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Physical science of the didodecyldimethylammonium bromide–water system: 1. Equilibrium phase behaviour†‡

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Surfactant molecules in solvents self-assemble into a large variety of structures depending on their chemical composition, concentration and temperature, summarized in the system's equilibrium phase diagram. However, the occurrence of long-lived metastable states can lead to incomplete or partly incorrect phase diagrams. By applying a set of complementary techniques and recording changes on different length scales, we determine an improved aqueous equilibrium phase diagram of the widely used double-chain surfactant didodecyldimethylammonium bromide (DDAB) over a broad concentration range ($\phi_{\text{DDAB}} = 3\text{--}100\text{ wt\%}$). We reveal that DDAB molecules exist as zero-hydrates in the room temperature solid state and decompose above $90\text{ }^{\circ}\text{C}$: the upper temperature of the phase diagram. Differential scanning calorimetry was used to characterise the transition's heat energy, kinetics and temperature, while the structure of the phases was characterized by small angle X-ray scattering and microscopy. Raman spectroscopy combined with computational techniques provided information regarding the conformational properties of the surfactant molecules. Our results were in good agreement with the literature phase diagram for moderate temperatures and surfactant concentrations. At $16\text{ }^{\circ}\text{C}$, a transition from a frozen lamellar phase (L_{β}) to a fluid lamellar phase L_{α} has previously been suggested across all concentrations (Dubois *et al.* 1998), with T_m coinciding with the Krafft temperature (T_c) determined in dilute systems. Here, we characterize for the first time the low temperature equilibrium phase for $\phi_{\text{DDAB}} > 3\text{ wt\%}$ as a crystalline dispersion, and determine the position and shape of the Krafft eutectic. The equilibrium phase below $14.1\text{ }^{\circ}\text{C}$ is now assigned to a coexistence region of surfactant hydrate crystals and water $XW_n + W$. At intermediate temperatures, the crystal hydrates XW_n melt gradually into the previously reported L_{α} phase, leaving a narrow coexistence region in the phase diagram $XW_n + L_{\alpha}$. In conclusion, an amended broad equilibrium phase diagram is presented, combining our new results with those previously reported in the literature.

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Introduction

Dialkyldimethylammonium halides were the first entirely synthetic double-chain amphiphiles found to form bilayer structures similar to those of phospholipids constituting biological membranes.¹ They are commonly abbreviated as $C_mC_n\text{DA}^+\text{X}^-$, where C_m and C_n represent the two long hydrocarbon chains, D (or DM) stands for the two methyl groups, A stands for the quaternary ammonium, and X stands for the counterion, most commonly either chloride or bromide. For symmetric chains, the convention is to abbreviate the number of carbons in each chain, *e.g.* with D standing for di-dodecyl or di-decyl. Because of their ability to form long-lived vesicles at very low surfactant concentrations, they are commonly used as stable models for membranes.² Furthermore, they became some of the most commonly used double-chain amphiphiles in applications, such as protein



electrochemistry³ and bio-sensors⁴ due to their excellent ability to simulate the natural environment for biomolecules, their high electrocatalytic activity and great structural stability. Since cationic lipids can also combine electrostatically with a wide variety of oppositely charged biomolecules, cells or other biological structures,⁵ they were found to be efficient coatings for fast ion exchange chromatography,⁶ capillary electrophoresis,⁷ and can be used in gene delivery through complex formation with negatively charged DNA.⁸ On the other hand, their ability to destroy existing cell membranes containing negatively charged phospholipids make them applicable as immunosuppressant agents^{9,10} or bactericides.^{10,11} This cytotoxicity is significantly reduced when coated nanoparticles instead of pure vesicles are used^{5,12} or neutral helper lipids are added.¹³ In the chemical industry, cationic surfactants are highly applicable as softeners or hair conditioners, due to their low solubility and ability to neutralize charged surfaces.^{9,14} They found further application as disinfections agents,⁹ herbicides,¹⁵ or as wetting^{10,16} and antistatic agents.¹⁰

One of the most important representatives of this group is the cationic double-chain surfactant didodecyldimethylammonium bromide ($((C_{12}H_{25})_2N^+(CH_3)_2Br^-$, abbreviated as DDAB, also known as dilauryldimethylammonium bromide) (see Fig. 1 top), first synthesized in 1977.¹ Its molecular properties and aqueous phases have been studied extensively.^{17–27} However, the most recently published phase diagram covering a broad ϕ_{DDAB} range of the DDAB–water system¹⁷ differs in the low temperature regime from those of the other known dialkyl-dimethylammonium halide water systems^{28–31} through the occurrence of a stable lamellar gel phase L_β at low temperatures in contrast to a crystalline dispersion. For dilute systems, where vesicles are observed, it has been reported that both a L_β to L_α phase transition happens at the same temperature as the melting of DDAB crystals^{23–26} (determining the systems' Krafft temperature T_c), and that the long-lived L_β phase can be induced when excessive overcooling is avoided.^{24,26}

In this paper, we present a revision to the existing broad phase diagram (see Fig. 1 bottom), which replaces the L_β phase with a region in which DDAB hydrate crystals coexist either with water $XW_n + W$ below 14.1 °C or with a lamellar phase $XW_n + L_\alpha$ (at intermediate temperatures), drawing it closer to its longer-chain analogues. A set of complementary experimental techniques was used to characterize the obtained phases over many length scales. Furthermore, the stability of the pure DDAB powder sample, which was identified as a zero-hydrate at room temperature (in contrast to previous studies), could only be confirmed up to 90 °C. At higher temperatures, the molecule thermally degrades, setting a new upper limit to any DDAB phase diagram. We contextualise our results with the current literature, which is reviewed in Section 3, and provide reasons for the amendments to the phase diagram.

Experimental

Materials

DDAB was purchased from Aldrich (purity 99%) and Fluka (purity 99%) for comparison, and stored in a desiccator (RH < 40%) at

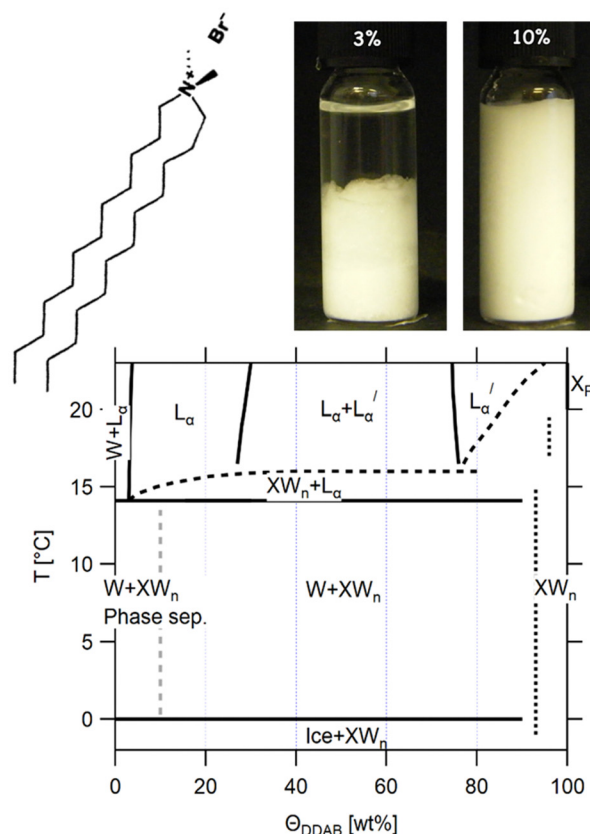


Fig. 1 (top) Sketch of the DDAB molecule, and photographs of the newly characterised 'white' phase; (bottom) proposed phase diagram of the binary DDAB/water system, where W corresponds to a dilute monomer solution (essentially pure water), L_α and L'_α to the swollen and collapsed lamellar phase, respectively, X_p to the powder crystal structure, and XW_n to a non-zero hydrate low temperature crystal structure. The position of the dotted lines in the diagram corresponding to XW_n as well as other non-zero hydrates are only estimated, as the exact number of water molecules are not known. The dashed grey line in the phase diagram limits the dilute region in which the low temperature dispersion of non-zero hydrates XW_n in W show a macroscopic phase separation (see left photograph at the top).

room temperature ($T \approx 20$ °C). Around 5 g of DDAB was recrystallised from ethyl acetate following established procedures,^{17,32} to ensure the results were not affected by impurities. In short, into a conical flask containing DDAB, ethyl acetate was incrementally added by Pasteur pipette (0.5–1 mL), with swirling, until the DDAB just dissolved. Diethyl ether was then added dropwise also with swirling, slowly reducing the polarity of the solvent system, until a precipitate remained upon swirling. The vessel was sealed to limit evaporation, and the solution cooled in a freezer. After 4 h, the flask was removed and the precipitate filtered. The nature of the precipitate was such that a large amount of product remained in the vessel. This was recrystallized from the same solvent system with extensive precipitation induced by an excess of diethyl ether (ca. 2–3 vol. eq.) rather than cooling. The precipitate was filtered to dryness in air and this process repeated twice. The pure product was dried with phosphorous pentoxide under a



nitrogen atmosphere. Because of the high capacity of the DDAB powder to absorb water, the sample was dried under vacuum for 48 h, and maintained under pure nitrogen atmosphere prior to measurements.

DDAB–water solutions. Samples expected to be in a lamellar phase at room temperature (see Fig. 1) with a volume of several cm^3 were prepared across a range of surfactant mass concentrations by diluting with distilled water (3 wt%, 5 wt%, 7 wt%, 10–85 wt% in 5 wt% steps). Samples were shaken and put on a roller mixer until they appeared homogeneous. More concentrated samples were stored for several days at 40 °C for equilibration. To remove air bubbles, all samples were centrifuged. Samples in the coexistence region (25–75 wt%) of the lamellar and collapsed lamellar phase (L_α/L'_α) were turbid, indicating phase coexistence, while samples above 75 wt% and below 25 wt% were optically clear. The samples were equilibrated for between one week and several months at the required temperature prior to measurement.

