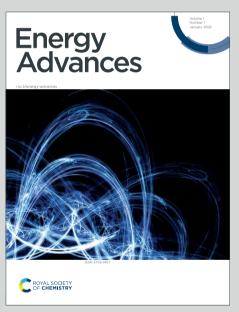




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Impact of Crystal Structure on the Thermoelectric Properties of n-Type ${\rm SrTiO_3}^\dagger$

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We present a detailed first-principles study of the electrical and thermal transport, and the thermoelectric figure of merit zT, of the oxide perovskite $SrTiO_3$ in the orthorhombic Pnma, tetragonal I4/mcm and cubic $Pm\bar{3}m$ phases. Analysis of the lattice thermal conductivity shows that the "particle-like" contribution, κ_p is highest in the $Pm\bar{3}m$ phase due to larger phonon group velocities. We also find that all three phases show significant heat transport through glass-like interband tunnelling. On the other hand, we predict the cubic and orthorhombic phases to show superior n-type conductivity, due to significantly stronger polar-optic phonon scattering and shorter electron lifetimes in the tetragonal phase. Due to its superior electrical properties, we predict that the $Pm\bar{3}m$ phase will attain a 25% larger high-temperature zT than the I4/mcm phase, while we predict the best zT can be obtained for the Pnma phase due to its favourable electrical properties and low κ_{latt} . This work provides new insight into the impact of structure type on the thermoelectric performance of oxide perovskites, and indicates targeting particular structure types, e.g. through chemical doping, could provide a facile route to optimising the zT of $SrTiO_3$ and related systems.

1 Introduction

Climate change due to anthropogenic greenhouse gas (GHG) emissions is the foremost scientific and technological challenge of the $21^{\rm st}$ century. In 2024, global temperatures exceeded $1.5\,^{\circ}{\rm C}$ relative to the pre-industrial 1990 baseline for the first time, with clear - and devastating - consequences from an increased prevalence of extreme weather events. 1 The majority of GHG emissions come from burning fossil fuels for energy, and achieving net zero emissions is key to mitigating climate change. This requires significant changes to how we produce and consume energy. In 2023, the US produced 27.4 Petawatt hours (PWh) of energy, with 82.4 % derived from fossil fuels. Of this, only 34.5% was used in energy services, and the remaining 65.7% was lost as waste heat. $^{2-4}$ This scale of energy waste means that technologies to improve energy efficiency are an important enabler of net zero.

Thermoelectric (TE) power harnesses the Seebeck effect in a TE material to converts heat to electricity and thus recover waste heat as electrical energy. A thermoelectric generator (TEG) com-

but are not limited to: battery-free power sources for wireless sensors, wearables and medical devices; 5-7 heat recovery from automobile powertrains and data centres; 8,9 and as a primary geothermal power source. 10 The conversion efficiency of TE material in typically measured by the dimensionless figure of merit zT: $zT = \frac{S^2 \sigma T}{\kappa_{\rm el} + \kappa_{\rm latt}} \tag{1}$

bines two TE materials with dominant p-type (holes) and n-type

(electrons) carriers, connected electrically in series and thermally

in parallel, to harvest electrical energy from the temperature gra-

dient between a heat source and sink. TEGs are solid state de-

vices with no moving parts, are maintenance free and easily scal-

able, and produce no noise or emissions during operation, mak-

ing them suitable for a wide range of applications. These include,

A large zT requires a high Seebeck (absolute) coefficient |S| and electrical conductivity σ to optimise the power factor, $S^2\sigma$ (PF), and a low electronic and lattice thermal conductivity $\kappa = \kappa_{\rm latt} + \kappa_{\rm el}$. High σ is characteristic of metals, whereas large |S| is typically associated with semiconductors and insulators, and low κ is associated with amorphous materials (glasses). The optimum physical properties for high-performance TEs therefore straddle three traditionally distinct classes of material. The three electrical properties are a product of the electronic structure, and the $\sigma/\kappa_{\rm el}$ and |S| are typically proportional and inversely proportional, respectively, to the charge carrier concentration, n, respectively. ¹¹ The $\kappa_{\rm latt}$ depends on the structure and chemical bonding, and is typically minimised in materials composed of heavy elements,

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 $[\]dagger$ Electronic Supplementary Information (ESI) available: optimised lattice parameters and comparison to experimental measurements; analysis of the "particle-like" contributions to the lattice thermal conductivity at 300 K; anisotropy in the κ_{latt} at 1000 K; "scattering phase space'; functions for the I4/mcm and Pnma phases of SrTiO3; anisotropy in the electrical transport at 1000 K; analysis of the electron mobility as a function of carrier concentration at 1000 K; and anisotropy in the thermoelectric figure of merit at 400, 600 and 1000 K. See DOI: 00.0000/00000000.

Currently, the most widely used thermoelectric (TE) materials are Bi_2Te_3 for near-room temperature applications (zT from \sim 1-1.5 at 350-450 K)^{4,14-16} and PbTe for high-temperature power generation ($zT \approx 2.2$ at 915 K), ¹⁷, due to a combination of a favourable electronic structure and intrinsically low thermal conductivity. 18,19 However, Te is scarce, and the environmental toxicity of Pb raises potential concerns over end-of-life disposal, both of which restrict these materials to niche applications.²⁰. Widespread adoption of TEGs thus requires alternative materials that balance high performance with sustainability and cost efficiency.

Oxides are attractive candidate thermoelectric materials due to their low toxicity, low cost, and also their exceptional chemical stability, the latter of which makes them particularly well suited to high temperature heat recovery in automotive and industrial settings. Oxides often exhibit intrinsically large Seebeck coefficients, but typically also suffer from low electrical conductivity and high lattice thermal conductivity, resulting in overall modest zT values. However, the discovery of high thermoelectric power factors in cobalt-based oxides in the 1990s led to the several families of prospective oxide TEs being identified. p-type oxides include the layered cobaltites Na_xCoO₂ ^{21–24}, $Ca_3Co_4O_9^{25-27}$, and $Bi_2Sr_2Co_2O_v^{28-30}$ n-type oxides include ZnO³¹ and the ABO₃ oxide perovskites, in particular SrTiO₃ ^{32–34} (STO) and CaMnO₃. 35,36

SrTiO₃ in particular has emerged as one of the most promising oxide perovskite TEs due to its chemical versatility, high thermal stability, and tunable electronic properties.³⁷ Compared to the related CaTiO3 and BaTiO3, STO has an intrinsically large absolute Seebeck coefficient (|S|), reasonable σ , superior PF, and impressive thermal stability at elevated temperatures. 37-41 Computational modelling has further determined that these advantageous properties are due to STO supporting a significantly higher σ while maintaining comparable |S| to other titanates. 42,43

STO is typically prepared and tested in thin-film form, with high-temperature zT competitive with other benchmark thin-film systems, e.g. $zT \approx 0.29$ at T = 1000 K in $Sr(Ti_{0.8}Nb_{0.2})O_{2.75}^{44}$ versus $zT \approx 0.3$ in Sb₂Te₃, ⁴⁵, $zT \approx 0.45$ in unoptimised SnSe, ⁴⁶ and $zT \approx 0.4$ in carbon nanotube films. 47 Control of nanostructure can potentially push this much higher, with an unprecedented $zT \approx 1.6$ at T = 298 K recently reported for Sr(Ti_{0.8}Nb_{0.2})O₃ through precisely controlled strain and interfacial polarisation. ⁴⁸ This is significantly higher than the zT = 0.02-0.08 obtained for bulk STO at room temperature, where large κ = 9-12 W m $^{-1}$ K $^{-1}$ limit the thermoelectric performance. ⁴⁹

The wide variation in experimental results is in part due to the high structural and chemical flexibility inherent to perovskites, which can adopt multiple crystal phases, and can accommodate doping at the A and B cation sites as well as significant levels of oxygen deficiency. Optimising STO and other oxide perovskite thermoelectrics therefore requires a good fundamental understanding of the underlying structure-property relationships. In a previous study, we applied a fully ab initio modelling approach to study the thermoelectric performance of the orthorhombic $CaTiO_3$, tetragonal $SrTiO_3$ and rhombohedral $BaTiO_3$. ⁴³ Among our key findings was that the crystal structure had a significant impact on the physical properties and in particular the κ_{latt} . In this work, we build on this with a detailed first-principles study of STO in the orthorhombic, tetragonal and cubic phases. We find that the smaller primitive cell of the $Pm\bar{3}m$ phase results in larger phonon group velocities and high κ_{latt} , whereas the I4/mcm phase shows significantly stronger polar-optic phonon carrier scattering and lower electrical conductivity and power factors. As a result, the hypothetical *Pnma* phase, which combines the lower κ_{latt} of the tetragonal phase and the high PFs of the cubic phase, is predicted to show a \sim 25% larger zT than the cubic phase at hightemperature, and \sim 50% larger zT than the tetragonal phase. This work therefore shows that materials engineering strategies to stabilise particular structural distortions from the cubic aristotype could be a facile route to optimising the performance of STO and other oxide perovskite thermoelectrics.

Computational modelling

2.1 Prediction of thermoelectric properties

2.1.1 Lattice thermal conductivity

The lattice thermal conductivity due to "particle-like" heat transport through phonons, κ_p , was initially calculated by solving the phonon Boltzmann transport equation (BTE) within the singlemode relaxation-time approximation (SM-RTA). 50

In the SM-RTA, the macroscopic κ_p is obtained as an average over contributions $\mathbf{\kappa}_{qj}$ from microscopic phonon modes qj, with wavevector \mathbf{q} and band index j, from: ⁵⁰

$$\mathbf{\kappa}_{p}(T) = \frac{1}{N_{q}V} \sum_{qj} \mathbf{\kappa}_{qj} = \frac{1}{N_{q}V} \sum_{qj} C_{qj}(T) \mathbf{v}_{qj} \otimes \mathbf{v}_{qj} \tau_{qj}(T)$$
(2)

The normalisation factor is the product of the unit-cell volume *V* and the number of wavevectors N_q included in the summation. The phonon mode heat capacities C_{qj} and group velocities v_{qj} are calculated from the harmonic phonon frequencies ω_{qj} as:

$$C_{\mathbf{q}j}(T) = \sum_{\mathbf{q}j} k_{\mathrm{B}} \left(\frac{\hbar \omega_{\mathbf{q}j}}{k_{\mathrm{B}}T}\right)^{2} n_{\mathbf{q}j}(T) (n_{\mathbf{q}j}(T) + 1)$$
(3)

$$\mathbf{v}_{qj} = \frac{\partial \omega_{qj}}{\partial \mathbf{a}} \tag{4}$$

The n_{qj} in Eq. (3) are the Bose-Einstein occupation numbers given by:

$$n_{qj}(T) = \frac{1}{\exp\left[\hbar\omega_{qj}/k_{\rm B}T\right] - 1}$$
 (5)

The phonon lifetimes τ_{qj} are determined from the inverse of the phonon linewidths (scattering rates) Γ_{q_j} :

$$\tau_{\mathbf{q}j}(T) = \frac{1}{\Gamma_{\mathbf{q}j}(T)} \tag{6}$$

The linewidths are calculated using third-order perturbation theory as outlined in Ref. 50, with the Γ_{qj} obtained as a sum of contributions from anharmonic energy- and (crystal) momentumconserving three-phonon scattering processes.

The SM-RTA model in Eq. (2) only considers phonon depopula-

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Furthermore, significant overlap between phonon modes, due either to small interband frequency spacing and/or short τ_{qj} (broad Γ_{qj}) can lead to heat conduction through "wavelike" interband tunnelling characteristic of amorphous materials (glasses). This additional contribution $\kappa_{\rm w}$ can be obtained by solving the Wigner transport equation using the approach outlined in Ref. 51. The $\kappa_{\rm w}$ can then be combined with either the RTA or LBTE models for the $\kappa_{\rm p}$ to compute the total lattice thermal as:

$$\mathbf{\kappa}_{\text{latt}}(T) = \mathbf{\kappa}_{\text{p}}(T) + \mathbf{\kappa}_{\text{w}}(T) \tag{7}$$

The κ_p , κ_w and κ_{latt} are 3×3 tensors, with the transport along the three Cartesian directions $\alpha = x$, y and z given by the diagonal elements $\kappa_{\alpha\alpha}$. As thermoelectric materials typically take the form of consolidated powders or thin films with randomly-oriented crystal grains, we compute a (scalar) average κ_{latt} from:

$$\kappa = \frac{1}{3} \text{Tr}[\kappa] = \frac{1}{3} \left[\kappa_{xx} + \kappa_{yy} + \kappa_{zz} \right]$$
 (8)

where Tr denotes the trace of the κ tensor. We distinguish the scalar and tensor quantities respectively using Roman and bold type.

