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A practical computational protocol for photocatalytic reactions beyond ground-state approximations

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Theoretical studies of heterogeneous photocatalysts typically discuss the band level alignment obtained by ground-state DFT, which does not capture the physics of light-driven processes. Here, we present a new computational protocol in which excited states are explicitly considered in the Gibbs free energy diagrams. This is applied to prototypical H₂O oxidation and O₂ reduction reactions on a single-atom Co-embedded g-C₃N₄ cocatalyst.

Photocatalytic energy conversion with transition metal single-atom cocatalysts (TM-SACs) includes applications in photocatalytic H₂ evolution, CO₂ reduction, nitrogen fixation, and organic synthesis.¹ Recently, outstanding progress has been achieved in H₂O₂ production by O₂ reduction and H₂O oxidation.^{2–8} In this exploratory study, we use the Co/g-C₃N₄ TM-SAC as a prototypical system to evaluate possible pathways within the oxygen evolution reaction (OER) network:

- standard 4e[−] OER and 2e[−] H₂O₂ formation through the classical *O and nonclassical *(OH)₂ intermediates,
- oxygen reduction reaction (ORR) to H₂O₂ (2e[−]) and to H₂O (4e[−]).

Reaction intermediates and pathways are depicted in Fig. 1a. Atomically dispersed cobalt in graphitic carbon nitride (g-C₃N₄) was experimentally found to improve H₂O₂ formation from the H₂O rate constant,² reduce the activation barriers of water oxidation and oxygen reduction,³ and enhance H₂O₂ production from O₂, despite highly positive reaction steps calculated from ground-state DFT.⁴ According to previous theoretical investigations of Co/g-C₃N₄, we placed Co in the plane of the heptazine-based 2D carbon nitride network in an M–N₄ bonding environment.^{6,9}

Here, we present our novel computational protocol (Fig. 1b), which allows us to find the correct theoretical approach needed to capture, at the DFT level, the preference towards photocatalytic H₂O₂ production in Co/g-C₃N₄.^{2–4} In this work, we describe

purely photocatalytic processes at room temperature, *i.e.* without an applied external potential. In this description, we use Kohn–Sham (KS) DFT to obtain the Gibbs free energy $G_0 = E_{\text{tot}} + E_{\text{ZPE}} + H - TS = E_{\text{tot}} + G(T)$, where E_{tot} is the total energy of the optimized system, E_{ZPE} is the zero point energy, H is the enthalpic term, and TS is the entropic term. The reaction thermodynamic profile is expressed in Gibbs free energy difference (ΔG) from one step to the next. The overall ΔG values

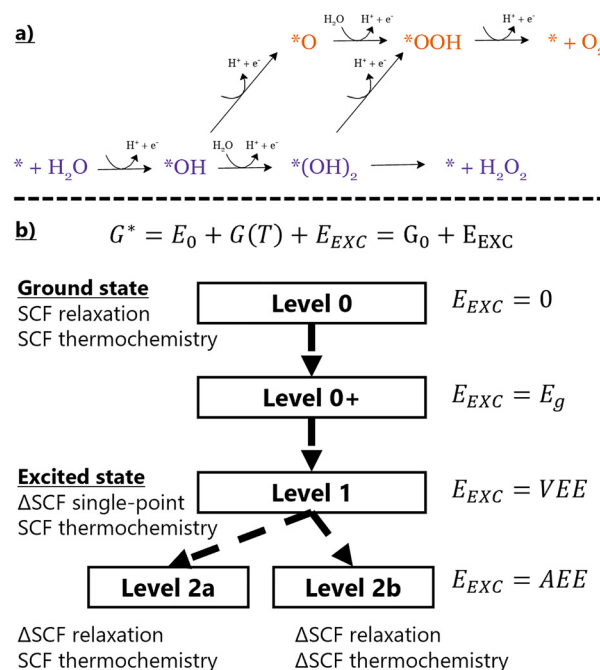


Fig. 1 (a) Schematic of the reaction pathway; orange and purple colors correspond to the 4e[−] O₂ evolution and the 2e[−] H₂O₂ evolution pathways, respectively. (b) Computational protocol hierarchy used to compute G^* – excited free energy profiles. At the topmost Level 0, the ground-state picture is presented ($E_{\text{EXC}} = 0$, $G^* = G$). Towards the bottom, increasingly robust and computationally intensive approximations are summarized with different quantities used as E_{EXC} : E_g (Kohn–Sham band gap), VEE (vertical excitation energy), and AEE (adiabatic excitation energy).

