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Resonant doping for high mobility transparent conductors: the case of Mo-doped In_2O_3 [†]

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Transparent conductors are a vital component of smartphones, touch-enabled displays, low emissivity windows and thin film photovoltaics. Tin-doped In_2O_3 (ITO) dominates the transparent conductive films market, accounting for the majority of the current multi-billion dollar annual global sales. Due to the high cost of indium, however, alternatives to ITO have been sought but have inferior properties. Here we demonstrate that molybdenum-doped In_2O_3 (IMO) has higher mobility and therefore higher conductivity than ITO with the same carrier density. This also results in IMO having increased infrared transparency compared to ITO of the same conductivity. These properties enable current performance to be achieved using thinner films, reducing the amount of indium required and raw material costs by half. The enhanced doping behavior arises from Mo 4d donor states being resonant high in the conduction band and negligibly perturbing the host conduction band minimum, in contrast to the adverse perturbation caused by Sn 5s dopant states. This new understanding will enable better and cheaper TCOs based on both In_2O_3 and other metal oxides.

New concepts

A major challenge for research on transparent conducting oxides (TCOs) is to overcome the inherent limitations of the compromise between transparency and conductivity. Traditionally, n-type doping has used the element one to the right in the periodic table of the host cation or anion. In this work, we show that for the high carrier densities needed for TCOs, conventional dopants, such as tin in indium tin oxide (ITO), hybridize with the host conduction band states, increasing the band curvature and the band-edge effective mass and reducing the mobility. Particular transition metal dopants have long been known to result in higher electron mobilities, but the mechanism for this has not been clearly elucidated. Using the example of molybdenum doping of indium oxide, we show that the appropriate choice of transition metal dopant gives a d state donor level that is resonant with the conduction band, thereby avoiding the detrimental effects of donor states mixing with the CBM. Moreover, as well as giving computational and spectroscopic evidence of the resonant doping phenomena, the enhanced doping behaviour is rationalised by invoking crystal field theory for the Mo 4d dopant states and emphasizing the role of the positive charge state of the dopant ion that has previously been overlooked. This new understanding paves the way for the realization of high performance TCOs.

Introduction

Transparent conducting oxides (TCO) combine the usually mutually exclusive properties of electrical conductivity and

optical transparency, making their use ubiquitous in consumer electronics and glass coatings.^{1,7} The global TCO market is predicted to have an annual growth rate exceeding 17%, reaching \$8.04 billion by 2022.⁸ The demand for higher conductivities and the volatile and high price of indium has led to the search for new TCO materials. However, as shown in Fig. 1, alternative indium-free TCOs such as graphene, carbon nanotubes and oxide/metal/oxide layers have failed to surpass or even reach ITO's performance;^{1,9,10} ITO continues to account for 60% of the transparent conductor market and 60% of global indium use.

Given this failure of the alternative transparent conductors, it is remarkable that In_2O_3 doped instead with molybdenum, giving double the conductivity of ITO, has not been adopted by industry in spite of first being suggested over 15 years ago. Reports of Mo-doped In_2O_3 have been sporadic and have contained little insight into the origins of its superior performance.

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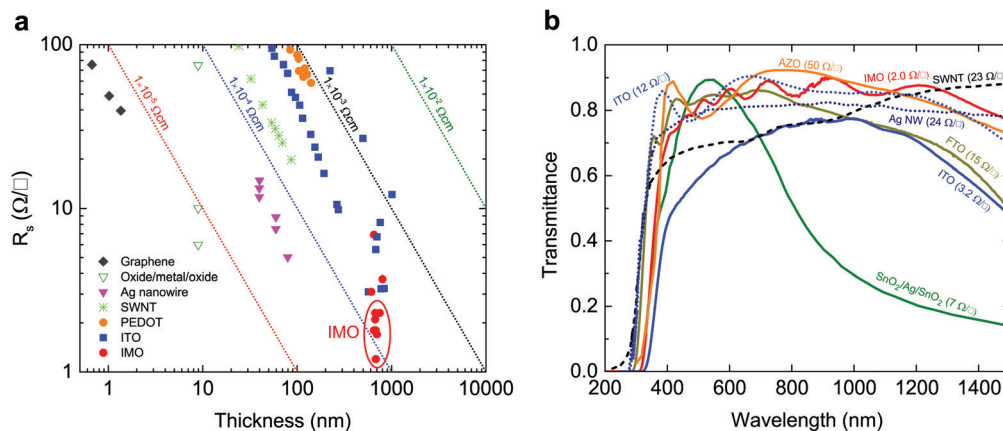