2.1.2 Electrical conductivity, Seebeck coefficient and electronic thermal conductivity

The electrical conductivity σ , Seebeck coefficient S and electronic thermal conductivity $\kappa_{\rm el}$ were determined by solving the electron BTE within the momentum relaxation-time approximation (MRTA). 53,54 .

We first calculate the spectral conductivity Σ according to:

$$\mathbf{\Sigma}(\varepsilon,T) = \sum_{i} \int \frac{1}{8\pi^{3}} \mathbf{v}_{kj} \otimes \mathbf{v}_{kj} \tau_{kj}(T) \delta\left[\varepsilon - \varepsilon_{kj}\right] d\mathbf{k}$$
 (9)

The summation and integral run over electronic states k_j , with wavevector k and band index j, band energy ε_{kj} , group velocity \mathbf{v}_{kj} and lifetime τ_{kj} . The \mathbf{v}_{kj} are given by the gradient of the electronic band structure as:

$$\mathbf{v}_{kj} = \frac{\partial \varepsilon_{kj}}{\partial k} \tag{10}$$

The τ_{kj} are calculated by combining approximate models of the electron scattering rates from acoustic deformation potential (ADP), polar-optic phonon (POP), ionised impurity (IMP) and piezoelectric (PIE) scattering using Matthiessen's rule: ⁵⁴

$$\tau_{\boldsymbol{k}j}^{-1}(T) = \Gamma_{\boldsymbol{k}j}^{\text{ADP}}(T) + \Gamma_{\boldsymbol{k}j}^{\text{POP}}(T) + \Gamma_{\boldsymbol{k}j}^{\text{IMP}}(T) + \Gamma_{\boldsymbol{k}j}^{\text{PIE}}(T) \tag{11}$$

Expressions for the scattering rates and matrix elements can be found in Ref. 54.

The Σ are then used to obtain the generalised moments of the transport distribution function, \mathcal{L}^n , from:

$$\boldsymbol{L}^{n}(\boldsymbol{\varepsilon}_{\mathrm{F}},T) = e^{2} \int \boldsymbol{\Sigma}(\boldsymbol{\varepsilon},T) \left(\boldsymbol{\varepsilon} - \boldsymbol{\varepsilon}_{\mathrm{F}}\right)^{n} \left[-\frac{\partial f^{0}(\boldsymbol{\varepsilon},\boldsymbol{\varepsilon}_{\mathrm{F}},T)}{\partial \boldsymbol{\varepsilon}} \right] d\boldsymbol{\varepsilon} \tag{12}$$

where $\varepsilon_{\rm F}$ is the Fermi energy and f^0 is the Fermi-Dirac distribution function:

$$f^{0}(\varepsilon, \varepsilon_{F}, T) = \frac{1}{\exp[(\varepsilon - \varepsilon_{F}) / k_{B}T] + 1}$$
 (13)

Finally, the ${\pmb \sigma}, {\pmb S}$ and ${\pmb \kappa}_{\rm el}$ are calculated from the ${\pmb L}^n(T)$ according to: 53,54

$$\boldsymbol{\sigma}(\varepsilon_{\mathrm{F}}, T) = \boldsymbol{L}^{0}(\varepsilon_{\mathrm{F}}, T) \tag{14}$$

$$\mathbf{S}(\varepsilon_{\mathrm{F}},T) = \frac{1}{eT} \frac{\mathbf{L}^{1}(\varepsilon_{\mathrm{F}},T)}{\mathbf{L}^{0}(\varepsilon_{\mathrm{F}},T)} \tag{15}$$

$$\mathbf{\kappa}_{\mathrm{el}}(\varepsilon_{\mathrm{F}}, T) = \frac{1}{e^2 T} \left[\frac{\left(\mathbf{L}^1(\varepsilon_{\mathrm{F}}, T) \right)^2}{\mathbf{L}^0(\varepsilon_{\mathrm{F}}, T)} - \mathbf{L}^2(\varepsilon_{\mathrm{F}}, T) \right]$$
(16)

The L^n , and hence the σ , S and $\kappa_{\rm el}$, depend on the Fermi energy. Under the assumption that dopants do not affect the host band structure, the $\varepsilon_{\rm F}$ can be adjusted to specify an extrinsic carrier concentration ("doping level"), n, to predict the effect of chemical doping. (This is termed the "rigid band approximation" (RBA).)

As for the $\kappa_{\rm latt}$, the σ , S and $\kappa_{\rm el}$ are 3×3 tensors, and scalar averages σ , S and $\kappa_{\rm el}$ can be obtained in an analogous manner to Eq. (8). The power factor $S^2\sigma$ in Eq. (1) is also orientation dependent, and the PF along a given Cartesian direction can be calculated from:

$$\left(S^2\sigma\right)_{\alpha} = S_{\alpha\alpha}^2\sigma_{\alpha\alpha} \tag{17}$$

The scalar average PF is obtained in the same way, but using the averaged S and σ to match how this quantity is evaluated from experimental measurements (i.e. we do not form and take the diagonal average of a "PF tensor").

2.1.3 Thermoelectric figure of merit

The calculated $\mathbf{\kappa}_{\text{latt}}$ and $\mathbf{\sigma}$, \mathbf{S} and $\mathbf{\kappa}_{\text{el}}$ can be combined to determine the thermoelectric figure of merit zT using Eq. (1) from first principles. The $\mathbf{\kappa}_{\text{latt}}$ is a function of temperature, while the three electrical properties are a function of both T and Fermi energy ε_{F} (extrinsic carrier concentration n; c.f. Eq. (7) and Eq. (14)-(16)). We therefore determine the zT as a (two-dimensional) function of both T and n.

The zT is orientation dependent and the values along the three Cartesian directions can be calculated as:

$$(zT)_{\alpha} = \frac{S_{\alpha\alpha}^2 \sigma_{\alpha\alpha} T}{\kappa_{\text{el},\alpha\alpha} + \kappa_{\text{latt},\alpha\alpha}}$$
(18)

As for the power factor, the scalar average ZT is calculated using the scalar averages of the four constituent properties, as opposed to the diagonal average of a "ZT tensor").

As noted in Section 2.1.1, heat transport through three different mechanisms can be taken into account when computing the κ_{latt} (particle-like transport through individual and collective phonon modes, and interband tunnelling). We discuss the contributions of these different mechanisms in detail in Section 3.1 below.

2.2 Density-functional theory calculations

Calculations were performed using pseudopotential plane wave density functional theory (DFT) as implemented in the Vienna Ab

Initial structures of SrTiO3 in the tetragonal I4/mcm and cubic $Pm\bar{3}m$ phases were taken from the Materials Project (MP) database⁵⁶ (mp-5229, mp-4651), and an orthorhombic Pnma structure was built by changing the A-site cation in CaTiO₃ (mp-1185232). All three structures were then fully optimised to tight tolerances of 10^{-8} eV on the total energy and 10^{-3} eV Å⁻¹ on the

Electron exchange and correlation were modelled using the PBEsol generalised gradient approximation (GGA) functional.⁵⁷ The ion cores were modelled using projector-augmented (PAW) pseudopotentials ^{58,59} with the following valence configurations: Ti - $3d^2 4s^2$; O - $2s^2 2p^4$; Sr - $4s^2 4p^6 5s^2$. The valence wavefunctions were described using a plane-wave basis with an 800 eV kinetic-energy cutoff, and the electronic Brillouin zones were sampled using Γ -centred Monkhorst-Pack **k**-point meshes ⁶⁰ with $6 \times 6 \times 6$, $5 \times 5 \times 3$, $3 \times 2 \times 4$ subdivisions for the $Pm\bar{3}m$, I4/mcm and Pnma phases respectively. These parameters were chosen based on explicit testing to converge the absolute total energies to < 1meV atom $^{-1}$ and the external pressure to < 1 kbar (0.1 GPa).

2.2.1 Lattice dynamics and thermal conductivity

Lattice-dynamics and thermal-conductivity calculations were performed using the supercell finite-differences approach implemented in the Phonopy and Phono3py codes. 50,61 The 2nd-order (harmonic) force constants were computed in $4 \times 4 \times 4$ expansions of the $Pm\bar{3}m$ unit cell and I4/mcm primitive cell (320/640 atoms), and a $4 \times 2 \times 4$ expansion of the *Pnma* unit cell (640 atoms). Atomprojected phonon density of states (PDoS) curves were computed by interpolating the phonon frequencies onto regular Γ -centred **q**-point grids with $12 \times 12 \times 12$ subdivisions using the linear tetrahedron method for Brillouin-zone integration. Phonon dispersions were obtained by evaluating the frequencies at strings of q points passing through the high-symmetry points in the respective Brillouin zones. Non-analytical corrections to the dynamical matrices at $q \to \Gamma$ were included using the approach in Ref. 62 using Born effective-charge tensors \mathbf{Z}^* and high-frequency dielectric constants $\boldsymbol{\varepsilon}_{\infty}$ computed using density-functional perturbation theory (DFPT).63

The 3rd-order (anharmonic) force constants were computed in a $3 \times 3 \times 3$ expansion of the $Pm\bar{3}m$ unit cell (135 atoms), a $2 \times 2 \times 2$ expansion of the I4/mcm primitive cell (80 atoms), and a $2 \times 1 \times 2$ expansion of the *Pnma* unit cell (80 atoms). The "particle-like" lattice thermal conductivities for band transport were calculated using the SM-RTA model by combining the second- and thirdorder force constants to evaluate the C_{qj} , group velocities \mathbf{v}_{qj} and lifetimes τ_{q_i} on uniform Γ -centred $22 \times 22 \times 22$, $8 \times 8 \times 8$ and $12 \times 12 \times 12$ **q**-point sampling meshes for the $Pm\bar{3}m$, I4/mcm and Pnma phases respectively. These meshes were chosen based on explicit testing to converge the scalar average of the ${m \kappa}_p$ tensors (Eq. (2)/(8)) to within 5% of the values obtained with larger sampling meshes. We also solved the full linearised phonon BTE to obtain the κ_p including contributions from collective phonons, and the Wigner transport equation to determine the $\kappa_{\rm w}$ contribution from interband tunnelling. 51

2.2.2 Electronic transport

Electronic transport calculations were performed using the AMSET code. 54 Accurate band gaps $E_{\rm g}$ were obtained from non-selfconsistent calculations with the HSE06 hybrid functional. 64,65 These calculations were also used to obtain electronic PDoS curves using a Gaussian smearing with a width $\sigma = 0.01$ eV. Uniform band-structure calculations were then performed with PBEsol and denser $12 \times 12 \times 12$, $10 \times 10 \times 6$, and $6 \times 4 \times 8$ **k**-point meshes for the $Pm\bar{3}m$, I4/mcm and Pnma phases, respectively, and the bandgaps increased to the HSE06 values using scissors operators. These meshes were further interpolated to $\sim 20\times$, $\sim 30\times$ and $\sim 10 \times$ higher densities when calculating the electrical transport properties. The charge densities from the calculations were also used to calculate the band energies at strings of k-points along the high-symmetry paths in the Brillouin zones to obtain electronic band structures, with the band gaps again corrected using scissors operators. The combined band structure and PDoS curves were plotted using sumo. 66

AMSET estimates the electronic relaxation times by summing scattering rates from four different processes, viz. acoustic deformation potential (ADP), polar optic phonon (POP), piezoelectric (PIE), and ionised impurity (IMP) scattering, requiring a range of material properties to be calculated. (We note that PIE scattering is negligible in the three systems examined in this work, as all three have centrosymmetric space groups and the piezoelectric moduli vanish by symmetry).