Analytical techniques

Thin-layer chromatography (TLC), electrospray ionization mass spectroscopy (ESI-MS) and nuclear magnetic resonance spectroscopy (NMR) were used to confirm the purity of the DDAB samples, as well as study their degradation products. The technical details are given in the ESI.†

Attenuated total reflectance Fourier transformed infrared spectroscopy (ATR FTIR). ATR FTIR spectroscopy was used to determine the hydration state of solid DDAB powder at room temperature, and upon drying from a liquid solution. The spectra were recorded in the region of 600–4000 cm^{-1} on a Shimadzu 8400 s FTIR with Pike Miracle ATR attachment (5–8 scans) for solid samples. Changes in the hydration state during evaporation from DDAB solutions were observed using an inVia Raman microscope with illuminatIR module (Renishaw) and an all reflective objective (ARO) (Smiths) (128 scans), allowing focussing onto specific regions in drying samples, albeit with reduced spectral quality. The spectra were corrected and analysed with the software WiRE 2.0 (Renishaw) and Origin 8.0.

Density measurements. The density ρ_{sol} of the dilute DDAB solutions depending on temperature (2–30 °C) and phase were studied using the oscillating U-tube densitometer (DA-510), calibrated with deionised water at 4, 10 and 20 °C. The setup required a sample volume of about 1 mL, which had to be introduced into the tube without droplets of air. This was difficult for viscous samples; therefore, measurements were performed on dilute solutions of 5 wt% and 10 wt%, and a 25 wt% sample was only used for the control. The observed quantitative dependence of ρ_{DDAB} on temperature was independent of surfactant weight concentration Φ_{DDAB} , when extracting the value using

$$\rho_{\text{DDAB}} = \frac{\rho_{\text{sol}}\rho_{\text{w}}}{\rho_{\text{w}} - (1 - \Phi_{\text{DDAB}})\rho_{\text{sol}}} \Phi_{\text{DDAB}} \quad (1)$$

The data were compared to the measured density dependence of pure water in the same range and analysed using Origin8.0.

Raman techniques and band assignment

Raman spectroscopy was used to investigate the conformational properties based on the vibrational states of the DDAB molecules in the aqueous solutions and solid samples, and their dependence on temperature and water concentration.

Raman spectroscopy. Vibrational spectra of bulk samples in solution were obtained using a Codberg T-800 triple grating spectrometer (excitation source: 514.5 nm of an argon laser; laser power at sample 500 mW; 400 μm slit, resulting in resolution of approximately 1.5 cm^{-1}). The samples were held in 100 mm diameter vials, which were temperature controlled to within 0.1 °C in a custom-built chamber (see the ESI,† Fig. S1). In the case of the solid sample, the powder was placed into a notch in an aluminium plate, and a low power red line (676.4 nm) of a Krypton laser was used as the excitation source, to minimize the anticipated strong heating effect on white powders. Spectra were recorded between $\nu = -4 \text{ cm}^{-1}$ and $\nu = 4000 \text{ cm}^{-1}$ ($\Delta\nu = 1 \text{ cm}^{-1}$, accumulation time/step = 1 s, overall scanning time $t \approx 80 \text{ min}$). The obtained peak at $\nu = 0 \text{ cm}^{-1}$ corresponding to the laser emission was used to calibrate the wavenumber shift, necessary to avoid any error induced by the electronics. To prevent destruction of the analyser by the laser beam, attenuating shutters were closed, prohibiting the recording of a signal up to about $\nu = 25 \text{ cm}^{-1}$ (see Fig. S1c, ESI†). It should be noted that a fluorescence background signal was observed, especially in more concentrated samples, or samples with an increased opaqueness, which could be partly removed through treatment with an intense laser line and corrected using Wire 2.0 (see the ESI,† Fig. S2). After background correction, the spectra were normalized using the peak between $\nu = 1400$ –1550 cm^{-1} using Origin8.0. Selected peaks were fitted with a combination of Gaussian (Lorentzian) curves using the Wire2.0 (Renishaw) software, until a fit of sufficient quality was obtained. As the fits depend on the starting positions and number of bands used, for comparing results, peaks were always fitted in the same manner.

Raman microscopy. The combination of Raman spectroscopy with confocal microscopy (Raman 300 with BX40 microscope, 10 $\times$ objective) allowed us to assess the Raman signal at different positions within a sample giving improved insight into the mixing behaviour of biphasic regions. A 100 μm thick sample was controlled in a custom-built sample cell ($\Delta T < 0.5 \text{ }^\circ\text{C}$, see the ESI,† Fig. S3). The 632.8 nm line of a HeNe laser was used as the excitation source (initial power 200 mW). Spectra were recorded on a CCD camera, calibrated using the laser peak and the peak of silicon (520.07 cm^{-1}). At settings ensuring maximum signal/noise ratio [hole size = 300 μm (500 μm for opaque samples), slit size = 150 μm (300 μm for opaque samples), 100% laser intensity] the resulting incident laser spot size was 21 μm (36 μm for opaque samples). The focus was adjusted to maximize signal/noise ratio. Spectra (recording time $\approx 5 \text{ min}$, by averaging 5–10 scans a 30s) were stable for up to 90 min apart from the decreased intensity of the fluorescent background (see the ESI,† Fig. S4). Compared to the Raman spectrum obtained above, the bands were slightly shifted to lower wavenumbers (see the ESI,† Fig. S5a–d) which was likely caused by the comparably poor calibration.



Furthermore, in the region of $2800\text{--}3100\text{ cm}^{-1}$ a small change in shape could be observed compared to the pure Raman spectra, which was caused by the different detection geometry used in the setups (see the ESI,† Fig. S5e). The recorded spectra were background corrected (polynomial fit) using LabSpec4.18 and Wire2.0, with respect to the spectrum of pure water in the sample cell. The peaks were normalized, by choosing a peak in the spectra which was least influenced by the measurement series, using LabSpec4.18 or Origin8.0.

Single molecule calculation. Single molecule calculations were used to support the assignment of the experimentally observed Raman frequencies, in combination with comparison to previous studies.^{33,34} All calculations were carried out using the software package Gaussian 03³⁵ running on a SUSE 9.x Linux HPC cluster (68 AMD Opteron processing cores) contained within EaStChem's Research Computing Facility's Hare cluster. Default convergence criteria were used for all calculations (maximum force = 0.00045, RMS force = 0.0003, maximum displacement = 0.0018, RMS displacement = 0.0012). After geometry optimization and testing (see the ESI†) the required level of approximation, the Raman spectra were obtained using BLYP 6-31G(d,p) (with scaling factor 0.992).

Small-angle X-ray scattering (SAXS)

SAXS was used to obtain information about the dependence of the repeat distance in the lamellar phases on surfactant concentration and temperature. Additionally, the strong forward scattering at low scattering vectors that was observed for the 'white' phase samples in the low temperature range was evaluated using the form factor of a particulate (such as a crystal) and the Porod scattering of its smooth interface in water. SAXS measurements were performed on a Nanostar U (Bruker, Karlsruhe), equipped with a rotating Turbo-Xray Source (TXS), operated at 40 kV/40 mA. The CuK_α radiation with $\lambda = 1.5418\text{ \AA}$ was focussed at the sample position by 2 crossed Göbel mirrors and 3 pinholes and scattering intensities detected on a 2D Hi-Star detector with 1048×1048 pixel resolution, positioned at a distance of 1.06 m and allowing a scattering vector range $0.008 < q < 0.2\text{ \AA}^{-1}$ with $q = 4\pi/\lambda \sin(\theta/2)$. The beam size was 0.5 mm. Absolute intensities [cm^{-1}] were obtained from comparison with a secondary standard, a thermoplastic polymer FEP1400 (Dupont Inc.), previously calibrated at the European Synchrotron Radiation Facility (ESRF), Grenoble, France. The data were obtained from random-oriented samples in glass capillaries (Hilgenberg, nominal thickness 1.5 mm), using an empty glass capillary for background correction. The samples were temperature-controlled in a custom-built cell ($\Delta T = 0.5\text{ }^\circ\text{C}$). The detected 'rings' were radially integrated using Bruker software. The data was background- and transmission-corrected using a Fortran program, and further analysed using IGOR Pro. Uncertainties in the intensity scale are of the order of 5–10% in view of possible thickness variations in the capillaries.

Microscopy

A Nikon Eclipse 80i microscope with a $10\times$ phase contrast objective (image size $2.2\text{ mm} \times 1.5\text{ mm}$) and an RMA 4376 (Media Cybernetics) camera were used to investigate structures in the micrometer length scale, such as multilamellar vesicles

or crystals, in liquid samples depending on surfactant concentration and temperature. To increase contrast, DDAB crystals in solution were recorded under crossed polarizers. If needed the sample was held in a temperature-controlled stage (linkam LTS350/TMS93/LNMP).