Fig. 1 Sheet resistances and optical transmittances of transport conducting electrodes. (a) Sheet resistance R_s as a function of film thickness for different transparent conducting films:¹ PEDOT-PSS;² ITO films;^{3,4} SWNTs;³ Ag nanogrid;³ oxide/Ag/oxide films;⁵ and graphene.³ This figure is based on Ellmer's¹ with data points for IMO added and highlighted by the red ellipse. The IMO films have the lowest sheet resistances. The dotted diagonal lines denote constant resistivity values. (b) Spectral transmission of different transparent electrode films: single walled carbon nanotubes (SWNT) (23 $\Omega/\square$), Ag nanowires (24 $\Omega/\square$), aluminium-doped ZnO (AZO, 50 $\Omega/\square$), ITO (12 $\Omega/\square$),⁵ $\text{SnO}_2/\text{Ag}/\text{SnO}_2$ (7 $\Omega/\square$),⁶ compared with our measurements of IMO (2 $\Omega/\square$), ITO (3.2 $\Omega/\square$), and fluorine-doped SnO_2 (FTO, 15 $\Omega/\square$). All materials which approach IMO's sheet resistance have much inferior infrared transparency.

In fact, reports of IMO showing promising performance seem to have been treated merely as a curiosity, and thus IMO was never identified as a research direction deserving of further detailed investigation. Perhaps this lack of research and dearth of understanding has prevented industry overcoming its inertia to substitute an established high performing material for a significantly better one. Here we present a comprehensive explanation of why IMO outperforms ITO. This work opens the pathway for immediate commercial adoption of IMO, and for the development of other high performing TCOs.

Results

Mo universally delivers higher conductivity than Sn in In_2O_3

Comparing Mo and Sn dopants in In_2O_3 (Fig. 2), we find that higher mobilities and lower resistivities are universally

obtained with Mo. Fig. 2, which shows the Van der Pauw resistivity and mobility as a function of carrier concentration, includes data from our chemical vapour-deposited films as well as those from other studies of IMO and ITO. X-ray diffraction (Fig. S1a, ESI[†]) confirmed the cubic bixbyte structure of the films. Film thickness varied from 670–800 nm for IMO and 700–1600 nm for ITO as determined by cross-sectional scanning electron microscopy (Fig. S1b, ESI[†]). Calibrated secondary ion mass spectrometry (Fig. S2, ESI[†]) indicates that the dopant concentrations are the same as the free electron densities, implying that within the uncertainty there is one free electron per Mo atom in IMO and Sn atom in ITO. For IMO, a resistivity as low as $0.8 \times 10^{-4} \Omega \text{ cm}$ has been achieved, almost half of the $1.4 \times 10^{-4} \Omega \text{ cm}$ for ITO. This is enabled by IMO's extremely high mobilities displayed in Fig. 1b. Mo clearly outperforms Sn as a dopant, with IMO films having mobilities