Deformation potentials were computed by performing a series of single-point energy calculations on deformed structures, generated using AMSET, with PBEsol. The high-frequency, ionic and total dielectric constants $\boldsymbol{\varepsilon}_{\infty}$, $\boldsymbol{\varepsilon}_{\text{ionic}}$ and $\boldsymbol{\varepsilon}_{\text{s}} = \boldsymbol{\varepsilon}_{\infty} + \boldsymbol{\varepsilon}_{\text{ionic}}$, together with the Born effective charges Z* and piezoelectric moduli, were determined using DFPT. 63 Explicit tests found that $2\times$ ($Pm\bar{3}m/Pnma$ phases) and $3\times$ denser **k**-point sampling (I4/mcmphase) compared to the "base" meshes used for geometry optimisation were required to converge the $\boldsymbol{\varepsilon}_{\infty}$. The \boldsymbol{Z}^* were used to determine the infrared (IR) activities of the phonon modes at $\mathbf{q} = \Gamma$, 67,68 evaluated with Phonopy, and to calculate the polar optic phonon (POP) frequency ω_{po} . Finally, the elastic constant matrix elements C_{ij} were computed using PBEsol and the finite-differences finite-differences routines in VASP (denser kpoint sampling was not required for these calculations).

Results and Discussion

3.1 Structure, phonon spectra and lattice thermal conduc-

The optimised structures of the three SrTiO₃ phases are shown in Fig. 1. For all three systems the lattice parameters are in excellent agreement with experimental measurements, with maximum differences of 0.55% in the lattice parameters and 0.42% in the unit cell volumes of the $Pm\bar{3}m$ and I4/mcm phases (Table S1, ESI^{\dagger}). We note that the hypothetical *Pnma* phase of STO has not been observed experimentally, but is adopted by heavily-doped derivatives, and our predicted lattice parameters and cell volumes are within 0.56 and 1.58%, respectively, of the measurements on SrTi_{0.9}Fe_{0.1}Ta_{0.1}O₃ reported in Ref. 69.

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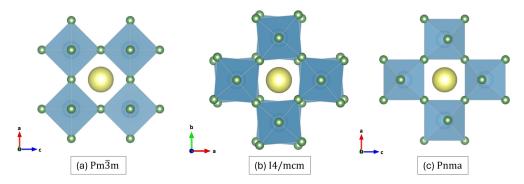


Fig. 1 Optimised structures of $SrTiO_3$ in the cubic $Pm\overline{3}m$ (a), tetragonal I4/mcm (b) and orthorhombic Pnma phase (c). The I4/mcm and Pnma structures are oriented so show the equivalence to the cubic structure. The Sr, Ti and O atoms are shown in yellow, light blue and green respectively. These images were prepared using the VESTA software. The Sr, Ti and O atoms are shown in yellow, light blue and green respectively.

Both the lower-symmetry tetragonal I4/mcm and orthorhombic Pnma phases can be generated from the "parent" $Pm\bar{3}m$ structure by rotations of the ${\rm TiO}_6$ octahedra. The I4/mcm phase is obtained by an anti-phase tilt of successive "layers" of ${\rm TiO}_6$ octahedra around the z direction, such that the a, b and c lattice vectors of the I4/mcm structure correspond to the (110), ($\bar{1}10$) and (002) directions in the cubic phase. The Pnma phase is obtained by a more complex combination of an in-phase tilt around x and antiphase tilts of the same angle around y and z, and the a, b and c lattice vectors correspond to the (011), (020) and (01 $\bar{1}$) directions in the $Pm\bar{3}m$ parent.

The calculated phonon spectra of the three $SrTiO_3$ phases are shown in Fig. 2. The cubic $Pm\bar{3}m$ structure has $n_a=5$ atoms in the primitive cell, resulting in $3n_a=15$ branches at each phonon wavevector ${\bf q}$. In contrast, the I4/mcm and Pnma structures have $n_a=10$ and 20, respectively, and thus considerably more complex phonon spectra with 30 and 60 bands per ${\bf q}$. The increase in complexity due to the larger primitive unit cells is further compounded by the lower band degeneracy from the reduced symmetry.

In all three systems, the A-site cation makes the largest contribution to the low-frequency modes, with sharp features in the DoS consistent with some degree of "rattling" behaviour. The mid-frequency optic modes are predominantly due to the motion of the Ti and O atoms, and can be attributed to deformations of the ${\rm TiO_6}$ octahedra, while all three systems show prominent high-frequency features associated with motion of the O atoms. The calculated phonon spectra of the $Pm\bar{3}m$ and I4/mcm phases agree well previous calculations. 72,73

With the exception of some small interpolation artefacts around $\mathbf{q} = \Gamma$ in the Pnma dispersion, the dispersions of the orthorhombic and tetragonal phases show no imaginary harmonic modes, indicating that both structures are dynamically stable. On the other hand, the dispersion of the $Pm\bar{3}m$ phase shows prominent dynamical instabilities at $\mathbf{q} = R$ and M, in agreement with previous calculations. ^{74,75} These off- Γ instabilities are related to the octahedral tilts that generate the lower-symmetry structures. ⁷⁶ We were not able to find reference phonon spectra for the Pnma phase, but the good agreement for the $Pm\bar{3}m$ and I4/mcm phases

compared to previous studies gives us confidence in our calculations on the orthorhombic phase.

The scalar-average "particle-like" conductivity, κ_p , of the three SrTiO₃ obtained using the single-mode relaxation-time approximation (SM-RTA) are compared in Fig. 3(a), and values at T = 1000 K are compared in Table 1. At 1000 K, we predict $\kappa_{\rm p}$ = 1.2-1.9 W m⁻¹ K⁻¹, with an ordering of $Pm\bar{3}m > I4/mcm > Pnma$. Compared to the intermediate I4/mcm phase, which we examined in our previous study, ⁴³ the lower-symmetry orthorhombic phase has a 13% lower $\kappa_p,$ but the κ_p is still 26% larger than that of the isostructural $CaTiO_3$ (0.96 W m⁻¹ K⁻¹). On the other hand, the high-symmetry $Pm\bar{3}m$ phase has a 34% higher $\kappa_{\rm D}$ than the 14/mcm phase. Taken together, this suggests the effects of crystal symmetry and A-site cation mass on the κ_p are both strong and of similar magnitude. On the other hand, the three phases of STO have very similar density $\rho = 5.1-5.12 \text{ g cm}^{-3}$ (Table S1[†]), which in our view cannot explain the significant variation in the $\kappa_{\rm p}$. This provides further support for the reduction in crystal symmetry being the key factor in the reduction in κ_p from the cubic to the orthorhombic phase.

To explore the origin of the differences in the RTA κ_p , we employ the analysis from our previous studies 13 and define a weighted-average phonon lifetime τ^{ph} such that the κ_p can be written:

$$\kappa_{p}(T) = \tau^{ph}(T) \times \frac{1}{N_{q}V} \sum_{qj} \frac{\kappa_{qj}(T)}{\tau_{qj}(T)}$$

$$= \tau^{ph}(T) \times \frac{1}{N_{q}V} \sum_{qj} C_{qj}(T) \frac{1}{3} \text{Tr} \left[\mathbf{v}_{qj} \otimes \mathbf{v}_{qj} \right]$$
(19)

where we have taken the scalar average of the group velocity outer product (c.f. Eq. (8)). The summation, $\kappa_p/\tau^{\rm ph}$, is temperature dependent due to the heat capacities C_{qj} , and the high-temperature saturation value provides a metric for comparing differences in group velocities between materials. ¹³ The $\tau^{\rm ph}$ can likewise be used to compare phonon lifetimes.

The κ_p/τ^{ph} and τ^{ph} as a function of temperature for the three phases of STO are compared in Figs 3(b) and 3(c), respectively, and values at T=1000 K are listed in Table 1. The calculated

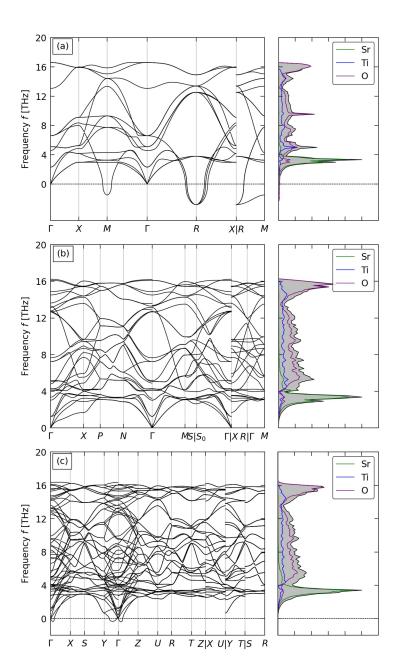
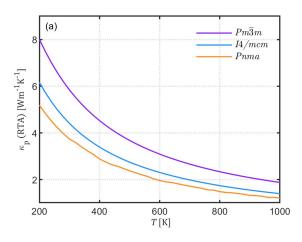
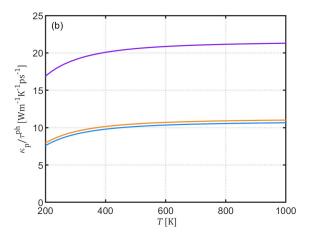


Fig. 2 Calculated phonon dispersion and density of states (DoS) of $Pm\bar{3}m$ (a), I4/mcm (b) and Pnma SrTiO₃ (c). The DoS curves show the total DoS in black/grey with the projections onto the Sr, Ti and O atoms in green, blue and purple respectively.

Table 1 Analysis of the "particle-like" (band transport) contributions κ_p to the scalar-average lattice thermal conductivity $\kappa_{\rm latt}$ of the three phases of SrTiO $_3$ examined in this work at T=1000 K. For each κ_p we show the harmonic function $\kappa_p/\tau^{\rm ph}$ and weighted-average lifetime $\tau^{\rm ph}$, defined in Eq. (19), together with the the integrals of the "scattering phase space" functions \bar{N}_2 from 0 to the maximum frequencies $f_{\rm max}$ in the phonon spectra, the average three-phonon interaction strengths \tilde{P}_1 , and number of scattering channels \tilde{N}_2 , defined in Eqs (26), (21) and (27). The latter three quantities are all scaled to allow for comparison between the three phases.

	$\kappa_{ m p}$	$\kappa_{ m p}/ au^{ m ph}$	$ au^{ m ph}$	$\frac{1}{(2\pi)^2} \int_{-\infty}^{f_{\text{max}}} \bar{N}_2(f) df$	$\tilde{P} \times (3n_a)^2$	$\tilde{N}_2/(3n_a)^2$
	$[W m^{-1} K^{-1}]$	$[W m^{-1} K^{-1} ps^{-1}]$	[ps]	$\overline{(3n_a)^2} \int_0^{\infty} N_2(f) df$	$[eV^2]$	$[THz^{-1}]$
$Pm\bar{3}m$	1.88	21.29	0.09	2.75×10^{-2}	5.36×10^{-7}	7.95×10^{-2}
I4/mcm	1.4	10.65	0.13	0.56×10^{-2}	5.08×10^{-7}	5.76×10^{-2}
Pnma	1.21	11.01	0.11	0.16×10^{-2}	6.09×10^{-7}	5.72×10^{-2}





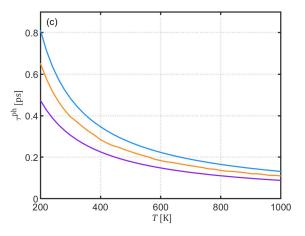


Fig. 3 "Particle-like" (band transport) contributions κ_p to the averaged lattice thermal conductivity $\kappa_{\rm latt}$ of the $Pm\bar{3}m$, I4/mcm and Pnma phases of SrTiO $_3$ (Eq. (2)). ⁵⁰ Plot (a) shows the scalar-average κ_p , calculated using Eq. (8), while plots (b) and (c) show the decomposition into the harmonic summation κ_p/τ^{ph} and weighted-average lifetime $\tau^{\rm ph}$ defined in Eq. (19). ¹³

 $\kappa_{\rm p}/\tau^{\rm ph}$ of the *Pnma* and *I4/mcm* phases are similar, differing by only 3.8% at 1000 K, whereas the group velocities of the $Pm\bar{3}m$

phase are around a factor of two larger. Given that the group velocities \mathbf{v}_{qj} are the gradient of the phonon dispersion, this difference can be attributed to the impact of the smaller primitive cell of the cubic phase on the phonon dispersion (c.f. Eq. (4), Fig. 2). On the other hand, the $\tau^{\rm ph}$ fall in the order $Pm\bar{3}m < Pnma < I4/mcm$, i.e. the cubic phase has the shortest phonon lifetimes. The $\tau^{\rm ph}$ of the Pnma phase is 17% shorter than the I4/mcm phase at 1000 K, resulting in a lower overall $\kappa_{\rm p}$, whereas the much larger $\kappa_{\rm p}/\tau^{\rm ph}$ of the $Pm\bar{3}m$ phase offsets the short $\tau^{\rm ph}$ and results in the largest predicted $\kappa_{\rm latt}$ among all three phases.

