water molecules were not determined using SCXRD. The effect of the hydrophilicity of the cationic components on the proton conduction properties was systematically studied. The proton conductivity completely depended on the type of cation (Fig. 6). According to the





Fig. 4 Representation of H-bonding networks in (a) trihydrate, (b) dihydrate, and (c) anhydrate. Reproduced from ref. 48 with permission from American Chemical Society, Copyright 2014.

adsorption measurements, the hydrophilic compounds, *i.e.*, those with a large number of water molecules in the interlayer space, showed a higher proton conductivity than the others. The most hydrophilic compound, Et-FeCr, showed the highest proton conductivity above  $10^{-4}$  S cm $^{-1}$  (25 °C, 80% RH). By contrast, the hydrophobic compound, Bu-FeCr, does not show high proton conduction under the same conditions. The relationship between water adsorption and proton conductivity in the same framework structure clearly suggested that the H-bonding network in the pore plays a critical role for high proton conduction.

Shigematsu *et al.* reported on the proton conductivity of MIL-53 derivatives,  $[M(OH)(bdc-R)]$  ( $M^{3+} = Al^{3+}$  or  $Fe^{3+}$ ;  $bdc^{2-} = 1,4$ -benzenedicarboxylate;  $-R = -COOH$ ,  $-H$ ,  $-NH_2$ ,  $-OH$ ), having different functional groups such as carboxylic acid, amino, and hydroxyl groups.<sup>37</sup> Other derivatives of the 1,4-benzenedicarboxylic acid (bdc) ligands, having various functional groups, can be introduced without major structural changes of the MIL-53 framework. These functional groups are arranged along the one-dimensional (1-D) channels of MIL-53, which can include



Fig. 5 The crystal structure of  $\{NR_3(CH_2COOH)\}-[MCr(ox)_3] \cdot nH_2O$ . (a) Representation of the coordination geometry around  $Mn^{II}$  and  $Cr^{III}$ , (b) the honeycomb layer structure, and (c) stacking view along the layers. Reproduced from ref. 49 with permission from American Chemical Society, Copyright 2012.

water molecules (Fig. 7). Then, in the 1-D channel, an additional proton from the acidic functional group, such as  $-COOH$ , can be accepted by the included water molecules to form the  $H_3O^+ - H_2O$  system in the pores. These compounds show proton conductivity in range of  $10^{-8}$ – $10^{-5}$  S cm $^{-1}$  under high humidity (95% RH) at ambient temperatures (298–353 K). The conductivity completely depends on the functional groups. The carboxylic acid-functionalized MIL-53 showed the highest conductivity, around  $10^{-5}$  S cm $^{-1}$ , suggesting that the concentration of the additional protons in the pores depends on the



Fig. 6 Humidity dependence of the proton conductivity at 298 K. The blue, green, red, purple, and gray colors correspond to the proton conductivity of Me-FeCr, Et-MnCr, Bu-FeCr, Bu-MnCr, and  $NBu_4$ , respectively. Reproduced from ref. 49 with permission from American Chemical Society, Copyright 2012.





Fig. 7 Schematic view of the basic framework structure of MIL-53.

$pK_a$  of the functional groups. The activation energies of these compounds are estimated to be 0.47–0.21 eV, which suggests that the proton conduction in these compounds mainly occurs through the Grotthuss-type mechanism.

The sulfonic acid group is one of the most acidic functional groups, having a relatively low  $pK_a$  of less than 0, meaning that if water molecules coexist,  $H_3O^+$  ions are stoichiometrically formed from the sulfonic acid group. Because the concentration of additional protons in  $H_3O^+$ – $H_2O$  is directly related to proton conductivity, the introduction of sulfonic acid is an ideal way to increase proton conductivity compared with a weak acid such as carboxylic or phosphonic acid. Phang *et al.* reported the introduction of the sulfonic acid group into the pores of a UiO-66 framework in 2015 (Fig. 8).<sup>36</sup> A post-synthetic method was used to obtain the sulfonic acid-functionalized UiO-66 (UiO-66– $(SO_3H)_2$ ). Oxidation of thiol-functionalized UiO-66 (UiO-66– $(SH)_2$ ) was performed with  $H_2O_2$  under hydrothermal conditions to give UiO-66– $(SO_3H)_2$ . Note that UiO-66 and its derivatives are quite stable even under highly acidic conditions.<sup>50</sup> UiO-66– $(SH)_2$  shows a moderate proton conductivity of  $2.5 \times 10^{-5} \text{ S cm}^{-1}$ . However, after the post-synthetic reaction, UiO-66– $(SO_3H)_2$  shows a superprotonic conductivity of  $0.84 \times 10^{-1} \text{ S cm}^{-1}$  at 80 °C under humidified conditions (90% RH), which is much higher than that of other proton conductors having carboxylic acid ( $\sim 10^{-3} \text{ S cm}^{-1}$ ) and phosphoric acid groups ( $\sim 10^{-2} \text{ S cm}^{-1}$ ). The activation energy of UiO-66– $(SO_3H)_2$  is estimated to be 0.32 eV, suggesting the existence of the Grotthuss-type mechanism in this system, while the exact positions of the adsorbed water molecules were not determined.



Fig. 8 (a) Crystal structure of UiO-66. (b) Scheme of the post-synthetic modification of UiO-66(SH)<sub>2</sub> to introduce sulfonic acid groups.

## 2.2. Hydroxide ions with water molecules

The hydroxide ion ( $OH^-$ ) also has potential for constructing a degenerate system with water molecules (the  $OH^-$ – $H_2O$  system) because of the capability of proton “back” transfer from  $H_2O$  to  $OH^-$  for the migration of the  $OH^-$  ionic carrier. In fact, the existence of the  $OH^-$ – $H_2O$  degenerate system in the water solvent was revealed by Tuckerman *et al.* in 2002 using MD simulation (Fig. 9).<sup>51</sup> The  $OH^-$  ion shows abnormally high mobility in water ( $20.6 \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1}$ ),<sup>45</sup> which is slightly lower than that of a proton ( $H^+$ : 36.2) and much higher than that of other ions (*e.g.*,  $Li^+$ : 4.0), meaning that the  $OH^-$  ion carrier potentially shows high ionic conductivity with water molecules. In the field of MOFs,  $OH^-$  ion inclusion was believed to be difficult because of the corrosive nature of the  $OH^-$  ions. Thus, MOFs seemed not to be good host materials for  $OH^-$  ions. However, recently,  $OH^-$  ions were successfully incorporated using some alkaline-stable MOFs, and their conductivity has been studied.<sup>52,56</sup>

In 2014, Sadakiyo *et al.* reported a basic design of  $OH^-$  ion-conductive MOFs. They proposed different types of MOFs that include the  $OH^-$  ion. Type A introduces the  $OH^-$  ions using cationic frameworks, while type B introduces hydroxide salts into the pores. They demonstrated a type B hydroxide ion-conducting MOF,  $(NBu_4)_m(A)_n\{Zn(mim)_2\}_6$  ( $Hmim = 2$ -methylimidazole;  $A =$  anions) (*e.g.*,  $OH^-(NBu_4-ZIF-8-OH)$ ), synthesized through a salt inclusion reaction using an alkaline-stable MOF (Fig. 10).<sup>52</sup> ZIF-8 (ref. 53) was used as a mother framework to incorporate the hydroxide ion salt of  $NBu_4OH$  into the pore of the MOF.  $NBu_4-ZIF-8-OH$  has an ionic conductivity of  $2.3 \times 10^{-8} \text{ S cm}^{-1}$  (99% RH, 25 °C), with  $10^{-12} \text{ S cm}^{-1}$  for the blank ZIF-8. From water adsorption measurements, the conductivity of  $NBu_4-ZIF-8-OH$  is derived from both  $OH^-$  and  $H_2O$ , suggesting the existence of an  $OH^-$ – $H_2O$  system in the pore. The activation energy was estimated to be 0.7 eV, which is much higher than that of hydrated  $OH^-$  ions ( $<0.2 \text{ eV}$ ),<sup>54</sup> and might be attributed to the small apertures in ZIF-8. A type A hydroxide-ion conductor was also reported by Nagarkar *et al.* in 2016.<sup>55</sup> They reported a cationic MOF  $[Ni_2(m-pymca)_3]OH \cdot nH_2O$  that includes  $OH^-$  ions as a counter ion together with water molecules in the pores (Fig. 11). The crystalline O atoms of  $H_2O$  or  $OH^-$  ions in the 1-D channel were determined by SCXRD, showing an H-bonding network between them. Thus, the  $OH^-$ – $H_2O$  system should exist in the 1-D channel. This MOF showed a high ionic conductivity of  $0.8 \times 10^{-4} \text{ S cm}^{-1}$  (99% RH, 27 °C) at ambient temperatures. They also showed a large difference in



Fig. 9 Schematic illustration of the migration of  $OH^-$  ions with water molecules in a solvent. Reproduced from ref. 51 with permission from Nature Publishing Group, Copyright 2002.