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are presented in Table S1, with each contribution listed separately in Table S2. The reaction mechanisms consist of proton-coupled electron transfer (PCET) steps with free energy described by the relation $G(\text{H}^+) + G(\text{e}^-) = \frac{1}{2}G(\text{H}_2)$. The reaction thermodynamics are evaluated in both ground and excited states. Since the scope of this study is to assess the catalytic activity of the chosen reaction using the proposed computational protocol, a few assumptions have been considered: (1) light absorption has the correct wavelength to excite the substrate to the conduction band; (2) the generated hole–electron pair is transferred at the interface; (3) the charges are fully separated and reach the catalytic center without recombination (verified by examining the charge density difference between the excited and ground states, see Fig. S3).

The standard ΔG profiles are expanded by explicitly considering the excited-state contributions in the Gibbs free energy calculations. In the proposed protocol, we consider an additional term E_{EXC} , in order to obtain the total expression for intermediate free energy $G^* = G_0 + E_{\text{EXC}}$ (here the ‘*’ denotes the excited state treatment and index ‘0’ denotes the ground state). The treatment of E_{EXC} considers different approximations for introducing the excited state contributions. In the ground state, E_{EXC} simply equals 0. We call this the ‘Level 0’ description. At Level 0+, ground-state calculations are still applied, but $E_{\text{EXC}} = E_{\text{CBM}} - E_{\text{VBM}} = E_{\text{g}}$, the Kohn–Sham eigenvalue band gap of the system. This represents a crude approximation for the energy increase when the material is illuminated by light. At Level 1, the vertical excitation energy $E_{\text{EXC}} = \text{VEE}$ is considered, calculated using the ΔSCF method.¹⁰ This is obtained by comparing the total energies of excited and ground-state systems without relaxing the atomic geometry of the excited state. Finally, at Level 2, we allow excited systems to relax to their adiabatic excitation energy $E_{\text{EXC}} = \text{AEE}$. The ΔSCF procedure used at the two topmost levels involves fixing band occupations at a desired configuration (‘non-Aufbau’), instead of filling them from the lowest to the highest energy bands (the ‘Aufbau’ principle). The density optimization algorithm is chosen so that it is possible to proceed without diagonalizing the Kohn–Sham matrix, which would inherently reorder the orbitals by increasing single-particle energy. This ensures converging to the desired excited state, instead of the ground state (for exact details, see the SI). Here, the selected configuration involves depopulating the one-electron valence band maximum (VBM) and filling the conduction band minimum (CBM) of the $\text{g-C}_3\text{N}_4$ support material.

Each of these modifications to the Gibbs free energy state function G describes slightly different physics, which we will outline in more detail. At the Level 0 approximation, $E_{\text{EXC}} = 0$ and $G^* = G$. The free energy profiles are equivalent to purely thermal reactions.

At Level 0+, $E_{\text{EXC}} = E_{\text{g}}$, where E_{g} is the Kohn–Sham band gap of the semiconductor catalyst support. This is a ground-state property accessible through the standard self-consistent field (SCF) iterative procedure and does not involve true excitations of any form. The E_{g} value can be used as an estimate of the absorption edge and to screen potential semiconductor

surfaces for use in photocatalysis. We include it in our analysis to determine the extent of agreement between this and higher-order approximations. For the purposes of this study, we do not consider any bands of Co-d character that appear within the band gap of $\text{g-C}_3\text{N}_4$ (midgap states). This omission stems from the fact that in TM-SAC photocatalysts, the principal semiconductor band gap excitation is the major contributor.¹ Metal sites add the possibility of some visible light absorption, but excitations of their localized and short-lived states do not offer useful pathways for efficient electron transfer. This is particularly the case at low loading densities typical of TM-SACs, where the photocatalytic activity is already maximized and further loading (which increases aggregation, metal use, and cost) does not improve the efficiency of the catalyst.¹¹

Level 1, the next step of our protocol, considers $E_{\text{EXC}} = \text{VEE}$, describing an electronic transition that obeys the Franck–Condon rule. In our workflow, charge transfer to the metal site is assumed to be an ultrafast process (≤ 1 ps for $\text{g-C}_3\text{N}_4$ SACs),^{12,13} outpacing competing recombination channels. Additionally, it is assumed that the chemical reaction step occurs within this timeframe without geometric relaxation. At this level, the transfer step is described as concerted PCET, in which charge transfer and nuclear rearrangement occur together. The subsequent intermediates relax only to their ground states between the excitations. ΔSCF calculations are performed to obtain VEE values. Without moving from the ground-state optimized geometry, an electron is promoted from the Kohn–Sham VBM of $\text{g-C}_3\text{N}_4$ to its CBM. We keep metal midgap states, if any, with their original occupations. The orbitals are allowed to relax self-consistently, with the constrained distribution of electrons across orbitals maintained throughout the procedure. After the calculation with ΔSCF occupations is finished, we compare the calculated total energies to obtain $\text{VEE} = E_{\Delta\text{SCF}}^* - E_0$, where E_0 is the total ground-state energy and $E_{\Delta\text{SCF}}^*$ is the vertical (*i.e.*, without atomic relaxation) excited state energy. VEE is expected to be lower than the band gap E_{g} , because it corresponds to the optical band gap. The electron and the hole interact through the self-consistent field, reducing the excitation energy relative to the single-particle gap, lowering VEE with respect to the band gap.