In the SM-RTA, the phonon lifetimes τ_{qj} are calculated as the inverse of the linewidths Γ_{qj} , which are obtained perturbatively from the imaginary part of the phonon self-energies. ⁵⁰ The Γ_{qj} can be written approximately as:

$$\tilde{\Gamma}_{qj}(T) = 2 \times \frac{18\pi}{\hbar^2} P_{qj} N_2(q, \omega_{qj}, T)$$
 (20)

The P_{qj} are the averaged three-phonon interaction strengths $\Phi_{qj,q'j',q''j''}$ given by:

$$P_{qj} = \frac{1}{(3n_{\rm a})^2} \sum_{q'j',q''j''} \left| \Phi_{qj,q'j',q''j''} \right|^2$$
 (21)

The function $N_2(\boldsymbol{q}, \omega, T)$ defines the "scattering phase space", i.e. the number of energy- and momentum-conserving scattering pathways available to a phonon with wavevector \boldsymbol{q} and frequency ω at temperature T:

$$N_2(\mathbf{q}, \omega, T) = N_2^{(1)}(\mathbf{q}, \omega, T) + N_2^{(2)}(\mathbf{q}, \omega, T)$$
 (22)

The functions $N_2^{(1)}$ and $N_2^{(2)}$ define separately the phase spaces for collision/coalescence (Type 1, two phonons \rightarrow one phonon) and decay/emission events (Type 2, 1 \rightarrow 2) and are given by:

$$N_{2}^{(1)}(\boldsymbol{q}, \boldsymbol{\omega}, T) = \frac{1}{N_{\boldsymbol{q}}} \sum_{\boldsymbol{q}', \boldsymbol{j}'', \boldsymbol{q}'', j''} \Delta(-\boldsymbol{q} + \boldsymbol{q}' + \boldsymbol{q}'')$$

$$\times \left[n_{\boldsymbol{q}', j'}(T) - n_{\boldsymbol{q}'', j''}(T) \right]$$

$$\times \left[\delta \left(\boldsymbol{\omega} + \boldsymbol{\omega}_{\boldsymbol{q}', j'} - \boldsymbol{\omega}_{\boldsymbol{q}'', j''} \right) - \delta \left(\boldsymbol{\omega} - \boldsymbol{\omega}_{\boldsymbol{q}', j'} + \boldsymbol{\omega}_{\boldsymbol{q}'', j''} \right) \right]$$
(23)

$$\begin{split} N_2^{(2)}(\boldsymbol{q},\omega) = & \frac{1}{N_{\boldsymbol{q}}} \sum_{\lambda'\lambda''} \Delta(-\boldsymbol{q} + \boldsymbol{q}' + \boldsymbol{q}'') \\ & \times \left[n_{\boldsymbol{q}'j'}(T) + n_{\boldsymbol{q}''j''}(T) + 1 \right] \times \delta\left(\omega - \omega_{\boldsymbol{q}'j'} - \omega_{\boldsymbol{q}''j''}\right) \end{split} \tag{24}$$

where the functions Δ and δ enforce the conservation of (crystal) momentum and energy, respectively. The three-phonon interaction strengths are determined from the harmonic frequencies and displacement vectors (eigenvectors) and the third-order force constants $\Phi^{(3)}$, while the N_2 depend on the harmonic frequencies only. With reference to Eq. (20), the average phonon lifetimes can therefore be interpreted in terms of a parameter \tilde{P} , describing the average strength of the three-phonon interactions and the level of phonon anharmonicity, and the size of the scattering phase space. ¹³

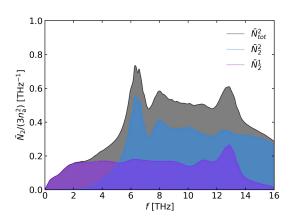


Fig. 4 Average "scattering phase space" function $\bar{N}_2(f)$ defined in Eq. (25) for the $Pm\bar{3}m$ phase of $SrTiO_3$ at T=1000 K. The separate phase spaces for collision and decay processes $(\bar{N}_2^{(1)}/\bar{N}_2^{(2)})$ are shown in blue and purple, respectively, and the total phase space is shown in grey.

To simplify the comparison between systems, it is useful to average the N_2 over \boldsymbol{q} to obtain functions of frequency only, i.e.:

$$\bar{N}_{2}(\boldsymbol{\omega},T) = \bar{N}_{2}^{(1)}(\boldsymbol{\omega},T) + \bar{N}_{2}^{(2)}(\boldsymbol{\omega},T)
= \frac{1}{N_{q}} \sum_{\boldsymbol{q}} N_{2}^{(1)}(\boldsymbol{q},\boldsymbol{\omega},T) + \frac{1}{N_{q}} \sum_{\boldsymbol{q}} N_{2}^{(2)}(\boldsymbol{q},\boldsymbol{\omega},T)$$
(25)

Also, whereas the \tilde{P} is a single parameter, and can in principle be compared quantitatively between systems, the \bar{N}_2 can only be compared qualitatively. We therefore compute and use one of two metrics to compare the scattering phase spaces. 13 First, we compute the integral of the \bar{N}_2 , which provides a measure of the size of the scattering phase space:

$$\int_0^{\omega_{\text{max}}} \bar{N}_2(\omega, T) \, d\omega \tag{26}$$

where ω_{max} is the highest frequency in the phonon spectrum. Secondly, we compute weighted-average \tilde{N}_2 calculated from the $\tau^{\rm ph}$ and \tilde{P} using Eq. (20):

$$\tilde{N}_{2} = \frac{\hbar^{2}}{36\pi} \frac{1}{\tau^{\text{ph}}} \frac{1}{\tilde{P}} \tag{27}$$

Finally, we also note that for comparison between systems with different n_a the \tilde{P} and N_2/\bar{N}_2 need to be multiplied and divided, respectively, by $(3n_a)^2$.

The calculated \bar{N}_2 for the $Pm\bar{3}m$ phase of STO at T=1000K is shown in Fig. 4, and equivalent plots for the I4/mcm and *Pnma* phases are given in Figs S1/S2.[†] We find that the scattering phase space of the low-frequency phonon modes is dominated by collision processes, while decay pathways become available from \sim 3 THz, are competitive with decay up to 13 THz, and are the dominant scattering mechanism for the high-frequency modes up to the $f_{\rm max} \approx 16$ THz (c.f. Fig. 2).

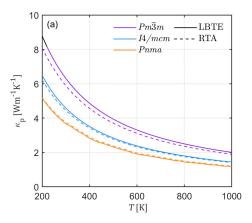
The calculated \tilde{P} and the phase space integral and \tilde{N}_2 defined in Eqs (26)/(27) for all three phases are listed in Table 1. The scaled \tilde{P} and \tilde{N}_2 indicate that the three-phonon scattering strengths and phase spaces are similar across all three phases are very similar, with \tilde{P} between $5.08 - 6.09 \times 10^{-7}$ eV² and \tilde{N}_2 between $5.72 - 7.95 \times 10^{-2}$ THz⁻¹. The \tilde{N}_2 fall in the order of *Pnma* $\approx I4/mcm < Pm\bar{3}m$, i.e. the cubic phase has a notably larger scattering phase space. On the other hand, the \tilde{P} fall in the order $I4/mcm < Pm\bar{3}m < Pnma$. The short τ^{ph} of the cubic phase compared to the other two phases is therefore a product of moderate three-phonon interaction strengths and a large scattering phase space, whereas the longer τ^{ph} of the tetragonal phase is due to comparatively weak three-phonon interactions and a small phase

The trend in the $\kappa_{\rm p}/\tau^{\rm ph}$ with crystal symmetry qualitatively mirrors our previous calculations on the Group IV-VI chalcogenides, including the "flagship" thermoelectric materials SnS and SnSe, where low group velocities were found to be characteristic of low-symmetry structures with large primitive cells. ¹³ In absolute terms, however, the κ_p/τ^{ph} of all three STO phases are $10-40\times$ larger than chalcogenide phases with comparable symmetry. On the other hand, the τ^{ph} at T=300 K range from 0.3-0.5 ps (Table S2[†]), placing them on the same order of magnitude as the shortest averaged lifetimes calculated in Ref. 13. The \tilde{N}_2 at room temperature are on the same order as the largest values obtained for the chalcogenides, while the averaged three-phonon interaction strengths fall within the the mid-to-upper range of \tilde{P} . Compared to these other flagship thermoelectric materials, the oxides thus have relatively large three-phonon scattering phase spaces, moderate-to-strong phonon anharmonicity, and, consequently, short $\tau^{\rm ph}$.

The trends in the group velocity and lifetimes compared to other classes of materials can be partially interpreted in terms of the chemical bonding. The harmonic frequencies and group velocities are both derived from the 2nd-order force constants (FCs), which describe the changes in atomic forces in response to small displacements of the atoms. Strong chemical bonding favours large FCs, high phonon frequencies, and, consequently, high group velocities (c.f. Eq. (4)). The three-phonon interaction strengths additionally depend on the 3rd-order FCs, which describe the changes in forces in response to pairwise atomic displacements. While we are not aware of any systematic studies to this effect, it is not unreasonable to expect the 2nd- and 3rd-order FCs to be at least loosely correlated, such that stronger bonding results in larger 2nd-order and 3rd-order FCs. From this point of view, the stronger bonding in the oxides results in larger group velocities, but also stronger three-phonon interactions and shorter phonon lifetimes. In these systems, the former dominates the $\kappa_{\rm p}$.

The generality of our finding that the κ_{latt} depends sensitively on crystal structure is also supported by a recent theoretical study of Zintl compounds, 77 which found low group velocities and, in some cases, short lifetimes to be favoured by inhomogeneous chemical bonding, as we find for the Pnma phase in the present study.

We also compared the κ_p obtained from the SM-RTA in Eq. (2) with that obtained by full solution of the linearised phonon Boltzmann transport equation (LBTE) (Table 2). 50,52 The conceptual difference between the two models is that the SM-RTA only considers depopulation events, whereas the LBTE approach also accounts for repopulation.



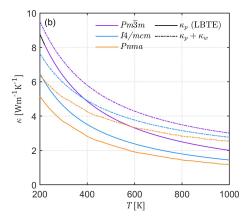


Fig. 5 Contribution to the scalar-average lattice thermal conductivity $\kappa_{\rm latt}$ of the $Pm\bar{3}m$, I4/mcm and Pnma phases of SrTiO $_3$ from "particle-like" (band) and "wave-like" (interband tunnelling) transport, $\kappa_{\rm p}/\kappa_{\rm c}$, as a function of temperature. Plot (a) compares the $\kappa_{\rm p}$ obtained with the single-mode relaxation-time approximation (Eq. (2)) and by full solution of the linearised Boltzmann transport equation (LBTE). ^{50,52} Plot (b) compares the $\kappa_{\rm p}$ obtained by solving the LBTE and the total $\kappa_{\rm latt} = \kappa_{\rm p} + \kappa_{\rm w}$ obtained by solving the Wigner transport equation to include interband tunnelling. ⁵¹

Table 2 Contributions to the scalar-average lattice thermal conductivity, $\kappa_{latt}=\kappa_p+\kappa_w$ of the three phases of SrTiO_3 examined in this work from "particle-like" conductivity κ_p and "wave-like" (interband tunnelling) conductivity κ_w at T=1000 K. Values of the κ_p obtained with the single-mode relaxation-time approximation (SM-RTA) and full solution of the linearised Boltzmann transport equation (LBTE) are given, together with the equivalent κ_{latt} .