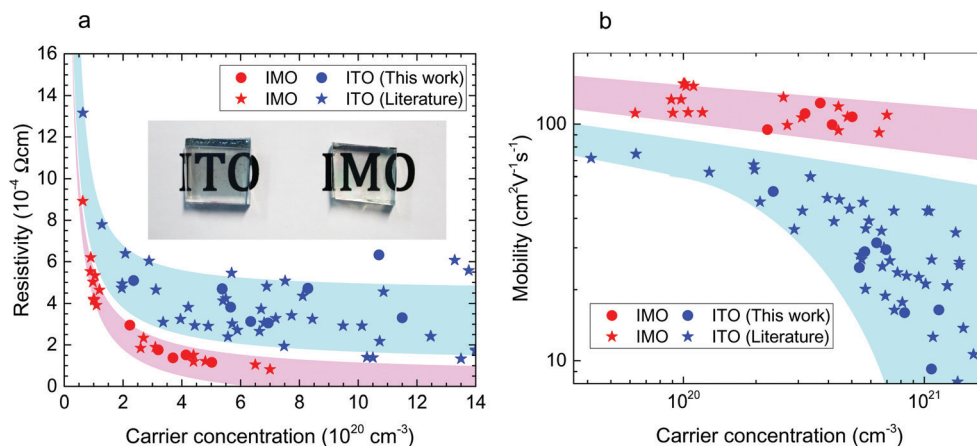


Fig. 2 Transport properties. (a) Resistivity versus free carrier concentration for polycrystalline ITO and IMO films. Inset shows a photograph of ITO and IMO films. (b) Hall mobility versus free carrier concentration. Data from this work are circles. Data plotted as stars are taken from the literature for IMO^{11–16} and ITO^{12,17–22} films. In this carrier concentration regime, the electron mobility is limited by ionized impurity scattering.



of up to $150 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ compared with the $80 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ for ITO. Table S1, ESI† provides further details of electronic and optical properties. From all available results, a trend of twice the conductivity for IMO over ITO of the same carrier concentration is apparent. Therefore only half the amount of indium is required for IMO films with both better optical properties and improved conductivity over ITO, giving potentially huge savings in materials and costs.

Conventional dopants impair mobility due to state mixing with host CBM

The main factor that limits the properties of TCOs is the trade-off between doping for increased conductivity and consequential decrease in optical transparency due to band tailing and the raised conduction electron plasma energy. Optical transmission spectra of IMO and ITO (Fig. 3a) show that IMO generally has greater transmission at 550 nm (2.25 eV), where the human eye is most sensitive (see also Table S1, ESI†). Optical absorption spectra of IMO and ITO (Fig. S3, ESI†) show similar optical band gaps (*via* the method of Dolgonos *et al.*²³), yet the conduction electron plasma edge from infrared reflectivity lies at strikingly lower energies in IMO, greatly enhancing transparency (see also Fig. 3a). Plasma frequency relates to carrier density and effective mass as $\omega_p^2 \propto n/\langle m^* \rangle$ and so these data indicate an inherent difference in the effective masses of conduction electrons between In_2O_3 doped with Sn and Mo, diverging from the commonly accepted rigid band model of doping.

The red-shifted IMO plasma edges are understood after plotting optical gap *versus* plasma energy in Fig. 3b. Both the IMO and ITO optical gaps increase monotonically with plasma energy due to band filling; however, the steeper IMO curve indicates a desirably reduced electron effective mass (a similar dependence holds between optical gap and carrier density in

Fig. S4a, ESI†). This effect is modelled in Fig. 3b using carrier statistics (as described in the ESI†). The conduction band minimum (CBM) or band edge effective mass used is $0.22m_e$ as determined previously from angle resolved photoemission and density functional theory (DFT) calculations.^{24–26} Modelling of the ITO data required a deviation from the rigid band model by increasing the band edge effective mass incrementally with Sn-content from $0.22m_e$ to $0.40m_e$ (in excellent agreement with previous theoretical predictions ref. 25). The carrier density-dependence of the effective mass for IMO and ITO is shown in Fig. S4b, ESI†. The correspondingly different conduction band dispersions in heavily doped IMO and ITO are shown schematically in Fig. 3c. The increasing band edge effective mass in ITO is consistent with the additional decrease in mobility as carrier concentration increases as seen in Fig. 2b and modelled in Fig. S3c, ESI†. In contrast to ITO, the IMO data in Fig. 3b is well reproduced using a fixed band edge effective mass of $0.22m_e$ for all Mo concentrations.

Mo dopant states lie at favourable energies in In_2O_3

The undoped In_2O_3 and IMO band structures calculated using density functional theory (DFT) using 80 atom unit cells are shown in Fig. 4a and b. For IMO, one indium atom is replaced by one Mo atom, corresponding to a Mo concentration of 3.125% of the cations. Mo 4d levels in IMO are energetically separated from the CBM and do not mix readily with the In 5s-O 2p-dominated CBM. The Mo 4d levels can be seen as mid-gap states and as a donor state resonant in the conduction band in the calculated band structure (Fig. 4b). Mo states mix minimally with those of the In_2O_3 CBM; in contrast Sn states strongly perturb the CBM. This is supported by Fig. 4c–f, which depict the DFT-calculated partial charge densities. At the CBM, whilst the IMO electron density is delocalised across the lattice, minimal density exists near the Mo (green) atom (Fig. 4d);