At the final step of our protocol, Level 2, $\text{AEE} = E_{\Delta\text{SCF-rel}}^* - E_0$, where $E_{\Delta\text{SCF-rel}}^*$ (rel refers to atomic relaxation) is the excited-state energy with the atomic positions relaxed with non-Aufbau occupations. The underlying physics describes the process of step-wise PCET. The intermediate first relaxes on the photo-excited energy surface before the proton transfer occurs. We expect AEE to always be lower than both E_{g} and VEE. We note the possibility of considering the excited state thermochemistry (Level 2b) for reactions with a reduced reaction kinetics *vs.* relaxation of the excitation. This is, however, beyond the scope of the current work in which we consider a non-equilibrium process^{14,15} with ground-state thermochemistry (Level 2a).

Among many approaches used to model photochemical processes, ΔSCF stands out as a promising method for screening-level frameworks capable of high-throughput analysis of heterogeneous photocatalysts. This simple approach, the



effectiveness of which we demonstrate here, should in the future supplement the existing *ab initio* molecular dynamics methods, as documented *e.g.* in recent studies by Carter *et al.*^{16,17} The current approach draws from the existing techniques and goes beyond their typical range of applicability.

To validate our computational protocol, we consider a four-electron OER reaction, going through classical intermediates $* + \text{H}_2\text{O} \rightarrow *\text{OH} \rightarrow *\text{O} \rightarrow *\text{OOH} \rightarrow *\text{OO} \rightarrow * + \text{O}_2$ ($4e^-$) and a two-electron H_2O_2 evolution $* + \text{H}_2\text{O} \rightarrow *\text{OH} \rightarrow *(\text{OH})_2 \rightarrow * + \text{H}_2\text{O}_2$ ($2e^-$), which follows the same initial steps but branches after $*\text{OH}$. We allow both $2e^-$ and $4e^-$ oxidation reactions to proceed through the nonclassical $*(\text{OH})_2$ intermediate.¹⁸ In most of our calculated profiles, O_2 evolution proceeds through the path of $*(\text{OH})_2$, as the classical $*\text{O}$ has a higher ΔG value. We also include the $*\text{OO}$ intermediate with the purpose of a more direct comparison of steps that involve the desorption of the final products, $*(\text{OH})_2 \rightarrow * + \text{H}_2\text{O}_2$, and $*\text{OO} \rightarrow * + \text{O}_2$, separating them from the proton-electron transfer steps.

We first turn our attention to the values computed at different approximations for E_{EXC} by two electron density functionals: a commonly used semilocal PBE+D3(BJ) functional (hereafter PBE) and a hybrid HSE06+D3(BJ) (hereafter HSE), in which vdW D3 dispersion corrections are considered. The PBE results are found to be volatile and without a clear trend that can be easily interpreted (see Fig. S1). Thus, we will focus on the results for the HSE functional, plotted in Fig. 2. In our spin-polarized calculations, we considered two possible excitations for each intermediate, spin-up and spin-down, and selected the one that produced the lowest E_{EXC} . In the initial calculation without adsorbates, Co has a +3 oxidation state, evidenced by the total magnetic moment of $2.2\mu_{\text{B}}$ for PBE and $2.5\mu_{\text{B}}$ for HSE, depicting the Co^{3+} triplet state, obtained in an unrestricted calculation.

Out of the three quantities considered as E_{EXC} , E_{g} is always the highest, followed by VEE, and finally AEE. The difference between these parameters in subsequent steps is what determines the differences between the calculated ΔG profiles. The VEE to AEE difference for the $*\text{OH}$, $*\text{O}$, $*(\text{OH})_2$, and $*\text{OOH}$ intermediates ranges from low to moderate (0.02–0.10 eV). However, the lowering of AEE with respect to VEE differs substantially for $*$ (bare catalytic site) (1.15 eV) and $*\text{OO}$ (0.38 eV). The first leads to a systematic upward shift of the ΔG profile starting from $*\text{OH}$. The second manifests itself with the lowest

desorption energy of O_2 found at the HSE-L2a level of just 0.81 eV. On the other hand, the difference between E_{g} and VEE is less systematic and significant at every step. The biggest changes occur at the second electron transfer steps, $*\text{O}$ and $*(\text{OH})_2$.