Fig. 10 Representation of the crystal structure of ZIF-8 (ref. 53) and a schematic image of salt inclusion. (a) Cage and (b) 3-D porous SOD structures of ZIF-8. (c) Schematic view of the preparation procedure for  $NBu_4-ZIF-8-OH$ . Reproduced from ref. 52 with permission from American Chemical Society, Copyright 2014.



Fig. 11 (a) Crystal structure of  $[Ni_2(m-pymca)_3]OH \cdot nH_2O$  along the channel. (b) Schematic representation of a cationic MOF with an anionic supramolecular chain of hydroxide anions and water molecules inside the MOF pore for efficient hydroxide ion conduction. Reproduced from ref. 55 with permission from Royal Society of Chemistry, Copyright 2016.

conductivities under  $H_2O$  and  $D_2O$ , which indicates that a proton transfer process is included in the ionic conduction in this system. The activation energy was estimated to be 0.19 eV, which is quite a low value as in the case of proton conduction by the Grotthuss mechanism, implying that the  $OH^-$  ion conduction in this system occurs by a Grotthuss-like mechanism, *i.e.*, a proton “back” transfer along the H-bonding network.

Another example was reported by Li *et al.* in 2017.<sup>56</sup> Free  $OH^-$  ions together with various cations (*i.e.*,  $NBu_4$  and [EVIm] (EVIm = 1-ethyl-3-vinylimidazolium)) were incorporated into a charge-neutral MOF (Fig. 12),  $[Cu_6(NDI)_3] \cdot guest$  (**FJU-66**,  $H_2NDI = 2,7$ -bis(3,5-dimethyl)dipyrazol-1,4,5,8-naphthalene-tetracarboxydiimide). **FJU-66** showed extremely high stability under alkaline conditions at around pH 14 and thus could be used as an alkaline-stable mother framework. The conductivity of **FJU-66** with the hydroxide salt completely depends on the included



Fig. 12 Ionic transport pathway of **FJU-66[EVIm]OH**. (a) Packing view of **FJU-66[EVIm]OH** along the *a* direction. (b) Packing view of the available water pathways in **FJU-66** along the *a* and *b* directions. (c) Possible supramolecular chain formed by  $OH^-$  anions and water molecules inside the channel of **FJU-66** for efficient  $OH^-$  ion conduction. Reproduced from ref. 56 with permission from American Chemical Society, Copyright 2017.

salts and is in the range from  $10^{-7}$  to  $10^{-2} S cm^{-1}$  at 30 °C under 95% RH. **FJU-66[EVIm]OH** showed the highest conductivity of  $5.7 \times 10^{-2} S cm^{-1}$  with a very low activation energy of 0.11 eV, suggesting that ionic conduction occurs through a Grotthuss-like mechanism using the proton back transfer.

### 3. Ammonia-based degenerate system for proton conduction in MOFs

The pore of MOFs is a useful space for the encapsulation of small molecules such as gases, organic molecules, and proton-conducting media. In particular,  $NH_3$  adsorption in MOFs has been investigated for the storage of a renewable energy source with a high energy density, as well as removal of corrosive and toxic gases. In general, however, the presence of  $NH_3$  species is detrimental to most MOF compounds because  $NH_3$  can replace the existing ligand, resulting in structural decomposition. Nevertheless, the  $NH_3$  ( $NH_4^+$ ) encapsulated in a pore can serve as an efficient proton conducting medium in MOFs because of its H-bonding ability. In addition,  $NH_3$  is able to generate a  $NH_4^+ - OH^-$  system with water molecules because of its high solubility. Meanwhile the degenerate system of  $NH_4^+ - NH_3$  can be described as a coexistence of protonated  $NH_3$  and pure  $NH_3$ . The mobility of  $NH_4^+$  in the presence of  $NH_3$  is  $0.94 \pm 0.35 cm^2 s^{-1} V^{-1}$ ,<sup>57</sup> which is a lower value than that for other ions ( $H^+$ ,  $OH^-$ , and  $Li^+$ )<sup>45</sup> in water. However, its H-bonding ability facilitates long range proton diffusion through the H-bond network. In this section, we deal with the stability of MOFs against  $NH_3$  and  $NH_3$  ( $NH_4^+$ )-mediated proton conductivity, and the dynamic behavior of  $NH_3$  ( $NH_4^+$ ) in the pores of MOFs for proton conduction.

#### 3.1. Stability of metal-organic frameworks against $NH_3$

The structural stability of MOFs has been widely investigated with respect to thermal, chemical, and mechanical aspects because it is an important factor for various applications.<sup>50,51,58</sup> In particular, the stability in the presence of water species is



a crucial issue for real-world applications because water vapor exists in process environments such as natural gas streams, industrial flue gas, or pollutant separation.<sup>59</sup> Moreover, the stability of MOFs toward hydrolysis is one of the key factors for proton-conductive MOFs. Like in a water system, NH<sub>3</sub>-mediated proton conductivity in MOFs can be affected by structural stability under the NH<sub>3</sub> atmosphere because NH<sub>3</sub> is able to work not only as a conducting medium, but also as a coordinating ligand. Fundamentally, the structural stability of MOFs against NH<sub>3</sub> is estimated by the gas sorption isotherm and powder X-ray diffraction (PXRD) pattern analysis. The unstable MOFs indicate decreased porosity and surface areas with degradation of crystallinity, including peak broadening in PXRD patterns during the repeated NH<sub>3</sub> adsorption-desorption process. Previously, MOFs constructed from Zn<sub>4</sub>O or Cu-paddlewheels as secondary building units (SBUs) have been reported to be unstable in NH<sub>3</sub>.<sup>60,61</sup> By contrast, in most cases, there is no mention of structural stability for MOFs in NH<sub>3</sub> sorption experiments. In 2014, Kajiwara *et al.* reported on a systematic stability study of various types of MOFs against NH<sub>3</sub> gas (Table 1).<sup>62</sup> They considered the effects of the metal cation species and type of organic linker. To check the stability of MOFs against NH<sub>3</sub>, degassed samples were loaded into an NH<sub>3</sub> exposure system for 2 h at various temperatures and PXRD patterns were compared before and after NH<sub>3</sub> exposure. Some MOFs that had high thermal stability decomposed at room temperature under the NH<sub>3</sub> atmosphere. The metal center of MOFs is strongly related to stability. Specifically, the divalent metal cation is unstable under NH<sub>3</sub>, except for MOF-74 and ZIF-8. In addition,

MOFs constructed from oxophilic metal cations, such as MIL-125(Ti<sup>IV</sup>), UiO(Zr<sup>IV</sup>), MIL-103(Tb<sup>III</sup>), and MOF-76(Ln<sup>III</sup>), show a high stability toward NH<sub>3</sub>, whereas the less oxophilic In<sup>III</sup> center is kinetically labile and reacts easily with the N of NH<sub>3</sub>. The most stable MOFs were derived from Al(III) and Cr(III) metal cations because of the inertness of the metal cation and oxophilicity. Furthermore, the ligand length and the metal-ligand bond strength are stability factors. Longer ligands weaken the structural stability because of the high void space generation. For ZIF-8, the anionic mim linker with a formal charge of -0.5 on each N atom has a stronger basicity than NH<sub>3</sub> and is strongly bound to the metal center. Consequently, seven types of MOFs, such as MIL-53(Al), Al-BTB, MOF-76(M) (M = Y, Yb), MIL-101(Cr), ZIF-8, and MOF-74(Mg), which have an oxophilic M<sup>II</sup> center, chemically inert M<sup>III</sup> center, chelate-type coordinating ligand, or anionic linker, showed high stability with NH<sub>3</sub> up to 350 °C. These materials are also highly stable in water,<sup>63,64</sup> which implies that the stability of MOFs against NH<sub>3</sub> has a similar trend toward water. Considering the predictions for the deconstruction of MOFs by NH<sub>3</sub>, the decomposition mechanism is similar to that of water.<sup>60,65</sup>

Rieth and Dinca reported in 2018 on NH<sub>3</sub> adsorption capacity, kinetics, and structural stability against NH<sub>3</sub> for iso-reticular MOFs.<sup>66</sup> They synthesized M<sub>2</sub>Cl<sub>2</sub>BTDD and M<sub>2</sub>Cl<sub>2</sub>-BBTA, which have different pore sizes achieved by ligand extension (Fig. 13, M = Co, Ni, Cu; BTDD = bis(1*H*-1,2,3-triazolo [4,5-*b*],[4',5'-*i*])dibenzo[1,4]dioxin; BBTA = 1*H*,5*H*-benzo(1,2-*d*),(4,5-*d'*)bistriazole). Among the three metal species, Ni<sup>2+</sup> compounds are most stable toward NH<sub>3</sub>. Ni<sub>2</sub>Cl<sub>2</sub>BBTA with