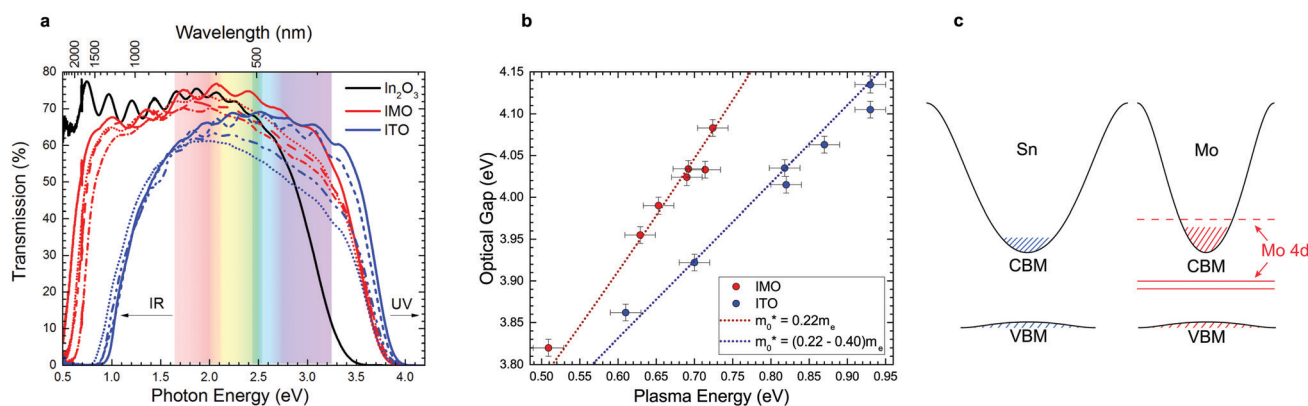


Fig. 3 Optical transmission and associated properties. (a) Optical transmission of IMO and ITO films (on 3.6 mm-thick soda lime glass) with a range of carrier concentrations, and a nominally undoped In_2O_3 film, revealing greatly enhanced transparency in IMO due to plasma edges lying at lower energies. (b) Optical gap *versus* plasma edge energy of IMO and ITO films, the steeper gradient for IMO indicates a (highly desirable) reduced conduction band minimum effective mass with respect to that of ITO. Model curve lines are calculated using Fermi statistics with a density-of-states averaged effective mass. (c) Schematic representation of the band structure of ITO (left) and IMO (right) with the same carrier concentration. The IMO has a narrower conduction band dispersion with lower band edge effective mass than ITO and so a higher Fermi level is required to obtain the same number of states as in ITO. In IMO, the resonant and midgap Mo 4d bands are shown, respectively, by the dashed and solid red lines. No Sn state is shown in the ITO band structure schematic as the Sn 5s states mix with the states of the conduction band.