Differential scanning calorimetry (DSC)

DSC was used to identify the temperature and properties of the thermal phase transitions. DSC measurements on solution samples were carried out on the Mettler DSC30 in disposable crucibles made of aluminium under a nitrogen flow of 20 mL min^{-1} . Before the measurements, the equipment was calibrated using indium, gallium, lead and bismuth with scanning rates of 2, 5 and $10\text{ }^\circ\text{C min}^{-1}$. For samples larger than 10 mg, an aluminium oxide filled reference crucible was used. In order to confirm that the observed melting peak around $15\text{ }^\circ\text{C}$ is associated with the transition of the 'white' phase and is not present in overcooled clear samples, respective reference samples were loaded into the crucible in a cold room ($5\text{ }^\circ\text{C}$), and immediately put into the precooled device. The optimised scanning rate of $1\text{ or }2\text{ }^\circ\text{C min}^{-1}$ was chosen, after studying the dependence of the onset temperature and peak width on scanning rate was measured for rates of 10, 5, 2, 1 and $0.1\text{ }^\circ\text{C min}^{-1}$. Samples were in general scanned between $2\text{ }^\circ\text{C}$ and $20\text{ }^\circ\text{C}$ with the upper limit expanded for samples with high DDAB concentration. For selected samples, the influence of water freezing was also studied by extending the lower limit of the scan range down to $-20\text{ }^\circ\text{C}$. No influence of water freezing on the position or shape of the DDAB melting transition was observed. The onset temperature and peak width were within the experimental error of $0.3\text{ }^\circ\text{C}$ for the relative temperature for scanning rates of $1\text{ }^\circ\text{C}$. However, the calibration of the absolute temperature (error about $2\text{ }^\circ\text{C}$) was of comparably low precision. Furthermore, no dependence of peak width on sample mass or relative contact area between crucible and sample was found, indicating that the observed effects were not caused by a temperature gradient across the sample. In addition, control measurements on pure water were performed to ensure the observed effects were not artefacts of the equipment. For comparison of samples with different mass and DDAB concentration, the measured heat flow was normalized by dividing by the sample mass and DDAB volume fraction. The transition enthalpies were estimated by integrating the peak areas over the transition time. The changes in enthalpy observed with concentration lie within the error in the measured enthalpy value of $\delta\Delta H_{\text{DDAB}} = 5\text{ kJ mol}^{-1}$, which is mostly caused by variations due to scan rate, DDAB freezing temperature or sample history. In the low temperature water freezing runs, the enthalpy value of the DDAB melting transition shifted to the upper range of the measured values, but still lay within the measurement error of non-frozen values.

Review of phase studies of the DDAB–water system

In order to put the obtained experimental results into context, we provide below (and as a summary in Table 1) a thorough



Table 1 Selected properties of the cationic surfactant DDAB

Molecular mass m	461 g mol ⁻¹
Molecular volume V_m	784 Å ³ (20 °C), 792 Å ³ (40 °C)
Density ρ	0.98 kg cm ⁻³ (20 °C) ¹⁹
Area per headgroup	63 Å ² (L_α)–68 Å ² (L'_α) (depending on temperature and salt concentration) ^{17,19}
Chain length l_c	16.68 Å (fully stretched) ^{10,18}
Chain volume V_c	703.7 Å ³ ^{10,18}
Distance between bilayers in fully swollen lamellar phase	80 nm (decreases with increasing salt concentration) ¹⁹
Bilayer thickness a_b	24 Å (varies with temperature) ¹⁹
Ion layer thickness a_{Br}	7 Å ¹⁹
Critical vesicle concentration CVC	0.05 mM (2.3×10^{-3} wt%) ²⁴
Critical multilamellar phase concentration CVC ₂	0.7 mM (31×10^{-3} wt%) [0.21 mM (9.5×10^{-3} wt%) as multilamellar vesicles] ²⁴

review of the reported studies of the molecular properties of DDAB and the phases formed in the binary aqueous system, as well as comparisons with other dialkyldimethylammonium halide systems.

The aqueous phase behaviour of DDAB (as well as of other representatives of this group^{28–31}) has been extensively studied in the past.^{17–24} At temperatures above 16 °C (assigned as the chain melting temperature T_m ^{19,24} or Krafft temperature T_c ^{23,25,26}) two optically identical lamellar phases have been reported: the swollen lamellar phase L_α (3–28 wt%^{17,20} or 3–30 wt%^{9,36}), and the collapsed lamellar phase L'_α (83–91 wt%⁹ > 75 wt%^{17,20} 75–85 wt%³⁶). In contrast to the L_α phase, some counterions in the L'_α phase are expected to be bound to the bilayers, resulting in a ‘neutral’ bilayer, between which the hydration force and not the electrostatic force can be considered the dominant repulsive force.^{9,17,37} For intermediate concentrations, both phases coexist, stabilized by the interplay of the two repulsive forces which differ in decay length^{9,17,37} and compete both with a strong attraction. The existence of such a miscibility region, also known for other systems,³⁷ has only been reported for dialkyldimethylammonium halides with bromide as the counter ion.^{17,28,30,31} One explanation is that chloride ions are more strongly hydrated compared to bromide, which decreases their binding affinity to the surface of the aggregates.^{10,17,22,38} An alternative explanation is the strong electrostatic coupling observed for bromide ions when in close proximity to bilayers:³⁹ for such small distances the counterions are assumed to be only influenced by the surface charge of the bilayer, and not by the electrostatic field of the other counterions; for long distances (the Poisson Boltzmann regime) their position is, to a large degree, influenced by the other counterions. For systems showing strong coupling, a separation between two phases with different distances between the ‘charged plates’ can be predicted.³⁹

When going from the L_α phase to the L'_α phase a sudden increase in head group area and concomitant decrease in bilayer thickness was observed, which both relax with increasing surfactant concentration.¹⁷ The critical point at which the two lamellar phases merge is around 75 °C (72 °C²¹) at 62.2 wt%.^{10,32}

At lower surfactant concentration (<3 wt%) (analogous to other dialkyldimethylammonium halide systems) a fully swollen lamellar phase coexists with a dilute liquid phase, often described as a vesicle phase, showing unilamellar vesicles at low concentration,^{24,40} and multilamellar vesicles with increasing surfactant concentration.^{10,24,41} However, there is ongoing

discussion regarding the equilibrium status of vesicles,^{42,43} even long-lived ones, due to the bending energy of the surfactant monolayers: thermodynamically bilayers should either be flat (for positive bending rigidity) or extremely curved to make very small vesicles (here rigidity is negative and higher order in the curvature expansion becomes necessary to restore stability). Below the CVC (critical vesicle concentration) of 0.002 wt% a monomer solution has been identified,²⁴ while in related systems small spherical or cylindrical micelles have been reported.^{30,31} For temperatures above 22 °C, a flow birefringent long-lived metastable sponge phase L_3 has also been observed instead of the equilibrium coexistence region.¹⁹

Commonly for dialkyldimethylammonium systems, the lamellar phase is limited at low temperature by the Krafft temperature T_c , below which the dilute liquid phase coexists with crystals or crystal hydrates.^{23,28,29,44,45} A large hysteresis is observed for the freezing of the lamellar phases due to the kinetic hindrance of the crystallization of the surfactant.^{30,31,46} This leads to the occurrence of metastable phases, which can be of liquid crystalline or crystalline character. In the case of vesicles, the occurrence of gel phases such as the L_β phase – a lamellar phase, in which the fluid character of the bilayers is highly decreased^{43,47} – have been frequently reported at low temperatures, which can require long equilibration times for the molecules to rearrange.^{8,27,48} The melting temperatures T_m of these gel phases often correspond to the Krafft temperature. For the DDAB vesicle system, this was confirmed and it was shown that a long-lived L_β phase can be formed by avoiding excessive overcooling (> 5 °C).^{24,26} In contrast to other dialkyl dimethylammonium halide systems, in DDAB an L_β phase has not only been reported for the vesicular solutions, but has been suggested for the bulk lamellar phases^{17,19,20} in the equilibrium phase diagram. The chain melting temperature T_m in the swollen lamellar phase¹⁹ coincides with that observed in vesicle solutions,^{8,10,24,26,27} while a slightly higher transition temperature of 24 °C has been reported in the case of the collapsed lamellar phase.³² The L_β lamellar phases were described as clear solutions, with spacings similar to L_α phases, obtained by SAXS.^{17,19}

The behaviour of the solid DDAB phase has been studied by DSC and X-ray diffraction.⁴⁹ The sample has been reported to degrade at 160 °C (the upper boundary of a DDAB phase diagram) below which it shows three phase transitions: (1) at 30 °C the monohydrate (or di-hydrate⁵⁰) undergoes polytetic



melting to the pure crystal, (2) at 58.6 °C there is a transition into a liquid crystalline phase, and (3) at 76.2 °C occurs a polymorphic transition within the liquid crystal phase.

Results and discussion

When we cooled aqueous solutions of DDAB in the range of $\phi_{\text{DDAB}} = 3\text{--}90\%$ below T_m (≤ 10 °C), the samples turned white (see Fig. 1 top right). These ‘white’ phases were stable up to around 15 °C, *i.e.* close to their reported chain melting (T_m) or Krafft (T_c) temperatures. The occurrence of a white phase is in contradiction with the description of the “optically clear” L_β phase,¹⁷ which has been suggested in this region in the latest reported broad equilibrium phase diagram.¹⁷ In order to assess the equilibrium nature and the properties of the ‘white’ phase, a range of experiments were conducted. As it is known that the low monomer solubility, and thus, low monomer exchange rates between aggregates reported for dialkyldimethylammonium halide systems will lead – especially for crystalline phases – to long equilibration times, the historical treatment of the samples is highly significant.¹⁰ Thus, the influence of sample history on the (kinetics of the) phase transitions was investigated in the second part of this study.⁵¹

DDAB powder ($T \geq 20$ °C)

The phase behaviour, especially of the pure DDAB sample, can be strongly influenced by impurities.^{29,30,52} Three impurities were expected to be found in the DDAB sample: (i) water, caused by the existence of crystal hydrates and/or by the high water affinity of the sample; (ii) DDAB analogues of slightly different chain lengths, which could not be removed by recrystallization, but could be confirmed absent by ESI-MS and NMR analysis of the samples (see the ESI,† Fig. S6 and S7); and (iii) degradation products caused by thermal decomposition of DDAB at higher temperatures.