Gibbs free energy profiles in the ground state and at higher levels of our protocol are plotted in Fig. S2. We note that the values of absolute Gibbs free energies, especially for gaseous intermediates, depend on the accuracy of the density functional. However, the ΔG profiles considered here rely on relative differences between reaction steps, with the functional-specific errors not influencing the qualitative outcome. Additionally, our calculations of gaseous species are in good agreement with experiments, as shown in Table S3. At Level 0, the $2e^-$ reaction proceeds with $*(\text{OH})_2$ coupling and desorption as the potential-determining step (PDS) of H_2O_2 production. The $4e^-$ reaction also proceeds through $*(\text{OH})_2$, as $*\text{O}$ is higher in energy by 0.95 eV. In the $4e^-$ process, the coupling to $*\text{OOH}$ has the highest PDS energetic cost of 1.97 eV, which is significantly lower than the 2.56 eV for H_2O_2 production. The ground-state calculation thus predicts O_2 to be the majority product over H_2O_2 . In the excited state, the potential determining step remains the one involving O–O coupling but depending on the protocol level, its relative intensity changes and influences the predicted major product. Thus, at Level 0+ and 1, $*(\text{OH})_2$ is more stabilized, and $*\text{OOH}$ remains at a similar position in the ΔG diagram. This increases both PDSs and preserves the original preference towards O_2 . What changes at Level 2a is a less stable ΔG value of $*\text{OH}$ and $*(\text{OH})_2$, leading to a lower potential difference for $\text{HO}^*-\text{*OH}$ coupling and desorption. At the same time, $*\text{OOH}$ is less stable than at lower levels, leading to a lower PDS for the $2e^-$ path towards H_2O_2 over the $4e^-$ path to O_2 .

The trends for O_2 vs. H_2O_2 preference are visualized in Fig. 3, including both functionals, and both OER and ORR processes. With the PBE functional, a balance between the formation of the two products is maintained as the points lie close to the $X = Y$ line, indicating equal O_2 and H_2O_2 formation probabilities. Level 2a with PBE (PBE-L2a) is an exception, showing the strongest preference towards H_2O_2 , both in $2e^-$ water oxidation (Fig. 3a) and in $2e^-$ O_2 reduction (Fig. 3b) processes. We quantify the magnitude of this preference by introducing the parameter $\Delta\Delta G_{\text{OER}} = \Delta G_{\text{PDS}-\text{O}_2} - \Delta G_{\text{PDS}-\text{H}_2\text{O}_2} = 0.98$ eV. In the ORR, the thermodynamic feasibility of H_2O_2 production is expressed by $G(* + \text{H}_2\text{O}_2) - G(*\text{OOH})$; if this value is negative, H_2O_2 is the major product. From Level 0 to Level 1, HSE simulations show a strong preference towards $4e^-$ $\text{O}_2/\text{H}_2\text{O}$ production. At the most precise protocol level, HSE-L2a, both oxidation and reduction paths can be seen as viable to obtain H_2O_2 ($\Delta\Delta G = 0.35$ eV, $G(* + \text{H}_2\text{O}_2) - G(*\text{OOH}) = -0.35$ eV), in agreement with existing experimental evidence.^{2–4} It is worth noting that the non-classical $*(\text{OH})_2$ intermediate makes a critical difference in the predicted products. If not present, the OER path could only go through the classical $*\text{O}$ intermediate, and H_2O_2 would have only been preferred at the PBE-L2a level (very weakly, $\Delta\Delta G = 0.09$ eV). However, since the $*(\text{OH})_2$ reaction path is enabled, H_2O_2 is preferred when PBE-L0 (very weakly, $\Delta\Delta G = 0.07$ eV), PBE-L2a ($\Delta\Delta G = 0.98$ eV), or HSE-L2a ($\Delta\Delta G = 0.35$ eV) are used. While PBE-L0

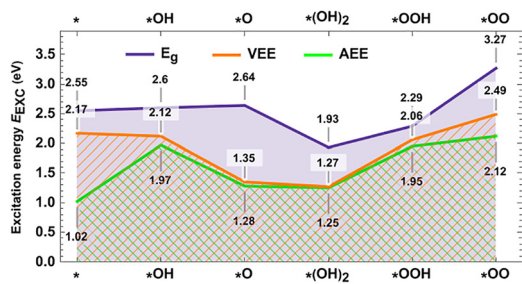


Fig. 2 E_{EXC} values computed using HSE06+D3(BJ) in different reaction steps: Kohn–Sham band gap (E_{g}), vertical excitation energy (VEE), and adiabatic excitation energy (AEE).