Table 1 The results of the ammonia stability test for MOFs<sup>62</sup>

Compounds	Chemical formula (* <sup>a</sup> )	<i>T</i> <sub>d</sub> <sup>b</sup> [°C]	Metal ion oxidation state	Thermal stability with NH <sub>3</sub> <sup>c</sup>			
				RT	200 °C	300 °C	350 °C
	Cu <sub>2</sub> (bpdc) <sub>2</sub> (bpy)	310	II	–			
	Zn <sub>3</sub> (bpdc) <sub>3</sub> (bpy)	380	II	–			
HKUST-1	Cu <sub>3</sub> (btc) <sub>2</sub> *	340	II	–			
MOF-5	Zn <sub>4</sub> O(bdc) <sub>3</sub>	420	II	–			
	Mg(for) <sub>2</sub>	430	II	–			
MIL-68(In)	In(OH)(bdc)	450	III	–			
MIL-125	Ti <sub>8</sub> O <sub>8</sub> (OH) <sub>4</sub> (bdc) <sub>6</sub>	360	IV	+	+	–	
UiO-66	Zr <sub>6</sub> O <sub>4</sub> (OH) <sub>4</sub> (bdc) <sub>6</sub> *	470	IV	+	+	–	
UiO-67	Zr <sub>6</sub> O <sub>4</sub> (OH) <sub>4</sub> (bpdc) <sub>6</sub> *	490	IV	+	+	–	
MIL-103(Tb)	Tb(btb)*	490	III	+	+	–	
MOF-74(Ni)	Ni <sub>2</sub> (dobdc)*	340	II	±	±	±	±
MOF-74(Mg)	Mg <sub>2</sub> (dobdc)*	390	II	+	+	+	+
MOF-74(Zn)	Zn <sub>2</sub> (dobdc)*	430	II	+	+	±	±
MOF-76(Tb)	Tb(btc)*	470	III	+	+	+	–
MOF-76(Y)	Y(btc)*	>500	III	+	+	+	+
MOF-76(Yb)	Yb(btc)*	>500	III	+	+	+	+
DUT-5	Al(OH)(bpdc)	>500	III	+	+	±	–
MIL-53(Al)	Al(OH)(bdc)	>500	III	+	+	+	+
MIL-101(Cr)	Cr <sub>3</sub> O(OH)(bdc) <sub>3</sub> *	390	III	+	+	+	+
Al-BTB	Al(btb)	>500	III	+	+	+	+
ZIF-8	Zn(mim) <sub>2</sub>	>500	II	+	+	+	+

<sup>a</sup> MOFs with open metal sites are denoted with \*. <sup>b</sup> Thermal decomposition temperature determined by TGA. <sup>c</sup> +, the structure is maintained; ±, partially decomposed; –, completely decomposed. Abbreviations of ligands: bpy = 4,4'-bipyridine (ND), for = formate (OD), mim = 2-methylimidazole (ND), bdc = benzene-1,4-dicarboxylate (OD), bpdc = biphenyl-4,4'-dicarboxylate (OD), btc = benzene-1,3,5-tricarboxylate (OD), dobdc = 2,5-dioxidobenzene-1,4-dicarboxylate (OD), and btb = benzene-1,3,5-tris(4-benzoate) (OD). OD: oxygen donor; ND: nitrogen donor.





between H<sub>2</sub>adp and water molecules (O(7)⋯O(10), 3.043(4) Å and O(7)⋯O(9), 3.122(3) Å); and between water molecules (O(9)⋯O(10), 2.711(7) Å) are closed to those of (NH<sub>4</sub>)<sub>2</sub>(H<sub>2</sub>adp) [Zn<sub>2</sub>(ox)<sub>3</sub>]·3H<sub>2</sub>O. This implied that the counterion exchange is not effective in a guest molecule arrangement. However, a remarkable difference is the non-hydrogen bonding of the K<sup>+</sup> ion instead of the H-bonding NH<sub>4</sub><sup>+</sup>, despite the nearly identical position (Fig. 14). The absence of H-bonding associated with NH<sub>4</sub><sup>+</sup> provided a lower proton conductivity (1.2 × 10<sup>-4</sup> S cm<sup>-1</sup> at 25 °C, under 98% RH) by approximately two orders of magnitude compared with that of NH<sub>4</sub><sup>+</sup>. These results strongly suggest that the NH<sub>4</sub><sup>+</sup> medium is crucial not only for increasing proton carrier concentration by acidic character (pK<sub>a</sub> = 9.2), but also for facilitating proton transfer by forming H bonding with neighboring molecules.

In 2011, Pardo *et al.* reported an oxalate-bridged bimetallic 3-D chiral anionic network including NH<sub>4</sub><sup>+</sup> species with the formula (NH<sub>4</sub>)<sub>4</sub>[MnCr<sub>2</sub>(ox)<sub>6</sub>]·4H<sub>2</sub>O (Fig. 15).<sup>72</sup> In the framework, two types of oxalate ligands are observed. One of them shows the uncoordinated O of the oxalate ligand, which is directed toward ordered water molecules in channel A along the helical *c*-axis. Another oxalate ligand links Cr(III) to Mg(II) ions in a bis-bidentate way. The counterions (NH<sub>4</sub><sup>+</sup>) and the guest molecules (H<sub>2</sub>O) are located around the oxalate network in the A channel, giving rise to high proton conductivity at room temperature. In the two types of channels (A and B), the A channel, decorated by the terminal O of oxalate, has a well-defined helical chain of ammonium cations [N⋯N = 2.839(7)–2.892(6) Å], indicating H-

bonding networks with the O atoms of the terminal oxalates [N⋯O = 2.795(6)–2.960(8) Å]. Although water molecules are present in both pores, the water molecules in channel A, stabilized by the terminal oxalate O with an H-bonding network, are only refined. As humidity increases, the  $\sigma$  value is enhanced by five orders of magnitude from 2.4 × 10<sup>-9</sup> S cm<sup>-1</sup> at 9% RH to 1.1 × 10<sup>-3</sup> S cm<sup>-1</sup> at 96% RH, which improved to 1.7 × 10<sup>-3</sup> S cm<sup>-1</sup> at 313 K. The activation energy ( $E_a$ ) for the ionic conductivity estimated from the Arrhenius plot is 0.23 eV (Fig. 15b inset). These results imply that the high proton conductivity is derived from an efficient H-bonding network through the Grotthuss mechanism. They believed that the A channel that included H-bonding networks among the terminal oxalate, NH<sub>4</sub><sup>+</sup> cations, and ordered H<sub>2</sub>O molecules is an attractive potential pathway for the proton conduction triggered by humidity.

**3.2.2 Aqueous-NH<sub>3</sub> inclusion in MOFs.** Aqueous NH<sub>3</sub> (ammonia water) is a solution of NH<sub>3</sub> in water. Recently, a few results have been reported for the proton conductivity of MOFs using various concentrations of aqueous NH<sub>3</sub> solution vapor instead of pure water vapor.<sup>73–75</sup> In 2014, Bazaga-García *et al.* reported the enhanced proton conductivity of a calcium phosphonate framework through post-synthetic modifications using aqueous NH<sub>3</sub>.<sup>73</sup> The calcium phosphonate framework was constructed from Ca<sup>2+</sup> ions and the rigid polyfunctional ligand 5-(dihydroxyphosphoryl) isophthalic acid (PiPhtA), giving the formula Ca<sub>2</sub>[(HO<sub>3</sub>PC<sub>6</sub>H<sub>3</sub>COOH)<sub>2</sub>]<sub>2</sub>[(HO<sub>3</sub>PC<sub>6</sub>H<sub>3</sub>(COO)<sub>2</sub>H)(H<sub>2</sub>O)<sub>2</sub>]·5H<sub>2</sub>O, Ca-PiPhtA-I. Ca-PiPhtA-I has a high water content in the Ca<sup>2+</sup> metal centre (two water molecules coordinated) and a 1-D



Fig. 15 (a) Structure of (NH<sub>4</sub>)<sub>4</sub>[MnCr<sub>2</sub>(ox)<sub>6</sub>]·4H<sub>2</sub>O. NH<sub>4</sub><sup>+</sup> counterion and H<sub>2</sub>O guest molecules are represented as a sphere. Red, green, gray, cyan, and blue correspond to oxygen, chromium, carbon, manganese, and nitrogen atoms, respectively. (b) Cole–Cole semi-circle plot at 295 K and 96% RH. (c) RH dependence of  $\sigma$  for (NH<sub>4</sub>)<sub>4</sub>[MnCr<sub>2</sub>(ox)<sub>6</sub>]·4H<sub>2</sub>O at 295 K. Reproduced from ref. 72 with permission from American Chemical Society, Copyright 2011.