Hydration state of the powder. A first estimation of the water content in the dry powder of DDAB could be obtained from the $^1\text{H-NMR}$ spectra (see the ESI,† Fig. S7) measured in dry acetonitrile (MeCN) (filled in a glove box). While water would be readily absorbed by the DDAB powder upon contact with the atmosphere, the water content for samples dried in the oven for a prolonged time, estimated from integrating the water peak at $\delta = 2.18$ ppm, was less than 1 H_2O molecule in 4 DDAB molecules. Furthermore, no water peak can be found in the ATR FTIR spectrum of the recrystallized sample (black line in Fig. 2a), confirming that indeed all water molecules can be removed from DDAB and a zero-hydrate, depicted as X, defines the high-concentration boundary at 100 wt% of the phase diagram at room temperature.

To investigate the appearance of additional stable crystal hydrates at room temperature, an 85 wt% solution (L'_α phase) – containing less than five water molecules per DDAB molecule – was observed during evaporation of its water content at room temperature (Fig. 2b). The water peaks could be fitted with two main broad Gaussians around 3370 cm^{-1} and 3475 cm^{-1}

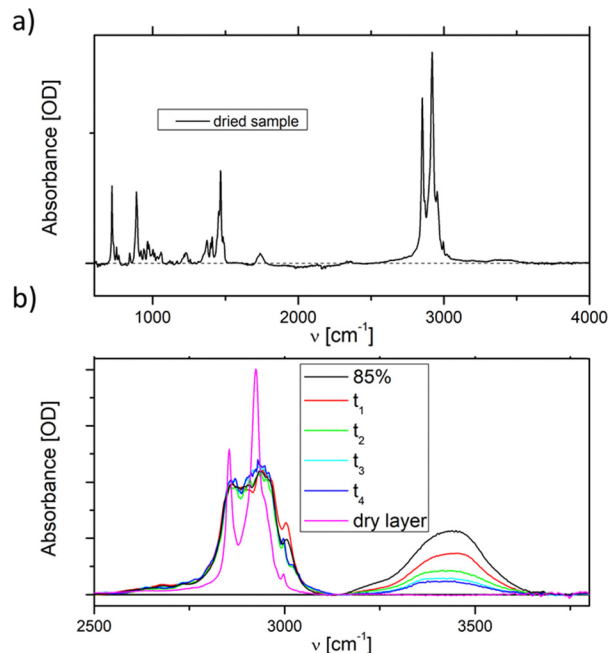


Fig. 2 Room temperature ATR FTIR spectra of (a) recrystallised dry DDAB samples and (b) during the evaporation of a condensed DDAB solution, showing a smooth decrease in water peak, until all water is evaporated.

corresponding to the symmetrical and asymmetrical stretching modes of water, respectively. During evaporation, a smooth decrease in peak intensity was observed, suggesting limited structural changes in the water. Thus, the results suggest that, in contrast to DODAB⁴⁵ and DODMAC,²⁹ which show distinct sharp peaks in the vibrational water spectrum, a zero-hydrate X is the stable and only crystalline form of DDAB at room temperature. Thus, the high affinity of water under atmospheric conditions would lead to the dissolution of the surface of some DDAB crystals, resulting in a coexistence region of X with the concentrated L'_α phase reported to start in the concentration range of 85–91 wt% (see above).

Conformational properties of DDAB

A stable Raman spectrum of the solid DDAB sample has been obtained (see Fig. 3 black lines and Table 2), in which the majority of peaks could be assigned, in agreement with the literature.³³ The spectrum indicates an all-trans extended chain structure: (i) the dominance of the symmetric C–H stretching vibrations (2880 cm^{-1}) over the asymmetric C–H stretching vibration (2850 cm^{-1}) indicates a high order in the hydrocarbon chains, and (ii) the 1060 cm^{-1} and 1130 cm^{-1} bands are characteristic of C–C stretching vibrations for the all-trans conformation of the chain.

Thermal stability of DDAB

At temperatures above $T \approx 90$ °C the white DDAB powder changes its colour to yellowish-brown (within the period of one week). This colour change is more apparent at higher temperatures and is frequently accompanied by a melting of the DDAB



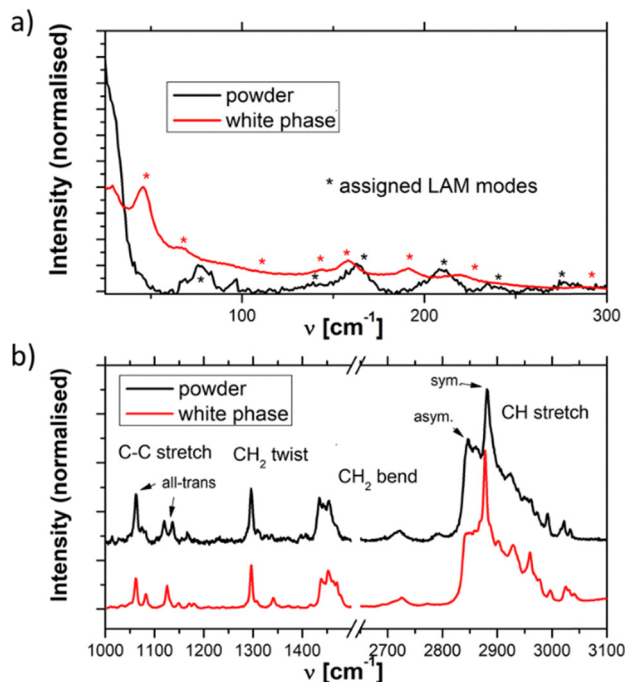


Fig. 3 Raman spectra of the DDAB powder (black line) and 'white' phase (red line) in the (a) low and (b) medium-high frequency range.

powder. The colour change is likely to be related to the degradation of the quaternary ammonium ion into the thermally stable amine,^{46,52} and subsequent N-oxidation of the amine (see the ESI,† Fig. S8). The degradation pathway of DDAB, expected to be caused by nucleophilic attack by the bromide ion,⁴⁶ was confirmed using TLC analysis of samples subjected to different temperatures and exposure times, as well as ¹H-NMR analysis of the degraded sample.

The melting of the coloured DDAB sample, rapid at temperatures of 150 °C (close to the previously assigned degradation temperature⁴⁹), can be assigned to the decomposition into the amine, which is in a liquid state at this temperature, making the use of melting point analysis for determining the purity of DDAB meaningless, similar to the case of related systems.^{30,31}

In summary, the DDAB sample used in this study could be shown to be of sufficient purity to allow the study of the phase behaviour of the binary DDAB water system at temperatures below the thermal degradation temperature of DDAB ($T_{\text{deg}} \approx 90$ °C). Furthermore, a zero-hydrate is the stable crystalline form of the DDAB powder at room temperature, in which the chains of the DDAB molecule are in an all-trans conformation.

Thermal phase transitions of aqueous DDAB solutions

The thermal properties of aqueous DDAB solutions, which were anticipated to be in either the swollen or collapsed lamellar phase at room temperature, were investigated by DSC in the temperature range between $T = -20$ °C and $+20$ °C. Two freezing and melting transitions were identified around 0 °C and 15 °C (Fig. 4a). The large hysteresis between the exothermic

Table 2 Raman bands of the purified DDAB powder at room temperature

ν [cm ⁻¹]	$\Delta\nu$ [cm ⁻¹]	Rel. height	Area (%)	Assignment
77	11	0.163	2	LAM mode
142	18	0.047	1	LAM mode
163	18	0.123	2	LAM mode ³³
209	12	0.122	2	LAM mode
237	15	0.032	0	LAM mode ³³
278	12	0.054	1	LAM mode ³³
417	19	0.073	1	LAM mode ³³
440	7	0.043	0	Unassigned ³³
465	4	0.073	0	Unassigned ³³
479	9	0.029	0	
521	11	0.019	0	Unassigned ³³
564	3	0.019	0	Unassigned ³³
725	10	0.062	1	CH ₃ rock from N ⁺ (CH ₃) ₂ group ³³
761	14	0.148	2	CH ₃ rock from N ⁺ (CH ₃) ₂ group ³³
879	10	0.092	1	
891	9	0.102	1	CH ₃ rock & CN ⁺ stretch ³³
918	3	0.021	0	CN ⁺ stretch ³³
943	10	0.020	0	Unassigned ³³
979	14	0.021	0	Unassigned ³³
1062	8	0.376	3	C-C sym stretch & CH ₂ wag. ³³
1120	8	0.139	1	Unassigned ³³
1136	6	0.140	1	C-C asym stretch & CH ₂ (<i>gauche</i>) wag. ³³
1167	5	0.055	0	CH ₂ rock ³³
1232	1	0.033	0	CH ₂ wag., crystal. & CH ₂ twist ³³
1296	8	0.403	3	CH ₂ twist ³³
1311	7	0.066	0	
1332	17	0.028	0	CH ₂ wag ³³
1403	14	0.026	0	
1434	10	0.303	3	CH ₂ bend ³³
1443	7	0.144	1	CH sym bend N ⁺ (CH ₃) ₂ group ³³
1454	15	0.291	4	CH ₂ bend & CH asym bend from N ⁺ (CH ₃) ₂ group ³³
1469	10	0.081	1	
2719	24	0.065	1	Unassigned ³³
2791	23	0.053	1	Unassigned ³³
2845	17	0.067	8	CH asym stretch of CH ₂ ³³
2862	19	0.572	10	CH asym stretch of CH ₂ ³³
2882	16	1	16	CH sym stretch of CH ₃ ³³
2900	23	0.417	11	
2924	27	0.408	10	CH sym stretch of N ⁺ (CH ₃) ₂ ³³
2950	18	0.265	4	
2962	9	0.232	2	CH asym stretch of N ⁺ (CH ₃) ₂ ³³
2974	9	0.193	1	
2992	6	0.144	1	Unassigned ³³
3021	12	0.132	2	

cooling and endothermic heating peaks indicates slow kinetics and the existence of stable supercooled phases over a broad temperature range. The reversible transition centred near 0 °C is assigned to the freezing and melting of the water in the samples based on the known temperature and enthalpy values for pure water, and its dependence on sample concentration. The second phase transition around 15 °C has been previously assigned to the $L_{\beta} \rightarrow L_{\alpha}$ phase transition,¹⁹ with the transition temperature corresponding to the chain melting temperature T_m . Due to the mismatch in optical properties (the L_{β} phase has been described as a clear phase, while the low temperature phase observed in this study is white (see Fig. 1)), and the detailed characterization of the white low temperature phase (see the Section "The low temperature phase"), this transition