	[W m ⁻¹ K ⁻¹]						
	κ _p (SM-RTA)	κ _p (LBTE)	$\kappa_{ m w}$	κ _{latt} (SM-RTA)	κ _{latt} (LBTE)		
$Pm\bar{3}m$	1.88	2.01	1.0	2.88	3.01		
I4/mcm Pnma	1.4 1.21	1.44 1.18	1.32 1.36	2.72 2.57	2.77 2.54		

In our previous work on the lanthanide cobalates LnCoO₃ ⁷⁸ we found that "wave-like" tunnelling made a significant contribution to the overall κ_{latt} . We find the same for all three phases of SrTiO₃, with the $\kappa_{\rm w}$ accounting for 33-35% of the $\kappa_{\rm latt}$ of the $Pm\bar{3}m$ phase at 1000 K, depending on whether the $\kappa_{\rm p}$ is calculated using the SM-RTA or LBTE models, and a larger 47-49 and 52-54% of the κ_{latt} of the lower-symmetry I4/mcm and Pnma phases (Table 2). The larger κ_w of the tetragonal and orthorhombic phases can be explained by the more complex phonon dispersions leading to a smaller interband spacing, which more than compensates for the narrower linewidths (longer lifetimes) compared to the cubic phase (c.f. Fig. 2 and Table 1). While we only considered the Pnma phases of the $LnCoO_3$, we predicted a similar $\sim 50\%$ contribution from the $\kappa_{\rm w}$ to the $\kappa_{\rm latt}$. ⁷⁸ We have also found that the κ_w is much more significant in the more structurally-complex " π " phases of the chalcogenides SnS and SnSe than the simpler orthorhombic phases. 79 When taken together with the present results, this suggests that there may be a universal trade-off between high κ_p in higher-symmetry phases and high κ_w in in lowersymmetry phases.

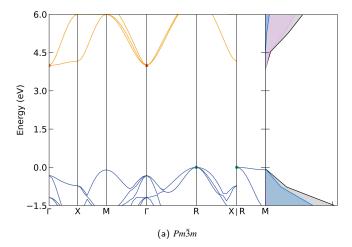
Taken together, our analysis shows that the κ_{latt} of $SrTiO_3$ is a balance of several competing factors. The "particle-like" conductivity, κ_p , is largest in the high-symmetry $Pm\bar{3}m$ phase, where the

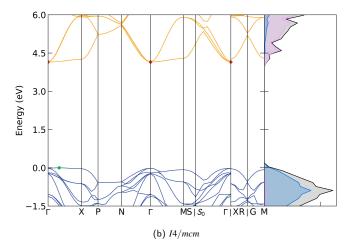
large phonon group velocities compensate for shorter lifetimes. On the other hand, the interband tunnelling contribution, $\kappa_{\rm W}$, is larger in the lower-symmetry I4/mcm and Pnma phases, where the smaller interband frequency spacing outweighs the narrower linewidths. Overall, however, we predict the $Pm\bar{3}m$ phase to have a 5-10% larger $\kappa_{\rm latt}$ than the I4/mcm phase, and a 10-20% larger $\kappa_{\rm latt}$ than the Pnma phase, at 1000 K, and we therefore conclude that the phonon group velocities are the biggest factor in determining the higher thermal conductivity of the cubic phase. The difference between the tetragonal and orthorhombic phases is more subtle, but the shorter phonon lifetimes of the Pnma phase outweigh the slightly larger group velocities and $\kappa_{\rm w}$ to yield a 5-10% lower $\kappa_{\rm latt}$.

More generally, the short phonon lifetimes in comparison to the chalcogenides suggests that the most fruitful approach to optimising the κ_{latt} of the oxide perovskites is likely to be targeting lower group velocities, e.g. through weaker chemical bonding. Our recent set of similar calculations on the LnCoO $_3$ identified lower group velocities, attributed to the weaker ionic bonding, as a key factor in the lower κ_{latt} , which supports this hypothesis. ⁷⁸

Finally, we also consider the directional anisotropy in the $\kappa_{\rm latt}$. Due to the symmetry of the $Pm\bar{3}m$, I4/mcm and Pnma structures, the diagonal elements of the κ_{latt} are $\kappa_{xx} = \kappa_{yy} = \kappa_{zz} = \kappa_{latt}$, $\kappa_{xx} = \kappa_{latt}$ $\kappa_{yy} \neq \kappa_{zz}$ and $\kappa_{xx} \neq \kappa_{yy} \neq \kappa_{zz}$. The independent components of the $\kappa_{\rm p}$, obtained using the SM-RTA and LBTE, the $\kappa_{\rm w}$ and the $\kappa_{\rm latt}$ at T=1000 K are compared in Tables S3 and S4.[†] The $\kappa_{\rm p}$ of the I4/mcm phase show modest anisotropy, with the thermal conductivity along the a = b and c directions differing from the scalar average κ_p in Table 2 by 7.6 and 15% respectively, and with similar % differences obtained for both the SM-RTA and LBTE $\kappa_{\rm p}$. The anisotropy in the Pnma phase is much smaller, at 2.1-4.4% of the κ_p . The anisotropy in the κ_w is also relatively small, with maximum differences of 2.8 and 4.1% in the orthorhombic and tetragonal phases. Notably, differences in the κ_p and κ_w combine to minimise the anisotropy in the κ_{latt} , with differences of 2.9-6% and 1.4-4.1%, respectively, for the I4/mcm and Pnma phases. Our calculations therefore predict minimal anisotropy in the κ_{latt} in

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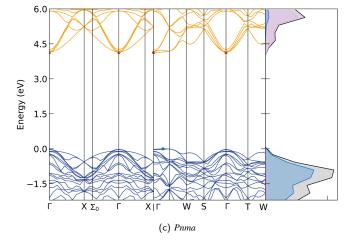


Fig. 6 Electronic band structure and density of states (DoS) of the (a) $Pm\bar{3}m$, (b) I4/mcm and (c) Pnma phases of $SrTiO_3$. On each band structure the valence and conduction bands are coloured blue and yellow, respectively, and the valence- and conduction-band minima are marked by green and red circles. On each DoS plot, the total DoS is shown in grey and the projections onto the O 2p and Ti 3d states are shown in blue and pink, respectively.

both low-symmetry phases of STO.

As noted in the previous section, the c = z and b = y directions in the I4/mcm and Pnma are equivalent to the a = b = c direc-

Table 3 Calculated electronic band gaps E_g of the three phases of SrTiO₃ examined in this work compared to other experimental and theoretical studies where available.

	$E_{\rm g,dir}$ [eV]	$E_{\rm g,indir}$ [eV]
Pm3m	4.23	4.0
I4/mcm	4.15	4.14
Pnma	4.13	-
Expt 80,81	3.75	3-3.25

tions in the $Pm\bar{3}m$ phase. For the tetragonal phase, we predict the largest κ_p along the c direction, and the κ_{latt} along this direction obtained using the SM-RTA and LBTE κ_p are equal to and 2.7% smaller than, respectively, the κ_{latt} along the three axes in the cubic phase. For the orthorhombic phase, on the other hand, we predict the lowest $\kappa_{\rm p}$ and $\kappa_{\rm w}$ along the b direction, with the result that the κ_{latt} is 14-19% smaller than in the cubic phase. This suggests that the phonon transport along the c direction in the 14/mcm phase remains similar to the parent cubic phase, but is significantly disrupted in the *Pnma* phase, which again highlights the large impact of the lower crystal symmetry on the κ_{latt} .

3.2 Electronic Structure and transport properties

The electronic band structure and density of states (DoS) of the three SrTiO₃ phases are compared in Fig. 6. In all three systems, the valence- and conduction-band edges are formed respectively from O 2p and Ti 3d states. The impact of crystal symmetry on the electronic band structure is similar to that on the phonon dispersion, with the increase in the complexity of the unit cells from the $Pm\bar{3}m$ to the Pnma phase resulting in more complex band structures. In the $Pm\bar{3}m$ phase, the valence-band maximum (VBM) is located at k = R, whereas in the I4/mcm and Pnma phases the VBM is located along the $\Gamma \to X$ and $\Gamma \to W$ paths, respectively. The conduction-band minimum (CBM) of all three phases is located at $\mathbf{k} = \Gamma$.

Using the HSE06 hybrid functional, we predict bandgaps E_g between 4-4.25 eV for the three phases, which are considerably larger than both the direct $E_g = 3-3.25$ eV and the indirect $E_g =$ 3.75 eV reported in experiments. 80,81 However, given the large E_{g} , we would not expect the overestimation of the bandgaps to significantly impact the calculated electronic properties. A measured bandgap for Pnma STO is not available, but our predicted band gap value is consistent with the insulating nature predicted in Ref. 82.

Fig. 7 shows the predicted scalar-average electrical conductivity σ , absolute Seebeck coefficient |S|, power factor $S^2\sigma$ (PF) and electronic thermal conductivity κ_{el} of the three STO phases with n-type doping as a function of doping level n at a fixed T = 1000K. A similar plot showing the temperature dependence properties at a fixed $n = 2 \times 10^{21}$ cm⁻³ is provided in Fig. S2.[†]

The relationship between n and σ is given by:

$$\sigma = \frac{ne^2 \tau^{\text{el}}}{m_{\sigma}^*} \tag{28}$$

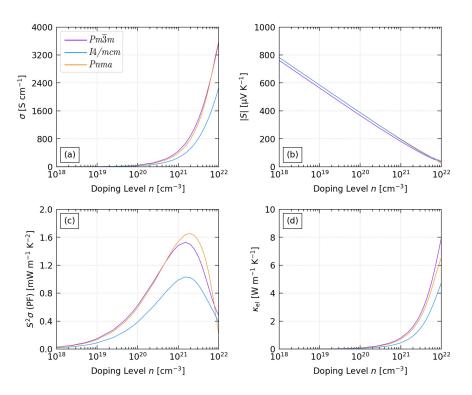


Fig. 7 Predicted scalar-average electrical properties of n-type $Pm\bar{3}m$, I4/mcm and Pnma phases of $SrTiO_3$ as a function of extrinsic carrier concentration n ("doping level") at a fixed temperature T=1000 K: (a) electrical conductivity σ , (b) absolute Seebeck coefficient |S|, (c) power factor $S^2\sigma$ (PF), and (d) electronic thermal conductivity $\kappa_{\rm el}$.

 $au^{\rm el}$ is a weighted-average electron lifetime, comparable to the $au^{\rm ph}$ obtained from analysing the particle-like lattice thermal conductivity (c.f. Eq. (19)). Similarly, m_σ^* is a weighted-average carrier "effective mass" for electronic conductivity, averaged over the bands that contribute to the σ . The approximately linear rise in σ with n results in a steep rise in σ when the carrier concentration is plotted on a logarithmic scale as in Fig. 7(a). We predict that $n > 10^{20}~{\rm cm}^{-3}$ are required to obtain a reasonable σ .

On the other hand, the S is inversely proportional to the n according to:

$$S = \frac{8\pi^2 k_{\rm B}^2}{3qh^2} m_S^* \left(\frac{\pi}{3n}\right)^{2/3} \tag{29}$$

where $q = \pm e$ for hole and electron carriers and m_S^* is the Seebeck effective mass and is related to m_σ^* through: ¹¹

$$m_{\rm S}^* = N_{\rm V}^{2/3} m_{\rm \sigma}^* \tag{30}$$

where N_V is the valley degeneracy. This dependence results in a monotonic decrease in |S| with n, again when plotted on a logarithmic scale (Fig. 7(b).

The opposing behaviour of σ and |S| result in a peak in the $S^2\sigma$, with the PFs optimised at $n\approx 2\times 10^{21}$ cm⁻³. This is in line with previous studies. ^{43,83} While pristine stoichiometric SrTiO₃ can have relatively low n on the order of 10^{15} cm⁻³, ⁸⁴ exposure of the material to reducing conditions can produce large concentrations of oxygen vacancies, which act as electron donors and yield carrier concentrations above 10^{20} cm⁻³ without explicit chemical doping. ⁸⁵ It is possible to obtain $n>10^{21}$ cm⁻³ with explicit dop-

ing, for example by replacing Sr with La and/or Ti with Nb. ^{85–87} The carrier concentration we predict is required to optimise the PFs should therefore be readily accessible in experiments.