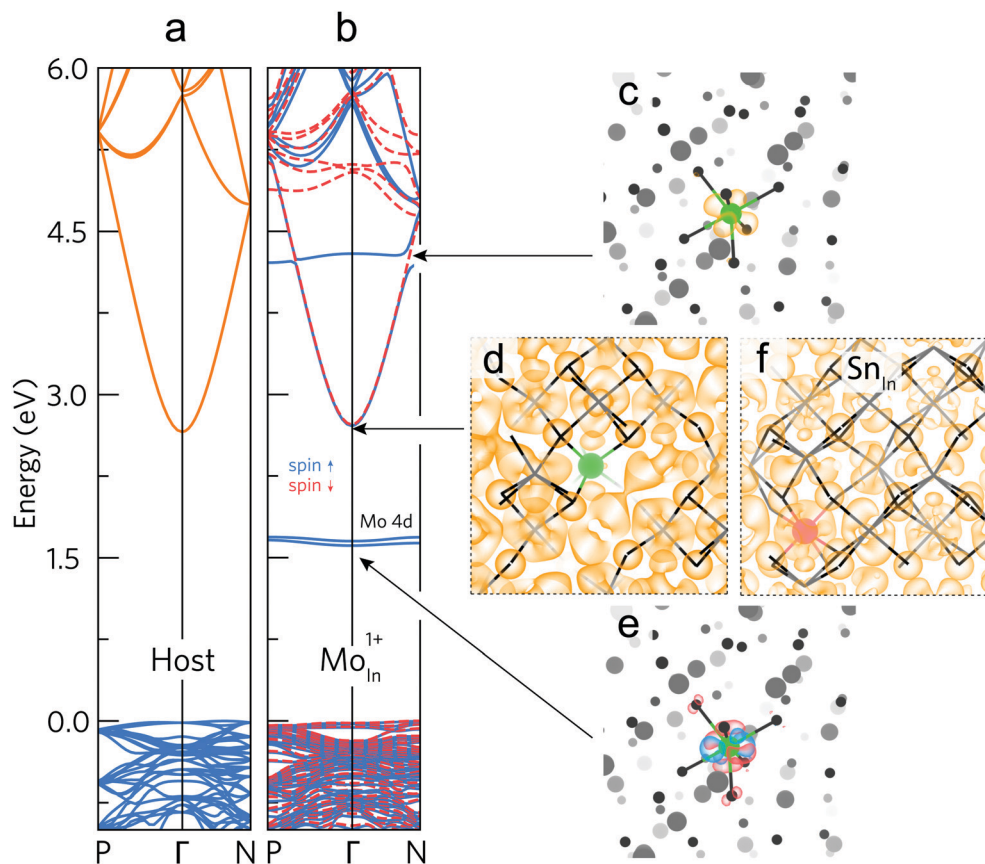


Fig. 4 Band structures and partial charge densities. (a) and (b) Band structures for undoped In_2O_3 and for IMO, including both spin components, with the Mo donor in the ionized $1+$ charge state. The zero of the energy scale is the VBM. (c)–(e) show the partial charge densities for IMO corresponding to the resonant state in the conduction band, at the CBM and for the two states in the band gap respectively. (f) The partial charge density at the CBM is also shown for ITO. The $\text{Mo}_{\text{In}}^{24\text{d}}$ atom is green, the $\text{Sn}_{\text{In}}^{8\text{b}}$ atom is red and the In_2O_3 lattice is portrayed using a wireframe. For the resonant state and the midgap states, the O and In atoms are shown by black and grey spheres and the 'bonds' on the In_2O_3 lattice are removed in order to clearly visualise the MoO_6 distorted octahedra.

in contrast, considerable density exists across the ITO lattice, including around the Sn (red) atom (Fig. 4f). The Sn 5s states hybridize with the In 5s/O 2p character CBM.

The Mo 4d states are depicted schematically in Fig. 5a and are observed in the photoemission and inverse photoemission spectra shown in Fig. 5b. Conduction band photoemission shown in Fig. 5c directly evidences the different conduction band dispersion for IMO and ITO discussed above. (See also Fig. S5, ESI† and associated descriptions of additional photoemission and X-ray absorption data.) While the midgap states might be thought to impair transparency, this is shown not to be the case from the transmission data in Fig. 3. This is because optical transitions to and from the midgap Mo 4d states have only minimal dipole intensity.

Why Mo 4d states are at favourable energies

To explain why Mo in In_2O_3 has two occupied 4d states within the band gap and one donor state resonant with the conduction band, we consider the electronic structure and crystal field environment of Mo in In_2O_3 . Mo and Sn have respective electron configurations of $[\text{Kr}]4\text{d}^55\text{s}^1$ and $[\text{Kr}]4\text{d}^{10}5\text{s}^25\text{p}^2$, while bixbyite cubic In_2O_3 has two distinct indium sites: the 8b and

24d Wyckoff sites, with respective regular and tetragonally-distorted octahedral crystal environments. At an indium site, three electrons participate in bonding, leaving Sn or Mo respectively in a $[\text{Kr}]4\text{d}^{10}5\text{s}^1$ or $[\text{Kr}]4\text{d}^3$ configuration, that is one Sn 5s or three Mo 4d as the outermost electrons. At Fermi levels matching experiments (around VBM + 3.3 eV) Sn or Mo preferentially substitute on the respective 8b or 24d sites (each donating one conduction electron), whilst $\text{Mo}_{\text{In}}^{8\text{b}}$ has a neutral charge state (donating no carriers), see Fig. S6, ESI†. The Jahn–Teller-like distortion at the 24d site splits the three-fold degenerate t_{2g} levels (valid for octahedral symmetry), shifting the d_{xy} orbital up in energy to the vicinity of the CBM, and d_{xz} and d_{yz} down into the gap, as shown in the unfolded band structures for the neutral charge state ($\text{Mo}_{\text{In}}^{24\text{d}} q = 0$) in Fig. S7, ESI†. If all Mo 4d states lie below the CBM (as reported elsewhere from calculations),²⁷ then no effective doping would occur at room temperature; the experimental results shown in Fig. 2 clearly rule this out. If the highest occupied Mo 4d state lies just above the CBM (reported elsewhere),¹² it would merge with the occupied CBM, increasing the electron effective mass and reducing mobility, and the Fermi level would be pinned by the partially occupied 4d state.