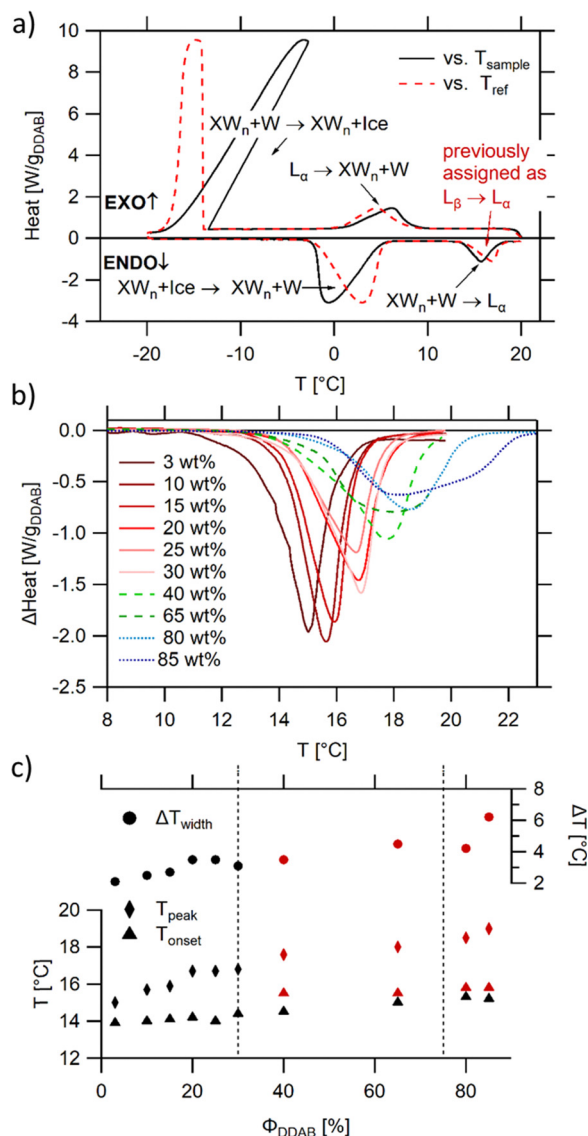


Fig. 4 DSC analysis of aqueous DDAB solution: (a) representative scan in the -20 °C to 20 °C temperature range showing two melting and two freezing transitions ($\Phi_{\text{DDAB}} = 25$ wt%) with the black and red lines displaying the data against the sample or reference temperature, respectively; (b) dependence of the peak assigned to the melting of hydrated DDAB crystals on DDAB concentration; (c) dependence on transition onset (determined using a line fit), peak temperature and peak width on DDAB concentration. For concentrations above 30 wt%, a broadening of the peak occurs (red markers), and the second onset displays the beginning of the underlying peak. The dashed lines indicate the phase boundaries between the swollen and collapsed lamellar phase at high temperature, as well as their coexistence region.

is here assigned to the melting of crystal hydrates in water $\text{XW}_n + \text{W} \rightarrow \text{L}_\alpha$. It should be noted that this is consistent with the measurements of the Krafft temperature²⁵ for dilute DDAB solutions performed by conductivity measurements. As is commonly observed for systems in which the monomer exchange between aggregates is slow,¹⁰ the degree of supercooling of the L_α phase before the start of the $\text{L}_\alpha \rightarrow \text{XW}_n + \text{W}$ transition as well as the transition kinetics depend strongly on the sample history

(see the ESI,† Fig. S8). This behaviour is common for a nucleation and growth process, where the amount of surviving nucleation centres often determines the kinetics (see also part II of this study⁵¹), and supports that a crystallization process occurs during this phase transition. Furthermore, the heat required for the $\text{XW}_n + \text{W} \rightarrow \text{L}_\alpha$ phase transition is proportional to the surfactant concentration, supporting its assignment to the DDAB molecules and not the water phase (see Fig. 4b). Over the whole concentration range, transition enthalpy values $\Delta H_{\text{DDAB}} = (38 \pm 0.5) \text{ kJ mol}^{-1}$ could be extracted. The kinetics of the melting transition have a non-cooperative character (characteristic for a non-isothermal phase transition) (see also part II of this study⁵¹).

The broadening of the peaks which is observed for concentrations above 30 wt% (samples in the $\text{L}_\alpha + \text{L}'_\alpha$ coexistence region or pure L'_α phase) can be either a result of several underlying transitions or the change in the melting pathway as proposed by the new phase diagram (which is a direct consequence of the rules of phase science for a eutectic phase transition – see below). For $\Phi_{\text{DDAB}} < 30$ wt% (but above 3 wt%) the melted crystals would form the L_α phase. In contrast, for $\Phi_{\text{DDAB}} > 75$ wt% the melting would first result in the formation of a small fraction of L_α phase. The remaining crystals would then melt into the L'_α phase. For samples in the intermediate concentration range, crystals would first melt with increasing temperature into the L_α phase, and then above a critical temperature transform into the L_α or L'_α phase at a ratio given by the phase boundaries. The later transformation has an isothermic characteristic, but would still appear broadened in DSC scans. The non-isothermic characteristic of the phase transition is further studied in part II of this study.⁵¹

Structural properties of the lamellar phases

As already mentioned, the lamellar phases have already been extensively studied in the past.^{19,20,53} For the sake of comparison, some of the reported measurements were repeated in order to directly assess the changes in structure and shape of the aggregates in the low temperature phase. The existence of the lamellar phase could be confirmed through its birefringent character when observed through crossed polarizers, except at very low concentration, when the birefringence was comparably weak, giving the sample the appearance of an isotropic solution. The concentration range of the swollen lamellar phase was therefore investigated using SAXS in the range of 5 – 25 wt%. This range was limited by the detector limit (Bragg peaks for concentrations below 5 wt% were covered by the beam stop), hampering the comparison of the onset of the lamellar phase with literature values. As expected, the observed Bragg peaks, and therefore the repeat distance in the lamellar phase $D^* = a_w + \delta$, where a_w is the water layer thickness and δ the bilayer thickness, depend on sample concentration (Fig. 5a). This dependence can be approximated using a simple geometrical dependence

$$a_w = \frac{\rho_{\text{DDAB}}(1 - \Phi_{\text{DDAB}})}{\rho_w \Phi_{\text{DDAB}}} \delta, \quad (2)$$



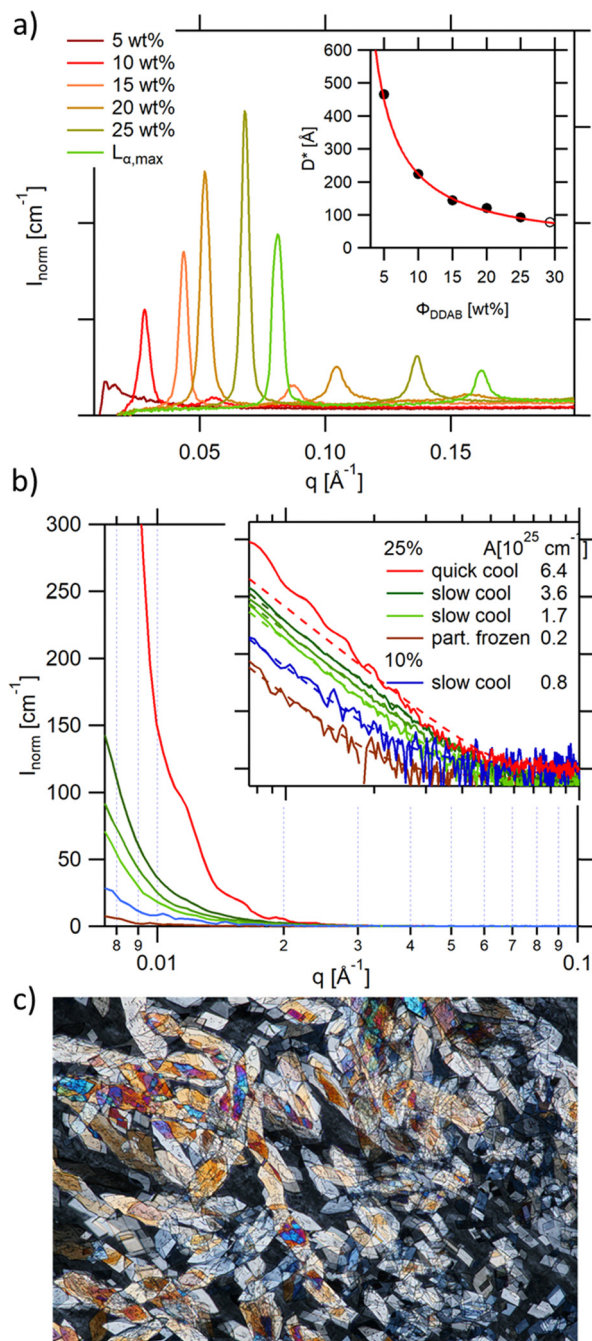


Fig. 5 (a) Bragg peaks seen in the SAXS spectra of aqueous DDAB solutions being in the L_α phase showing a decrease in repeating distance with increasing DDAB concentration (inset: the line shows the least squares fit to the data giving a bilayer thickness of $\delta = (22.4 \pm 0.4) \text{ \AA}$); (b) scattering intensity at small q values for a number of samples containing the 'white' phase. The q^{-4} behaviour can be explained by scattering of single crystals in the phase. The Guinier regime can only be resolved for comparably small crystals obtained with fast cooling rates (red trace), while in slower cooled samples only the Porod scattering can be observed. The scattering intensity changes with cooling rate, and decreases with decreasing DDAB concentration, as well as for partially frozen samples. The inset shows the log-log presentation of the data. The prefactor (given in the figure legend) of the q^{-4} dependence was obtained by fitting the data with eqn (4) (dashed lines); (c) DDAB crystals of the 'white' phase observed under crossed polarizers (image size $2.2 \times 1.5 \text{ mm}$).