Finally, large n results in "degenerate" semiconducting behaviour with a metallic-like dependence of the conductivity on temperature (Fig. $S2^{\dagger}$). Under these circumstances, the κ_{el} is related to the σ through the Wiedemann-Franz law:

$$\kappa_{\rm el} = L\sigma T$$
(31)

where L is the Lorentz number. As a result, the $\kappa_{\rm el}$ rises steeply above $n\approx 10^{20}$, reaching values of ~ 1 W m⁻¹ K⁻¹ at the $n\approx 2\times 10^{21}$ cm⁻³ that optimises the PF, and becomes comparable in magnitude to the $\kappa_{\rm latt}$ at $n\approx 5\times 10^{21}$ cm, ⁻³ (Fig. 7(d), c.f. Table 2).

We note that we have excluded the temperature dependence of the properties in Eqs (28)-(31) for brevity, but the effective masses m_σ^*/m_S^* , $\tau^{\rm el}$ and L are in general temperature dependent. All four parameters may also in general depend on the n.

Table 4 lists the values of the four electrical properties at $n=2\times 10^{21}~\rm cm^{-3}$ and $T=1000~\rm K$. We predict the $Pm\bar{3}m$ and Pnma phases to show similar electrical properties, with the cubic phase having a 10% higher σ and the latter an 11% larger |S|. The net result is that the Pnma phase is predicted to have a 10% larger PF and, due to its lower σ , a 9.9% lower $\kappa_{\rm el}$. On the other hand, while all three phases have similar |S|, the I4/mcm phase has notably poorer σ , which results in a 32/62% smaller peak PF compared to the $Pm\bar{3}m$ and Pnma phases, albeit with the benefit of a 40-60% lower $\kappa_{\rm el}$.

Given the similar E_g , the lower electrical conductivity of the *I4/mcm* phase is somewhat surprising. To investigate this further, we followed the procedure in Ref. 88 to obtain an estimate of the m_{σ}^* and m_{S}^* . These calculations entail performing calculations using the constant relaxation-time approximation (CRTA), in which the τ_{ki} in Eq. (9) are replaced by a constant relaxation time τ^{el} . In these calculations, the $\tau^{\rm el}$ act as a scaling factor for the σ , and thus by comparing the CRTA conductivity to that calculated with per-state scattering rates we can determine weighted-average $au^{\rm el}$ that can be used to compare between systems in the same way as the $\tau^{\rm ph}$ in Eq. (19).

The calculated m_{σ}^* , $m_{\rm s}^*$ and $\tau^{\rm el}$ at $n=2\times 10^{21}~{\rm cm}^{-3}$ and T=1000 K are included in Table 4. We calculate very similar $m_{\sigma}^* =$ 0.74-0.79 m_e and $m_s^* = 2.29-2.49 m_e$ for the three systems. The 5.9 and 8.6% larger m_S^* of the I4/mcm and Pnma phases compared to the cubic phase account for the majority of the 7.7/11.5% larger |S|. On the other hand, the 2.6-5.1% difference in the m_{σ}^* of the *Pnma* and I4/mcm phases compared to the $Pm\bar{3}m$ phase indicate that the much lower σ of the tetragonal phase is not due to differences in effective masses. Instead, the calculated $au^{\rm el}$ indicate that the I4/mcm phase has significantly stronger electron scattering compared to the other two phases.

Analysis of the mobility μ as a function of n at T=1000K shows shows that the μ is dominated by polar-optic phonon (POP) scattering (Fig. S3 †). The associated μ_{POP} are between 1.5-2× larger in the *Pnma* and $Pm\bar{3}m$ phase, indicating that the shorter $\tau^{\rm el}$ in the I4/mcm phase is due to stronger POP scattering. The treatment of POP scattering in this work is based on the Frölich model for an electron in a dielectric medium interacting with a dispersionless optic phonon mode with frequency $\omega_{\rm po}$. ⁸⁹ The scattering matrix elements g are of the form: 90

$$g \propto \left[\frac{\hbar\omega_{\text{po}}}{2} \left(\frac{1}{\varepsilon_{\infty}} - \frac{1}{\varepsilon_{\text{S}}}\right)\right]^{\frac{1}{2}}$$
 (32)

where ε_{∞} and ε_{S} are the scalar averages of the high-frequency and static dielectric constants. The three systems have similar $\omega_{\rm po} = 5.2$ -6.5 THz and similar $\varepsilon_{\infty} = 6.75$ -7 ε_0 . The $\varepsilon_{\rm S}$ span a much larger range of 220-350 ε_0 , but are much larger than the ε_{∞} , and so the latter therefore dominate the right-hand expression in Eq. (32). AMSET uses a modified version of the Frölich model that accounts for anisotropy in the dielectric properties, but this is is unlikely to explain the stronger POP scattering in the I4/mcm phase because the $\boldsymbol{\varepsilon}_{\infty}$ tensors are almost isotropic, with the directional components $\varepsilon_{\infty,\alpha\alpha}$ differing by at most 2% from the scalar averages. The matrix elements in AMSET also incorporate a term for the overlap of the electronic states. Moreover, to calculate the scatteing rates (inverse lifetimes), the g are combined with an expressions accounting for thermal population and the conservation of energy similar to those in Eqs (23)/(24). ⁵⁴ It is currently not possible to separate the two types of contribution from the nature of the electronic states, but we can nonetheless infer that the stronger POP scattering in the I4/mcm phase is due to these and not to differences in the model optic phonon and dielectric properties.

We recently performed a similar analysis for the chalcogenides

SnS and SnSe, ⁷⁹ which yielded m_{σ}^* and $m_{S}^* = 0.15$ -0.27 and 0.7-0.81 respectively. The oxides therefore have a larger m_{σ}^* , resulting in lower σ that requires roughly an order of magnitude larger nto offset. While the oxides have a 3-4 \times larger m_S , potentially resulting in a larger |S|, this is counterbalanced by the large nrequired to optimise the PF. Also, while Ref. 79 did not calculate $\tau^{\rm el}$, similar results to those obtained with per-state τ_{kj} were obtained using a typical $\tau^{el} = 10$ fs (10⁻¹⁴ s), which suggests a weighted-average relaxation time around an order of magnitude longer than we calculate for STO. The analysis of the κ_{latt} in the previous section suggested that the stronger bonding in the oxides mey lead to stronger phonon anharmonicity and shorter phonon lifetimes. Drawing a parallel, analysis of the $au^{\rm el}$ suggests that this also results in stronger electron scattering and shorter electron lifetimes.

Our previous study of the LnCoO₃ yielded $m_{\sigma}^* = 2.26-2.6 m_{\rm e}$ and $m_s^* = 5.27-5.74 m_e$ at the *n* that maximise the PF. ⁷⁸ In terms of optimising the properties, this suggests that, as for the κ_{latt} , exploring alternative perovskite chemistries may be fruitful, although weaker chemical bonding may have the undesirable side effect of increasing the conductivity effective masses. It would be of particular interest to determine whether the much lower σ of the *I*4/*mcm* phase is replicated over other perovskite materials, as, if so, it would imply that this phase should ideally be avoided. The results in the present study are however insufficient to confirm or otherwise generality of this finding.

Finally, we again consider again the directional anisotropy in the electrical properties. The diagonal $\sigma_{\alpha\alpha}$, $S_{\alpha\alpha}$ and $\kappa_{\rm el,\alpha\alpha}$ components of the σ , S and $\kappa_{\rm el}$ tensors, and the corresponding power factors $S_{\alpha\alpha}^2 \sigma_{\alpha\alpha}$, calculated at $n = 2 \times 10^{21}$ cm⁻³ and T = 1000K are shown in Table S5.[†] The tetragonal phase shows fairly minimal anisotropy, with up to 5% differences in the directional σ , S and $S^2\sigma$ compared to the scalar averages, and a slightly larger 7.5% variation in the κ_{el} . The electrical properties of the orthorhombic phase show more anisotropy, with up to 6.2-9% variation in the σ , S and $\kappa_{\rm el}$, and 12.7/10.9% higher/lower $S^2\sigma$ along the crystallographic b and c directions compared to the scalar average, which, for this system, is close to the PF along the a direction. While larger than the anisotropy in the κ_{latt} , we still consider this to be relatively modest.

The I4/mcm structure shows the largest σ and $\kappa_{\rm el}$ but the smallest absolute S along the c direction. The |S| is similar to the cubic phase, but the σ and $\kappa_{\rm el}$ are much smaller, as is the $S^2\sigma$. The equivalent comparison for the *Pnma* phase shows the smallest σ , largest |S| and intermediate $\kappa_{\rm el}$ along the b direction. The σ and $\kappa_{\rm el}$ are lower than those in the $Pm\bar{3}m$ phase, but more comparable than those in the tetragonal phase, whereas the |S| and, consequently, the PF, are significantly larger. We therefore infer that the distortions in the two lower-symmetry phases have a significant impact on the electrical properties relative to the cubic phase, even when compared along equivalent directions.

3.3 Thermoelectric figure of merit

Combining the lattice thermal conductivity and electricaltransport properties discussed in the two preceding sections al-

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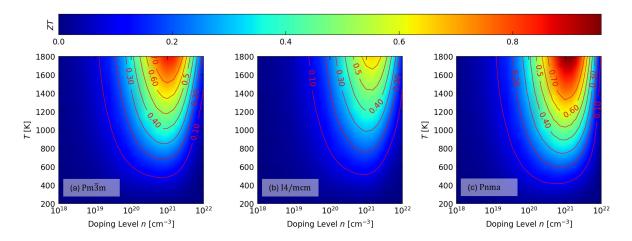


Fig. 8 Predicted scalar-average n-type thermoelectric figure of merit zT of the $Pm\bar{3}m$, I4/mcm and Pnma phases of $SrTiO_3$ as a function of extrinsic carrier concentration ("doping level") n and temperature T.

Table 4 Analysis of the scalar-average n-type electronic properties of the three phases of $SrTiO_3$ examined in this work at T=1000 K and $n=2\times 10^{21}$ cm⁻³. For each phase we show the electronic conductivity σ , Seebeck coefficient S, power factor $S^2\sigma$ and electronic thermal conductivity κ_{el} . We also show the conductivity and Seebeck effective masses m_σ^*/m_S^* and weighted-average electronic lifetime τ^{el} calculated as described in the text.

	σ [S cm $^{-1}$]	S [μV K ⁻¹]	$S^2 \sigma$ [mW m $^{-1}$ K $^{-2}$]	$\kappa_{\rm el}$ [W m ⁻¹ K ⁻¹]	m_{σ}^* $[m_{\mathrm{e}}]$	m_S^* $[m_e]$	τ ^{el} [fs]
Pm3m	88.1	-130	1.5	1.61	0.78	2.21	1.22
I4/mcm Pnma	51.9 78.9	-140 -145	1.02 1.65	0.93 1.45	0.82 0.8	2.34 2.4	0.76 1.12

lows is to predict the figure of merit, zT. Our analysis of the κ_{latt} found that the additional contribution to the "particle-like" contribution, κ_p , obtained by solving the linearised Boltzmann transport equation over the less computationally-demanding single-mode relaxation-time approximation was relatively small, but that the wave-like contribution from interband tunnelling, κ_w , was significant in all three phases. On the basis that combining the LBTE κ_p with the κ_w should give the most accurate description of the κ_{latt} , we used these values for calculating the zT.

Fig. 8 shows the predicted scalar-average zT of the three phases of $SrTiO_3$ as a function of doping level n and temperature T. Given the fall in the κ_{latt} with temperature and the behaviour of the power factor $S^2\sigma$ with n (c.f. Figs 5 and 7), the best performance is obtained at high T and relatively large $n \approx 10^{21}$ cm⁻³.

Table 5 lists the maximum predicted zT, $zT_{\rm max}$, for T=400, 600 and 1000 K, roughly matching the low-, mid- and high-temperature heat-recovery scenarios outlined in Ref. 91. We predict $zT_{\rm max}$ of <0.1, 0.13-0.21 and 0.31-0.47 at the three temperatures, all of which are lower than the typical benchmark zT=1 but which are consistent at the higher temperature with experimental measurements. With the exception of the cubic and tetragonal phases having similar predicted $zT_{\rm max}$ at 400 K, we predict that the zT fall in the order of $Pnma > Pm\bar{3}m > I4/mcm$ at all three temperatures. The relatively poor performance of the tetragonal phase is primarily due to its low conductivity, which does not compensate for its larger absolute Seebeck coefficient and results in a low power factor. On the other hand, the superior performance of the Pnma phase compared to the $Pm\bar{3}m$ phase is primarily due to its 15-30% lower $\kappa_{\rm latt}$ and correspondingly

lower total thermal conductivity, as well as to the combination of slightly lower σ and slightly larger |S| producing a 2-4% larger $S^2\sigma$.