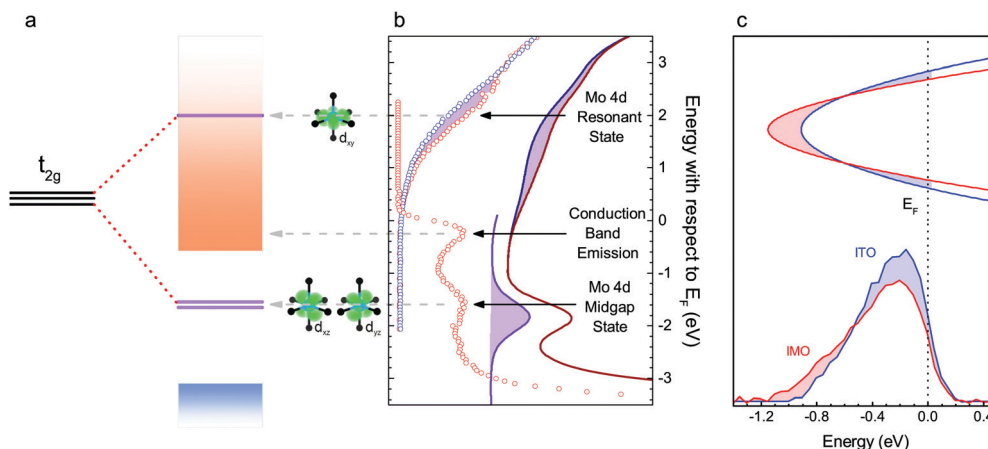


Fig. 5 Spectroscopy of electronic structure. (a) Schematic diagram of Mo 4d t_{2g} states and their corresponding orbitals (depicted in green), splitting into the upper state, d_{xy} , resonant with the conduction band (orange shading), the two lower states, d_{xz} and d_{yz} , in the band gap and the valence band (blue shading). The splitting resulting from tetrahedral elongation Jahn–Teller distortion of the MoO_6 octahedron is shown for comparison with the highly distorted $\text{Mo}_{\text{In}}^{24\text{d}}$ depicted in Fig. 4. (b) Inverse photoemission data from ITO (blue) and IMO (red), showing extra intensity in the IMO data, corresponding to an unoccupied Mo 4d state resonant with the conduction band. Also shown is high energy photoemission data of the conduction band emission, Mo 4d midgap states and valence band onset of IMO. The features in part (a) of the figure are aligned to the corresponding peaks in the spectra. (c) Schematic band diagram, showing wavevector (vertical axis) versus energy (horizontal axis) representing the conduction bands of similarly doped IMO (red) and ITO (blue) aligned to the Fermi level. Below are background subtracted HAXPES spectra displaying conduction band emission from IMO (red, $n = 5.0 \times 10^{20} \text{ cm}^{-3}$) and ITO (blue, $n = 6.3 \times 10^{20} \text{ cm}^{-3}$). The spectra are normalised to the In 5s-dominated valence band peak at -9 eV . The shaded regions emphasise the additional intensity of the ITO peak and additional width of the IMO peak.