(with $\rho_{\text{DDAB}} \approx \rho_{\text{w}}$) resulting in an estimated bilayer thickness of $\delta = (22.4 \pm 0.4) \text{ \AA}$, close to the literature value¹⁹ of $24 \text{ \AA}$ (Table 1).

The high concentration limit of the swollen lamellar phase L_α was estimated by phase separating a sample in the $L_\alpha + L'_\alpha$ coexistence region by centrifugation (3000 rpm, 8 h, 20°C), and measuring the repeating distance D^* of the dilute phase. The obtained value corresponded to a surfactant concentration of approximately $\Phi_{\text{DDAB}} = (29.5 \pm 0.5) \text{ wt}\%$, which is in good agreement with the literature value of 28%^{17,20} or 30%.^{9,36} Finally, it should be mentioned that the Bragg peak signal did not change within measurement error in the measured temperature range, even when the L_α phase was supercooled. It should be noted that the SAXS characterisation of the supercooled L_α phase, as well as its optically clear appearance, agree with the characterisation of the previously assigned equilibrium L_β phase,¹⁷ with the exception that no phase transition can be measured between the two phases by DSC, suggesting that during their study, the structural characterisation experiments were conducted on the non-equilibrium long-live supercooled L_α phase.

Conformational properties of the lamellar phases. The conformational properties of the lamellar phases were investigated using Raman spectroscopy (see the black line in Fig. 6a and b and Table 3). The results were found independent of time, scan number or historical treatment (*e.g.* freezing).

Furthermore, apart from predictable changes in the relative intensity of the DDAB to water peaks, no dependence on DDAB concentration or type of lamellar phase could be observed (see the ESI,† Fig. S10). The homogeneity of the spectra throughout the sample was confirmed using Raman microscopy. As expected, an increased *gauche* content in the hydrocarbon chains and thus an increased fluidity in the bilayers of the lamellar phase, compared to the powder sample, was observed as the appearance of a strong band at 1088 cm^{-1} in the C–C bending region of the spectrum,³³ as well as an increase in the ratio I_{2850}/I_{2880} of the asymmetric to the symmetric C–H stretching vibration. The more fluid character of the sample is also supported by the observed broadening of the vibrational bands and by the disappearance of the LAM frequencies in the spectrum. Interestingly, the Raman signal also showed no effect of the degree of supercooling of the lamellar phase in the peaks corresponding to the DDAB molecules, supporting the assignment as a supercooled L_α phase.

In contrast to the DDAB molecule, the structure of the water molecules is affected by the DDAB concentration and sample temperature, as evident in the changes in the shape of the water peak above 3000 cm^{-1} (see Fig. 6c left and the ESI,† Table S1). With increasing surfactant concentration, the vibration assigned to the asymmetric stretching mode of water molecules also increased, which is commonly associated with an increase in order of the water molecules.³⁴ When comparing to pure water solution even at low temperature, the relative intensity of the symmetric stretching mode compared to the asymmetric stretching mode is already low in dilute samples, but further dramatically reduces upon increasing DDAB concentration. Interestingly, the supercooled lamellar phase shows opposing behaviour, suggesting that

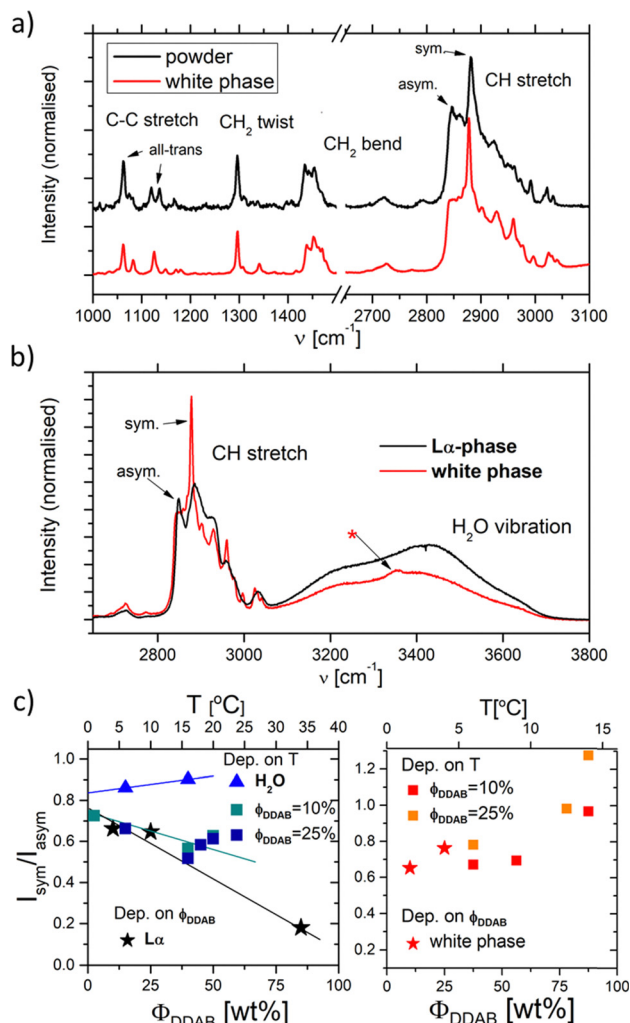


Fig. 6 (a) and (b) Raman spectra of aqueous DDAB solution in the lamellar phase (black) compared to the 'white' phase (red). (c) Ratio of the $I_{\text{sym}}/I_{\text{asym}}$ water peaks depending on DDAB concentration, phase and temperature (see also the ESI,† Table S1).

with the degree of supercooling, water in the lamellar phase exists with a more fluidlike characteristic.

Structural properties of the low temperature phase ('white' phase)

As already mentioned, if the aqueous DDAB solution is cooled sufficiently, a dramatic increase in turbidity is observed resulting in a whitish appearance (Fig. 1 top right). This whitening takes a long time (up to several months at temperatures close to the phase transition temperature, while only minutes at $T < 5^\circ\text{C}$). The white colour suggests microscopic phase coexistence due to scattering from the multiple phase boundaries. For thin samples (below 100 μm), transmission of light was sufficiently increased that crystals could be resolved under a microscope (Fig. 5c). Once a white sample is heated above the phase transition temperature, it returns to its original optically clear appearance.

For the white low temperature samples with surfactant concentration $\Phi_{\text{DDAB}} \leq 10$ wt% macroscopic phase separation

was observed (see the left photograph in Fig. 1) by sedimentation of the denser white phase, containing dispersed DDAB, from a clear liquid phase (indicated by a grey broken line in the proposed phase diagram in Fig. 1). This phase separation could be enhanced by centrifugation. The ratio of clear phase to white phase decreased with Φ_{DDAB} until, for higher surfactant concentrations, no phase separation was observed, even with prolonged centrifugation. No DDAB molecules could be identified in the clear liquid using analytical methods. Therefore, this phase was denoted as W. The exact position of the boundary in the phase diagram below which macroscopic phase separation could be observed was determined by removing the clear liquid phase from the sedimented white phase in phase separated samples. The samples were heated to room temperature to transform into their corresponding lamellar phase and their repeating distance was probed by SAXS. The measured repeating distance corresponded to a lamellar phase of $\Phi_{\text{DDAB}} = 10$ wt%.

The density of samples in the 'white' phase was measured, and the density corresponding to the DDAB molecules $\rho_{\text{DDAB,white}} = (1.1 \pm 0.2) \text{ kg dm}^{-3}$ extracted, a value about 15% higher than that of the lamellar phase of $\rho_{\text{DDAB,L}_\alpha} = (0.97 \pm 0.01) \text{ kg dm}^{-3}$, which is in good agreement with the reported literature value¹⁹ (Table 1). Therefore, the comparably high density of DDAB in the 'white' phase, compared to water, can explain the sedimentation behaviour discussed above.

The SAXS spectrum of the 'white' phase itself (Fig. 5b) does not show any series of Bragg peaks, which is incompatible with the existence of an L_β phase in this temperature range.¹⁹ In contrast, high forward scattering intensities at small q values ($q < 0.05 \text{ \AA}^{-1}$) and a decay following a q^{-4} envelope, characteristic for the hard-soft interface scattering of small single crystals in the sample are observed. In samples in which the freezing was performed comparably rapidly (resulting in comparably small crystallites) the signature of an incompletely resolved Guinier regime (with missing plateau) at around $q \sim 0.007 \text{ \AA}^{-1}$ *i.e.*

$$I(q) \sim \exp\left(-\left(\frac{(qR)^2}{5}\right)\right) \quad (3)$$

can be resolved (see Fig. 5b, red line). In this case, an effective radius of the crystalline scatterer R can be estimated for spheres (used also as a model for anisometric randomly oriented particles) from the first minimum of the spherical form factor that corresponds to $qR = 4.49$. For the sample in Fig. 5b (red line) this minimum appears around $q \sim 0.01 \text{ \AA}^{-1}$ suggesting $R \sim 0.04 \mu\text{m}$ which can be used to estimate the particles' surface-to-volume ratio $S/V = 3/R \sim 7 \times 10^5 \text{ cm}^{-1}$. Judging from the observed oscillatory behaviour, the particle distribution is relatively mono-dispersed. Furthermore, the q -dependence for $q > 0.02 \text{ \AA}^{-1}$ is a power law with exponent -4 suggesting a smooth, flat surface, with a surface fractal dimension of 2. More detailed information about the crystal shape cannot be obtained from the isotropic data.