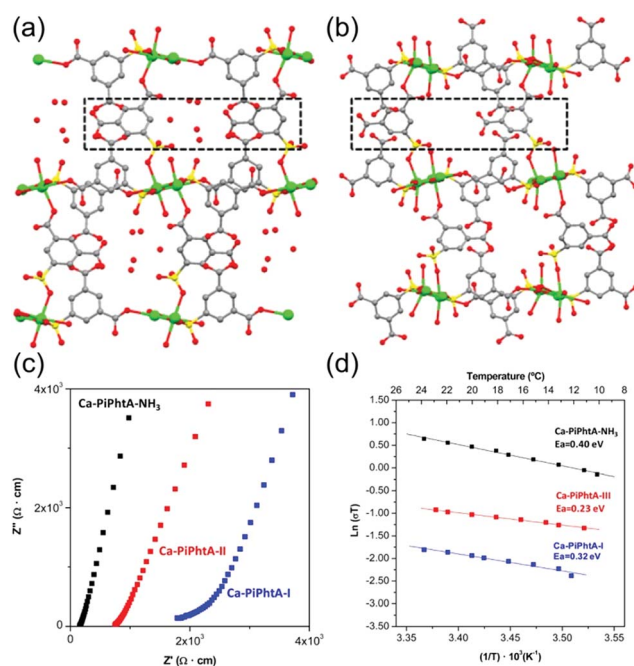


Fig. 16 *b*-axis view (*a*-axis horizontal) of the crystal structures of Ca-PiPhtA-I (a) and Ca-PiPhtA-II (b) showing the slightly different conformation of the 1-D channels along the *c* axis. (c) Plot of the complex impedance plane of Ca-PiPhtA compounds at 24 °C and 98% RH. (d) Arrhenius plots vs.  $T^{-1}$  from 10 to 24 °C. Reproduced from ref. 73 with permission from American Chemical Society, Copyright 2014.



channel (five lattice water molecules). In this pillared layered structure, the hydrophilic 1-D channel is observed along the *b*-axis, which is filled with five lattice water molecules per unit cell. The lattice water molecules exhibit water-to-water interactions providing an extended H-bond network along the 1-D channels as a potential proton transfer pathway. The removal of the five lattice water molecules at 75–130 °C indicated a partially dehydrated structure (Ca-PiPhtA-II, Fig. 16b). To include the NH<sub>3</sub> species in the pore, Ca-PiPhtA-I was exposed to 28% aqueous NH<sub>3</sub> solution, resulting in the inclusion of 7NH<sub>3</sub> and 16H<sub>2</sub>O molecules in Ca-PiPhtA-NH<sub>3</sub>. However, a detailed structural analysis of Ca-PiPhtA-NH<sub>3</sub> is impossible because of the lack of crystallinity with a partial structure decomposition. The IR spectrum of Ca-PiPhtA-NH<sub>3</sub> reveals that the water stretching vibrational signal shifts to a lower wave number, implying the presence of a strong H bond. Interestingly, the dehydrated sample does not take up NH<sub>3</sub> in NH<sub>3</sub>-temperature programmed desorption (TPD) measurements, which means that NH<sub>3</sub>-H<sub>2</sub>O adsorption occurred through the cooperative mechanism of H-bonding interactions. The proton conductivity values for Ca-PiPhtA-I and Ca-PiPhtA-II were  $5.7 \times 10^{-4}$  and  $3.6 \times 10^{-4}$  S cm<sup>-1</sup> at 24 °C and 98% RH, respectively. These values increased up to  $1.3 \times 10^{-3}$  S cm<sup>-1</sup> at 40 °C (water-equilibrated state was called Ca-PiPhtA-III). However, the conductivity value was not retained at high temperatures (>45 °C) because of the dehydration process. Ca-PiPhtA-NH<sub>3</sub> represented a maximum value of  $\sigma$  ( $6.6 \times 10^{-3}$  S cm<sup>-1</sup>) at 24 °C and 98% RH. The activation energies (*E*<sub>a</sub>) for the proton transfer in Ca-PiPhtA-I (0.32 eV), Ca-PiPhtA-III (0.23 eV), and Ca-PiPhtA-NH<sub>3</sub> (0.40 eV) are in the range of those of the Grotthuss mechanism.

Liang *et al.* investigated in 2014 the difference in proton conductivity in water and various concentrations of the aqua NH<sub>3</sub> medium. They used two 3-D Co<sup>II</sup> MOFs,  $\{[\text{Co}_3(m\text{-ClPhIDC})_2(\text{H}_2\text{O})_6] \cdot 2\text{H}_2\text{O}\}_n$  [1; *m*-ClPhH<sub>3</sub>IDC = 2-(*m*-chlorophenyl)imidazole-4,5-

dicarboxylic acid] and  $\{[\text{Co}_3(p\text{-ClPhHIDC})_3(\text{H}_2\text{O})_3] \cdot 6\text{H}_2\text{O}\}_n$  (2; *p*-ClPhH<sub>3</sub>IDC = 2-(*p*-chlorophenyl)imidazole-4,5-dicarboxylic acid) (Fig. 17).<sup>74</sup> The two compounds have a similar 1-D channel system and different water contents (coordinating six and two free water molecules for 1 and coordinating three and six free water molecules for 2). Furthermore, these compounds are highly stable while soaking in water and in boiling water, or under treatment with 7.4 M NH<sub>3</sub>·H<sub>2</sub>O solution vapor without structural change. However, the crystal structures and guest composition of the aqueous NH<sub>3</sub>-treated samples were not given. The conductivity of compound 1 under humid conditions (98% RH, 30 °C) was  $2.73 \times 10^{-6}$  S cm<sup>-1</sup> and increased to  $7.62 \times 10^{-4}$  S cm<sup>-1</sup> at 100 °C with an activation barrier of 1.58 eV. By contrast, compound 2 showed a maximum proton conductivity of  $2.47 \times 10^{-4}$  S cm<sup>-1</sup> at 90 °C and 98% RH. For further enhanced proton conductivity, the two MOFs were exposed to different concentrations of aqua-NH<sub>3</sub> vapor from 2.11 to 7.40 M. As the NH<sub>3</sub> concentration increased to 7.40 M, the conductivity values of the two MOFs increased by two orders of magnitude, from  $7.44 \times 10^{-7}$  to  $4.39 \times 10^{-5}$  S cm<sup>-1</sup> for 1 and from  $5.71 \times 10^{-7}$  to  $4.23 \times 10^{-5}$  S cm<sup>-1</sup> for 2. At 100 °C with a concentration of 7.4 M, these MOFs have a superionic conductivity of  $2.89 \times 10^{-2}$  and  $4.25 \times 10^{-2}$  S cm<sup>-1</sup>, respectively. Obviously, both factors, a high concentration of aqua NH<sub>3</sub> vapor and temperature, are beneficial for proton conduction. The activation energy barrier of compound 1 at an NH<sub>3</sub>-H<sub>2</sub>O concentration of 4.93 M was changed from 0.25 eV at 30–60 °C to 0.73 at 70–100 °C, which means that proton-hopping diffusion is favorable through the H-bonding networks at low temperatures (<60 °C), and that the vehicular transfer motion of NH<sub>4</sub><sup>+</sup> and H<sub>3</sub>O<sup>+</sup> is dominant at high temperatures (>60 °C). The enhanced conductivity triggered by the aqueous-NH<sub>3</sub> vapor originated from protonation of the conducting medium and the H-bonding ability of NH<sub>4</sub><sup>+</sup> with a synergistic effect on the proton conduction process. However, for an intuitive understanding of the proton conduction mechanism, obtaining a convincing structure for NH<sub>3</sub> confined in MOFs remains challenging.

### 3.2.3 Additional protonation to anhydrous NH<sub>3</sub> in MOFs.

Previous studies have demonstrated NH<sub>3</sub> (NH<sub>4</sub><sup>+</sup>)-mediated proton conductors through the simultaneous introduction of the NH<sub>4</sub><sup>+</sup> counterion during MOF synthesis or aqueous-NH<sub>3</sub> vapor loading exhibiting an improved proton conductivity. Anhydrous NH<sub>3</sub>-mediated proton conductivity was reported recently using MIL-53(Al) derivative MOFs through pure NH<sub>3</sub> gas adsorption.<sup>76</sup> MIL-53 (Al) derivatives that are well known for their high stability are synthesized from Al<sup>III</sup> ions and H<sub>2</sub>bdc ligands with various functional groups, (H<sub>2</sub>bdc-(COOH)<sub>2</sub>, 1), (H<sub>2</sub>bdc-(NH<sub>2</sub>), 2), (H<sub>2</sub>bdc-(OH), 3), and (H<sub>2</sub>bdc, 4), indicating the difference in proton-donating ability (*pK*<sub>a</sub>). All samples are stable under 100 kPa of NH<sub>3</sub>. In NH<sub>3</sub> adsorption-desorption measurements, compound 1 adsorbed two more additional equivalents of NH<sub>3</sub> than the other compounds because of the acid-base reaction by the dangling two carboxylic acid groups in the ligand (Fig. 18a). This implies that NH<sub>3</sub> can exist as NH<sub>4</sub><sup>+</sup> species, which is confirmed by IR spectroscopy, XPS, and solid-state <sup>2</sup>H NMR. The crystal structures incorporating NH<sub>3</sub> molecules were determined by Rietveld refinement analysis of PXRD, which shows the formation of an H-bonding network among