Table S6 compares the directional values of the zT, $S^2\sigma$ and κ_{tot} under the same conditions as the zT_{max} in Table 5. The zTof the *I*4/*mcm* phase show modest anisotropy, with a 3.2% larger zT_{max} along the a=b direction and a 6.5% smaller zT_{max} along the c direction compared to the scalar average at T=1000 K. This is due primarily to differences in the thermal conductivity. The Pnma phase shows more significant anisotropy, with a 3.9% larger PF and 4.3% smaller κ_{tot} along the b direction resulting in an 8.4% higher zT_{max} compared to the scalar average, and a 7.8% smaller PF and 0.93% higher κ_{tot} along the c direction producing a 10% lower zT_{max} . As for the electrical properties, we find little correspondence between the zT of the cubic phase and the those along the c direction in the I4/mcm phase and the b direction in the *Pnma* phase, which indicates that the large impact of the structural distortions on the electrical properties also carries through to the figure of merit.

Experimental values of zT span a range of 0.27-0.37, with $\sigma=200\text{-}303~\mathrm{S~cm^{-1}}$, S=-168 to -233 $\mu\mathrm{V~K^{-1}}$, and $\kappa=2.6\text{-}3.1~\mathrm{W~m^{-1}~K^{-1}}$ at $T=1000~\mathrm{K.}^{92\text{-}94}$ Assuming the $Pm\bar{3}m$ phase, we predict values of between $zT=0.2~(n=10^{20}~\mathrm{cm^{-3}},~\sigma=46.1~\mathrm{S~cm^{-1}},~S=\text{-}367~\mu\mathrm{V~K^{-1}},~\kappa=3.09~\mathrm{W~m^{-1}~K^{-1}}$ and $zT=0.37~(n=5\times10^{20}~\mathrm{cm^{-3}},~\sigma=227~\mathrm{S~cm^{-1}},~S=\text{-}152~\mu\mathrm{V~K^{-1}},~\kappa=3.41~\mathrm{W~m^{-1}~K^{-1}})$. These predictions, in particular those at the larger n, are reasonably consistent with experimental measurements, confirming the accuracy of our modelling approach. In particular, with reference to Table 2, and as found in our previous

Table 5 Predicted maximum scalar-average n-type zT, $zT_{\rm max}$, of the three phases of $SrTiO_3$ examined in this work at T=400, 600 and 1000 K, roughly corresponding to the low-, medium- and high-temperature heat-recovery scenarios outlined in Ref. 91. For each predicted zT we also show the associated extrinsic carrier concentrations ("doping levels") n, Seebeck coefficients S, electrical conductivities σ , power factors $S^2\sigma$ (PFs), and lattice, electronic and total thermal conductivities κ_{latt} , κ_{el} and κ_{tot} .

	T	n		S	σ	$S^2\sigma$ (PF)	κ [W m ⁻¹ K ⁻¹]		
	[K]	$[\mathrm{cm}^{-3}]$	ZT	$[\mu { m V~K^{-1}}]$	$[S cm^{-1}]$	$[mW m^{-1} K^{-2}]$	$\kappa_{\rm el}$	κ_{latt}	κ_{tot}
	400	7.5×10^{20}	0.06	-109	900	1.06	0.76	5.79	6.55
Pm3̄m	600	7.5×10^{20}	0.15	-150	581	1.31	0.7	4.29	4.99
	1000	1×10^{21}	0.39	-182	448	1.48	0.79	3.01	3.8
I4/mcm	400	7.5×10^{20}	0.06	-128	484	0.79	0.4	4.9	5.3
	600	1×10^{21}	0.13	-148	432	0.94	0.49	3.77	4.26
	1000	1×10^{21}	0.31	-195	261	0.99	0.45	2.77	3.22
Pnma	400	5×10^{20}	0.09	-148	500	1.08	0.4	4.25	4.65
	600	7.5×10^{20}	0.21	-166	487	1.34	0.58	3.33	3.91
	1000	1×10^{21}	0.47	-198	392	1.54	0.7	2.54	3.24

work, ⁷⁸ accounting for wave-like tunnelling contributions to the κ_{latt} is necessary to obtain realistic values. With this in mind, our predictions suggest that experiments have likely achieved close to the maximum possible for pristine bulk-like cubic STO, but that significant performance enhancements could be possible by targeting chemical modifications (e.g. doping) that stabilise the orthorhombic phase - according to our analysis, doing so would largely retain the favourable electrical properties of the $Pm\bar{3}m$ phase while significantly reducing the κ_{latt} .

Conclusions

In summary, we have carried out a detailed ab initio modelling study of the impact of crystal structure on the thermoelectric performance of the archetypal oxide perovskite SrTiO3 in the orthorhombic Pnma, tetragonal I4/mcm and cubic $Pm\bar{3}m$ phases.

Analysis of the structural dynamics and lattice thermal conductivity shows that the primary impact of structure type is that the smaller primitive cell of the $Pm\bar{3}m$ phase results in larger phonon group velocities and a larger contribution from "particlelike" (band) transport to the κ_{latt} , which more than offsets its shorter phonon lifetimes. More generally, compared to the flagship Group IV-VI chalcogenide TEs, the oxides show relatively strong phonon scattering and short phonon lifetimes, but this is more than compensated by larger group velocities. Based on this, efforts to optimise (i.e. reduce) the κ_{latt} of STO and other oxide perovskites should focus on chemical modifications or alternative perovskite chemistries that favour lower-symmetry crystal structures and which have weaker chemical bonding. A second notable finding from our analysis of the κ_{latt} is the large contribution from wave-like transport, which has a large impact on all three phases but is most significant for the lower-symmetry structures. Taken together with our previous work on the lanthanide cobalates, we suggest that accounting for transport through this mechanism is important for an accurate description of the κ_{latt} in oxide perovskites, and that the increase in this term in lowersymmetry structures may be universal across different oxide perovskite chemistries.

Analysis of the electrical properties indicates that the I4/mcmphase has significantly lower electrical conductivity due to strong polar-optic phonon scattering, whereas the Pnma phase shows comparable or higher power factors to the higher-symmetry $Pm\bar{3}m$ phase due to the combination of a lower σ but larger absolute Seebeck coefficent. Comparing again to the Group IV-VI chalcogenides, we find that the power factors of the oxides are limited by high conductivity effective masses and short electron lifetimes, and that the high carrier concentrations required to offset this counteract the higher |S|. From a fundamental perspective, it is interesting to note that the oxides show both short phonon and electron lifetimes, which could indicate that the electrical properties and κ_{latt} may be coupled in a way which is yet to be examined in detail. We also believe the low predicted σ of the I4/mcm phase warrants further investigation, particularly to determine whether similar behaviour is observed across different perovskite chemistries.

Finally, our predicted zT show that, while STO cannot achieve the benchmark $zT \ge 1$ even at a high T = 1000 K, it may be possible to significantly improve upon existing experimental studies by targeting the stabilisation of lower-symmetry structures and in particular the orthorhombic *Pnma* phase.

We hope that the results presented here will ultimately provide some important insight to support ongoing efforts to obtain highperformance oxide thermoelectrics for sustainable energy recovery.

Author contributions

Conceptualization, methodology, software and writing - all authors; data curation, formal analysis and investigation - AZK and JMF; funding acquisition - JMS; project administration and supervision - JMF and JMS; resources - JMS.

Conflicts of interest

There are no conflicts to declare.

Data availability

Raw data from this study will be made available to download free of charge after publication from an online repository at https://doi.org/10.17632/9h4b89b79r. Our analysis code is available on GitHub at https://github.com/skelton-group/ZT-Calc-Workflow.

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Notes and references

- 1 World Meteorological Organization, State of the Climate Report, 2024.
- 2 H. Ritchie and M. Roser, ${\it CO}_2$ and ${\it Greenhouse}$ ${\it Gas}$ ${\it Emissions},$ 2020, https://ourworldindata.org/emissions-by-sector.
- 3 I. MacLeay, K. Harris and A. Annut, *Digest of united kingdom energy statistics 2015.*, Stationery Office, in Department of Energy & Climate Change National Statistics, 2015.
- 4 R. Freer and A. V. Powell, *Journal of Materials Chemistry C*, 2020, **8**, 441–463.
- 5 H. Xie, Y. Zhang and P. Gao, Micromachines, 2023, 14, 31.
- 6 T. Torfs, V. Leonov, C. V. Hoof and B. Gyselinckx, 2006 5th IEEE Conference on Sensors, 2006, 427–430.
- 7 Y. Rao, C. Xu, M. Voss, P. Ying, H. Reith, K. Nielsch, T. Bechtold and D. Hohlfeld, *Advanced Materials Technologies*, 2024, 9, 2301157.
- 8 N. V. Burnete, F. Mariasiu, C. Depcik, I. Barabas and D. Moldovanu, *Progress in Energy and Combustion Science*, 2022, **91**, 101009.
- H. Zhou, T. Tian, X. Wang and J. Li, Applied Energy, 2023, 332, 120539.
- 10 L. Catalan, P. Alegria, M. Araiz and D. Astrain, *Applied Thermal Engineering*, 2023, **222**, 119843.
- 11 G. Tan, L.-D. Zhao and M. G. Kanatzidis, *Chemical Reviews*, 2016, **116**, 12123–12149.
- 12 A. Walsh, D. J. Payne, R. G. Egdell and G. W. Watson, *Chem. Soc. Rev.*, 2011, **40**, 4455–4463.
- 13 S. K. Guillemot, A. Suwardi, N. Kaltsoyannis and J. M. Skelton, *J. Mater. Chem. A*, 2024, **12**, 2932–2948.
- 14 R. Deng, X. Su, Z. Zheng, W. Liu, Y. Yan, Q. Zhang, V. P. Dravid, C. Uher, M. G. Kanatzidis and X. Tang, *Science Advances*, 2018, 4, eaar5606.
- 15 H. Lee, T. Kim, S. C. Son, J. Kim, D. Kim, J. Lee and I. Chung, Materials Today Physics, 2023, 31, 100986.
- B. Zhu, X. Liu, Q. Wang, Y. Qiu, Z. Shu, Z. Guo, Y. Tong, J. Cui,
 M. Gu and J. He, *Energy Environ. Sci.*, 2020, 13, 2106–2114.
- 17 K. Biswas, J. He, I. D. Blum, C.-I. Wu, T. P. Hogan, D. N. Seidman, V. P. Dravid and M. G. Kanatzidis, *Nature*, 2012, 489, 414–418.
- 18 Z. M. Gibbs, H. Kim, H. Wang, R. L. White, F. Drymiotis, M. Kaviany and G. Jeffrey Snyder, *Applied Physics Letters*, 2013, 103, 262109.
- 19 O. Delaire, J. Ma, K. Marty, A. F. May, M. A. McGuire, M.-H. Du, D. J. Singh, A. Podlesnyak, G. Ehlers, M. D. Lumsden and