Table 3 Raman bands of aqueous DDAB solutions in the L_α or L'_α phase at room temperature

ν [cm^{-1}]	$\Delta\nu$ [cm^{-1}]	Rel. Height	Area (%)	Assignment
772	34	0.040	2	CH_2 rock in $\text{CH}_2\text{-N}^+(\text{CH}_3)_2$ group ³³
840	19	0.024	2	
848	12	0.018	3	
872	16	0.035	4	
890	15	0.064	4	CH_3 rock & CN^+ stretch ³³
910	27	0.034	4	
928	16	0.027	4	
1066	32	0.136	3	C-C sym stretch & CH_2 wag. ³³
1084	14	0.096	8	
1127	19	0.039	8	
1301	18	0.207	5	
1321	52	0.076	8	C-C stretch (<i>gauche</i> conformation) ³³
1437	14	0.287	6	
1455	32	0.439	5	C-C asym stretch & CH_2 (<i>gauche</i>) wag. ³³
2849	17	0.897	6	CH_2 bend ³³
2880	45	1	6	
2910	52	0.656	7	CH_2 bend & CH asym bend from $\text{N}^+(\text{CH}_3)_2$ group ³³
2931	22	0.417	7	
2964	45	0.469	3	CH asym stretch of CH_2 ³³
3033	29	0.090	4	
3219	210	0.590	—	CH sym stretch of CH_3 ³³
3434	243	1	—	
3620	101	0.120	—	H_2O

The q^{-4} Porod scattering can also be seen for the other samples displayed in Fig. 5b (visible in the log-log presentation in the inset) in which the large crystal size prohibits a clear observation of the Guinier regime and can be used to estimate the surface-to-volume S/V independently using

$$I(q) = 2\pi(\Delta\rho_e)^2\Phi_{\text{crystal}}\frac{S}{V}q^{-4} \quad (4)$$

where $\Delta\rho_e$ is the difference in electronic scattering length density between the DDAB crystals and water and Φ_{crystal} is their volume fraction. The electronic scattering length density for the DDAB molecules (in the high density crystal at low temperatures of 0–14 °C) can be estimated to be $\rho_{e,\text{DDAB}} = 10.2 \times 10^{10} \text{ cm}^{-2}$ and that for water $\rho_{e,\text{H}_2\text{O}} = 9.5 \times 10^{10} \text{ cm}^{-2}$, giving $\Delta\rho_e = 0.7 \times 10^{10} \text{ cm}^{-2}$. Uncertainties are due to assumption about the mass densities. For the sample Fig. 5b (red line) the prefactor of the q^{-4} envelope estimated by fitting the data is about $6 \times 10^{25} \text{ cm}^{-5}$. Combining this result with that of the S/V parameter estimated from the Guinier regime, we obtain $\Phi_{\text{crystal}} = 0.3$. This value is close to the DDAB concentration of the original sample of 25 wt%, with all DDAB molecules and some water molecules (in the case of a non-zero hydrate) constituting the crystal volume. It should be noted that the low q and high q regime are consistently connected to the same particle geometry. For smaller S/V ratio, as would be the case for larger crystals, or smaller crystalline phase concentration (as would be the case for a partially frozen sample or smaller Φ_{DDAB}) a decrease in peak intensity can be expected, which could explain the variations of peak height between the samples. If we compare a range of prefactors which we obtained for the 25% sample through various cooling speeds and sample histories (and use $S/V = 3/R$ to estimate the radius of a sphere

from the S/V value), we obtain sizes in the 10s to 100s of nm. In general, one can say that the absence of Bragg peaks in the scattering spectrum of the 'white' phase and the strong scattering at low q values strongly supports that the low temperature phase is a phase of small crystals of a few tens to hundreds of nanometers radius in size, dispersed in water.

Conformational properties of the 'white' phase. A typical Raman spectrum of the 'white' low temperature phase is shown in Fig. 3 or Fig. 6 (red line) (see also Table 4). This spectrum does not change with DDAB concentration between 10 wt% and 25 wt% except for an improvement in the signal to noise ratio for $\Phi_{\text{DDAB}} = 25 \text{ wt\%}$. Decreasing the temperature does not change the peak positions or their shape, but decreases significantly the signal to noise ratio. The upper temperature limit of the pure Raman signal of the 'white' phase was found to be 14.1 °C. Furthermore, the Raman signal obtained by Raman microscopy in the C–H stretching, C–H bending and C–C twisting region was of sufficient quality to confirm the homogeneity within one sample, even after 90 min. A number of comparably sharp peaks also in the region of the LAM vibrations could be identified for the 'white' phase, indicating an increase in lattice vibrations in the sample, typical for crystalline phases. We note that the lattice vibrational modes (in all regions of the spectrum) clearly differ from those obtained for the powder (see Fig. 3a), suggesting a different crystalline structure in the low-temperature phase.

Preliminary powder X-ray diffraction measurements performed on the powder and the low temperature phase confirm the existence of at least two stable crystalline forms in the DDAB samples in the investigated temperature range (see the ESI,† Fig. S11). We were not able to grow suitable crystals for single-crystal XRD analysis. The distinct diffraction patterns



Table 4 Raman bands of the 'white' phase

ν [cm ⁻¹]	$\Delta\nu$ [cm ⁻¹]	Rel. height	Area (%)	Assignment
46	8	0.263	4	LAM mode
68	7	0.067	2	LAM mode
111	7	0.032	2	LAM mode
141	5	0.036	2	LAM mode
158	16	0.109	2	LAM mode ³³
190	11	0.079	2	LAM mode
241	14	0.019	2	LAM mode
288	18	0.009	2	LAM mode
372	13	0.030	2	LAM mode
391	10	0.021	1	LAM mode
415	15	0.024	2	LAM mode ³³
446	19	0.010	1	Unassigned ³³
469	12	0.021	2	Unassigned ³³
509	11	0.034	2	
523	4	0.008	2	Unassigned ³³
770	7	0.033	2	CH ₃ rock from N ⁺ (CH ₃) ₂ group ³³
845	8	0.054	0	CH ₃ rock from CH ₂ -NCH ₃ group ³³
885	6	0.048	2	
891	8	0.088	1	CH ₃ rock & CN ⁺ stretch ³³
1034	8	0.022	2	
1062	6	0.297	1	C-C sym stretch & CH ₂ wag. ³³
1083	7	0.140	0	C-C stretch (<i>gauche</i> conformation) ³³
1126	8	0.216	1	C-C asym stretch & CH ₂ (<i>gauche</i>) wag. ³³
1149	7	0.052	1	
1170	7	0.046	1	
1181	9	0.045	1	
1297	6	0.42	2	CH ₂ twist ³³
1308	8	0.056	1	
1341	8	0.089	1	
1438	8	0.204	2	CH ₂ bend ³³
1445	13	0.174	2	CH sym bend from N ⁺ (CH ₃) ₂ group ³³
1453	8	0.263	2	CH ₂ bend & CH asym bend from N ⁺ (CH ₃) ₂ group ³³
1461	9	0.199	2	
1470	9	0.195	2	
2842	13	0.551	2	CH asym stretch of CH ₂ ³³
2853	15	0.463	2	CH asym stretch of CH ₂ ³³
2863	14	0.474	2	CH asym stretch of CH ₂ ³³
2871	8	0.399	2	
2877	6	1	3	CH sym stretch of CH ₃ ³³
2886	18	0.646	2	CH sym stretch of CH ₃ ³³
2903	17	0.413	2	
2917	19	0.252	2	
2930	17	0.354	2	
2943	31	0.213	2	
2960	5	0.119	2	
2961	16	0.277	2	CH asym stretch of N ⁺ (CH ₃) ₂ ³³
2976	15	0.181	1	
2997	9	0.105	2	Unassigned ³³
3026	12	0.146	2	
3041	14	0.063	2	
3250	260	1.004	—	H ₂ O sym stretch ³⁴
3356	71	0.268	—	H ₂ O
3445	188	1	—	H ₂ O asym stretch ³⁴
3596	122	0.258	—	H ₂ O

suggest the existence of one or several stable crystal hydrates at low temperature and/or conformational changes of the DDAB molecule compared to the zero-hydrate crystal.