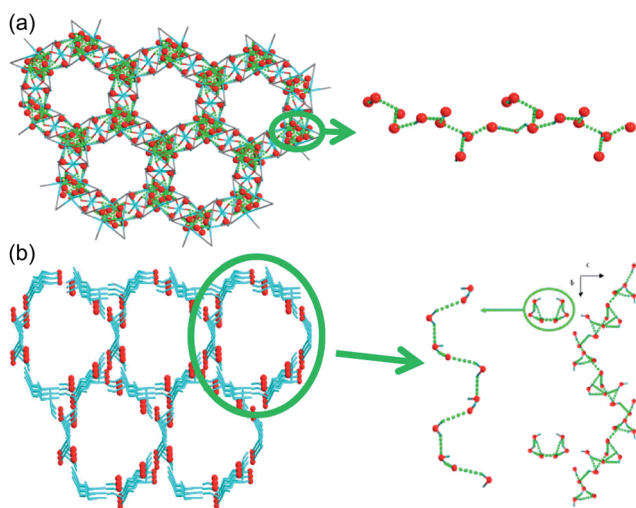
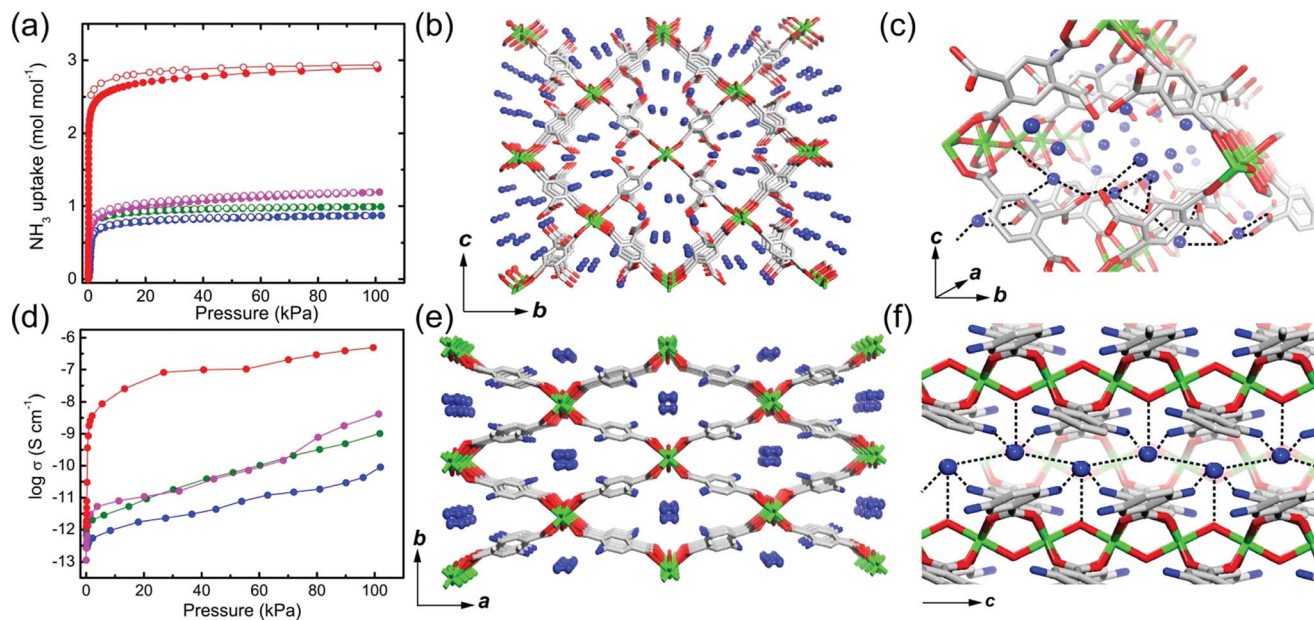


Fig. 17 1-D channels with water molecules in (a)  $\{[\text{Co}_3(m\text{-ClPhIDC})_2(\text{H}_2\text{O})_6] \cdot 2\text{H}_2\text{O}\}_n$  (1) and (b)  $\{[\text{Co}_3(p\text{-ClPhHIDC})_3(\text{H}_2\text{O})_3] \cdot 6\text{H}_2\text{O}\}_n$  (2). Red spheres represent O atoms in water, and green dots present H-bonding networks. Reproduced from ref. 74 with permission from American Chemical Society, Copyright 2017.





**Fig. 18**  $\text{NH}_3$  adsorption–desorption isotherm, structure of  $\text{NH}_3$ @MIL-53(Al) derivatives, and proton conductivity. (a)  $\text{NH}_3$  adsorption–desorption profiles at 298 K and 100 kPa. The different colors represent MIL-53(Al) derivatives ( $-(\text{COOH})_2$ , red;  $-\text{NH}_2$ , green;  $-\text{OH}$ , pink;  $-\text{H}$ , blue). (b and c) Crystal structures of  $\text{NH}_3$ @MIL-53(Al) $-(\text{COOH})_2$  and (e and f)  $\text{NH}_3$ @MIL-53(Al) $-(\text{NH}_2)$ . (d)  $\text{NH}_3$  pressure dependence of proton conductivity in MIL-53(Al) derivatives. Reproduced from ref. 76 abiding by the terms of the license from Chemrxiv, Copyright 2018.

the  $\text{NH}_3$ , the framework ( $\mu\text{-OH}$  and the functional group of the ligand), and the adjacent  $\text{NH}_3$  (Fig. 18c and f). The confined  $\text{NH}_3$  guests are aligned in a zigzag shape along the 1-D channels, and the distance of adjacent  $\text{NH}_3$  was shortened with decreased acidity of the functional group because of the reduced attraction from the pore wall. Meanwhile,  $\text{NH}_3$  molecules confined in MIL-53(Al) $-(\text{COOH})_2$  are well distributed in the overall framework with a strong interaction supported by  $\text{NH}_3$ -TPD. Proton conductivity was measured by using an *in situ* system with controlled pure  $\text{NH}_3$  gas pressure. The initial low conductivity values of the four compounds under vacuum at 298 K ( $1.2 \times 10^{-12}$ ,  $2.8 \times 10^{-13}$ ,  $1.1 \times 10^{-13}$ , and  $6.6 \times 10^{-13}$   $\text{S cm}^{-1}$ ) markedly increased up to  $4.9 \times 10^{-7}$ ,  $1.0 \times 10^{-9}$ ,  $4.2 \times 10^{-9}$ , and  $9.1 \times 10^{-11}$   $\text{S cm}^{-1}$  for **1**, **2**, **3**, and **4**, respectively, as the  $\text{NH}_3$  pressure increased to 100 kPa (Table 2). The small change in the  $\text{NH}_3$  pressure and pore environment by the functional group triggers a large change in the conductivity. As expected, the acid functional group in the ligand strongly affects the proton conductivity and the simultaneous formation of  $\text{NH}_4^+$  species plays a key role in a degenerate  $\text{NH}_4^+ + \text{NH}_3 \rightleftharpoons \text{NH}_3 +$

$\text{NH}_4^+$  proton diffusion pathway. Under the saturated  $\text{NH}_3$  pressure at 290 K, the conductivity of compound **1** became  $2.56 \times 10^{-5}$   $\text{S cm}^{-1}$ , which is comparable to the anhydrous proton conductivity in MOFs. The activation energy for proton conduction in compound **1** estimated by using the Arrhenius plot under  $\text{NH}_3$  saturated pressure at various temperatures is 0.46 eV. These results are the first report of anhydrous  $\text{NH}_3$ -mediated proton-conductive MOFs with crystallographic analysis.

### 3.3. Dynamic behavior of $\text{NH}_4^+$ for proton conductivity in MOFs

Molecular dynamics (MD) is one of the interesting topics regarding porous MOFs. Molecules located in the pore interact with a framework and exhibit a unique behavior. Indeed, the dynamic behavior of the conducting medium incorporated in porous materials helps in understanding the proton conduction mechanism. In particular, quasi-elastic neutron scattering (QENS) and solid-state NMR are powerful tools for investigating the dynamic molecular motion of protic species because the H atom has a larger incoherent neutron-scattering cross section ( $\sigma_{\text{inc}} = 80b$ ,  $1b = 10^{-24}$   $\text{cm}^2$ ) compared with other atoms such as C ( $\sigma_{\text{inc}} = 0b$ ), N ( $\sigma_{\text{inc}} = 0.5b$ ), O ( $\sigma_{\text{inc}} = 0b$ ), and D ( $\sigma_{\text{inc}} = 2.1b$ ), and NMR is a selectively sensitive probe for local MD. Therefore, the dynamic motions of all species containing an H atom can be selectively detected through incoherent neutron scattering and NMR.

In 2014, Miyatsu *et al.* clarified the relationship between proton conductivity and the phase transition associated with the dynamic behavior of  $\text{NH}_4^+$  and water molecules in 2-D  $(\text{NH}_4)_2(\text{H}_2\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  and  $\text{K}_2(\text{H}_2\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$ .<sup>77</sup> To measure neutron scattering, the methylene H atoms

**Table 2**  $\text{NH}_3$ -mediated proton conductivity of MIL-53(Al) derivatives<sup>76</sup>

Compounds	$\text{NH}_3$ uptake amounts <sup>a</sup> (mole per mole)	Conductivity ( $\text{S cm}^{-1}$ )	
		In a vacuum	100 kPa $\text{NH}_3$
MIL-53(Al) $-(\text{COOH})_2$	2.9	$1.2 \times 10^{-12}$	$4.9 \times 10^{-7}$
MIL-53(Al) $-\text{NH}_2$	1.0	$2.8 \times 10^{-13}$	$1.0 \times 10^{-9}$
MIL-53(Al) $-\text{OH}$	1.2	$1.1 \times 10^{-13}$	$4.2 \times 10^{-9}$
MIL-53(Al)	1.0	$6.6 \times 10^{-13}$	$9.1 \times 10^{-11}$

<sup>a</sup> 298 K and 100 kPa.