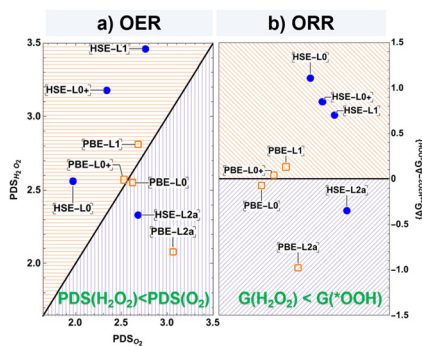


Fig. 3 Preference towards different OER and ORR products at different framework levels with the PBE+D3(BJ) and HSE06+D3(BJ) functionals. (a) In the analysis of H_2O oxidation to $\text{O}_2/\text{H}_2\text{O}_2$, the X and Y axes correspond to the potential determining steps of O_2 and H_2O_2 evolution reactions. $X = Y$ is the line of equal ΔG for potential determining steps. Simulations in which H_2O_2 is preferred are below the line, and O_2 is preferred above the line. (b) For O_2 reduction, Y axis is the Gibbs free energy of the H_2O_2 product versus $^*\text{OOH}$ intermediate. Below $Y = 0$, H_2O_2 formation is thermodynamically stable (“downhill”) from $^*\text{OOH}$ and above, only H_2O is thermodynamically favorable. Orange and purple colors correspond to the $4e^- \text{O}_2$ evolution/ $4e^- \text{O}_2$ reduction and the $2e^- \text{H}_2\text{O}_2$ evolution/ $2e^- \text{O}_2$ reduction pathways, respectively.

is qualitatively correct when taken at face value, we attribute the result to fortuitous compensation of systematic errors in the semilocal GGA-type (including PBE) density functionals.¹⁹ This may also be the case in the comparison of HSE-L2a versus PBE-L2a, which gives the same qualitative conclusions in terms of ΔG and $\Delta\Delta G$ values.

The protocol levels with intermediate accuracy at Levels 0+ and 1 are in agreement in predicting the opposite result. Finally, Level 2a, with both PBE and HSE functionals, gives the correct majority product. The ORR pathways, on the other hand, are not affected by this intermediate, as H_2O_2 production from O_2 does not proceed beyond the $2e^-$ process. The same three functional-protocol level combinations predict H_2O_2 as a thermodynamically allowed ORR product. More specifically, it is determined by the negative ΔG value for the step $^*\text{OOH} + \text{H}^+ + e^- \rightarrow ^* + \text{H}_2\text{O}_2$ (“downhill” process, purple area of Fig. 3b), in contrast to the positive value that predicts a positive reaction (“uphill”, orange area of Fig. 3b), with only H_2O as a thermodynamically allowed product at lower protocol levels.

In summary, we demonstrated a possible application of a new practical protocol based on computational techniques that are easily transferrable between ground- and excited-state descriptions, while sacrificing little of the efficiency. We showed that, in the case of the OER and ORR on $\text{Co/g-C}_3\text{N}_4$, the ΔSCF approach used to relax the excited state (Level 2a) gave predictions of reaction thermodynamics exactly in line with the knowledge from previous experimental studies, with H_2O_2 preference in both reaction paths.

We presented herein a novel, detailed computational protocol to obtain robust free energy profiles of photocatalytic reactions explicitly considering excited state contributions. By building on the ground-state DFT methodology, the ΔSCF treatment of excited-state band occupations allows access to

standard methodology and post-processing techniques normally applied to ground-state DFT results.

At this point, we conclude that for the OER and the ORR on $\text{Co/g-C}_3\text{N}_4$, the use of a hybrid functional and at least the ΔSCF treatment of the excited states with atomic relaxation is essential to predict the correct products. ΔSCF without relaxation may be insufficient, just as any approximation based on Kohn–Sham eigenvalues. In due course, the protocol should be further validated with calculations for other catalysts and reactions. The models applied here in the minimal demonstration can be expanded to describe interactions with the environment, predict reaction kinetics (in addition to thermodynamics), extend their applicability to other types of reactions (such as photo-electrocatalysis), and, in general, better reproduce experimental conditions.

Conflicts of interest

There are no conflicts to declare.

Data availability

The data supporting this article have been included as part of the supplementary information (SI). Supplementary information is available. See DOI: <https://doi.org/10.1039/d5cc06211j>.

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