In order to correlate the changes in the Raman spectra with conformational changes in the DDAB molecule, single molecule calculations have been carried out. The appearance of the band at around 1082 cm⁻¹ in the low temperature crystalline phase, suggests a distinct *gauche* conformation in the DDAB chain,³³ however less pronounced than in the lamellar phase (Fig. 6, red line), which is also supported from the reduced ratio

of the I_{2850}/I_{2880} modes. Raman frequencies were calculated for several DDA+ conformations, which differ in the *gauche* content of the chains. The Raman spectrum of the most stable DDA+ configuration featuring all-trans chains (upper left corner in Fig. 7) differs remarkably, especially in the region of the C-H stretching modes, from the experimentally obtained spectra of both the powder and the 'white' phase. This is reasonable, because calculations were performed on isolated molecules in the gas phase, which neglect the effects of packing in solid and lamellar structures. However, the following trends can still be



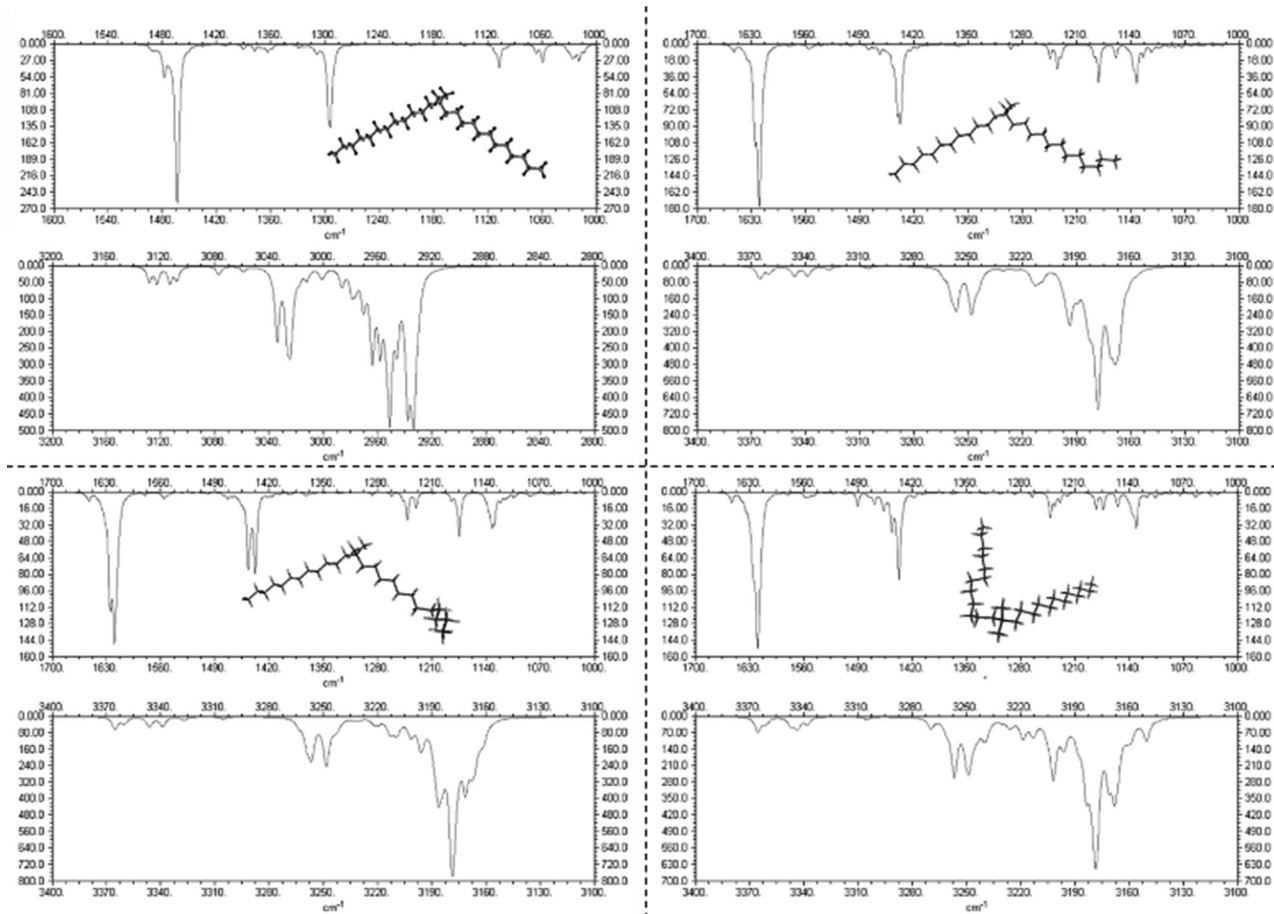


Fig. 7 Calculated Raman spectra of DDA⁺ conformations differing in the position of *gauche* kinks in the hydrocarbon chain. The most stable conformation (all-trans) is shown in the top left corner.

deduced from these calculations: (i) the introduction of *gauche* kinks in the chain influences the ratio of the peaks $I_{\text{CHsym}}/I_{\text{CHasym}}$; (ii) *gauche* kinks at positions closer to the head group lead to a peak shape similar to the peaks in the powder or the 'white' phase, whilst kinks towards the end seem to be rather characteristic of the L_α phase; (iii) the structure of the three bands between 1000 cm^{-1} and 1150 cm^{-1} support such an assignment, with the middle peak likely corresponding to the experimental peak at 1080 cm^{-1} which does not vanish for the all-trans conformation of the alkyl chain, but decreases with positioning of the *gauche* kinks closer to the head group (Fig. 7). It should also be noted, that the conformation of DDAB molecules with a kink close to the head group is similar to the crystal structure obtained for its slightly longer analogues DODAB⁴⁵ and DODMAC.⁴³

It should also be noted, that the water peak in the 'white' phase is distinct from that in the L_α phase (see the red line in Fig. 6b). An additional sharp peak around 3350 cm^{-1} could be identified which increases with decreasing temperatures. This peak might suggest the existence of a crystal hydrate, as sharp water bands are characteristic for bound water molecules. Furthermore, in contrast to the lamellar phase, an increase in the surfactant concentration or temperature leads to an

increase of the ratio $I_{\text{sym}}/I_{\text{asym}}$ water stretch (Fig. 6c right). This suggests that the disorder in the water phase increases with increasing temperature (as expected for pure water), but also with increasing surfactant concentration. This also offers support for the observation that dense phases cannot be separated by sedimentation or centrifugation.

In summary, all the performed characterizations of the low temperature phase suggest that the equilibrium phase is a coexistence phase of a crystal hydrate with a very dilute liquid phase $\text{XW}_n + \text{W}$. Further study of the temperature dependence of the structure at low water concentration, ensuring sufficiently long equilibration times, is necessary to obtain greater insight into the hydration state of the low-temperature crystals and its transformation temperature into the zero-hydrate form. In summary, all the performed characterizations of the low temperature phase suggest that the equilibrium phase is a coexistence phase of a crystal hydrate with a very dilute liquid phase $\text{XW}_n + \text{W}$. A further study of the temperature dependence of the structure at low water concentration, ensuring sufficiently long equilibration times, is necessary to obtain greater insight into the hydration state of the low-temperature crystals and its transformation temperature into the zero-hydrate form.



The proposed new phase diagram

Combining the results obtained in this study with information in the literature, a modified broad phase diagram for the low temperature region of the aqueous DDAB system is proposed (see Fig. 1). The previously suggested L_β phase is replaced by a coexistence region of a crystalline phase XW_n and a very dilute (near pure water) monomer solution W, which we draw at $\Phi_{\text{DDAB}} = 0\%$. This is consistent with the phase transition for W to Ice seen at 0°C , and the invariance in XW_n composition in the low temperature range. The hydration state of the crystal hydrate phase at low temperatures could not be resolved, which would fix the position of the vertical line separating the W + XW_n and XW_n regions at high DDAB concentration. However, the crystalline form differs in structure from the zero-hydrate, depicted as X_P , found in the DDAB powder at room temperature. Furthermore, the occurrence of a distinct and sharp water peak in the Raman spectrum suggests the formation of a hydrate rather than a polymorph of the zero-hydrate. The accurate transition temperature between the two crystalline phases as well as the number and character of intermediate crystal structures still has to be determined, and, therefore, this part of the phase diagram is represented with broken lines.

At higher temperatures, and compositions below 85 wt%, the phase diagram is consistent with the phase diagram reported in the literature. Two lamellar phases can be found, the swollen L_α phase and the collapsed L'_α phase, which coexist over a broad temperature and concentration range. Based on the rules of phase science, both the L_α phase and the L'_α phase, need to have at their lower temperature limits a eutectic discontinuity.^{43,52,54} The eutectic discontinuity of the L'_α phase could, in general, lay above or below the eutectic of the L_α phase. Both versions have been reported for other systems.⁵⁵ The observed results, however, suggest that there is a region in the phase diagram in which the L_α phase coexists with the crystalline phase (see also part II of this study⁵¹). Therefore, it can be assumed that the eutectic limiting the L_α phase corresponds to the Krafft eutectic, whilst the lower limit of the L'_α phase can be found at higher temperatures, which is also in agreement with our DSC data as well as the previously reported transition temperature of 24°C for the L'_α phase.³⁶ The exact position of the discontinuity limiting the collapsed L'_α phase can, however, not be determined from the performed experiments. Furthermore, the thermal stability limit of DDAB is close to 90°C , which is therefore the upper limit of the phase diagram.

Conclusions

A detailed study of the equilibrium phase behaviour of the binary DDAB/water system has been presented. The samples used in this study were shown to be of sufficient purity such that the reported properties did not change with additional purification. The obtained results, based on a range of experimental techniques, characterizing the samples at different length scales, could not be explained within the frame of the

latest reported broad equilibrium phase diagram.¹⁷ The low temperature phase, which was previously suggested to be an L_β phase, was replaced by a coexistence region of a crystal hydrate phase XW_n and a dilute monomer solution W. This phase differs not only in optical properties (being white in contrast to the clear L_β phase), but also its crystalline character could be confirmed by Raman spectroscopy, small and wide angle X-ray scattering and microscopy. Our results suggest that the previously proposed L_β phase for concentrations above 3 wt% is likely to correspond to the non-equilibrium supercooled L_α phase. Our results do not disagree with the characterization and report of the L_β phase in the dilute vesicle system, which has already been reported as a long-lived non-equilibrium phase only obtained when the formation of crystals is avoided by limited overcooling below T_c .^{24,26} A detailed study of the thermal phase transition involving the crystal/water coexistence region and the L_α phase is presented in part II of this study,⁵¹ elucidating the exact position of the boundary between the L_α phase and its coexistence with the crystals. In future, a detailed study of the high concentration region is needed in order to obtain the exact position of the lower temperature limit of the collapsed L'_α phase as well as the hydration state and thermal stability limit of the crystalline phase found at low temperatures.

Data availability

The data supporting this article have been included as part of the ESI.†

Conflicts of interest

There are no conflicts to declare.

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