Fig. 19 2-D intensity maps obtained by neutron powder diffraction on IRIS for (a)  $(\text{NH}_4)_2(\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  and (b)  $\text{K}_2(\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$ . The intensity is given on a logarithmic scale. The white dashed line represents each transition temperature. Reproduced with permission from ref. 77 with permission from Royal Society of Chemistry, Copyright 2014.

of adipic acid in  $(\text{NH}_4)_2(\text{H}_2\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  and  $\text{K}_2(\text{H}_2\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  were deuterated to reduce their contribution to the scattering signal. Therefore, the major signals originated from  $\text{NH}_4^+$ ,  $\text{H}_2\text{O}$ , and carboxylic acid. QENS measurements were carried out using three neutron spectrometers (AGNES, IRIS, and HFBS) with different energy resolutions to cover a time range between 0.1 ps and 10 ns. In the adiabatic calorimetry experiment,  $(\text{NH}_4)_2(\text{H}_2\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  and  $\text{K}_2(\text{H}_2\text{adp})$

$[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  showed different phase transition temperatures at 86 and 138 K, respectively. Neutron powder scattering showed changes in the Bragg peaks located at  $Q = 1.60\text{--}1.64 \text{ \AA}^{-1}$  and  $Q = 1.67\text{--}1.70 \text{ \AA}^{-1}$  at the transition temperatures (Fig. 19). Compared with  $\text{K}_2(\text{H}_2\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$ ,  $(\text{NH}_4)_2(\text{H}_2\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  indicated a more dramatic change. We note that SCXRD did not provide a significant structural change between 50 and 100 K because of the difficulty of detecting H atoms in X-rays. This means that the phase transition originated from H atoms. Relaxational dynamics were studied by QENS measurements. The dynamic structure factor  $S(Q, \omega)$  was fitted to the following equations (Fig. 20a):

$$S(Q, \omega) = R(Q, \omega) \otimes \{\delta(\omega) + \sum L_i(Q, \omega)\} + \text{BG} \quad (3)$$

$$L_i(Q, \omega) = \frac{\Gamma(Q)}{(\pi\omega^2 + \Gamma^2(Q))} \quad (4)$$

where  $L_i(Q, \omega)$  describes the relaxation of H atoms and  $\Gamma(Q)$  is the half-width at half-maximum of the Lorentz function. The relaxation  $\Gamma(Q)$  is independent of  $Q$ , which means that the motions of H atoms had a local origin. The Arrhenius plot of the relaxation time in Fig. 20b shows four relaxation modes ( $E_a = 2.3, 4.5, 7.7, \text{ and } 12.9 \text{ kJ mol}^{-1}$  for  $L_1, L_2, L_3, \text{ and } L_4$ , respectively) in  $(\text{NH}_4)_2(\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  and only two relaxation modes ( $L_{K1}$  and  $L_{K2}$ ) in  $\text{K}_2(\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$ . The  $L_{K1}$  and  $L_{K2}$  modes were observed around  $L_3$  and  $L_4$ , which means that four modes ( $L_3, L_4, L_{K1}, \text{ and } L_{K2}$ ) were derived from water molecules, whereas the  $L_1$  and  $L_2$  motions having a low activation energy are associated with  $\text{NH}_4^+$ . The H bonds of  $\text{NH}_4^+$  were weaker than that of water and indicated low activation energy. The geometrical information of the two relaxation modes for  $\text{NH}_4^+$ ,  $L_1$ , and  $L_2$  was studied through the relative integrated intensities of the elastic incoherent structure factor (EISF) (Fig. 20c). The incoherent scattering reflects only the H atom motion in  $\text{NH}_4^+$  with a tetrahedral geometry because of the negligible incoherent scattering of the N atom. Among the several dynamic models, such as  $C_3$  jump,  $T_d$  jump, and continuous rotation about the  $C_3$  axis and  $C_2$  axis,  $\text{NH}_4^+$  ions continuously rotate around the  $C_3$  axis during the jumping motion between two preferred orientations. From these results, the phase transition and unique dynamic motion of  $\text{NH}_4^+$  for proton conduction could be clearly observed.

The dynamic motion and proton conduction mechanism of  $\text{NH}_4^+$  confined in MIL-53(Al)-(COOH)<sub>2</sub> were investigated by  $^2\text{H}$  solid-state NMR through line shape and spin-relaxation time analysis at various temperatures (Fig. 21).<sup>76</sup> As mentioned above, pure  $\text{NH}_3$  molecules are converted to  $\text{NH}_4^+$  by protonation from the dangling  $-(\text{COOH})_2$  in the ligand. Furthermore, one of the  $\text{NH}_3$  molecules has an interaction with the  $\mu_2\text{-OH}$  bridge. These results are reflected in an anisotropic signal (Ia: coupling parameters,  $Q_{\text{eff}} = 73 \text{ kHz}$ ,  $\eta_{\text{eff}} = 0$ ; and Ib:  $Q_0 = 223 \text{ kHz}$ ,  $\eta = 0.1$ , static  $\text{ND}_4^+$ ) and an isotropic one (II, mobile  $\text{ND}_4^+$ ). The anisotropic signal exhibits rapid rotational motion of static  $\text{NH}_3$  molecules around their  $C_3$  symmetry axis. In addition, restricted librations between  $\mu\text{-O-D-ND}_3$  contributed to the larger coupling constant in the anisotropic signal. The isotropic signal originated from the complex isotropic reorientation and

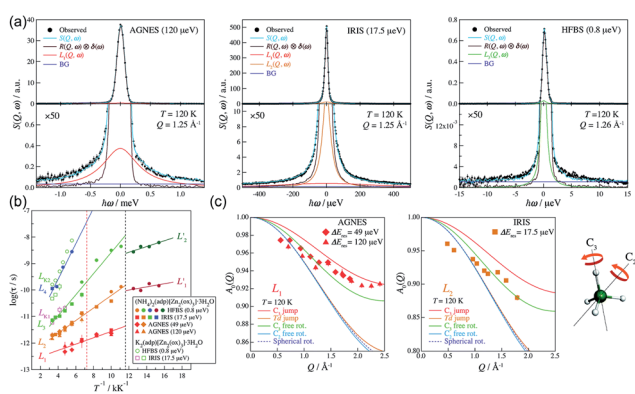
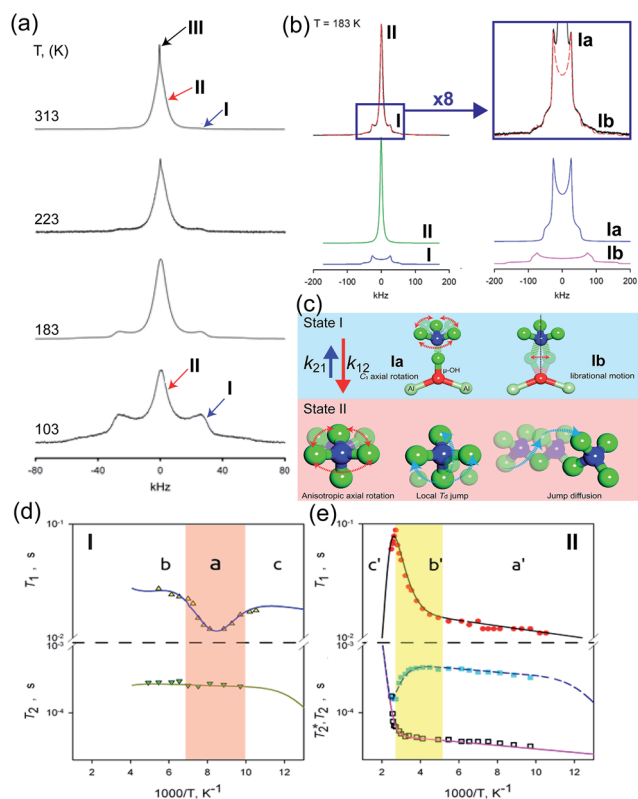


Fig. 20 (a) QENS profiles of  $(\text{NH}_4)_2(\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  obtained by using AGNES, IRIS, and HFBS spectrometers. (b) Arrhenius plot for the relaxation times of  $(\text{NH}_4)_2(\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  (filled symbols) and  $\text{K}_2(\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  (open symbols) at  $Q_{\text{av}} = 1.25 \text{ \AA}^{-1}$ . (c) EISF of  $(\text{NH}_4)_2(\text{adp})[\text{Zn}_2(\text{ox})_3] \cdot 3\text{H}_2\text{O}$  for the  $L_1$  mode measured by AGNES (left) and the  $L_2$  mode measured by IRIS (right). Solid curves represent the calculated EISF based on several model functions. Reproduced from ref. 77 with permission from Royal Society of Chemistry, Copyright 2014.