Both previous works fail to consider Mo atoms in a +1 charge state,^{12,27} which increases the distortion of the octahedra and the splitting of the t_{2g} -derived 4d energy levels, making the d_{xy} orbital resonant with the conduction band. This contributes a conduction electron without detrimental hybridization with the CBM states; whilst the singly-occupied d_{xz} and d_{yz} orbitals are stabilized by the bond length contraction and pushed deeper into the band gap (see $\text{Mo}_{\text{In}}^{24\text{d}}$ $q = +1$ in Fig. S7, ESI†). A schematic representation of this t_{2g} level splitting is shown in Fig. 5a along with partial electron densities for the d_{xy} , d_{xz} , and d_{yz} orbitals (full schematic molecular orbital diagrams for MoO_6 octahedra are shown in Fig. S8, ESI†). Indeed, the calculated partial electron charge densities around the Mo atom at the resonant Mo level (Fig. 4c) and two mid-gap levels (Fig. 4e) show clear similarities respectively to the schematic d_{xy} , and a combination of the d_{xz} and d_{yz} orbitals of Fig. 5a. This picture of the Mo 4d state energies in IMO is further corroborated by additional confidence in the calculated results coming from comparisons of the bond lengths from calculations and those determined from extended X-ray absorption fine structure measurements (see Fig. S9, ESI† and related discussion).

IMO is as durable as ITO

The durability of our CVD IMO films has been compared to that of both our CVD ITO films and commercial ITO films. This was done by measuring the sheet resistance and transmission before and after tape, scratch, heat and acid tests, as shown in Fig. S10, ESI†. IMO films were found to be as durable as the ITO films.

Design criteria established for high mobility TCOs

Beyond having a transformative impact by replacing the ubiquitous ITO with better and cheaper IMO, this work enables design

criteria for other high mobility TCOs to be established: (1) transition metal dopants are required so that their donor d states hybridize minimally with the host cation s states of the CBM, avoiding problems inherent with conventional s level dopants; (2) the transition metal dopant atoms must possess d orbital energy levels such that the dopant is a singly charged donor to minimize mobility-reducing ionized impurity scattering; and (3) the donor level must be resonant within the conduction band to avoid a high effective mass, low mobility d state at or close to the CBM.

No barrier to ITO being replaced by cheaper, better IMO

IMO is an optically and electronically superior material to the commercially-dominant transparent electrode, ITO. This makes IMO not only more suited for the many diverse applications that ITO is currently used for, but also implies enormous potential for industrial cost savings as much thinner films of IMO can be produced with properties equal to or better than ITO of the same carrier concentration. We have combined theory and experiment to explore the reasons for the drastic differences between these two In_2O_3 -based TCOs. The rigid band model fails to describe the variation of optoelectronic properties of ITO with doping concentration. For heavy Sn-doping, the role of the Sn 5s states in perturbing the host In_2O_3 conduction band and increasing the band edge effective mass must be included to describe both the evolution of optical gap and mobility with doping. Having identified this shortcoming of ITO, we show that this is avoided by instead using Mo as the dopant. The different energetic position and atomic orbital character of Mo states compared with those of Sn means that negligible hybridization between Mo states and the CBM occurs. These findings provide a new



immediately viable and durable alternative to ITO, the industry standard TCO. While Mo and Sn are similarly priced, IMO films with half the thickness offer huge cost savings over ITO films of the same sheet resistance. Moreover, the understanding presented will enable the design of other TCO materials and dopants with improved transparent conducting properties.

Methods

Material fabrication

We prepared nominally undoped, Mo-doped and Sn-doped In_2O_3 films deposited on SiO_2 coated (50 nm sodium diffusion barrier) soda-lime glass (NSG) *via* AACVD using a cold-wall horizontal gas flow reactor. Precursors and solvents were procured from Aldrich and used as received. These consisted of $\text{InCl}_3\cdot\text{H}_2\text{O}$ (0.2 g, 4.4 mmol) dissolved in methanol (20 mL). $(\text{NH}_4)_6\text{Mo}_7\text{O}_{24}\cdot 4\text{H}_2\text{O}$ was incorporated with a range of 1–7 mol% for Mo-doped films and $\text{C}_4\text{H}_9\text{SnCl}_3$ with a range of 0.5–5 mol% for Sn-doped films. The precursor–solvent mixtures were ultrasonicated for 10 min to help precursors dissolve before the resulting homogeneous solutions were atomized to create an aerosol mist using a piezoelectric device. The N_2 carrier gas flow was held at 0.6 L min^{-1} and the substrate temperature was maintained at 450°C . All films were transparent, well adhered to the substrate and stable in air. Film durability was tested and compared to that of CVD ITO and commercial ITO coated glass (see Fig. S10, ESI†) which proved comparable. IMO film thicknesses ranged from 670–800 nm while ITO films ranged from 700–1600 nm.