- B. C. Sales, Nature Materials, 2011, 10, 614-619.
- 20 D. Champier, Energy Conversion and Management, 2017, 140, 167–181.
- 21 I. TERASAKI, Phys. Rev. B, 1997, 56, 685-687.
- 22 H. Yakabe, K. Kikuchi, I. Terasaki, Y. Sasago and K. Uchinokura, Proceedings of the 1997 16th International Conference on Thermoelectrics, 1997, p. 523 527.
- 23 W. Koshibae, K. Tsutsui and S. Maekawa, *Physical Review B* Condensed Matter and Materials Physics, 2000, **62**, 6869 6872.
- 24 Y. Miyazaki, Solid State Ionics, 2004, 172, 463-467.
- 25 M. Shikano and R. Funahashi, *Applied Physics Letters*, 2003, **82**, 1851 1853.
- 26 H. Fukutomi, Y. Konno, K. Okayasu, M. Hasegawa and H. Nakatsugawa, *Materials Science and Engineering: A*, 2009, **527**, 61–64.
- 27 J. D. Baran, M. Molinari, N. Kulwongwit, F. Azough, R. Freer, D. Kepaptsoglou, Q. M. Ramasse and S. C. Parker, *The Journal of Physical Chemistry C*, 2015, 119, 21818–21827.
- 28 R. Funahashi, I. Matsubara and S. Sodeoka, *Applied Physics Letters*, 2000, **76**, 2385 2387.
- 29 J. Diez, E. Guilmeau, M. Madre, S. Marinel, S. Lemonnier and A. Sotelo, *Solid State Ionics*, 2009, 180, 827–830.
- 30 E. Combe, R. Funahashi, T. Barbier, F. Azough and R. Freer, *Journal of Materials Research*, 2016, **31**, 1296–1305.
- 31 T. Tsubota, M. Ohtaki, K. Eguchi and H. Arai, *Journal of Materials Chemistry*, 1997, **7**, 85 90.
- 32 T. Okuda, K. Nakanishi, S. Miyasaka and Y. Tokura, *Phys. Rev. B*, 2001, **63**, 113104.
- 33 H. Muta, K. Kurosaki and S. Yamanaka, *Journal of Alloys and Compounds*, 2003, **350**, 292–295.
- 34 H. Muta, K. Kurosaki and S. Yamanaka, *Journal of Alloys and Compounds*, 2005, **392**, 306–309.
- 35 T. Kobayashi, H. Takizawa, T. Endo, T. Sato, M. Shimada, H. Taguchi and M. Nagao, *Journal of Solid State Chemistry*, 1991, **92**, 116–129.
- 36 D. Flahaut, T. Mihara, R. Funahashi, N. Nabeshima, K. Lee, H. Ohta and K. Koumoto, *Journal of Applied Physics*, 2006, 100, 084911.
- 37 D. A. Muller, N. Nakagawa, A. Ohtomo, J. L. Grazul and H. Y. Hwang, *Nature*, 2004, 430, 657–661.
- 38 J. Haeni, P. Irvin, W. Chang, R. Uecker, P. Reiche, Y. Li, S. Choudhury, W. Tian, M. Hawley, B. Craigo, A. Tagantsev, X. Pan, S. Streiffer, L. Chen, S. Kirchoefer, J. Levy and D. Schlom, *Nature*, 2004, 430, 758–761.
- 39 H. Muta, A. Ieda, K. Kurosaki and S. Yamanaka, *Materials Letters*, 2004, **58**, 3868–3871.
- 40 A. F. Santander-Syro, O. Copie, T. Kondo, F. Fortuna, S. Pailhès, R. Weht, X. G. Qiu, F. Bertran, A. Nicolaou, A. Taleb-Ibrahimi, P. Le Fèvre, G. Herranz, M. Bibes, N. Reyren, Y. Apertet, P. Lecoeur, A. Barthélémy and M. J. Rozenberg, *Nature*, 2011, 469, 189–193.
- 41 C. Mallada, J. Menéndez, O. Dura, M. López de la Torre, R. Menéndez and R. Santamaría, *Journal of the European Ce*-

42 A. Mubarak, International Journal of Modern Physics B, 2016,

30, 1650141.

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Access Article. Published on 19 2025. Downloaded on 04/09/25 03:43:51

- 43 A. Z. Khan, J. M. Flitcroft and J. M. Skelton, Mater. Adv., 2024. **5**, 652–664.
- 44 S. Kumar, A. Barasheed and H. Alshareef, ACS Applied Materials and Interfaces, 2013, 5, 7268-7273.
- 45 L. Goncalves, P. Alpuim, A. Rolo and J. Correia, Thin Solid Films, 2011, 519, 4152-4157.
- 46 S. Saini, P. Mele and A. Tiwari, Journal of Physics and Chemistry of Solids, 2019, 129, 347-353.
- 47 W. Zhao, S. Fan, N. Xiao, D. Liu, Y. Tay, C. Yu, D. Sim, H. Hng, Q. Zhang, F. Boey, J. Ma, X. Zhao, H. Zhang and Q. Yan, Energy and Environmental Science, 2012, 5, 5364-5369.
- 48 J. Chen, H. Chen, F. Hao, X. Ke, N. Chen, T. Yajima, Y. Jiang, X. Shi, K. Zhou, M. Döbeli, T. Zhang, B. Ge, H. Dong, H. Zeng, W. Wu and L. Chen, ACS Energy Letters, 2017, 2, 915-921.
- 49 S. Ohta, T. Nomura, H. Ohta and K. Koumoto, J. Appl. Phys., 2005, 97, 034106.
- 50 A. Togo, L. Chaput and I. Tanaka, Phys. Rev. B, 2015, 91, 094306.
- 51 M. Simoncelli, N. Marzari and F. Mauri, Phys. Rev. X, 2022, **12**, 041011.
- 52 L. Chaput, Phys. Rev. Lett., 2013, 110, 265506.
- 53 G. K. Madsen, J. Carrete and M. J. Verstraete, Computer Physics Communications, 2018, 231, 140-145.
- 54 A. M. Ganose, J. Park, A. Faghaninia, R. Woods-Robinson, K. A. Persson and A. Jain, Nat. Commun., 2021, 12, 2222.
- 55 G. Kresse and J. Hafner, Phys. Rev. B, 1993, 47, 558-561.
- 56 A. Jain, S. P. Ong, G. Hautier, W. Chen, W. D. Richards, S. Dacek, S. Cholia, D. Gunter, D. Skinner, G. Ceder and K. A. Persson, APL Materials, 2013, 1, 011002.
- 57 J. P. Perdew, A. Ruzsinszky, G. I. Csonka, O. A. Vydrov, G. E. Scuseria, L. A. Constantin, X. Zhou and K. Burke, Phys. Rev. Lett., 2008, 100, 136406.
- 58 Blöchl, P. E., Phys. Rev. B, 1994, 50, 17953-17979.
- 59 G. Kresse and D. Joubert, Phys. Rev. B, 1999, 59, 1758-1775.
- 60 H. J. Monkhorst and J. D. Pack, Phys. Rev. B, 1976, 13, 5188-
- 61 A. Togo and I. Tanaka, Scripta Materialia, 2015, 108, 1-5.
- 62 X. Gonze and C. Lee, Phys. Rev. B, 1997, 55, 10355-10368.
- 63 Gajdoš, M. and Hummer, K. and Kresse, G. and Furthmüller, J. and Bechstedt, F., Phys. Rev. B, 2006, 73, 045112.
- 64 A. V. Krukau, O. A. Vydrov, A. F. Izmaylov and G. E. Scuseria, J. Chem. Phys., 2006, 125, 224106.
- 65 J. M. Skelton, D. S. D. Gunn, S. Metz and S. C. Parker, Journal of Chemical Theory and Computation, 2020, 16, 3543-3557.
- 66 A. M. Ganose, A. J. Jackson and D. O. Scanlon, Journal of Open Source Software, 2018, 3, 717.
- 67 D. Porezag and M. R. Pederson, Phys. Rev. B, 1996, 54, 7830-7836.
- 68 J. M. Skelton, L. A. Burton, A. J. Jackson, F. Oba, S. C. Parker and A. Walsh, Phys. Chem. Chem. Phys., 2017, 19, 12452-

- 12465.
- 69 R. Shukla, S. J. Patwe, S. K. Deshpande, S. N. Achary, P. S. R. Krishna, A. B. Shinde, J. Gopalakrishnan and A. K. Tyagi, Scientific Reports, 2016, 6, 23400.
- 70 C. J. Howard and H. T. Stokes, Acta Crystallographica Section B, 1998, **54**, 782–789.
- 71 K. Momma and F. Izumi, Journal of Applied Crystallography, 2011, 44, 1272-1276.
- 72 Z. Zhang, K. Yuan, J. Zhu, X. Fan, J. Zhou and D. Tang, Applied Physics Letters, 2022, 120, 262201.
- 73 B. Himmetoglu, A. Janotti, H. Peelaers, A. Alkauskas and C. G. Van de Walle, Phys. Rev. B, 2014, 90, 241204.
- 74 N. M. Tubman, C. J. N. Coveney, C.-E. Hsu, A. Montoya-Castillo, M. R. Filip, J. B. Neaton, Z. Li, V. Vlcek and A. M. Alvertis, Phonon-mediated electron attraction in SrTiO₃ via the generalized Fröhlich and deformation potential mechanisms, 2025, https://arxiv.org/abs/2501.17230.
- 75 J.-J. Zhou, O. Hellman and M. Bernardi, Phys. Rev. Lett., 2018, **121**, 226603.
- 76 J. S. Bechtel and A. Van der Ven, Phys. Rev. Mater., 2018, 2, 025401.
- 77 K. Guo, T. Weng, Y. Jiang, Y. Zhu, H. Li, S. Yuan, J. Yang, J. Zhang, J. Luo, Y. Grin and J.-T. Zhao, Materials Today Physics, 2021, 21, 100480.
- 78 A. Khan, J. Flitcroft and J. Skelton, Phys. Chem. Chem. Phys., 2024, -.
- 79 M. Zhang, I. Pallikara, J. M. Flitcroft and J. M. Skelton, J. Mater. Chem. A, 2025, 13, 5415-5426.
- 80 M. Cardona, Phys. Rev., 1965, 140, A651-A655.
- 81 K. van Benthem, C. Elsässer and R. H. French, Journal of Applied Physics, 2001, 90, 6156-6164.
- 82 M. Kar, Electronic and optical properties of SrTiO3 perovskite using semi-local and hybrid first principles density functional theory, 2021.
- 83 Y. Zhu, J. M. Skelton, D. J. Lewis and R. Freer, Journal of Physics: Energy, 2024, 6, 025027.
- 84 X.-L. Shi, H. Wu, Q. Liu, W. Zhou, S. Lu, Z. Shao, M. Dargusch and Z.-G. Chen, Nano Energy, 2020, 78, 105195.
- 85 J. Ravichandran, W. Siemons, D.-W. Oh, J. T. Kardel, A. Chari, H. Heijmerikx, M. L. Scullin, A. Majumdar, R. Ramesh and D. G. Cahill, Phys. Rev. B, 2010, 82, 165126.
- 86 J. Wang, B.-Y. Zhang, H.-J. Kang, Y. Li, X. Yaer, J.-F. Li, Q. Tan, S. Zhang, G.-H. Fan, C.-Y. Liu, L. Miao, D. Nan, T.-M. Wang and L.-D. Zhao, Nano Energy, 2017, 35, 387-395.
- 87 S. Ohta, T. Nomura, H. Ohta, M. Hirano, H. Hosono and K. Koumoto, Applied Physics Letters, 2005, 87, 092108.
- 88 Z. M. Gibbs, F. Ricci, G. Li, H. Zhu, K. Persson, G. Ceder, G. Hautier, A. Jain and G. J. Snyder, npj Computational Materials, 2017, 3, 8.
- 89 H. Frhlich, Advances in Physics, 1954, **3**, 325–361.
- 90 C. Verdi and F. Giustino, Phys. Rev. Lett., 2015, 115, 176401.
- 91 S. LeBlanc, S. K. Yee, M. L. Scullin, C. Dames and K. E. Goodson, Renewable and Sustainable Energy Reviews, 2014, 32, 313-327.

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- 92 A. Kikuchi, N. Okinaka and T. Akiyama, *Scripta Materialia*, 2010, **63**, 407–410.
- 93 H. Wang, C. Wang, W. Su, J. Liu, Y. Zhao, H. Peng, J. Zhang, M. Zhao, J. Li, N. Yin and L. Mei, *Materials Research Bulletin*,
- 2010, **45**, 809–812.
- 94 D. Srivastava, C. Norman, F. Azough, M. C. Schäfer, E. Guilmeau, D. Kepaptsoglou, Q. M. Ramasse, G. Nicotra and R. Freer, *Phys. Chem. Chem. Phys.*, 2016, 18, 26475–26486.

Data Availability Statement

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Raw data from this study will be made available to download free of charge after publication from an online repository at https://doi.org/10.17632/9h4b89b79r. Our analysis code is available on GitHub at https://github.com/skelton-group/ZT-Calc-Workflow.