**Fig. 21** (a) The temperature dependence  $^2\text{H}$  NMR of  $\text{ND}_3$  confined in the framework with three main components marked by arrows. (b) Line shape analysis for the  $\text{ND}_3$ -saturated framework at 183 K: (top) experimental (black solid line) and full simulation (red dashed line); 8-times magnified spectra—experimental (black solid line) and full simulation (red dashed line); (bottom) simulation deconvolution into two main fractions: I (anisotropic) and II (isotropic); simulation deconvolution of the anisotropic fraction: Ia and Ib. (c) Dynamic motion of Ia: fast axial rotation, Ib: restricted libration, and II: isotropic reorientation including internal rotation, local  $T_d$  jump and jump diffusion. (d and e) Spin-relaxation time ( $T_1$  and  $T_2$ ) for I and II. Reproduced from ref. 76 abiding by the terms of the license from Chemrxiv, Copyright 2018.

local internal rotational motion of mobile  $\text{ND}_4^+$  with two distinct rotation mechanisms. All dynamic motions are shown in Fig. 21c. Although the major species of  $\text{ND}_3$  confined in the pore are the mobile  $\text{ND}_4^+$  in the overall temperature range, a small fraction of static  $\text{ND}_3$  is present even at 313 K, implying a slow exchange rate between both species ( $<0.5$  kHz). The equilibrium constant ( $K_{\text{eq}}$ ) derived from  $\exp(\Delta S/R) \exp(-\Delta H/RT)$ , where  $\Delta S = 30.34 \text{ J mol}^{-1} \text{ K}^{-1}$  and  $\Delta H = 3.4 \text{ kJ mol}^{-1}$ , coincides with the quantitative analysis of a relative population of two species through line-shape analysis. The  $T_1$  relaxation of the anisotropic signal shows a clear minimum (region a), whereas  $T_1$  of the isotropic signal exhibits flat-like behavior and a drastic increase in the high-temperature region (regions a' and b'). This means that the mobile  $\text{ND}_4^+$  has complex multiple motions in isotropic reorientation and an activation process mechanism change with the same geometrical motion. Considering the proton conduction mechanism, the local internal rotational motion of mobile  $\text{ND}_4^+$  is responsible for the Grotthuss mechanism, resulting in the diffusion

coefficient ( $D$ ) evaluated from  $C_3$  axis rotation motion being  $3.3 \times 10^{-10} \text{ m}^2 \text{ s}^{-1}$  with a  $20 \text{ kJ mol}^{-1}$  activation barrier. Furthermore, the high activation energy for proton conduction ( $0.46 \text{ eV}$ ) estimated from AC impedance measurements can account for the isotropic reorientation motion with random rotations, as well as the jump-diffusion process observed in region c'. The activation barrier of the related motion is  $50 \text{ kJ mol}^{-1}$ , with a slow correlation time ( $\tau = 3.6 \times 10^{-5} \text{ s}$ ), which gives a low diffusion coefficient ( $1 \times 10^{-15} \text{ m}^2 \text{ s}^{-1}$ ) at 300 K. Although this is a lower diffusion coefficient value than that of the hopping mechanism, the value is acceptable considering the observed conductivity. The solid-state NMR measurement strongly supports the proton conduction mechanism predicted from the crystallographic analysis.

### 3.4. Theoretical/computational study for the proton conduction mechanism

Understanding of the conduction mechanism is a key for rational designing of proton conductors. In general, polymer based-electrolytes have a lack of long range-order resulting in difficulty to characterize their conduction mechanism. However, MOFs are able to provide fundamental insight into the conduction mechanism due to their crystalline properties. Nevertheless, unlike a lot of experimental observations for proton conduction in MOFs, the theoretical and computational studies to elucidate the proton mobility inside the pore are still quite scarce. In 2013, Paesani reported molecular dynamic simulation of proton mobility in water-mediated proton transfer of flexible MIL-53(Cr), constructed from  $\text{CrO}_4(\text{OH})_2$  clusters with terephthalate linkers forming 1 D channels.<sup>78</sup> They employed the anharmonic multistate empirical valence bond (aMS-EVB)<sup>79</sup> model in a 32 unit cell of a framework with a function of the loading number ( $N$ ) of water molecules ( $N = 0$  to  $20\text{H}_2\text{O}$ ) per unit cell and temperature (300, 350, and 400 K). The model describes not only a hydrated structure but also a charge defect related to the presence of an excess proton in the H-bond network. The excess proton was randomly added to one  $\text{H}_2\text{O}$  molecule and equilibrated for 1 ns. The radial distribution function (RDF) indicated the relationship between a center of excess charge (CEC) and bridge hydroxy group ( $\mu_2\text{-OH}$ ). At a loading of  $N \leq 10\text{H}_2\text{O}$ , two broad and structured peaks are located at  $R = 3.0$  and  $5.5 \text{ \AA}$  which are indicative of strong interaction between the excess proton and  $\mu_2\text{-OH}$  in the framework, whereas a higher  $\text{H}_2\text{O}$  loading inducing pore opening by breathing shows fewer structured RDF peaks due to the screening of direct interaction by the solvation of the excess proton with water molecules. In addition, the hydrated proton structure in the pores was determined by analysis of the two dimensional probability distribution  $P(\delta, R_{\text{O}_0\text{O}_1})$  which is a difference of distance between the center of the excess charge (CEC) and the adjacent oxygen atoms ( $\text{O}_0$  and  $\text{O}_1$ ) of the  $\text{H}_2\text{O}$  molecule ( $\delta = R_{\text{O}_0\text{-CEC}} - R_{\text{O}_1\text{-CEC}}$ ). According to the analysis, the hydrated proton structure is favorable to form a distorted Eigen-like cation as  $N$  increases. In other words, Zundel-like structures of the hydrated proton are present in the narrow pore of MIL-53 with a low  $\text{H}_2\text{O}$  content. The transition free energy indicating



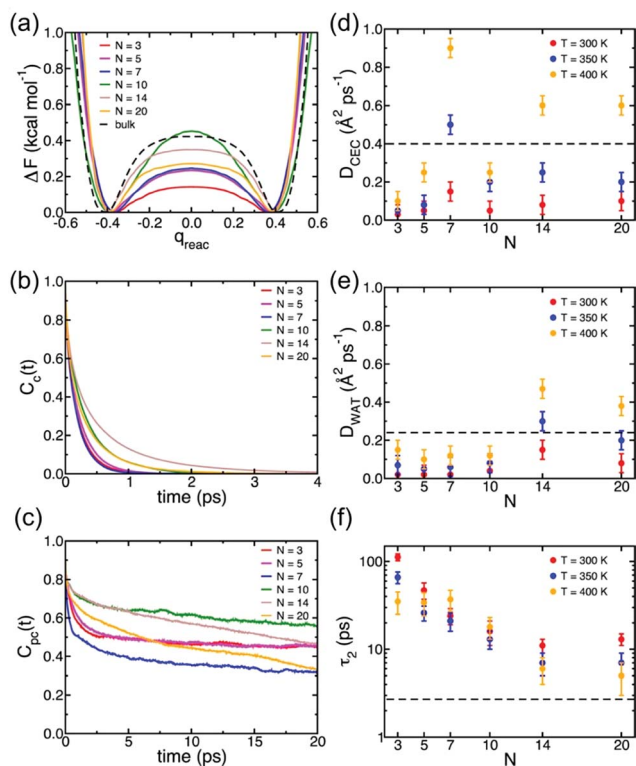


Fig. 22 (a) Free energy profiles of proton transfer in MIL-53(Cr) calculated as a function of the MS-EVB reaction coordinate  $q_{\text{reac}} = c_1^2 - c_2^2$ . The results for bulk water are taken from ref. 78. (b) Continuous time correlation function,  $C_c(t)$ . (c) Pseudocontinuous time correlation function,  $C_{\text{pc}}(t)$ . All results for MIL-53(Cr) were obtained at  $T = 300$  K as a function of the number of water molecules ( $N$ ) adsorbed per unit cell. (d) Proton diffusion coefficient,  $D_{\text{CEC}}$ . (e) water diffusion coefficient,  $D_{\text{WAT}}$ , and (f) water orientational relaxation time,  $\tau_z$ , calculated MIL-53(Cr) as a function of both temperature and number of water molecules ( $N$ ) adsorbed per unit cell. The dashed lines indicate the corresponding values calculated for bulk water at 300 K.<sup>78</sup> Reproduced from ref. 79 with permission from American Chemical Society, Copyright 2012.

proton transfer between two adjacent water molecules is expressed as  $\Delta F = -kT \ln(q_{\text{reac}})$ ,  $q_{\text{reac}} = c_1^2 - c_2^2$  ( $c_1^2$  and  $c_2^2$  being the probabilities of the two EVB states) (Fig. 22a). The central point ( $q_{\text{reac}} = 0.0$ ) means that the excess proton has symmetric hydrogen bonding with donor and acceptor water molecules. As shown in Fig. 22a, the free energy barrier is lower than that of bulk water excluding  $N = 10$  where MIL-53 undergoes a pore transition from narrow to a large pore. Moreover, the increased temperature reduces the barrier height. Overall, the relatively low free energy barrier clearly reflects that the confined environment facilitates more proton conduction than bulk water. The lifetimes,  $\tau_{\text{pc}}$ , evaluated from the fitting of the long-time decay of  $C_{\text{pc}}(t)$  are short with tens of picoseconds for  $N = 3, 5, 10$ , which are longer than that of bulk water ( $\tau_{\text{pc}} = 1.7$  ps).<sup>80</sup> It is implied that long distance proton transfer through the confined water in MIL-53 is suppressed compared to that in the bulk system. This result is coincident with the diffusion coefficient (Fig. 22d and e). As a result, the confined water-mediated proton conduction in MIL-53 shows

a low free energy barrier for proton transfer with slow proton diffusion suggesting a slow rearrangement of hydrogen bonding in the pore.