Material characterisation

Film thickness was determined by cross sectional scanning electron microscopy (SEM) using a JEOL JSM-6301F field emission SEM at an accelerating voltage of 5 kV. Hall effect measurements (for the determination of resistivity ρ , charge carrier mobility μ and free carrier concentration n) were performed at room temperature with a Keithley 2182A nanovoltmeter and 6220 current source at a maximum field strength of 0.8 T in the van der Pauw geometry. Infrared (IR) reflectance measurements were performed using a Bruker Vertex 70v Fourier transform infrared spectrometer. All measurements were performed at 45° angle of incidence, utilising the Pike Veemax II accessory, and S-polarising filter. All FTIR measurements were performed with a near-IR light source, CaF_2 beam splitter and DLATGS detector. Transmission measurements were obtained with use of a Shimadzu UV-Vis-IR 3700 spectrophotometer with an integrating sphere detector. Hard X-ray photoelectron spectroscopy was performed at the I09 beamline at Diamond Light source. Measurements were performed at both 6.45 keV and 2.15 keV for different depth dependence. Photoelectrons were collected and analysed using a SCIENTA EW-4000 electron energy analyser. The sample was irradiated in grazing incidence geometry, that is an angle of $\sim 3^\circ$ between X-ray beam and sample surface. The energy calibration and resolution of the system were determined from a polycrystalline

Au foil. The energy resolution was determined by fitting a Gaussian–Fermi function convolution to the Fermi edge, and was found to be 300 meV. Inverse photoemission spectroscopy measurements were performed using a PSP Vacuum Technology BaO cathode dispenser electron source and an isochromat NaCl photon detector, both at 45° to the sample normal. Energy calibration was performed using the known energy position of the lowest occupied molecular orbital of multilayer C_{60} deposited *in situ* and the spectrometer resolution determined from a polycrystalline Au foil was 1.27 eV. The IMO and ITO samples were annealed to 300°C for 2 hours in preparation for IPES measurement.

Theoretical and modelling methods

Hybrid density functional theory (DFT) calculations were carried out on In_2O_3 using a plane-wave basis within the periodic code, VASP.^{28–31} We employ a screened non-local exchange–correlation density functional (HSE06).³² The projector augmented wave method (PAW)³³ was used to describe the core and valence electrons interaction. Full details of the calculations performed are provided in the ESI.† The band unfolding code BandUp was used to obtain a primitive cell representation of the band structure.^{34,35}

Sample plasma energies were extracted from IR reflectivity measurements utilizing a two-oscillator dielectric model³⁶ and transfer matrix method for optical simulation.³⁷ A four layer (vacuum/ In_2O_3 / SiO_2 /soda-lime glass) stratified medium was used in the model, with complete incoherence being assumed in the glass substrate and partial incoherence in the vacuum/ In_2O_3 interface. The absorption spectra were calculated from the transmission spectra of the samples using the Beer–Lambert relation. Optical gaps were extracted from the absorption spectra using a method proposed by Hamberg,³⁸ illustrated by Dolgonos *et al.*²³ which better accounts for degeneracy in materials compared to the more common Tauc analysis. A carrier statistics model was used in order to relate optical gap and plasma energy through the density-of-states average effective mass.

Author contributions

TDV and DOS devised the study. JENS, BADW and TDV wrote the manuscript with input from PAEM, MB and DOS. SS, CJC and IPP designed the sample growth that was performed by SS. JENS, AR, TJF, HJE, DAD and T-LL performed the HAXPES measurements which were analysed by JENS with input from TDV and VRD. JENS performed and analysed the IPES measurements with input from TDV and VRD. ZWL-H and LFJP performed and analysed the XAS measurements. MF and PW performed the SIMS measurements and analysed the data with JENS and TDV. NP performed the ion implantation of the SIMS standards. XRD was performed by TJF. SEM was performed by SS. The optical and transport measurements were performed by JENS, MB and SS, and analysed and modelled by JENS, with input from MB and TDV. BADW and DOS performed the first principles calculations and analysed the results.



The authors contributed to the scientific discussion and edited the manuscript.

Conflicts of interest

The authors declare that two authors (MF and PW) are affiliated to NSG Group which manufactures and sells TCO-coated glass.

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