Borges *et al.* reported a joint experimental (QENS)/molecular dynamics (MD) simulation study of water-mediated proton transfer in UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub>.<sup>81</sup> The structure of UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub> is constructed by Zr<sub>6</sub>O<sub>4</sub>(OH)<sub>4</sub> cluster connected by six terephthalic acid functionalized with carboxylic acid. This compound has two types of cages, tetrahedral (5.2 Å) and octahedral (7.0 Å) connected by a triangular window. It shows a high conductivity value ( $2.3 \times 10^{-3}$  S cm<sup>-1</sup>) at RH 95% and 90 °C with a low activation energy of 0.17 eV. The result from the fitting of QENS at low and high  $Q$  indicated that there are two dynamic species. One is free protons diffusing to long distance and another is rotating water molecules. Proton diffusion happened predominantly from jumping between the solvated protons through local reorientational motion. The self-diffusion coefficients ( $D_s$ ) of the proton and water are  $3.5 \times 10^{-9}$  m<sup>2</sup> s<sup>-1</sup> and  $1.4 \times 10^{-10}$  m<sup>2</sup> s<sup>-1</sup> at 373 K, respectively. Both exhibit lower values than those of bulk water ( $D_s(\text{H}_2\text{O}) = 2.3 \times 10^{-9}$  m<sup>2</sup> s<sup>-1</sup> and  $D_s(\text{H}^+) = 9.4 \times 10^{-9}$  m<sup>2</sup> s<sup>-1</sup> at 300 K)<sup>82,83</sup> The computational approach of  $D_s$  for water is in good agreement with QENS data, whereas the simulated  $D_s(\text{CEC})$ , faster than that of H<sub>2</sub>O, was an underestimated QENS value (Fig. 23a). This observation means that proton transfer is dominated by the Grotthuss mechanism rather than the vehicle mechanism. Interestingly, MD trajectories proved that water molecules are positioned in a tetrahedral cage at 300 K having a strong interaction with the free -CO<sub>2</sub>H functional group. In addition the residence time of water molecules in the tetrahedral cage is quite long (*ca.* 3 ns) and few of them migrate to the octahedral cage exhibiting a stagnant H-bonding network in the tetrahedral cage. At high temperature, however, all cages are equally occupied by water molecules showing a longer H-bond network connected to two cages and a significantly decreased residence time (*ca.* 125 ps). The connection of cages through the longer H-bond network offers a path for proton jumping from one cage to another. Therefore, the high conductivity of UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub> is attributed to the fast diffusivity over a long distance. The further in-depth exploration of MD simulation was carried



Fig. 23 (a) Arrhenius plot of  $D_s$  for protons (squares) and water molecules (circles) in the fully hydrated UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub>: QENS (open symbols) and aMS-EVB3-MD simulations (full symbols). (b) Illustration of simulation result for the water (blue)-mediated pathway with proton (orange) along the tetrahedral (A) and octahedral (B) of UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub> at 450 K. Reproduced from ref. 81 with permission from Wiley-VCH, Copyright 2016.





Fig. 24 (a) Self-diffusivities of water (empty symbols and dashed lines) and the center of excess charge (full symbols and solid lines) simulated at 400 K in UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub> as a function of water loading defined as the number of water molecules ( $n_{H_2O}$ ) per unit cell (uc). (b) Residence time of water molecules in the cages of UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub> averaged over aMS-EVB3 trajectories obtained at 400 K as a function of water loading. (c) Simulated distribution of water in the tetrahedral (from 1 to 8) and octahedral (from 9 to 12) cages of UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub> at 400 K. Reproduced from ref. 84 with permission from American Chemical Society, Copyright 2017.

out with dependence on the loading amounts of water molecules for the solvated proton structure, thermal dynamics and dynamics of hydrated protons in the 3D cage of UiO-66(Zr)-(CO<sub>2</sub>H)<sub>2</sub>.<sup>84</sup> As the water loading increases,  $D_s(CEC)$  and  $D_s(H_2O)$  present different trends (Fig. 24a). The former substantially increases with high loading of water corresponding to high conductivity. In contrast,  $D_s(H_2O)$  has a maximum at the intermediated loading and decreases with high loading, where the guest diffusion suffers from a predominant steric hindrance effect. In addition, RDF shows a first peak around 2.5–2.6 Å which corresponds to the Zundel cation (2.5 Å). The small size (<3 Å) of first coordination sphere for pivot-hydronium ion means the deficient solvation by water molecules. The average number of hydrogen bonds per water molecules (1.1, 1.5, 1.7, 2.0, and 2.15 for 20, 40, 50, 70, and 80H<sub>2</sub>O/(unit cell, uc) is lower than that of bulk water (3.6),<sup>85</sup> which can be attributed to the confinement effect and hydrogen bonding with the -CO<sub>2</sub>H group. In addition, hydrogen bonding (HB) lifetimes ( $\tau_{HB}$ ) decrease and increase sequentially as loading amounts increase (low (93 ps), intermediate (23 ps), and high water loading (52 ps)). This can be explained by the strong trapping by -CO<sub>2</sub>H at low water loading, favorable interactions with more freedom at intermediate loading, and the static HB network induced by steric hindrance at high loading. The residence time of water in the cage at high loading is approximately 1.5 ns due to slow translation and rotation motion by the static HB network (Fig. 24b). The evaluation of excess proton migration from one cage to another cage shows a distinct number of cages crossing depending on the level of water loading. The high loading facilitates proton migration toward at least three tetrahedral cages and four octahedral cages. Therefore, high relative

humidity is beneficial to create a conduction path between cages with high conductivity. Although MD simulation is beneficial for fundamental understanding of the conduction mechanism at the molecular level, the related studies are still scarce. Future endeavors for computational study toward the various MOF structures and conducting media are required.

## 4. Conclusions and prospects

A H-bonded degenerate system of a conducting medium through acid–base chemistry is an interesting platform to design efficient solid-state proton conductors. In particular, H<sub>2</sub>O and NH<sub>3</sub> having an attractive conjugate acid–base system (H<sub>3</sub>O<sup>+</sup>–H<sub>2</sub>O, OH<sup>−</sup>–H<sub>2</sub>O, and NH<sub>4</sub><sup>+</sup>–NH<sub>3</sub> systems) are efficient conducting media because of their competent H-bonding ability. Recently, numerous reports have dealt with the proton conductivity of MOFs in various structural designs and strategies. In general, the proton conductivity of pristine MOFs is insignificant, whereas the incorporation of a proton conducting medium in a void space of MOFs considerably enhances the proton conductivity with the formation of a complete H-bonding network between the framework and the confined conducting medium. The major conducting medium of MOFs is water with additional acid molecules or functional groups for improved conductivity. In addition, NH<sub>3</sub> as a conducting medium, which is either an alternative or a companion of water, has also attracted interest. The NH<sub>3</sub> uptake in MOFs enhances the proton conduction properties and the coexistence with water facilitates protonation between the conducting media (NH<sub>3</sub>–H<sub>2</sub>O). However, the structural stability of MOFs in the presence of H<sub>2</sub>O and NH<sub>3</sub> with a high proton conductivity is still challenging and indispensable for practical applications in energy carriers with high-performance proton conduction. In particular, the intuitive understanding of the conduction mechanism in NH<sub>3</sub> mediated MOF proton conductors through the structural analysis is still scarce due to the structural stability problem.

To date, the investigation of proton conductivity in MOFs has focused on the discovery of a new proton-conducting pathway through the conducting medium; the scientific progress indicates a conductivity value comparable to that of Nafion. The accumulated experimental knowledge suggests that (1) a hydrophilic channel or (2) acid species contained in the pore and framework and (3) defect and disordered sites are the major factors for high proton conductivity in MOFs. Moreover, the proton donation by acidic species to the conducting medium expedites the development of a degenerate proton-conduction system with increased conductivity. For practical applications of proton-conductive MOFs to FCs, future endeavors for bulk protonic conductivity, stability of MOFs in the redox reaction process, and computational mechanism analysis are required. In conclusion, with consideration of all challenges, the development of potential MOF materials for high proton conductivity should be directed toward the use of inert and oxophilic metal species with a low  $pK_a$  functional group of ligands. Furthermore, the expansion of materials to organic and inorganic



species for composites is expected to achieve practical proton-conductive MOFs.

## Conflicts of interest

There are no conflicts to declare.

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